

# Conventional Magnets for Accelerators

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# Objectives.

- **The presentation deals with d.c. magnets only.**
- **It includes some material presented at the ‘introductory’ level CAS meetings.**
- **However, additional material emphasises the judgement of magnetic quality in design and manufacture.**

# Contents:

## **i) No current or steel:**

- Laplace's equation with scalar potential;
- Cylindrical harmonic solutions in two dimensions;

## **ii) Introduce steel yoke:**

- Ideal pole shapes for dipole, quad and sextupole;
- Field harmonics-symmetry restraints and significance;

## **iii) Introduce current:**

- Ampere-turns in dipole, quad and sextupole;

# Contents (cont.)

## **iv) Magnet geometry:**

- Yoke and coil geometry- 'C', 'H' and 'window frame' designs; designs;

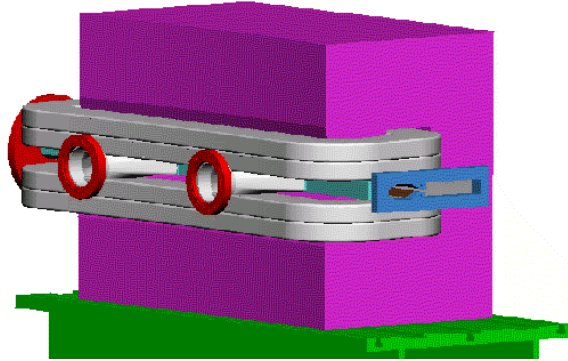
## **v) Field computation and pole optimisation:**

- Field computation techniques;
- Design of pole geometry for dipole, quad and sextupole;

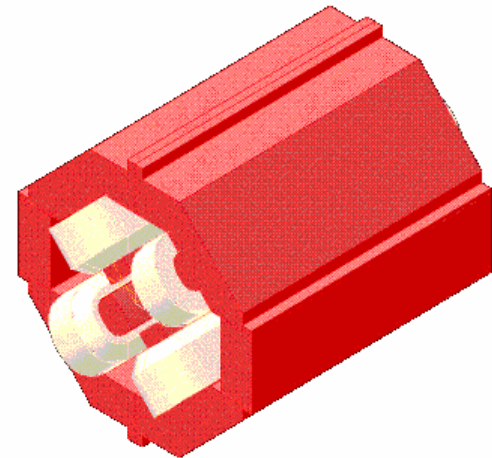
## **v) Judgement of field quality during design and after manufacture.**

# Magnets we know about:

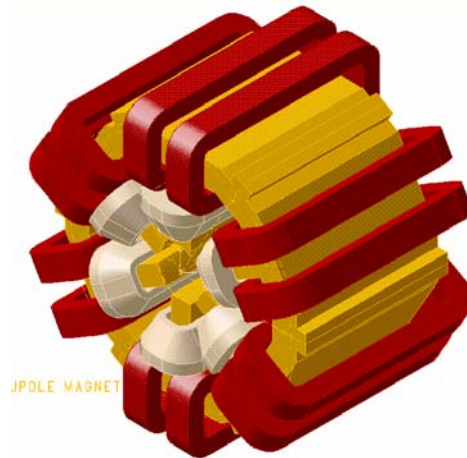
Dipoles to bend the beam:



Quadrupoles to focus it:



Sextupoles to correct chromaticity:  
chromaticity:



**We need to establish a formal approach to describing these magnets.**

# But first – nomenclature!

**Magnetic Field:** (the magneto-motive force produced by electric currents)

symbol is  $\mathbf{H}$  (as a vector);

units are Amps/metre in S.I units (Oersteds in cgs);

**Magnetic Induction or Flux Density:** (the density of magnetic flux driven through a medium by the magnetic field)

symbol is  $\mathbf{B}$  (as a vector);

units are Tesla (Webers/m<sup>2</sup> in mks, Gauss in cgs);

**Note:** induction is frequently referred to as "Magnetic Field".

**Permeability of free space:**

symbol is  $\mu_0$  ;

units are Henries/metre;

**Permeability** (abbreviation of **relative permeability**):

symbol is  $\mu$ ;

the quantity is dimensionless;

# No Currents - Maxwell's equations:

$$\underline{\nabla} \cdot \underline{\mathbf{B}} = 0 ;$$

$$\underline{\nabla} \times \underline{\mathbf{H}} = \underline{\mathbf{j}} ;$$

In the absence of currents:  $\underline{\mathbf{j}} = 0$ .

Then we can put:  $\underline{\mathbf{B}} = - \underline{\nabla} \phi$

So that:  $\underline{\nabla}^2 \phi = 0$  (Laplace's equation).

Taking the two dimensional case (ie constant in the z direction) and solving for cylindrical coordinates (r,θ):

$$\phi = (E+F \theta)(G+H \ln r) + \sum_{n=1}^{\infty} (J_n r^n \cos n\theta + K_n r^n \sin n\theta + L_n r^{-n} \cos n \theta + M_n r^{-n} \sin n \theta )$$

# In practical situations:

The scalar potential simplifies to:

$$\phi = \sum_n (J_n r^n \cos n\theta + K_n r^n \sin n\theta),$$

with  $n$  integral and  $J_n, K_n$  a function of geometry.

Giving components of flux density:

$$\begin{aligned} B_r &= - \sum_n (n J_n r^{n-1} \cos n\theta + n K_n r^{n-1} \sin n\theta) \\ B_\theta &= - \sum_n (-n J_n r^{n-1} \sin n\theta + n K_n r^{n-1} \cos n\theta) \end{aligned}$$



# Significance

This is an infinite series of cylindrical harmonics; they define the allowed distributions of  $\mathbf{B}$  in 2 dimensions in the absence of currents within the domain of  $(r, \theta)$ .

Distributions not given by above are not physically realisable.

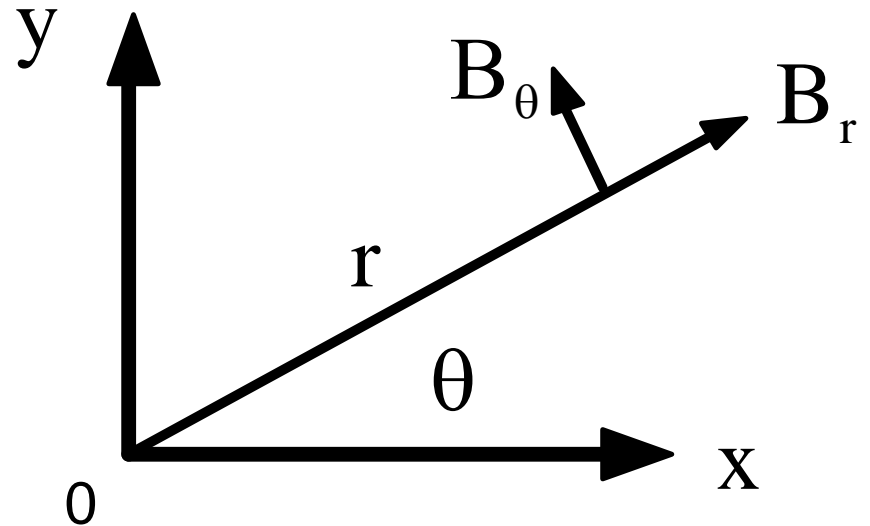
Coefficients  $J_n, K_n$  are determined by geometry (iron boundaries or remote current sources).

# Cartesian Coordinates

In Cartesian coordinates, the components are given by:

$$B_x = B_r \cos \theta - B_\theta \sin \theta,$$

$$B_y = B_r \sin \theta + B_\theta \cos \theta,$$



# Dipole field: $n = 1$

## Cylindrical:

$$B_r = J_1 \cos \theta + K_1 \sin \theta;$$

$$B_\theta = -J_1 \sin \theta + K_1 \cos \theta;$$

$$\phi = J_1 r \cos \theta + K_1 r \sin \theta.$$

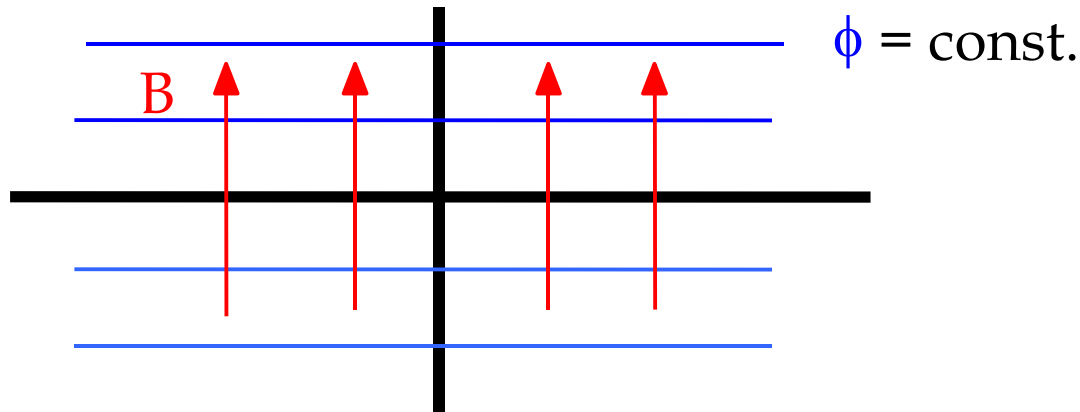
## Cartesian:

$$B_x = J_1$$

$$B_y = K_1$$

$$\phi = J_1 x + K_1 y$$

So,  $J_1 = 0$  gives vertical dipole field:



$K_1 = 0$  gives  
horizontal  
dipole field.

# Quadrupole field: $n = 2$

## Cylindrical:

$$B_r = 2 J_2 r \cos 2\theta + 2K_2 r \sin 2\theta;$$

$$B_\theta = -2J_2 r \sin 2\theta + 2K_2 r \cos 2\theta;$$

$$\phi = J_2 r^2 \cos 2\theta + K_2 r^2 \sin 2\theta;$$

## Cartesian:

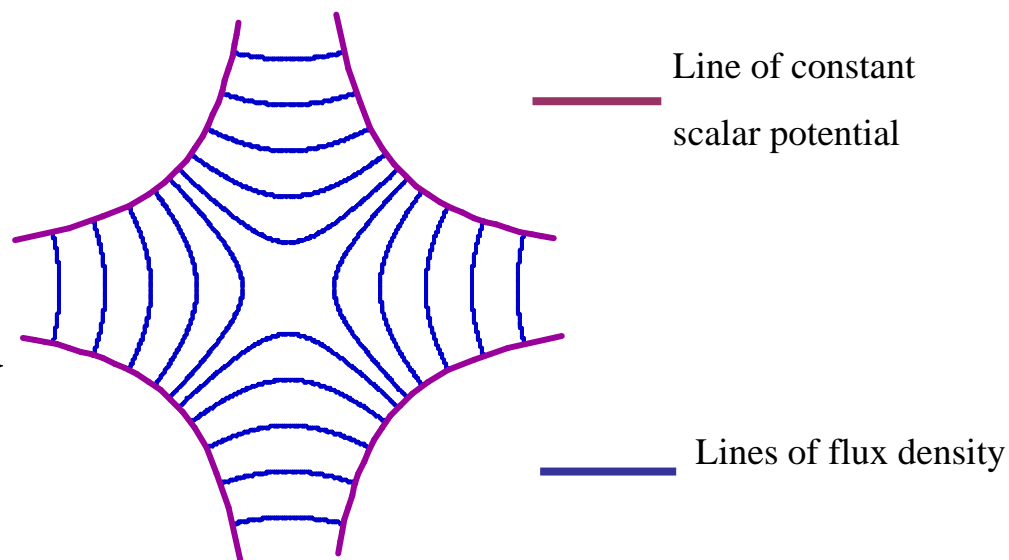
$$B_x = 2 (J_2 x + K_2 y)$$

$$B_y = 2 (-J_2 y + K_2 x)$$

$$\phi = J_2 (x^2 - y^2) + 2K_2 xy$$

$J_2 = 0$  gives 'normal' or 'right' quadrupole field.

$K_2 = 0$  gives 'skew' quadrupole fields (above rotated by  $\pi/4$ ).



# Sextupole field: $n = 3$

## Cylindrical;

$$B_r = 3 J_3 r^2 \cos 3\theta + 3K_3 r^2 \sin 3\theta;$$

$$B_\theta = -3J_3 r^2 \sin 3\theta + 3K_3 r^2 \cos 3\theta;$$

$$\phi = J_3 r^3 \cos 3\theta + K_3 r^3 \sin 3\theta;$$

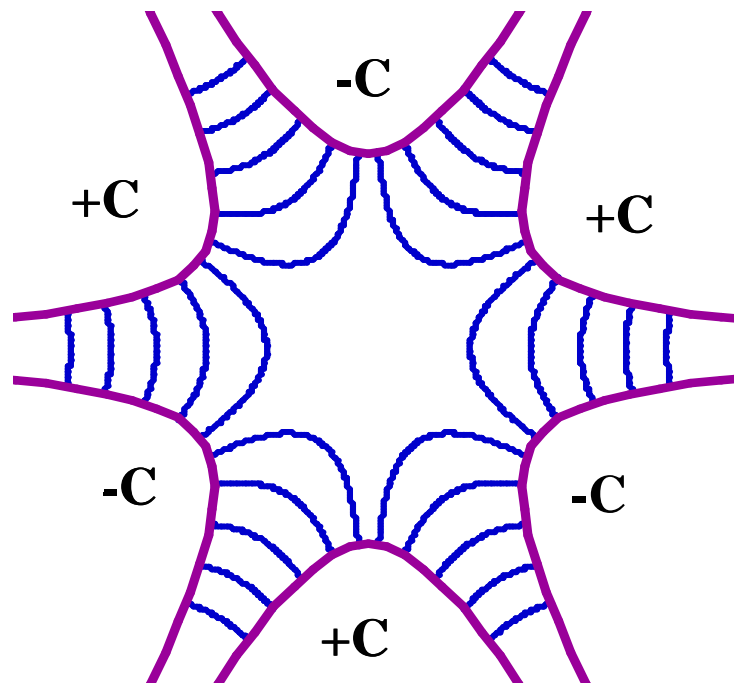
## Cartesian:



$$B_x = 3 \{ J_3 (x^2 - y^2) + 2K_3 yx \}$$

$$B_y = 3 \{ -2 J_3 xy + K_3 (x^2 - y^2) \}$$

$$\phi = J_3 (x^3 - 3y^2x) + K_3 (3yx^2 - y^3)$$

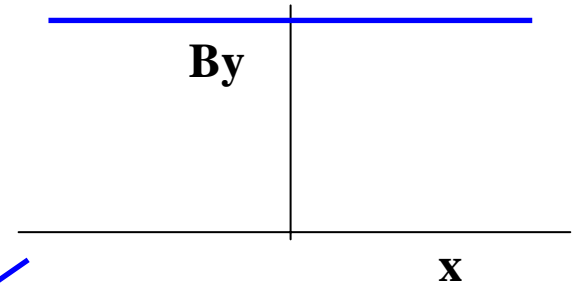
$J_3 = 0$  giving 'normal' or 'right' sextupole field.



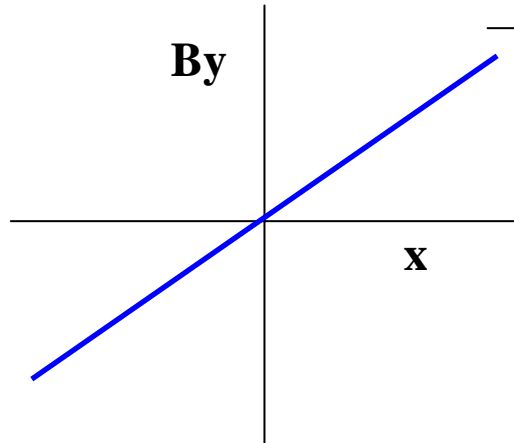
-  Line of constant scalar potential
-  Lines of flux density

# Summary; variation of $B_y$ on x axis

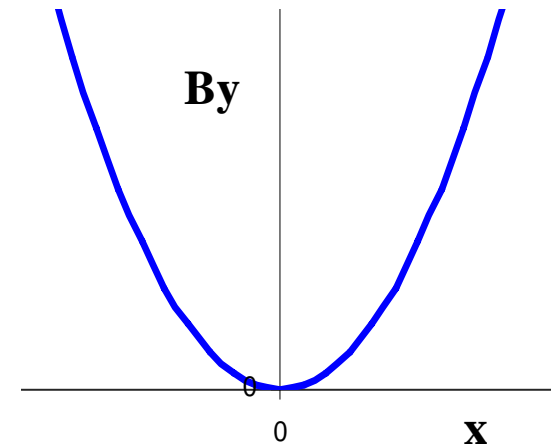
Dipole; constant field:



Quad; linear variation:



Sext.: quadratic variation:



# Alternative notation (USA)

$$B(x) = B \rho \sum_{n=0}^{\infty} \frac{k_n x^n}{n!}$$

magnet strengths are specified by the value of  $k_n$ ;  
(normalised to the beam rigidity);

order  $n$  of  $k$  is different to the 'standard' notation:

|           |                |
|-----------|----------------|
| dipole is | $n = 0$ ;      |
| quad is   | $n = 1$ ; etc. |

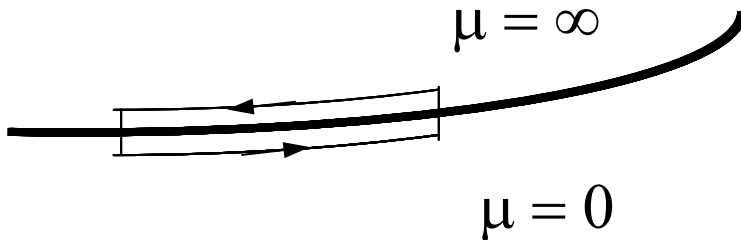
$k$  has units:

|                    |                 |
|--------------------|-----------------|
| $k_0$ (dipole)     | $m^{-1}$ ;      |
| $k_1$ (quadrupole) | $m^{-2}$ ; etc. |

# Introducing Iron Yokes

What is the ideal pole shape?

- Flux is normal to a ferromagnetic surface with infinite  $\mu$ :



$$\text{curl } \mathbf{H} = 0$$

$$\text{therefore } \int \mathbf{H} \cdot d\mathbf{s} = 0;$$

$$\text{in steel } \mathbf{H} = 0;$$

$$\text{therefore parallel } \mathbf{H} \text{ air} = 0$$

$$\text{therefore } \mathbf{B} \text{ is normal to surface.}$$

- Flux is normal to lines of scalar potential, ( $\mathbf{B} = -\nabla\phi$ );
- So the lines of scalar potential are the ideal pole shapes!  
(but these are infinitely long!)



# Equations for the ideal pole

Equations for Ideal (infinite) poles;

( $J_n = 0$ ) for **normal** (ie not skew) fields:

**Dipole:**

$$y = \pm g/2;$$

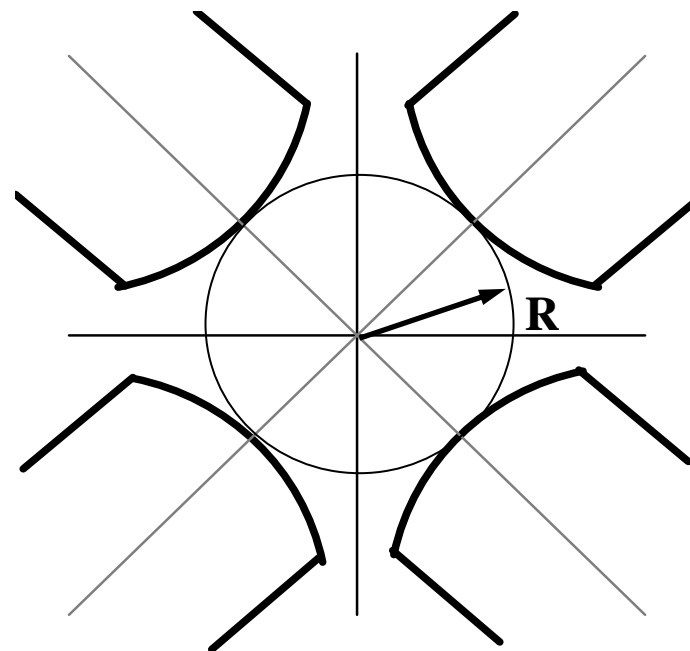
( $g$  is interpole gap).

**Quadrupole:**

$$xy = \pm R^2/2;$$

**Sextupole:**

$$3x^2y - y^3 = \pm R^3;$$

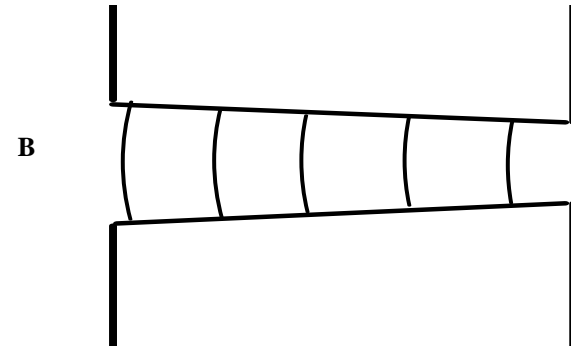


# Combined function (c.f.) magnets

'Combined Function Magnets' - often dipole and quadrupole field quadrupole field combined (but see next-but-one slide):

A quadrupole magnet with physical centre shifted from magnetic centre.

Characterised by 'field index'  $n$ ,  
+ve or -ve depending  
on direction of gradient;  
do not confuse with harmonic  $n$ !



$$n = - \left( \frac{\rho}{B_0} \right) \left( \frac{\partial B}{\partial x} \right),$$

$\rho$  is radius of curvature of the beam;

$B_0$  is central dipole field

# Pole of a c.f. dip.& quad. magnet

If physical and magnetic centres are separated by  $X_0$

Then 
$$B_0 = \left( \frac{\partial B}{\partial x} \right) X_0;$$

therefore 
$$X_0 = -\rho/n;$$

in a quadrupole 
$$x'y = \pm R^2/2$$

where  $x'$  is measured from the true quad centre;

Put 
$$x' = x + X_0$$

So pole equation is 
$$y = \pm \frac{R^2}{2} \frac{n}{\rho} \left( 1 - \frac{nx}{\rho} \right)^{-1}$$

or

$$y = \pm g \left( 1 - \frac{nx}{\rho} \right)^{-1}$$

where  $g$  is the half gap at the physical centre of the magnet

# Other combined function magnets.

## Other combinations:

- dipole, quadrupole and sextupole;
- dipole & sextupole (for chromaticity control);
- dipole, skew quad, sextupole, octupole ( at DL)

## Generated by

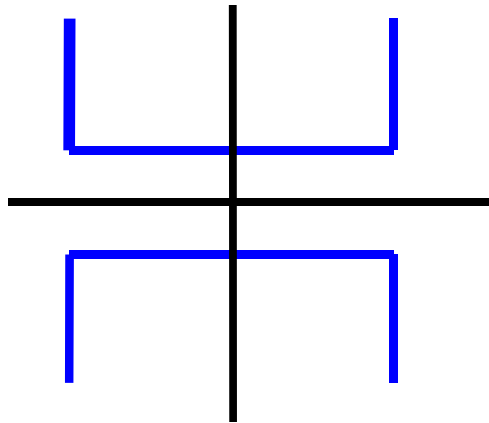
- pole shapes given by sum of correct scalar potentials
  - amplitudes built into pole geometry – not variable.
- multiple coils mounted on the yoke
  - amplitudes independently varied by coil currents.

# The practical Pole

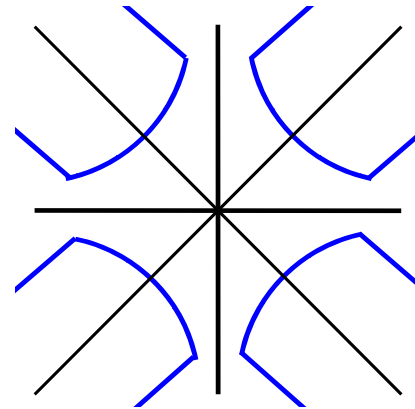
Practically, poles are finite, **introducing errors**; these appear as higher harmonics which degrade the field distribution.

However, the iron geometries have certain symmetries that **restrict** the nature of these errors.

Dipole:



Quadrupole:



# Possible symmetries:

Lines of symmetry:

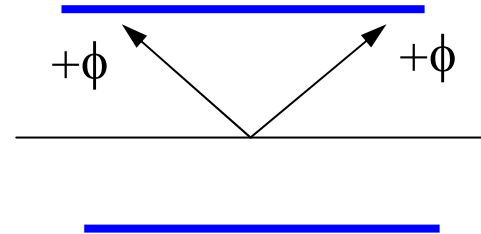
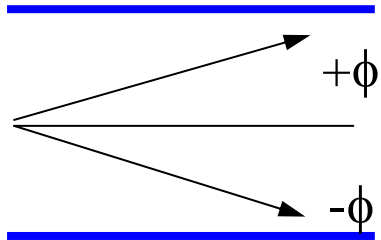
|   | Dipole:  | Quad           |
|---|----------|----------------|
| Pole orientation<br>determines whether pole<br>is normal or skew. | $y = 0;$ | $x = 0; y = 0$ |

Additional symmetry  $x = 0;$        $y = \pm x$   
imposed by pole edges.

The additional constraints imposed by the symmetrical pole  
pole edges limits the values of  $n$  that have non zero  
coefficients

# Dipole symmetries

| Type             | Symmetry                            | Constraint   |
|------------------|-------------------------------------|--|
| Pole orientation | $\phi(\theta) = -\phi(-\theta)$     | all $J_n = 0$ ;  |
| Pole edges       | $\phi(\theta) = \phi(\pi - \theta)$ | $K_n$ non-zero<br>only for:<br>$n = 1, 3, 5, \text{etc}$ ; |



So, for a fully symmetric dipole, only 6, 10, 14 etc pole errors can be present.

# Quadrupole symmetries

| Type             | Symmetry                              | Constraint   |
|------------------|---------------------------------------|--|
| Pole orientation | $\phi(\theta) = -\phi(-\theta)$       | All $J_n = 0$ ;  |
|                  | $\phi(\theta) = -\phi(\pi - \theta)$  | $K_n = 0$ all odd $n$ ;                                      |
| Pole edges       | $\phi(\theta) = \phi(\pi/2 - \theta)$ | $K_n$ non-zero<br>only for:<br>$n = 2, 6, 10, \text{ etc}$ ; |

So, a fully symmetric quadrupole, only 12, 20, 28 etc pole errors can be present.



# Sextupole symmetries

| Type             | Symmetry  | Constraint  |
|------------------|---|---|
| Pole orientation | $\phi(\theta) = -\phi(-\theta)$<br>$\phi(\theta) = -\phi(2\pi/3 - \theta)$<br>$\phi(\theta) = -\phi(4\pi/3 - \theta)$ | All $J_n = 0$ ;<br>$K_n = 0$ for all $n$<br>not multiples of 3; |
| Pole edges       | $\phi(\theta) = \phi(\pi/3 - \theta)$   | $K_n$ non-zero only<br>for: $n = 3, 9, 15, \text{ etc.}$        |

So, a fully symmetric sextupole, only 18, 30, 42 etc pole errors can be present.

# Summary - 'Allowed' Harmonics

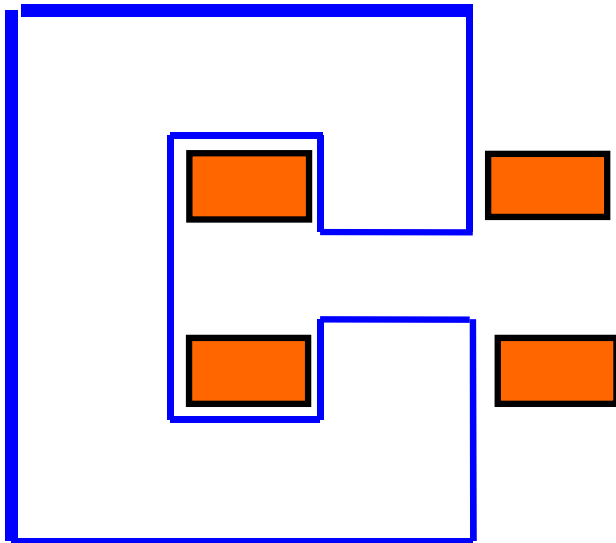
Summary of 'allowed harmonics' in fully symmetric magnets:  
magnets:

| <b>Fundamental geometry</b>           | <b>'Allowed' harmonics</b>   |
|---------------------------------------|--|
| <b>Dipole, <math>n = 1</math></b>     | <b><math>n = 3, 5, 7, \dots</math><br/>( 6 pole, 10 pole, etc.)</b>    |
| <b>Quadrupole, <math>n = 2</math></b> | <b><math>n = 6, 10, 14, \dots</math><br/>(12 pole, 20 pole, etc.)</b>  |
| <b>Sextupole, <math>n = 3</math></b>  | <b><math>n = 9, 15, 21, \dots</math><br/>(18 pole, 30 pole, etc.)</b>  |
| <b>Octupole, <math>n = 4</math></b>   | <b><math>n = 12, 20, 28, \dots</math><br/>(24 pole, 40 pole, etc.)</b> |

# Asymmetries generating harmonics (i).

Two sources of asymmetry generate ‘forbidden’ harmonics:

i) yoke asymmetries only significant with low permeability:

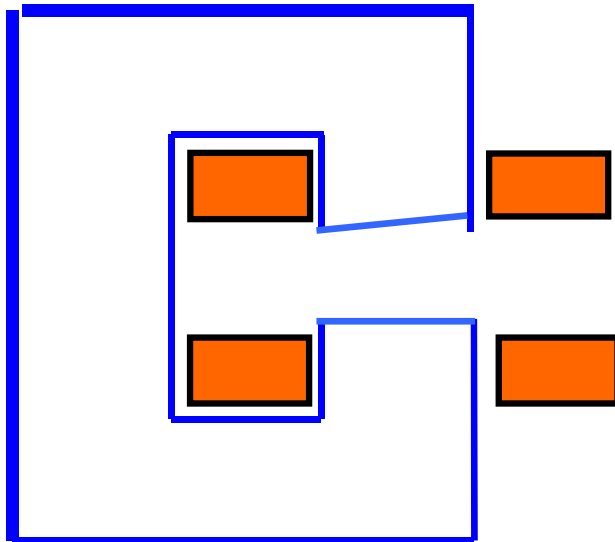


eg, C core dipole not completely symmetrical about pole centre, but negligible effect with high permeability.

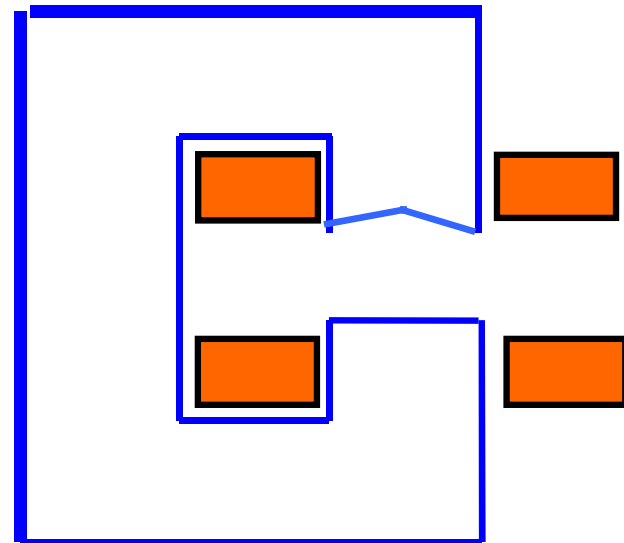
Generates  $n = 2, 4, 6$ , etc.

# Asymmetries generating harmonics (ii)

ii) asymmetries due to small manufacturing errors in dipoles:  
dipoles:



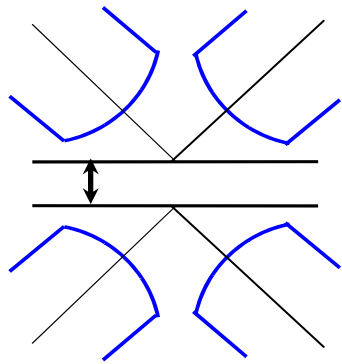
$n = 2, 4, 6$  etc.



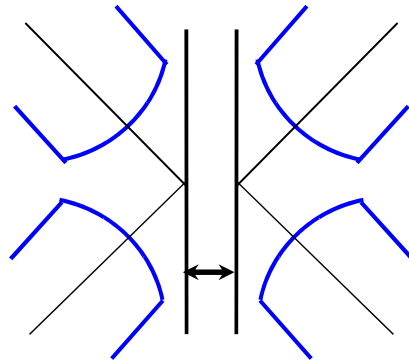
$n = 3, 6, 9$ , etc.

# Asymmetries generating harmonics (iii)

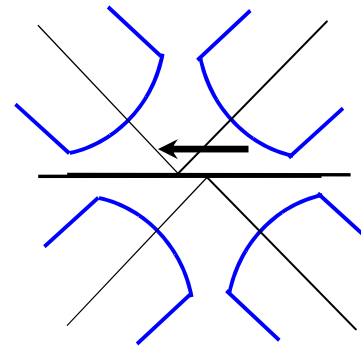
ii) asymmetries due to small manufacturing errors in quadrupoles:  
quadrupoles:



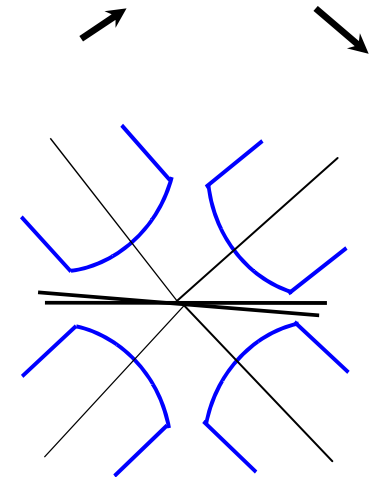
$n = 4$  - ve



$n = 4$  + ve



$n = 3$ ;



$n = 2$  (skew)

$n = 3$ ;

These errors are bigger than the finite  $\mu$  type, can seriously affect machine behaviour and must be controlled.

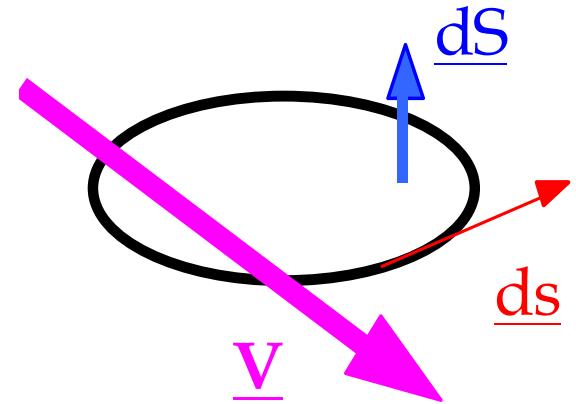
# Introduction of currents

Now for  $\underline{j} \neq 0$

$$\underline{\nabla} \underline{H} = \underline{j};$$

To expand, use Stoke's Theorem:  
for any vector  $\underline{V}$  and a closed  
curve  $s$  :

$$\int \underline{V} \cdot \underline{ds} = \iint \text{curl } \underline{V} \cdot \underline{dS}$$



Apply this to:  $\text{curl } \underline{H} = \underline{j}$ ;

then in a magnetic circuit:

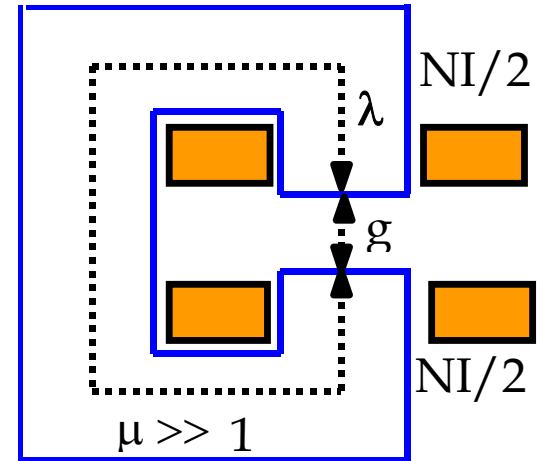
$$\int \underline{H} \cdot \underline{ds} = N I;$$

$N I$  (Ampere-turns) is total current cutting  $\underline{S}$

# Excitation current in a dipole

B is approx constant round the loop  
made up of  $\lambda$  and  $g$ , (but see below);

But in iron,  $\mu \gg 1$ ,  
and  $H_{\text{iron}} = H_{\text{air}} / \mu$  ;



So

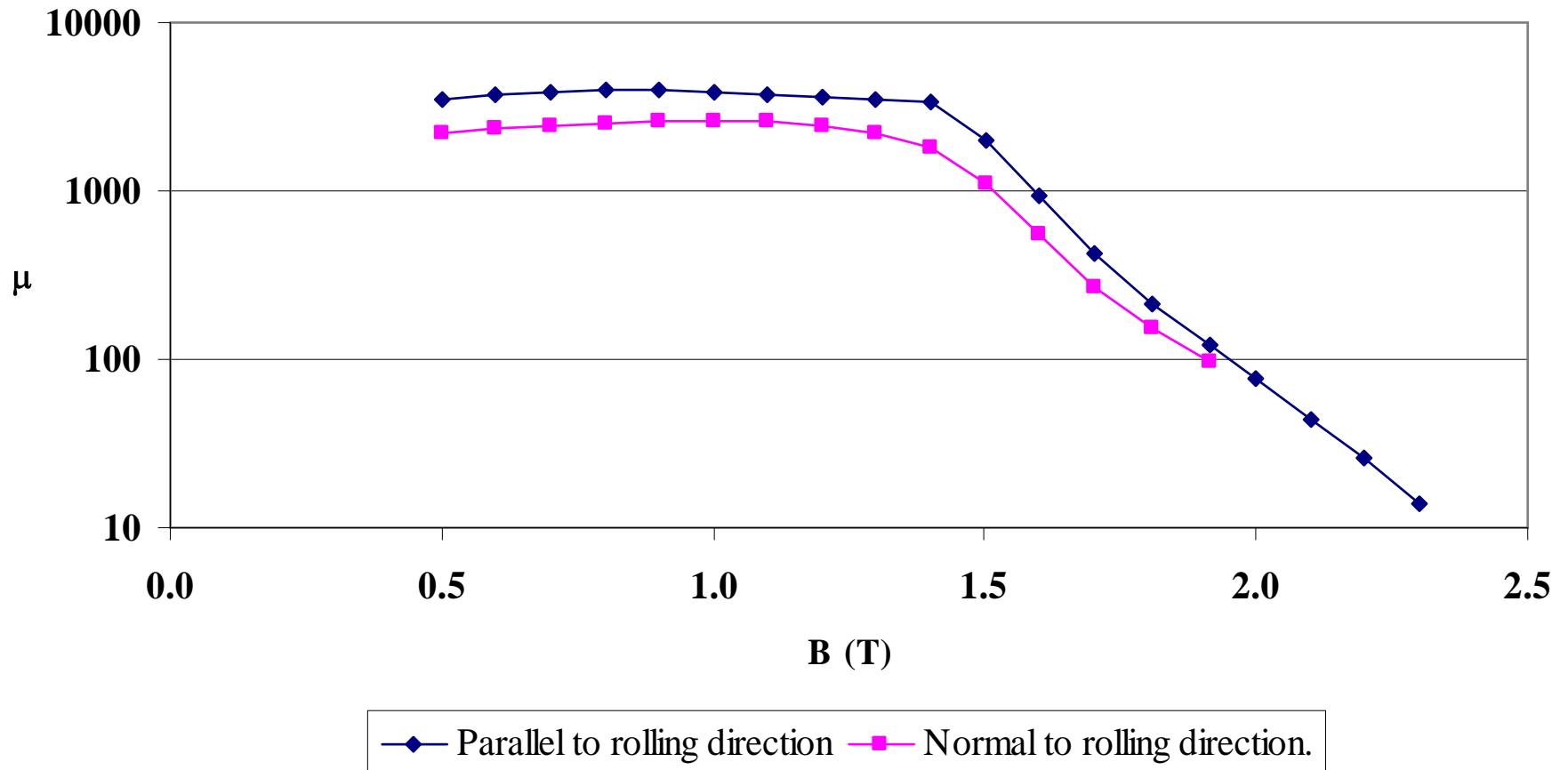
$$B_{\text{air}} = \mu_0 NI / (g + \lambda/\mu);$$

$g$ , and  $\lambda/\mu$  are the 'reluctance' of the gap and iron.

Approximation ignoring iron reluctance ( $\lambda/\mu \ll g$ ):

$$NI = B g / \mu_0$$

# Relative permeability of low silicon steel





# Excitation current in quad & sextupole

For quadrupoles and sextupoles, the required excitation can be calculated by considering fields and gap at large  $x$ . For example: **Quadrupole:**

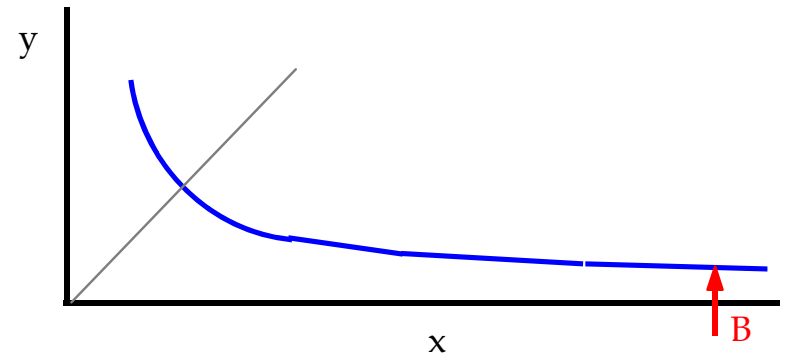
Pole equation:  $xy = R^2 / 2$   
On  $x$  axes  $B_Y = gx$ ;  
where  $g$  is gradient (T/m).

At large  $x$  (to give vertical lines of  $B$ ):

$$N I = (gx) (R^2 / 2x) / \mu_0$$

ie

$$N I = g R^2 / 2 \mu_0 \text{ (per pole).}$$



The same method for a

**Sextupole,**

(coefficient  $g_S$ ), gives:

$$N I = g_S R^3 / 3 \mu_0 \text{ (per pole)}$$

# General solution for magnets order n

In air (remote currents! ),

$$\mathbf{B} = \mu_0 \mathbf{H}$$

$$\mathbf{B} = -\nabla\phi$$

Integrating over a limited path

(not circular) in air:

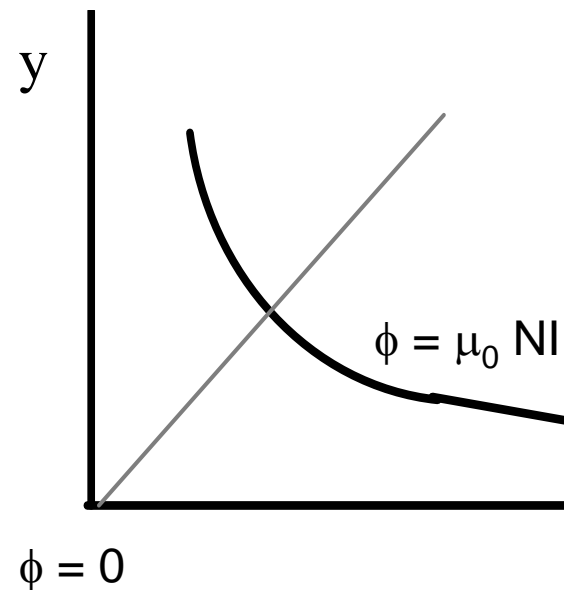
$$NI = (\phi_1 - \phi_2)/\mu_0$$

$\phi_1, \phi_2$  are the scalar potentials at two points in air.

Define  $\phi = 0$  at magnet centre;

then potential at the pole is:

$$\mu_0 NI$$



Apply the general equations for magnetic field harmonic order n for non-skew magnets (all  $J_n = 0$ ) giving:

$$NI = (1/n) (1/\mu_0) \{B_r/R^{(n-1)}\} R^n$$

Where:

NI is excitation per pole;

R is the inscribed radius (or half gap in a dipole);

term in brackets  $\{ \}$  is magnet strength in T/m<sup>(n-1)</sup>.

# Magnet geometry

Dipoles can be 'C core' 'H core' or 'Window frame'

## "C" Core:

Advantages:

Easy access;

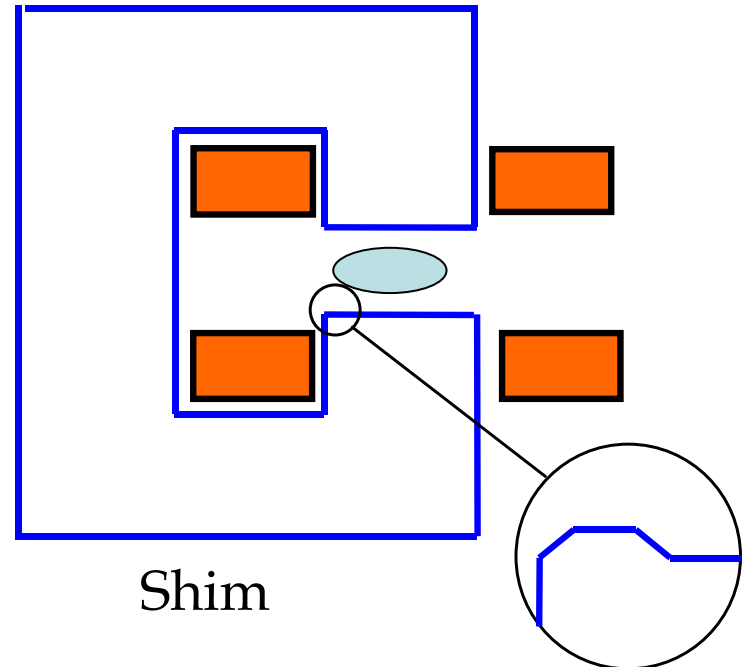
Classic design;

Disadvantages:

Pole shims needed;

Asymmetric (small);

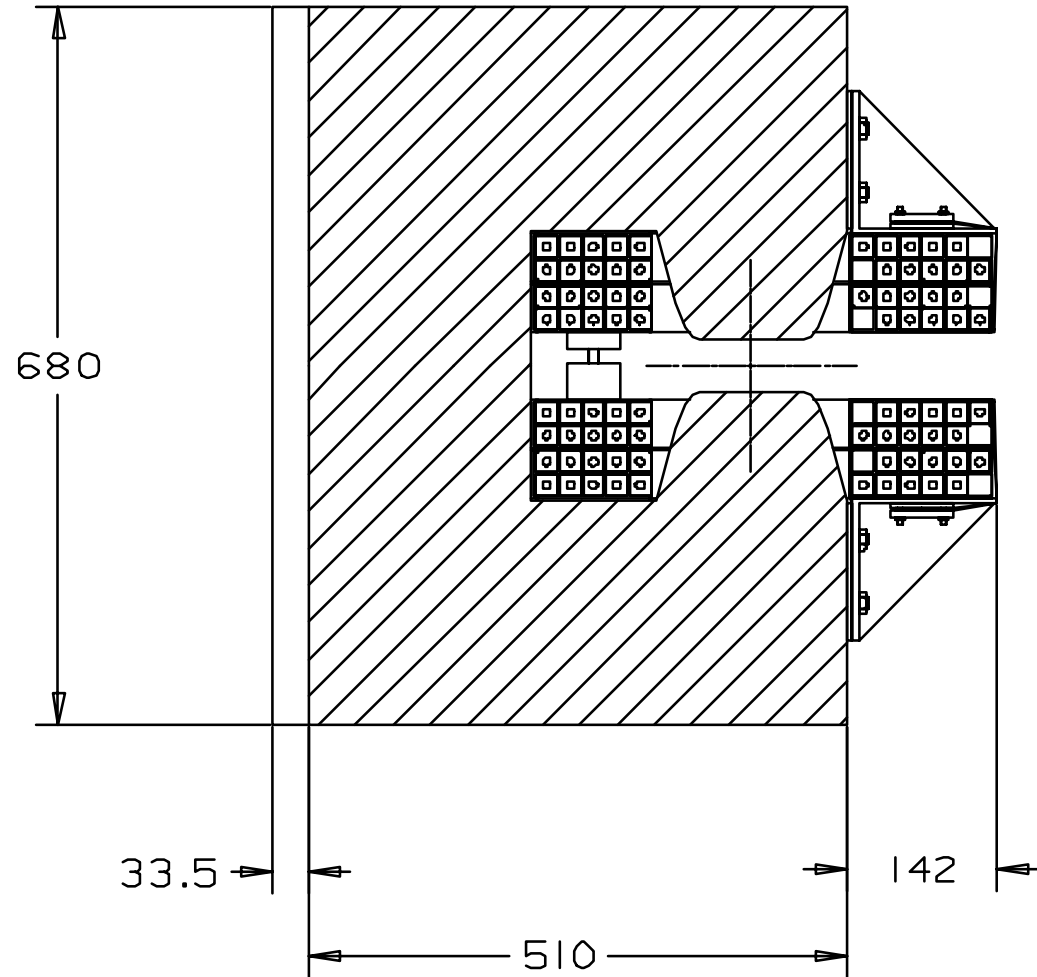
Less rigid;



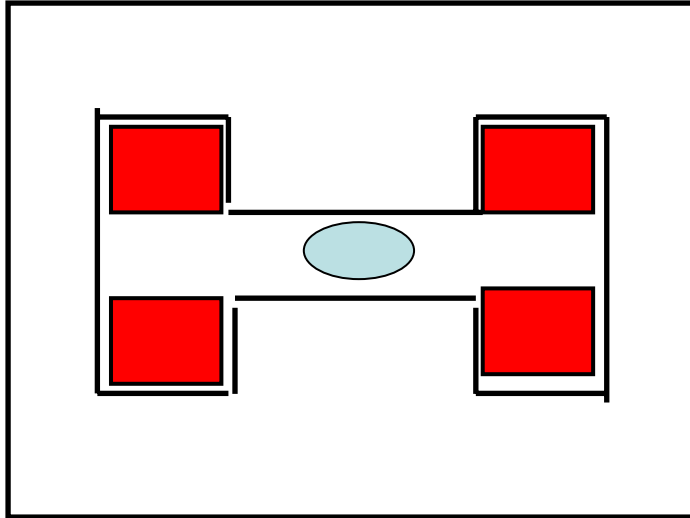
The 'shim' is a small, additional piece of ferro-magnetic material added on each side of the two poles – it compensates for the finite cut-off of the pole, and is optimised to reduce the 6, 10, 14..... pole error harmonics.

# A typical 'C' cored Dipole

Cross section of the Diamond storage ring dipole.



# H core and window-frame magnets



'H core':

Advantages:

Symmetric;

More rigid;

Disadvantages:

Still needs shims;

Access problems.

'Window Frame'

Advantages:

High quality field;

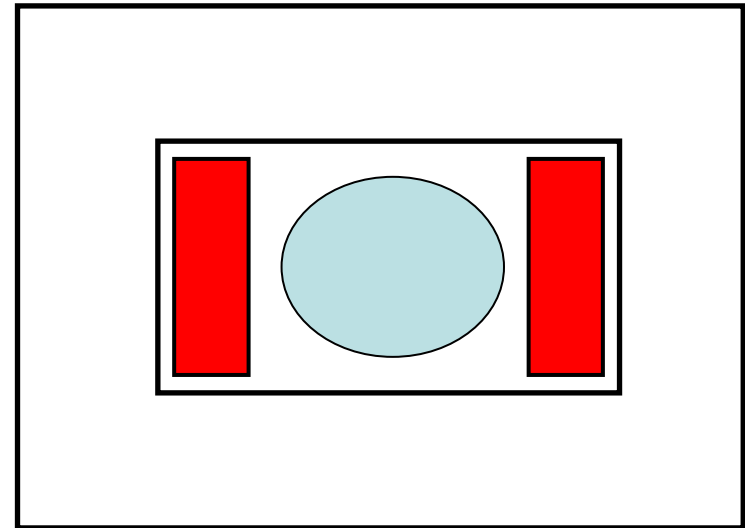
No pole shim;

Symmetric & rigid;

Disadvantages:

Major access problems;

Insulation thickness

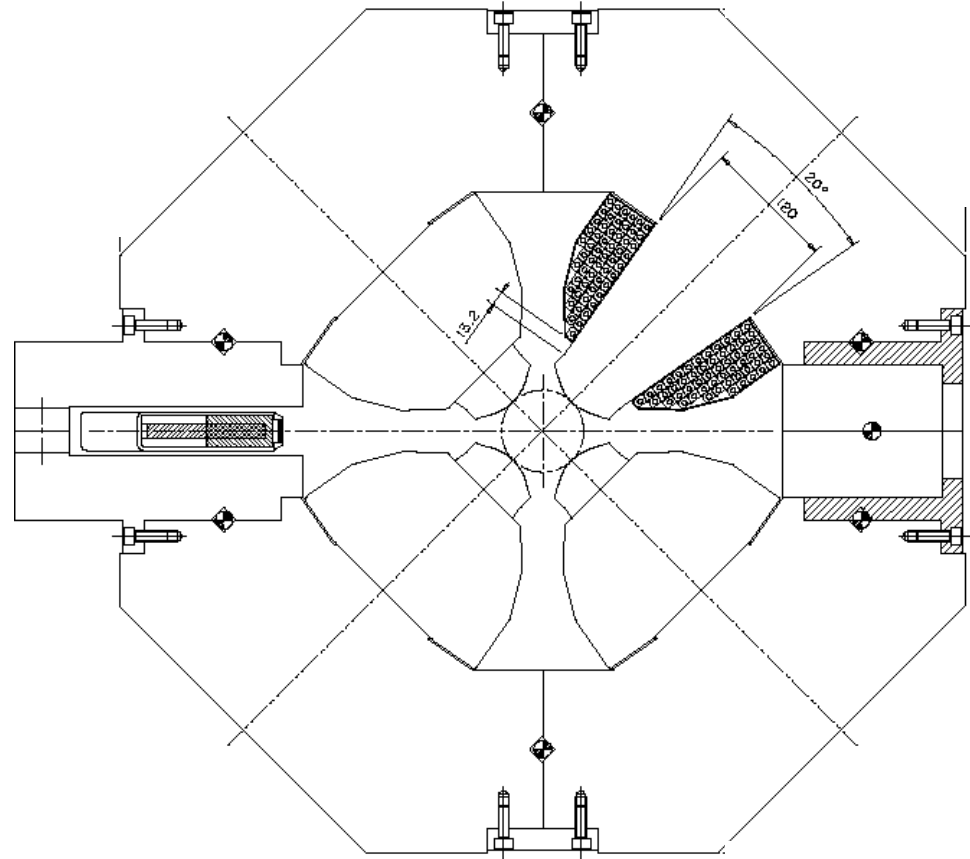


# An open-sided Quadrupole.

‘Diamond’ storage ring quadrupole.

The yoke support pieces in the horizontal plane need to provide space for beam-lines and are not ferro-magnetic.

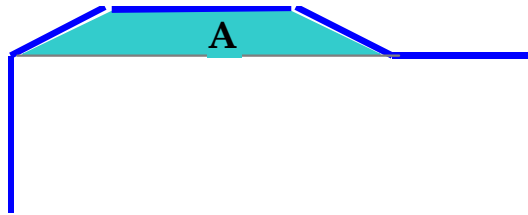
Error harmonics include  $n = 4$  (octupole) a finite permeability error.



# Typical pole designs

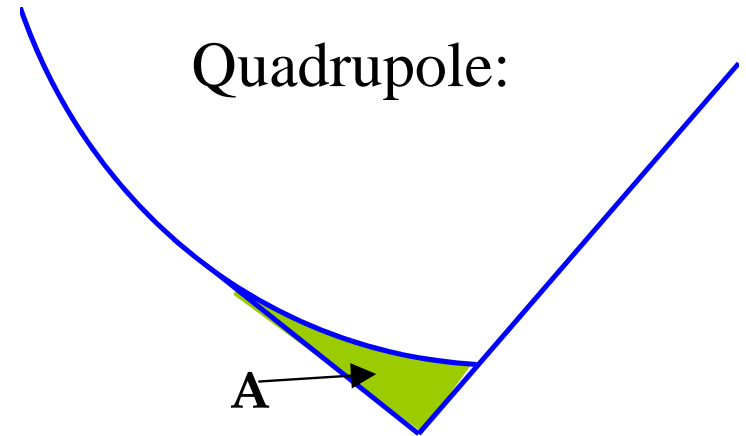
To compensate for the non-infinite pole, shims are added at the pole edges. The area and shape of the shims determine the amplitude of error harmonics which will be present.

Dipole:



The designer optimises the pole by ‘predicting’ the field resulting from a given pole geometry and then adjusting it to give the required quality.

Quadrupole:

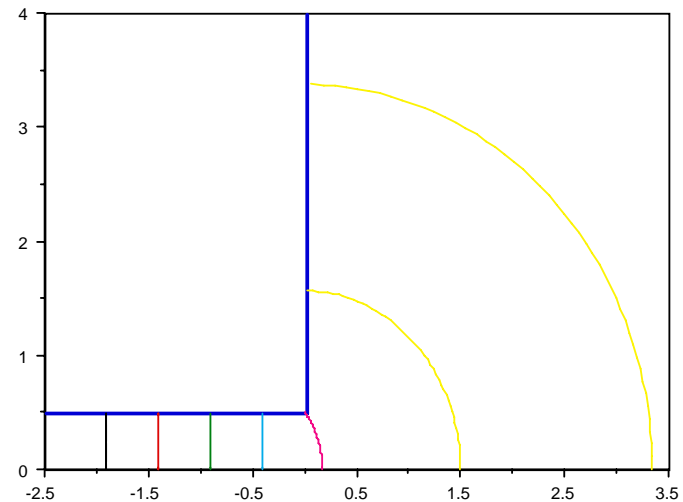
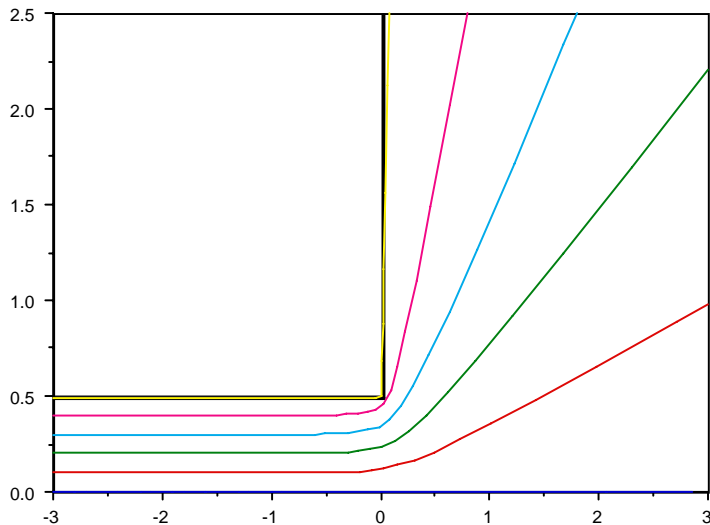


When high fields are present, chamfer angles must be small, and tapering of poles may be necessary

# Design (i).

Pre computers, numerical methods and other maths methods were used to predict field distributions.

Still used - 'conformal transformations'; mapping between complex planes representing the magnet geometry and a configuration that is analytic. Examples below are for lines of i) constant scalar potential; ii) flux on a square end of a magnet pole.





# Design (ii)

Computer codes are now used; eg the Vector Fields Fields codes - 'OPERA 2D' and 'TOSCA' (3D).

These have:

- finite elements with variable triangular mesh;
- multiple iterations to simulate steel non-linearity;
- extensive pre and post processors;
- compatibility with many platforms and P.C. o.s.

Technique is iterative:

- calculate flux generated by a defined geometry;
- adjust the geometry until required distribution is achieved.  
achieved.

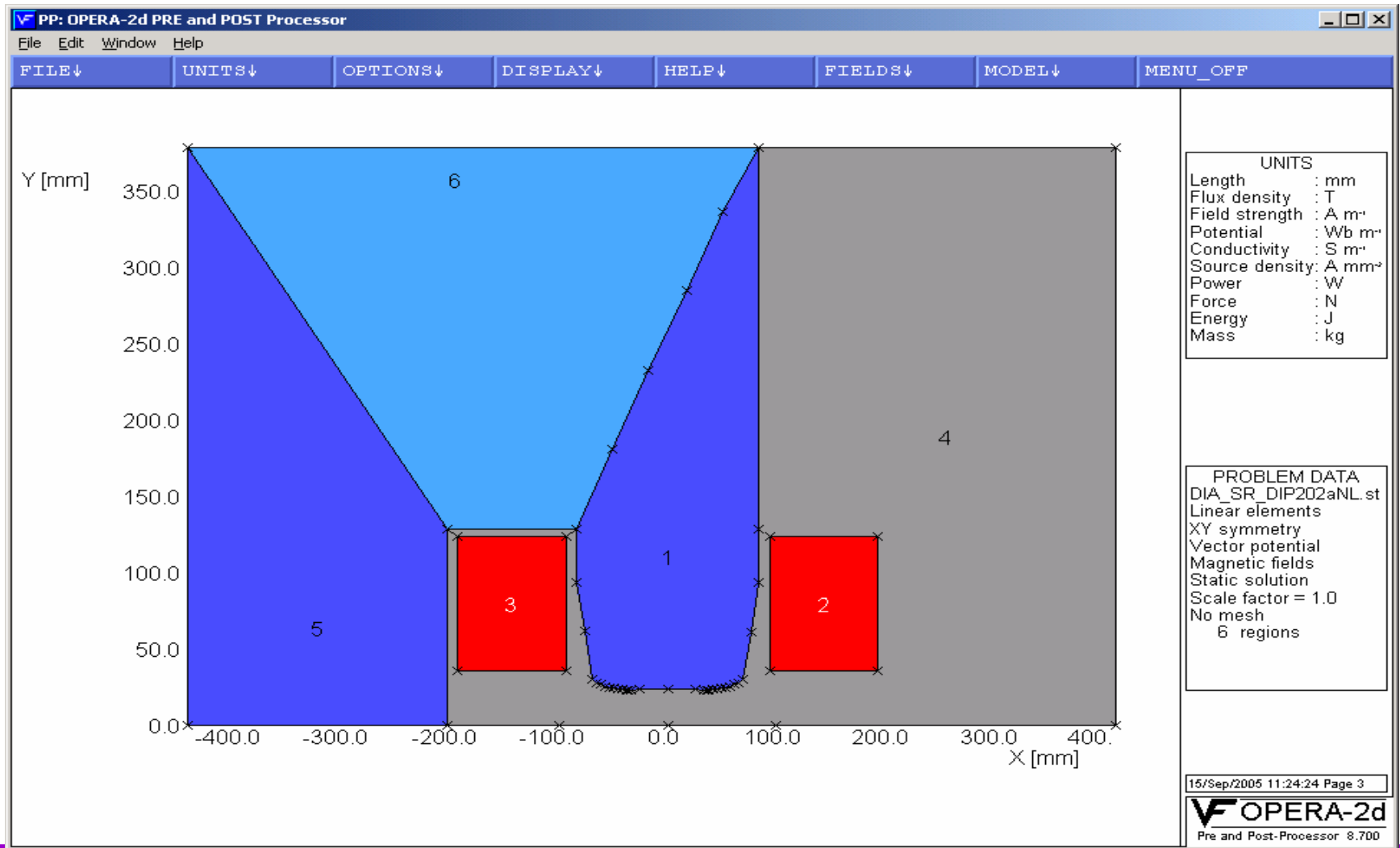
# Design Procedures – OPERA 2D.

## Pre-processor:

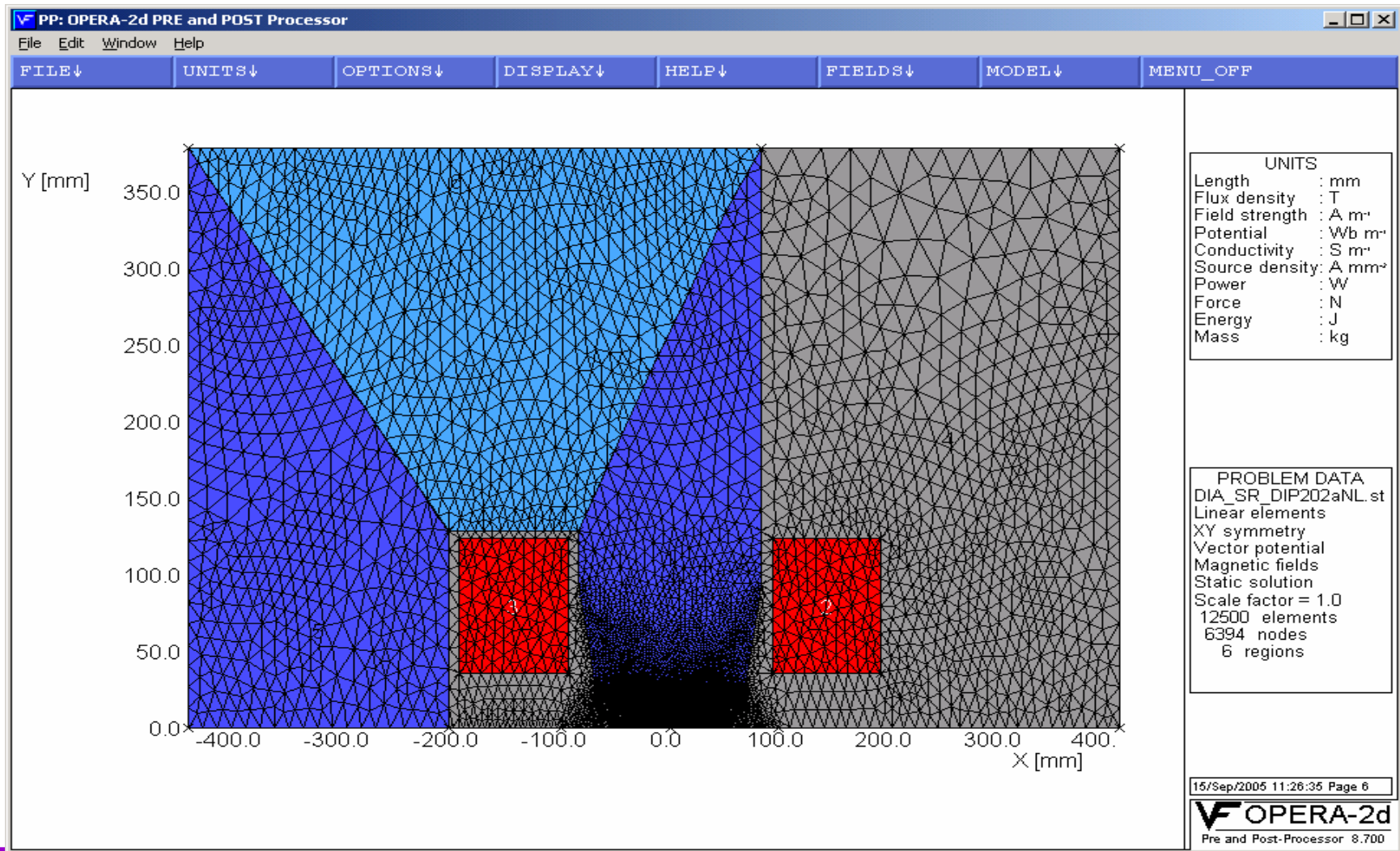
The model is set-up in 2D using a GUI (graphics user's user's interface) to define 'regions':

- steel regions;
- coils (including current density);
- a 'background' region which defines the physical physical extent of the model;
- the symmetry constraints on the boundaries;
- the permeability for the steel (or use the pre-programmed curve);
- mesh is generated and data saved.

# Model of Diamond s.r. dipole

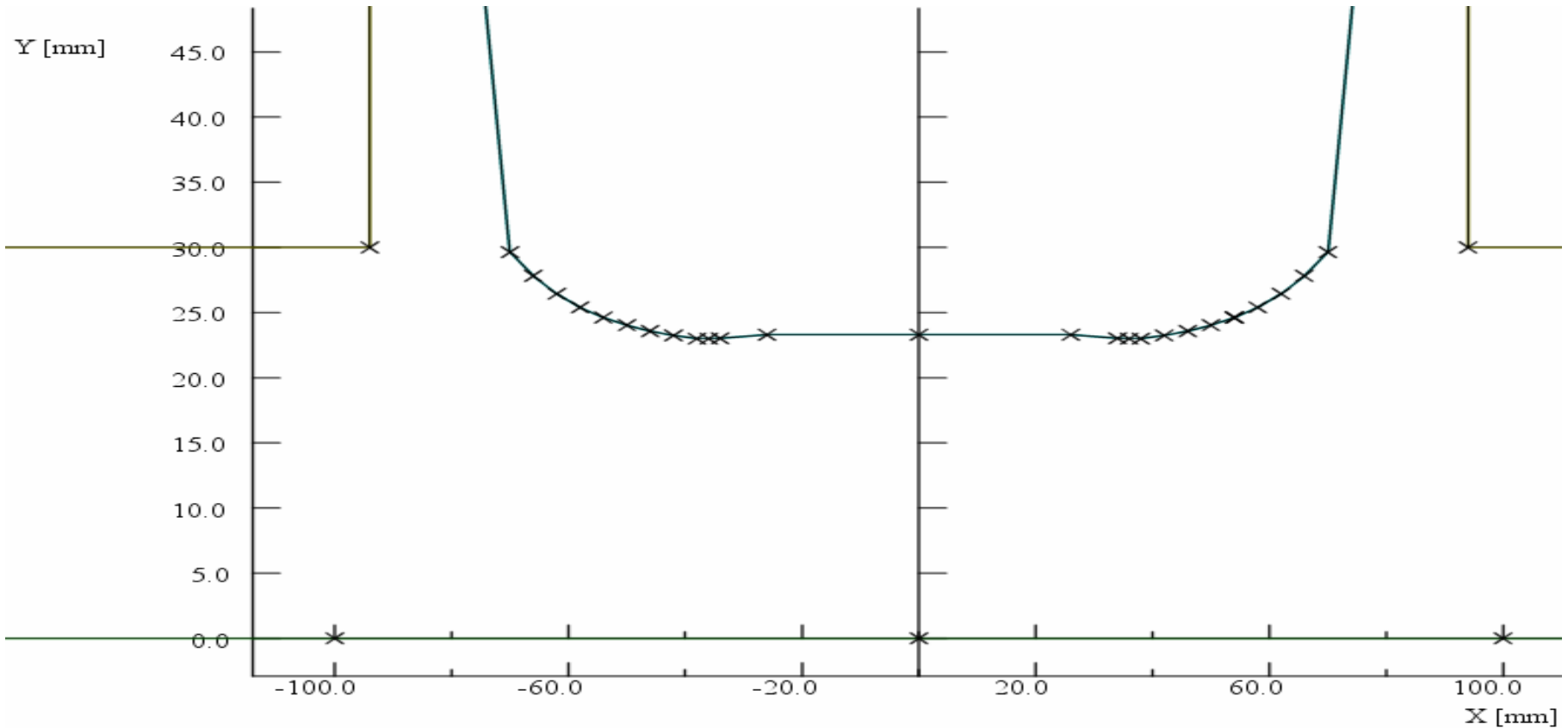


# With mesh added

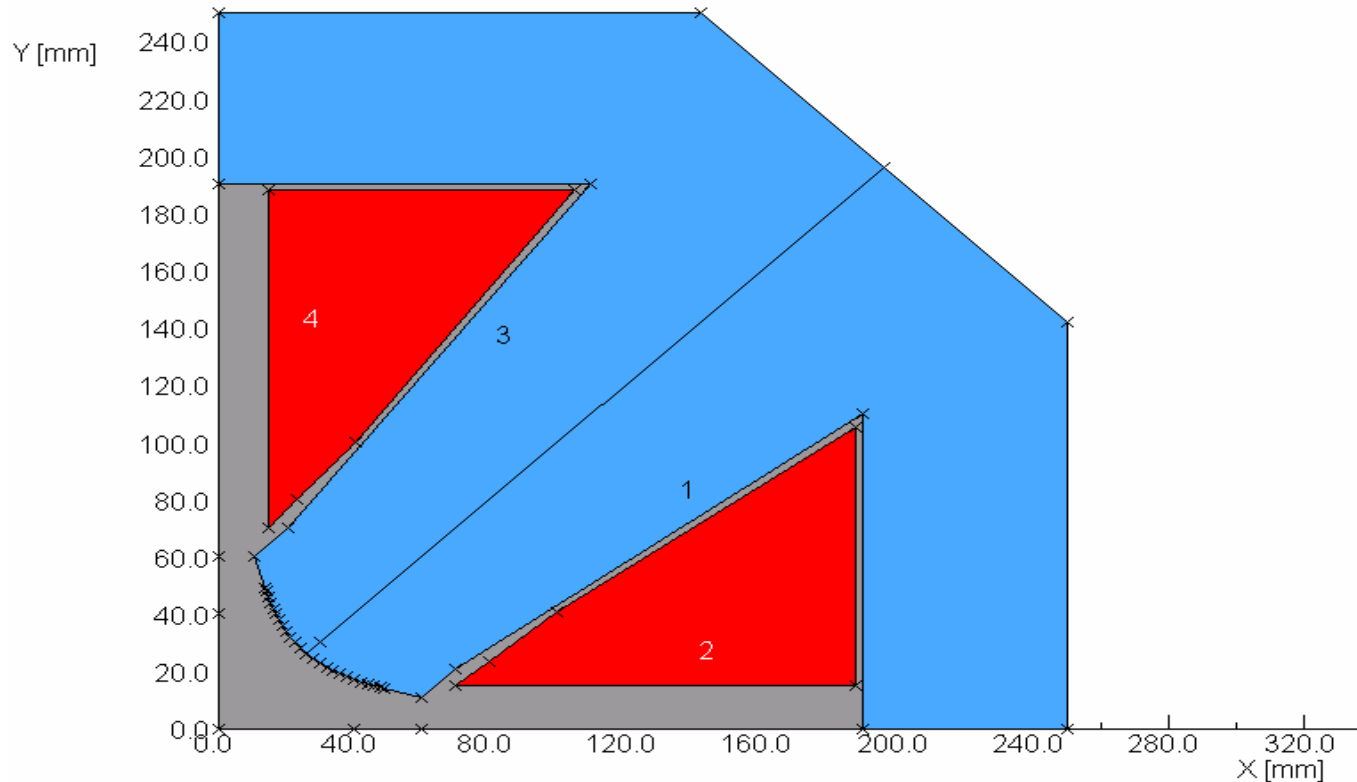


# 'Close-up' of pole region.

Pole profile, showing shim and Rogowski roll-off for Diamond 1.4 T dipole.:



# Diamond quadrupole model



Note – one eighth of quadrupole could be used with opposite symmetries defined on horizontal and  $y = x$  axis.

# Calculation.

Data Processor:

either:

- linear which uses a predefined constant permeability for a for a single calculation, or
- non-linear, which is iterative with steel permeability set set according to B in steel calculated on previous iteration.

# Data Display – OPERA 2D.

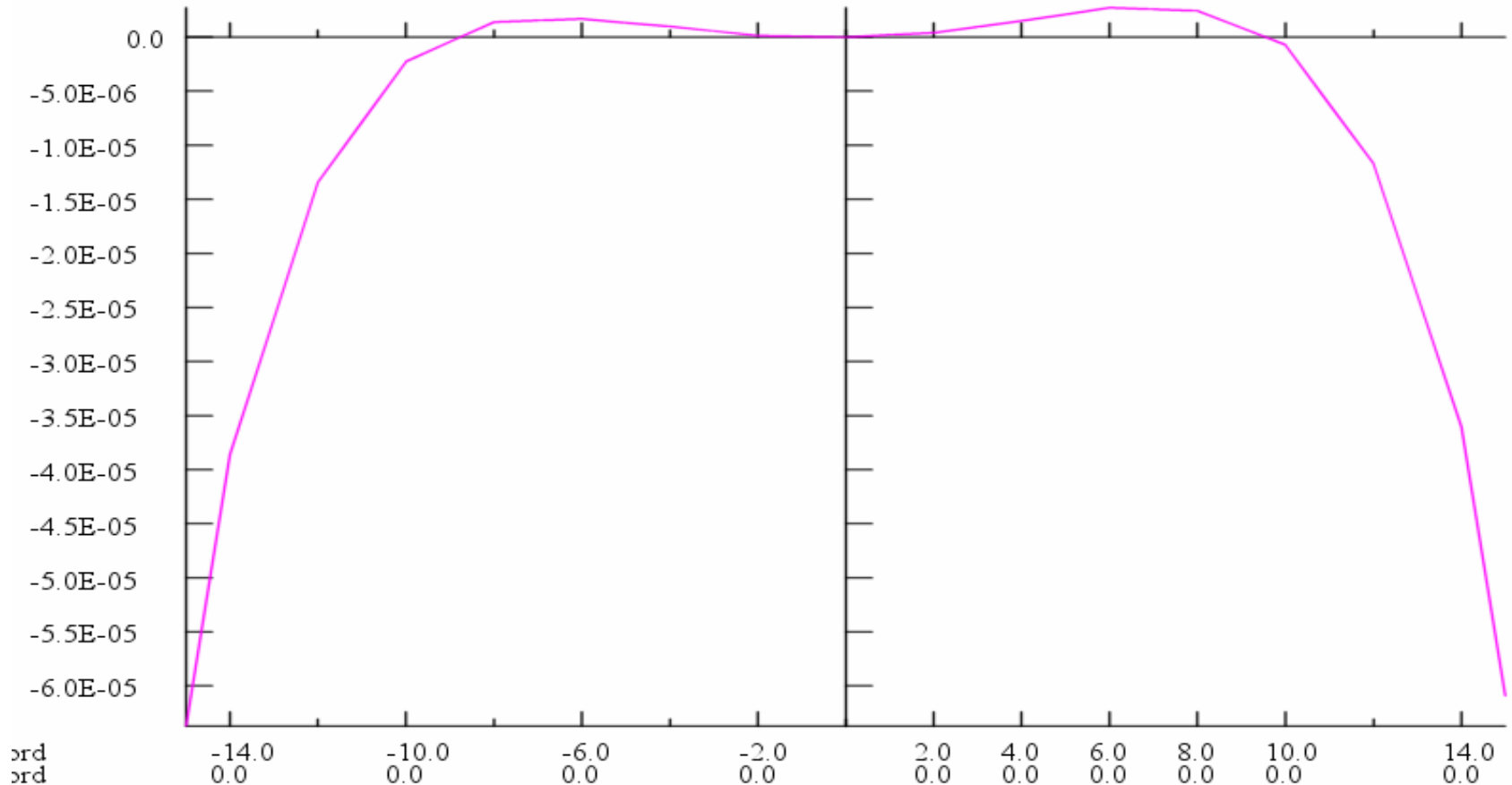
Post-processor:

uses pre-processor model for many options for displaying field amplitude and quality:

- field lines;
- graphs;
- contours;
- gradients;
- harmonics (from a Fourier analysis around a pre-defined defined circle).



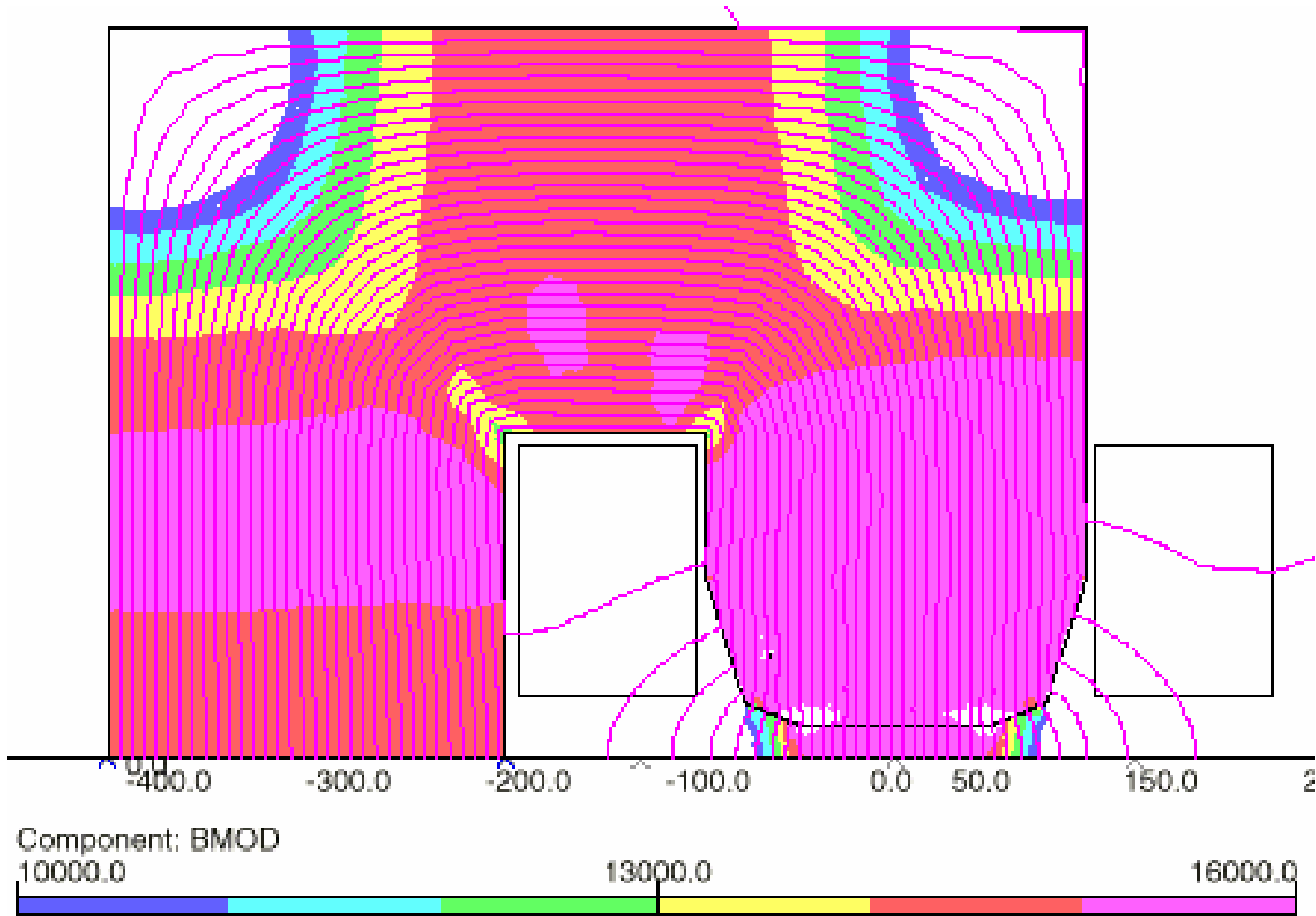
# 2 D Dipole field homogeneity on x axis



Diamond s.r. dipole:  $\Delta B/B = \{B_y(x) - B(0,0)\}/B(0,0)$ ;

typically  $\pm 1:10^4$  within the 'good field region' of  $-12\text{mm} \leq x \leq +12\text{mm}$ .

# 2 D Flux density distribution in a dipole.

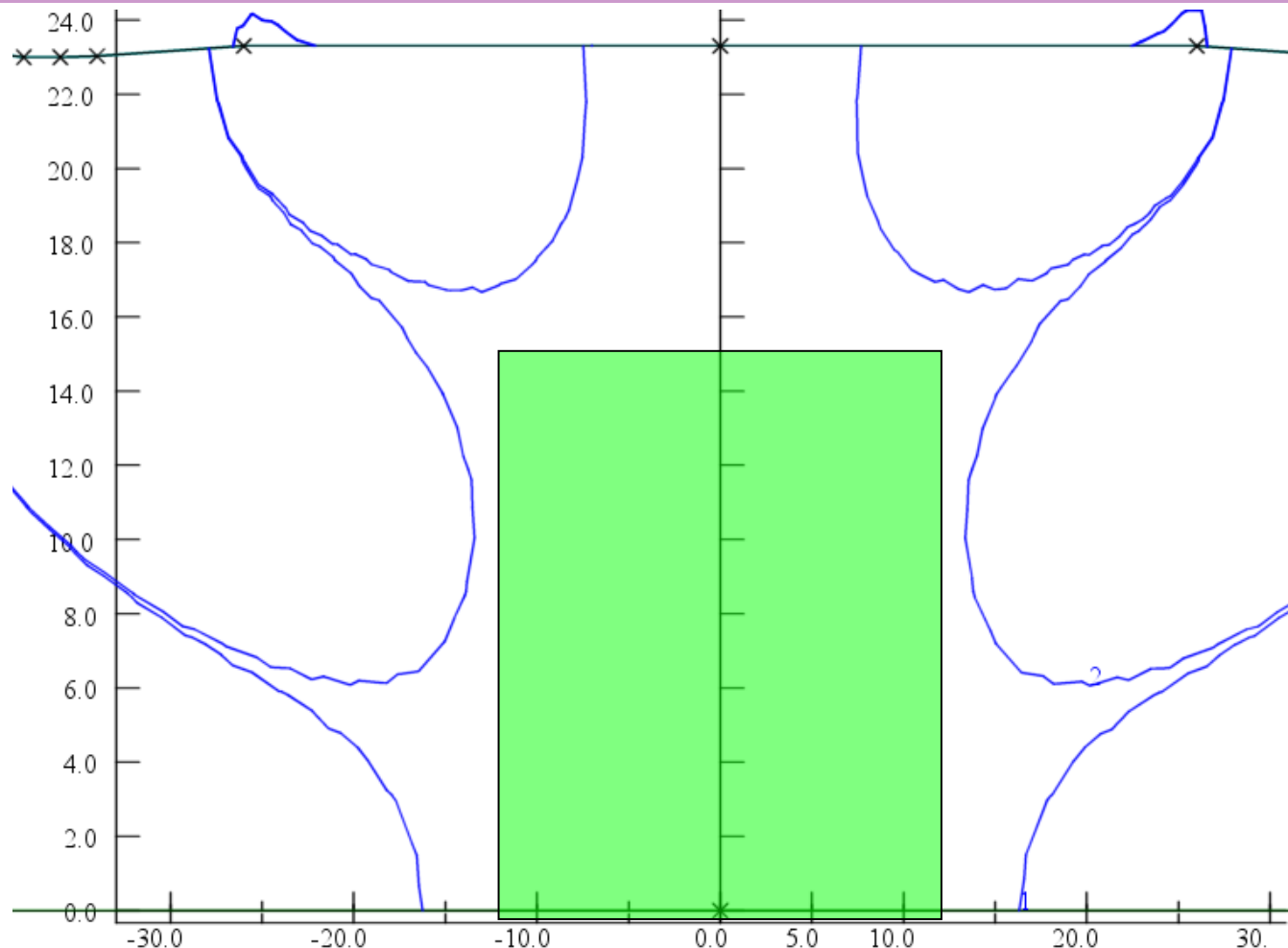


# 2 D Dipole field homogeneity in gap

Transverse  
(x,y) plane in  
Diamond s.r.  
dipole;

contours are  
 $\pm 0.01\%$

required good  
field region:

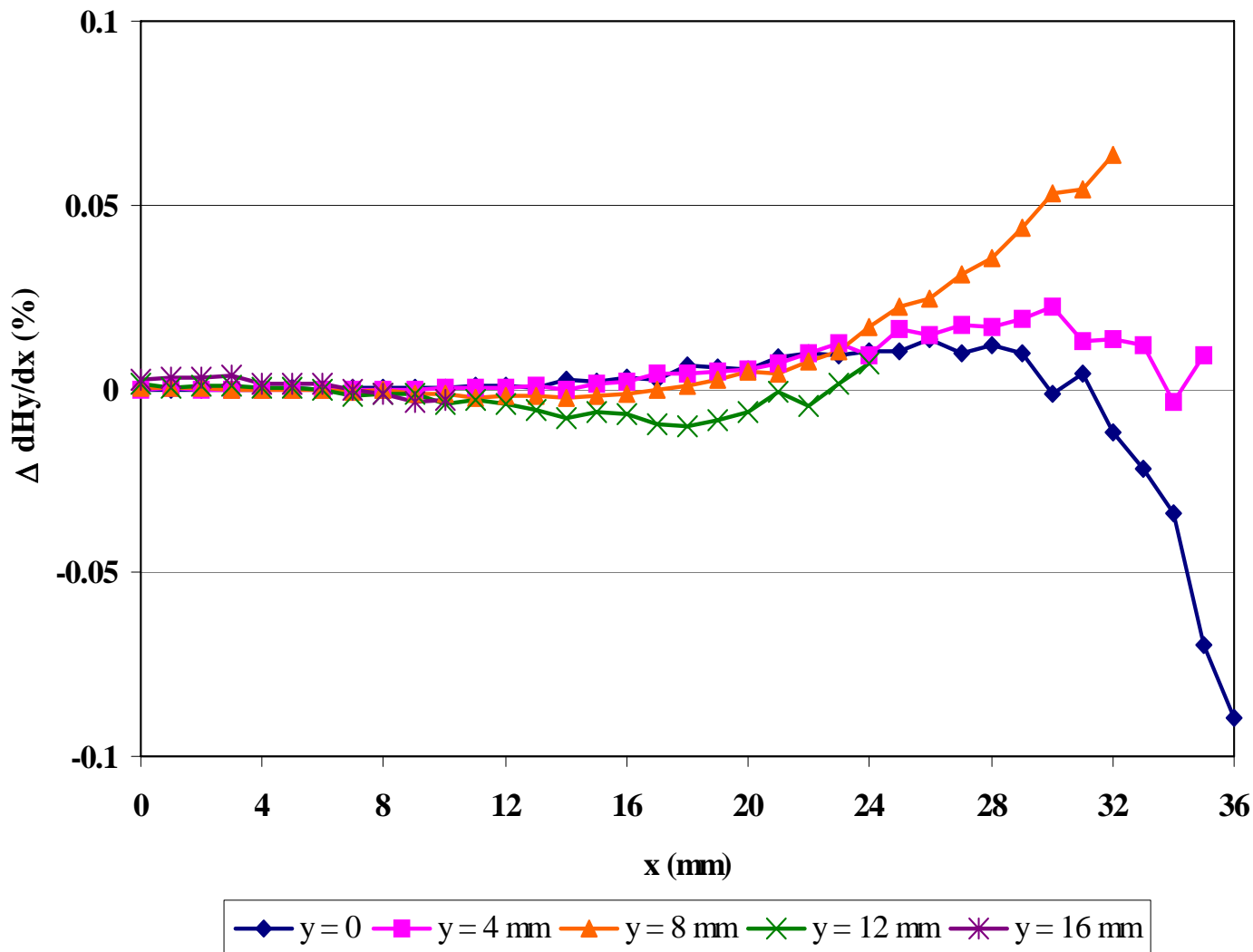


# 2 D Assessment of quadrupole gradient quality

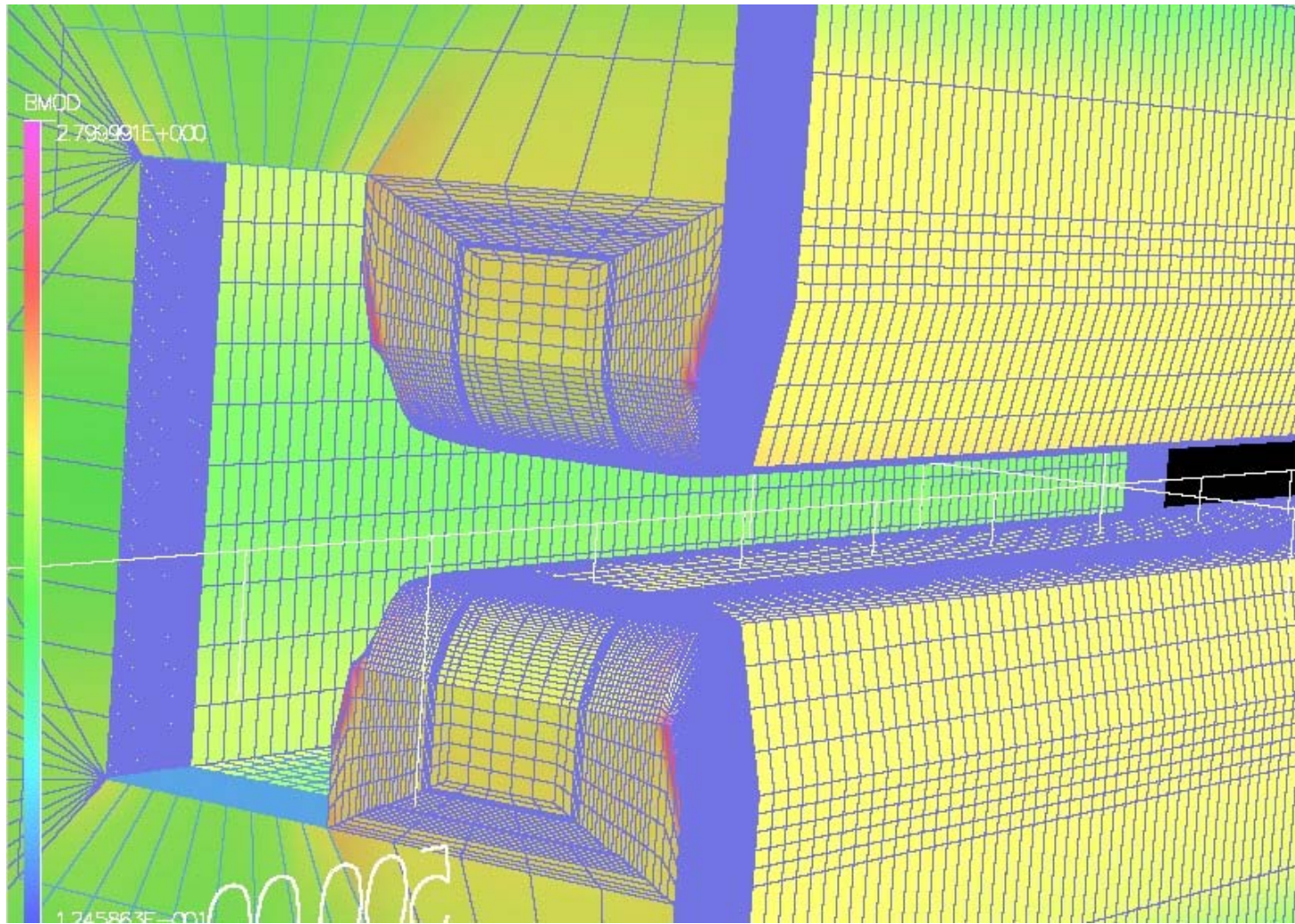
Diamond  
WM  
quadrupole:

graph is  
percentage  
variation in  
 $dBy/dx$  vs  $x$   
at different  
values of  $y$ .

Gradient  
quality is to  
be  $\pm 0.1\%$  or  
better to  $x =$   
36 mm.



# OPERA 3D model of Diamond dipole.



# Assessing results

A simple judgement of field quality is given by plotting:

|                  |                              |                          |
|------------------|------------------------------|--------------------------|
| • <b>Dipole:</b> | $\{B_y(x) - B_y(0)\}/B_Y(0)$ | $(\Delta B(x)/B(0))$     |
| • <b>Quad:</b>   | $dB_y(x)/dx$                 | $(\Delta g(x)/g(0))$     |
| • <b>6poles:</b> | $d^2B_y(x)/dx^2$             | $(\Delta g_2(x)/g_2(0))$ |

‘Typical’ acceptable variation inside ‘good field’ region:

$$\begin{aligned}\Delta B(x)/B(0) &\leq 0.01\% \\ \Delta g(x)/g(0) &\leq 0.1\% \\ \Delta g_2(x)/g_2(0) &\leq 1.0\%\end{aligned}$$

# Harmonics indicate magnet quality

The amplitude and phase of the harmonic components in a magnet provide an assessment:

- when accelerator physicists are calculating beam behaviour in a lattice;
- when designs are judged for suitability;
- when the manufactured magnet is measured;
- to judge acceptability of a manufactured magnet.

# Modern measurement techniques.

Magnets are now measured using rotating coil systems; systems; suitable for straight dipoles and multi-poles poles (quadrupoles and sextupoles).

This equipment and technique provides:

- amplitude;
- phase;

of each harmonic present, up to  $n \sim 20$ ;

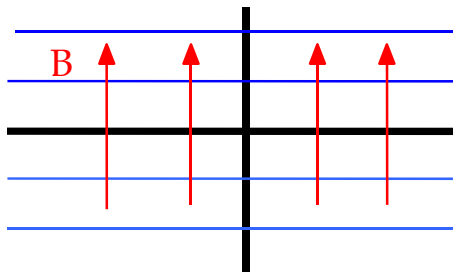
and:

- magnetic centre (x and y);
- angular alignment (roll, pitch and yaw).

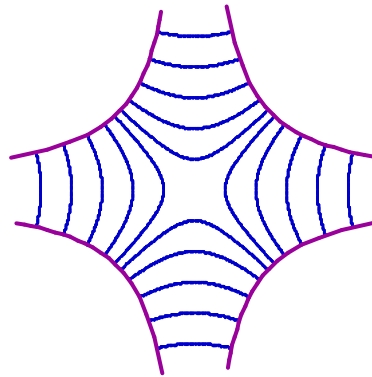


# The Rotating Coil

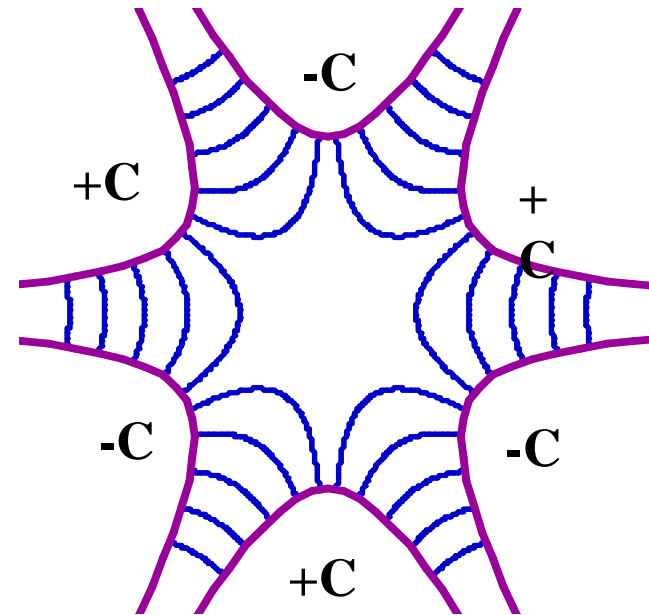
A coil continuously rotating (frequency  $\omega$ ) would cut the radial field and generate a voltage the sum of all the harmonics present in the magnet:



dipole:  $V = \sin \omega t$



quad:  $V = \sin 2 \omega t$



sextupole:  $V = \sin 3 \omega t$

Etc.

# Problems with continuous rotation

Sliding contacts: generate noise – obscures small higher order harmonics;

Irregular rotation: (wow) generates spurious harmonic signals;

Transverse oscillation of coil: (whip-lash) generates noise and spurious harmonics.

Solution developed at CERN to measure the LEP multi-pole magnets.

# Mode of operation

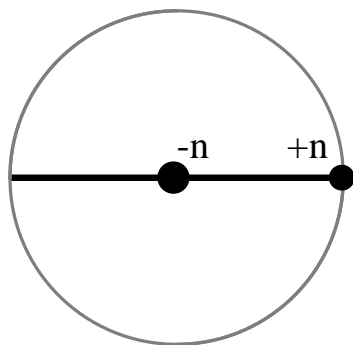
## Rotation and data processing:

- windings are hard wired to detection equipment and cylinders  
cylinders will make  $\sim 2$  revolutions in total;
- an angular encoder is mounted on the rotation shaft;
- the output voltage is converted to frequency and integrated  
integrated w.r.t. angle, so eliminating any  $\partial/\partial t$  effects;
- integrated signal is Fourier analysed digitally, giving  
harmonic amplitudes and phases.

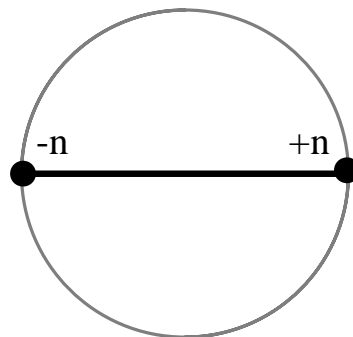
|                |                                       |                          |
|----------------|---------------------------------------|--------------------------|
| Specification: | relative accuracy of integrated field | $\pm 3 \times 10^{-4}$ ; |
|                | angular phase accuracy                | $\pm 0.2$ mrad;          |
|                | lateral positioning of magnet centre  | $\pm 0.03$ mm;           |
|                | accuracy of multipole components      | $\pm 3 \times 10^{-4}$   |

# Rotating coil configurations

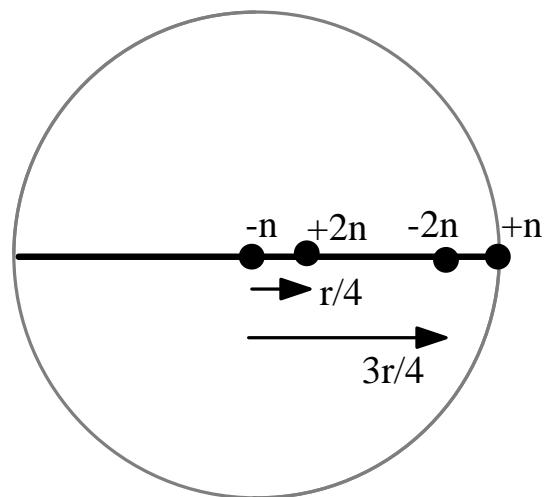
Multiple windings at different radii ( $r$ ) and with different numbers of turns ( $n$ ) are combined to cancel out harmonics, providing greater sensitivity to others:



All  
harmonics

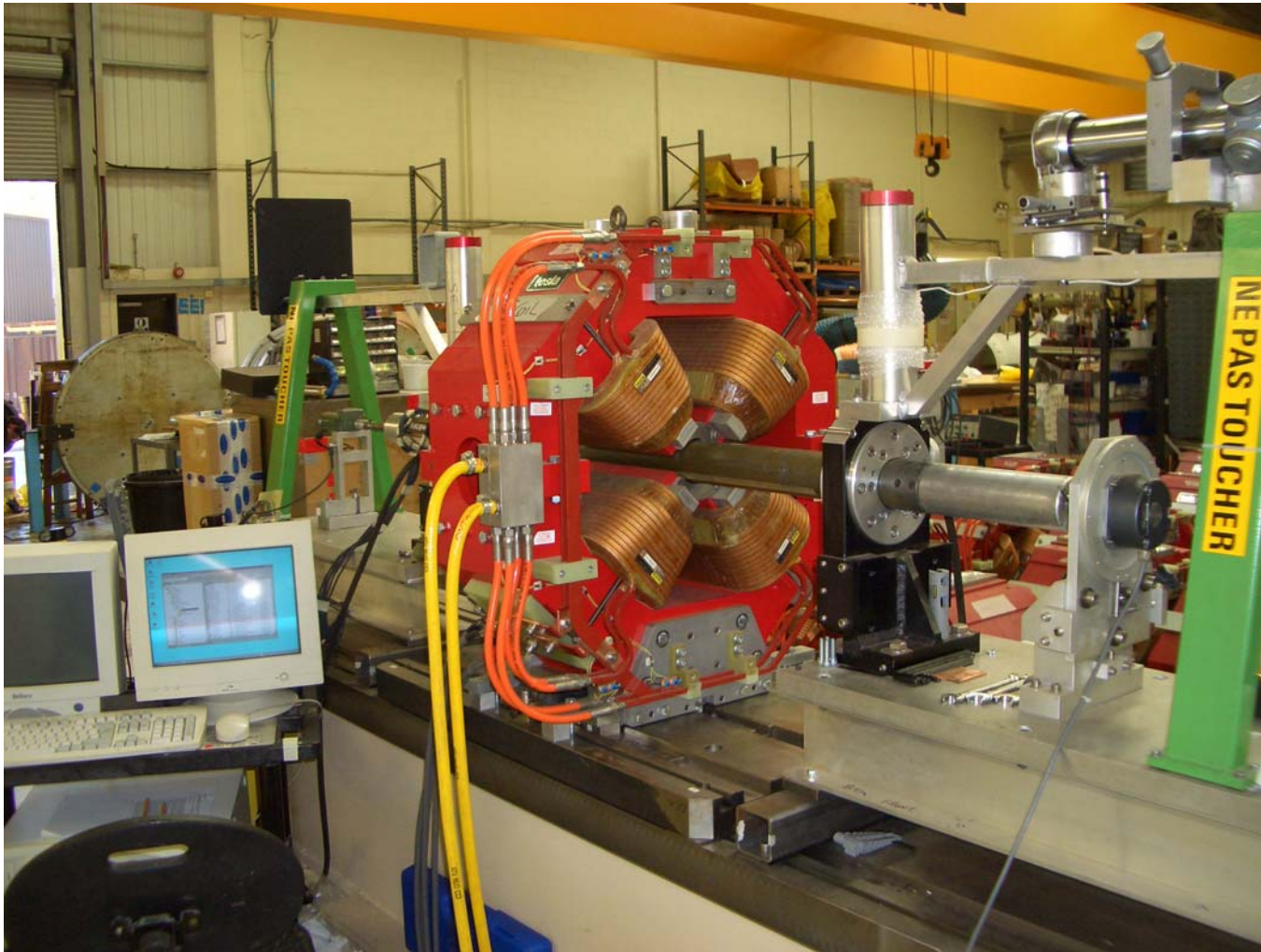


All odd  
harmonics,  
1,3,5 etc.



Dipole and  
quadrupole  
rejected.

# A rotating coil magnetometer.



# Test data used to judge Diamond quads.

|                                 |                                |                     |                                |                                  |     |
|---------------------------------|--------------------------------|---------------------|--------------------------------|----------------------------------|-----|
| Validity                        | This template is current       | Midplane adjustment | Next actions (Refer first):    |                                  |     |
| Iteration No.                   | 1                              | (+ to open)         | DLS referral done? (Yes/No/NA) | yes                              |     |
| Magnet type identifier          | WM                             | East (um):          | 240                            | Reject/Hold for refer? (S4, C6+) |     |
| Magnet serial                   | WMZ086                         | West (um):          | 80                             | Adjust vertical split (S3)?      | Yes |
|                                 |                                | Top (um):           | 80                             | Adjust midplane (C3/C4)?         | Yes |
|                                 |                                | Bottom (um):        | 0                              | Full align?                      |     |
| Date of test                    | 12/07/2005                     | C3 switch           | 1                              | Adjust dx only?                  |     |
| Tester                          | Darren Cox                     | S3 switch           | 1                              | Accept magnet?                   |     |
| Comments:                       | 180A preliminary               | C4 switch           | 1                              |                                  |     |
| DLS comments:                   | Please insert comments here    | S4++ switch         | 1                              |                                  |     |
| Dipole+NS007 reference angle    | 137.89068 (update fortnightly) | Full switch         | 1                              |                                  |     |
| Adjusted dipole reference angle | 137.90085                      | dx switch           | 1                              |                                  |     |

| Field quality data               |         | Post-shim prediction      | Alignment data [good pass/pass] | Value  | Outcome         |
|----------------------------------|---------|---------------------------|---------------------------------|--------|-----------------|
| R(ref) (mm)                      | 35.00   |                           | dx [0.025/0.05]mm               | -0.089 | Fail            |
| Current (A)                      | 180.00  |                           | dy [0.025/0.05]mm               | -0.059 | Fail            |
| Central strength (T/m)           | 17.6328 |                           | dz [2.5/5.0]mm                  | 2.414  | Good pass       |
| L(ef) (mm)                       | 407.253 |                           | Roll [0.1/0.2]mrad              | 0.052  | Good pass       |
| C3 (4-8)                         | -0.49   | Pass                      | Yaw [0.15/0.3]mrad              | -0.048 | Good pass       |
| S3 (6-12)                        | -10.88  | Refer, or shim vertical   | Pitch [0.15/0.3]mrad            | -0.085 | Good pass       |
| C4 (4-7)                         | 6.90    | Refer, or shim horizontal |                                 |        |                 |
| S4 (1-4)                         | 0.80    | Pass                      |                                 |        |                 |
| C6 (2.5-10)                      | 7.97    | Refer to DLS              |                                 |        | Adjust X alone? |
| C10,S10 : (N:3-5, W:6-8)         | 5.16    | Pass                      |                                 |        | Alignment OK?   |
| All other terms up to 20 (2.5-5) | 4.98    | Refer to DLS              |                                 |        |                 |

| Keys to use                 | N key | S key | NW foot | NE foot | SW foot | SE foot |
|-----------------------------|-------|-------|---------|---------|---------|---------|
| Next shims to use (rounded) | N/A   | N/A   | N/A     | N/A     | N/A     | N/A     |

| Shimming History      |        |        |         |         |         |         |
|-----------------------|--------|--------|---------|---------|---------|---------|
| Iteration#            | N key  | S key  | NW foot | NE foot | SW foot | SE foot |
| Shims in use          | 32.010 | 32.012 | 19.011  | 19.020  | 19.004  | 19.015  |
| Next shims (measured) | 0.000  | 0.000  | 0.000   | 0.000   | 0.000   | 0.000   |
| 3                     | 0.000  | 0.000  | 0.000   | 0.000   | 0.000   | 0.000   |
| 4                     | 0.000  | 0.000  | 0.000   | 0.000   | 0.000   | 0.000   |
| 5                     | 0.000  | 0.000  | 0.000   | 0.000   | 0.000   | 0.000   |
| Rounding errors       | 0.000  | 0.000  | 0.000   | 0.000   | 0.000   | 0.000   |
| Warnings              |        |        |         |         |         |         |