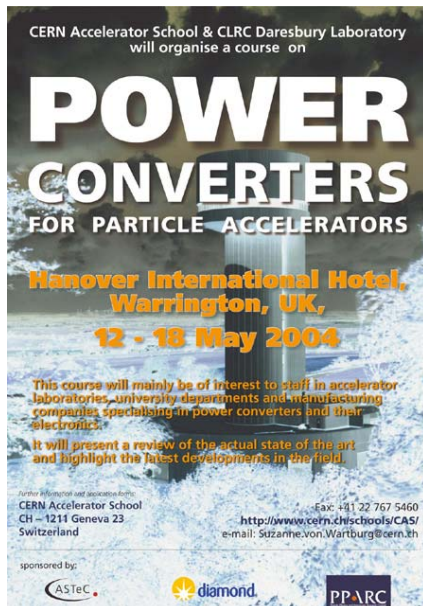


Regulation: recalls and digital loops

12-18th May 2004

**Power Converters
for particle accelerators
Warrington, UK**

Frédéric BORDRY
CERN



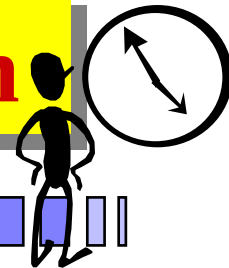
Basic recalls
(continuous and discrete domains)

Digital control system: RST algorithm

Example :LHC power converter regulation

MIMO to SISO

Continuous - time Models : Time Domain



Time Domain :

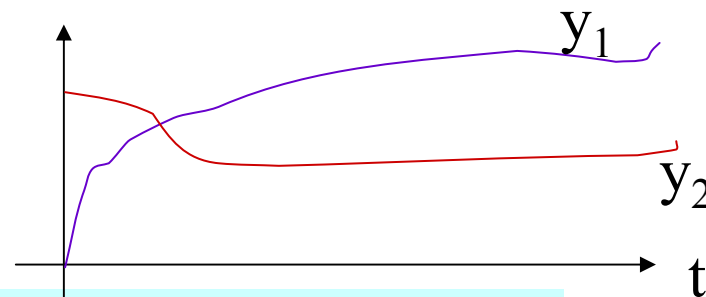
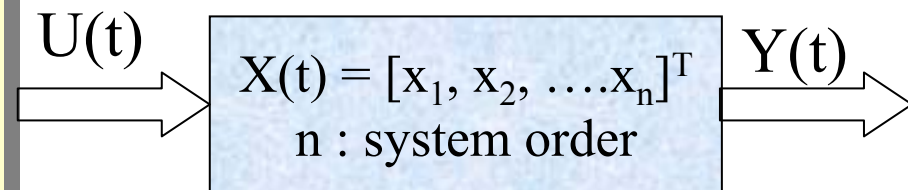
$$\frac{dX}{dt} = F[X(t), U(t)] ; X(t_0) = X(0)$$

$$Y(t) = G[X(t), U(t)]$$

Linear system

$$\frac{dX}{dt} = A(t).X(t) + B(t).U(t)$$

$$Y(t) = C(t).X(t) + D(t).U(t)$$

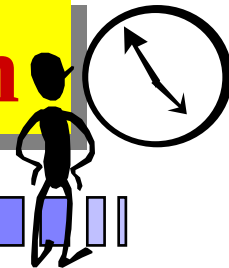


Examples : mono-input mono-output

$$1\text{st order : } \frac{dy}{dt} = -\frac{y(t)}{T} + \frac{G}{T} u(t)$$

$$2\text{nd order : } \frac{d^2y(t)}{dt^2} + 2.z.\omega_o.\frac{dy(t)}{dt} + \omega_o^2. Y(t) = \omega_o^2. u(t)$$

Continuous - time Models : Time Domain



Time Domain :

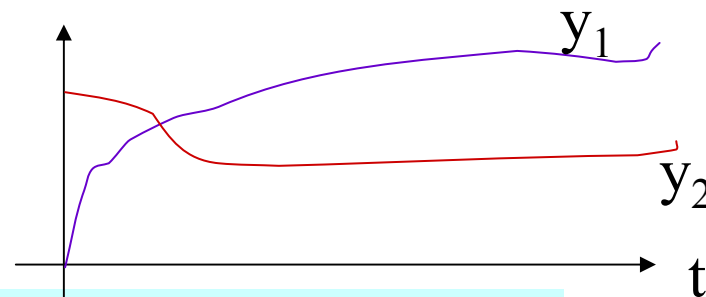
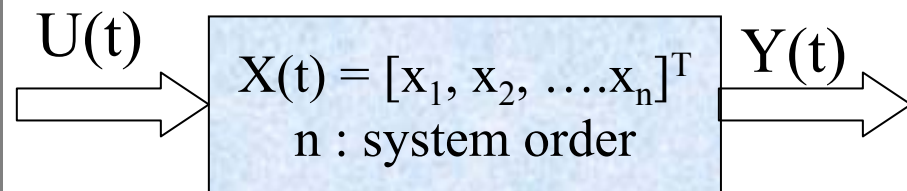
$$\frac{dX}{dt} = F[X(t), U(t)] ; X(t_0) = X(0)$$

$$Y(t) = G[X(t), U(t)]$$

Linear system

$$\frac{dX}{dt} = A.X(t) + B.U(t)$$

$$Y(t) = C.X(t) + D.U(t)$$



Examples : mono-input mono-output

1st order : $\frac{dy}{dt} = -y(t)/T + G/T u(t)$

2nd order : $\frac{d^2y(t)}{dt^2} + 2.z.\omega_o.\frac{dy(t)}{dt} + \omega_o^2.Y(t) = \omega_o^2.u(t)$

Continuous - time Models : Frequency Domain

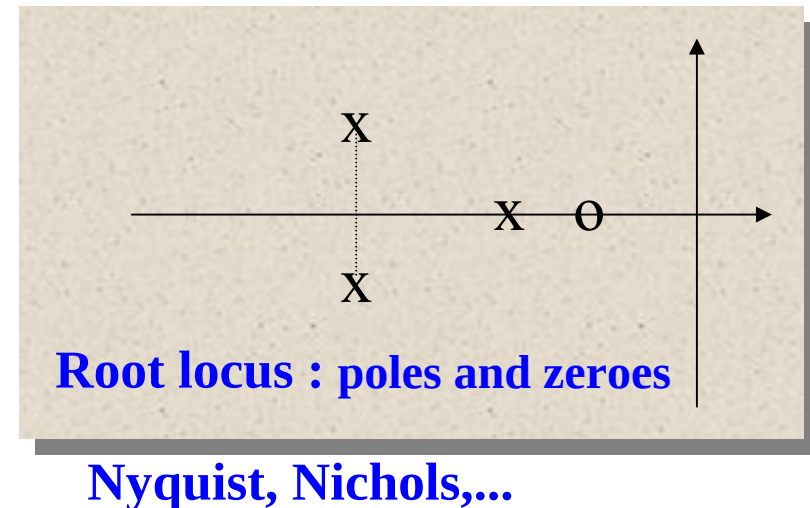
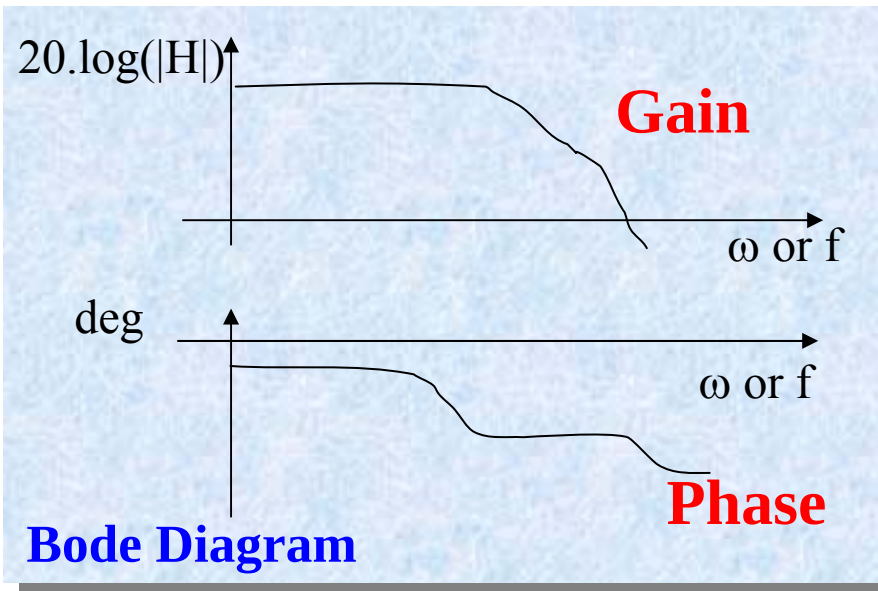
Linear system

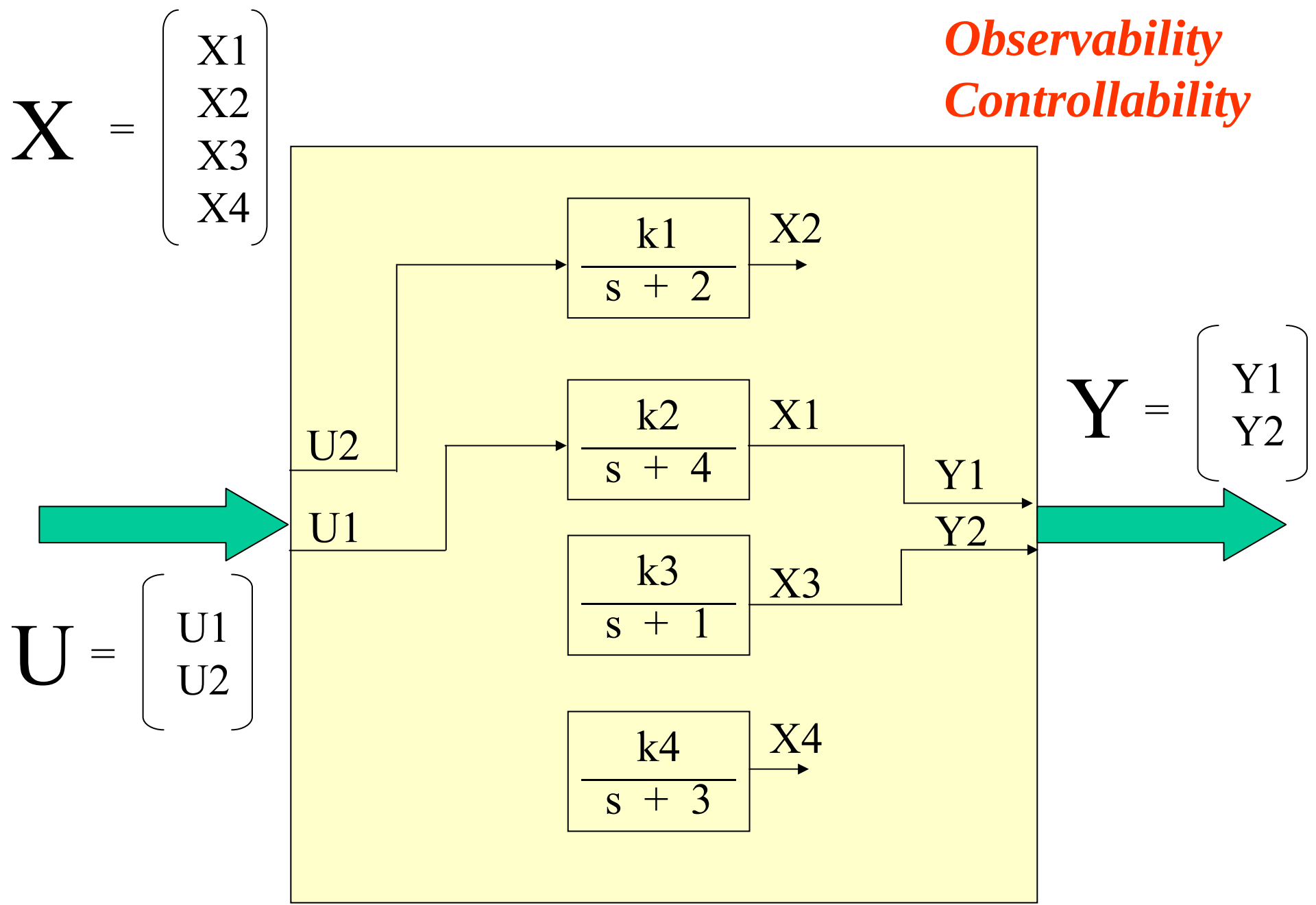
$H(s)$: transfer function



Note:

State Equation
Differential Eq.
Transfer function
Observability,
Controllability

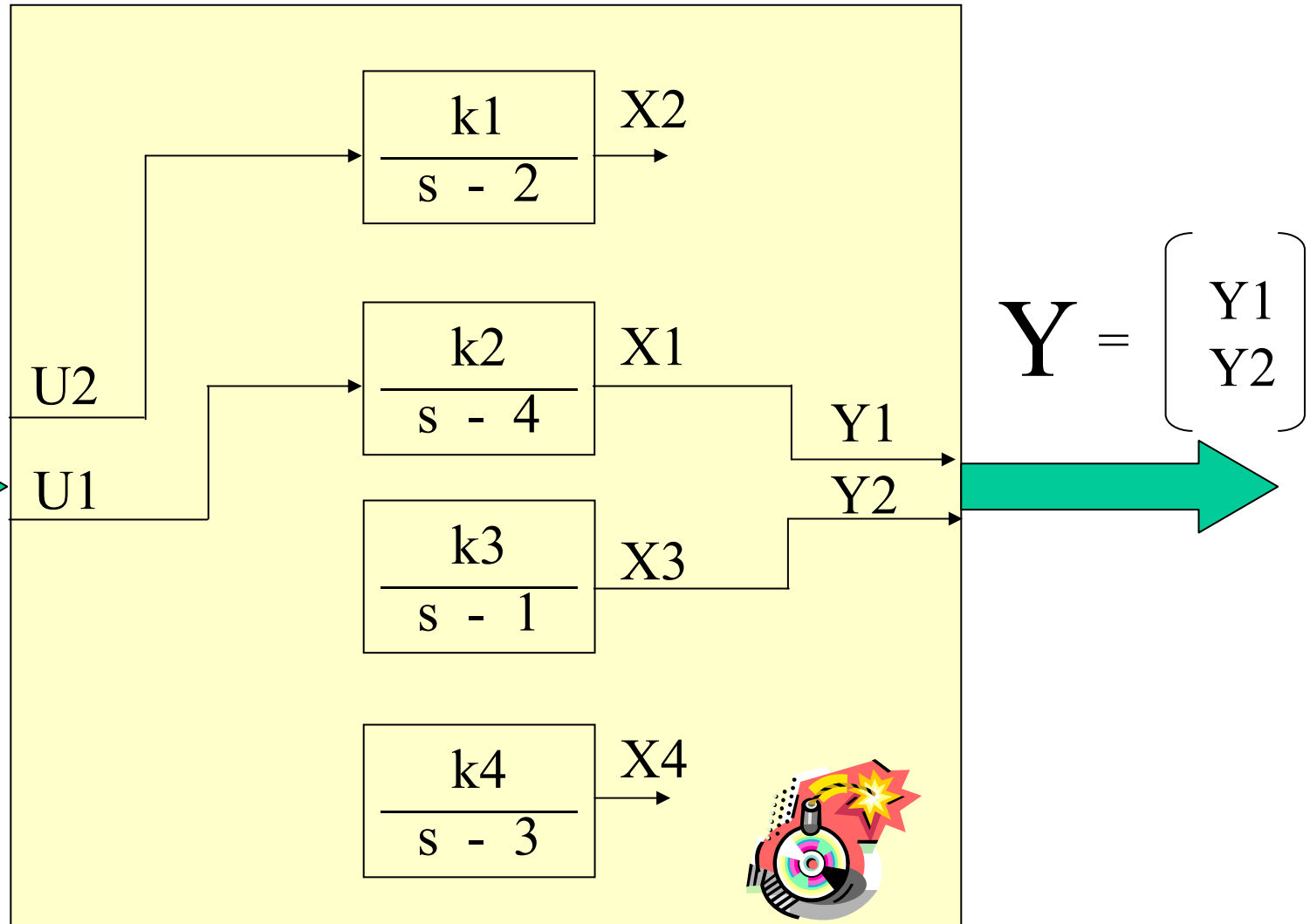




Observability
Controlability

$$\mathbf{X} = \begin{bmatrix} X1 \\ X2 \\ X3 \\ X4 \end{bmatrix}$$

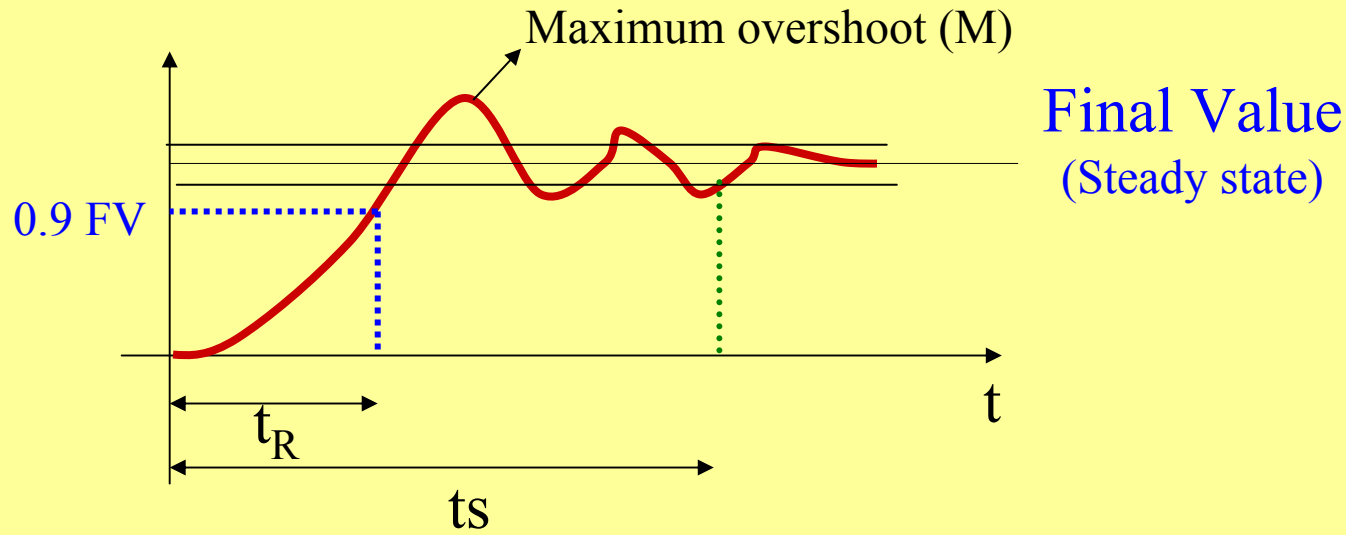
$$\mathbf{U} = \begin{bmatrix} U1 \\ U2 \end{bmatrix}$$



Must modify the system structure : addition of transducers and/or actuators

Continuous - time Models : Time responses

Response of a dynamic system for a step input



Example : 1st Order

$$H(s) = G/(1+sT)$$

$$FV = G$$

$$t_R = 2.2 T$$

$$t_s = 2.2 T \text{ (for 10\% FV)}$$

$$t_s = 3 T \text{ (for 5\% FV)}$$

$$M = 0$$

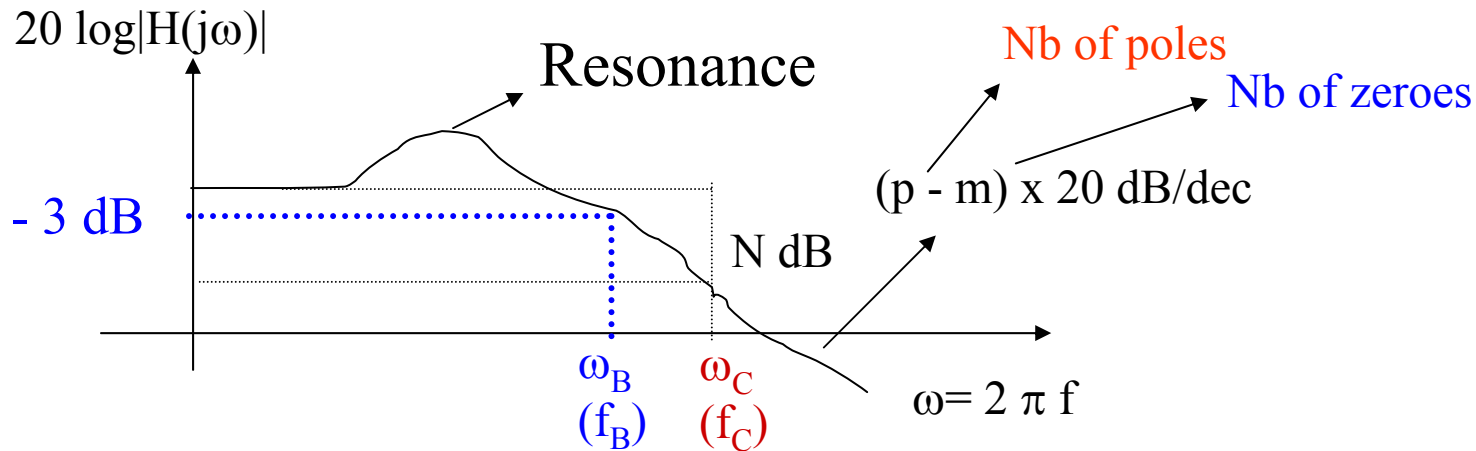
t_R : Rise Time ; define as the time needed to attain 90% of the final value ; or as the time needed for the output to pass from 10 to 90% of the final value

t_s : Settling Time ; define as the time needed for the output to reach and remain within a tolerance zone around the final value ($\pm 10\%$, $\pm 5\%$, $\pm 1\%$,...)

FV : Final Value ; a fixed output value obtained for $t \rightarrow \infty$

M : Maximum Overshoot ; expressed as a percentage of the final value

Continuous - time Models : Frequency responses

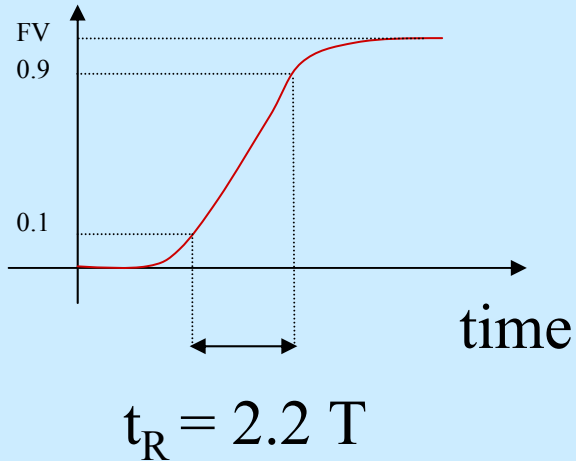
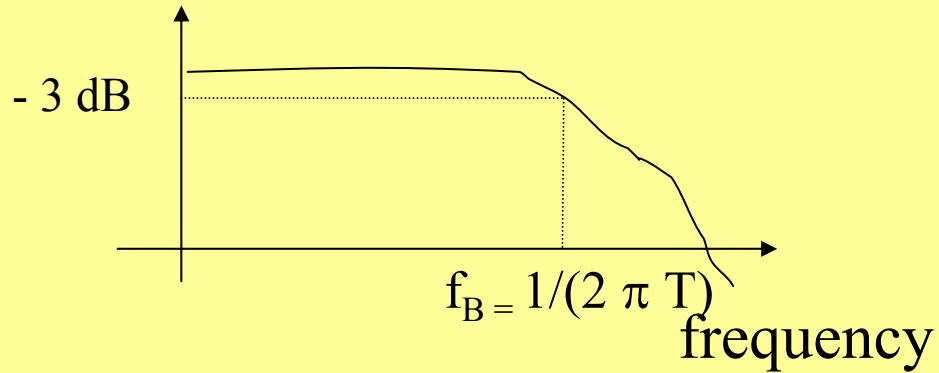


f_B : Bandwidth ; the frequency from which the zero-frequency (steady state) gain $G(0)$ is attenuated by more than 3 dB ; $G(\omega_B) = G(0) - 3\text{dB}$ or $G(\omega_B) = 0.707 \cdot G(0)$

f_C : Cut-off frequency ; the frequency from which the attenuation is more than N dB ;
 $G(\omega_C) = G(0) - N\text{dB}$

Q : Resonance factor ; the ratio between the gain corresponding to the maximum of the frequency response curve and the value $G(0)$

Reciprocity : Time / Frequency



$$f_B \cong 0.35 / t_R$$

System with delay τ

$$u(t) \Rightarrow u(t - \tau)$$

Reflects the fact that the input will act with a time delay of τ

Transfer function

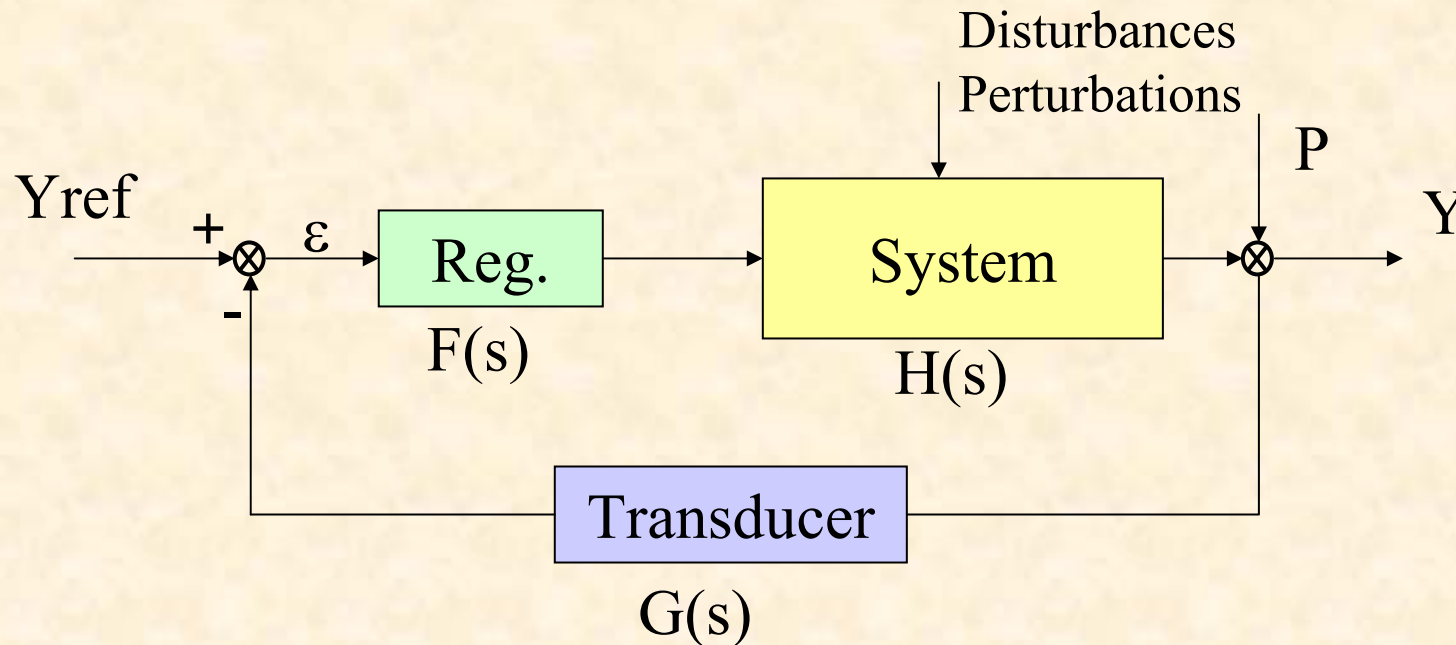
$$H(s) \Rightarrow H(s) e^{-s\tau}$$

$$H_{\text{delay}}(j\omega) = e^{-j\omega\tau} = |1| e^{-j\omega\tau}$$



No change on the gain but a phase proportional to the frequency

Closed Loop



Open loop : system $H(s)$; system with controller $F(s).H(s)$

Closed loop : $H_{CL}(s) = F(s).H(s) / [1 + F(s). H(s) G(s)]$

Steady state error : $F(s).H(s)$ must contains the internal model of the reference (the transfer function that generates $Y_{ref}(t)$ from the Dirac impulse ;
e.g. step = $(1/s) * \text{Dirac}$; ramp = $(1/s^2) * \text{Dirac}$, sine wave = $\omega_0/(p^2+\omega_0^2)*\text{Dirac} \dots$)

Closed Loop : Perturbation rejection



Perturbation-output sensitivity function :

$$S_{yp}(s) = Y(s) / P(s) = 1 / [1 + F(s).H(s).G(s)]$$

Perturbation rejection :

$S_{yp}(0) = 0$ to get a perfect rejection of the perturbation in steady state (controller must contain the classes of perturbation)

and

$$|S_{yp}(\omega)| < G ; \forall \omega$$

$$[\text{Typical value : } |S_{yp}(\omega)| < 2 \text{ (6dB)} ; \forall \omega]$$

If the energy of the perturbation is concentrated in a given frequency band, the $|S_{yp}(\omega)|$ should be limited in this band.

System dynamics

$$U \rightarrow \boxed{\frac{dX}{dt} = A.X + B.U} \rightarrow Y$$

$$X(t) = \underbrace{e^{A(t-t_0)} . X(t_0)}_{\text{Free state response}} + \underbrace{\int_{t_0}^t e^{A(t-\tau)} . B.U(\tau) d\tau}_{\text{Forced state response}}$$

Stability of the system:

$$\lim_{t \rightarrow \infty} e^{A(t-t_0)} . X(t_0) = 0$$

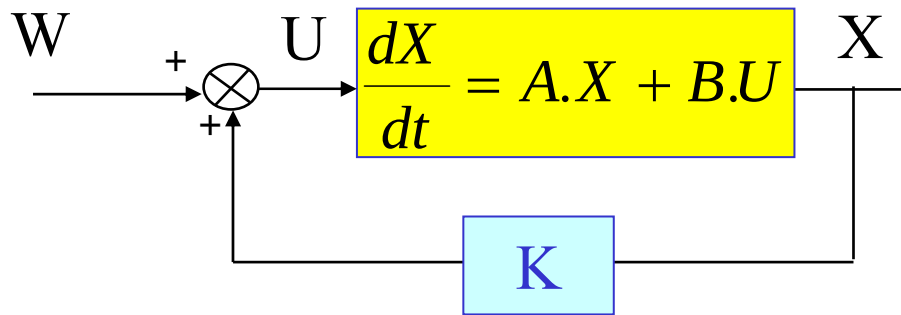
Sign of the real part of A eigenvalues must be negative.

Eigenvalues determine the dynamics of the system

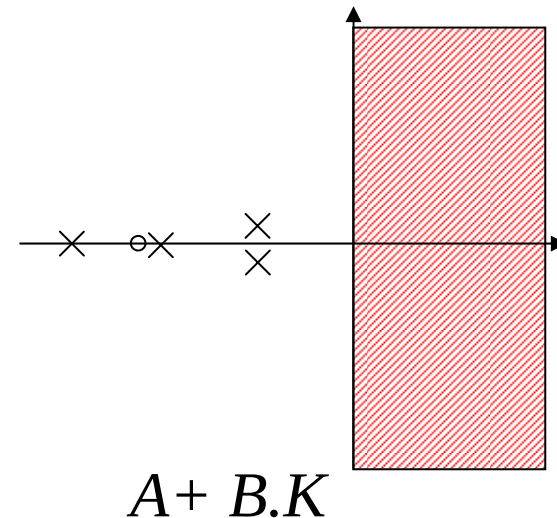
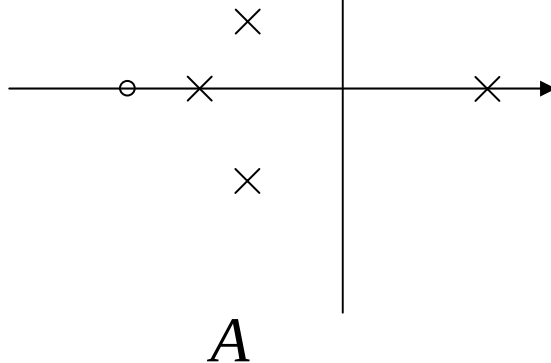
State feedback : change of system dynamics (controllable and observable modes)

$$\frac{dX}{dt} = A.X + B.U$$

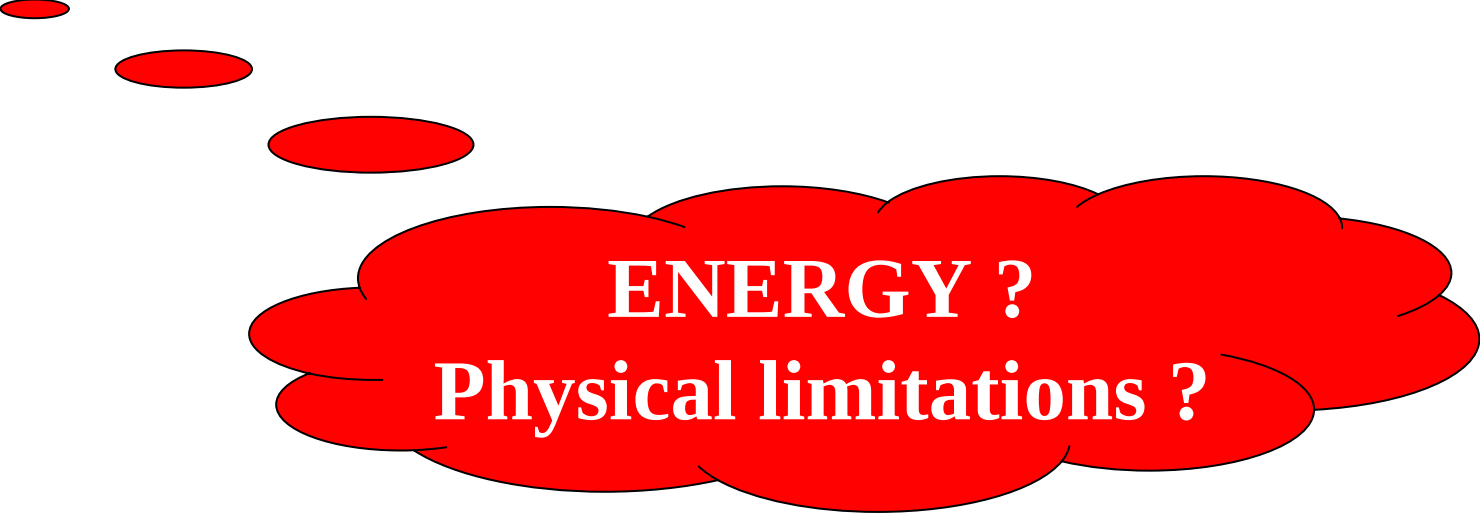
$$U = W + K.X$$



$$\frac{dX}{dt} = \underbrace{(A + B.K)}_{A_K}.X + \underbrace{B.W}_B$$



The system is (completely) controllable at any time t_0 if for any state $X(t_0)$ in the state space Σ and any state X in the state space Σ , there exist a finite time $t_1 > t_0$ and an input $U[t_0, t_1]$ that will transfer the state $X(t_0)$ to the state X at time t_1 .



ENERGY ?
Physical limitations ?

Closed Loop : Stability % Margins

Modulus Margin :

$$\Delta M = |1 + H(j\omega)|_{\min} = |S^{-1}_{yp}(j\omega)|_{\min}$$

Measure of perturbation rejection and robustness of non linearity and time variable parameters

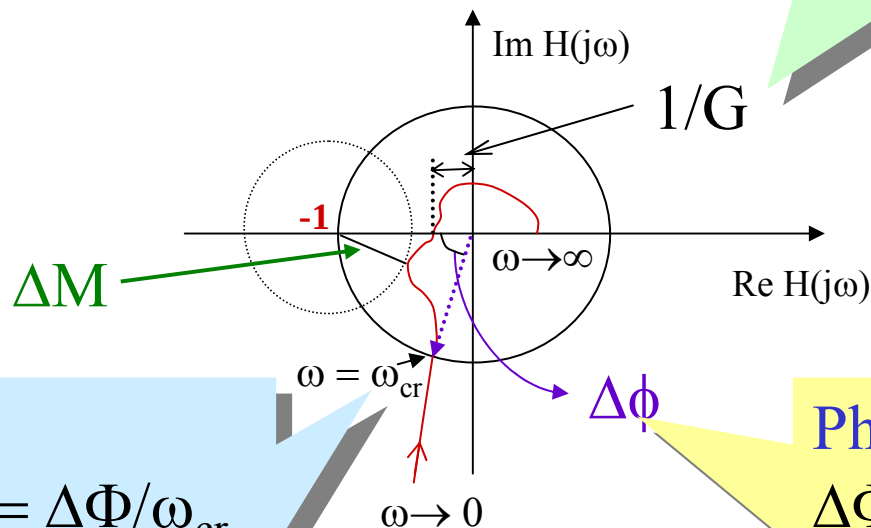
Typical : $\Delta M > 0.5$ (-6dB) [min: 0.4 (-8dB)]

Gain Margin :

$$\Delta G = 1 / |H(j\omega_{180})|$$

for $\Phi(\omega_{180}) = -180^\circ$

Typical : $G > 2$ (6dB) [min: 1.6 (4dB)]



Delay Margin :

$$\Delta \Phi = \omega_0 \cdot \tau ; \Delta \tau = \Delta \Phi / \omega_{cr}$$

additional delay that could be tolerate by the open loop system without instability for the closed loop system

Phase Margin :

$$\Delta \Phi = 180^\circ - \Phi(\omega_{cr})$$

ω_{cr} : crossing pulsation for $|H(j\omega_{cr})| = 1$

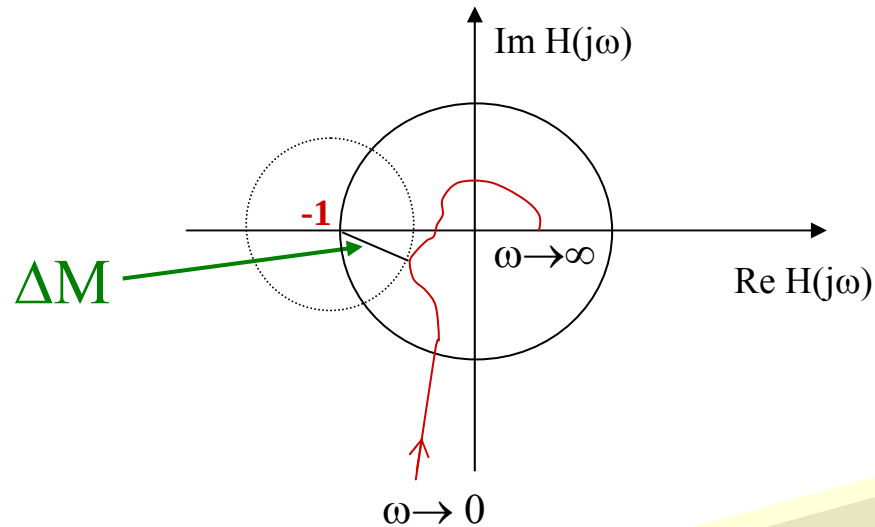
Typical : $30^\circ < \Delta \Phi < 60^\circ$

Modulus Margin :

$$\Delta M = |1 + H(j\omega)|_{\min} = |S^{-1}_{yp}(j\omega)|_{\min}$$

Measure of perturbation rejection and robustness of non linearity and time variable parameters

Typical : $\Delta M > 0.5$ (-6dB) [min: 0.4 (-8dB)]

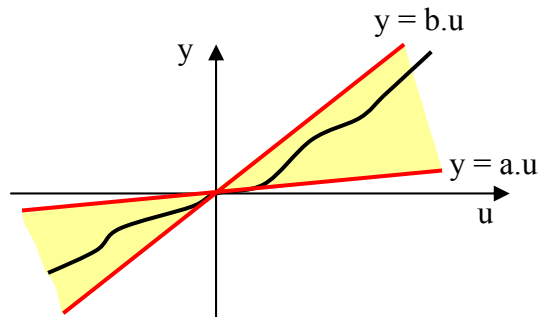
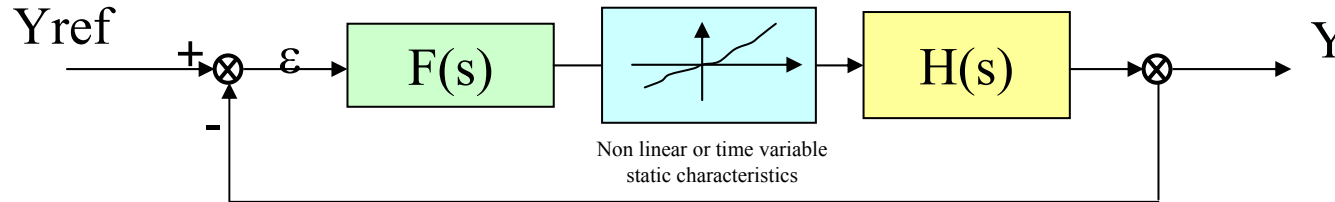


Modulus margin:

$\Delta M > 0.5$ implies a gain margin $\Delta G > 2$ and a phase margin $\Delta \Phi > 30^\circ$.

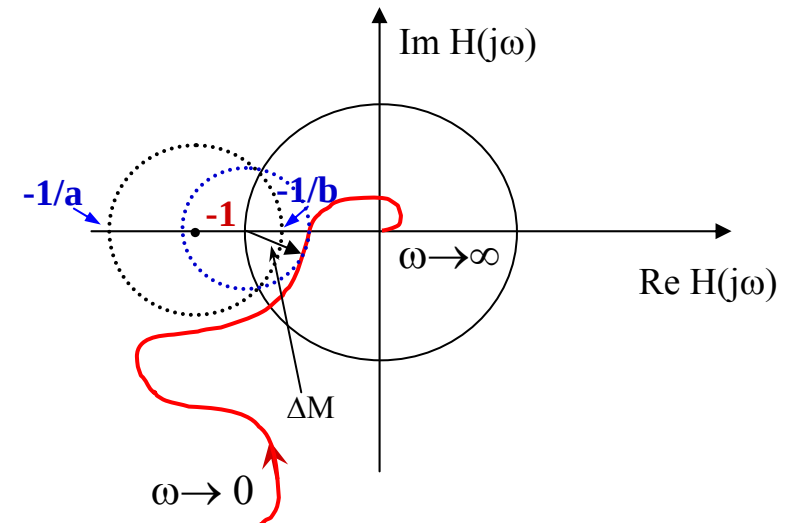
More generally, a good modulus margin guarantees good values for gain and phase margins. The converse is not true.

Robustness of non linearity and time-variable parameters % Modulus Margin



For a given modulus margin ΔM , the system will tolerate non-linear or/and time variable characteristics if these characteristics are located inside the sector defined par a minimum linear gain $1/(1+\Delta M)$ and a maximum linear gain $1/(1-\Delta M)$

If the non-linear and/or time variable characteristics belongs to an angular sector $[a,b]$ ($b>a>0$), the closed-loop system is stable if the Nyquist plot leaves on the left (for $\omega \nearrow$) the "critical" circle with center on the real axis and passing through the points $(-1/b,0)$ and $(-1/a,0)$ (without crossing the circle)



Controller Design

In order to design and tune a controller :

- 1) To specify the desired closed control loop performance
Regulation and tracking : rise time and max overshoot
or bandwidth and resonance
- 2) To choose a suitable controller design method
- 3) To know the dynamic model of the plant to be controlled
=> control model

Control model :

- Non parametric models : e.g. frequency response, step response,...
- Parametric models : e.g. state equation, differential equation, transfer function,,

To get the model :

- knowledge type model (based on the physic laws) ;

Converters : State space average models;
 Equivalent average circuit models

- identification models (from experimental data)



Choice of the desired performance

The choice of desired performance in terms of the response time (bandwidth) is linked to the dynamics of the open-loop system and to the power availability of the actuator during the transient :
acceleration of the natural response requires control peaks that are greater than the steady-state values



$$\begin{aligned} U_{\max}/U_{\text{static}} &\cong \text{desired speed/natural speed} \\ &\cong \text{desired bandwidth / natural bandwidth} \\ &\cong f_{\text{B}}^{\text{CL}} / f_{\text{B}}^{\text{OL}} \end{aligned}$$

Or, the actuators will have to be chosen as a function of the desired performance and the open-loop response of the system

Choice of the desired performance (cont'd)

**The robustness of the closed-loop system
is linked to the ratio $f_{\text{B}}^{\text{CL}} / f_{\text{B}}^{\text{OL}}$**
(sensitivity to the uncertainty
or variation of the model parameters)

**If the ratio is too high => bad robustness and
need to have a good knowledge of the process
model (high frequency identification)
or use of adaptive control**

LHC orbit corrector

$[\pm 60\text{A}, \pm 8\text{V}]$ (arc corrector)

Magnet : $L=7\text{ H}$; $R = 30\text{ m}\Omega$ (60m of 35 mm^2)

$$\mathbf{T = L/R = 300\text{ s} \Rightarrow f_{\text{OL}_B}^{\text{OL}} \cong 0.5\text{ mHz}}$$

$$\mathbf{U_{\text{static}} = R.I = 1.8\text{V}}$$

$$\mathbf{\text{Large signal : } u_{\text{max}}/u_{\text{static}} \cong 4 \Rightarrow f_{\text{CL}_B}^{\text{CL}} \cong 2\text{ mHz} \Rightarrow t_R = 175\text{ s}}$$

$(dI/dt_{\text{max}} \cong 1\text{A/s})$

$$\mathbf{\text{Small signal : } f_{\text{CL}_B}^{\text{CL}} \cong 1\text{ Hz} \Rightarrow u_{\text{max}}/u_{\text{stat}} \cong 1/0.5 \cdot 10^{-3} = 2000 !}$$

$$\mathbf{\text{Then } u_{\text{static}} = 6 / 2000 = 3\text{mV} \Rightarrow \Delta I = 3\text{mV}/30\text{ m}\Omega = 0.1\text{ A} = 0.15\text{ \% } I_{\text{max}}}$$

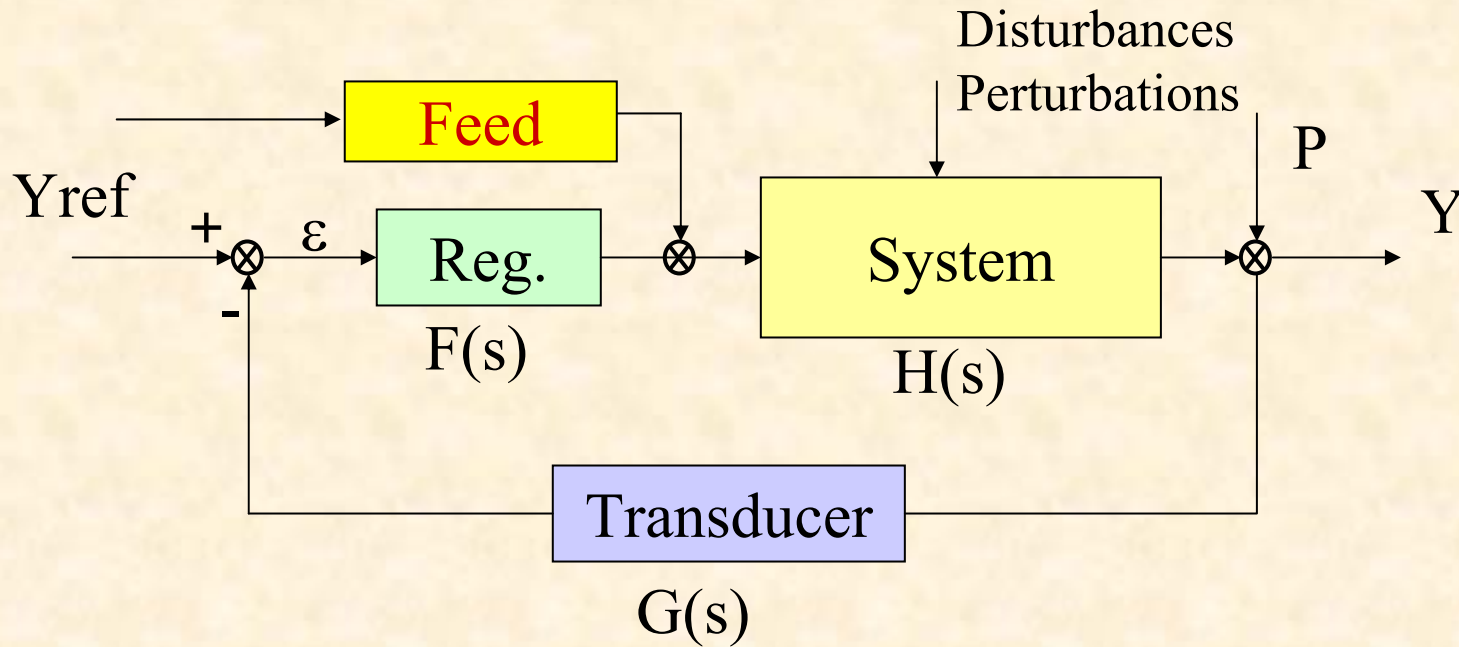
“The power converters involved in feedback of the local orbit may need to deal with correction rates between 10 and 500 Hz”;

$$f_s (\text{rate ?}) = 500\text{ Hz} \Rightarrow f_{\text{CL}_B}^{\text{CL}} \cong 50\text{Hz} (\Delta I = 1\text{ \% } : U_{\text{max}} = 2400\text{ V} \text{ ?????...})$$

$$(U_{\text{max}} = 8\text{V} \Rightarrow \Delta I = 30\text{ ppm } I_{\text{max}})$$



Analogue Control Systems

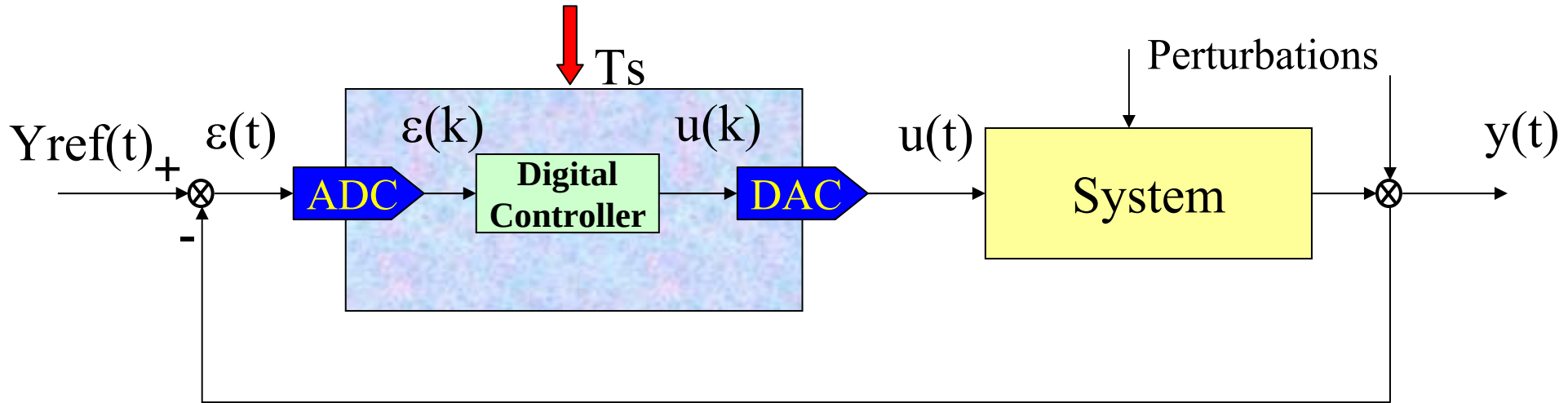


Open loop : system $H(s)$; system with controller $F(s).H(s)$

Closed loop : $H_{CL}(s) = F(s).H(s) / [1 + F(s). H(s) G(s)]$

Digital control systems

Digital realisation of an “analogue type” controller

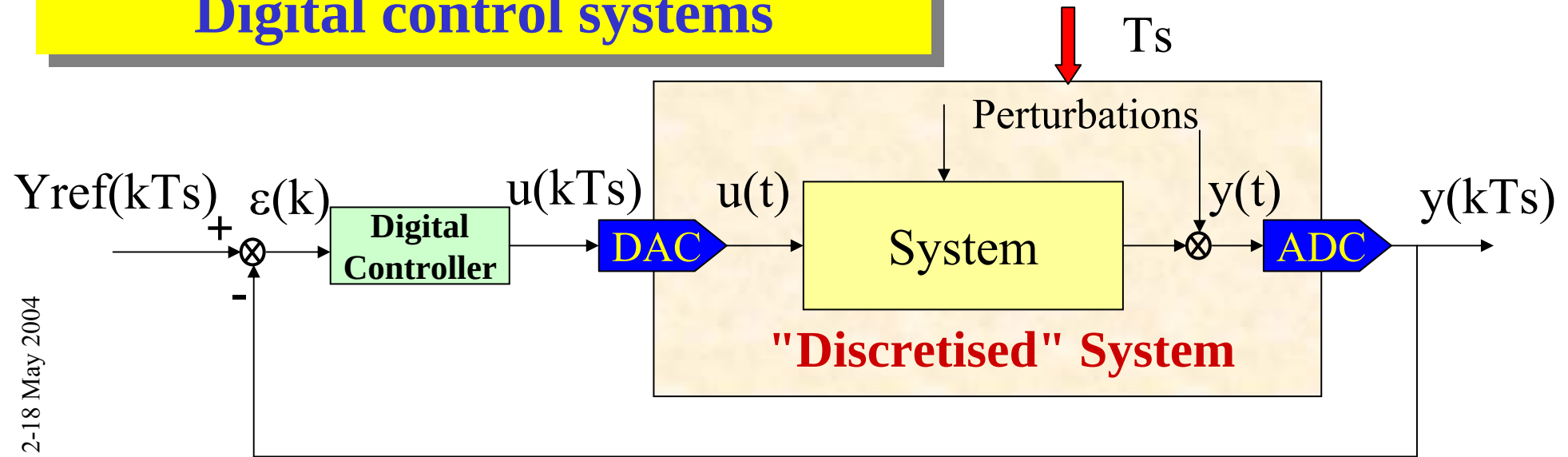


ADC- Digital controller - DAC should behave the same as an analogue controller (e.g. PID type), which implies **the use of a high sampling frequency** (the algorithm implemented is very simple)

Bad use of the potentialities of the digital controller

"It's not enough to put a tiger in your tank,
you've got to add BRAIN"

Digital control systems



The sampling frequency is chosen in accordance with the bandwidth desired for the closed-loop system

Intelligent use of the “computer” : high sampling period and then implementation of complex algorithms requiring greater computation time.

Not only a copy of analogue control : BRAINWARE

**Discrete-time system models
and
digital control algorithms**

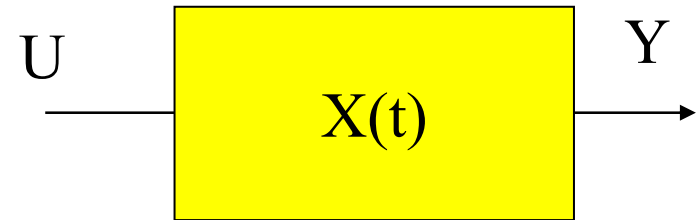
$$y(k) = f[y(k-i), u(k-j)]$$

or

$$H(z^{-1}) = z^{-d} B(z^{-1})/A(z^{-1})$$

$$\frac{dX}{dt}(t) = A.X(t) + B.U(t)$$

$$Y(t) = C.X(t) + D.U(t)$$



T_s : sampling period

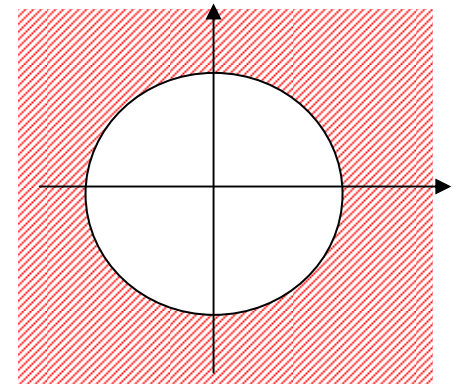
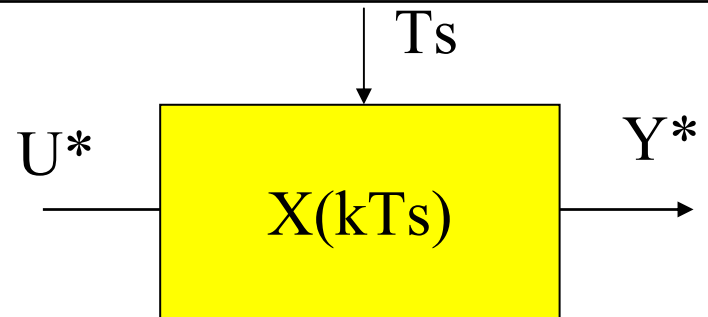
$$X[(k+1)T_s] = F.X(kT_s) + G.U(kT_s)$$

$$Y(kT_s) = C.X(kT_s) + D.U(kT_s)$$

$$F = e^{A.T_s}$$

$$G = A^{-1} \cdot (e^{A.T_s} - I) \cdot B$$

$$X[(k_0 + n)T_s] = \underbrace{F^n \cdot X(k_0 T_s)}_{\text{Free state response}} + \sum_{j=1}^n \underbrace{F^{n-j} G \cdot U[(k_0 + j - 1)T_s]}_{\text{Forced state response}}$$



Stability of the system:

$$\lim_{n \rightarrow \infty} F^n \cdot X(k_0 T_s) = 0$$

F eigenvalues modulus must be lower than 1

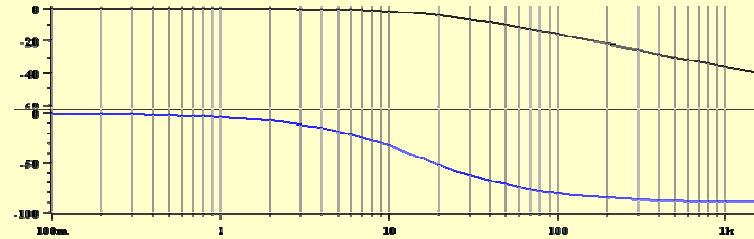
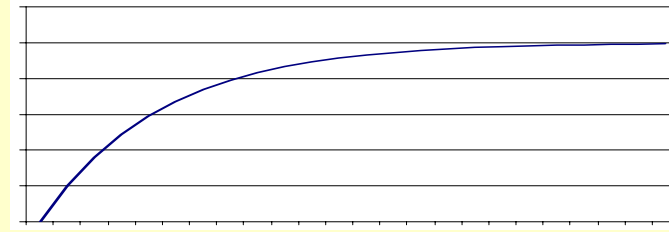
First order system

Analogue world

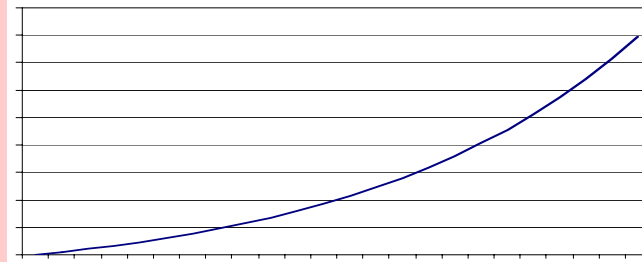
$$\frac{dy}{dt}(t) = -\frac{1}{T} \cdot y(t) + \frac{G}{T} \cdot u(t)$$

$$H(s) = \frac{G}{1 + sT}$$

$T > 0$



$T < 0$



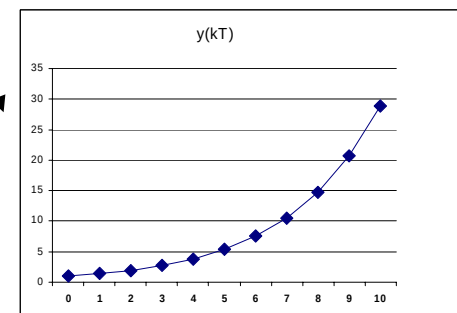
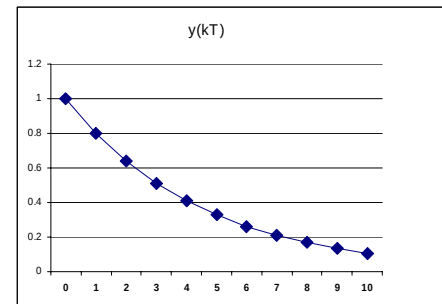
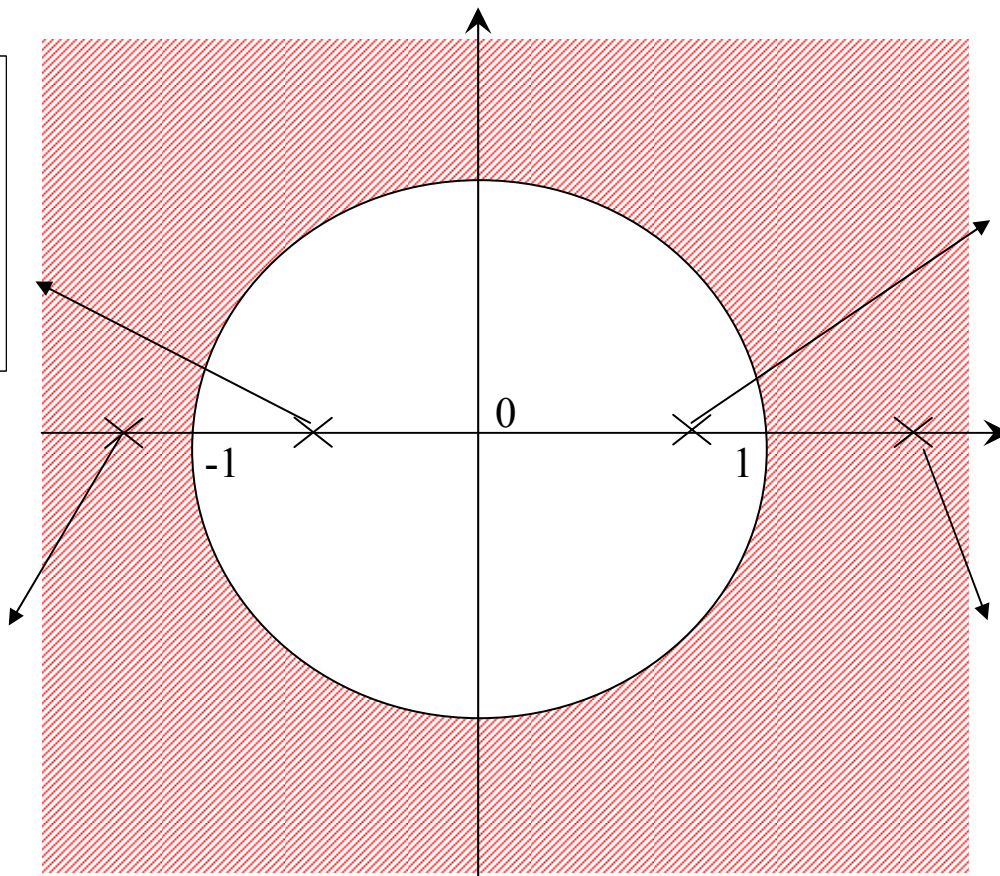
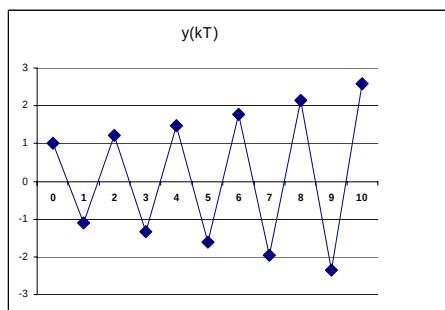
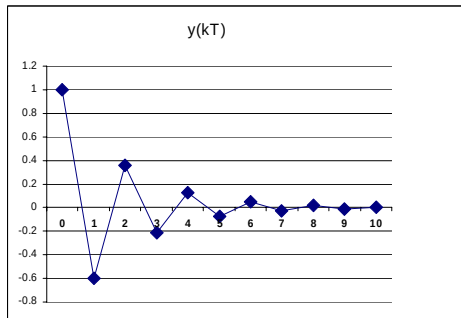
Discrete world

$$y(kTs) = -a_1 \cdot y[(k-1)Ts] + b_1 \cdot U[(k-1)Ts]$$

$$H(z) = \frac{b_1}{z + a_1} = \frac{b_1 z^{-1}}{1 + a_1 z^{-1}}$$

Digital first order system

$$H(z) = \frac{b_1}{z + a_1} = \frac{b_1 z^{-1}}{1 + a_1 z^{-1}}$$

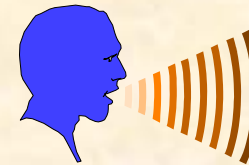


Free state response

Choice of sampling frequency

$$f_s = 1/T_s = (6 \text{ to } 25) * f_{CL_B}^{CL}$$

f_s : sampling frequency

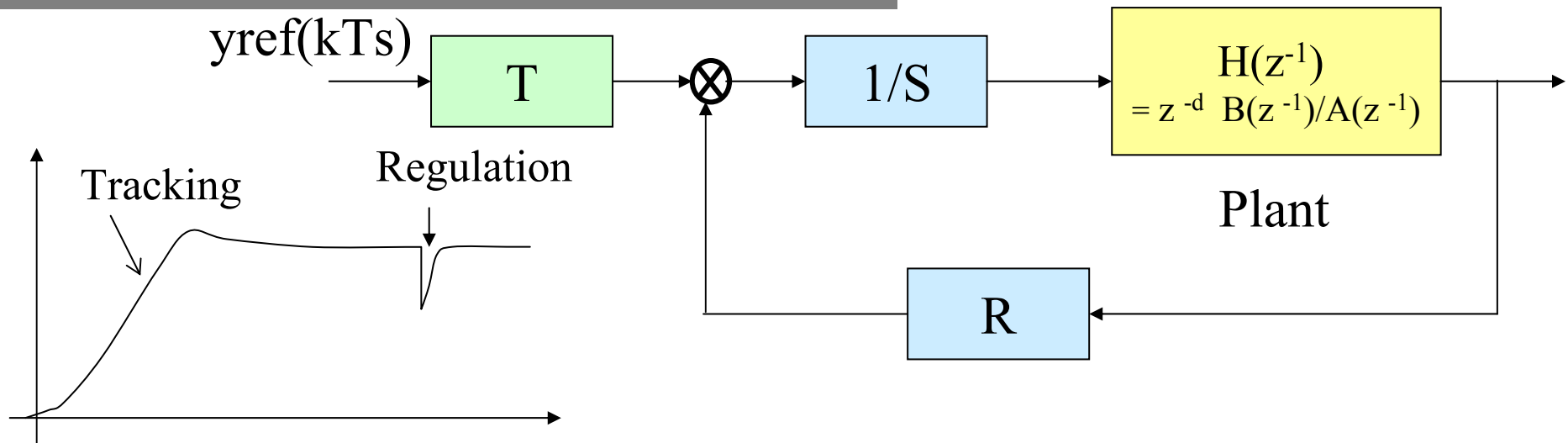


No more

$f_{CL_B}^{CL}$: bandwidth of the closed-loop system

If f_s is fixed $\Rightarrow$ limit for $f_{CL_B}^{CL}$ ($< f_s / 15$)

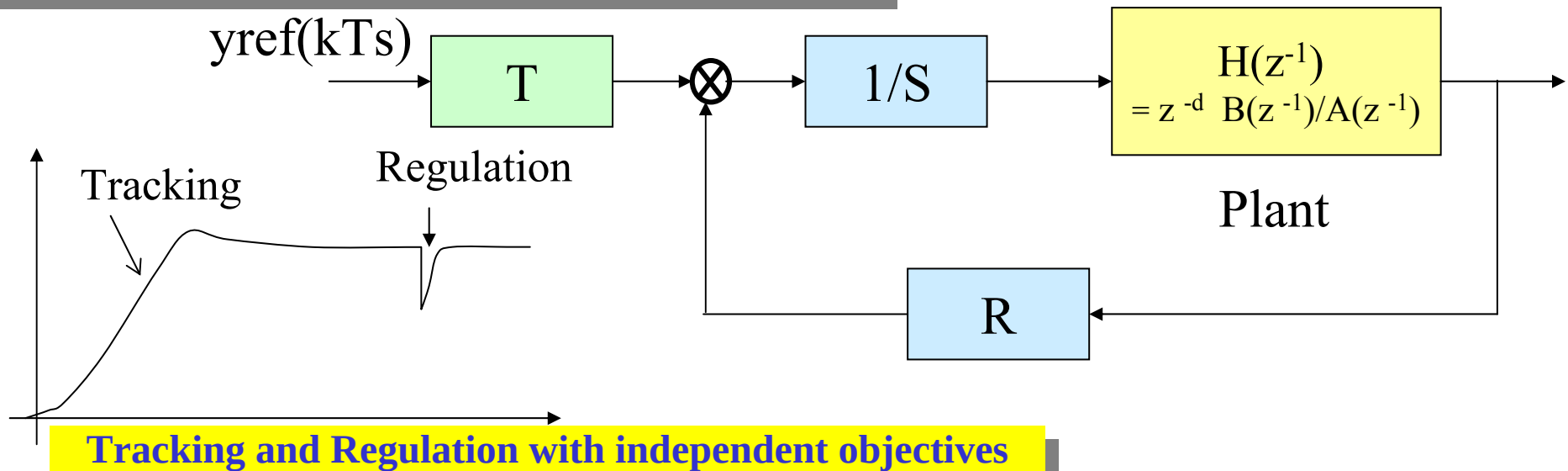
R.S.T control : generic control



RST :

- minimum variance tracking and regulation
- tracking and regulation with weighed input
- tracking and regulation with independent objectives,...

R.S.T control : generic control



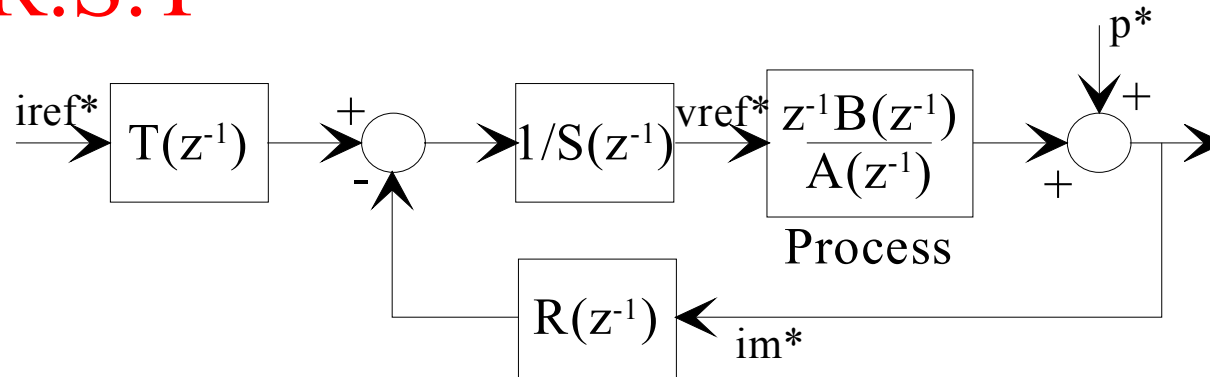
This control strategy permits a R.S.T digital controller to be designed for both stable and unstable systems:

- without restriction on the degrees of the polynomials $A(z^{-1})$ and $B(z^{-1})$ of the plant transfer function
- without restriction on the sampled time delay of the system (d)

This strategy can only be applied to discrete-time models with stable zeroes (minimum phase systems):

- high sampling period $\Rightarrow$ unstable zeroes
- fractional time delay $> 0.5 \times Ts$

R.S.T



Tracking:

$$\frac{im^*}{iref^*} = \frac{z^{-1}.B.T}{A.S + R.B.z^{-1}}$$

Regulation:

$$\frac{im^*}{p^*} = \frac{A.S}{A.S + R.B.z^{-1}}$$

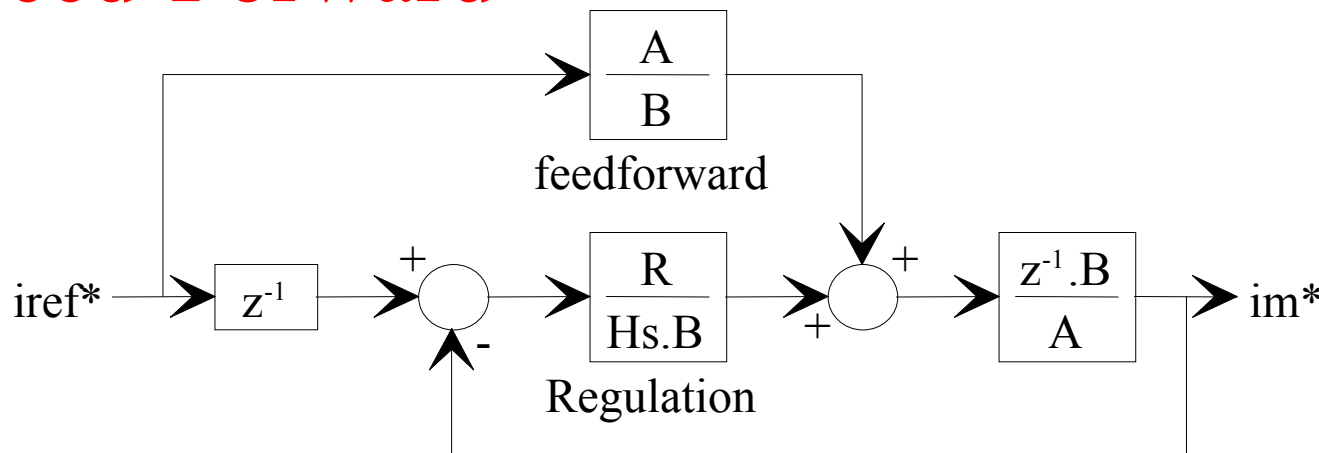


Tracking and Regulation
With Independent Objectives

$$S = B . Hs$$

$$T = A . Hs + z^{-1} . R$$

Feed-Forward



$$\frac{Im^*}{Iref^*} = z^{-1}$$

$$\frac{Im^*}{p^*} = \frac{A.Hs}{A.Hs + R.z^{-1}}$$

Time delay : 1st order system example

$$H(s) = G / (1 + T.s) \quad \Rightarrow \quad H(z^{-1}) = b_1 z^{-1} / (1 + a_1 z^{-1})$$

with $a_1 = -e^{-T_s/T}$; $b_1 = G.(1 - e^{-T_s/T})$

$$H(s) = G e^{-s\tau} / (1 + T.s) \quad \tau : \text{time delay}$$

T_s : sampling period

$$\tau = d. T_s + L \quad ; \quad 0 < L < T_s \quad \text{fractional time delay}$$

$$H(z^{-1}) = z^{-d} (b_1 z^{-1} + b_2 z^{-2}) / (1 + a_1 z^{-1})$$
$$= z^{-d-1} (b_1 + b_2 z^{-1}) / (1 + a_1 z^{-1})$$

$$\text{with } a_1 = -e^{-T_s/T} \quad ; \quad b_1 = G(1 - e^{(L-T_s)/T}) \quad ; \quad b_2 = G e^{-T_s/T} (e^{L/T} - 1)$$

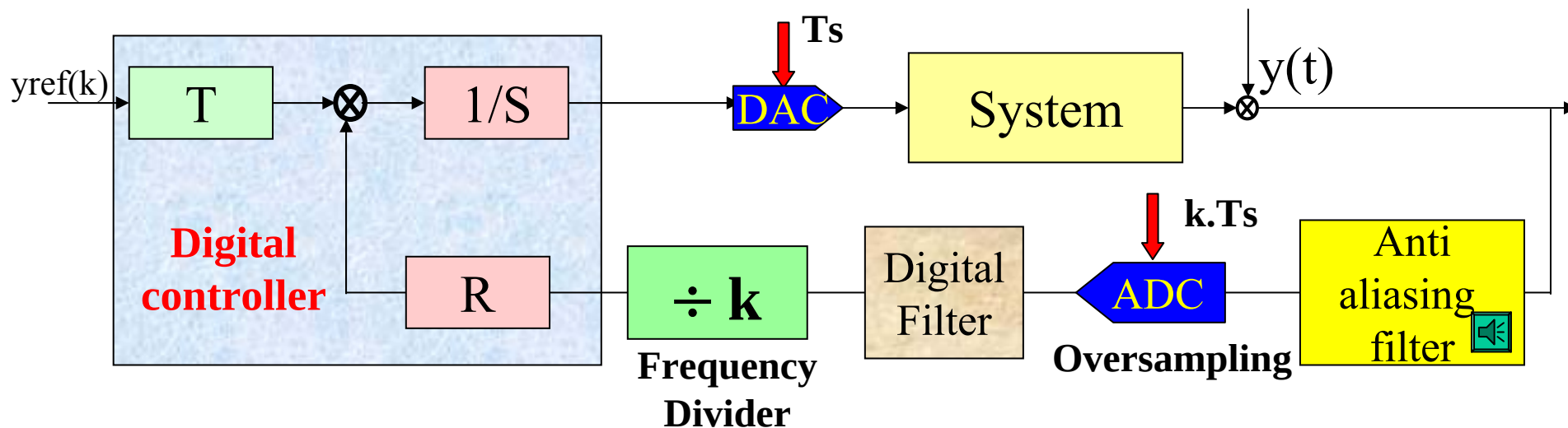
fractional time delay $\Rightarrow$ introduction of a zero in the discrete transfer function (if $L = 0 \Rightarrow b_2 = 0$)

If $L > 0.5$: $|b_2| > |b_1| \Rightarrow$ unstable zeroes

No problem on the system stability but limitation on the possible method to compute the regulator



Summary



Based on f_B^{OL} and power of the actuator : choice of the closed-loop performance [$f_B^{CL}(t_r)$ and $Q(M)$]

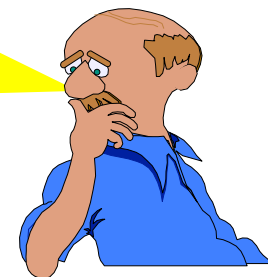
Robustness $\propto f_B^{CL} / f_B^{OL}$ (Internal saturation : controllability)

f_s (sampling frequency) : choice based on the f_B^{CL}

$$f_s = 1/T_s = (6 \text{ to } 25) * f_B^{CL}$$

Discrete model $H(z^{-1})$ at T_s

System model ?
 $f_B^{CL}(t_r)$, $Q(M)$?
 T_s ?

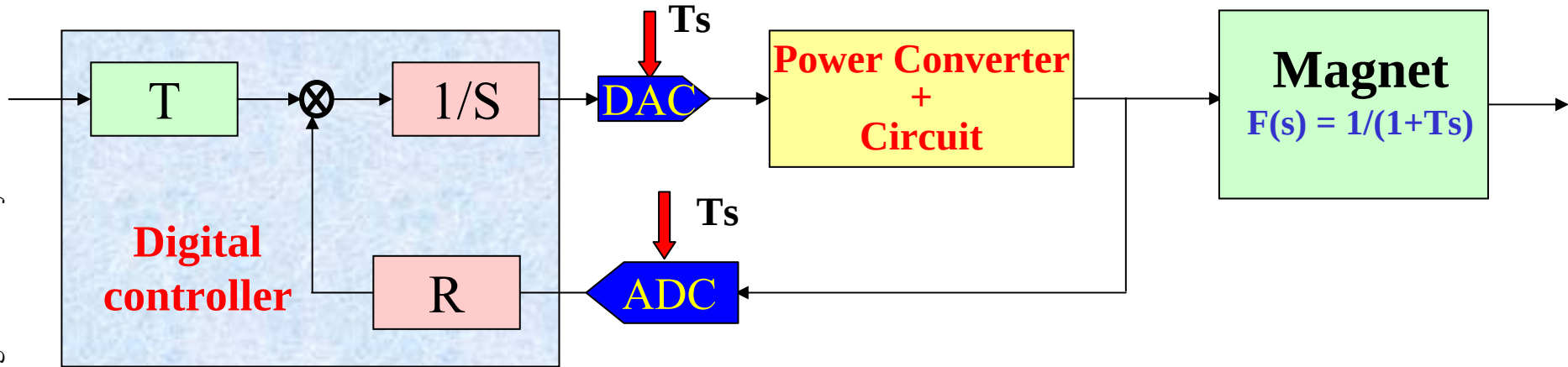


Tracking : dynamics

I^*_{ref}

I

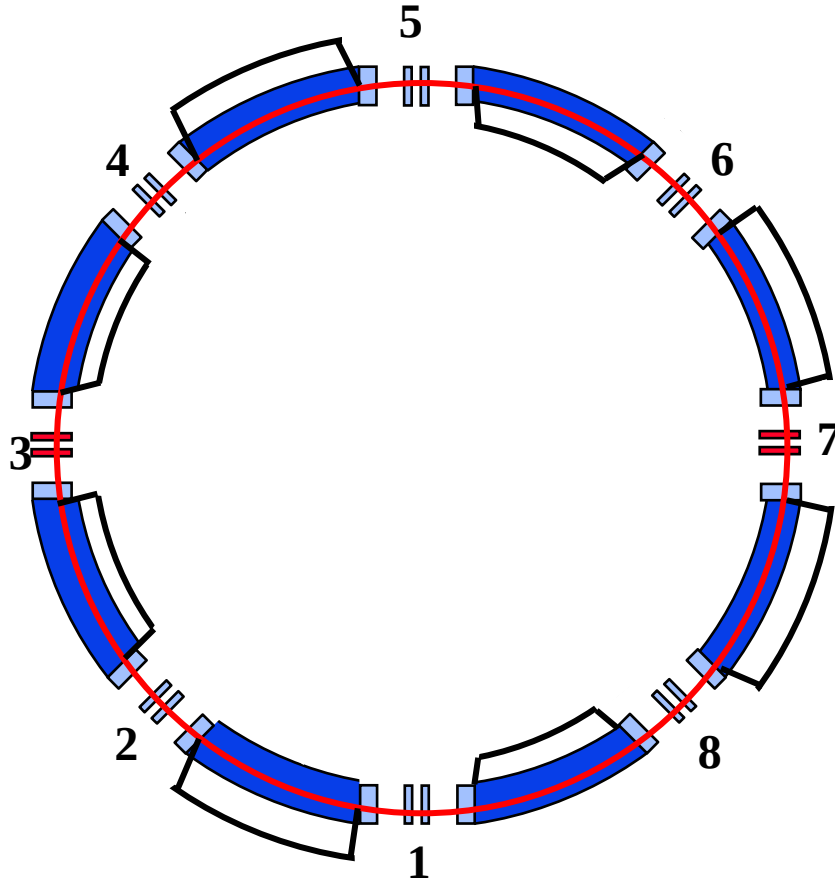
B



Dynamics :

- **Measurement and command must be synchronised : timing system**
- **Lagging error :**
 - # $I_{ref} \Rightarrow I$: regulation loop could be designed with no lagging error independent of the load time constant
 - # $I \Rightarrow B$: time constant (T : vacuum chamber, beam screen...) must be known : Measurement campaign in collaboration with magnet specialists

Tracking between the 8 main dipole converters



20 ppm Accuracy

$$\Delta B/B_{\text{nom}} = \Delta I/I_{\text{nom}} = 20\text{ppm}$$

$$\Delta B = 9 * 20 \cdot 10^{-6} = 1.8 \cdot 10^{-4} \text{ T}$$

$$\Delta B/B_0 = 3.3 \cdot 10^{-4}$$

Orbit excursion :

$$\delta X = D_x \cdot \Delta B/B_0 = \sim 0.7 \text{ mm}$$

**Could be corrected with a pilot run
and new cycle => reproducibility**

10 ppm reproducibility

Orbit excursion :

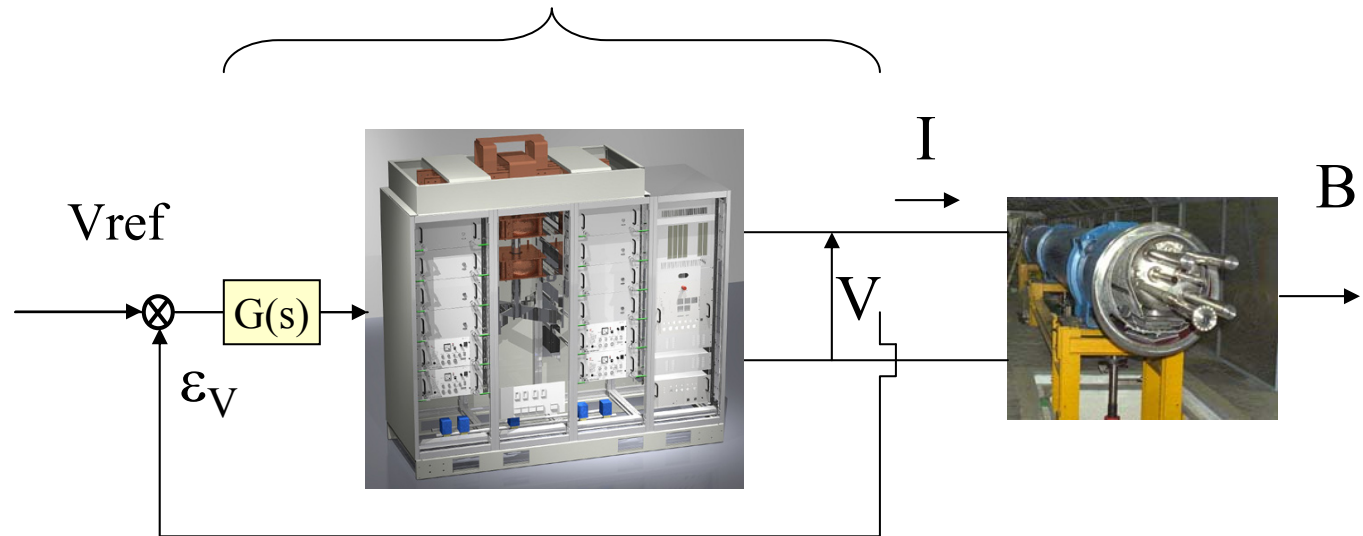
$$\delta X = D_x \cdot \Delta B/B_0 = \sim 0.35 \text{ mm !!!}$$

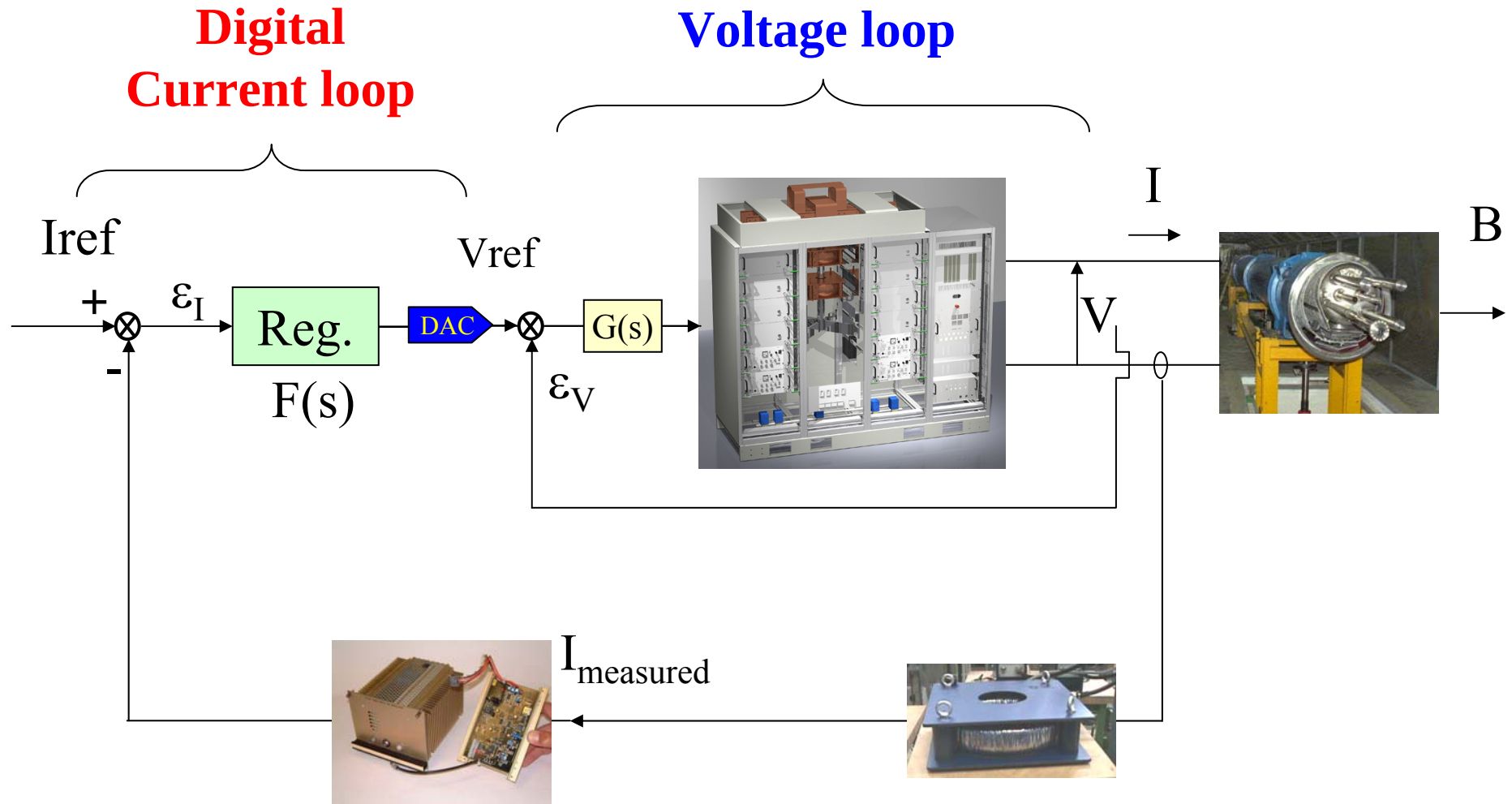
”It would be better with 5 ppm”

Example :LHC power converter control

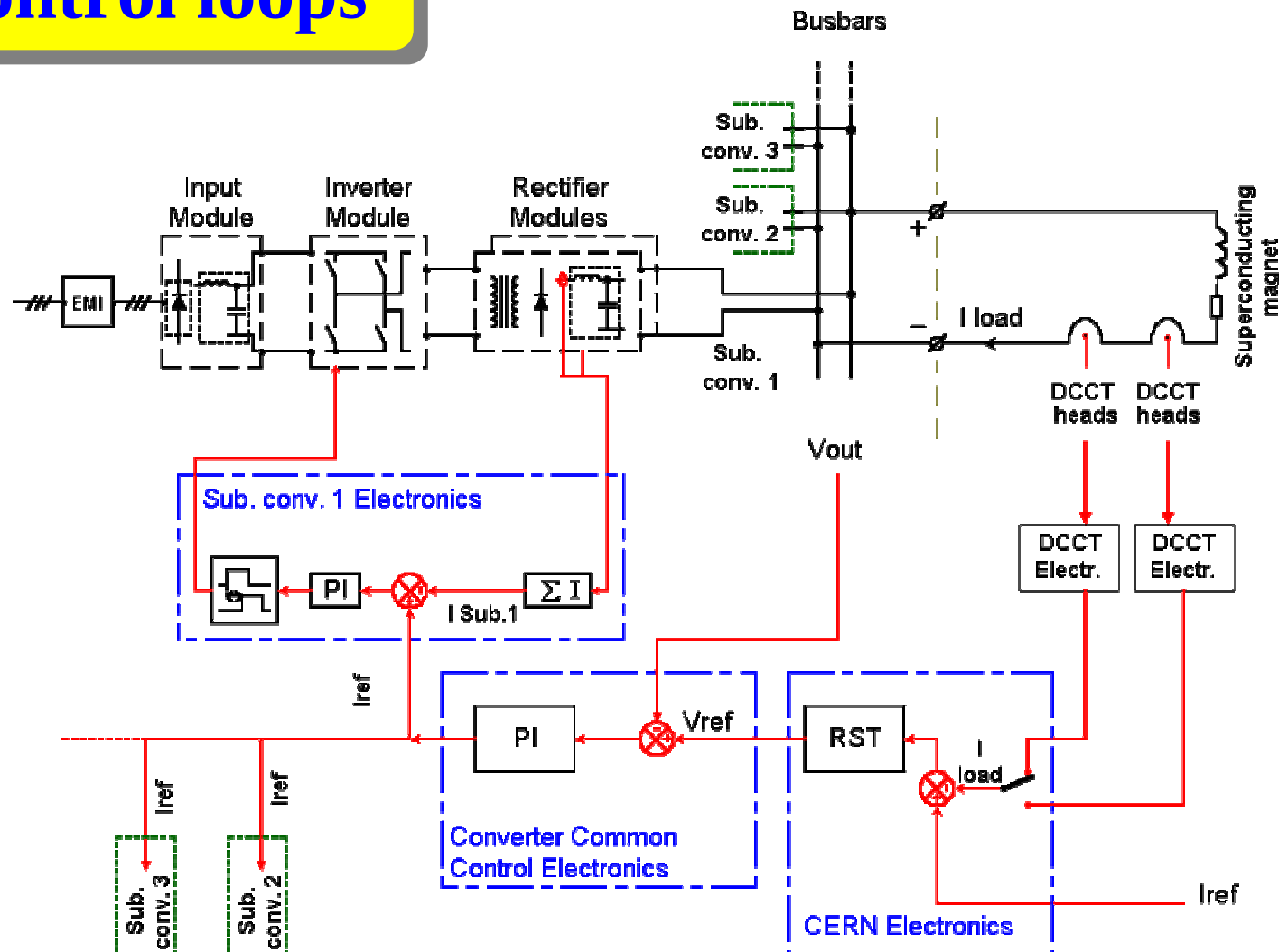
Global Voltage loop

Internal loops





Control loops



1- Fast internal current source

2- Global voltage loop

3- High precision current loop (DCCT)

$F_{CL_B} \sim 8 \text{ kHz}$

$F_{CL_B} \sim 700 \text{ Hz}$

$F_{CL_B} \sim 0.1 - 1 \text{ Hz}$

Digital controller



High precision 13kA DCCT

Connection rack



• **Very high performance is needed for the 24 main circuits: 8 main dipole and 16 main quadrupole (F and D) circuits.**

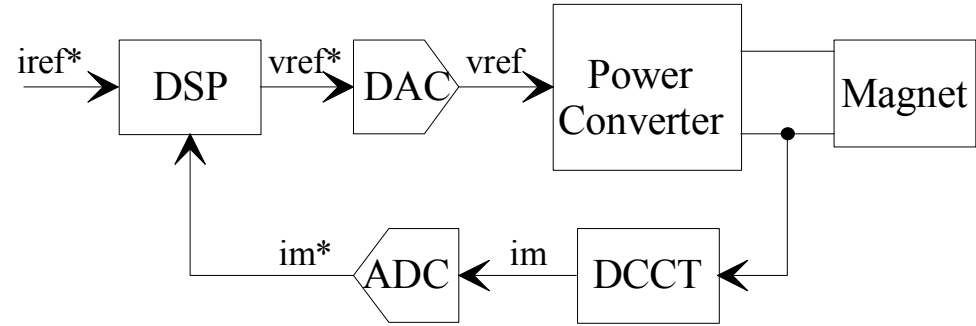
- ✓ **Short term stability (30 mins) : ± 3 ppm**
- ✓ **Reproducibility (24 hours) : ± 5 ppm**
- ✓ **Accuracy (1 year) : ± 20 ppm**

1 ppm = 1 part per million = 0.0001%
For main circuits 1 ppm = 13 mA

- ✓ **no overshoot**
- ✓ **no lagging error**



Power Converter Digital Loop



SYSTEM MODEL

The power converter (PC) with the voltage loop can be modelled by a second order system with two complex poles and a natural frequency equal to $\omega_{pc}=6,28\text{krad/s}$. The magnet model is a first order system with a high time-constant ($\tau_m=L_m/R_m=23\text{ks}$ for the main dipole circuits and $\tau_m=450\text{s}$ for the quadrupole circuits). If **the sampling period of the digital loop is high in comparison with the time-constant of the power converter** ($T_s > 10/\omega_{pc}$), the converter model can be reduced to a simple gain G_{PC} . Then the discrete model of the system is:

$$\frac{im^*}{vref^*} = \frac{G_{pc} \cdot 1/rm \cdot (1 - e^{-T_s/\tau_m}) \cdot z^{-1}}{1 - e^{-T_s/\tau_m} \cdot z^{-1}} \quad (1)$$

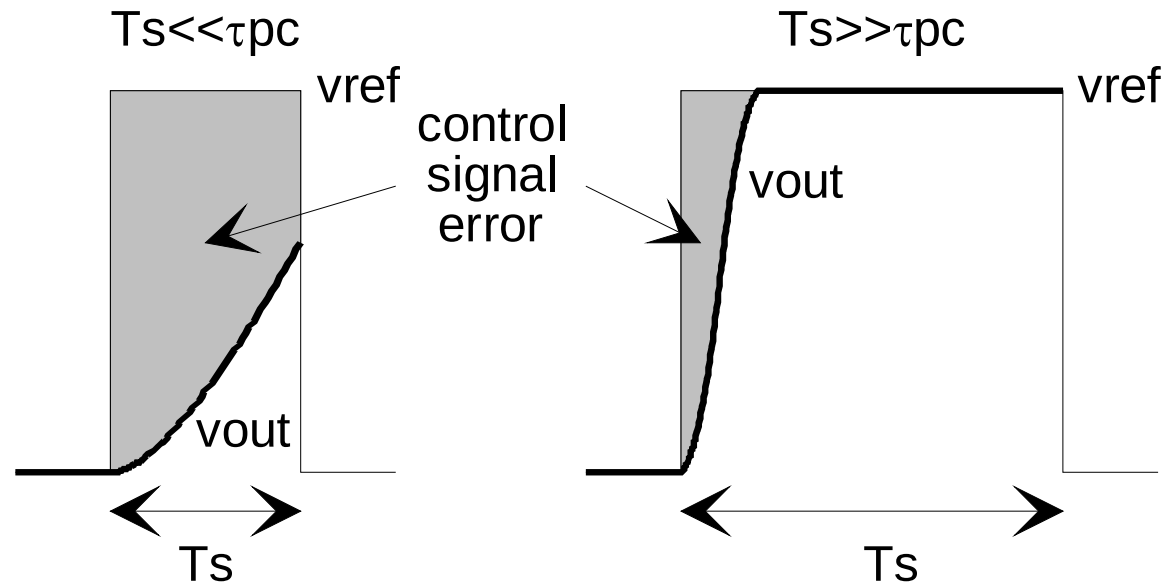
Furthermore, in the case of a high time-constant of the magnet in relation with the sampling period the equation (1) becomes:

$$\frac{im^*}{vref^*} \approx \frac{G_{pc} \cdot T_s / L_m \cdot z^{-1}}{1 - z^{-1}} \quad (2)$$

With the preceding assumptions, the system (power converter and magnet) can be considered, by the digital control, as a pure integrator.

$$F_B^{cl} \approx 1\text{Hz} \Rightarrow F_s \approx 10\text{Hz}$$

The sampling period (T_s) must be high in comparison with the converter time-constant: $T_s \gg \tau_{pc} = 1/\omega_{pc}$.

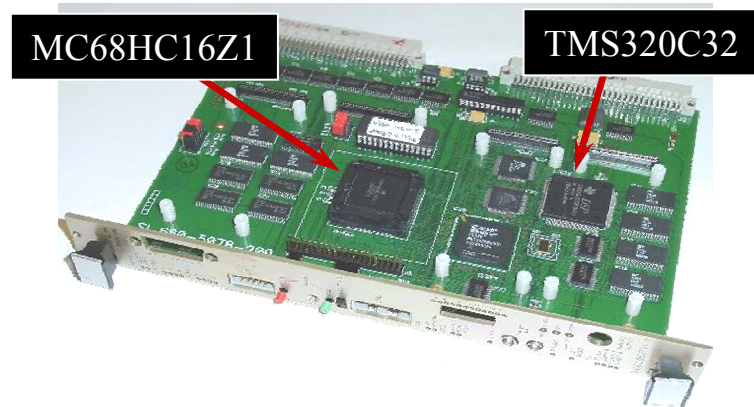


$$F_{pc} \approx 1\text{kHz} ;$$

(if $F_s \rightarrow 1\text{kHz}$ need to include the digital model of the voltage source)

Once again : not to chose T_s too small !!!!.... no copy of analogue world

RST CONTROLLER DESIGN



Tracking:

To get a good tracking of the reference (no lagging error, no overshoot), the transfer function that the controller must achieve between the reference i_{ref}^* and the output i_m^* is:

$$\frac{i_m^*}{i_{ref}^*} = z^{-1}$$

Regulation:

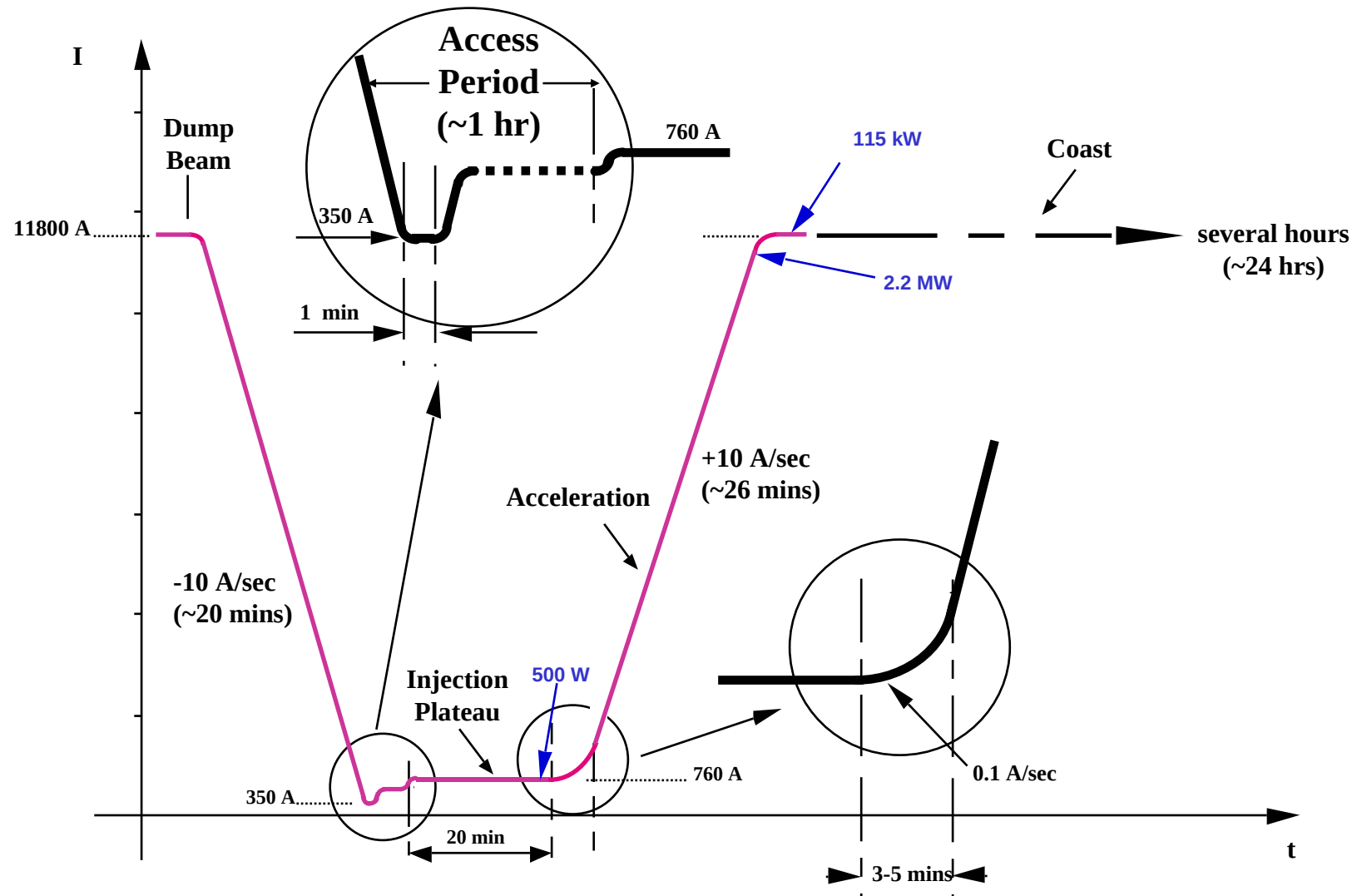
According to the LHC cycle, the bandwidth for the closed-loop system is chosen $f_b^{CL} \in [0.1\text{Hz}, 1\text{Hz}]$. The regulation is defined by the pole placement with a natural frequency $\omega_{cl} \in [0.628\text{rad/s}, 6.28\text{rad/s}]$ and with a damping factor greater than 1. To ensure a zero steady-state error when the reference is constant, the transfer function $1/S(z^{-1})$ must contain two integrators .

$$(1 - z^{-1})^2$$

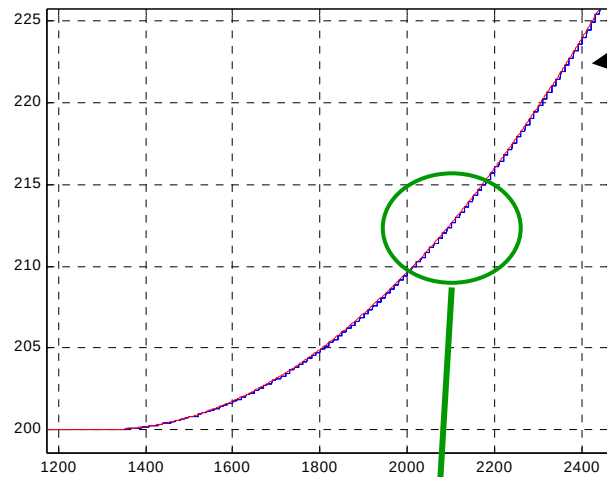
Power Converters for Particle Accelerators – Warrington 12-18 May 2004



Main Dipole Current Cycle



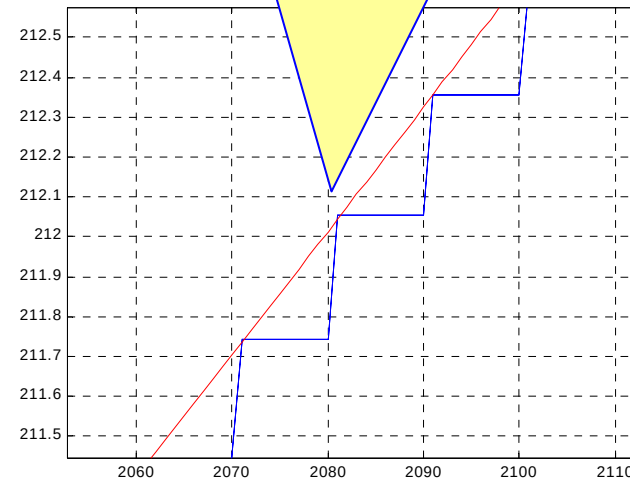
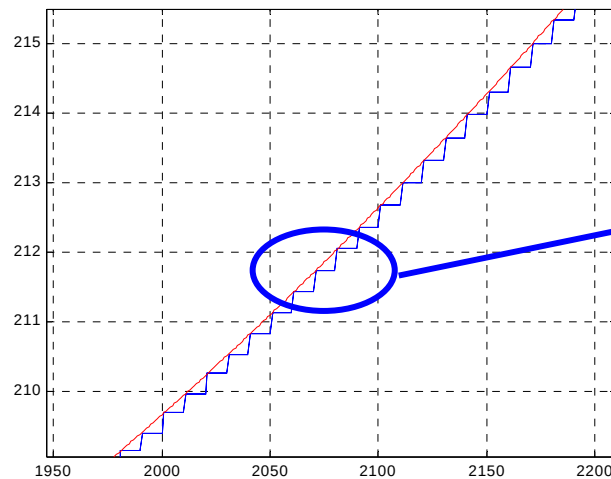
Start of the ramp (from 200 A to 225 A)



$dI/dt = 50 \text{ A/s}$

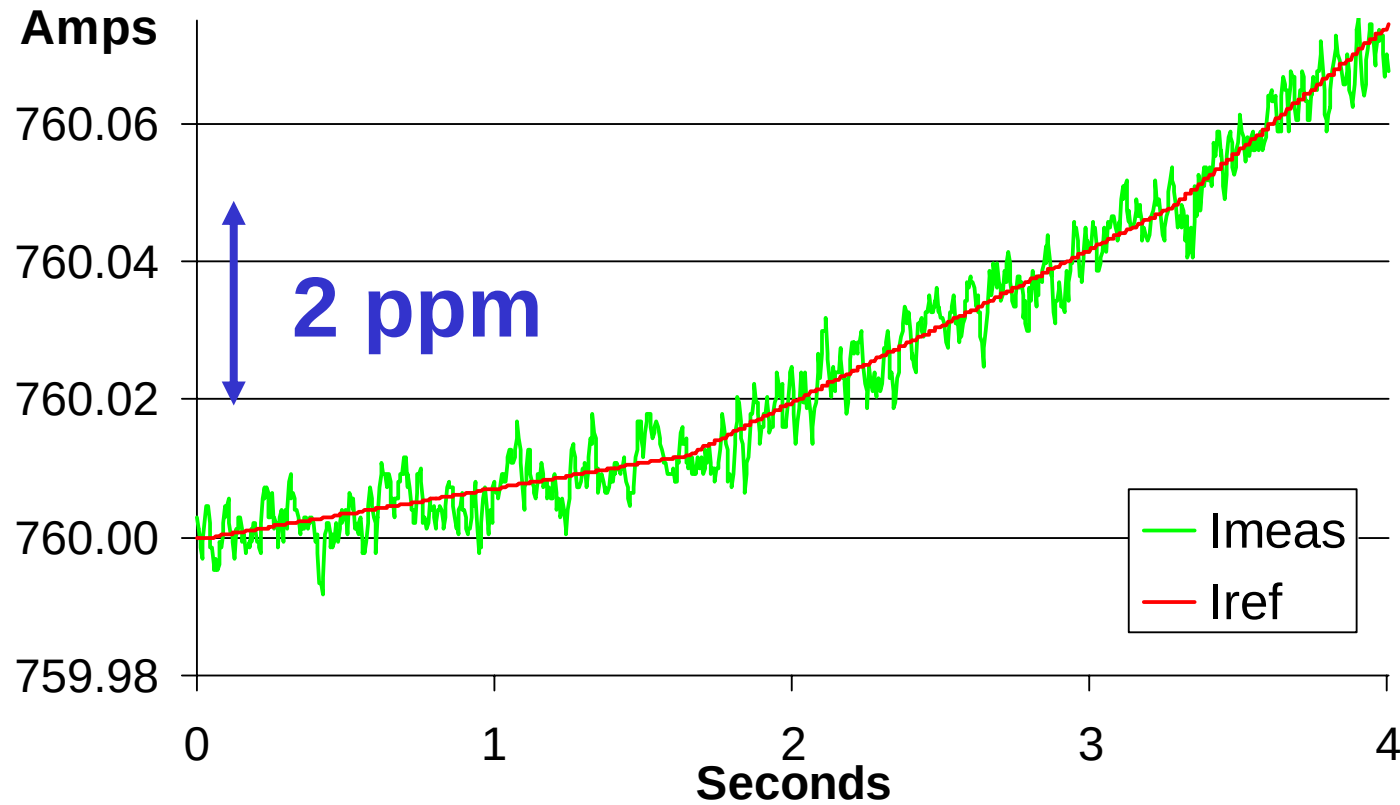
— I_{ref}
— ADC

No lagging error !

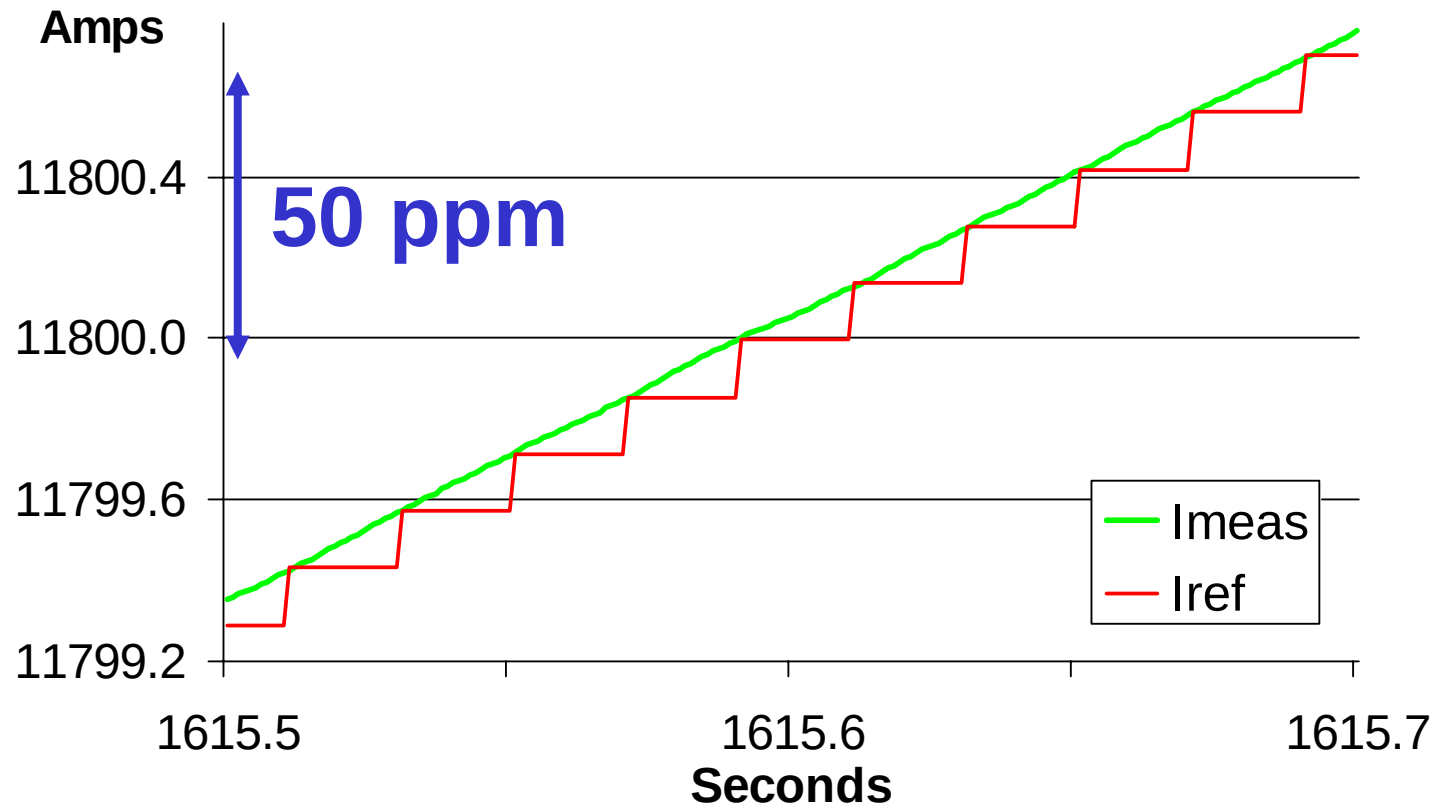


10 ms

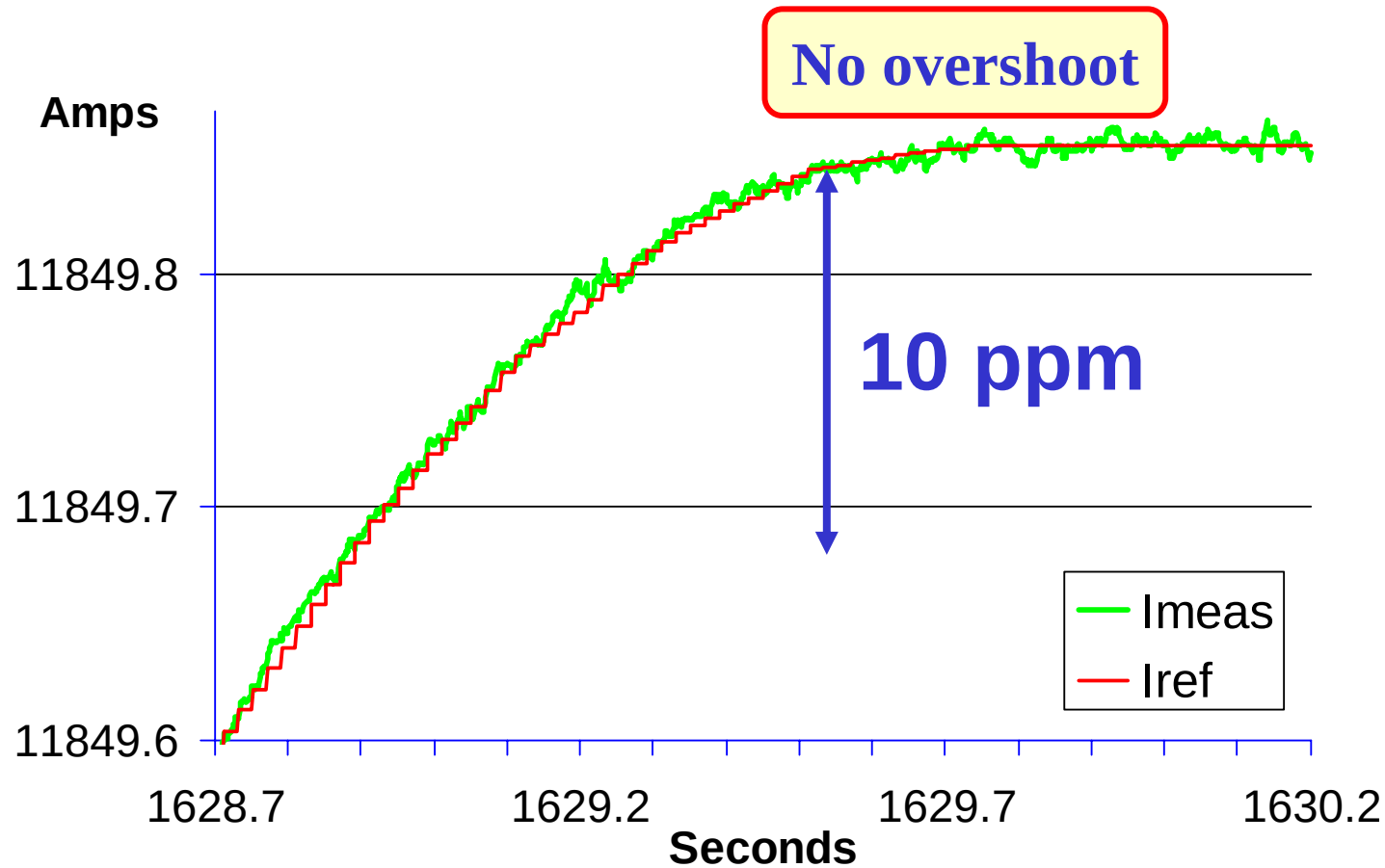
String 2 dipole circuit ramp (0-4s)



String 2 dipole circuit ramp (200ms)



String 2 dipole circuit ramp (last 1 s)



Multi Input and Multi Output Systems (MIMO)

Example : LHC Inner triplet powering

MIMO system => SISO system

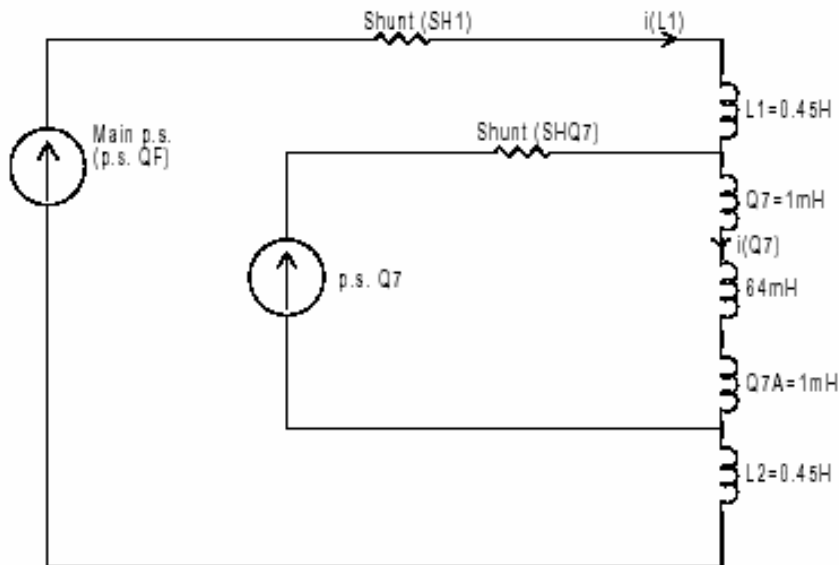


Figure: 1 Single Shunt P.S. Model

RHIC INSERTION REGION SHUNT POWER SUPPLY

(D. Bruno's paper at PAC'99)

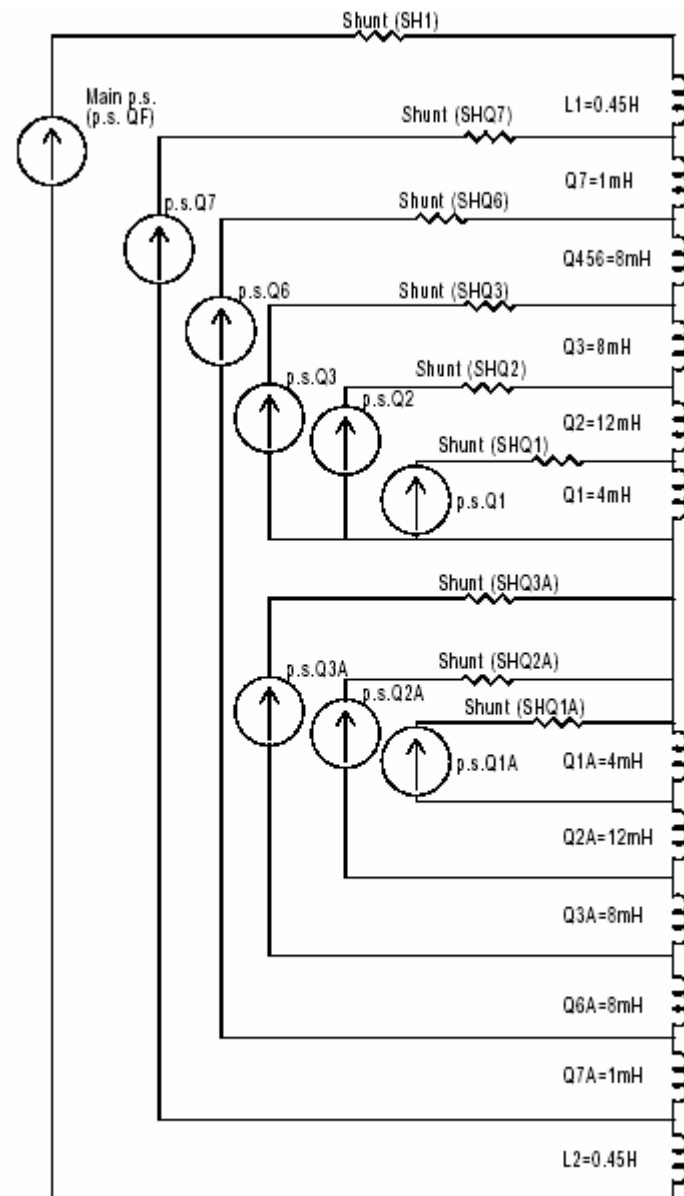
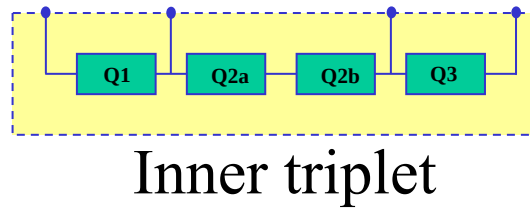
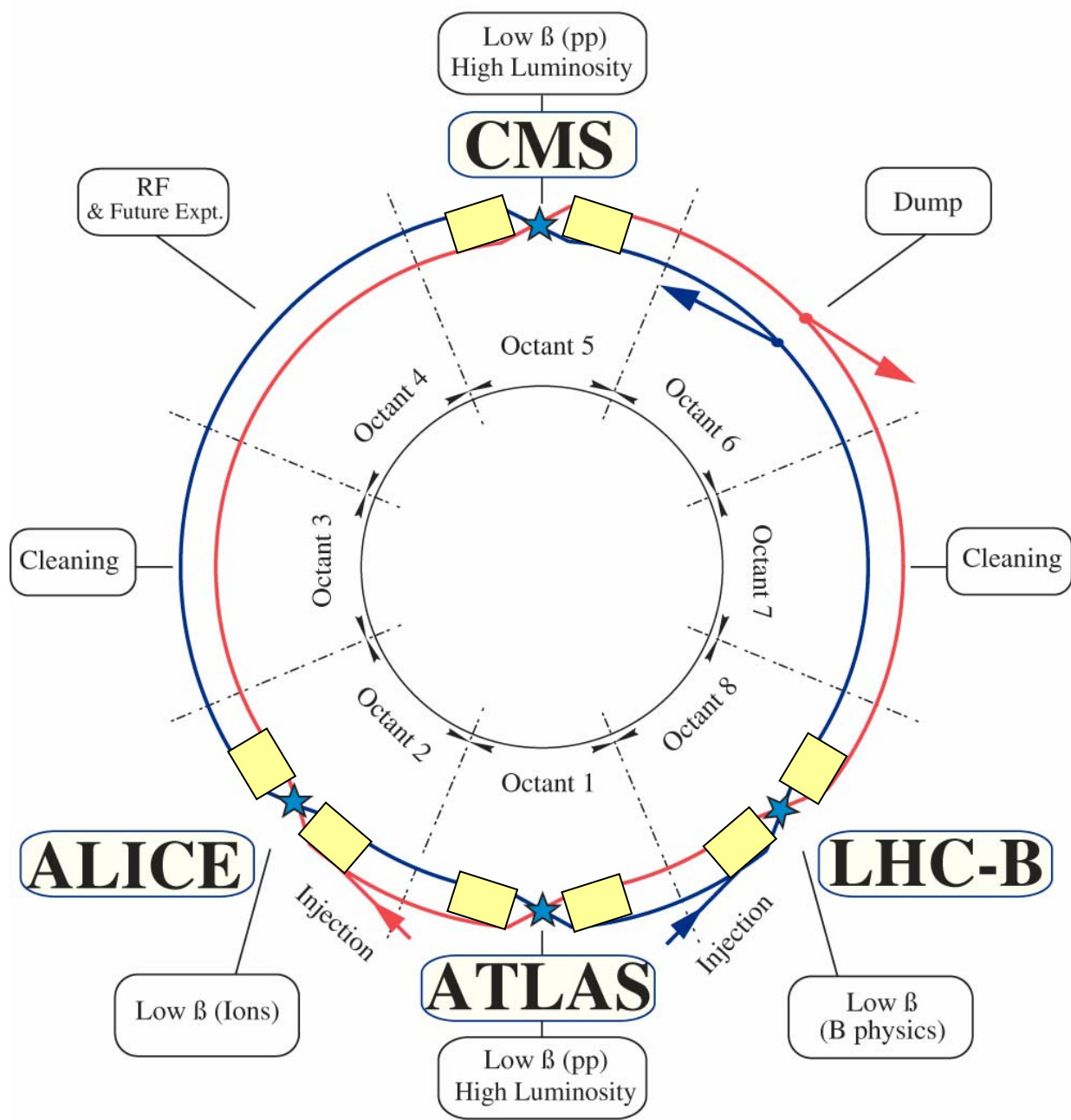
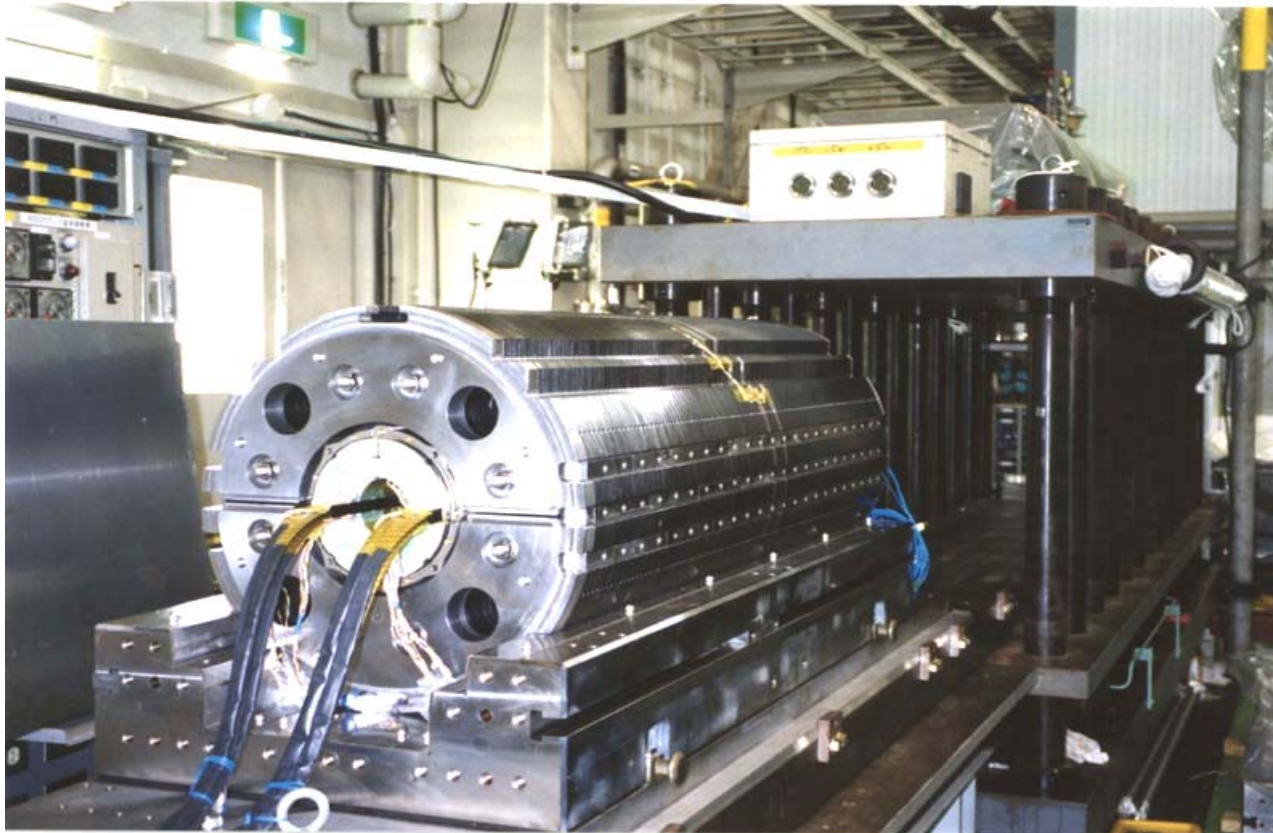


Figure: 3 Single Sextant PS Model

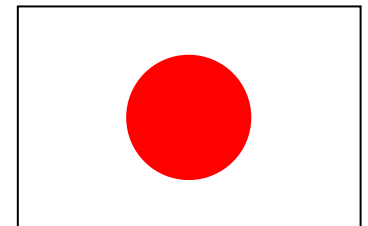
But also SPS transfer line (bypass converters), ...



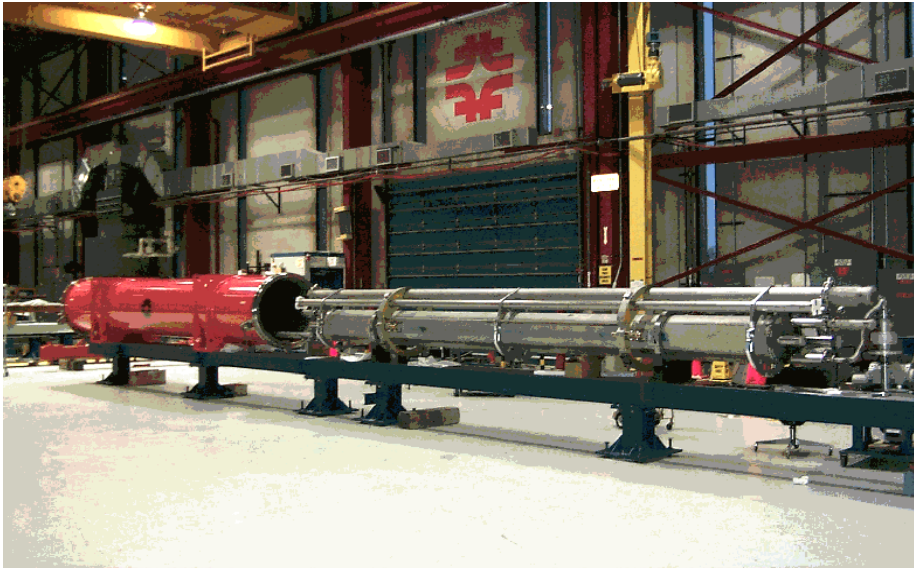
Prototype low- β quadrupole



MQXA (KEK)
205 T/m
 $I = 6450$ A
 $I_{\text{ultimate}} = 7$ kA
 $L1 = 91$ mH



Prototype MQXB being readied for cryostat insertion

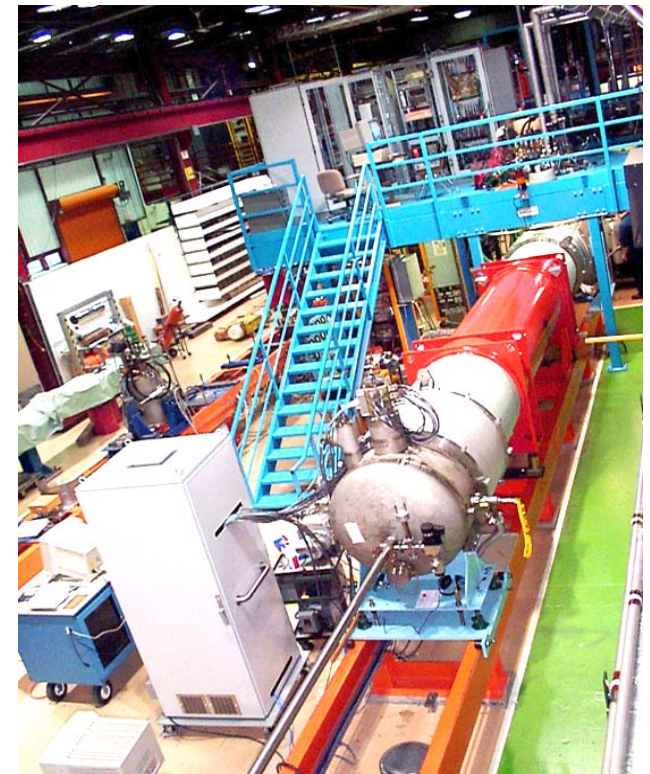
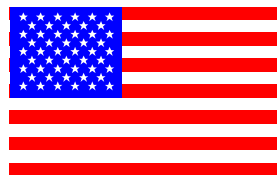


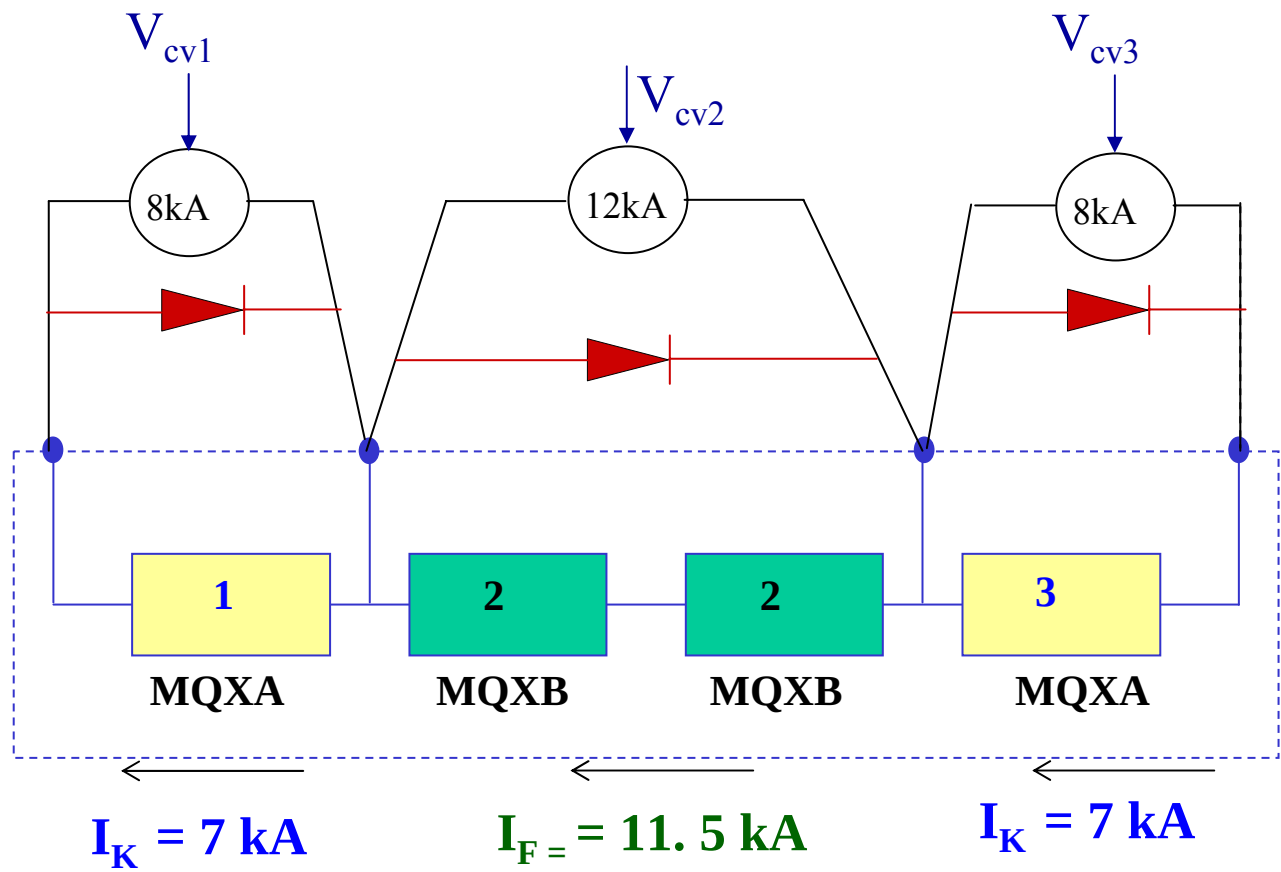
MQXB (Fermilab)

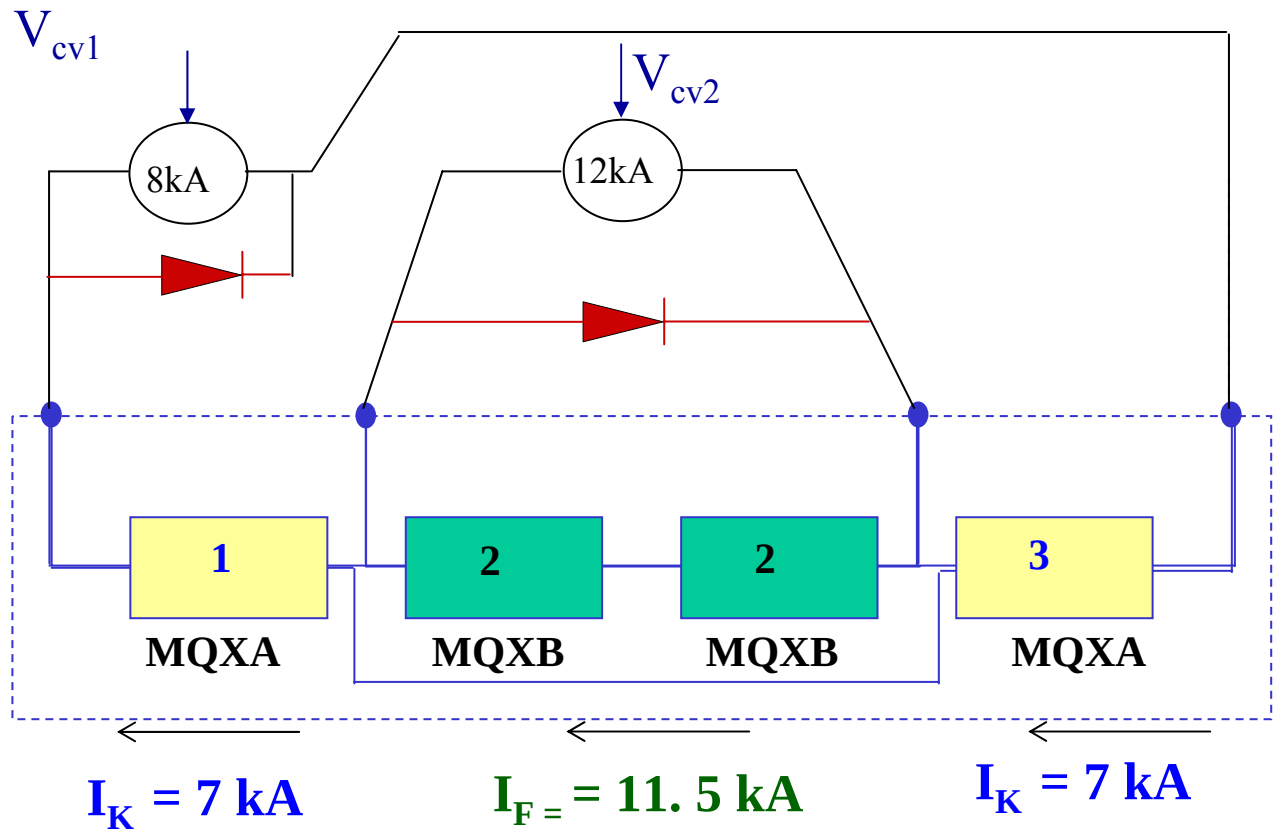
205 T/m

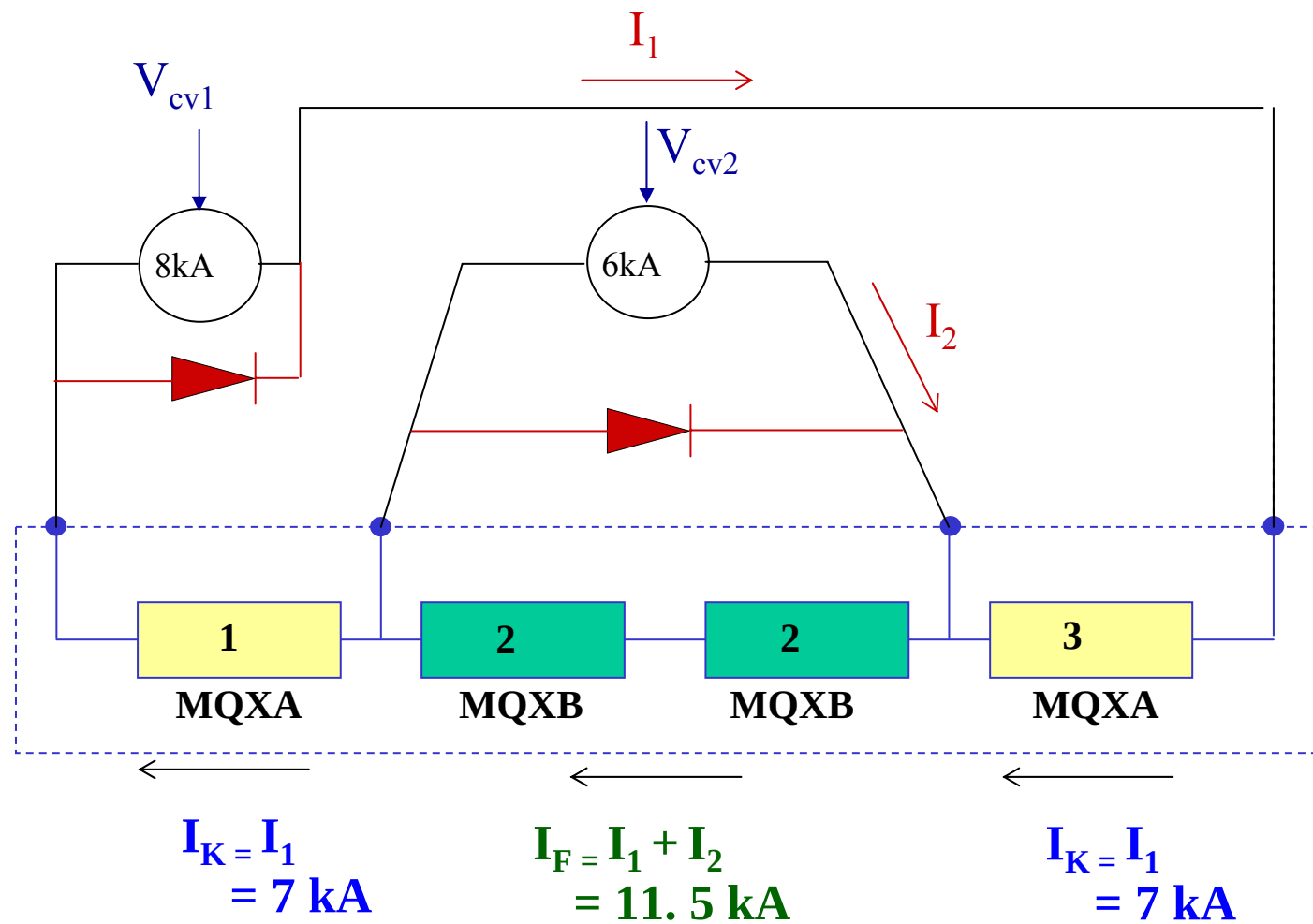
$I = 11390 \text{ A}$ (ultimate = 12290A)

$L2 = 18.5 \text{ mH}$

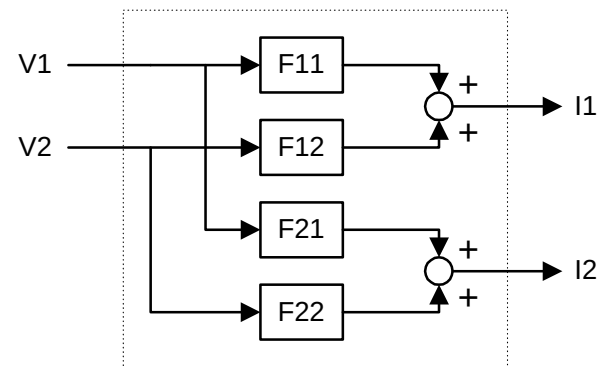
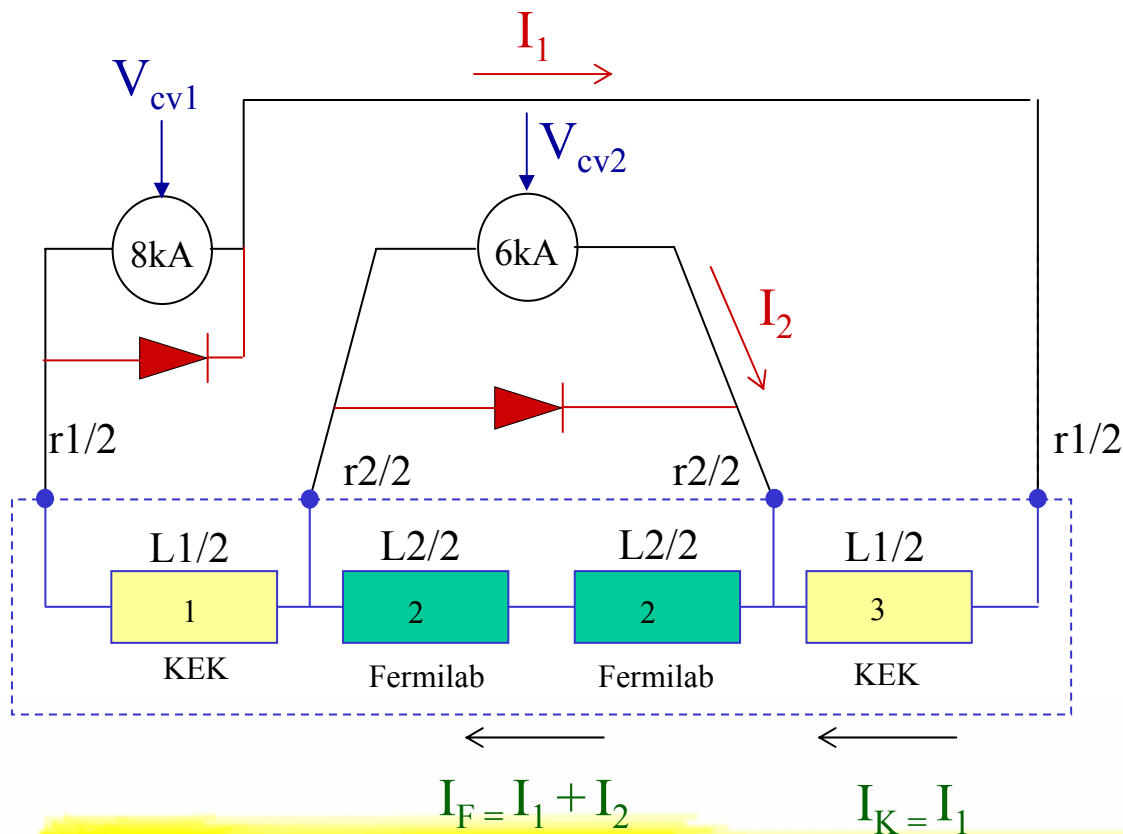






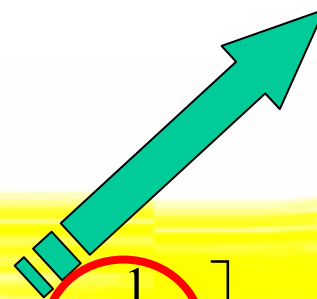


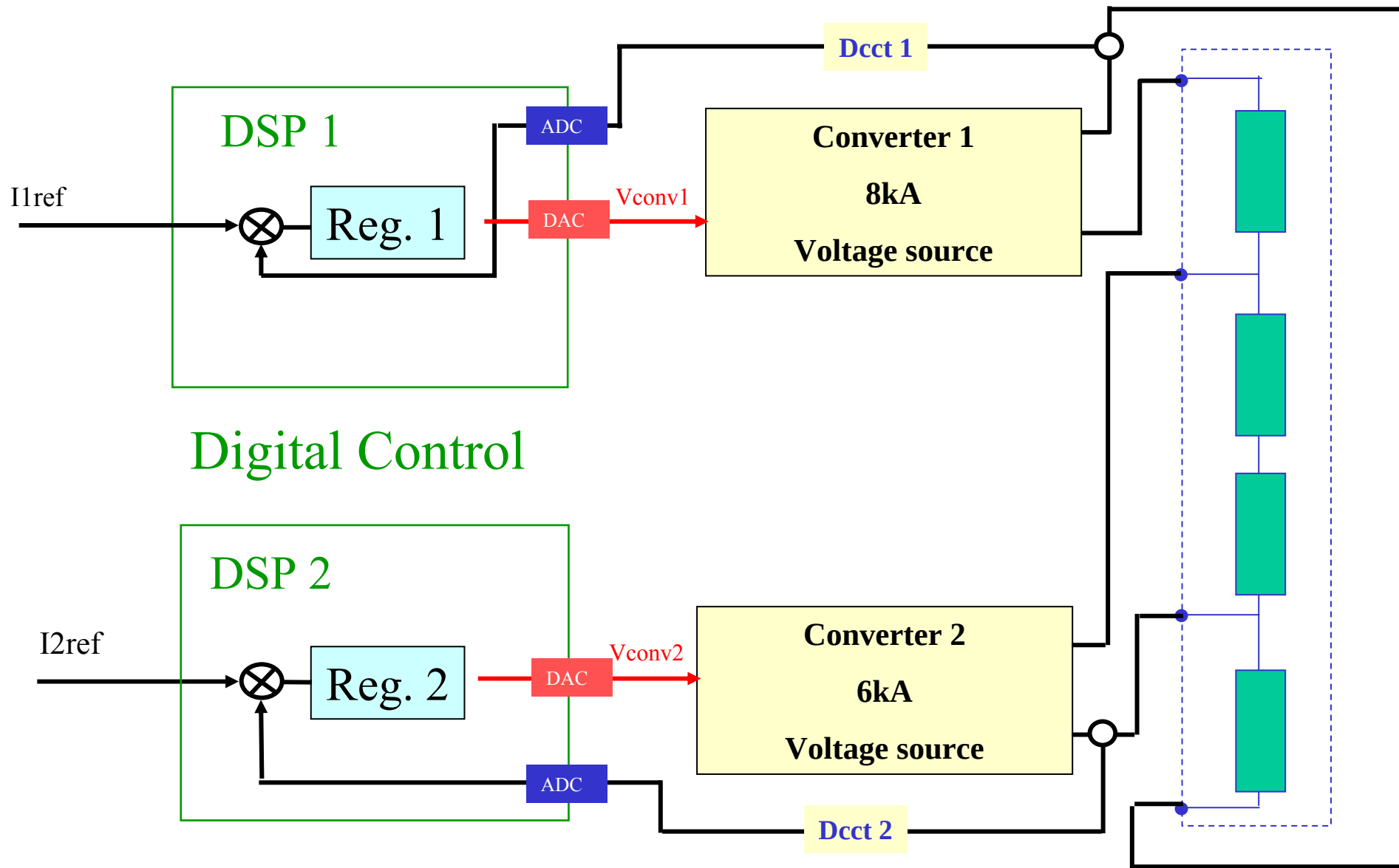
Inner Triplet : nested power converters



Inductive coupling

$$\frac{d}{dt} \begin{bmatrix} i1 \\ i2 \end{bmatrix} = \begin{bmatrix} -\frac{r1}{L1} & -\frac{r2}{L1} \\ \frac{r1}{L1} & -r2 \cdot \left(\frac{1}{L1} + \frac{1}{L2} \right) \end{bmatrix} \cdot \begin{bmatrix} i1 \\ i2 \end{bmatrix} + \begin{bmatrix} \frac{1}{L1} & -\frac{1}{L1} \\ -\frac{1}{L1} & \frac{1}{L1} + \frac{1}{L2} \end{bmatrix} \cdot \begin{bmatrix} V_{cv1} \\ V_{cv2} \end{bmatrix}$$





Current loops

Conclusion

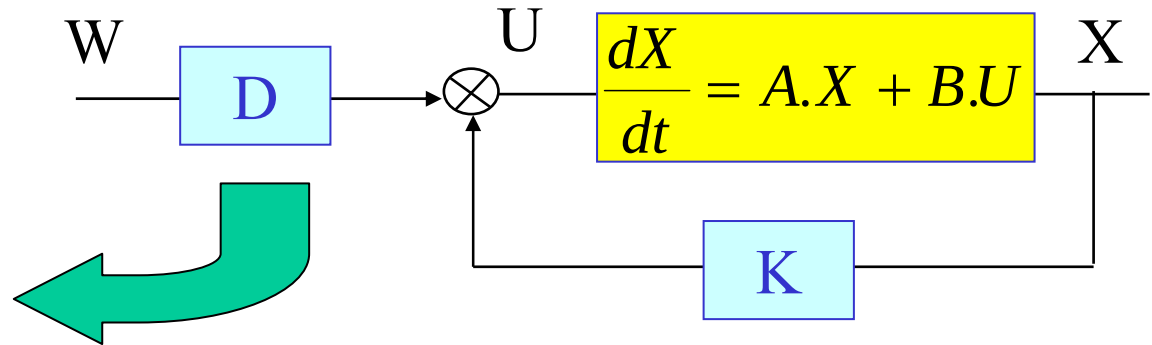
In theory, it is possible to use 2 independent controllers **without** decoupling but...

- the precision decreases with the order of the system
- the current loops are less robust:
 - to non linearities
 - to parameter changes
- a ratio of at least 10 is needed between the current loop bandwidths and the frequency of the reference currents
- slow down the ramp rate

Decoupling Principle :

$$\frac{dX}{dt} = A.X + B.U$$

$$\frac{dX}{dt} = \underbrace{(A + B.K)}_{Ad}.X + \underbrace{B.D}_{Bd}.W$$



Choice :

$$Ad = \begin{bmatrix} -\frac{r1}{L1 + L2} & 0 \\ 0 & -\frac{r2}{L2} \end{bmatrix}$$

$$Bd = \begin{bmatrix} \frac{1}{L1 + L2} & 0 \\ 0 & \frac{1}{L2} \end{bmatrix}$$

Ad and Bd : diagonal matrices

Decoupling matrices :

$$K = B^{-1} \cdot (Ad - A)$$

$$D = B^{-1} \cdot B$$

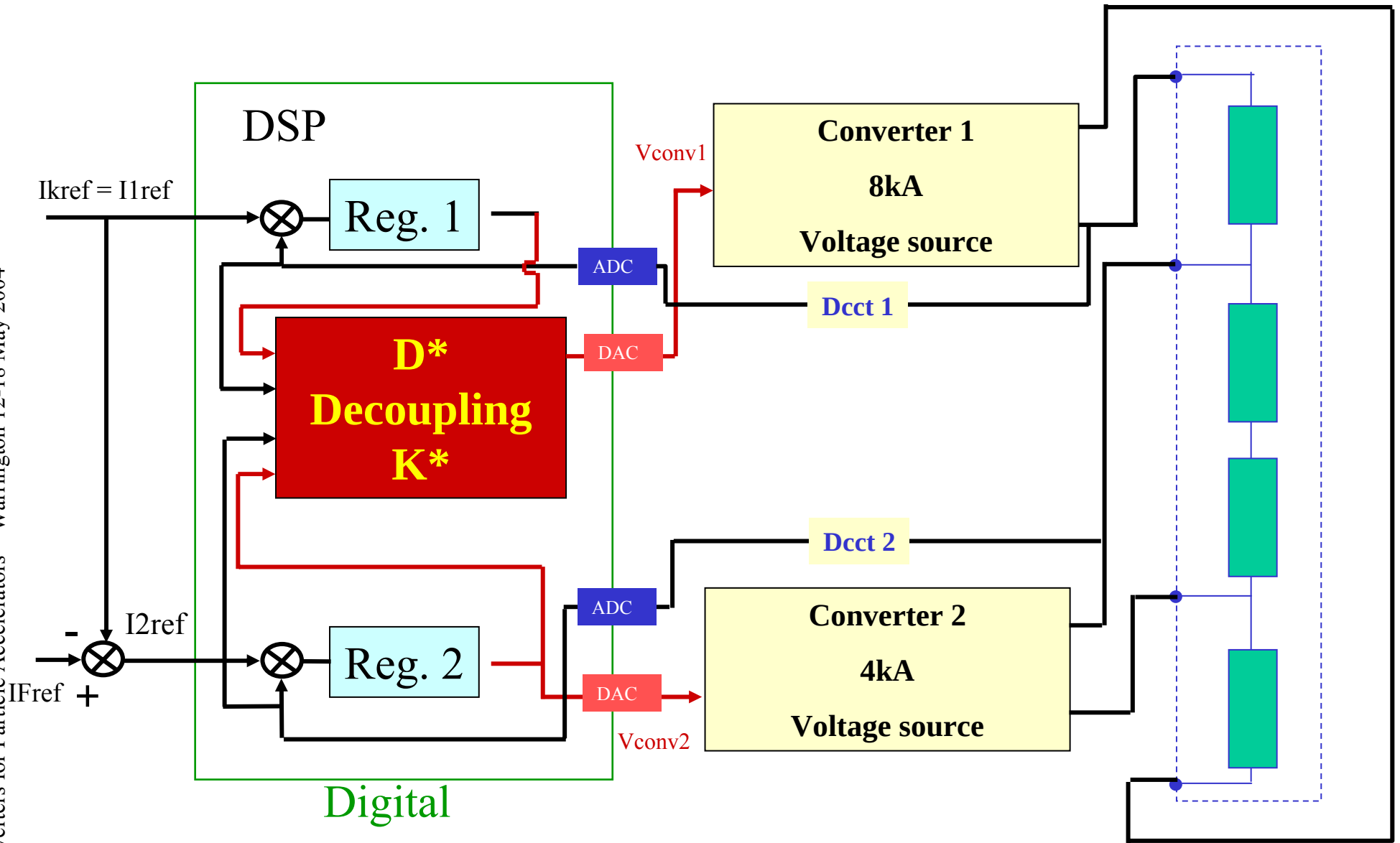
Digital :

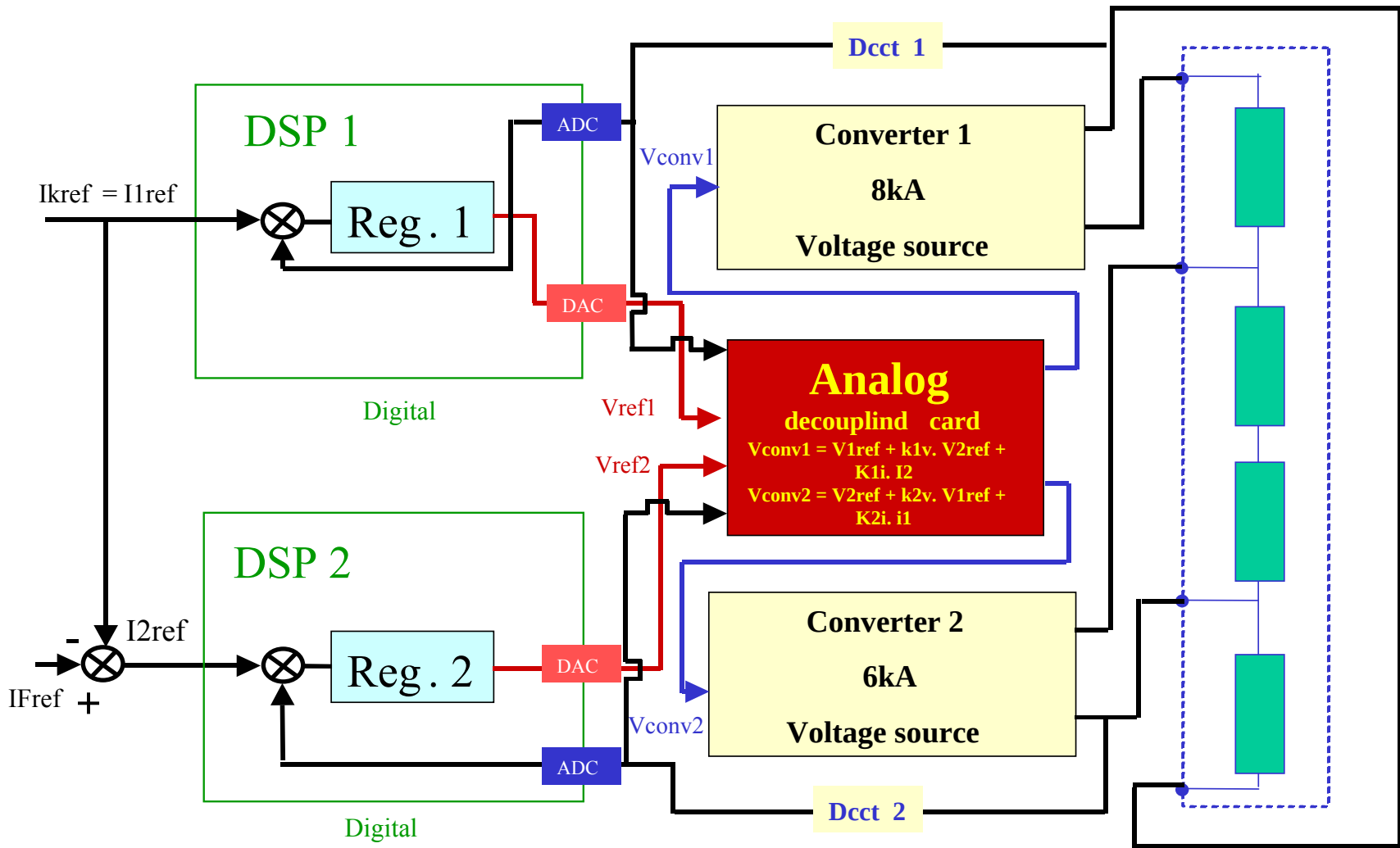
$$X^*(k+1) = F^*.X^*(k) + H^*.U^*(k)$$

$$\text{with } F^* = e^{A \cdot ts} ; H^* = A^{-1} \cdot (e^{A \cdot ts} - I) \cdot B$$

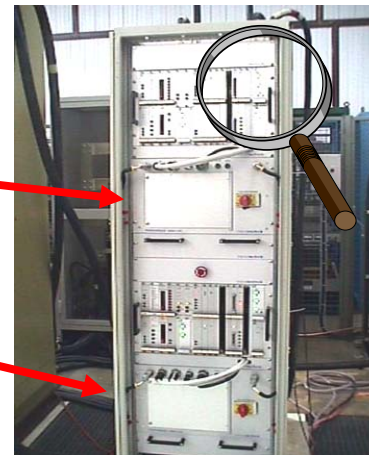
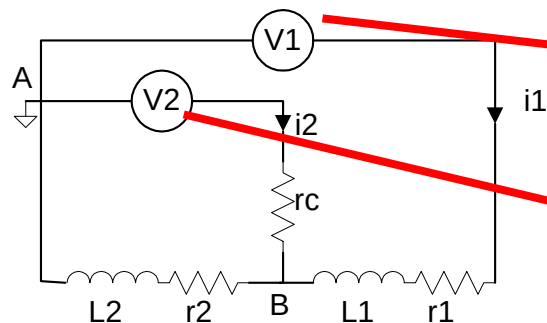
ts : sampling period

$$X^*(k+1) = Fd^*.X^*(k) + Hd^*.W^*(k)$$

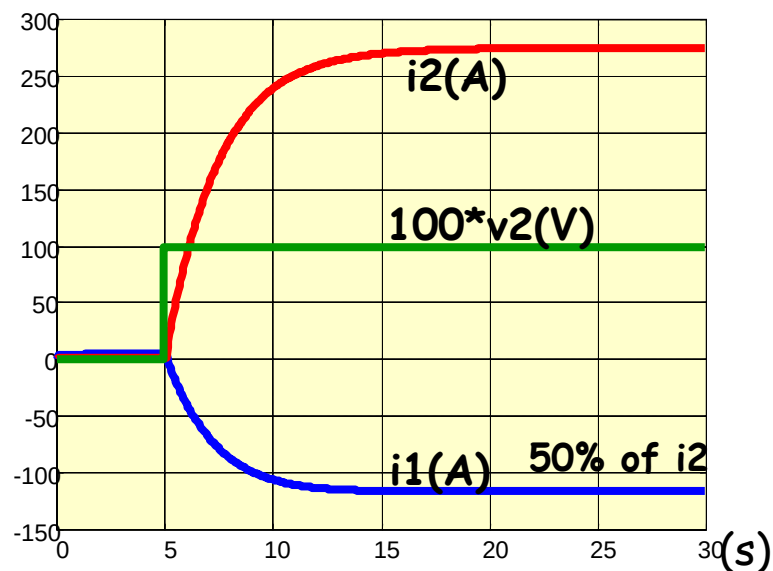




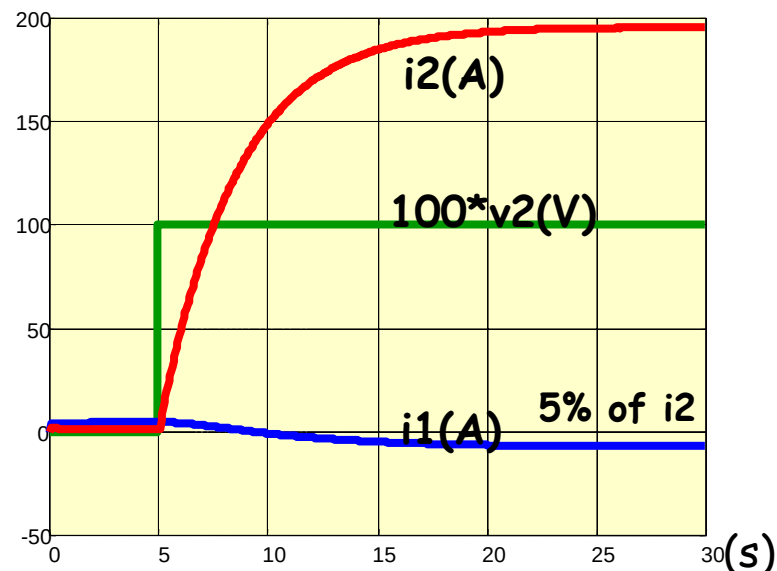
Experimental results



$2 * [600A, 10V]$

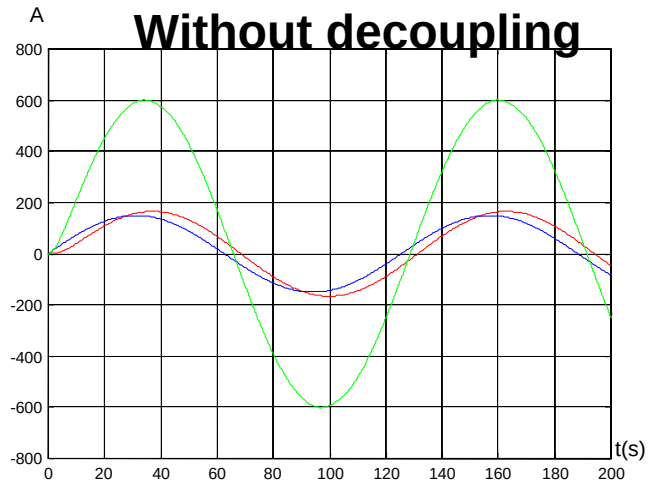


Without decoupling



With decoupling
(10% parameter error)

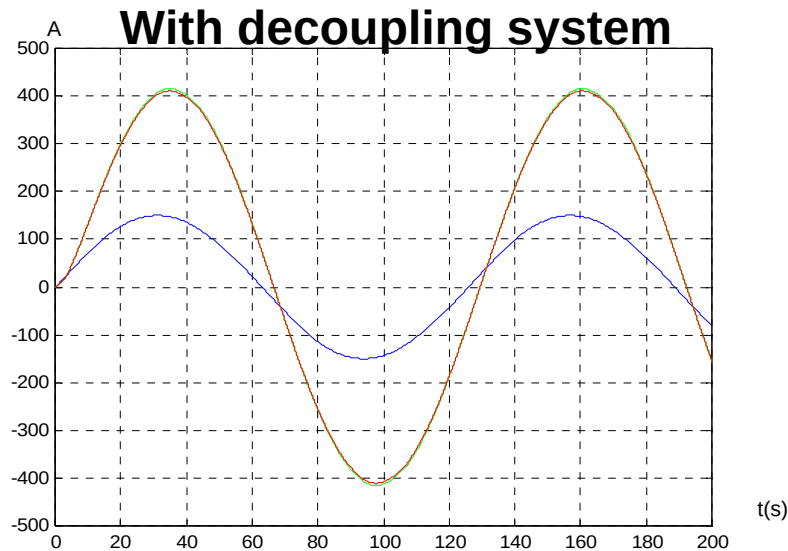
Decoupling solution



Blue: $50 \cdot V(\text{references})$

Green: I_1 with $V_1=V$ and $V_2=0$

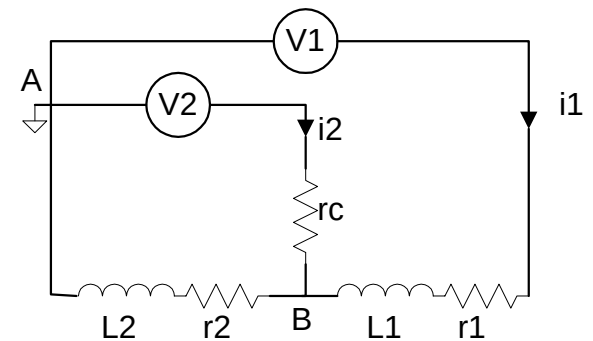
red: I_1 with $V_1=V$ and $V_2=V$



Blue: $50 \cdot V(\text{references})$

Green: I_1 with $V_1=V$ and $V_2=0$

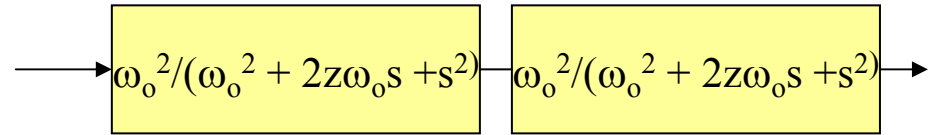
red: I_1 with $V_1=V$ and $V_2=V$



The end

Thank for your attention

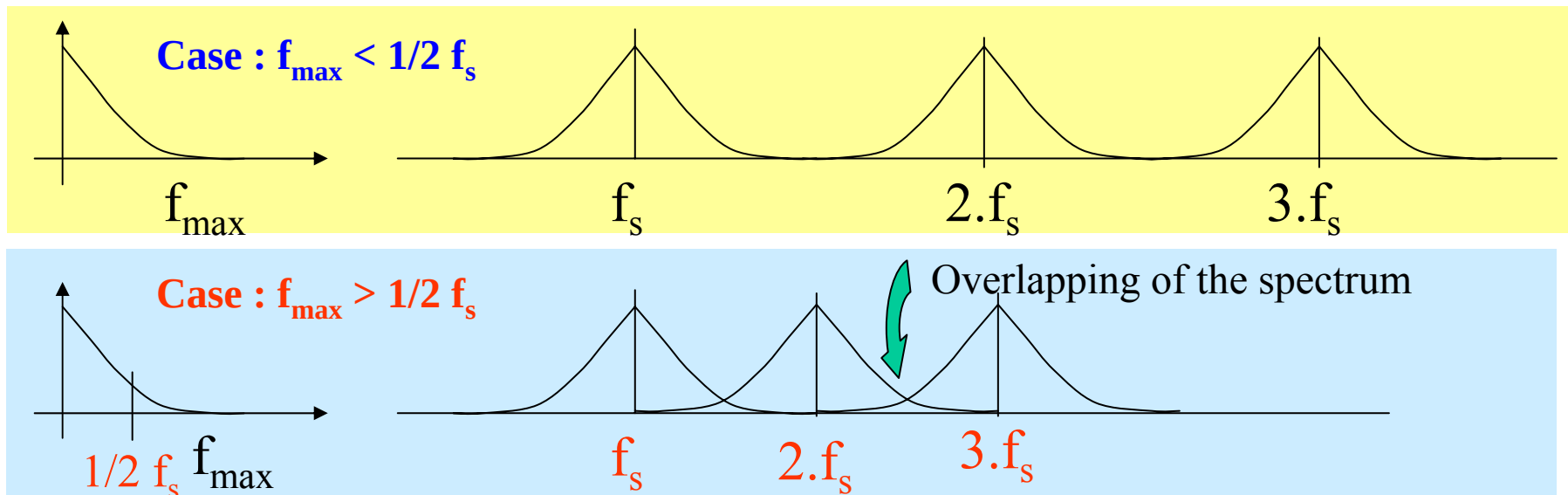
Anti-aliasing



Since the sampling frequency is fixed, in order to avoid the folding (overlapping, aliasing,...) of the spectrum ($\Rightarrow$ distortions), the analogue signals must be filtered prior to sampling to ensure that

$$f_{\max} < 1/2 f_s \quad (\text{Nyquist or Shannon criteria})$$

In the case of low frequency sampling, a sampling at a higher frequency could be carried out (integer multiple of the desired sampling frequency), using an appropriate anti-aliasing filter. Then the sampled signal is passed through a digital anti-aliasing filter followed by a frequency divider $\Rightarrow$ giving a sampled signal with the required frequency (f_s)

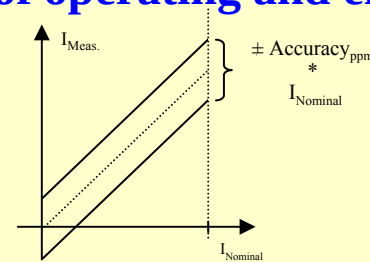


Glossary

– Accuracy

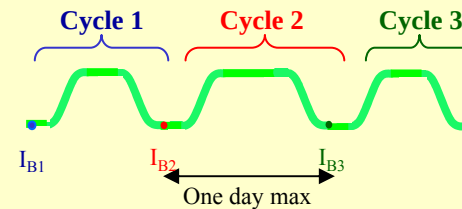
Long term setting or measuring uncertainty taking into consideration the full range of permissible changes* of operating and environmental conditions.

* requires definition



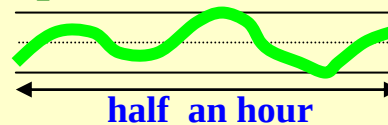
– Reproducibility

Uncertainty in returning to a set of previous working values from cycle to cycle of the machine.



– Stability

Maximum deviation over a period with no changes in operating conditions.



Accuracy, reproducibility and stability are defined for a given period

Precision is qualitative . Accuracy is quantitative.

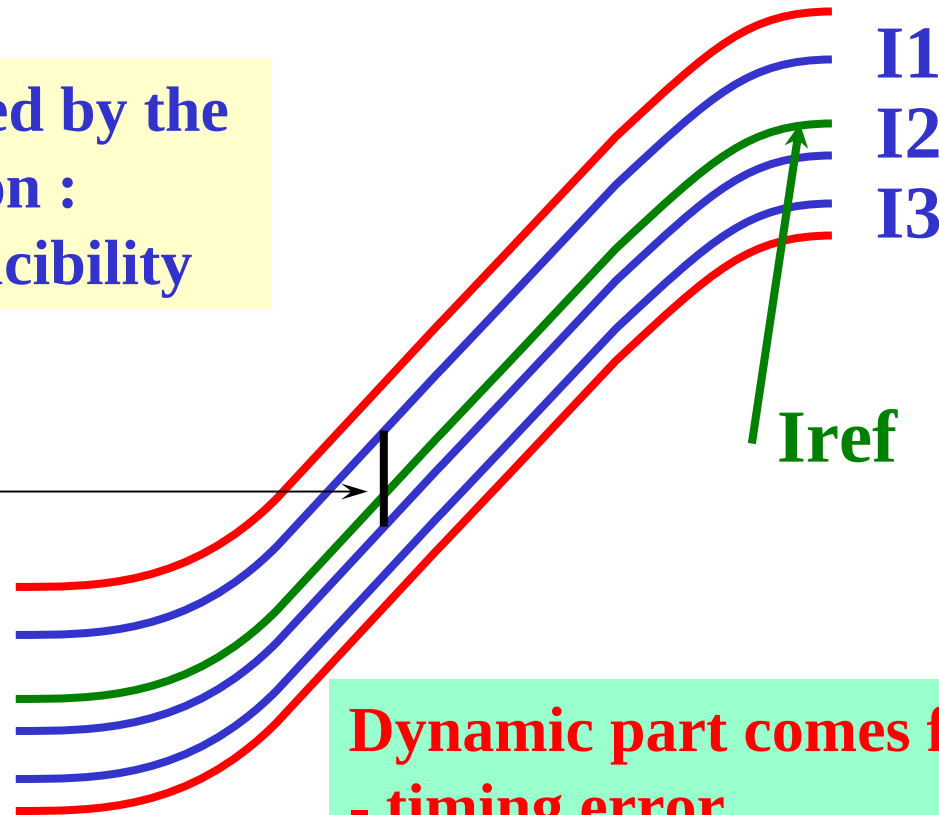


Tracking

Ability of the converter **S** to follow the reference function (static, dynamics)

Static part is covered by the static definition : accuracy, reproducibility

Tracking error between I1 and I2



Dynamic part comes from :
- timing error
- lagging error in the regulation



System Identification

1) Input/Output data acquisition under an experimental protocol

2) Choice of model structure (complexity : system order)

Parametric or non-parametric, continuous-time or discrete time

3) Estimation of the model parameters

4) Validation of the identified model

Structure and parameter values

