



Cyclotrons for hadron therapy

Marco Schippers



PAUL SCHERRER INSTITUT

i. Basic concepts and operation

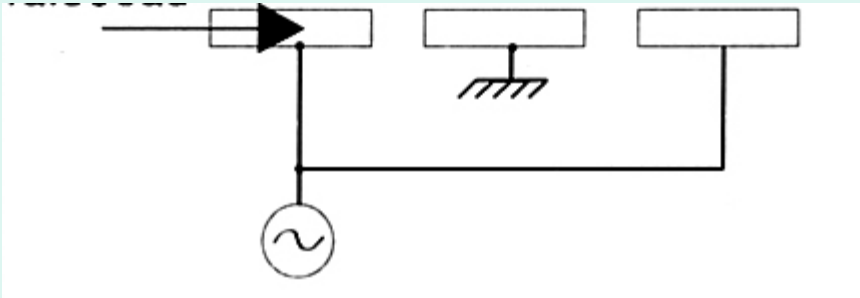
ii. Cyclotron

- a. Source
- b. Central region
- c. RF system
- d. Magnetic field

Synchro-Cyclotron

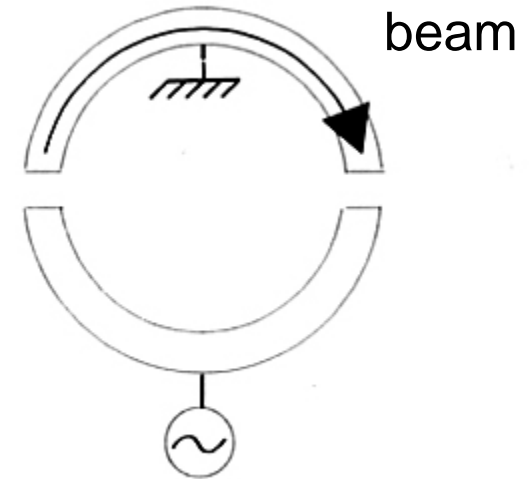
- e. Extraction

iii. Summary and conclusions



Wideroe's linear accelerator

how to
re-use
the RF



$$\frac{mv^2}{r} = Bqv$$

$$v = \frac{2\pi r}{T_{circle}}$$

$$T_{circle} = \frac{2\pi r}{v} = \frac{2\pi m \cancel{r}}{Bq \cancel{r}} = \frac{2\pi \cdot m}{Bq}$$

„**r cancels r**.... don't you see what this means?

The resonance condition does not depend on radius!“

(Lawrence to his PhD student, while bursting into his lab; 1930)

(almost) circular orbits:

$$\Rightarrow T_{circle} = \frac{2\pi.r}{v} = \frac{2\pi.m}{Bq}$$

$$B=2T \Rightarrow T=40 \text{ ns}$$

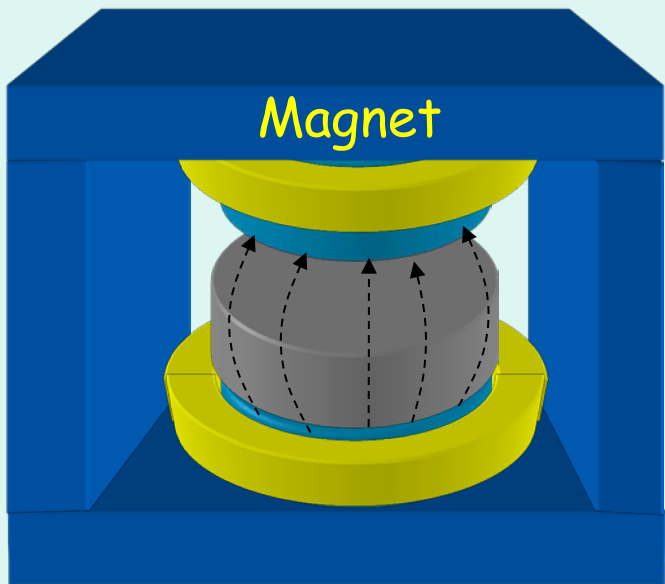
magnetic rigidity: $B\rho$ (= p/q):

**magnet strength B to
bend with radius ρ**

$$70 \text{ MeV } p: \quad B\rho = 1.2 \text{ Tm}$$

$$250 \text{ MeV } p: \quad B\rho = 2.4 \text{ Tm}$$

$$450 \text{ MeV/nucl } C^{6+}: \quad B\rho = 6.8 \text{ Tm}$$

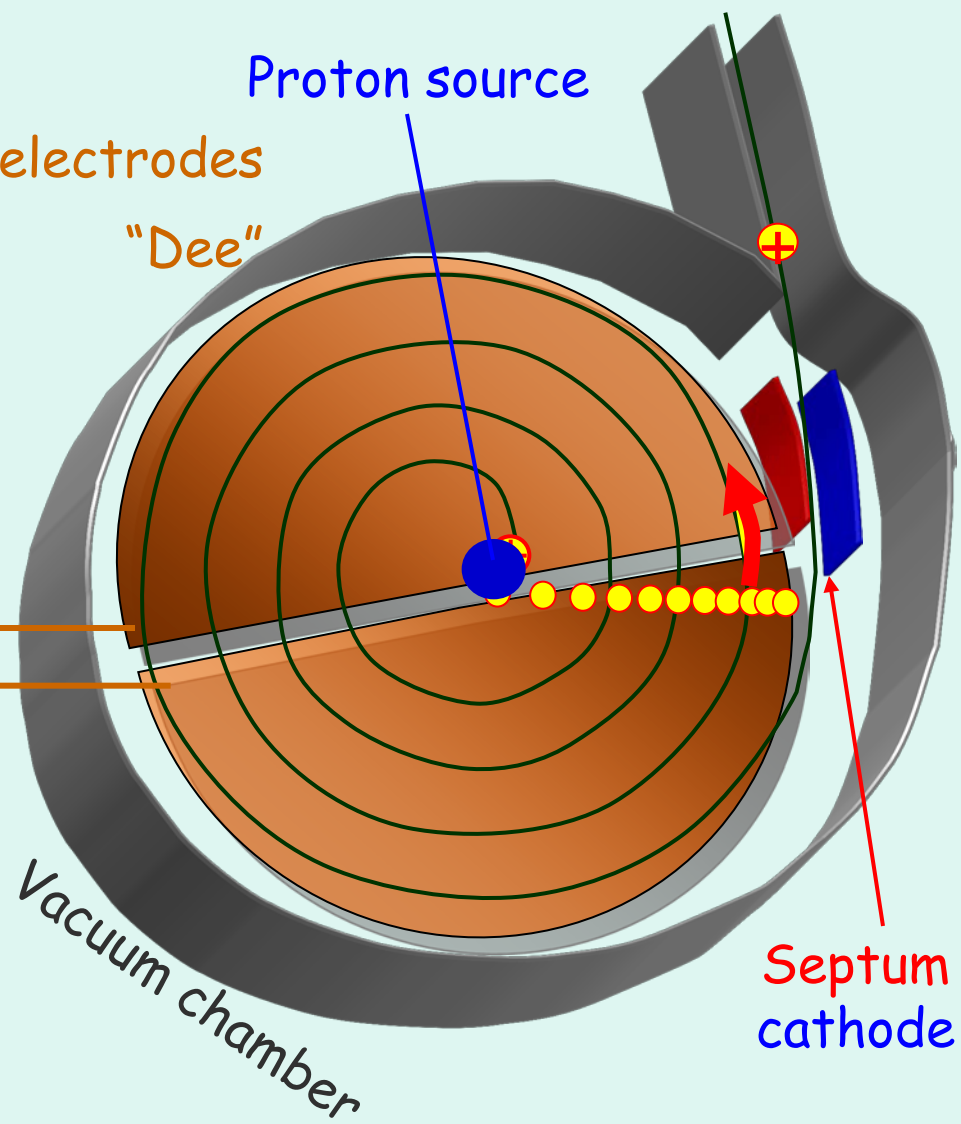


RF electrodes
"Dee"

Proton source

RF-Voltage "V_{dee}" 
 RF freq. ~25 MHz

At electrode slit crossing:
 Energy gain $\Delta E = V_{dee}$



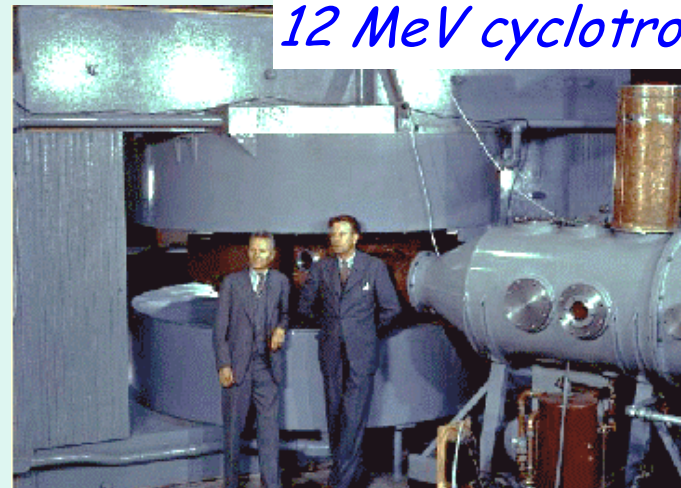
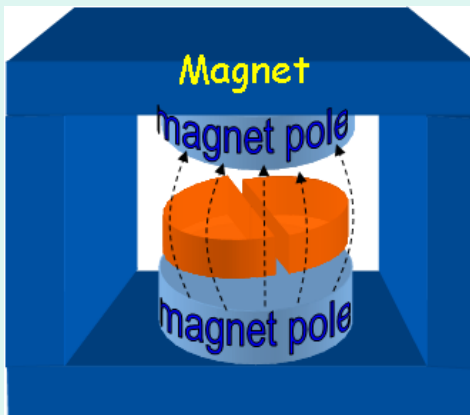
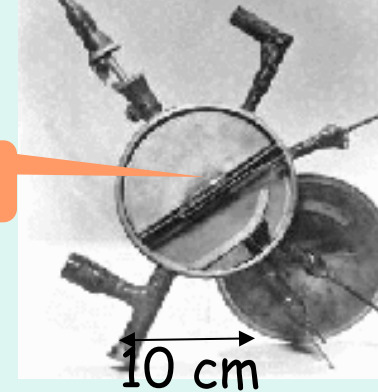


Ernest Lawrence
(1901-1958)

1930:

80 keV protons

Dee



12 MeV cyclotron (UC, 1940)



Protons

in use

Ø2-3.5-5 m

30-100-200 tons

Carbon ions

in design

Ø7 m

700-800 tons

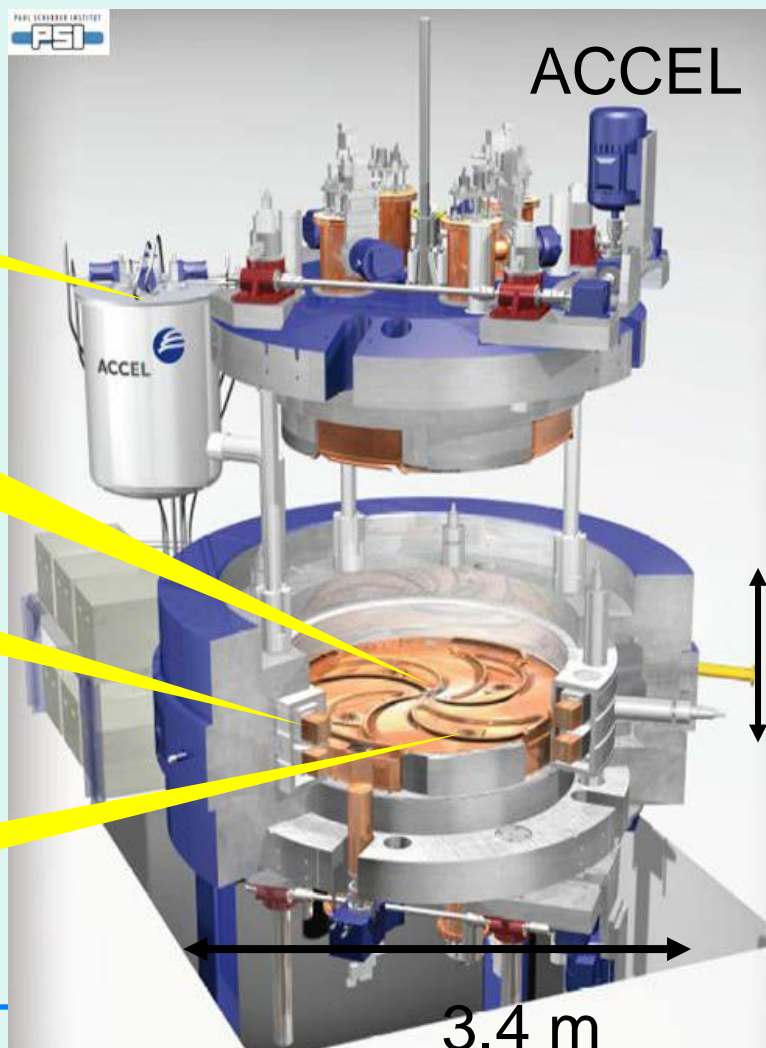
250 MeV proton cyclotron (ACCEL/Varian)

Closed He system
4 x 1.5 W @4K

Proton source

superconducting coils =>
2.4 - 3.8 T

4 RF-cavities:
72 MHz ~80 kV

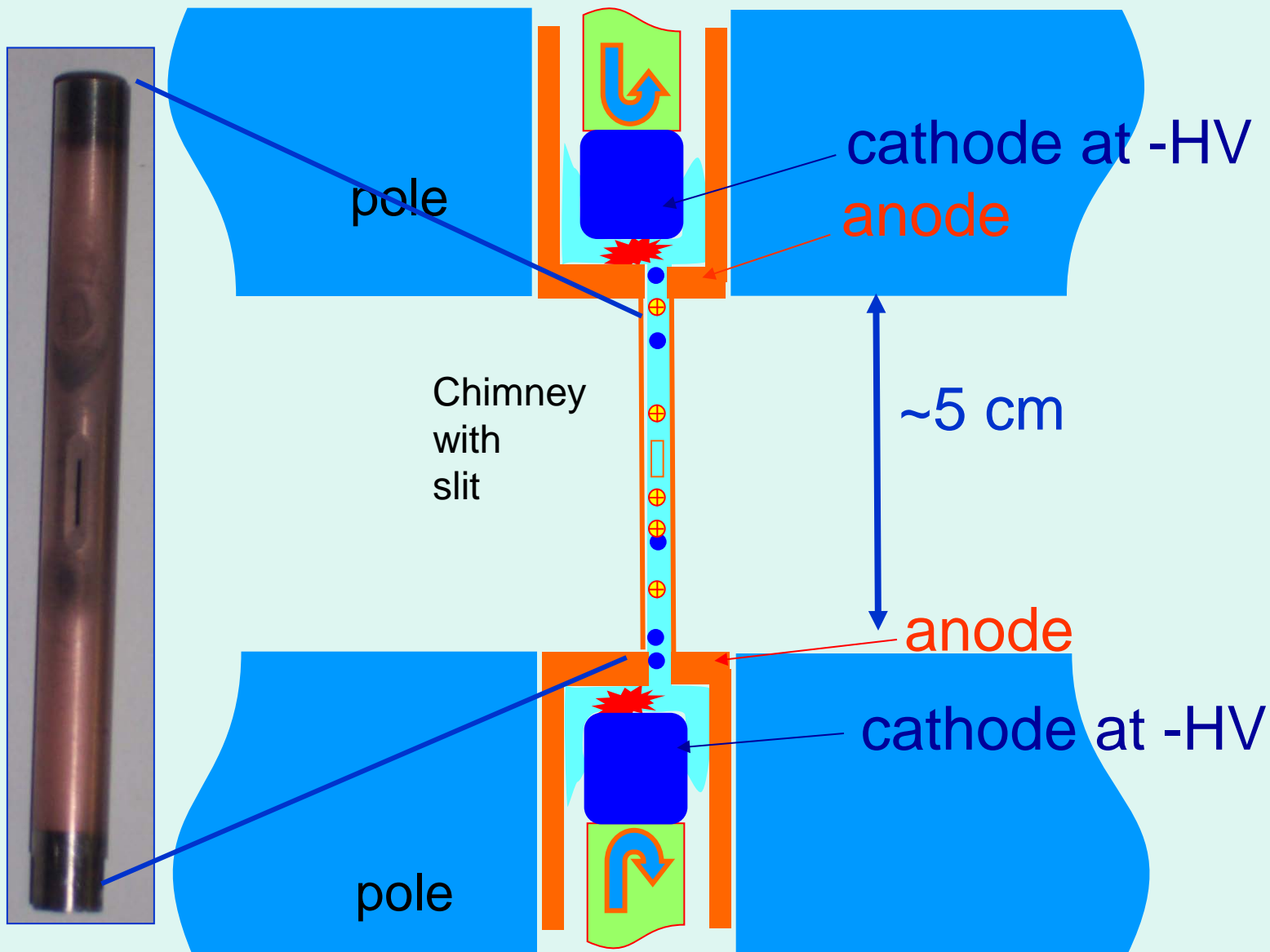


300 kW
90 tons

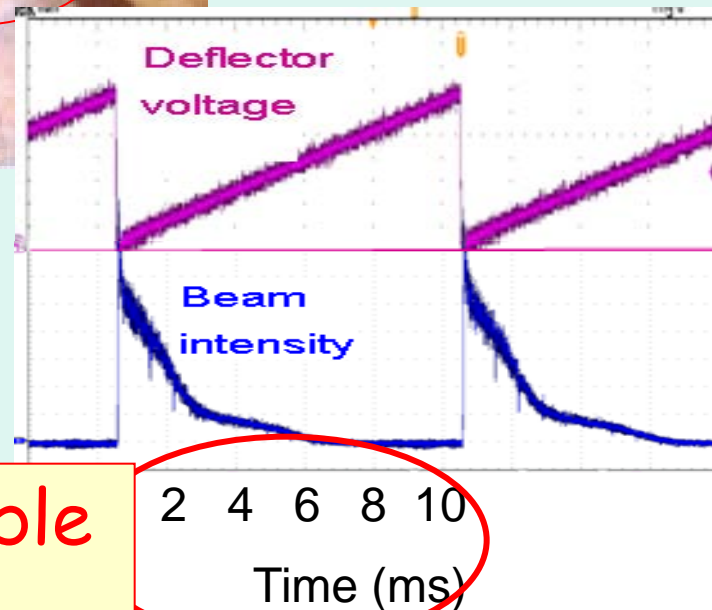
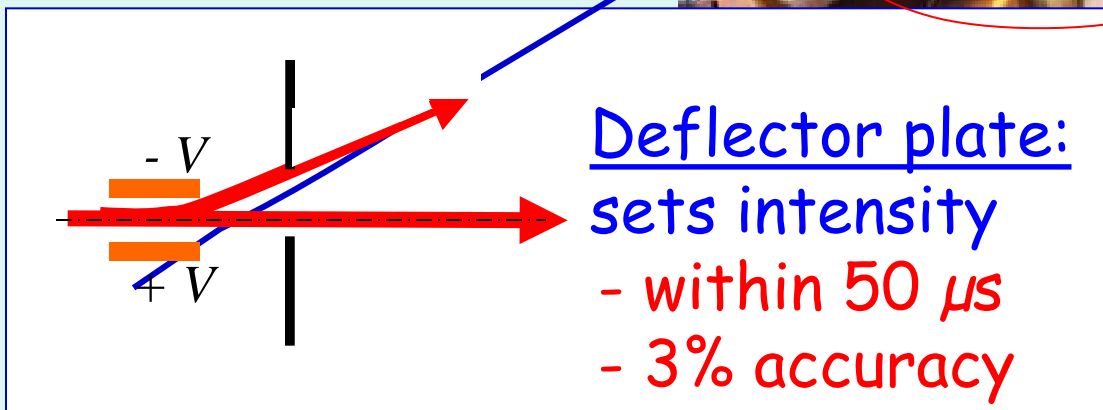
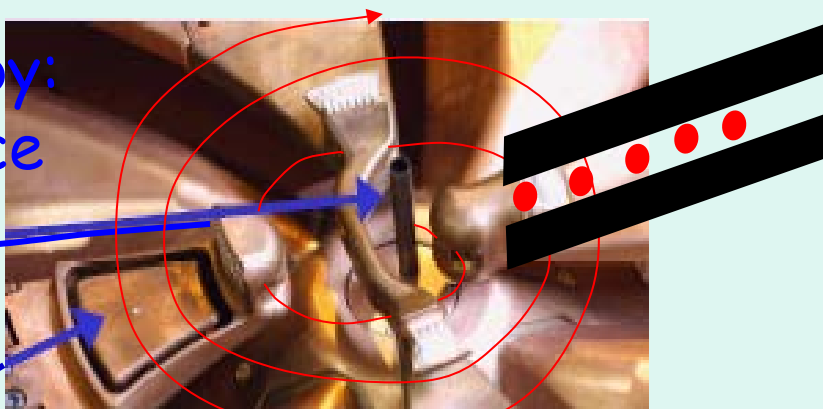
1.4 m

3.4 m

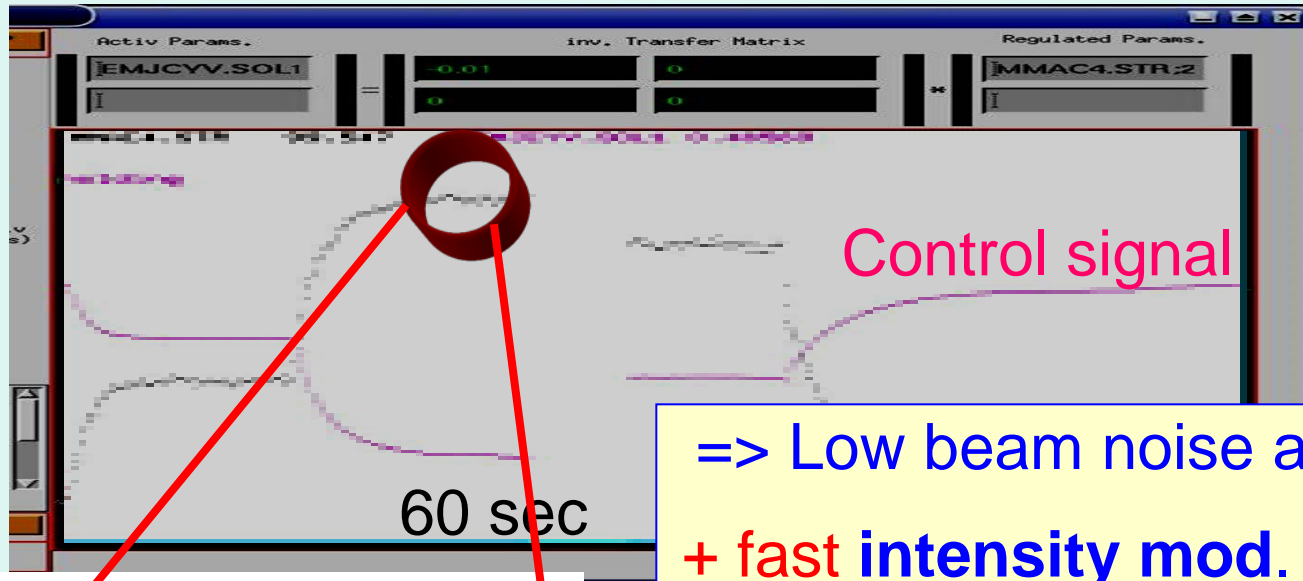
Internal proton source



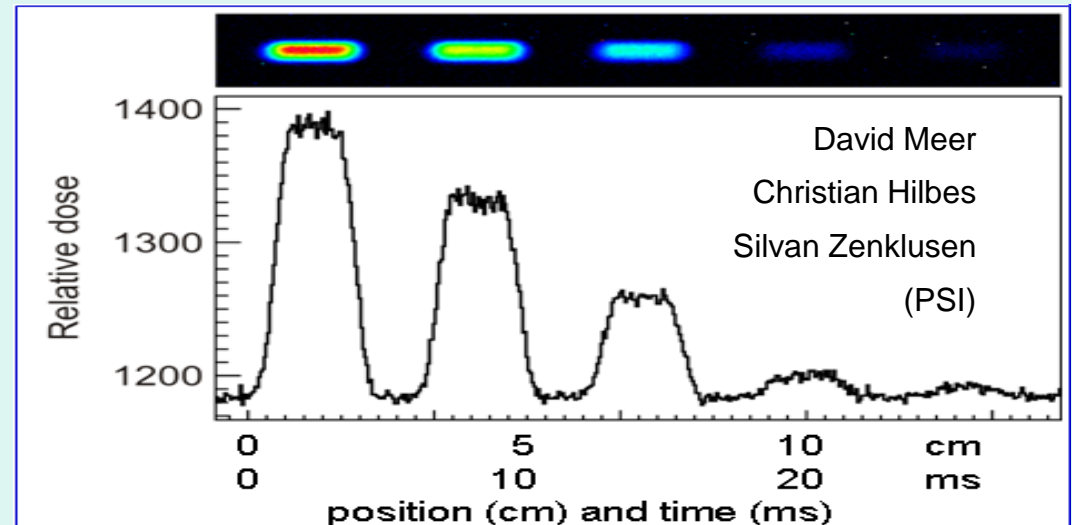
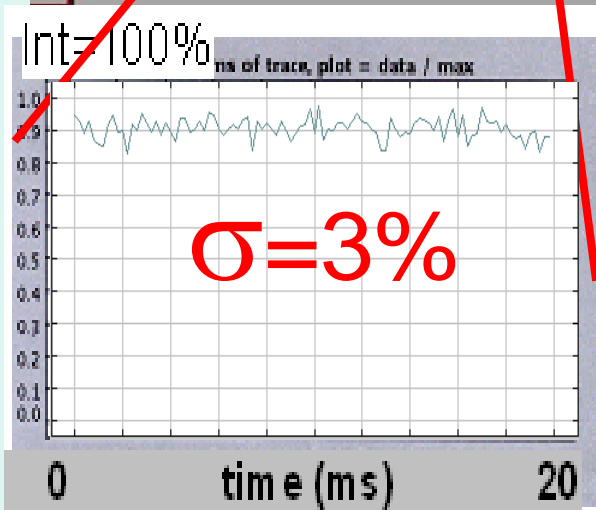
Max. intensity set by:
proton source

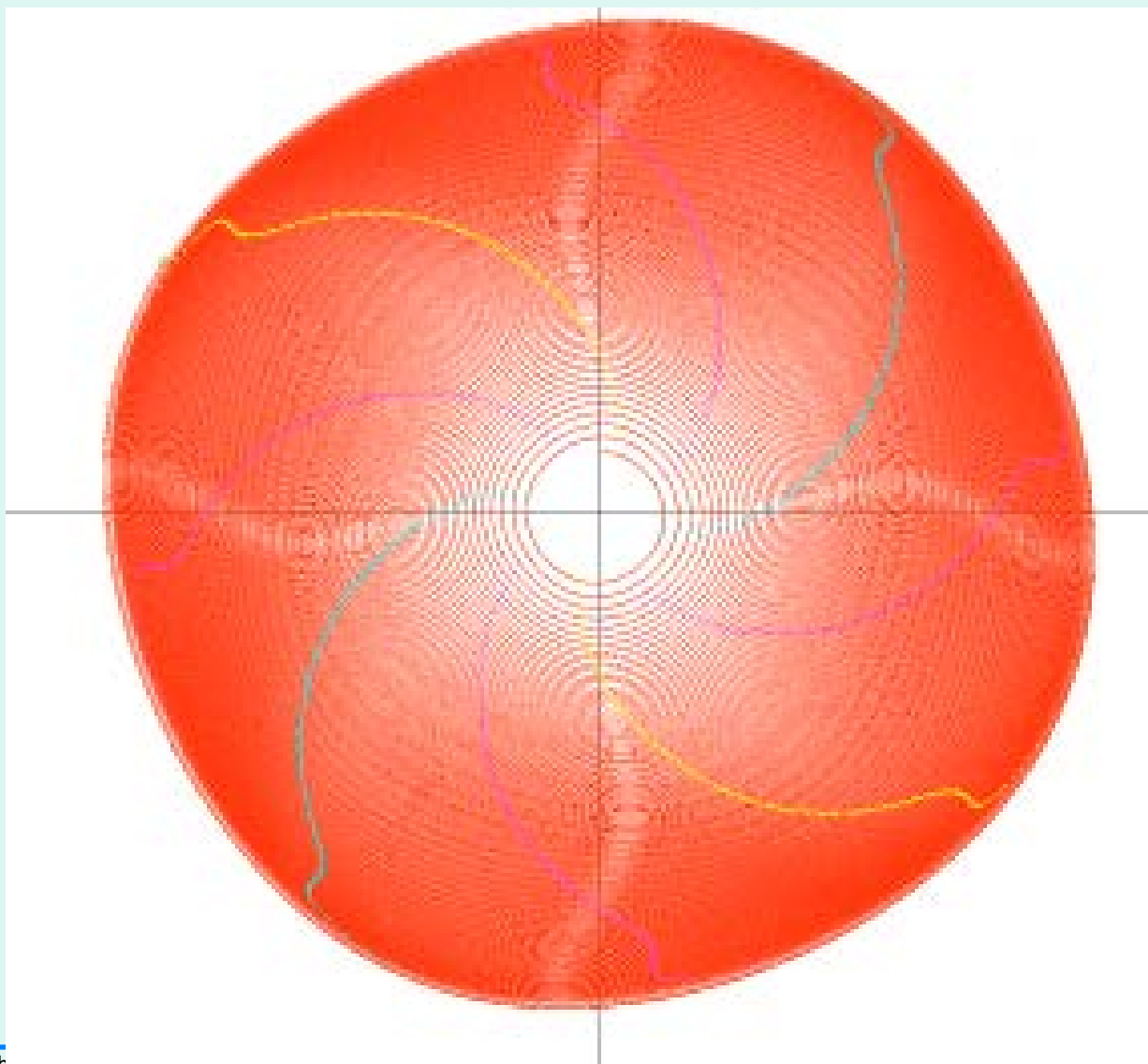


currently only possible
with a **cyclotron**

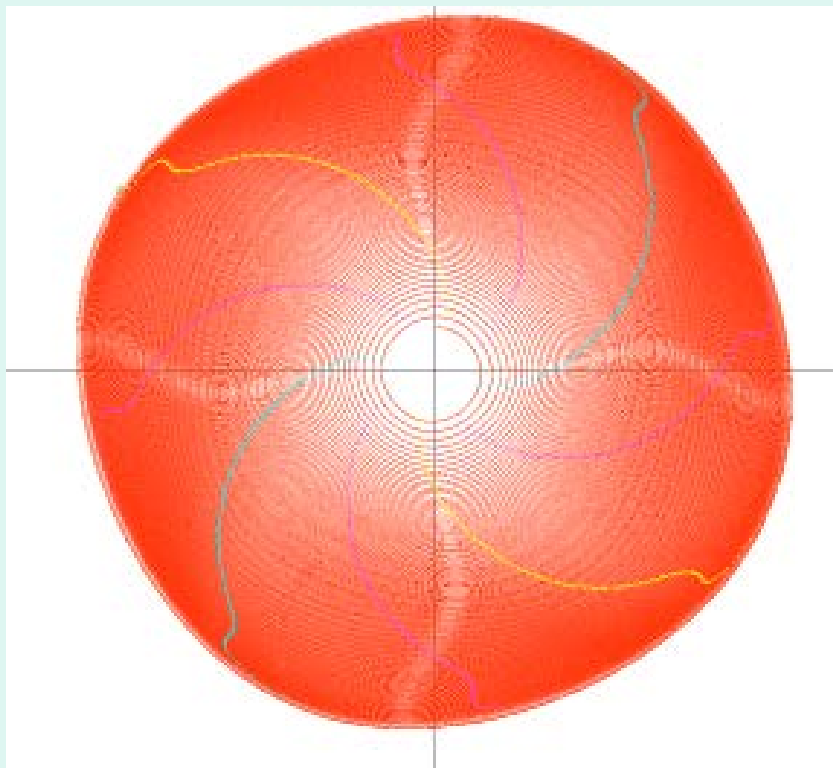


=> Low beam noise allows accurate + fast intensity mod. while scanning

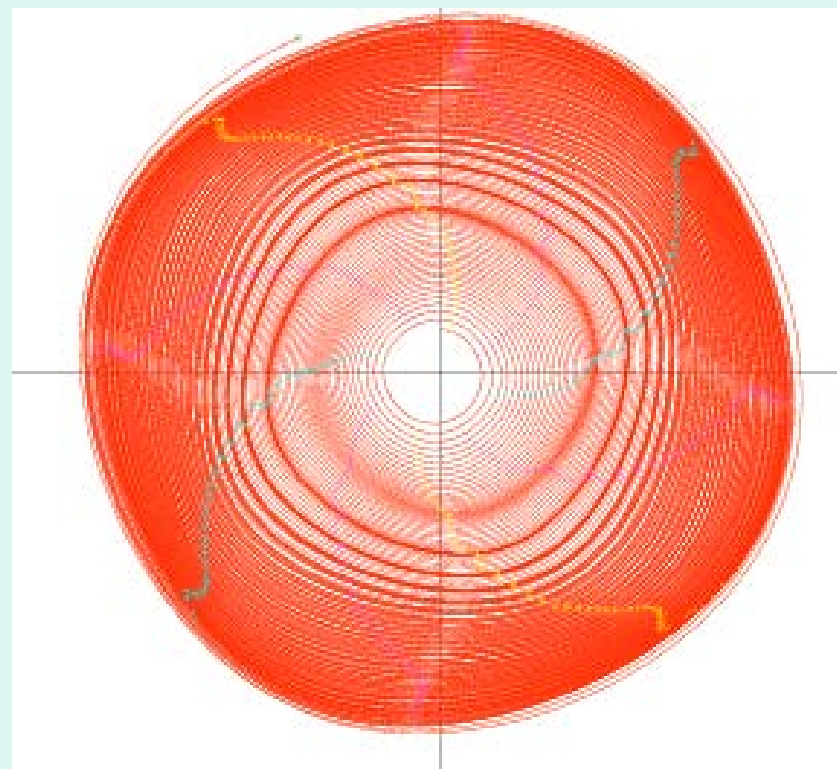




good centering

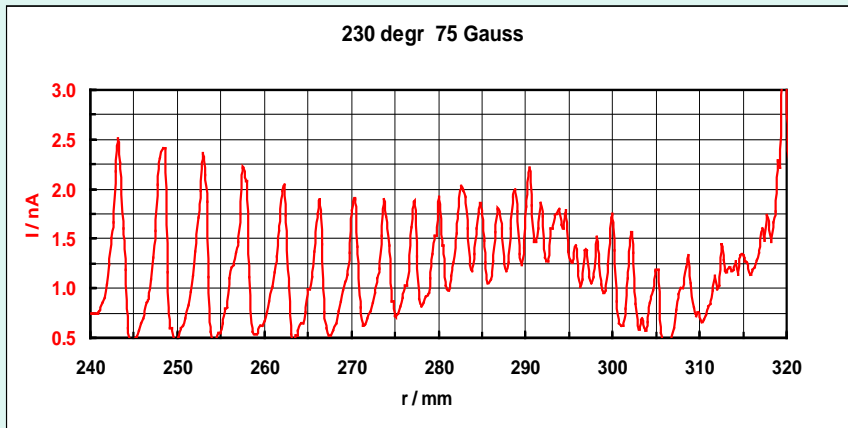


bad centering

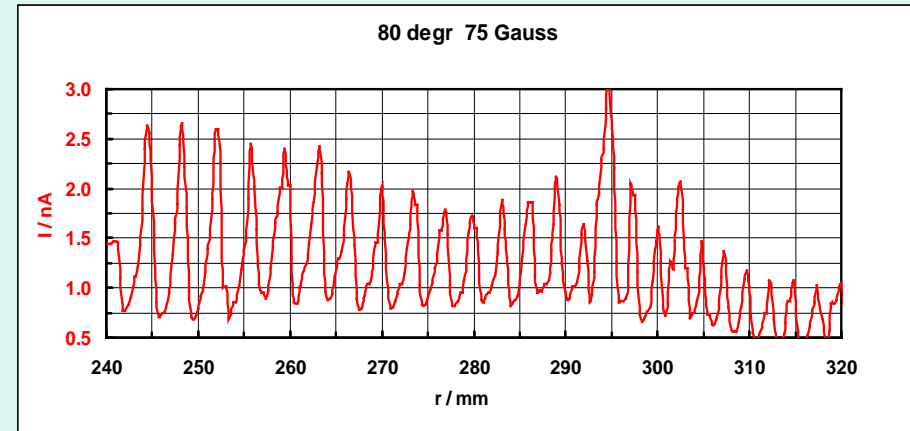


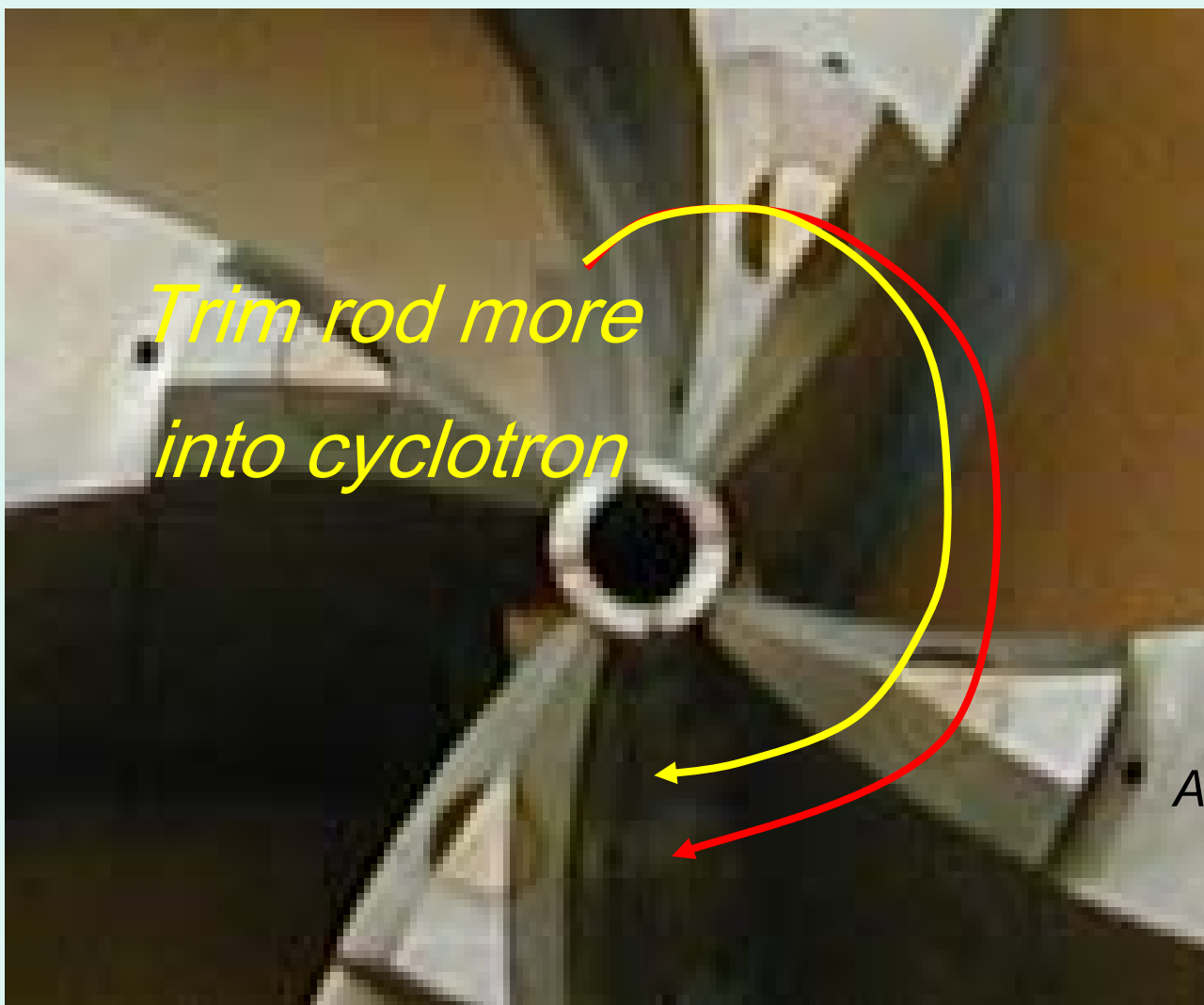
Measurement of the beam intensity
in the cyclotron as a function of radius:

bad centering

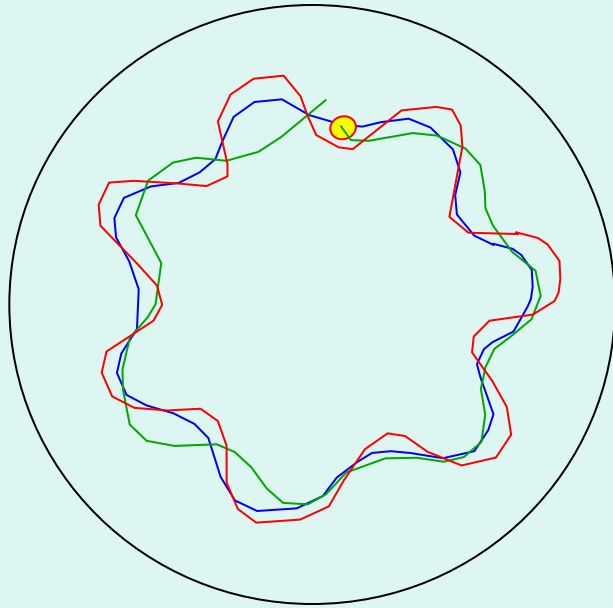


good centering





ACCEL/varian

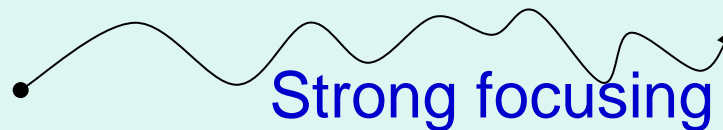


betatron freq $\nu \neq k \cdot$ revolution freq

(in general avoid: $n\nu_r + m\nu_z = p$; i.e. closed orbit)

Otherwise: Resonance \rightarrow Beam loss

Focusing strength: $\sim \nu^2$

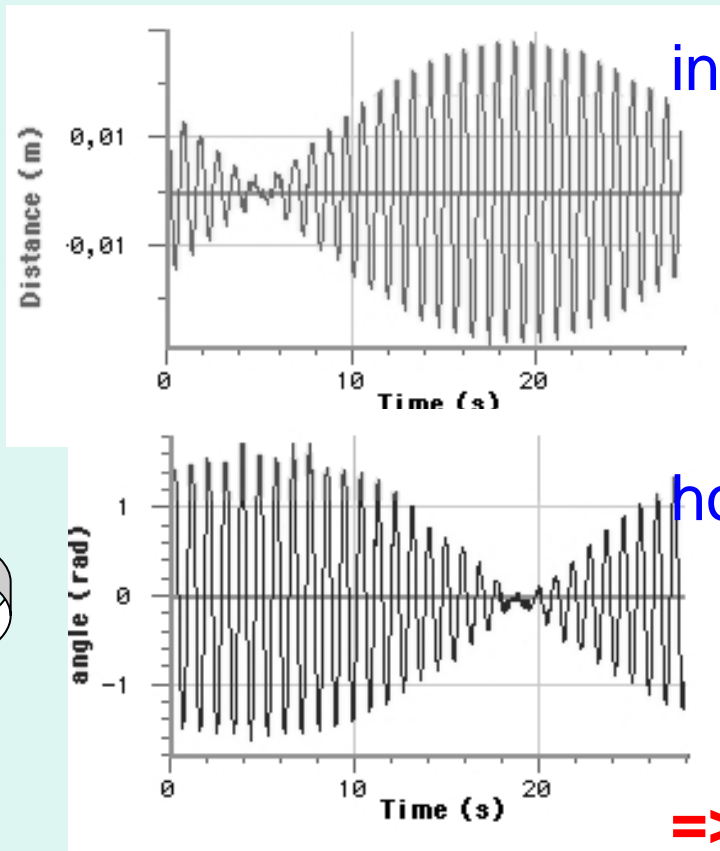
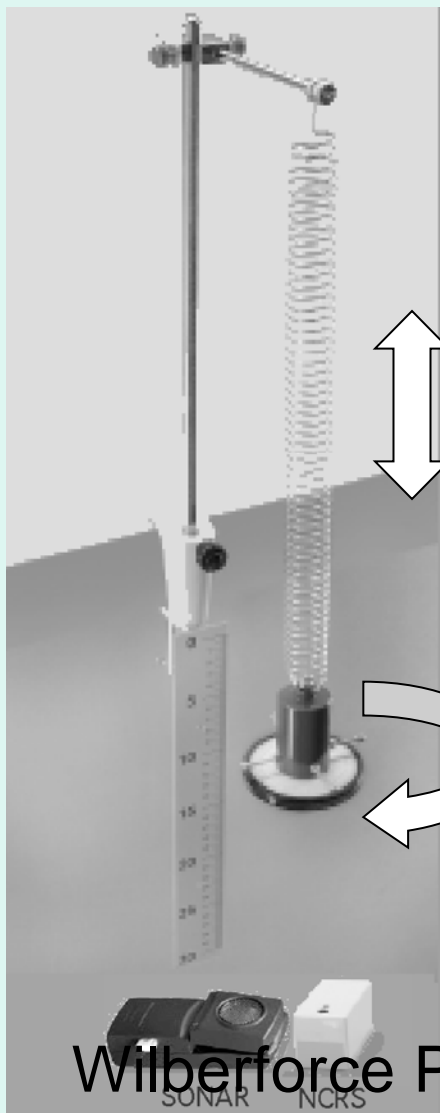


Coupled oscillations

Example of dangerous coupling resonance

in cyclotrons:

$$v_r - 2v_z = 0$$



horizontal oscillation

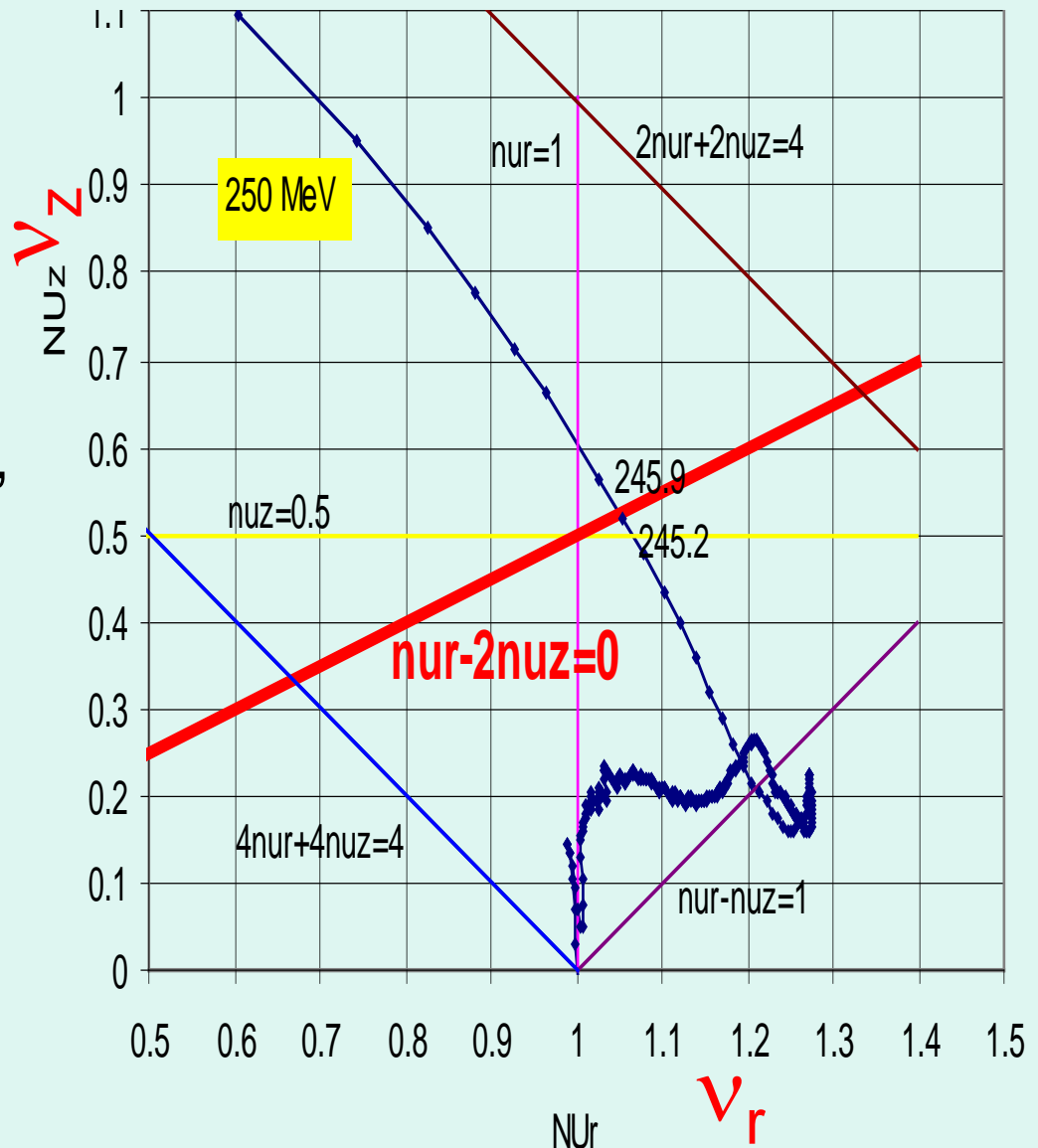
↔ vertical oscillation

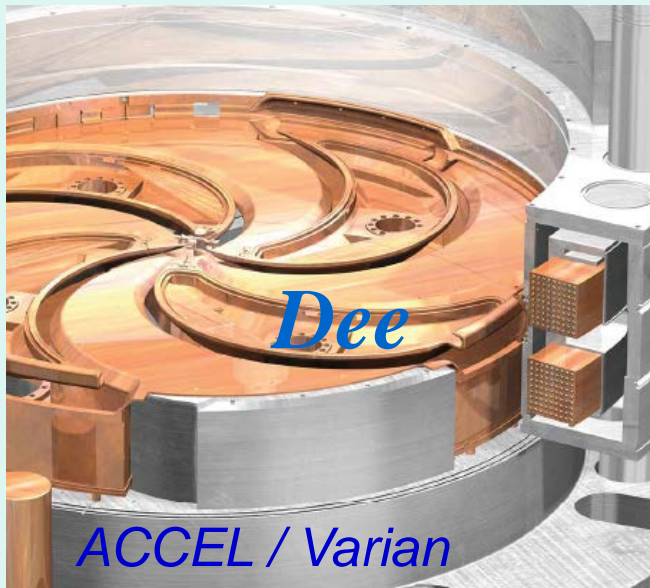
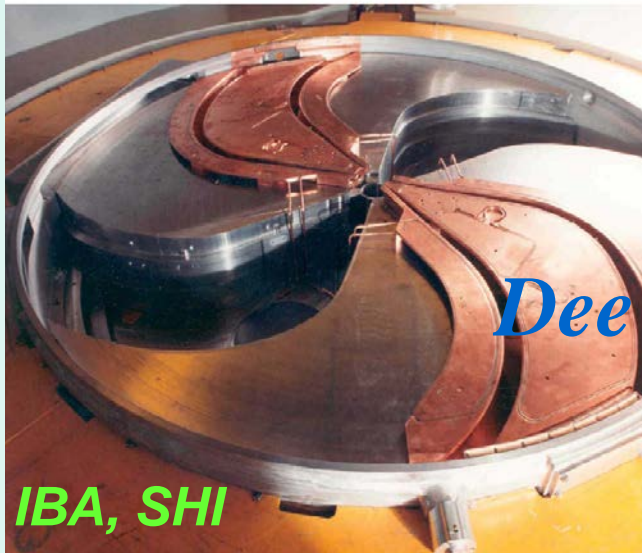
⇒ beam loss

Wilberforce Pendulum - YouTube.flv

$\nu_r(E)$ and $\nu_z(E)$

In a cyclotron, since $n=n(r)$,
the tunes vary during
acceleration





Important parameters:

Frequency: 20-80 MHz

Voltage amplitude on Dee : 30-80 kV

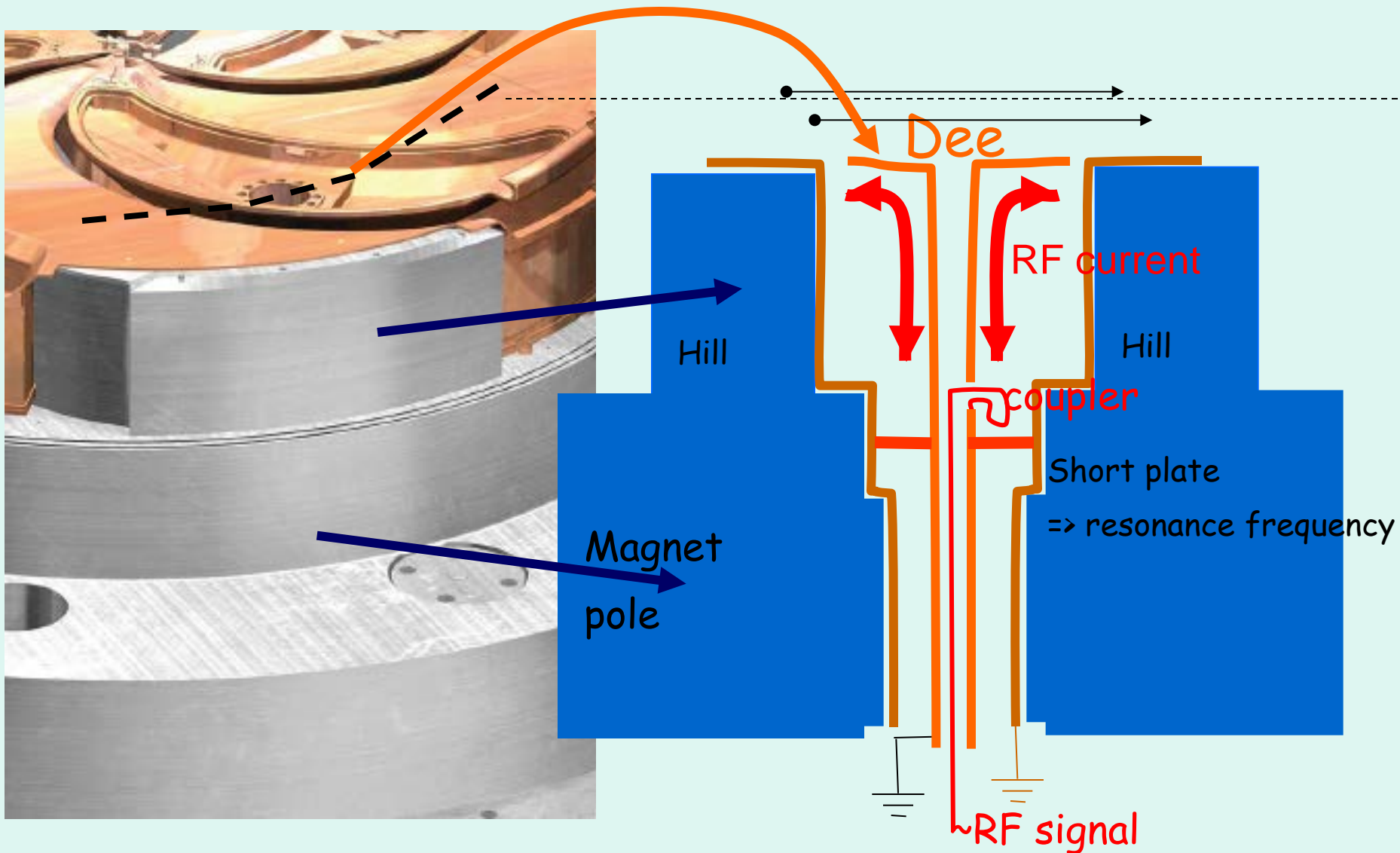
Number of Dee's: 2, 3, 4

Harmonic $h=f_{RF}/f_{orbit}$: 1, 2, ...

⇒ Energy gain per turn

⇒ Orbit separation

⇒ Extraction efficiency



Final energy is independent of V_{RF}

V_{RF} → energy gain dW per turn

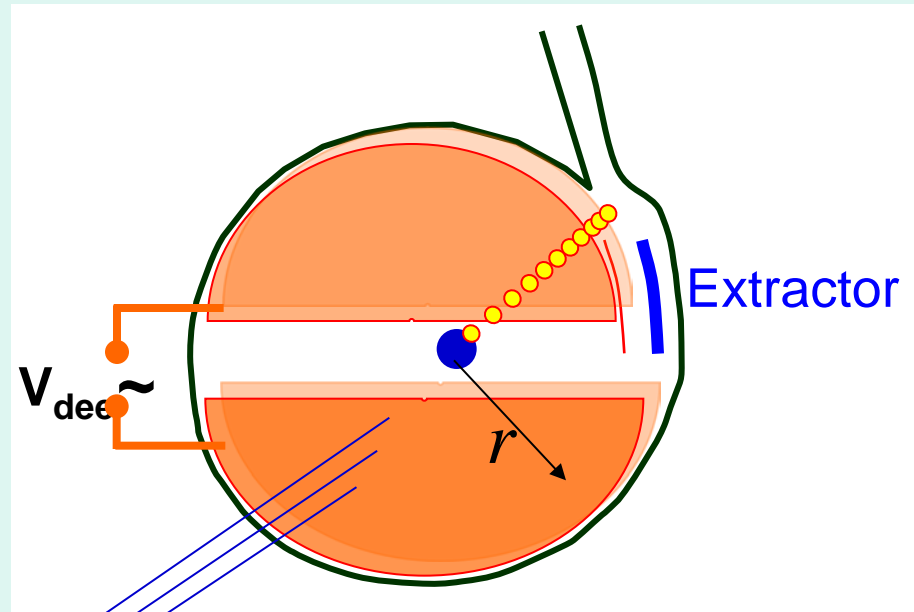
$$dW = N_{gaps} \cdot V_{ORF} \cdot \cos \varphi \quad (= \text{constant if } \varphi \text{ constant})$$

→ Number of turns

$$\frac{dr}{r} = 0.5 \frac{dW}{W} \rightarrow \delta r \propto \frac{1}{r}$$

→ turn separation dr decreases with energy

$$\frac{dr}{dn} = \frac{\gamma}{\gamma + 1} \cdot r \cdot q \cdot n_{cav} V_{dee} \cdot \frac{1}{E} \frac{f^2}{v_r^2}$$



Circular orbits:

Centripetal force = Magnetic force at extraction: $\frac{mv^2}{r} = Bqv$

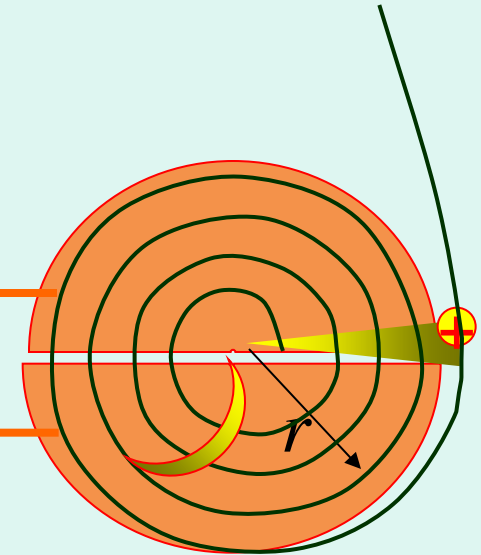
=> Small cyclotron: $r \downarrow$ then B must \uparrow

Cyclotron works while: T_{circle} independent from radius:
(particles move in pace with Vdee)

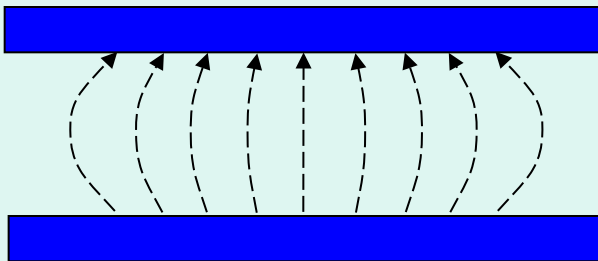
$$T_{circle} = \frac{2\pi \cdot m}{q \cdot B}$$

$$Freq = 1/T_{circle}$$

$$V_{dee} \sim$$



However: at very strong magnetic B-fields:



m = mass
 B = magnetic field
 q = charge

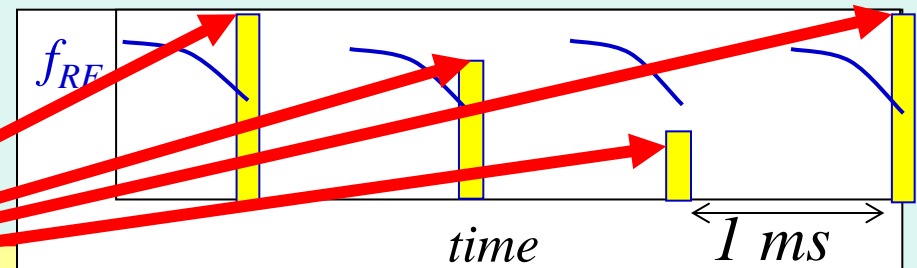
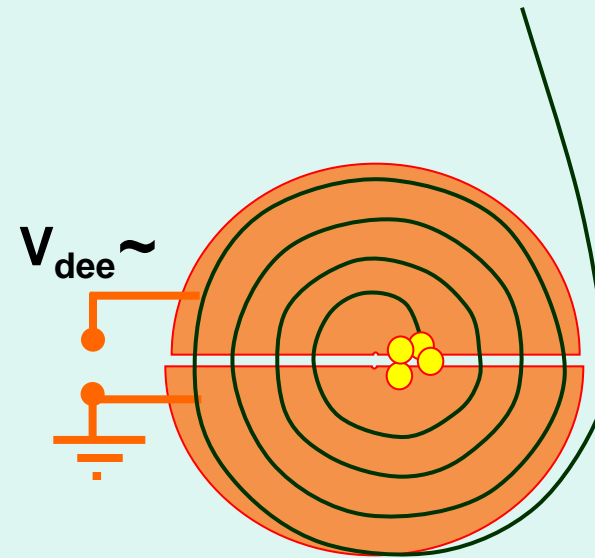
\Rightarrow Magnetic field **decreases** with radius $\Rightarrow T_{circle} \uparrow$
 \Rightarrow particles lose pace with RF.

T_{circle} increases with radius.

$$T = 1/f$$

SO: decrease f_{RF} with radius and extract

Repeat 1000 x per sec



Each pulse: set intensity at source **within ms**

(=> typ 10-30% accuracy)

=> Spot scanning requires >2 pulses per spot.

*Proposal of
H. Blosser, F. Marti, et al., 1989:*

- 250 MeV
- SC, 52 tons, **on a gantry**
- B(0)=5.5 Tesla

H. Blosser, NSCL (~1990):
SC-cyclotron for **neutron therapy**;
30 MeV p, mounted on a gantry in Detroit

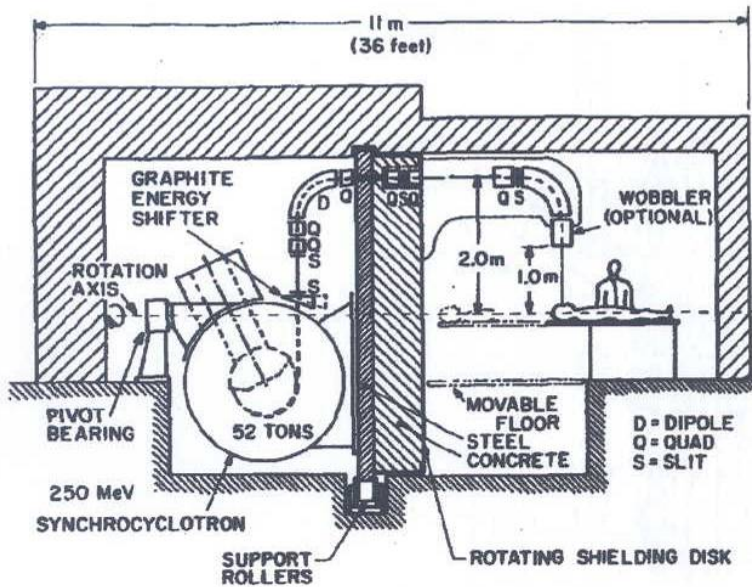


FIG. 9 -- Drawing showing synchrocyclotron rotating gantry arrangement with energy shifting wedge just after the cyclotron. Energy shifting can optionally be accomplished just ahead of the patient.

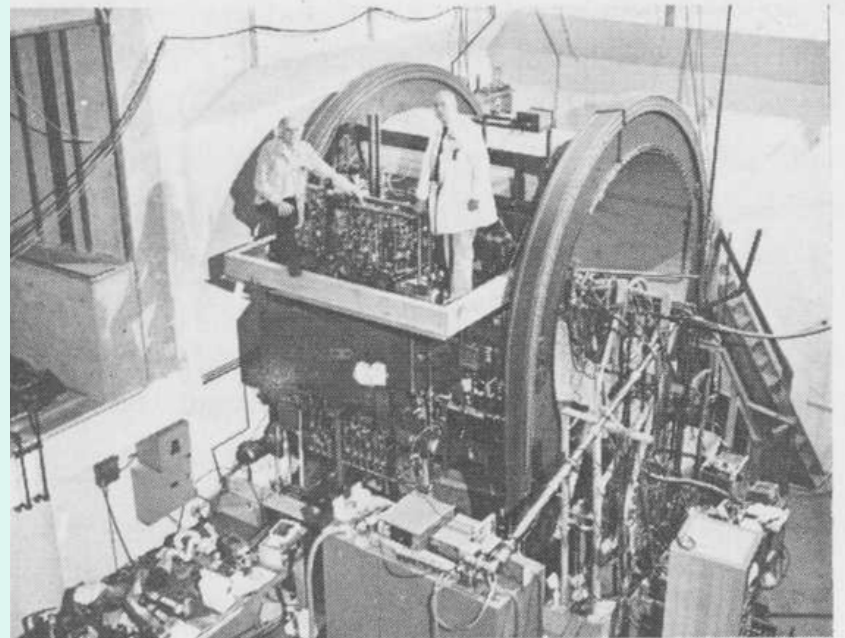


Fig. 2 Photo of the superconducting medical cyclotron on its gantry. Dr. William Powers and



First beam extracted in May 2010

First beam at IBA in 2013

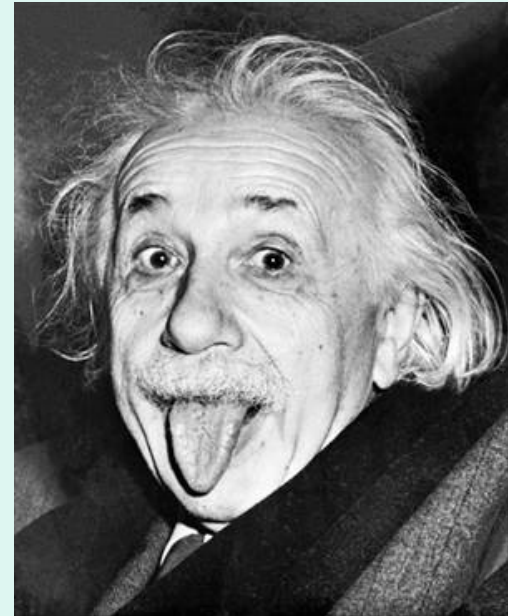
Cyclotron essential: $T_{circle} = \frac{2\pi \cdot m}{Bq} \Rightarrow T_{circle}$ constant for all radii

However, when $v \rightarrow c$: $m = \frac{m_0}{\sqrt{1 - v^2/c^2}} = \gamma \cdot m_0$

e.g: 10 MeV p: $v/c=0.14 \Rightarrow m=1.01 m_0$

250 MeV p: $v/c=0.61 \Rightarrow m=1.27 m_0$

$\Rightarrow T_{circle}$ increases with radius.



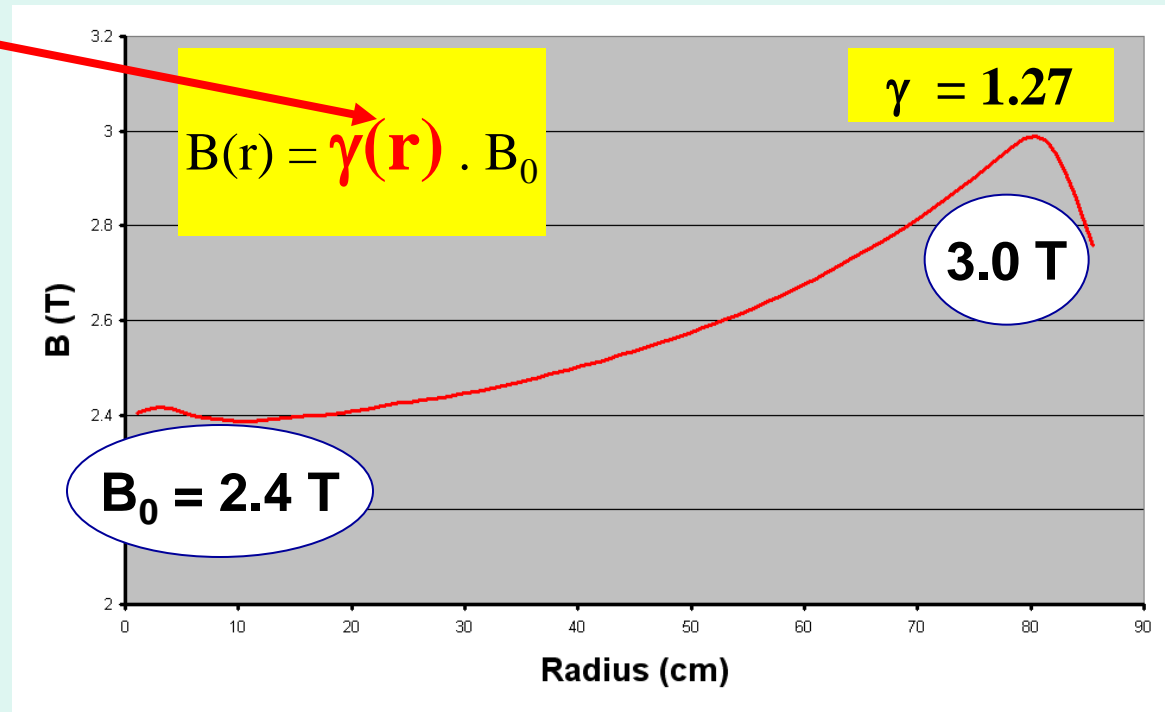
$$T_{circle} = \frac{2\pi \cdot m}{q \cdot B}$$

$$m = \frac{1}{\sqrt{1 - v^2/c^2}} \cdot m_0$$

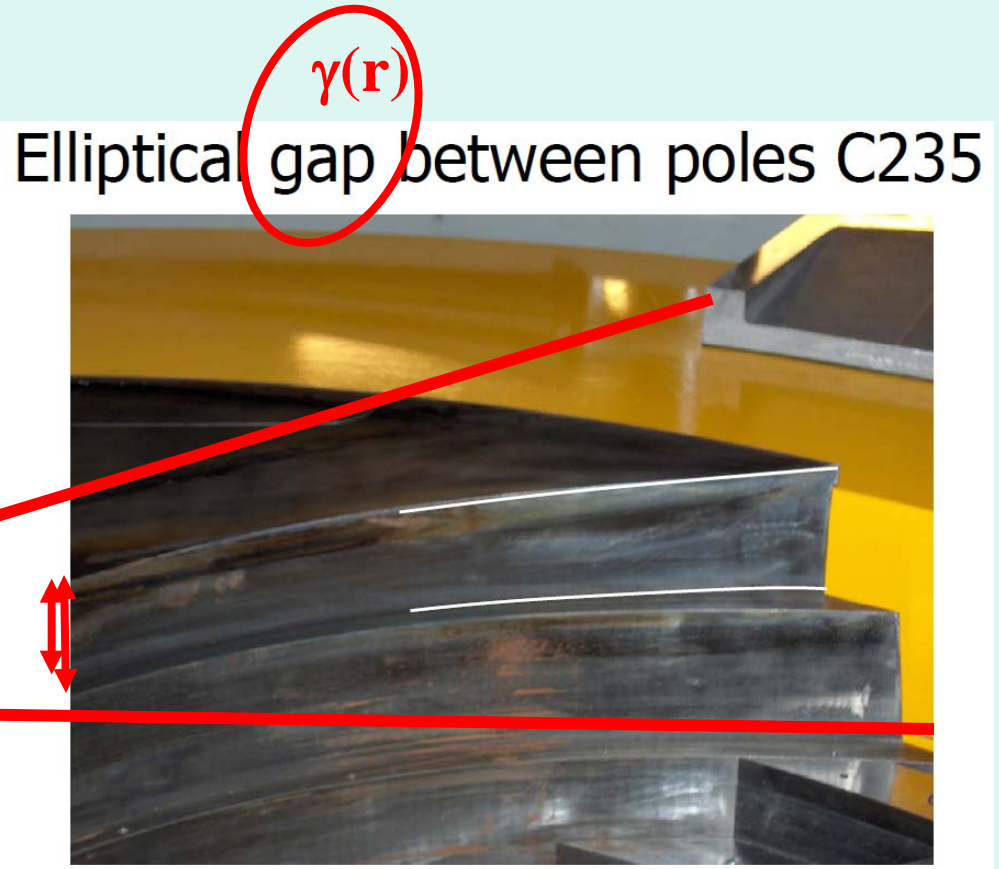
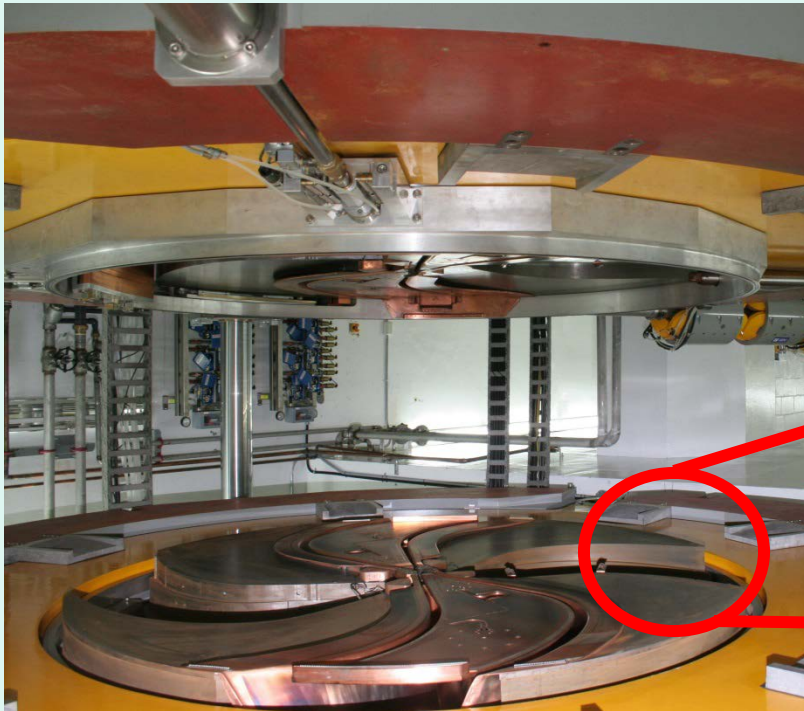
$\gamma(\mathbf{r})$

Remedies when T_{circle} increases with radius:

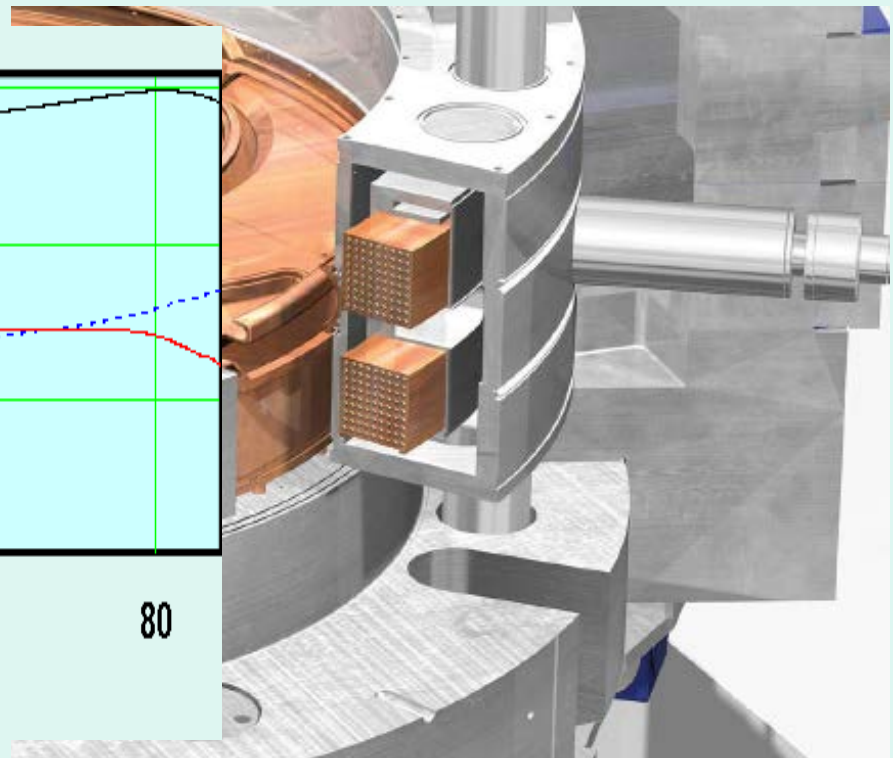
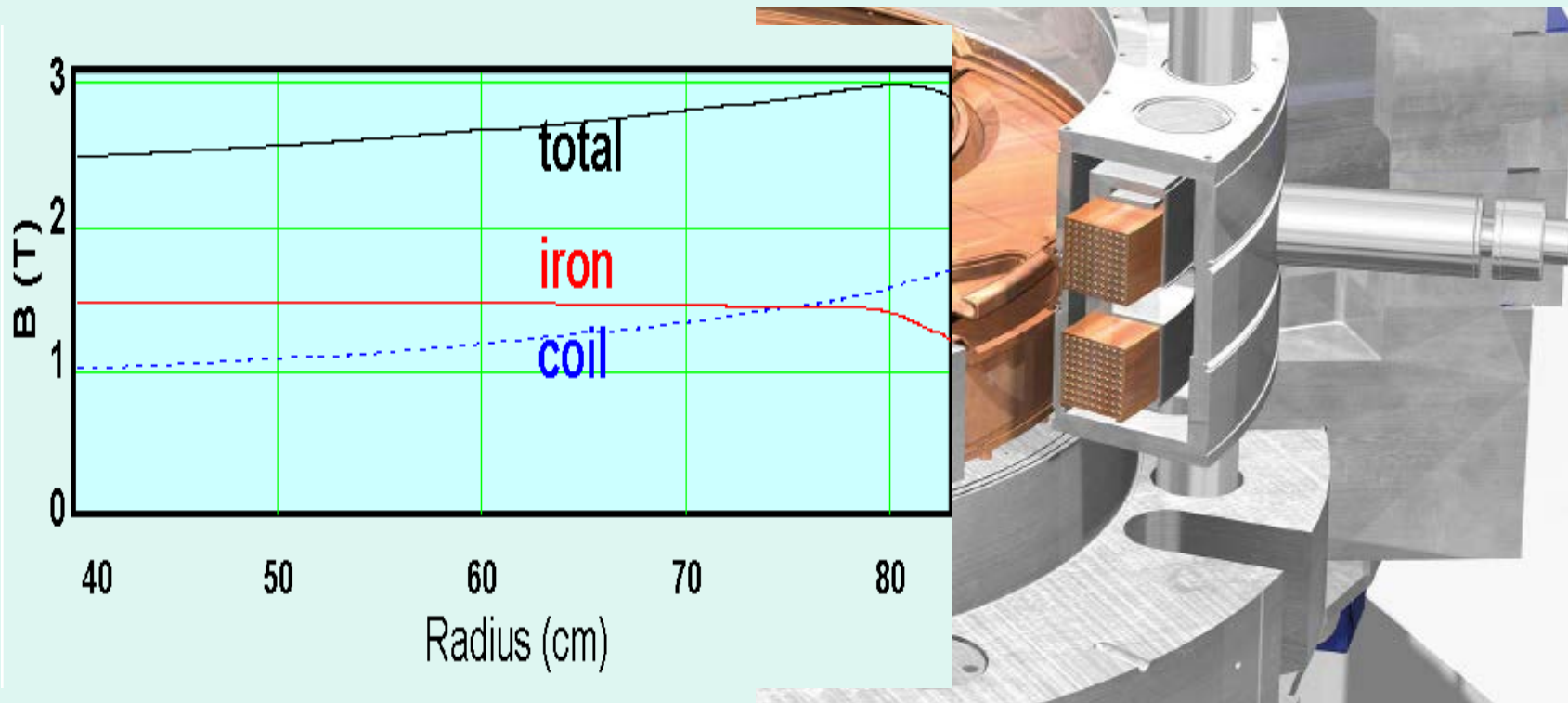
- 1) decrease f_{RF} with radius: *synchro-cyclotron*
- 2) increase B with radius: to compensate m -increase



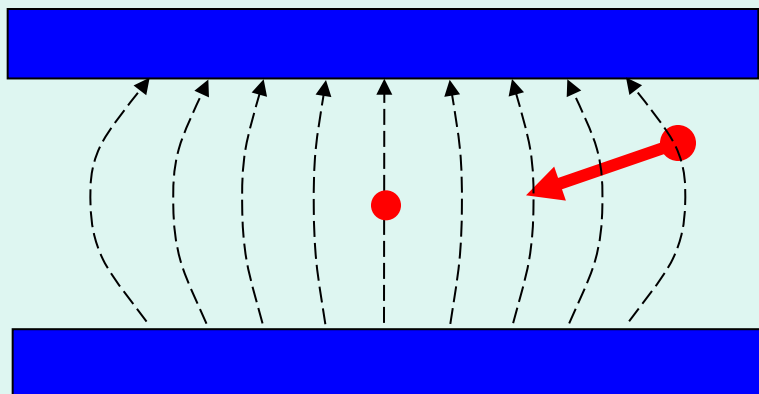
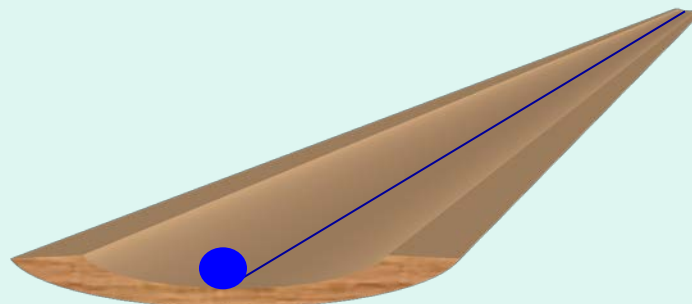
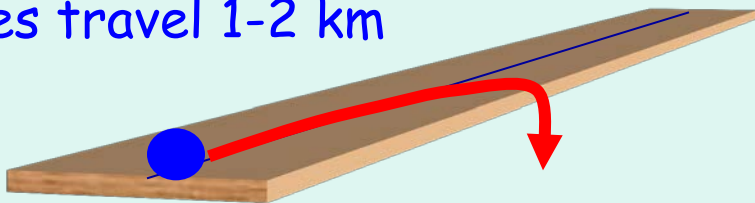
1) Decrease pole gap at large Radius (IBA)



- 2) Use SC coils to employ very strong electric current
 - very strong magnetic field
 - coil field shapes magnetic field (ACCEL / Varian)



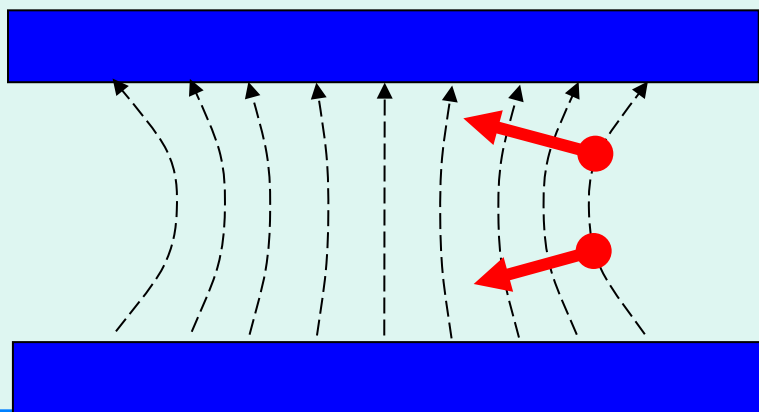
Particles travel 1-2 km



When B **decreases** with radius:

$n > 0 \Rightarrow$ Automatic **vertical stability**

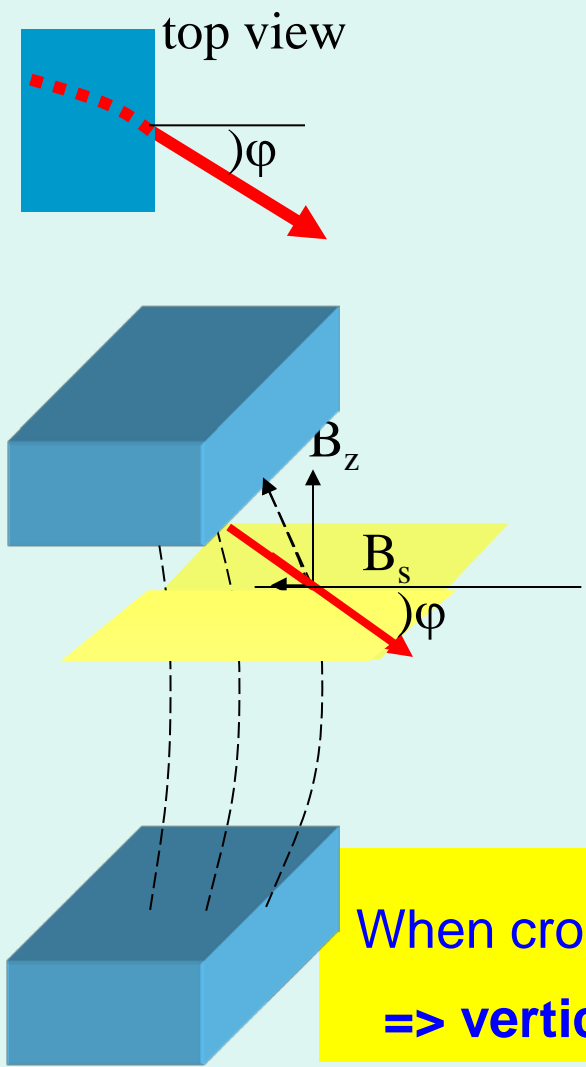
$$(v^2 = n)$$



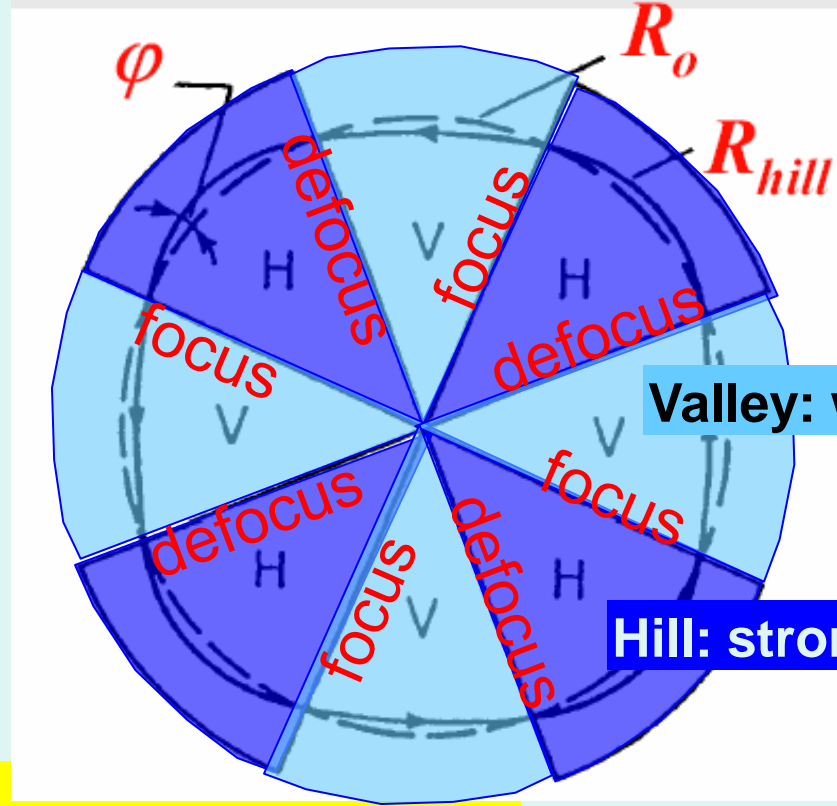
When B **increases** with radius:

$\Rightarrow n < 0 \Rightarrow$ **no vertical stability**





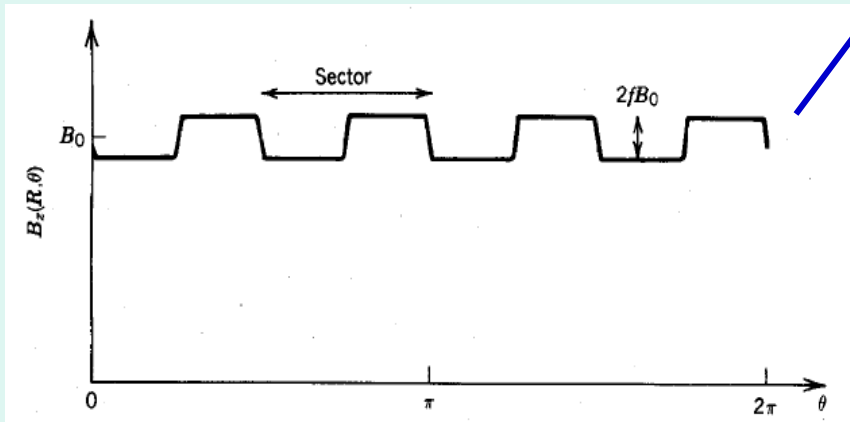
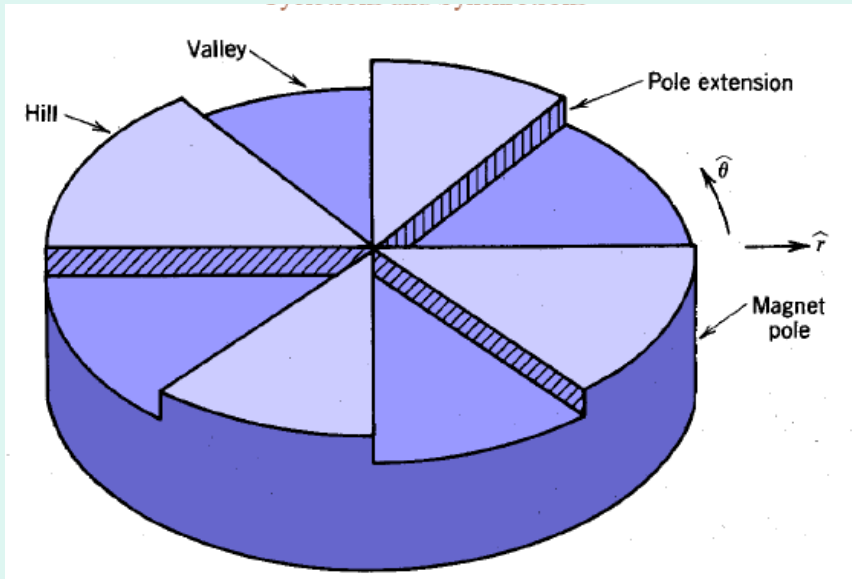
Thomas-Cyclotron (1938)



Valley: weaker field

Hill: strong field

When crossing B-change **not** \perp
 \Rightarrow vertical force from $B_s \times v$



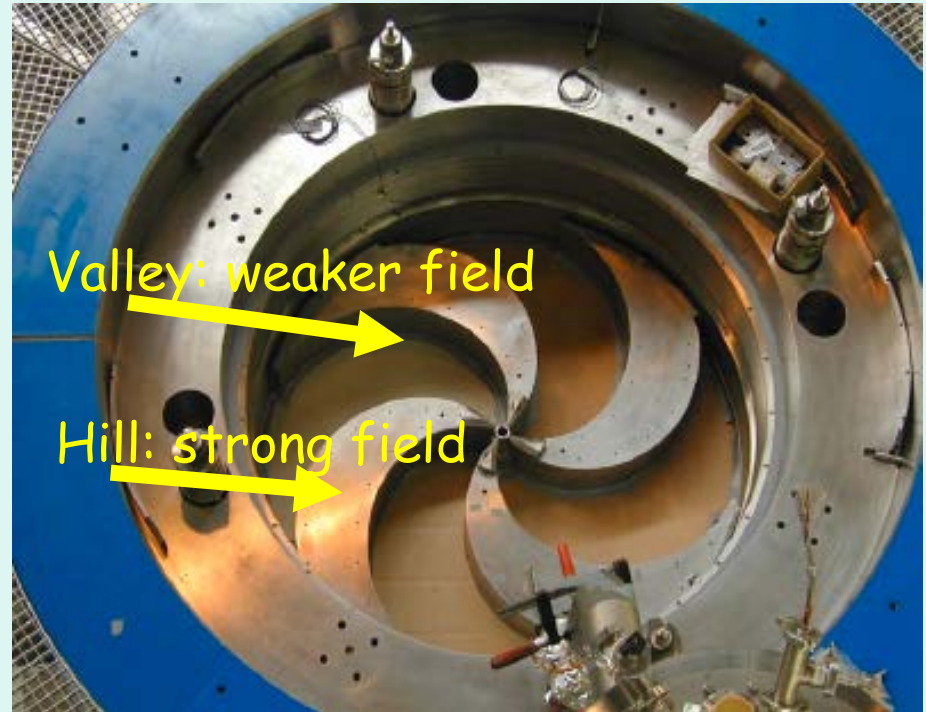
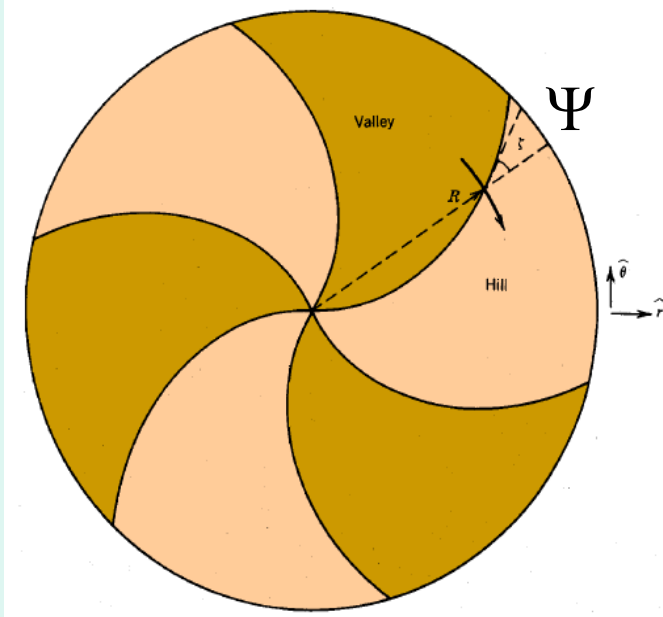
Flutter function:

$$F(r) = \overline{\left(\frac{B(r, \theta) - \overline{B(r)}}{\overline{B(r)}} \right)^2}$$

Thomas focusing:

$$v_z^2(r) = n(r) + F(r)$$

< 0 !

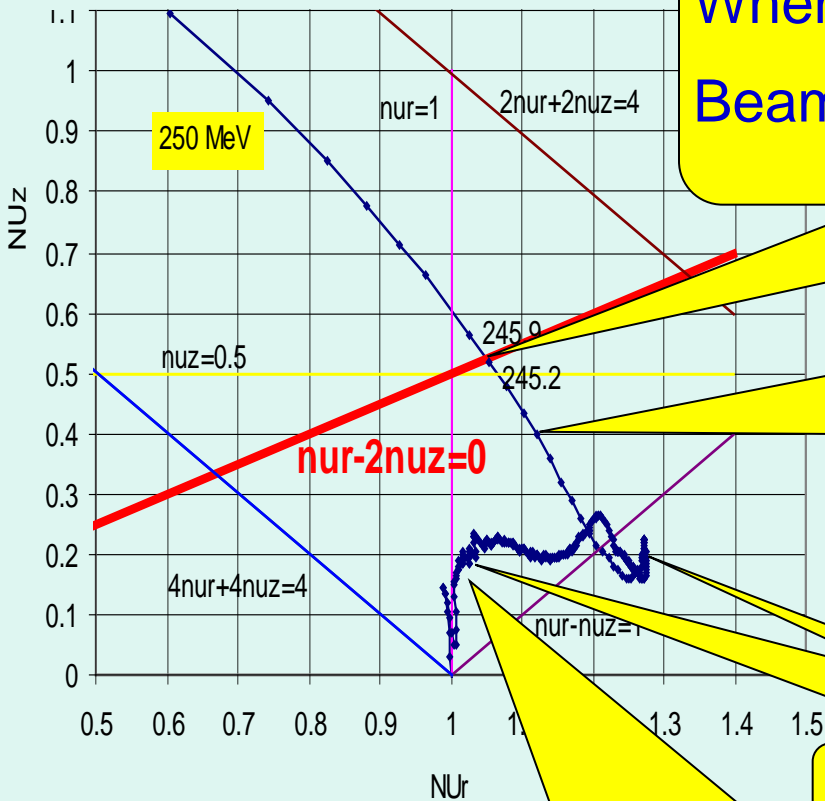


$$v_z^2(R) = n(R) + F(R) \cdot (1 + 2 \tan(\psi(R)))$$

to compensate :

- increasing $B\rho$
- Increasing defocussing by main field

=> increase angle Ψ with radius => spiral

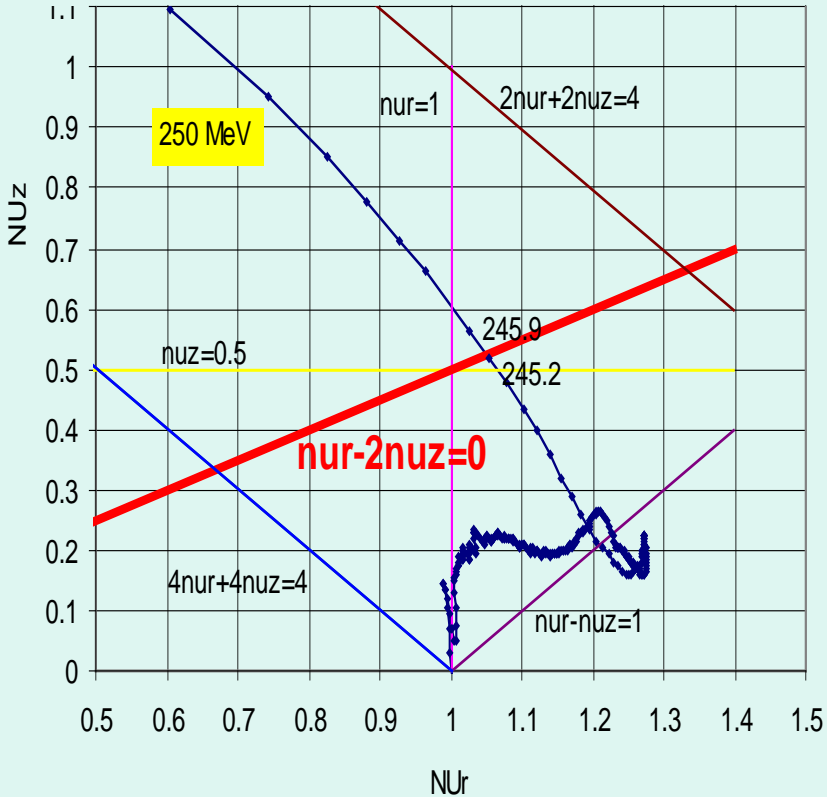


When crossing coupling resonance:
Beam centering reduces hor. betatron ampl.

approaching extraction: field edge
=> strong vertical focusing
=> In few turns towards extraction

$r=10-80$ cm: $v_r(r)$ follows $\gamma(r)$

In central region: homogeneous field
=> No vertical focusing



Design shape of hills such that:

- enough vertical focusing: $\nu_z > 0.15$
- resonances are avoided
- resonances are crossed quickly

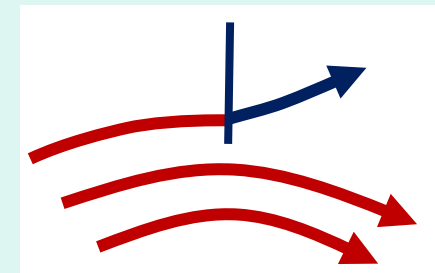
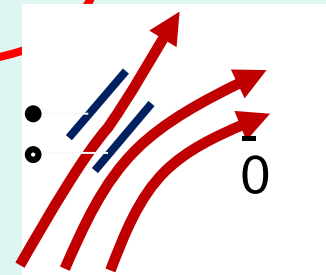
Turn separation $\frac{dr}{dn} = \frac{\gamma}{\gamma + 1} \cdot n \cdot q \cdot n_{cav} \cdot V_{dee} \cdot \frac{1}{E} \cdot \frac{f^2}{v_r^2}$

What will help:

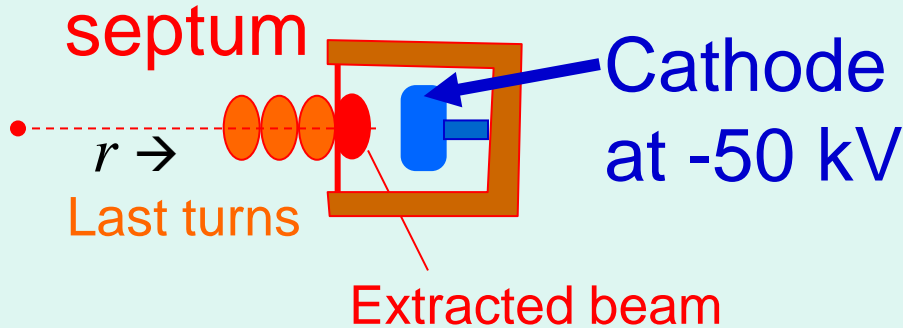
- Large radius of cyclotron
- Many high voltage cavities
- Exploit dropping of v_r (\Rightarrow fast drop of field)

In addition one could:

- Use resonances
and increase betatron amplitude
- Use stripping reactions to change q



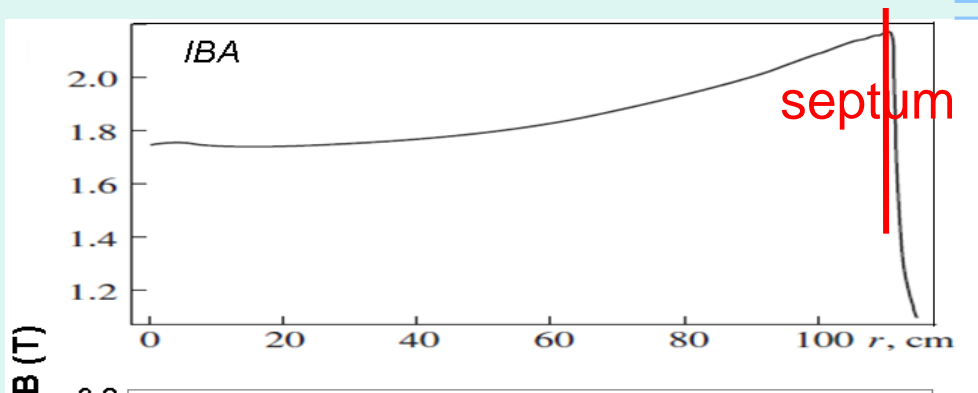
$$\delta r \propto \frac{1}{r}$$



IBA and SHI: elliptical pole gap

⇒ Fast field drop at outer radius

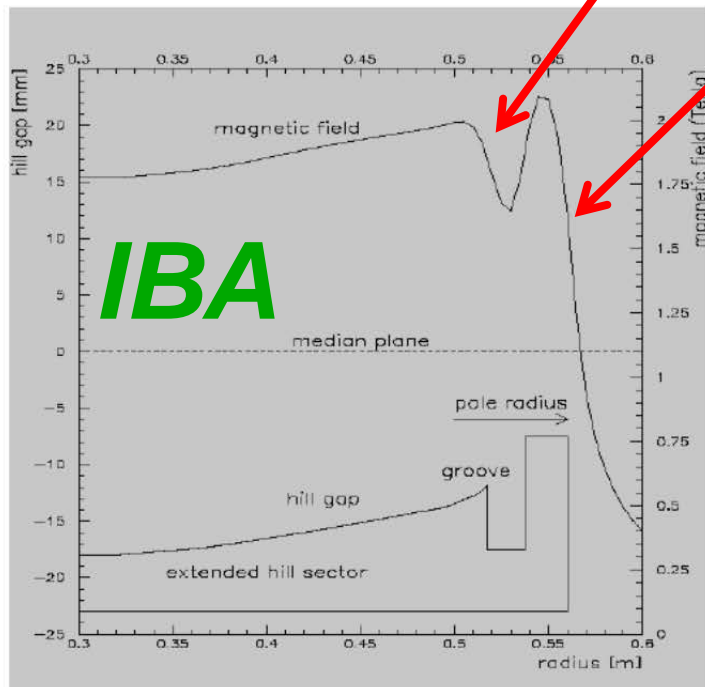
⇒ Cathode + weaker field quickly pull the beam „out“



Self-extraction: Realization *by IBA*

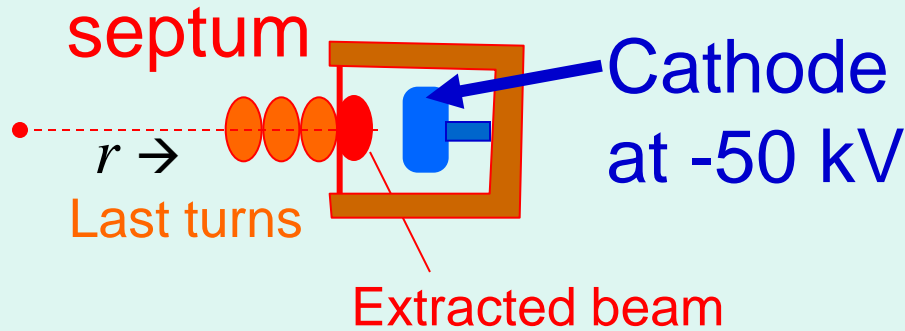
Small elliptical hill gap \Rightarrow allows for sharp radial gradients

‘magnetic septum’ \Rightarrow groove machined in the pole



Pole with groove

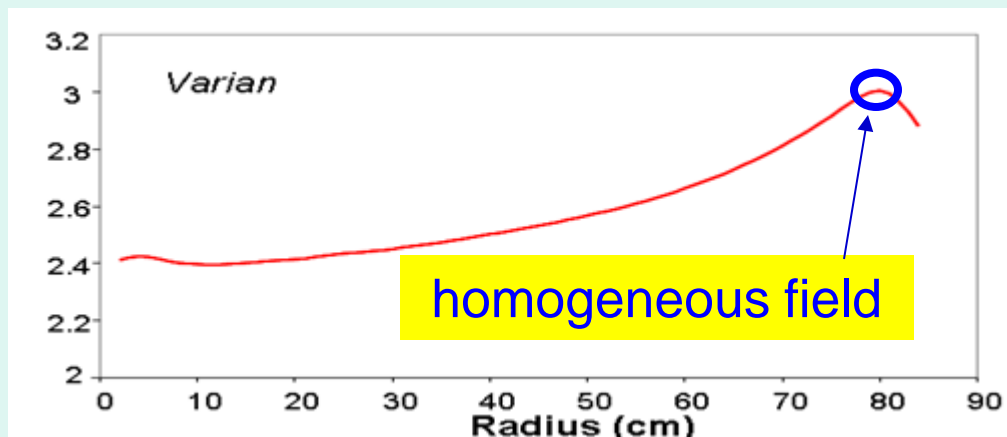




Varian:

flat poles & stronger field

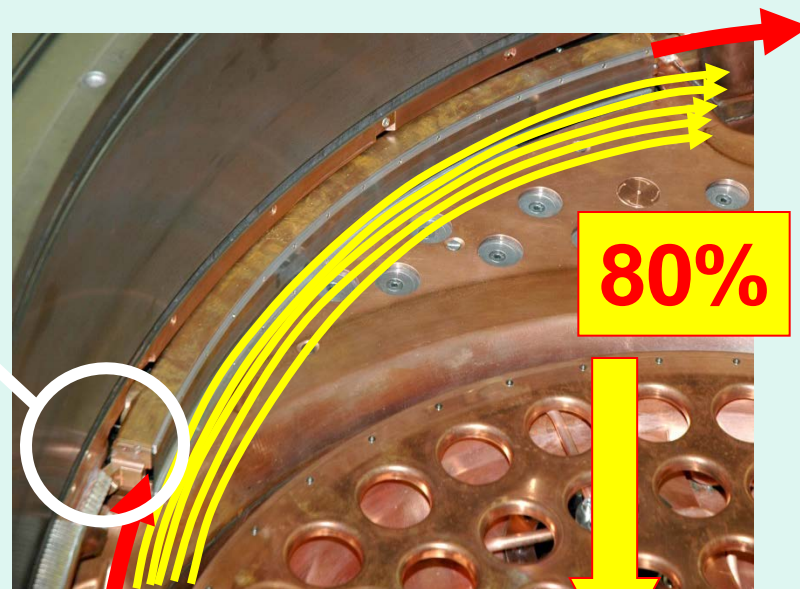
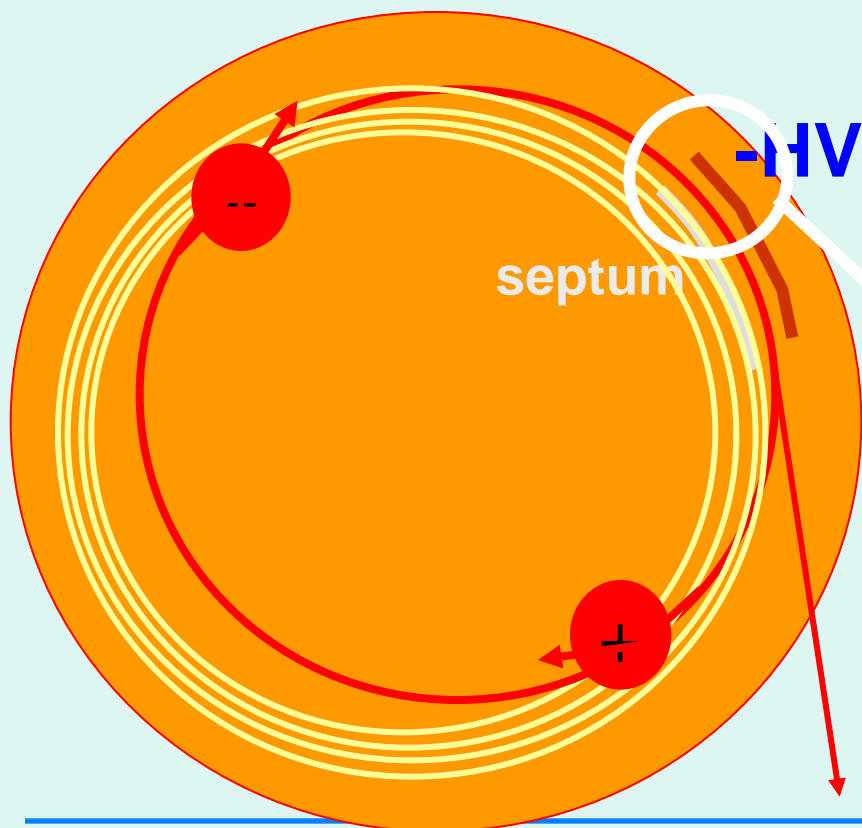
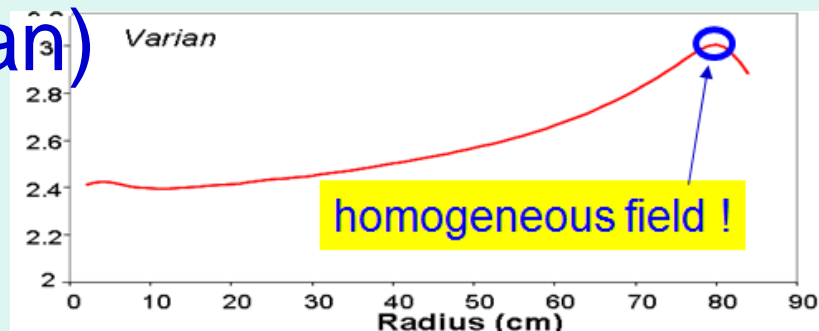
=> Use resonance



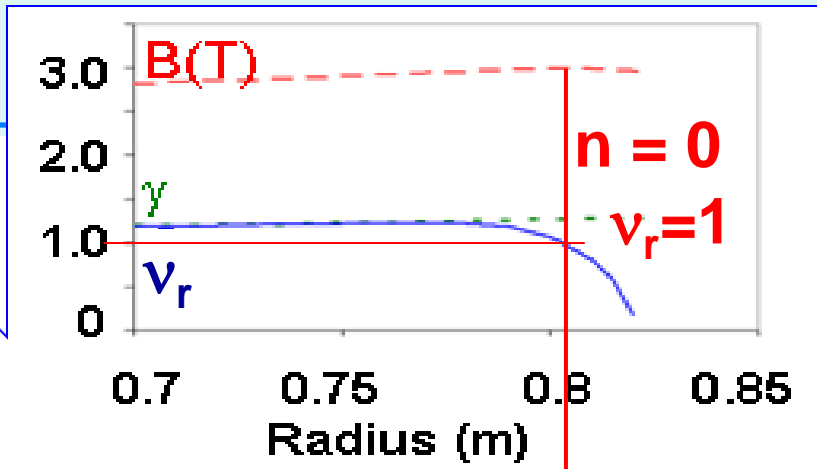
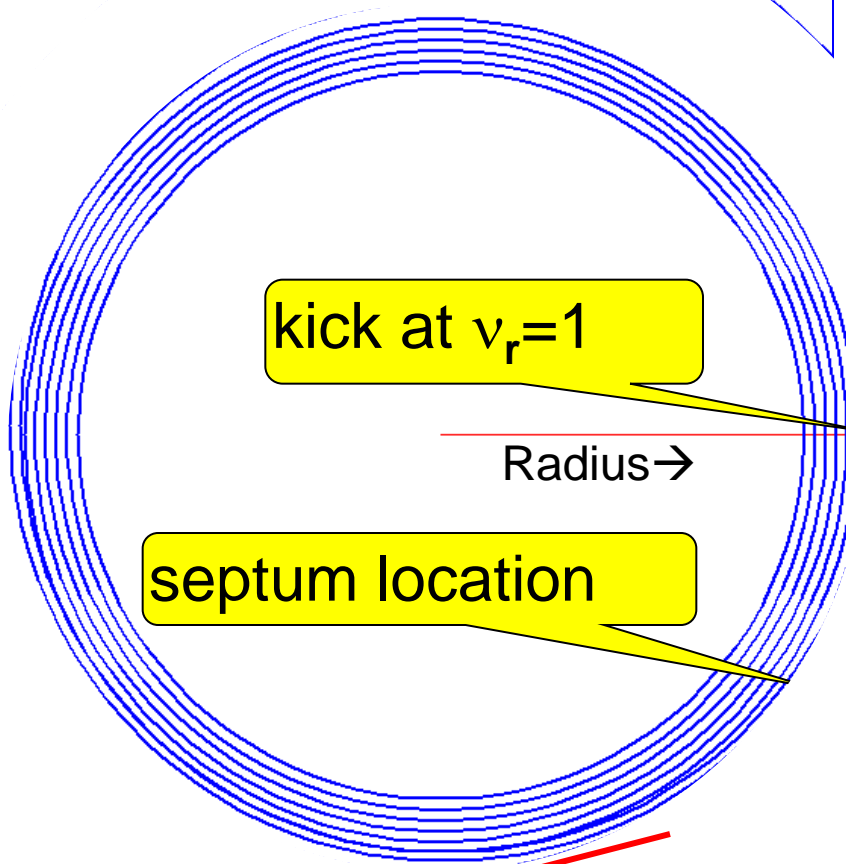
Resonant extraction (Varian)

uses homogeneous field ! $V_r=1$

→ Field bump shifts beam:



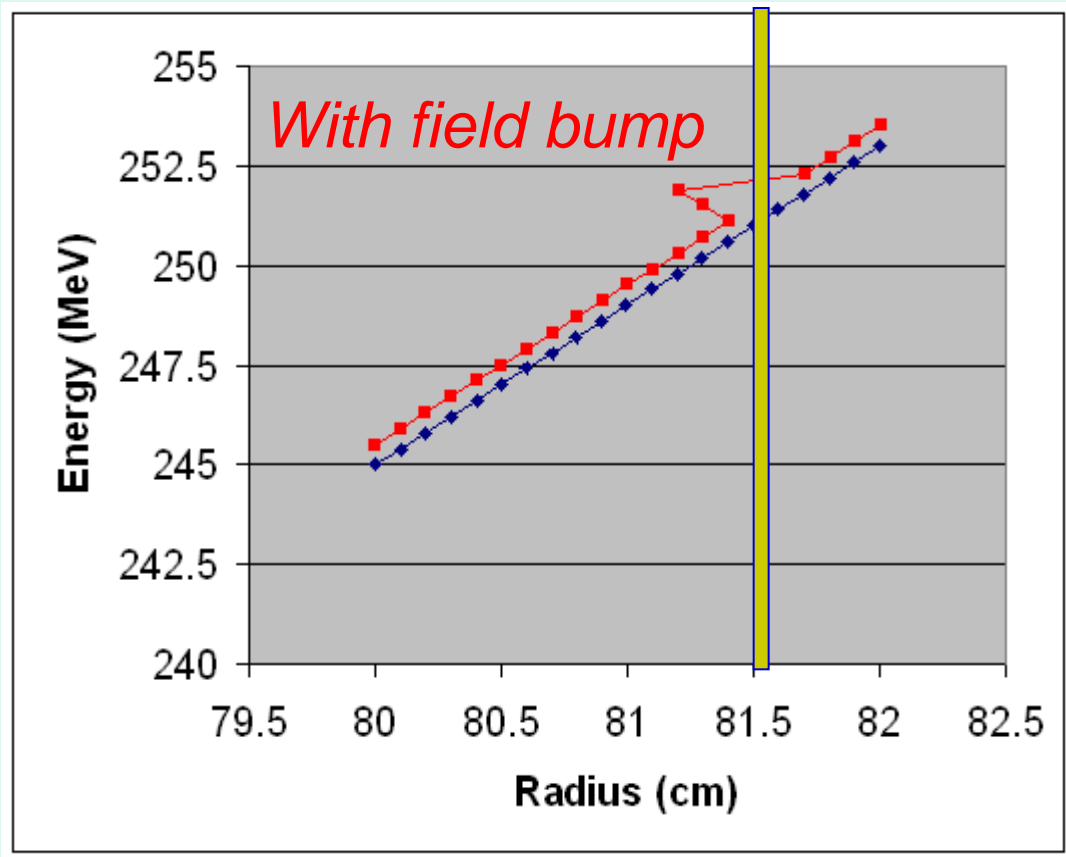
Low radioactivity

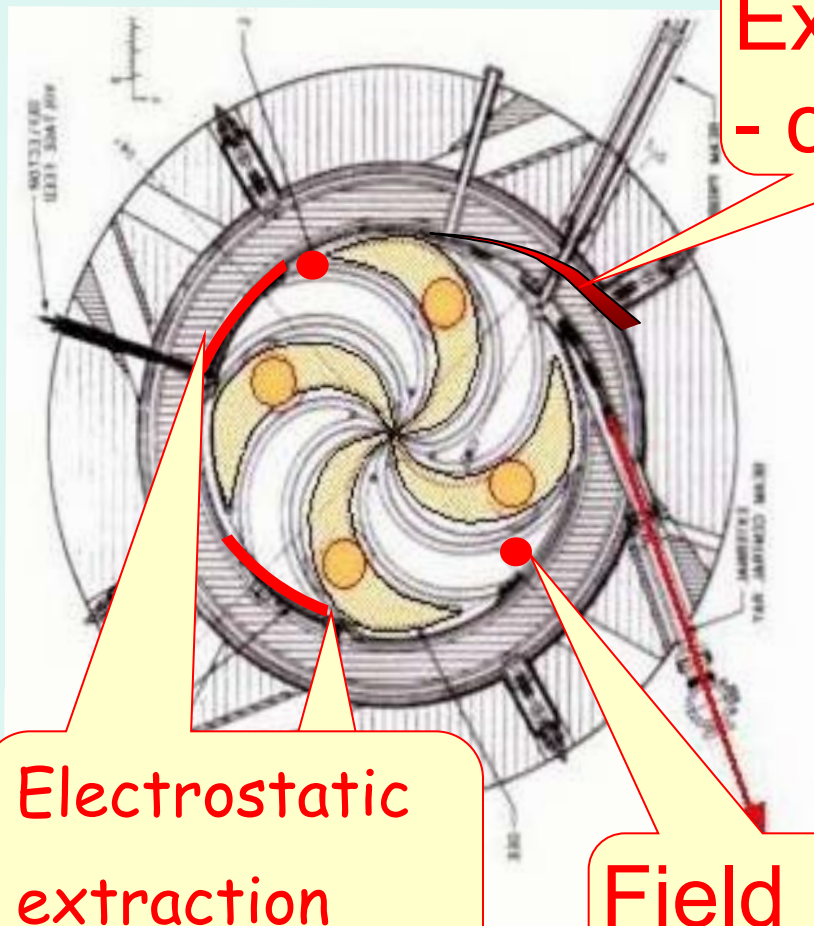


extracted beam

These orbits do not exist (extracted)

resonant extraction





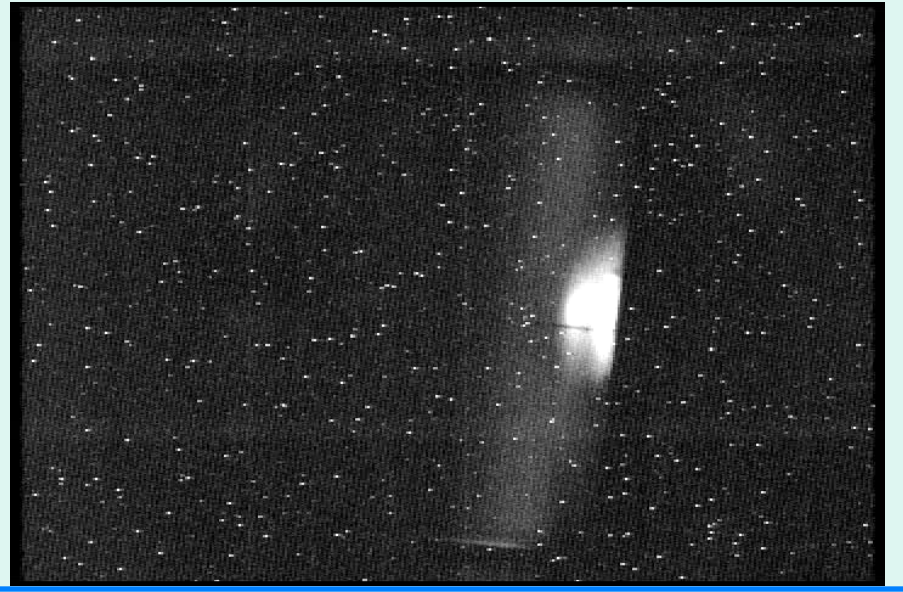
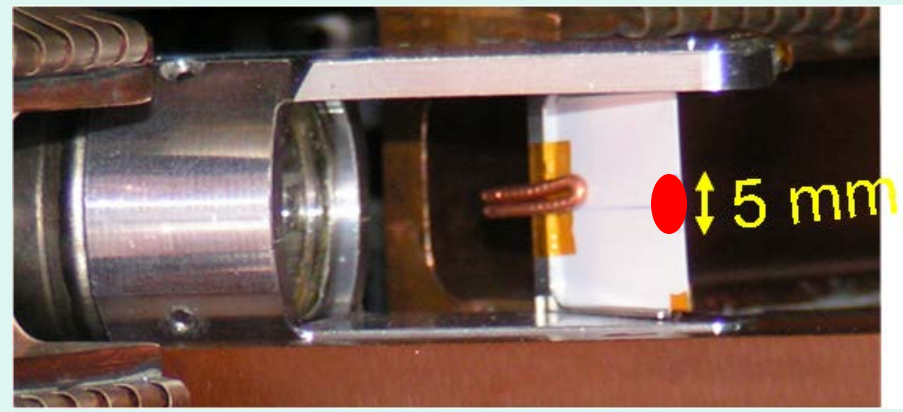
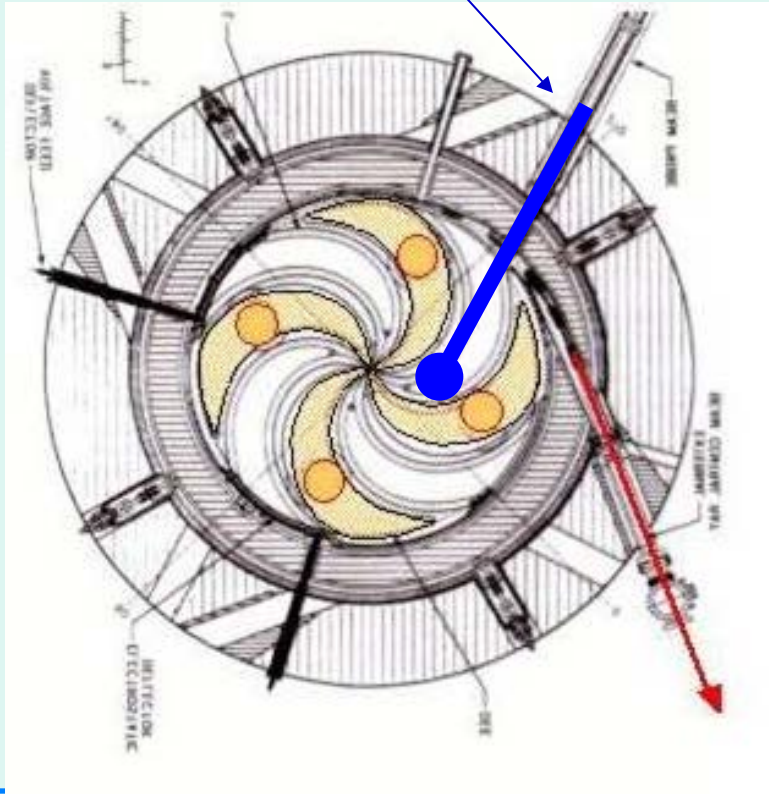
Extraction
- channel

Electrostatic
extraction
elements

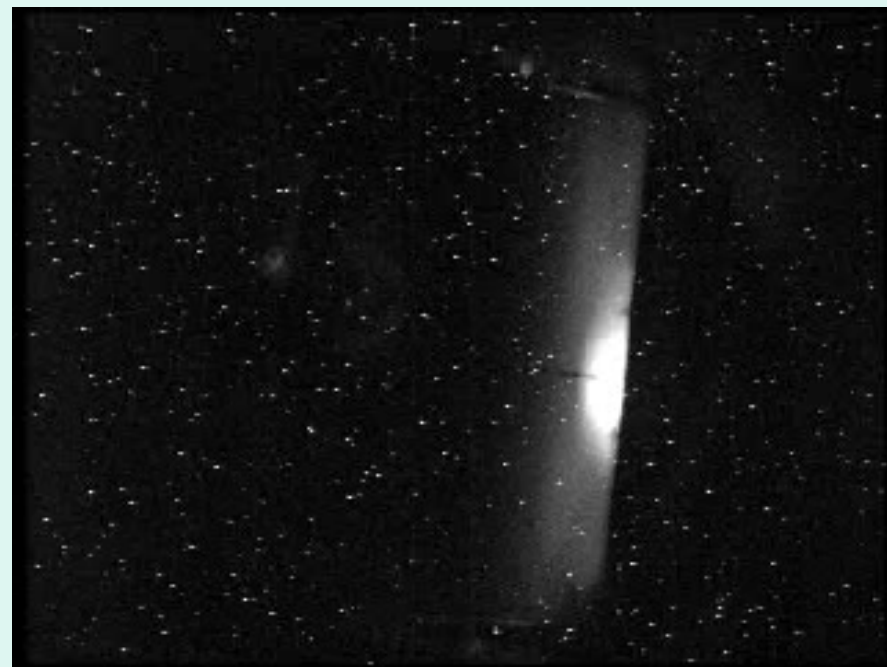
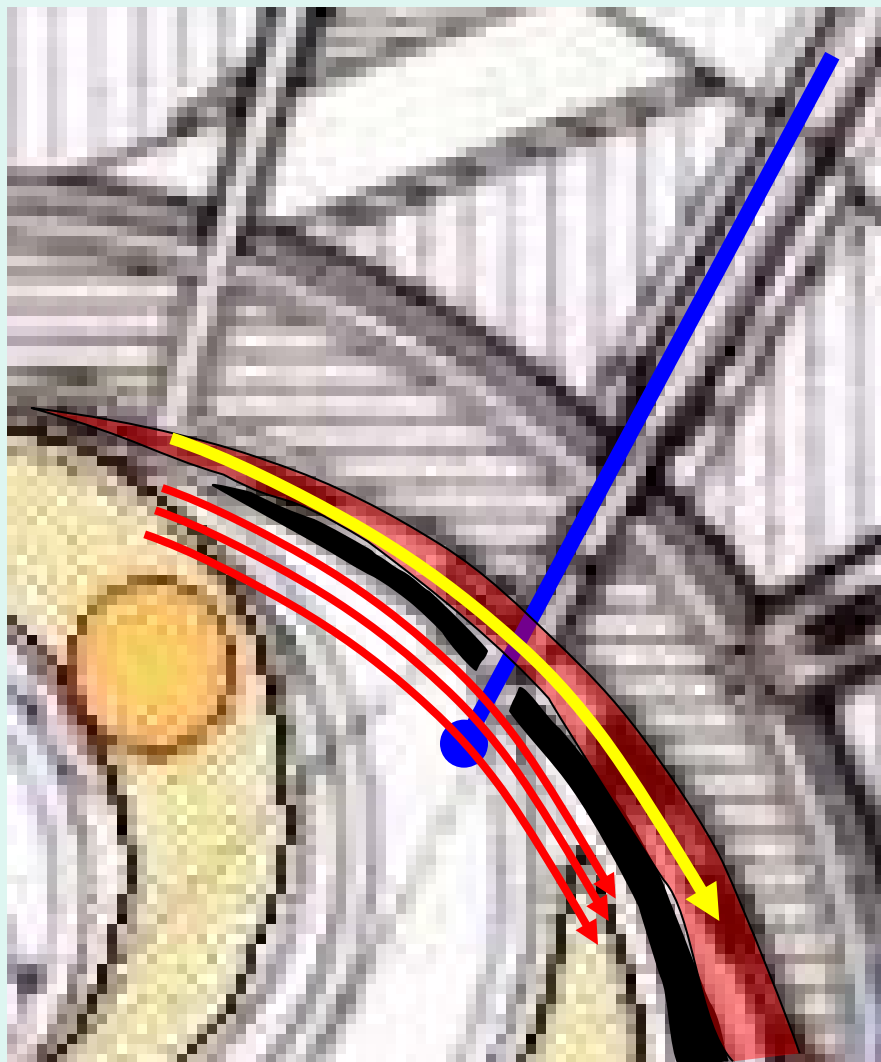
Field
bump

CEL / Varian)

Radial probe with camera + screen



through the extraction channel



After centering

Extraction-roxio1.mpg 0:40

Summary and Conclusions

=> a cyclotron provides:

- continuous beam
- «any» intensity
- very fast adjustable intensity
- accurate intensity control
- great reliability (few components)

+ range change of 5 mm < 100 ms

(with fast degrader and good magnets + power supplies)

Disadvantages: - activation of components near degrader
- no carbon ions (yet)

- Energy + its stability
- Beam size (emittance)
- Beam intensity: structure, stability (kHz) , adjustability (range, speed)
- Extraction efficiency

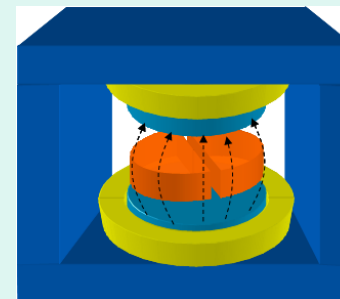
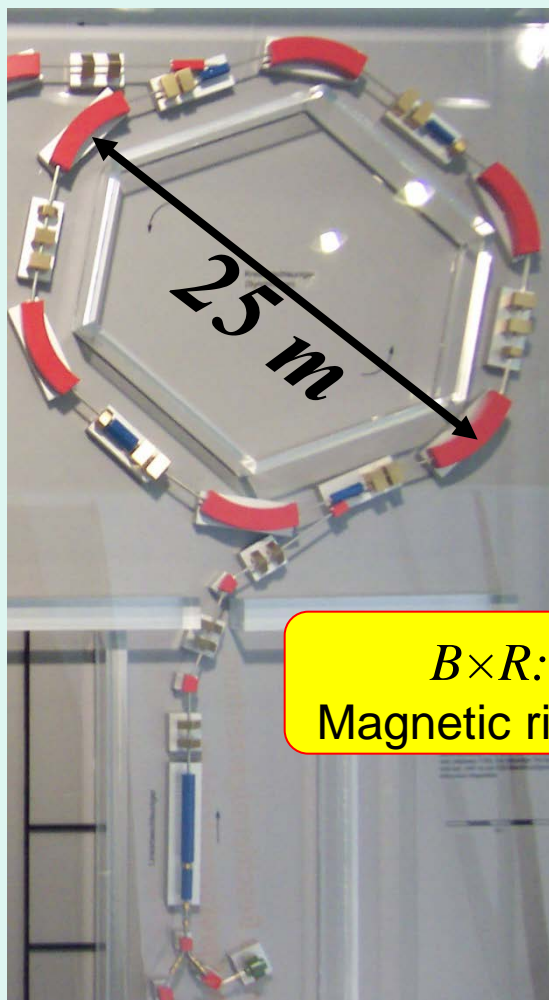
- Reliability
- Needed start up time after „off“ and after „open“
- modular control systems + comprehensive user interface
- Maintenance interval, maintenance time, maintenance effort
- Activation level (person dose per year)

- Ions: time to switch ion species
- Synchro cycl: rep. rate, dose/pulse adjustable (scanning)?

	cyclotron	synchro-cycl
Time structure	continuous	pulsed
Intensity	"any"	low
Size \varnothing	3.5 - 5 m	<2m
Scattering	ok	ok
Spot scanning	ok	>2 pulses/spot
Fast continuous scanning	ok	no



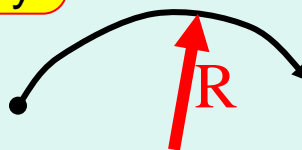




Carbon 6+
(450 MeV/nucl)
6.83 Tm

Proton
(250 MeV)
2.43 Tm

$B \times R$:
Magnetic rigidity



⇒ Cyclotron radius of C is **2.8** x R proton cyclotron
 ⇒ pole area x 2.8^2 = 8 x more iron ⇒ **700-800 tons**

Archade project, Caen (Fr)

Int. Conf. Cyclotron and appl, Tokyo 2004

IBA C400 CYCLOTRON PROJECT FOR HADRON THERAPY

Y. Jongen, M. Abs, W. Beeckman, A. Blondin, W. Kleeven, D. Vandeplassche, S. Zaremba,
IBA, Belgium

V. Aleksandrov, A. Glazov, S. Gurskiy, G. Karamysheva, N. Kazarinov, S. Kostromin,
N. Morozov, E. Samsonov, V. Shevtsov, G. Shirkov, E. Syresin, A. Tuzikov, JINR, Russia.

