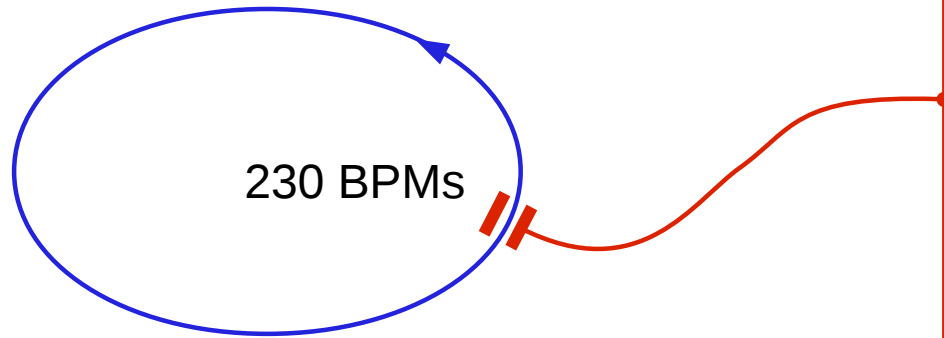


Model-Independent Analysis of Beam Position Monitor Measurements

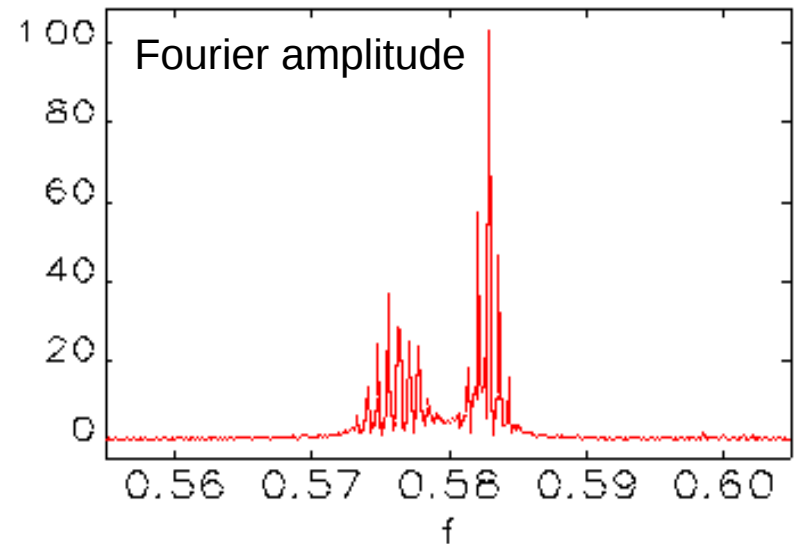
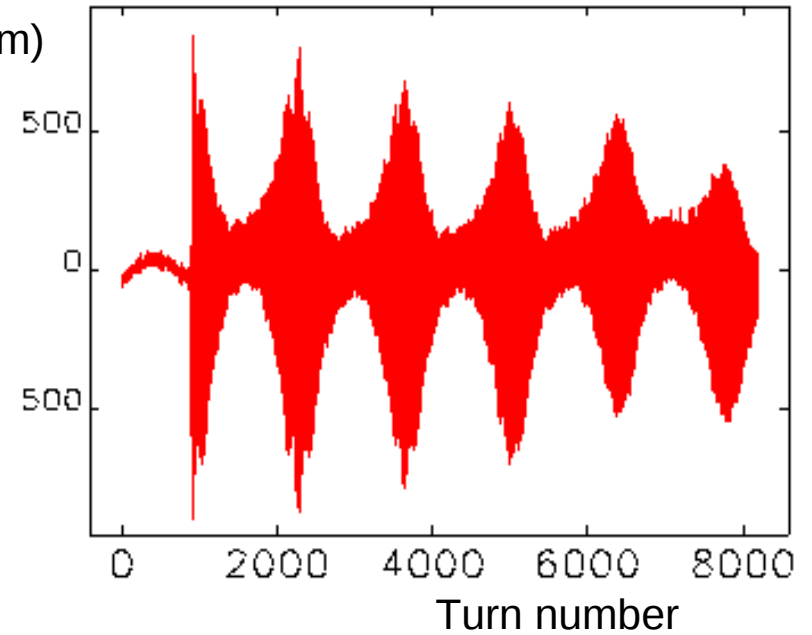
Alexey Petrenko, BINP, Novosibirsk, Russia

Turn-by-turn BPM signal after beam is kicked with a horizontal kicker

Tevatron collider

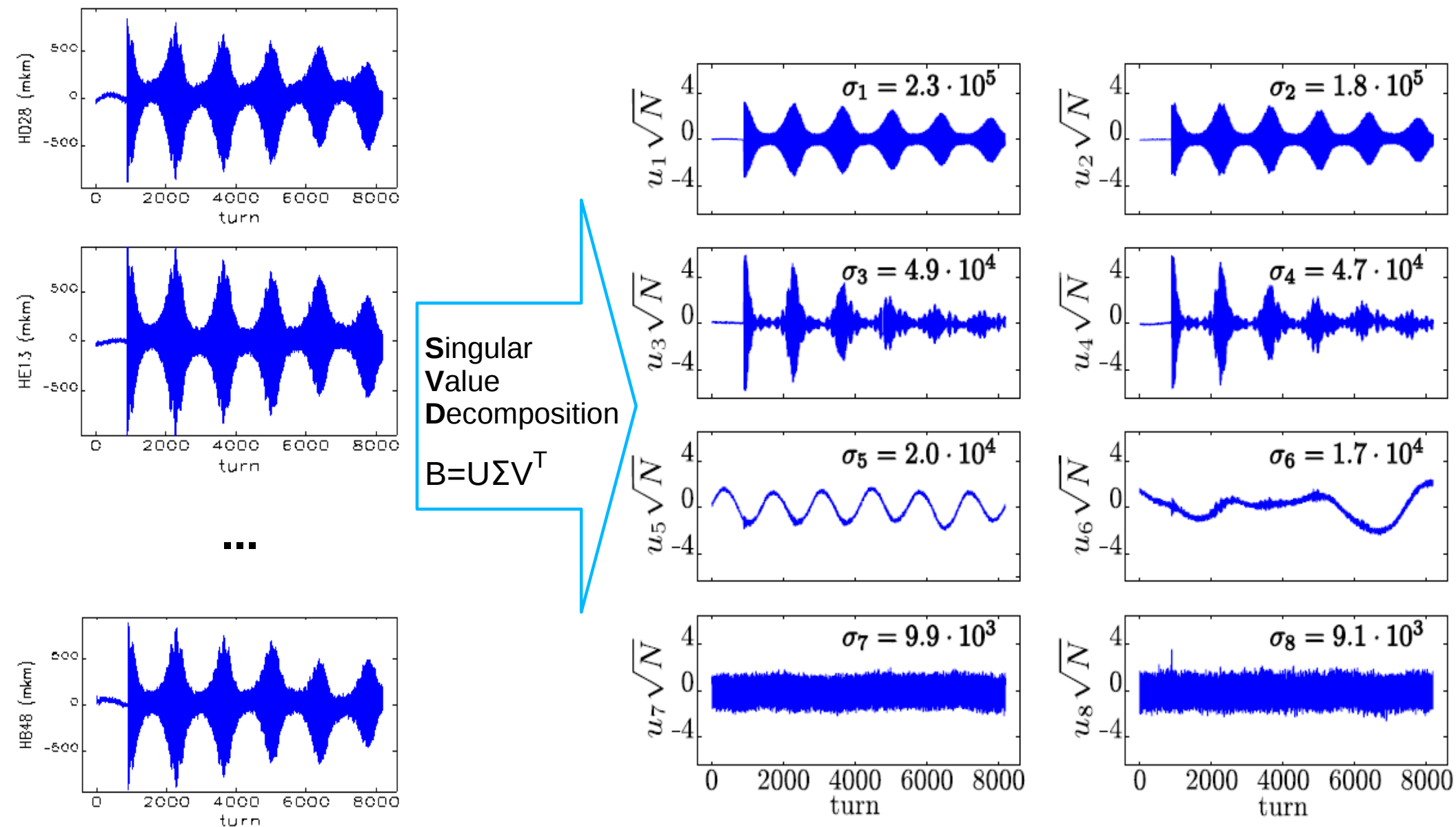


X (mkm)

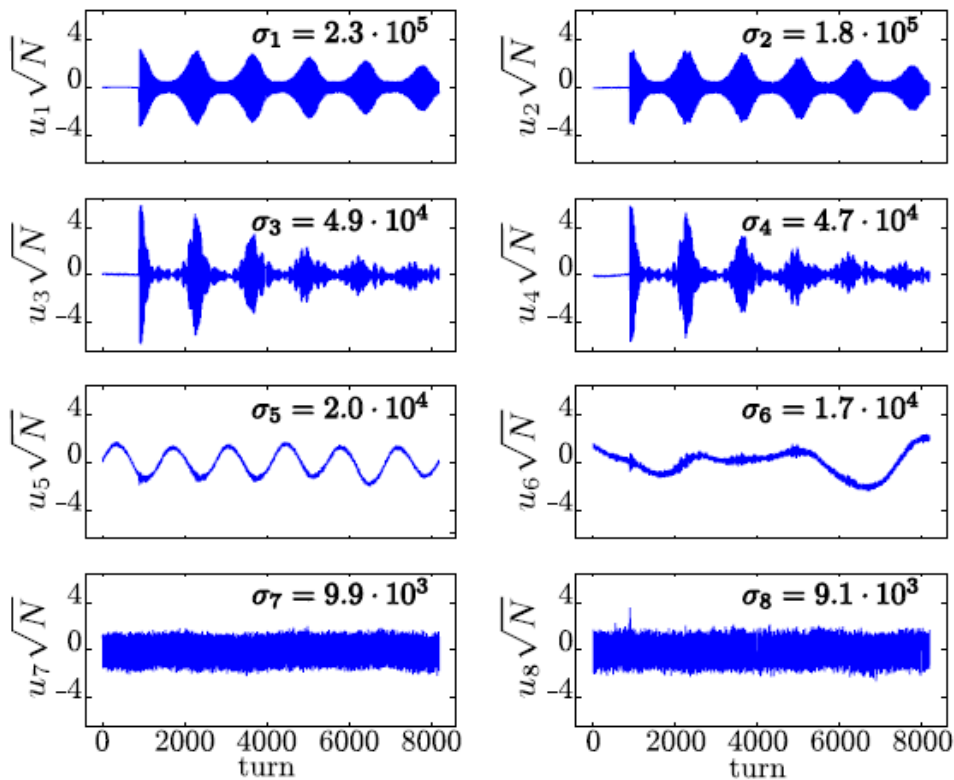


Model-Independent Analysis of BPM signals

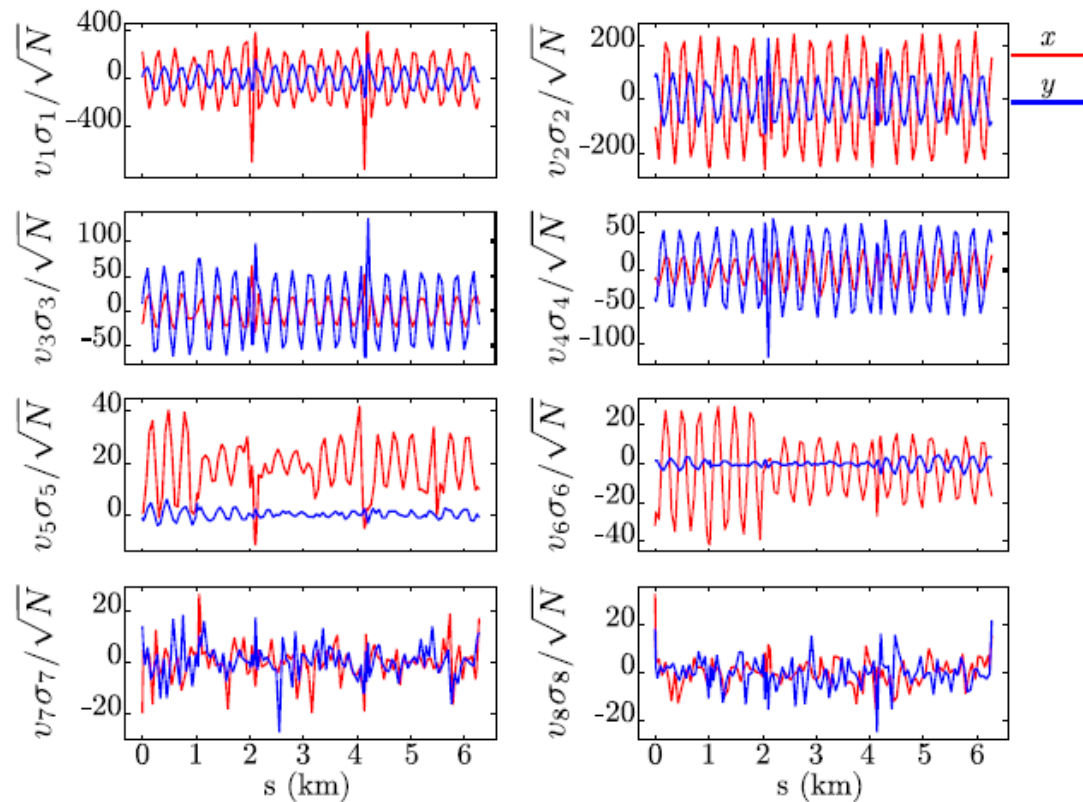
Signal from each BPM is represented as a linear combination of a small number of mutually independent (orthogonal) components:



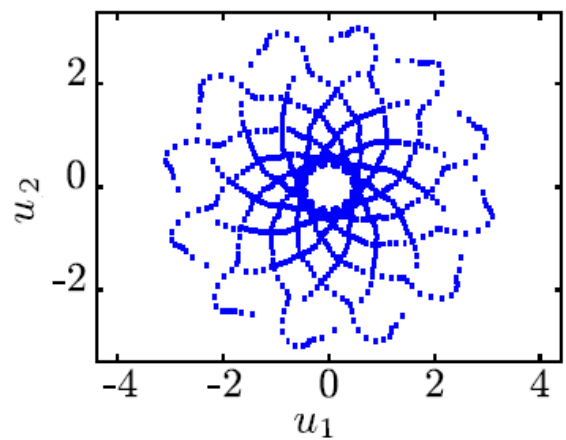
Temporal modes
(mutually independent components)



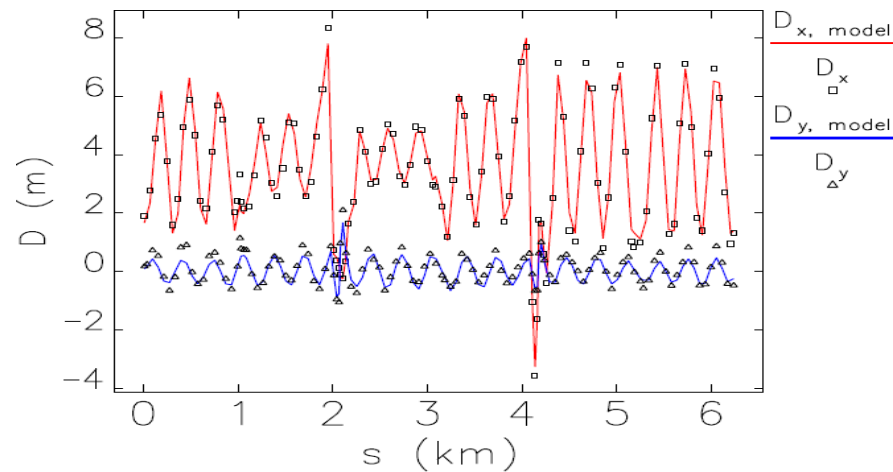
Spatial modes
(amplitude of temporal mode vs BPM position)



Beam centroid trace in phase space:



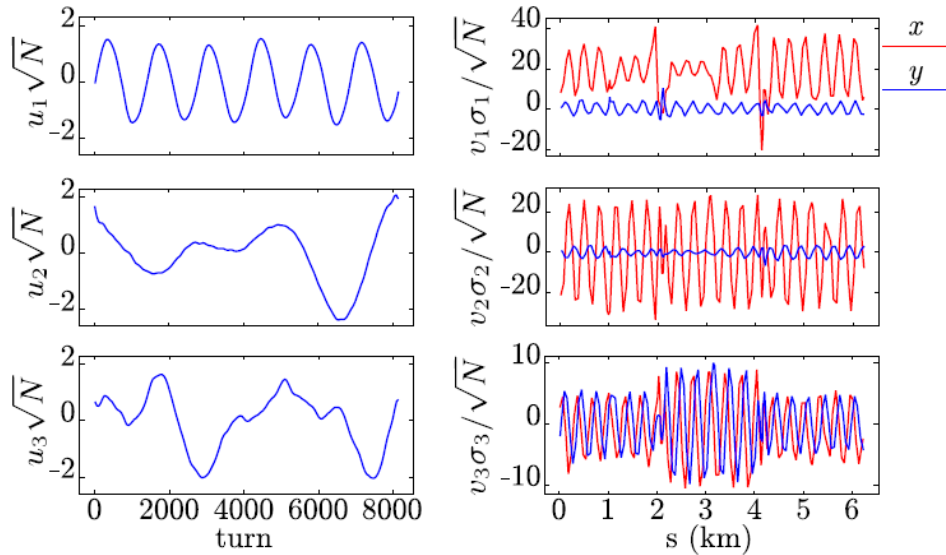
Lattice functions:



Horizontal and vertical dispersion function

Finding the source of some modes

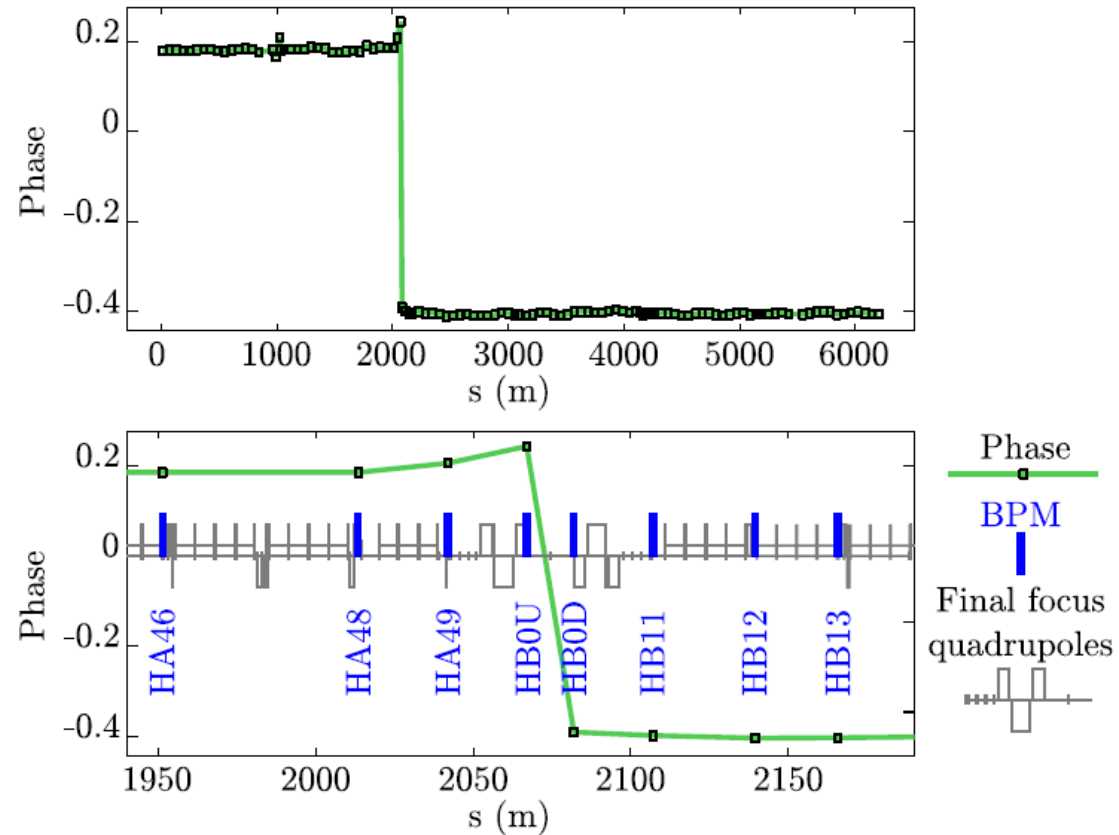
Slow modes (after low-pass Fourier filter)



At any pair of (horizontal) BPMs any spatial mode can be represented as a linear combination of two independent orbits:

$$\begin{cases} v_{\text{vibr}}(s_1) = C_1 v_{b1}(s_1) + C_2 v_{b2}(s_1) \\ v_{\text{vibr}}(s_2) = C_1 v_{b1}(s_2) + C_2 v_{b2}(s_2) \end{cases}$$

"Betatron" phase of mode 2 (vibrational mode)



$$\tan(\text{Phase}) = C_1 / C_2$$

Elements of transport matrix between BPMs

Using any 4 linearly independent orbits (e. g. spatial modes of betatron oscillations) it is possible to calculate some of the transport matrix elements between BPMs:

$$(x_1^a x_2^b - x_2^a x_1^b)/Q_{12} + (x_3^a x_4^b - x_4^a x_3^b)/Q_{34} = \mathcal{R}_{12}^{ab}$$

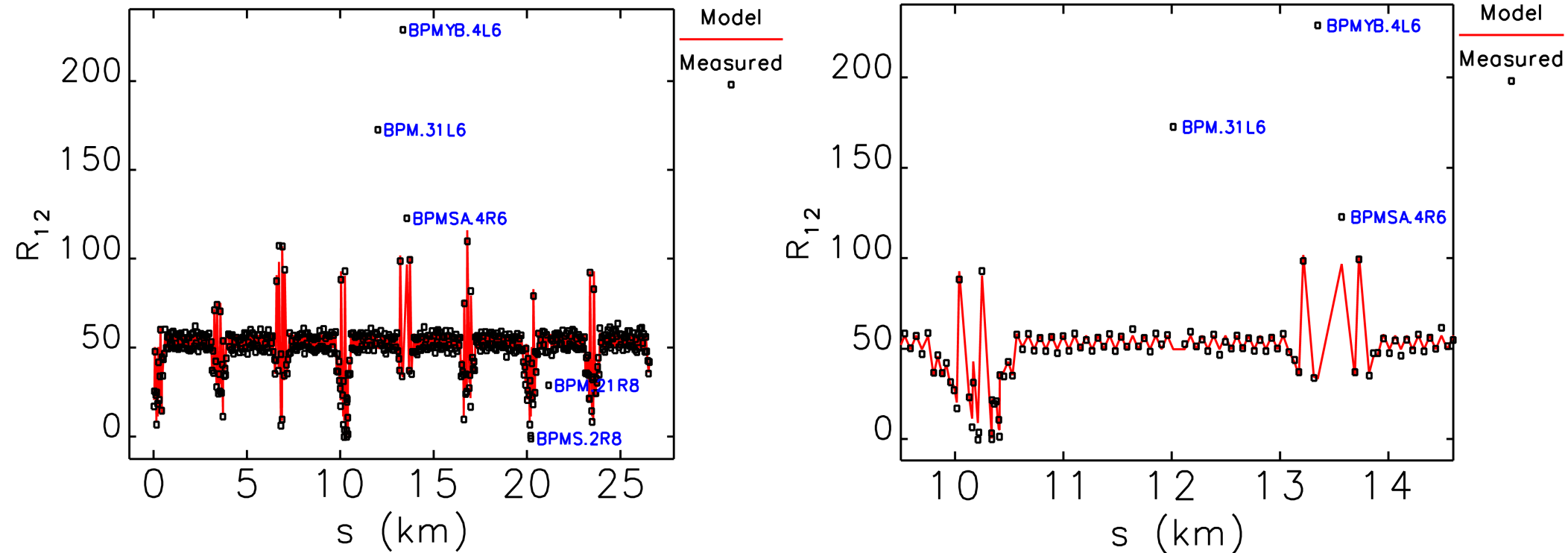
$$(x_1^a y_2^b - x_2^a y_1^b)/Q_{12} + (x_3^a y_4^b - x_4^a y_3^b)/Q_{34} = \mathcal{R}_{32}^{ab}$$

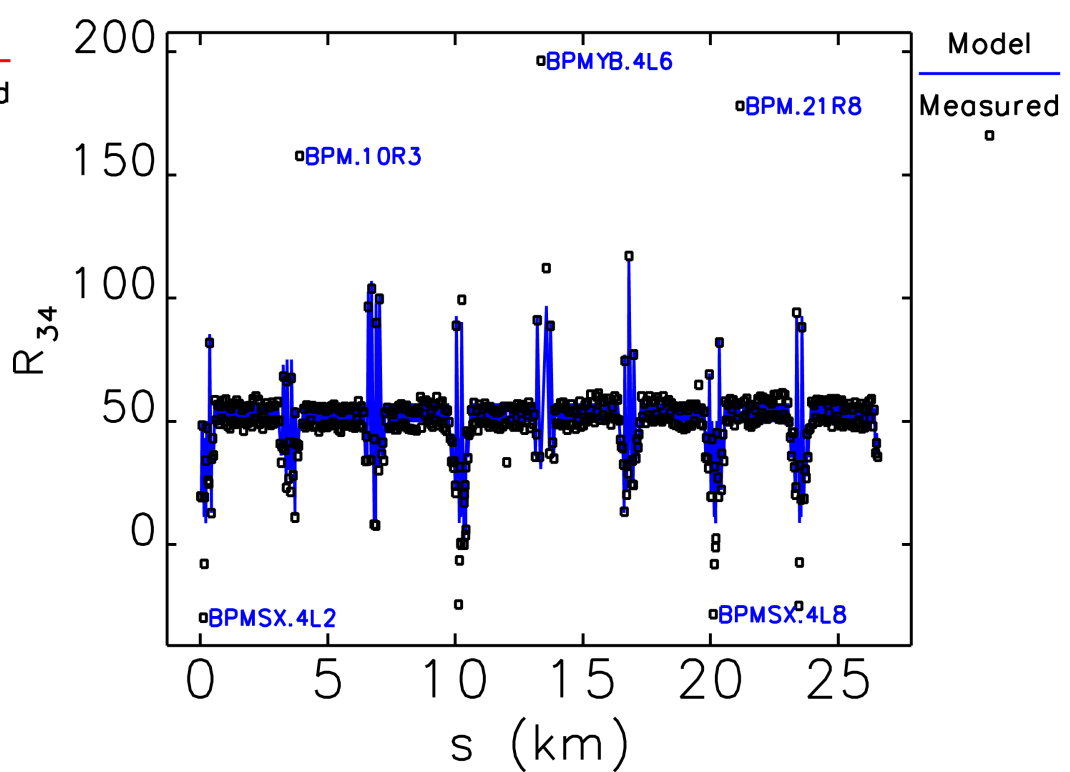
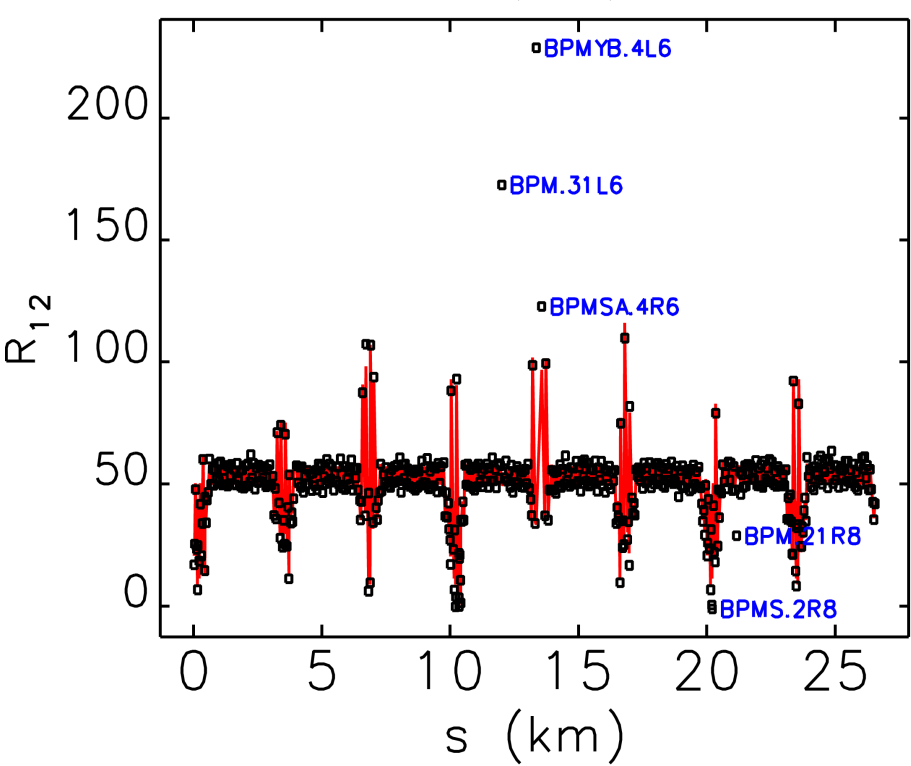
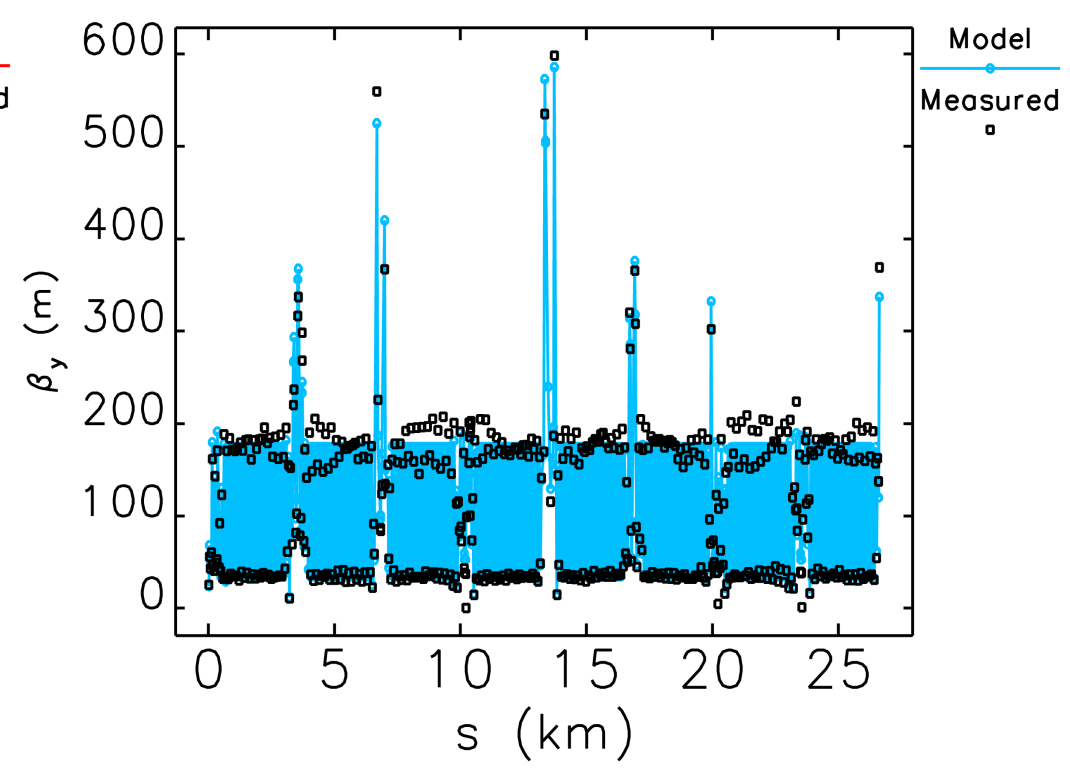
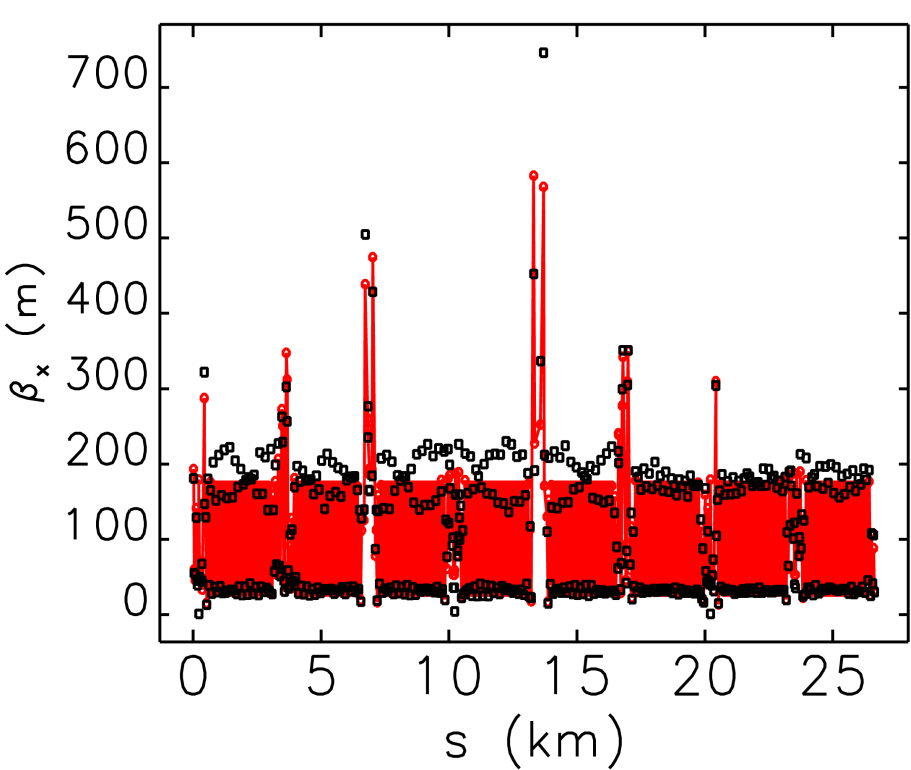
$$(y_1^a x_2^b - y_2^a x_1^b)/Q_{12} + (y_3^a x_4^b - y_4^a x_3^b)/Q_{34} = \mathcal{R}_{14}^{ab}$$

$$(y_1^a y_2^b - y_2^a y_1^b)/Q_{12} + (y_3^a y_4^b - y_4^a y_3^b)/Q_{34} = \mathcal{R}_{34}^{ab}$$

J. Irwin and Y. T. Yan, “*Beamline Model Verification Using Model Independent Analysis*”, Proceedings of EPAC 2000, Vienna, Austria.

R_{12} calculated from turn-by-turn measurements (courtesy R. Miyamoto) at the LHC:





Thank you for your attention!

In case you want to try the described techniques in your accelerator, I'll be glad to share my software or explain the details:

petrenko@ngs.ru