



Diagnostics Tools for Laser-Driven Plasma-Accelerators

Malte C. Kaluza

*Institute of Optics and Quantum Electronics
Friedrich-Schiller-Universität Jena, Germany*



Outline

- Motivation: Why plasma diagnostics necessary
- Pump-probe scenarios:
Which different types of probe pulses can be applied?
- Electro-magnetic probe pulses:
 - Shadowgraphy
 - Interferometry
 - E- and B-field sensitive techniques
- Particle probe pulses:
 - Proton probing
 - Detection of magnetic and electric field distributions



Motivation

- Laser-produced plasmas:
 - formation and modulation occurring on time scales of driving laser
 - density distribution?
 - temperature?
 - internal fields?
- High relevance for particle accelerators
 - plasma-wakefield accelerators: detect details of plasma wave
 - plasma ion accelerators: e.g. sheath field of accelerating fields from solid targets
- Pump-probe geometry well suited: probe interaction driven („pumped“) by main pulse



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Electromagnetic Probe Pulses

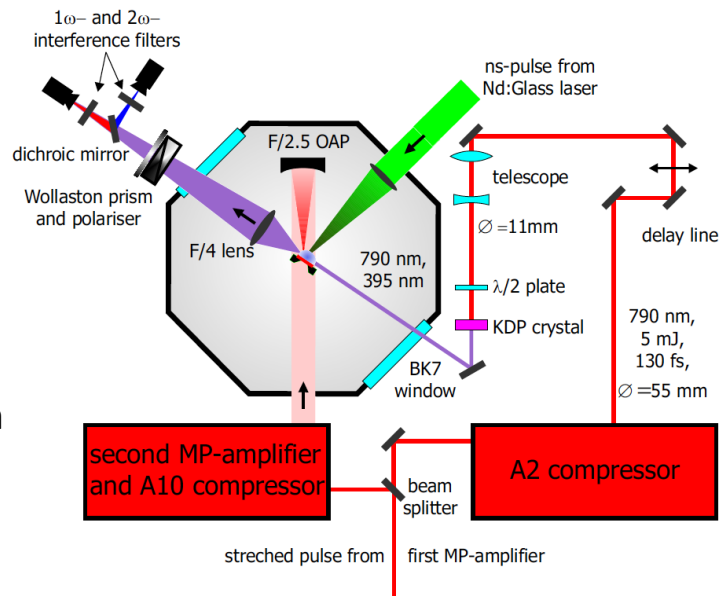
- Generation of synchronized optical probe pulses:

- split off part of the main pulse
- guide it towards interaction along different path
- adjust temporal delay

➔ perfect synchronization

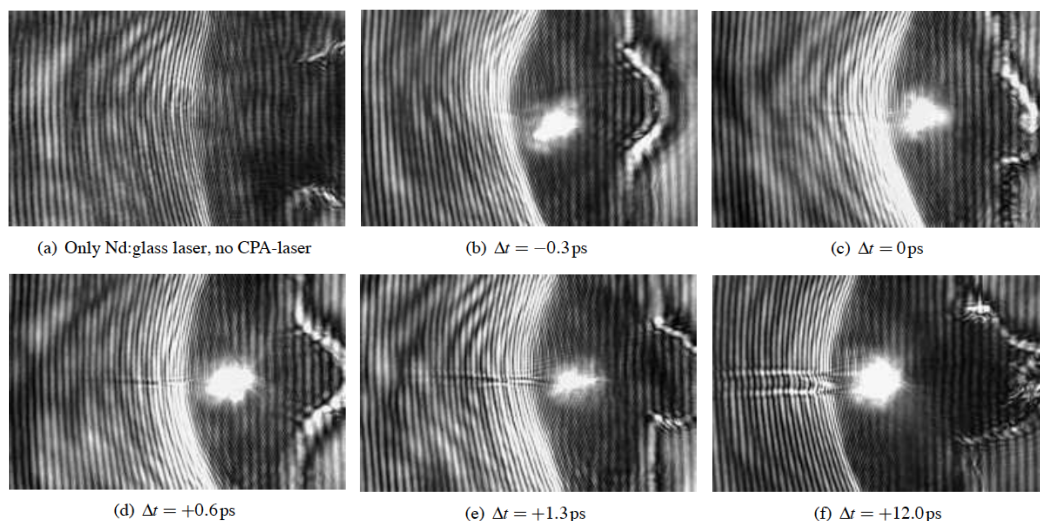
➔ probe pulse duration similar to main pulse

➔ record movie from subsequent shots at different delays



Electromagnetic Probe Pulses

- Delay scan of interaction of 10-TW laser pulse with preformed plasma at different shots:

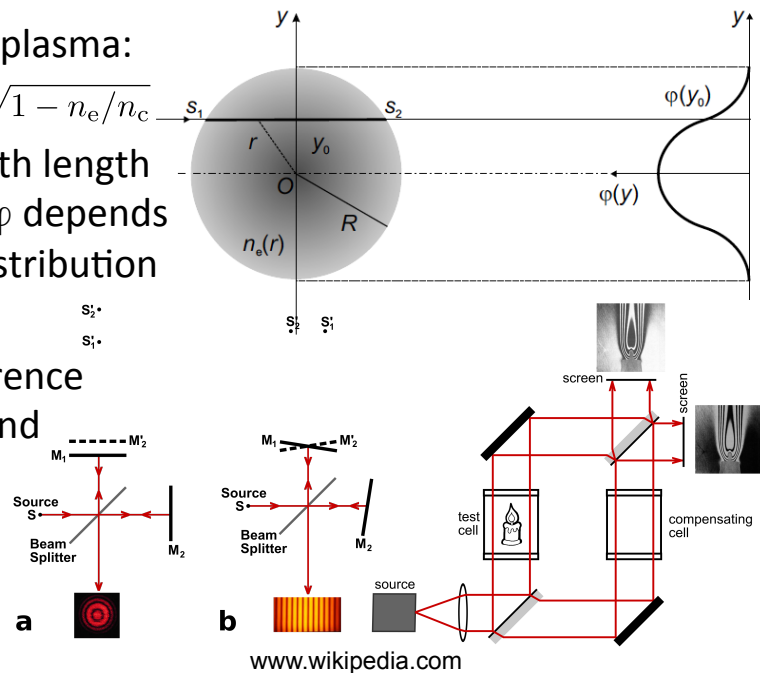


- How can we deduce the plasma density from these images?
- Use interferometry!

Interferometry

- Refractive index of a plasma:

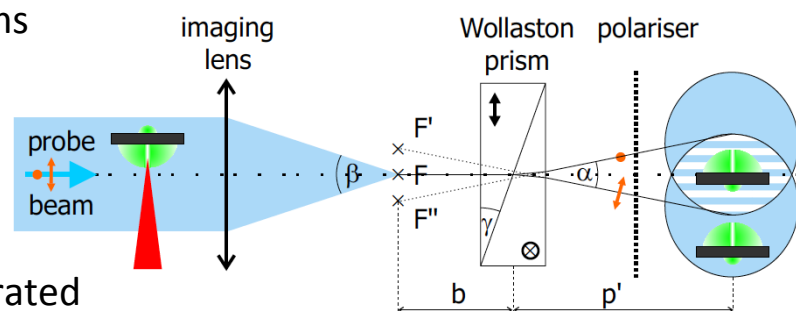
$$\eta = \sqrt{1 - (\omega_p/\omega_L)^2} = \sqrt{1 - n_e/n_c}$$
- Integrated optical path length or integrated phase φ depends on plasma density distribution seen by light rays:
- Visualize phase difference between probe ray and ray going through vacuum:
interferometer



- Challenge for short pulses: rays' path lengths need to be identical within pulse length (few μm)! easier: Wollaston prism

Interferometry

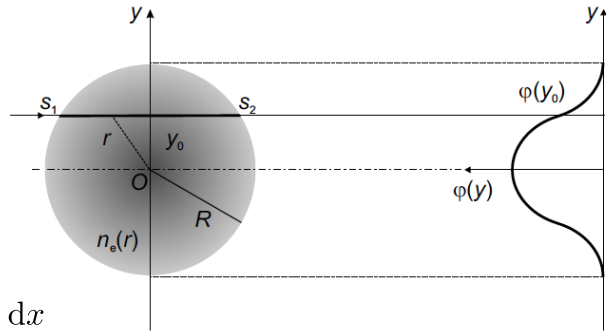
- Wollaston prism = polarizing beam splitter, combination of two birefringent prisms
- Probe pulse: polarization under 45° w.r.t. both optical axes
- Two replica separated by α , polarized perpendicularly to each other
- Imaging system: generation of two images shifted transversely
- Polarizer under 45° : interference between two replica possible, „mixing“ of beam parts going through interaction region and through vacuum
- Separation distance i of fringes on CCD:



$$i = \frac{\lambda_{\text{probe}}}{\alpha} \frac{p'}{b}$$

Interferometry

- Deduce plasma density distribution by assuming cylindrical symmetry:
- Phase shift difference between ray going through the plasma and through vacuum:



$$\Delta\varphi(y_0) = \Phi(y_0) = \frac{2\pi}{\lambda_L} \int_{x_1}^{x_2} [1 - \eta(x)] dx$$

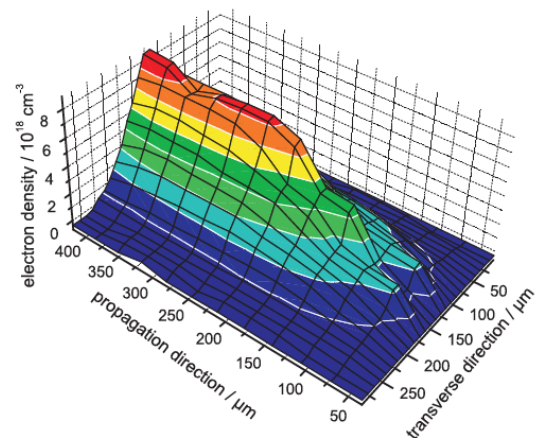
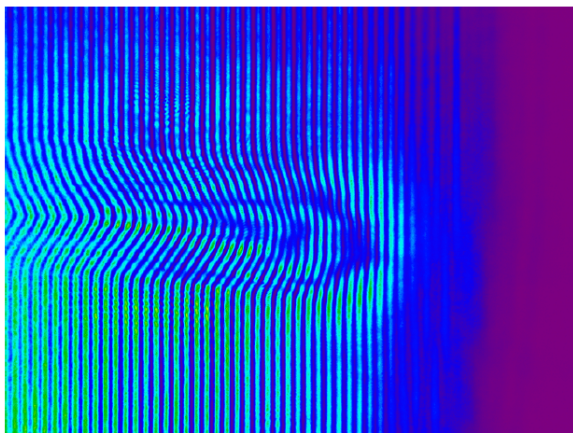
$$\approx \frac{\pi}{n_{cr}\lambda_L} \int_{x_1}^{x_2} n_e(x) dx = \frac{2\pi}{n_{cr}\lambda_L} \int_{y_0}^R \frac{n_e(r)r}{\sqrt{r^2 - y_0^2}} dr$$

- Deduce plasma density via Abel inversion:

$$n_e(r) = -\frac{n_{cr}\lambda_L}{\pi^2} \int_r^R \frac{d\Phi(y)}{dy} \cdot \frac{dy}{\sqrt{y^2 - r^2}}.$$

Interferometry

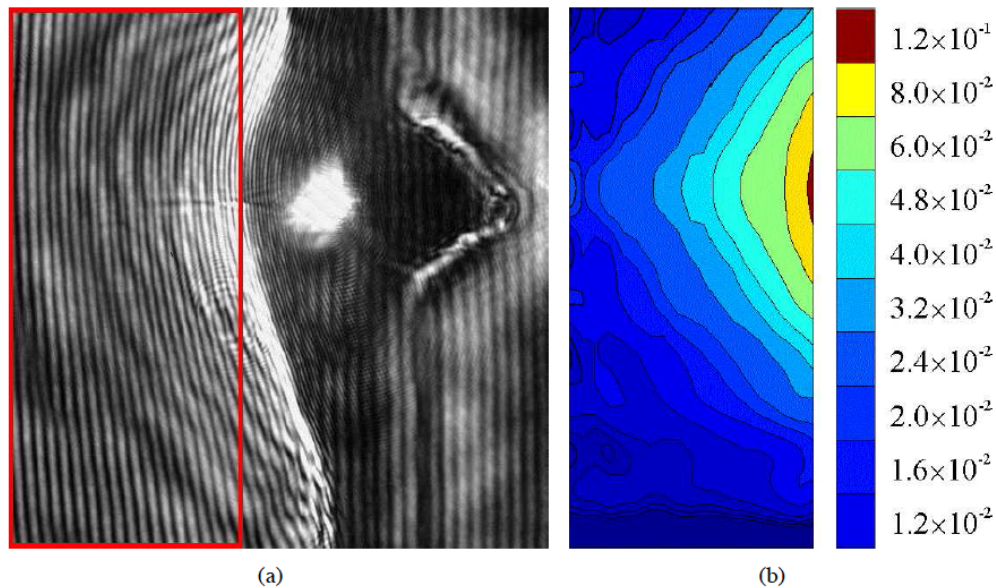
- Deduce plasma density distribution by assuming cylindrical symmetry:



H.-P. Schlenvoigt, PhD
thesis, Uni Jena (2009)

Interferometry

- Deduce plasma density distribution by assuming cylindrical symmetry:

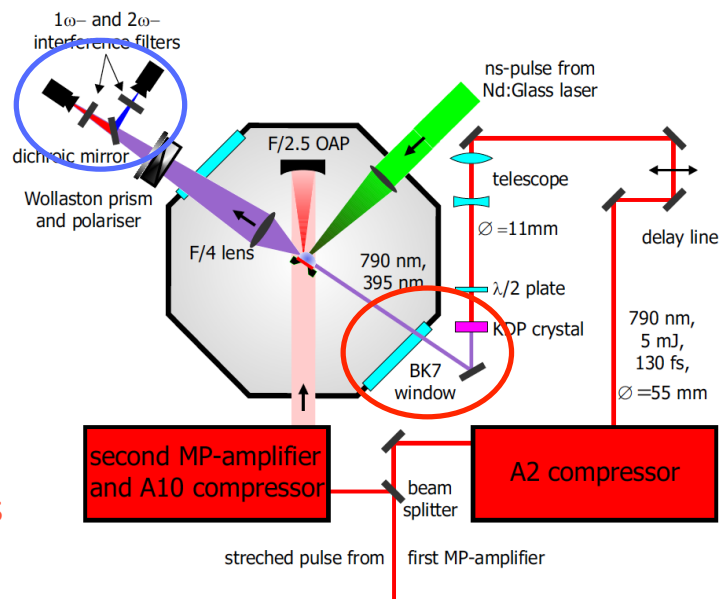


- Density given in units of n_{cr}

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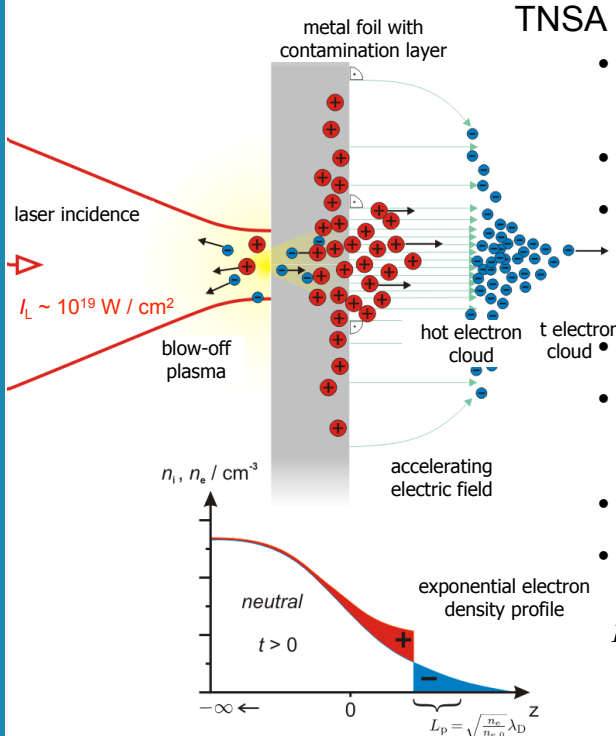
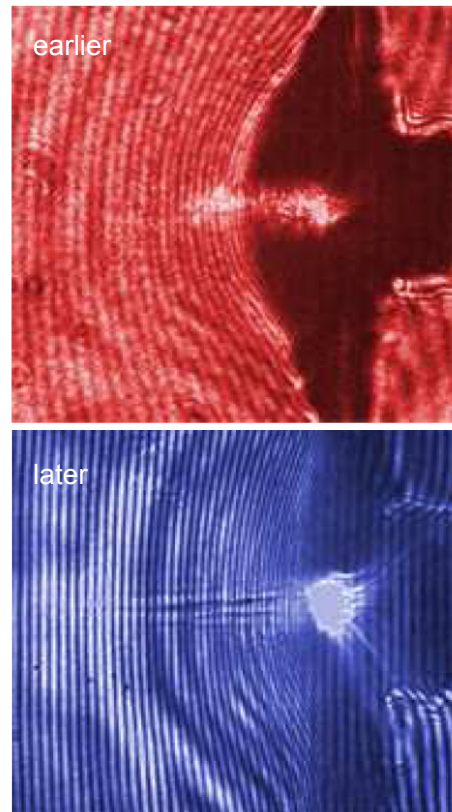
Electromagnetic Probe Pulses

- 2-color probe pulses: visualize different time steps of evolution during a single shot by taking 2 images at different times
- 2 pulses (1ω and 2ω) go through window at different speed (GVD) => separation by few ps
- Separate pulses after interaction: get 2 images of the same interaction at 2 different times



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- 2-color probe pulses:
visualize different time steps of evolution during a single shot by taking 2 images at different times
- 2 pulses (1ω and 2ω) go through window at different speed (GVD)
=> **separation by few ps**
- **Separate pulses after interaction:**
get 2 images of the same interaction at 2 different times



TNSA (Target Normal Sheath Acceleration)

- laser pulse generates relativistic electrons,
- they propagate through the foil and
- form an electric sheath field

$$\sim \text{TV/m} \quad \mathcal{E}_{\text{front}}(t) \approx 2 \sqrt{\frac{k_B T_e n_e}{\epsilon_0 (2eN + \omega_{pi}^2 t^2)}}$$

- charge distribution starts to expand,

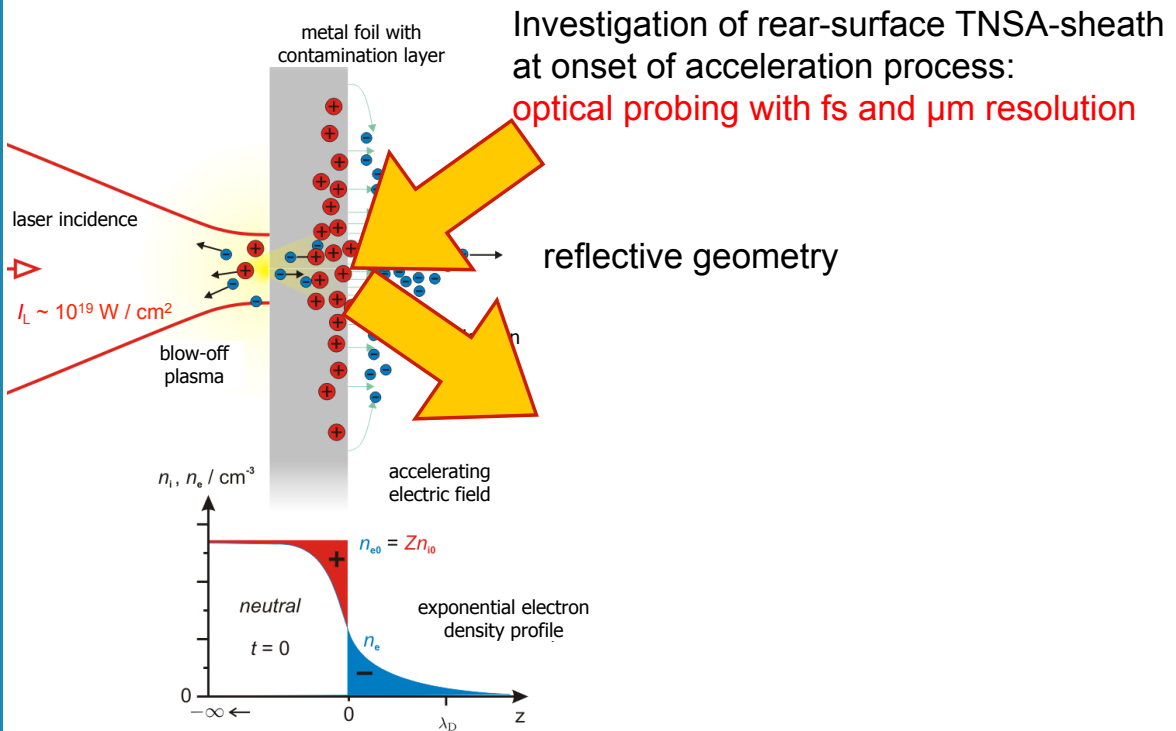
- acceleration length $\sim \mu\text{m}$
 $\sim \text{Debye-length} \quad \lambda_D = \sqrt{\frac{\epsilon_0 k_B T_e}{n_e e^2}}$
- lifetime of electric field $\sim f(\tau_L)$

- max. ion energies

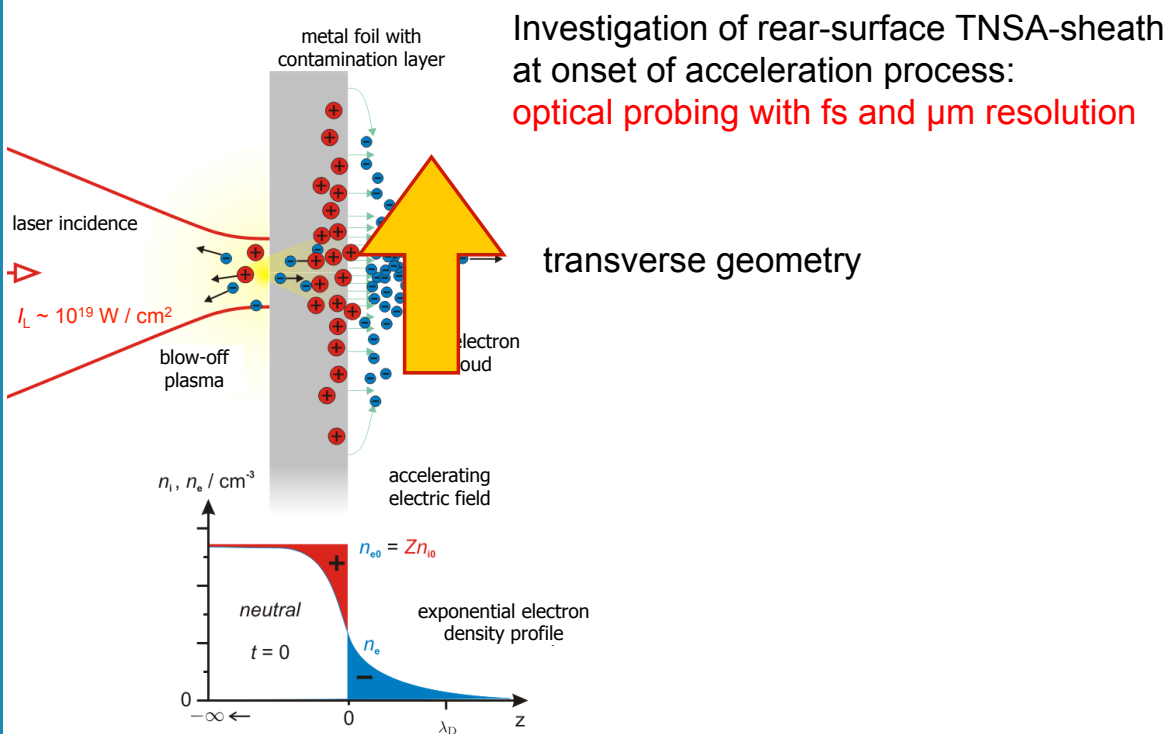
$$E_{\text{max}} = 2Zk_B T_e \left[\ln \left(\frac{\omega_{pi} t}{\sqrt{2} e N} + \sqrt{\left(\frac{\omega_{pi} t}{\sqrt{2} e N} \right)^2 + 1} \right) \right]^2$$

P. Mora, PRL **90**, 185002 (2003)

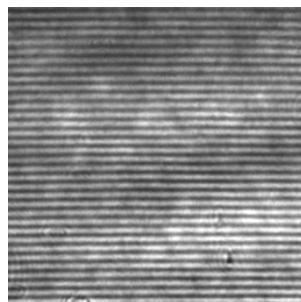
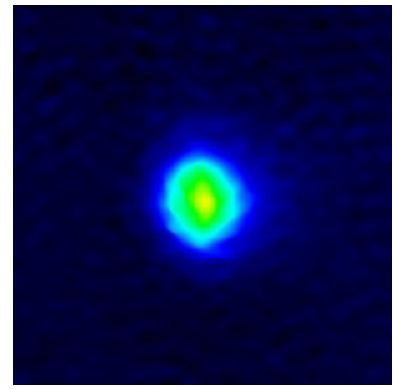
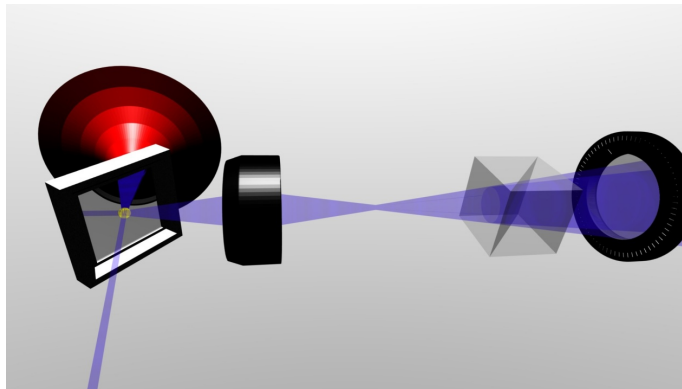
Electromagnetic Probe Pulses



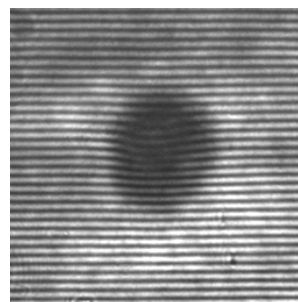
Electromagnetic Probe Pulses



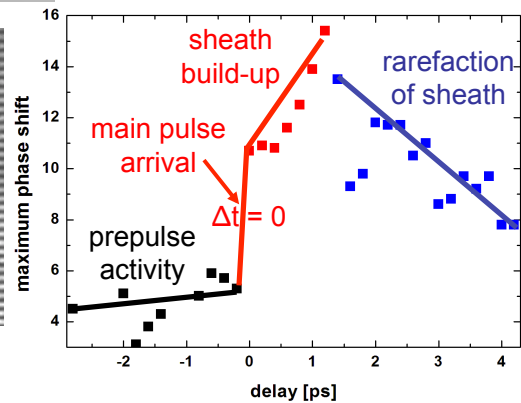
Electromagnetic Probe Pulses



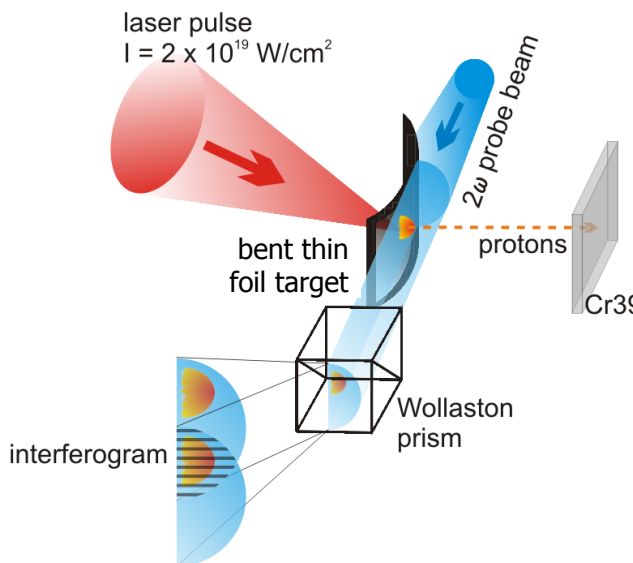
without main pulse



with main pulse



Electromagnetic Probe Pulses



phase shift (measured tangentially) $\Rightarrow$ 2D signal

$$\Delta\phi = \frac{\omega}{c} \int (\eta - 1) ds = \frac{\omega}{c} \int \left(\sqrt{1 - \frac{n_e}{n_c}} - 1 \right) ds$$

$$\approx \frac{\omega}{2cn_c} \int n_e ds$$

Abel inversion

$$h(y) = 2 \int_y^R f(y) \frac{r}{\sqrt{r^2 - y^2}} dr$$

3D electron density distribution (cylindrical symmetry)

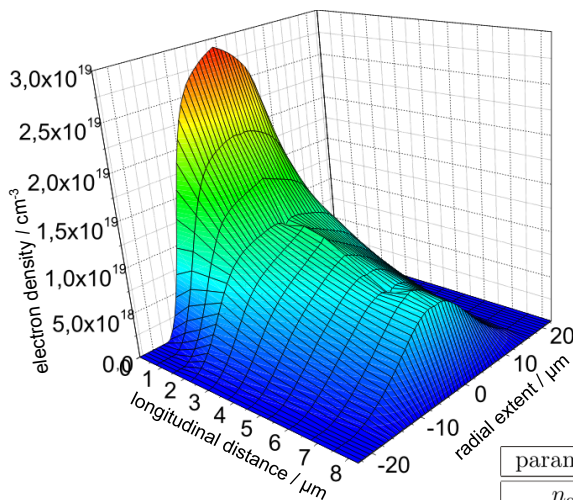
$$n_e(r, z, t) \sim \exp \left[-\frac{r(t)^2}{w_0^2} \right] \exp \left[-\frac{z(t)}{\lambda_D} \right]$$

Nomarski interferometer:
f/2 imaging onto 12-bit CCD
Wollaston prism + polarizer

- spatial resolution $\sim 1.1 \mu\text{m}$
 - temporal resolution $\sim 100 \text{ fs}$
- $\Rightarrow$ match dimensions of accel. process!

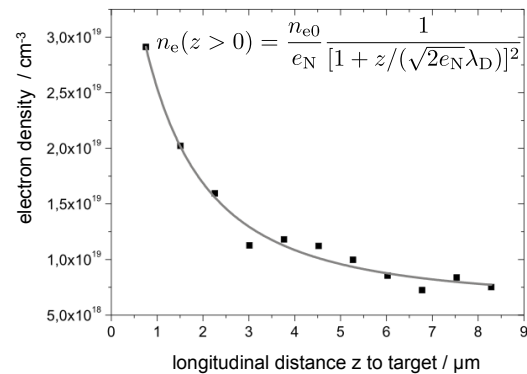


1st all-optical measurement of n_e -distribution driving laser ion acceleration!



at $t = 0$
(onset of acceleration process)

J. Crow *et al.*, J. Plasma Phys. (1975)

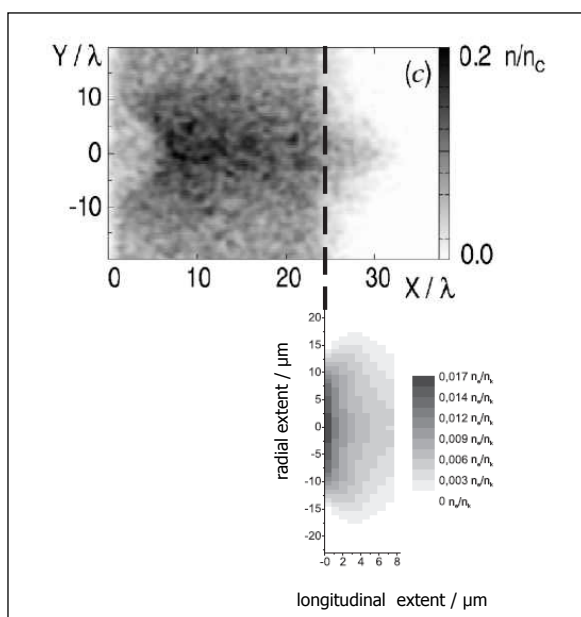


parameter	experimental data	theoretical prediction
n_{e0}	$(8.4 \pm 0.4) \times 10^{19} \text{ cm}^{-3}$	$9.44 \times 10^{19} \text{ cm}^{-3}$
λ_D	$(1.0 \pm 0.2) \mu\text{m}$	$0.64 \mu\text{m}$
w_{back}	$(21 \pm 1) \mu\text{m}$	$8.1 \mu\text{m}$
$k_B T_e$	$(1.5 \pm 0.4) \text{ MeV}$	0.71 MeV
E_{TNSA}	$(1.3 \pm 0.4) \text{ TV/m}$	1.1 TV/m

O. Jäckel, MCK *et al.*, New Journal of Physics **12**, 103027 (2010)



Comparison with numerical simulations

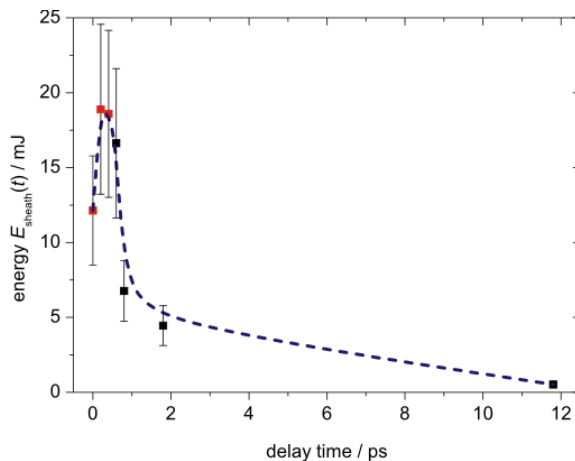


3D-PIC results by A. Pukhov for comparable laser conditions

- ⇒ comparable shape
- ⇒ deviation of absolute numbers (measured density smaller by a factor of 5)

A. Pukhov, PRL **86**, 16 (2001)

Energy content of electron sheath: $E_{e-} = k_B T_e N_e$



Conversion efficiency
 $E_{\text{laser}} \Rightarrow$ hot electrons:

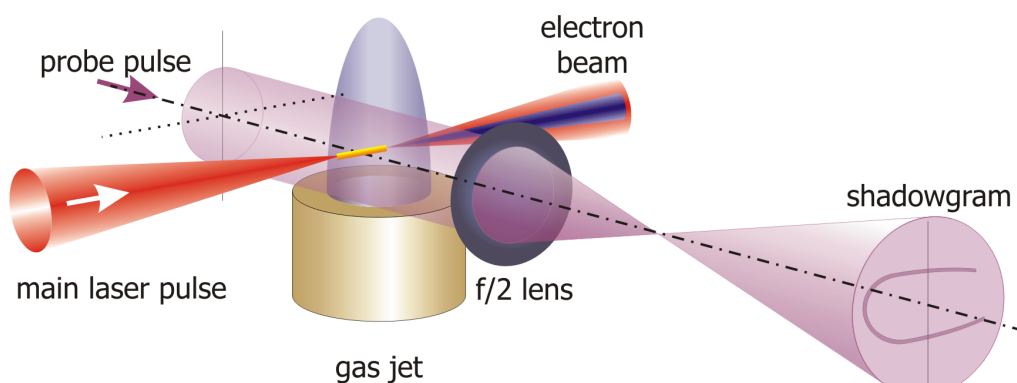
$$\eta = \frac{E_{e-}}{E_{L,\text{eff}}} = \frac{k_B T_e N_e}{E_{L,\text{eff}}}$$

$$\eta_{\text{sheath}} = (3.7 \pm 1.2)\%$$

$$\eta_{\text{total}} = (9 \pm 3)\%$$

(deduced from sheath's electron density and radial extent, assuming similar hot-e-density inside the target)

O. Jäckel, MCK *et al.*, New Journal of Physics **12**, 103027 (2010)



JETI parameters:

$$E_{\text{laser}} = 800 \text{ mJ}, \tau_{\text{laser}} = 85 \text{ fs},$$

$$f/6 \text{ OAP}, I_{\text{laser}} \approx 3 \times 10^{18} \text{ W/cm}^2$$

probe pulse:

$$\tau_{\text{probe}} \approx 100 \text{ fs @ } 1\omega$$

LWS-20 parameters:

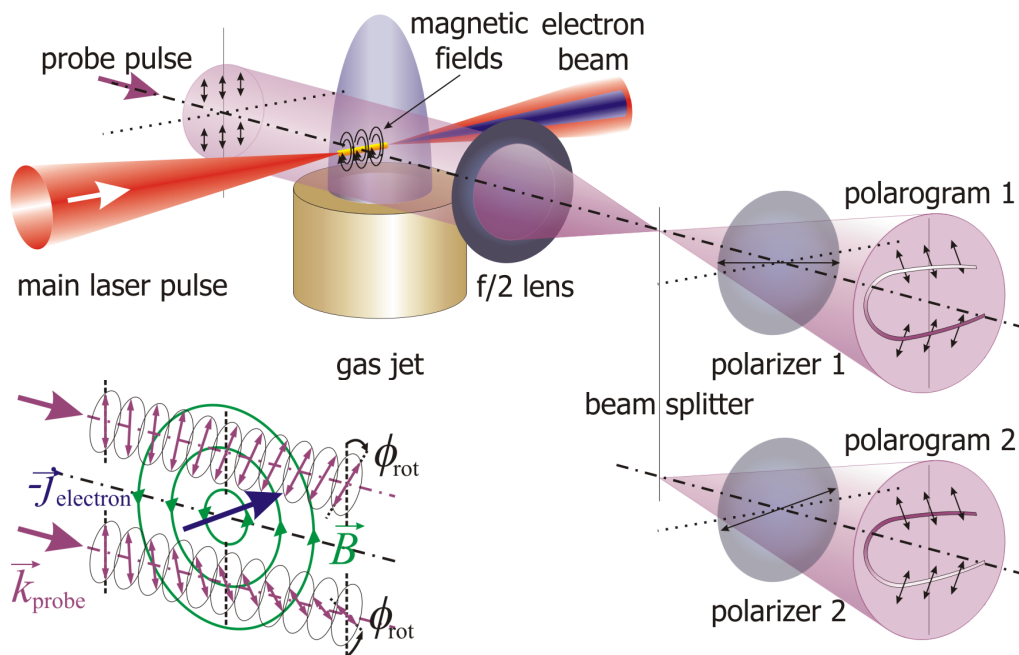
$$E_{\text{laser}} = 80 \text{ mJ}, \tau_{\text{laser}} = 8.5 \text{ fs},$$

$$f/6 \text{ OAP}, I_{\text{laser}} \approx 6 \times 10^{18} \text{ W/cm}^2$$

probe pulse:

$$\tau_{\text{probe}} \approx 8.5 \text{ fs @ } 1\omega$$

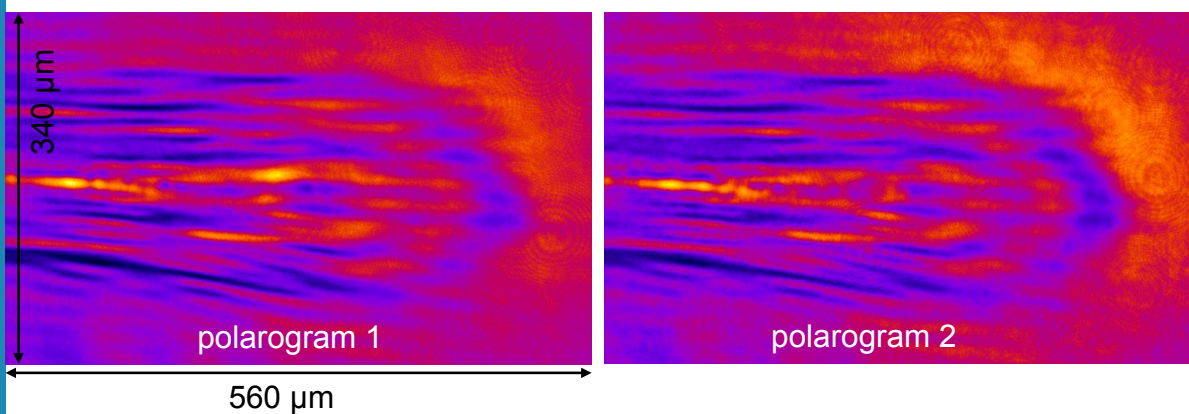
Electromagnetic Probe Pulses



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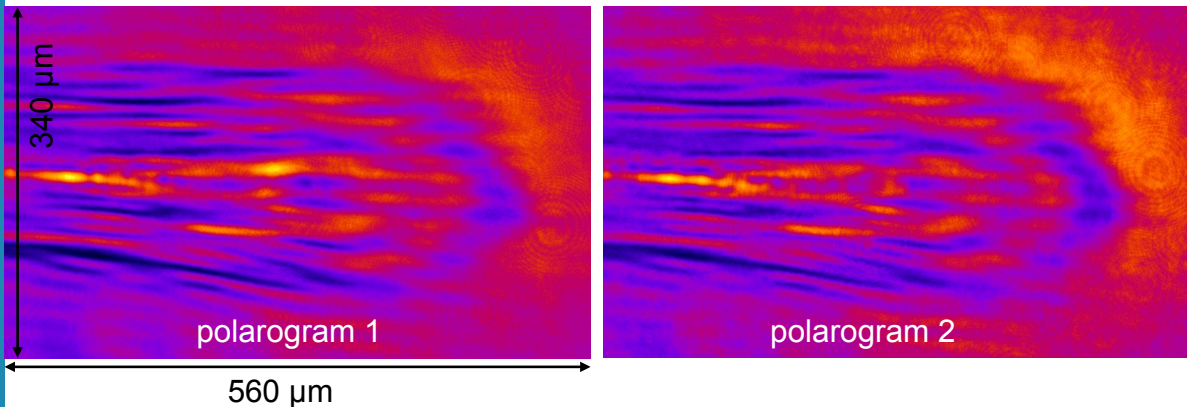
Electromagnetic Probe Pulses

Two polarograms from two (almost) crossed polarizers:



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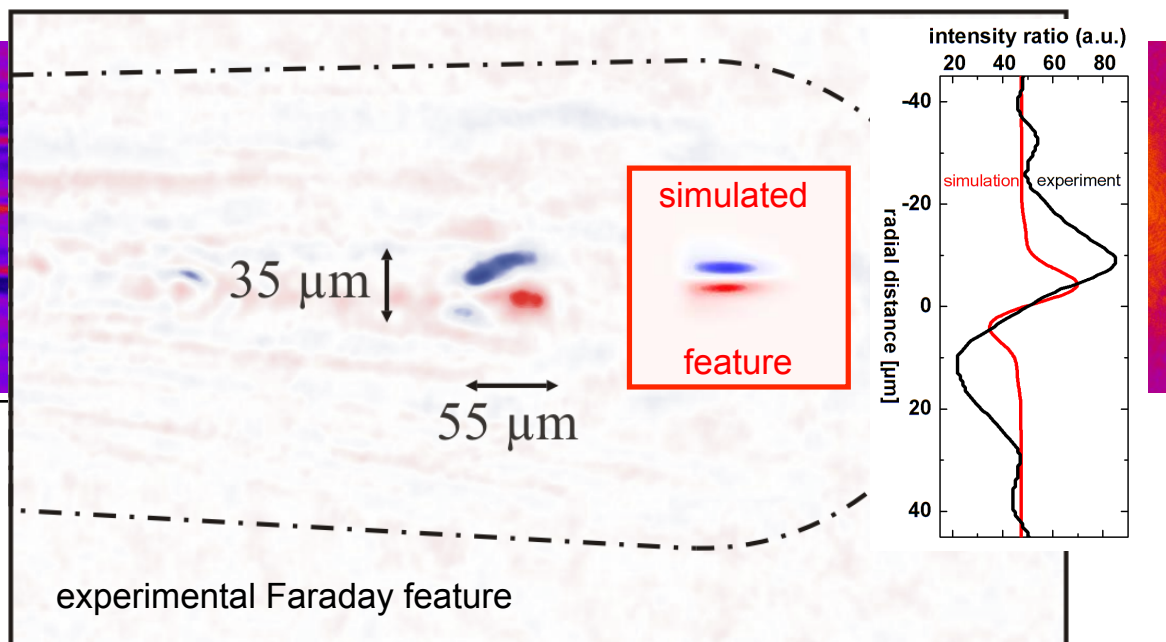
Two polarograms from two (almost) crossed polarizers:



$$I_{\text{pol1}} = I_0 [1 - \beta_1 \sin^2(90^\circ - \theta_{\text{pol1}} - \phi_{\text{rot}})] \quad I_{\text{pol2}} = I_0 [1 - \beta_2 \sin^2(90^\circ + \theta_{\text{pol2}} - \phi_{\text{rot}})]$$

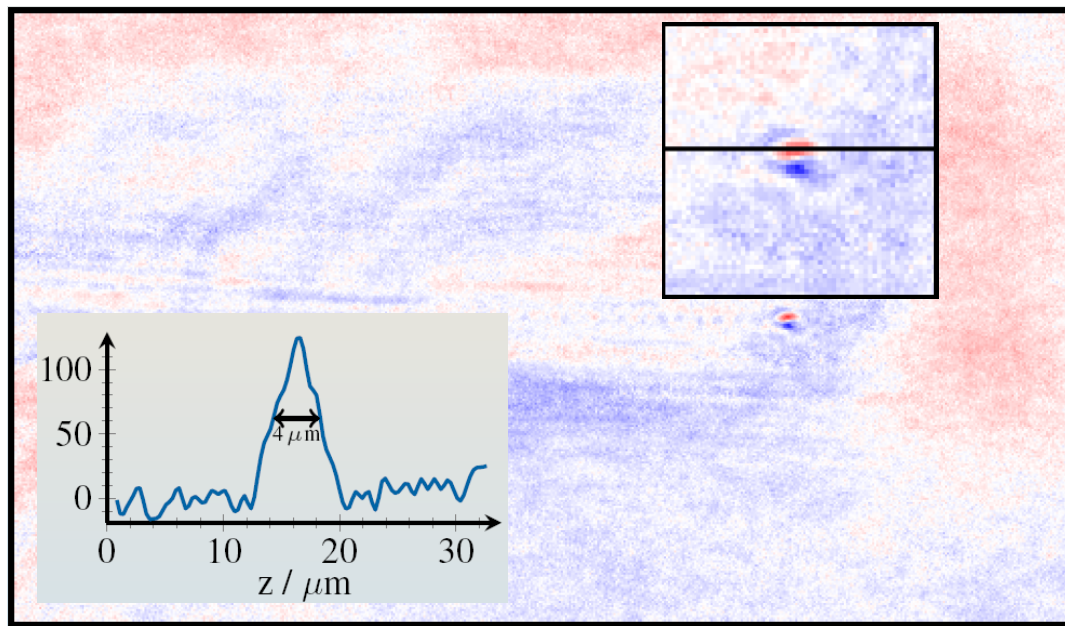
Deduce rotation angle ϕ_{rot} from pixel-by-pixel division of polarogram intensities:

$$I_{\text{pol1}}(x, y) / I_{\text{pol2}}(x, y)$$



Experimental evidence for B-fields from MeV electrons and bubble!

MCK *et al.*, Physical Review Letters **105**, 115002 (2010)

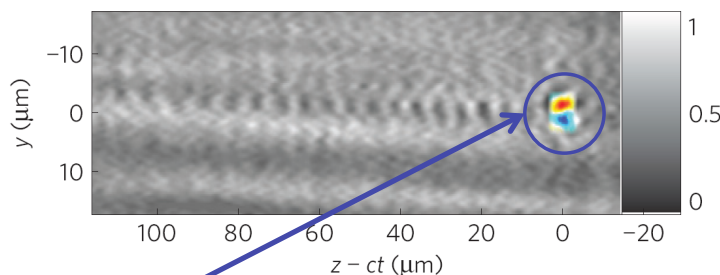


Electron bunch length: $\Delta z = 4 \mu\text{m}$

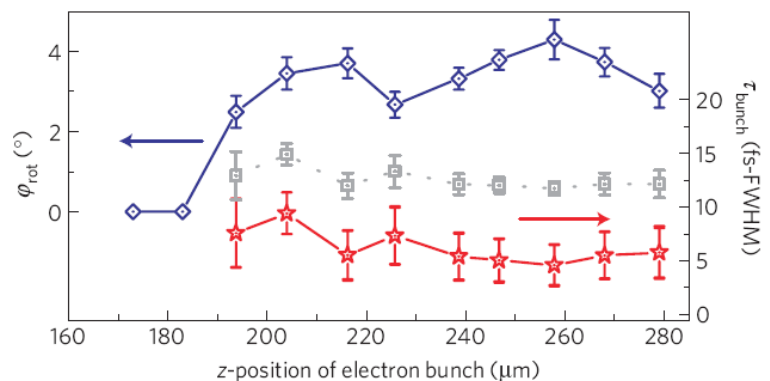
$\tau_{\text{FWHM}} = (6 \pm 2) \text{ fs}$, $\tau_{\text{RMS}} = (2.5 \pm 0.9) \text{ fs}$

A. Buck *et al.*, Nature Physics **7**, 543 (2011)

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- **Polarimetry:**
visualize e-bunch via
associated B-fields
- change delay between
pump and probe
⇒ movie of e-bunch
formation



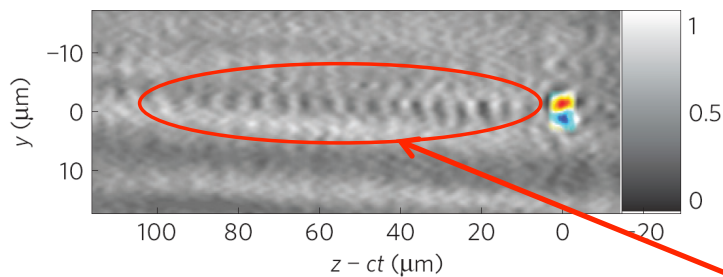
- observe e-bunch formation on-line!

A. Buck *et al.*, Nature Physics **7**, 543 (2011)

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Electromagnetic Probe Pulses

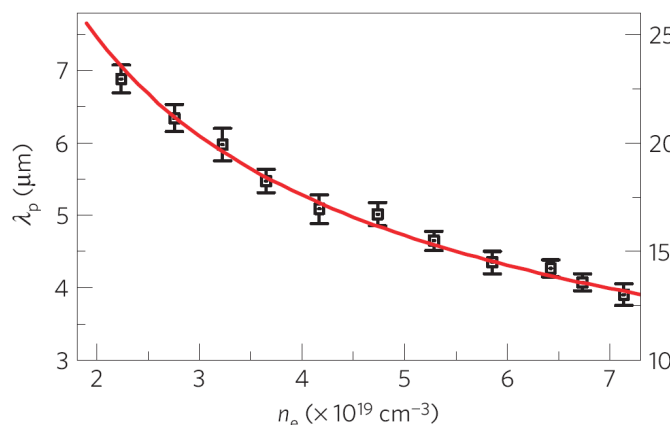
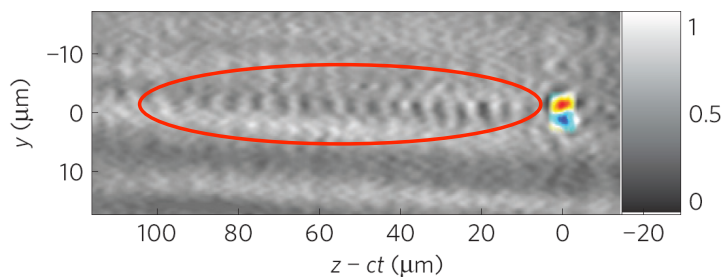


- **Polarimetry:**
visualize e-bunch via associated B-fields
 - change delay between pump and probe
⇒ movie of e-bunch formation
 - observe e-bunch formation on-line!
 - **Shadowgraphy:**
visualize plasma wave
 - change electron density ⇒ change plasma wavelength
- A. Buck *et al.*, Nature Physics **7**, 543 (2011)

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Electromagnetic Probe Pulses



- **Shadowgraphy:**
visualize plasma wave
 - change electron density ⇒ change plasma wavelength
- $$\lambda_p = v_{ph} T_p \approx \frac{2\pi c}{\omega_p} = 2\pi c \sqrt{\frac{\epsilon_0 m_e}{n_e e^2}}$$

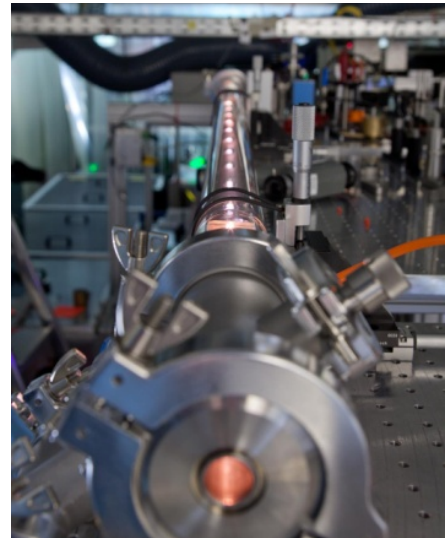
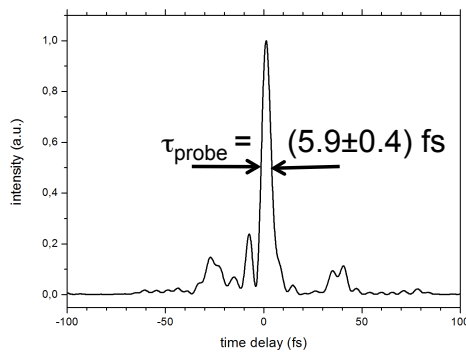
A. Buck *et al.*, Nature Physics **7**, 543 (2011)

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Electromagnetic Probe Pulses

- Few-cycle probe pulses
- Similar resolution with 35-fs driver laser:
- **frequency-broadening** of probe pulse (in gas-filled hollow fiber)

⇒ shorter τ_{probe}

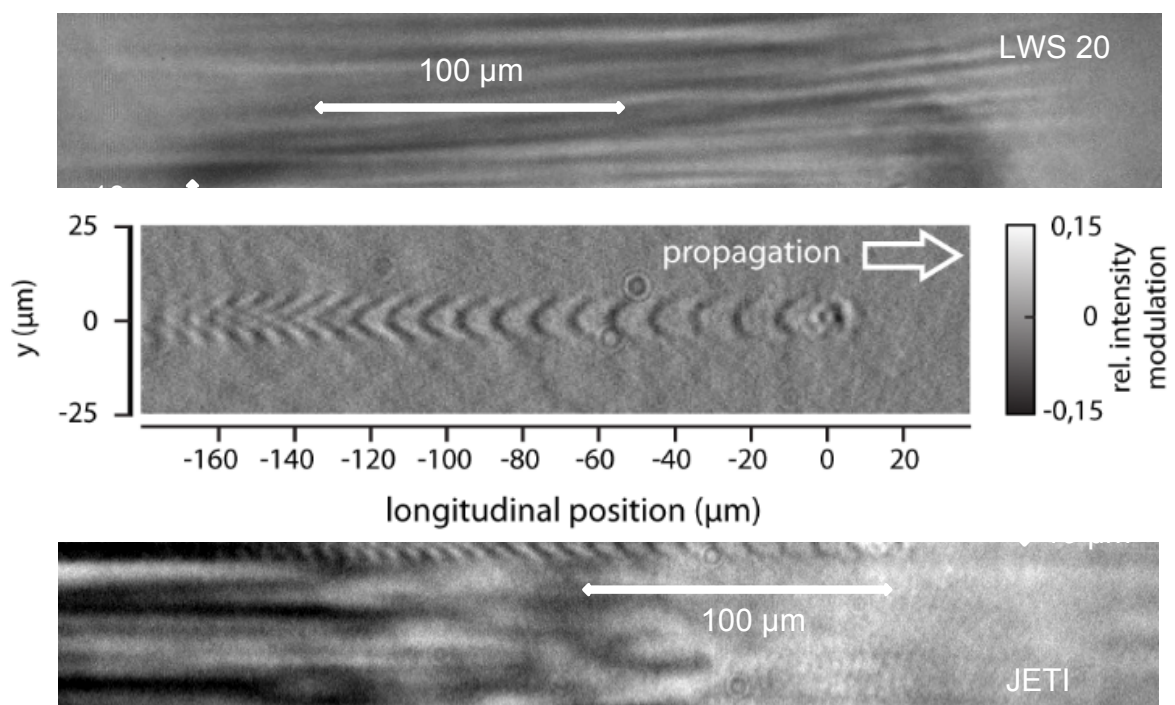


⇒ sub-main pulse temporal resolution,
1.1 μm spatial resolution with optimized imaging system

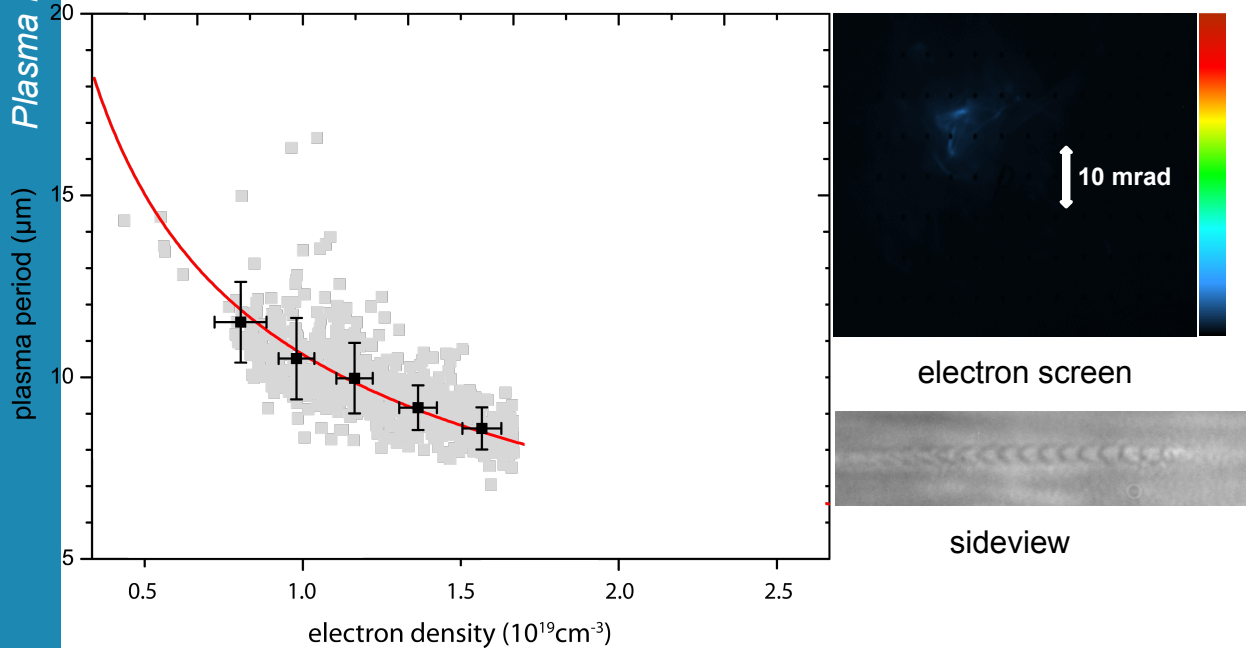
M. Schwab *et al.*, Appl. Phys. Lett. **103**, 191118 (2013)

Electromagnetic Probe Pulses

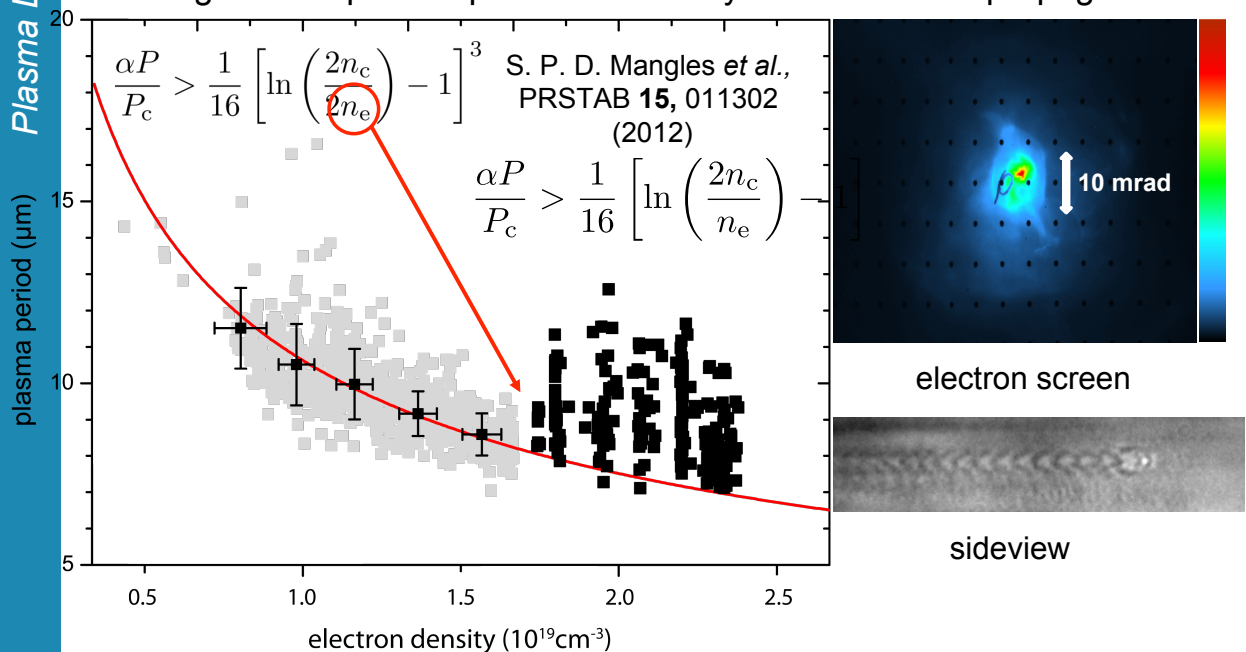
- Few-cycle probe pulses



- Length of 2nd plasma period vs. density after ~ 1.1 mm propagation



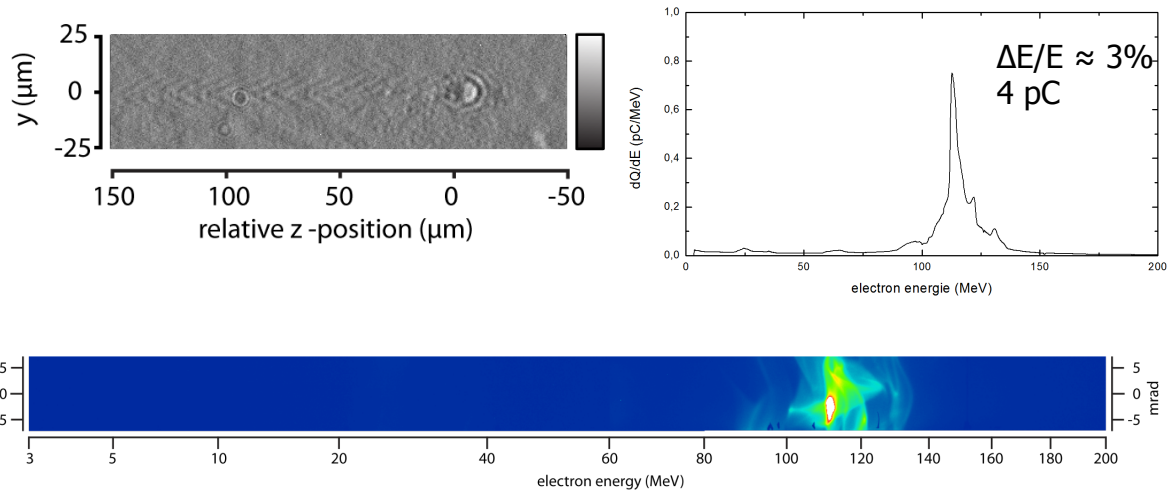
- Length of 2nd plasma period vs. density after ~ 1.1 mm propagation



Above threshold: increase of λ_p (beam loading)

Electromagnetic Probe Pulses

- After plasma wave evolution into single bubble:



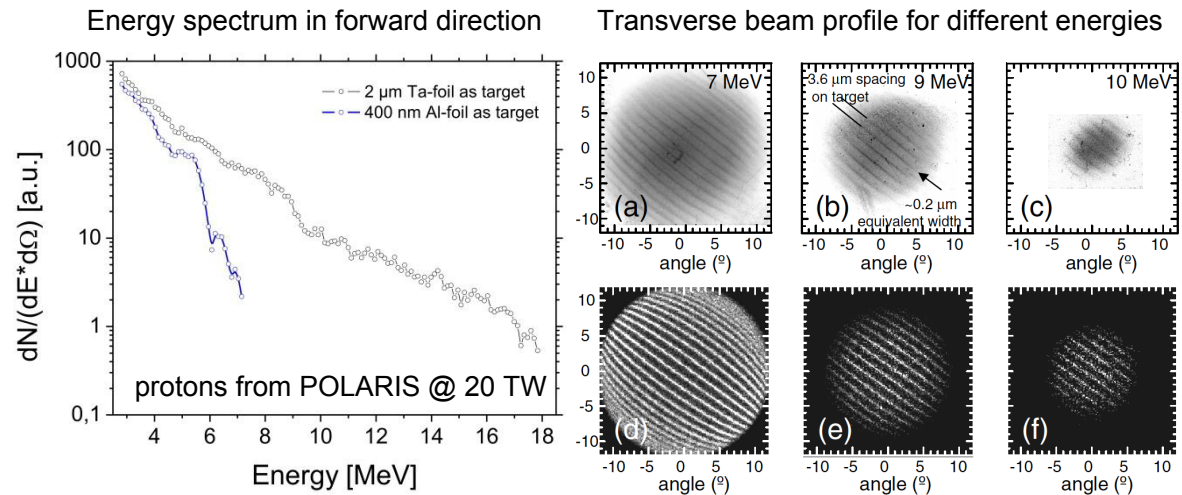
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Particle Probe Pulses

- Probing with laser-accelerated proton beams:
 - broad energy spectrum (up to few 10's of MeV)
 - laminar flow -> excellent imaging properties

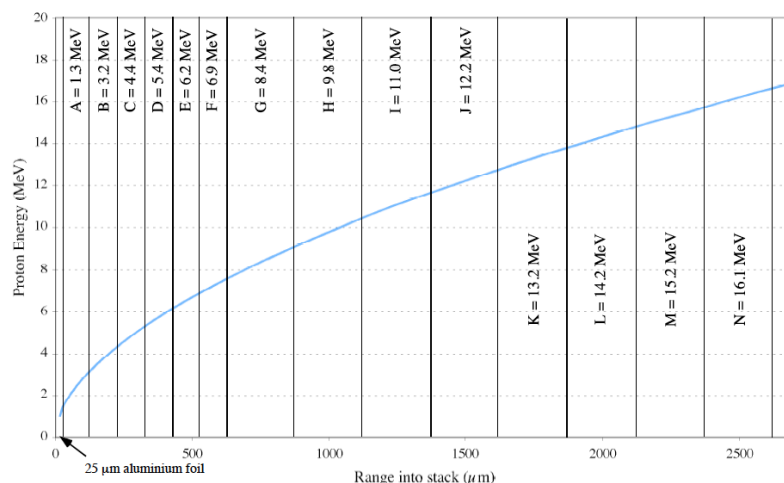


T. E. Cowan, PRL (2004)



Particle Probe Pulses

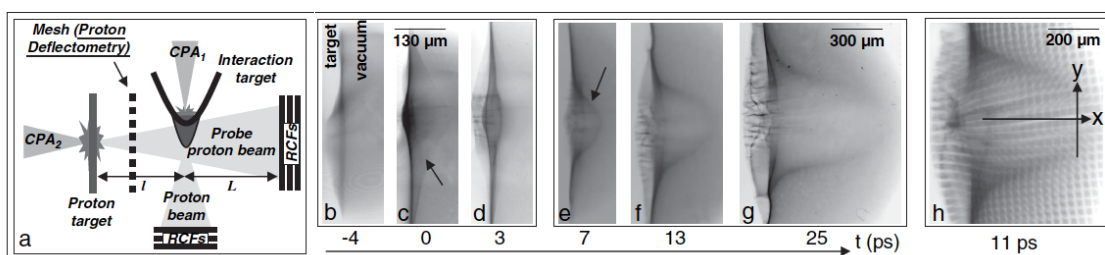
- Probing with laser-accelerated proton beams:
 - broad energy spectrum (up to few 10's of MeV),
 - laminar flow -> excellent imaging properties
 - energies detected separately in radiochromic film stack



L. Willingale, PhD thesis
Imperial College (2007)

- Probing with laser-accelerated proton beams:
 - broad energy spectrum (up to few 10's of MeV)
 - laminar flow -> excellent imaging properties
 - energies detected separately in radiochromic film stack
 - initial duration $\approx$ few times laser pulse duration, stretching due to different velocities
- Different images from different proton energies = snapshots from different times during the interaction
- Record movie of evolution of field distribution!

- Transverse probing with laser-accelerated proton beams:
 - proton deflection mainly due to electric fields

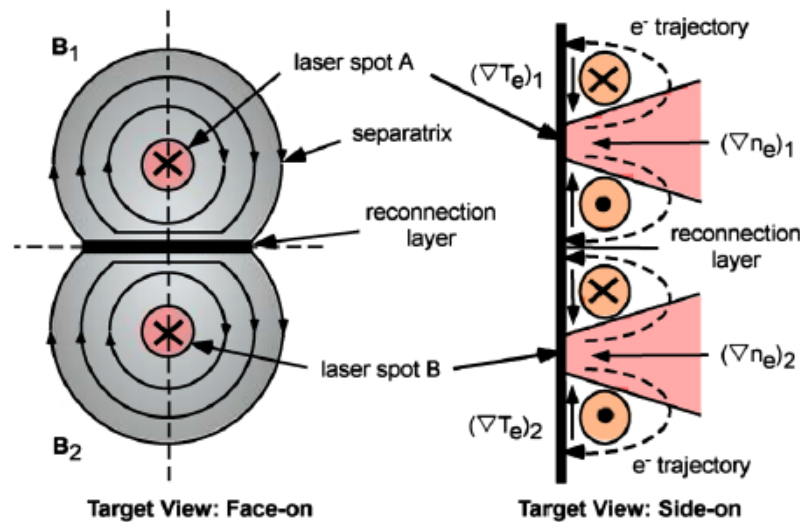


L. Romagnani, PRL (2005)

- record TNSA-sheath evolution in single shot,
- deduce sheath-field strength from mesh warping:

$$E_{\text{TNSA}} \geq 3 \times 10^{10} \text{ V/m}$$

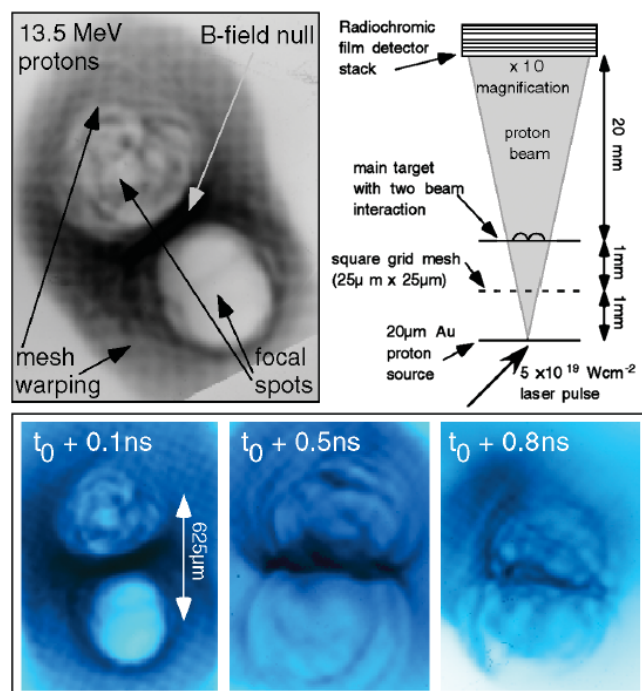
- Longitudinal probing with laser-accelerated proton beams:
 - proton deflection mainly due to magnetic fields



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P. Nilson, PRL (2006)

- Longitudinal probing with laser-accelerated proton beams:
 - visualize B-field geometry in 2-beam interaction
 - see merging of B-field structures between two plasma plumes
 - example of magnetic reconnection



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P. Nilson, PRL (2006)



Thanks to All Collaborators!



A. Sävert, M. Nicolai, M.B. Schwab, M. Reuter, M. Schnell,
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Helmholtz-Institute Jena

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S.P.D. Mangles, K. Poder, J. Cole, A. E. Dangor,
P. M. Nilson, Z. Najmudin
Imperial College London, UK

A.G.R. Thomas, L. Willingale, K. Krushelnick
Center for Ultrafast Optical Science, Michigan, US