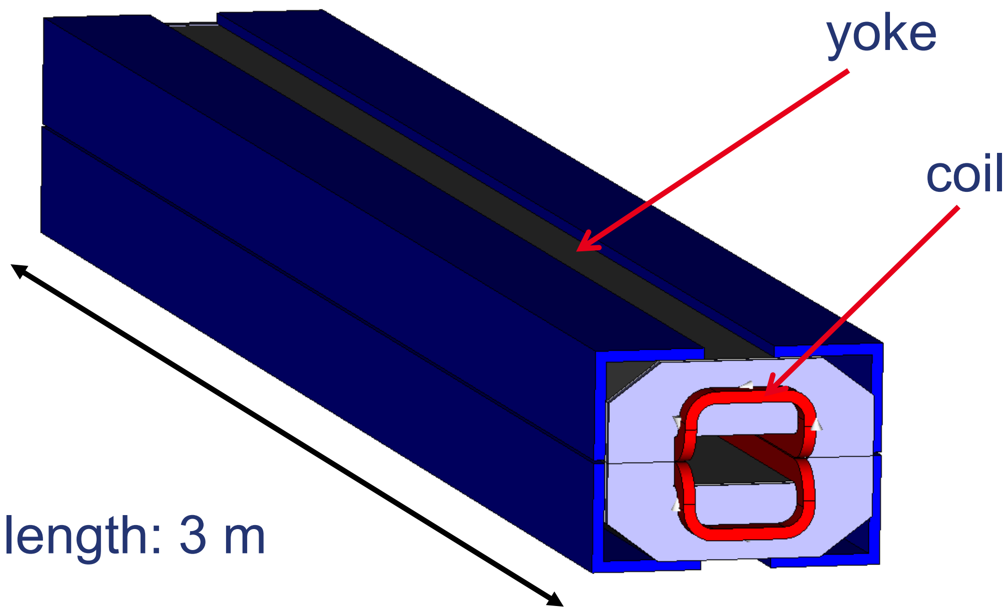
Field Solvers

Prof. Dr.-Ing. Herbert De Gersem

CERN Accelerator School 2018
Thessaloniki, Greece, 11-23 November 2018

Lecture 1 : Electromagnetic Field Simulation for Accelerators: Overview

Example: accelerator magnet



comparably simple ?

Example: GSI-SIS-100 magnet

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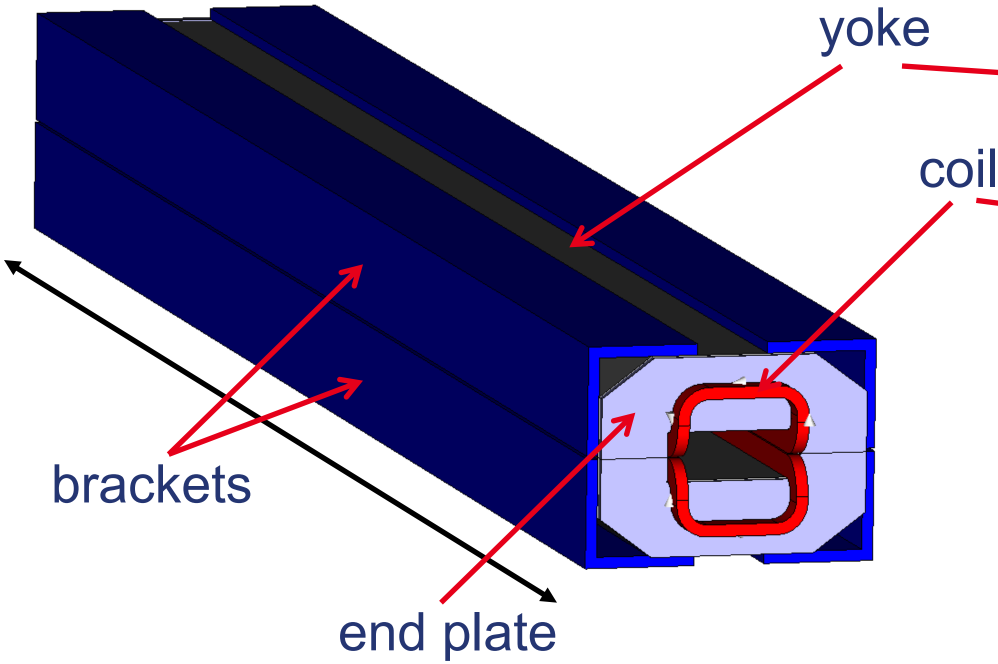


SIS100 dipole (prototype)

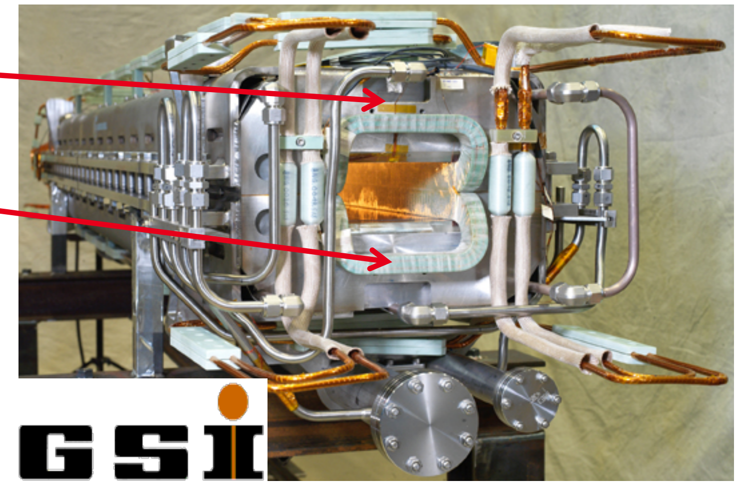


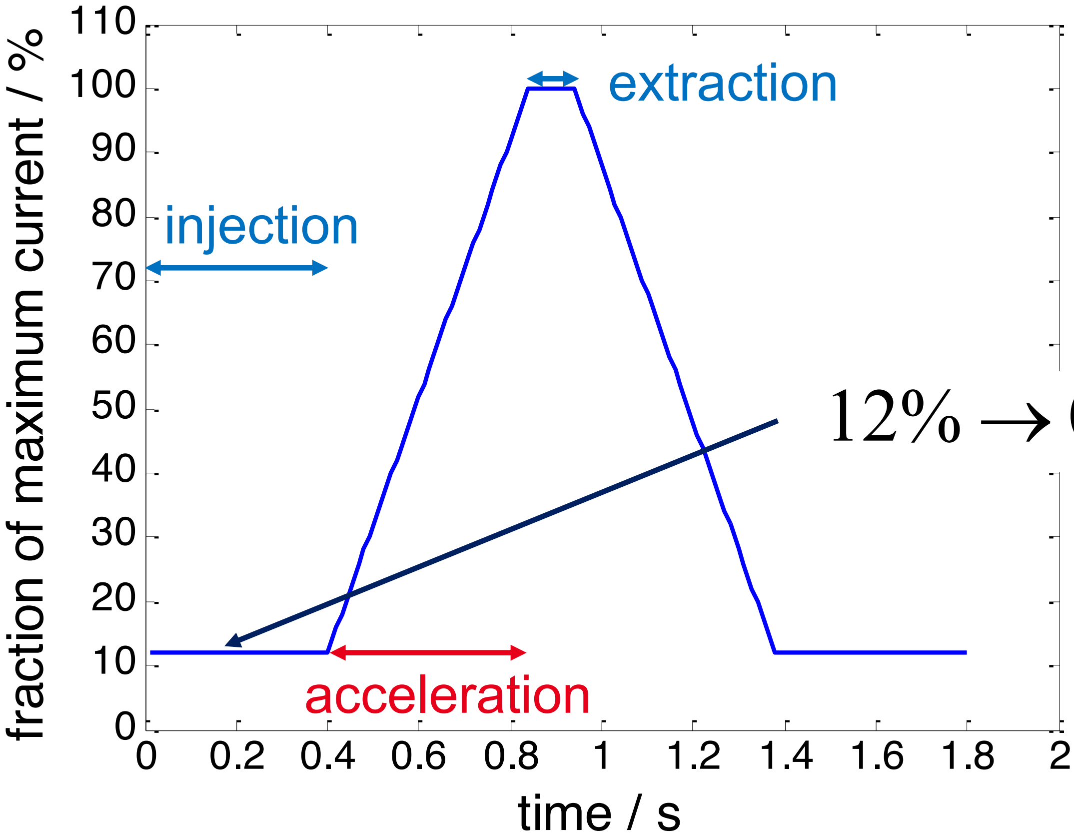
photo: J. Guse, GSI (www.gsi.de)

many geometric details
superconductive coils
helium cooling
mechanical deformation
radioactive hazards

length: 3 m

Example: GSI-SIS-100 magnet

excitation profile



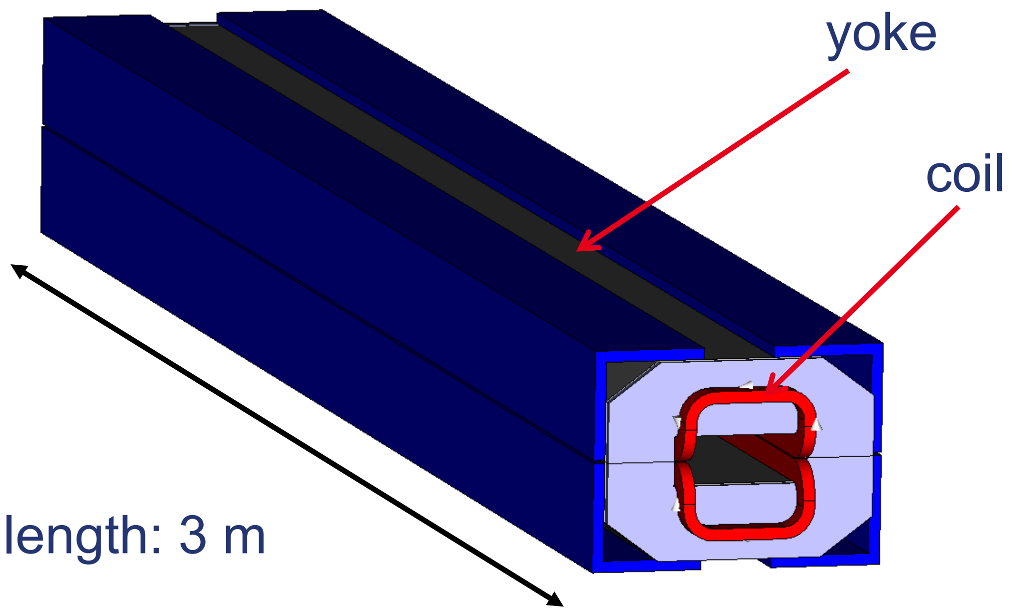
$12\% \rightarrow 0.24\ \mathrm{T}$

eddy currents

quench of superconductors

hysteresis

Example: accelerator magnet

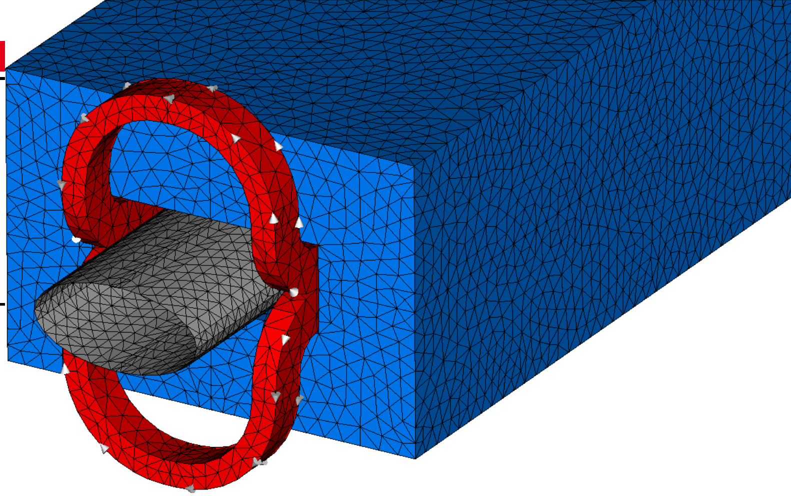


~~comparably simple ?~~

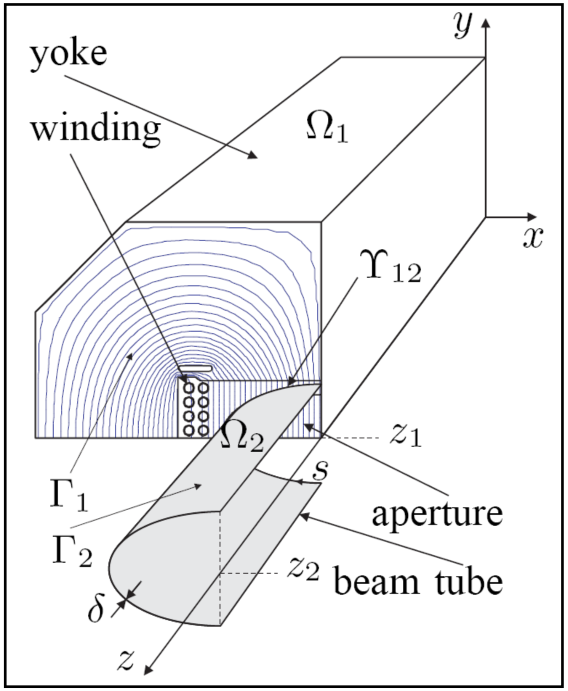
↓

unexpected complexity !

Overview



- magnet simulation (standard 3D FE solver)
- challenges
  - geometrical details
  - materials
  - transient effects
  - high accuracy
- magnet simulation (dedicated 3D FE solver)
- hybrid models
- stochastic models
- conclusions



Magnetoquasistatic formulation

differential equation: $$\nabla \times \left(\nu \nabla \times \vec{A} \right) + \sigma \frac{\partial \vec{A}}{\partial t} = \vec{J}_s$$

reluctivity

magnetic vector potential

conductivity

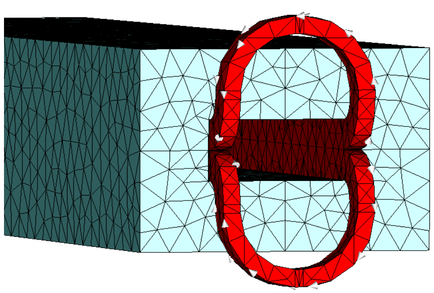
applied current density

Discretisation in space

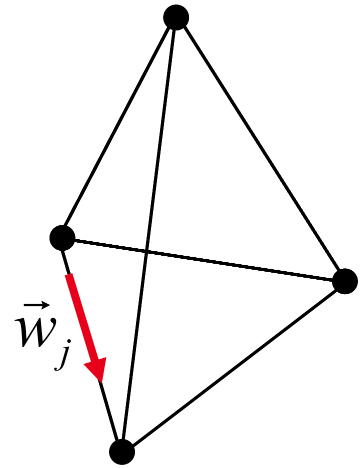
differential equation: $\nabla \times \left(\nu \nabla \times \vec{A} \right) + \sigma \frac{\partial \vec{A}}{\partial t} = \vec{J}_\mathrm{s}$

spatial discretisation $\vec{A} \approx \vec{A}_\mathrm{FE} = \sum_j \widehat{a}_j \vec{w}_j$

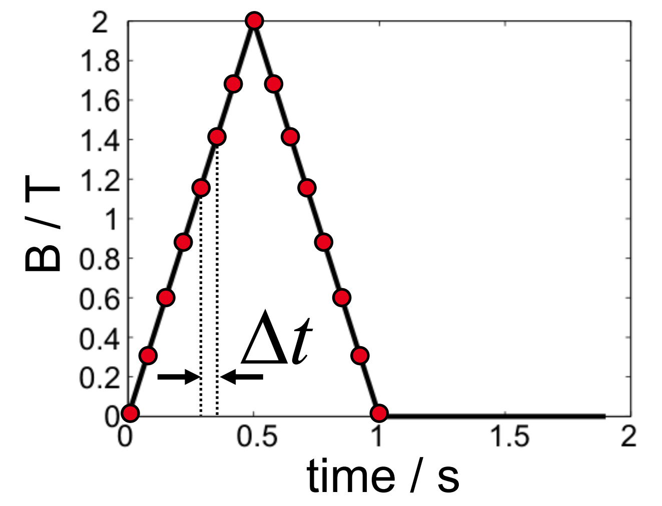
semi-discrete system: $\mathbf{K}_\nu \widehat{\mathbf{a}} + \mathbf{M}_\sigma \frac{\mathrm{d}\widehat{\mathbf{a}}}{\mathrm{d}t} = \widehat{\mathbf{j}}_\mathrm{s}$



shape functions:
edge finite elements
(curl-conforming)



Discretisation in time



differential equation

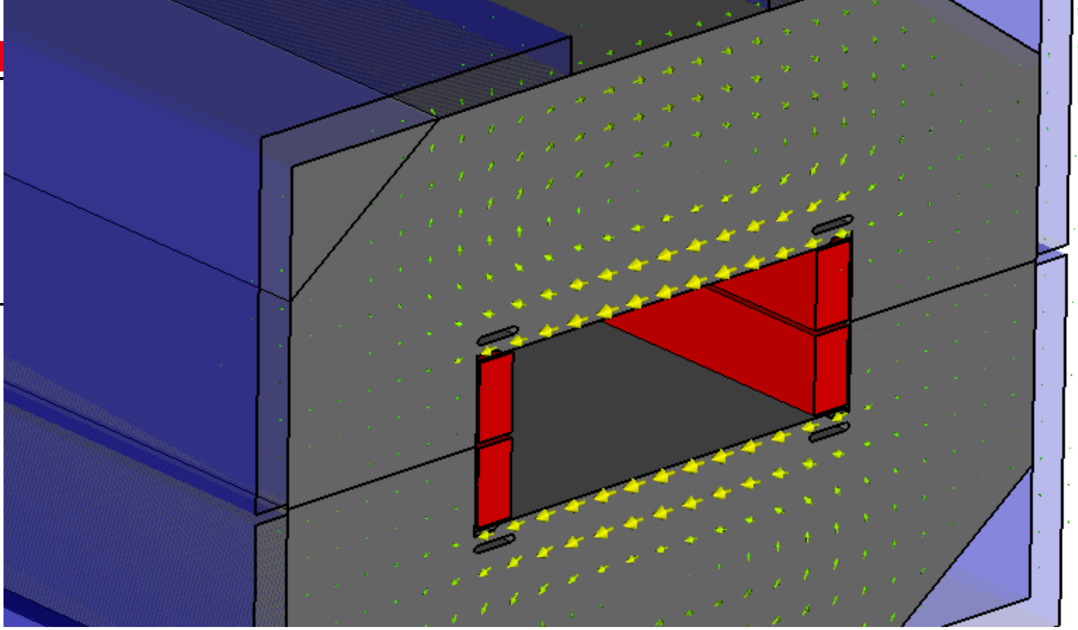
spatial discretisation

semi-discrete system: $$\mathbf{K}_{\nu}\widehat{\mathbf{a}} + \mathbf{M}_{\sigma}\frac{\mathrm{d}\widehat{\mathbf{a}}}{\mathrm{d}t} = \widehat{\mathbf{j}}_{\mathrm{s}}$$

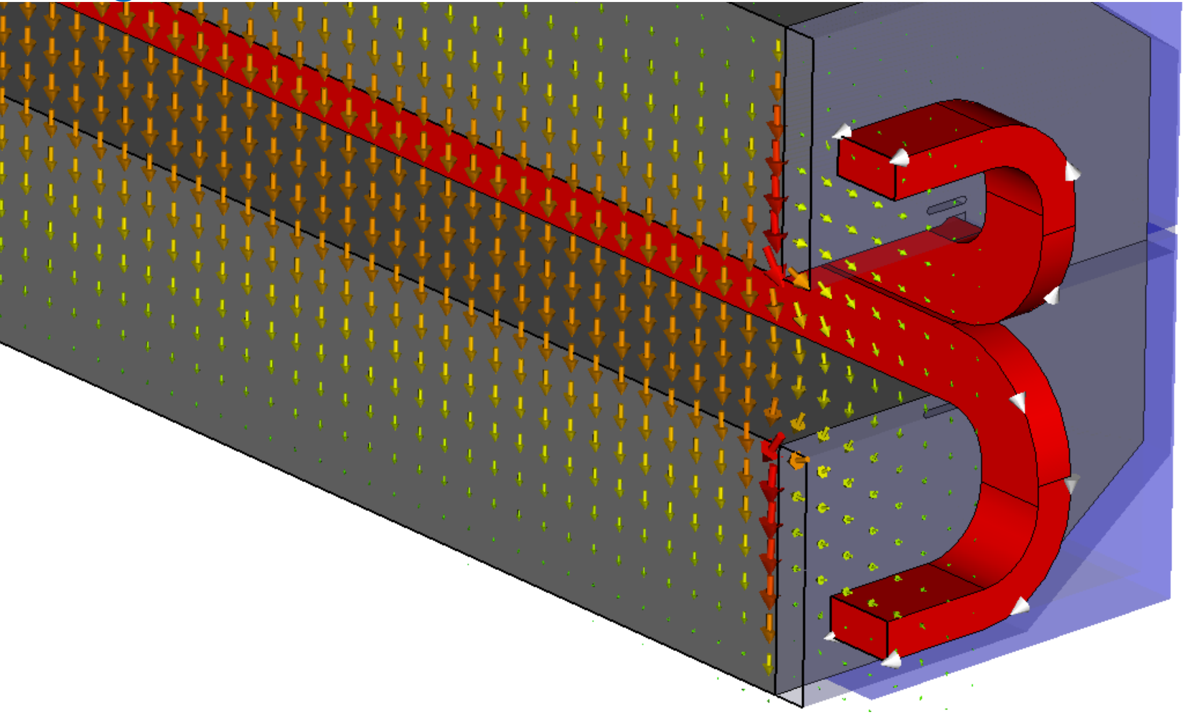
temporal discretisation

discrete system: $$\left(\mathbf{K}_{\nu} + \alpha\mathbf{M}_{\sigma}\right)\widehat{\mathbf{a}}_{k+1} = \mathrm{RHS}$$

Results



magnetic field



eddy currents
in the end plane

simulation by
CST EMStudio®

Electromagnetic field solvers

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- commercial
  or academic
  or freeware
- low-frequency
  and/or high-frequency
- circuit
  and/or 2D fields
  and/or 3D fields
- problem specific
  or multi-purpose
- electromagnetic fields
  and/or multi-physics
- cheap or expensive

non-exhaustive list !!

CEDRAT
CST
JMAG
infolytica corporation
opera simulation software
ANSYS
FEMM
FEKO Comprehensive Electromagnetic Solutions
COMSOL MULTIPHYSICS

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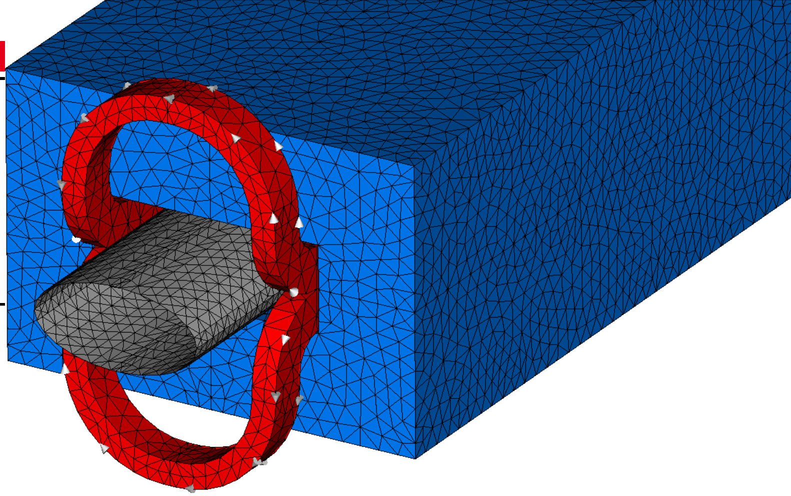
non-exhaustive list !!

FEMM

Overview



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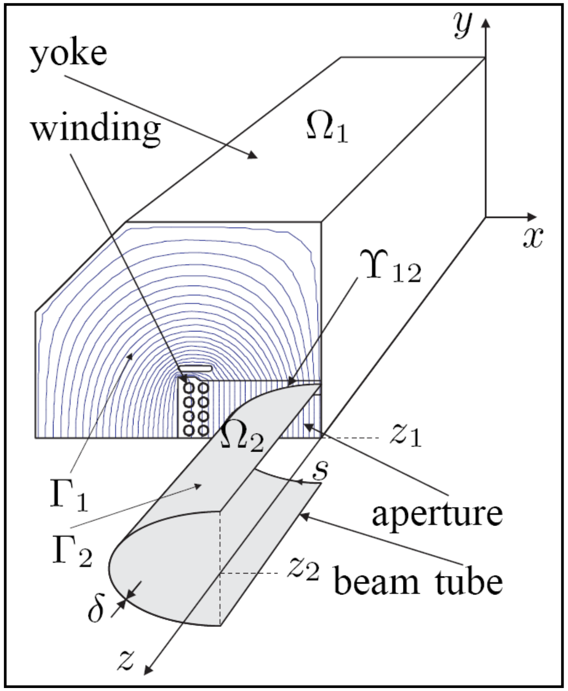


Challenge 1: Detailed geometry

yoke

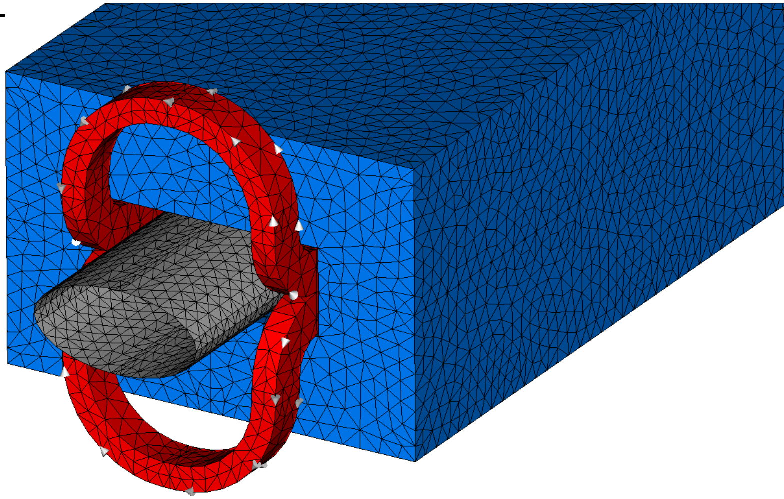
- length (meter)
  vs. lamination thickness (mm)
- shimming, holes

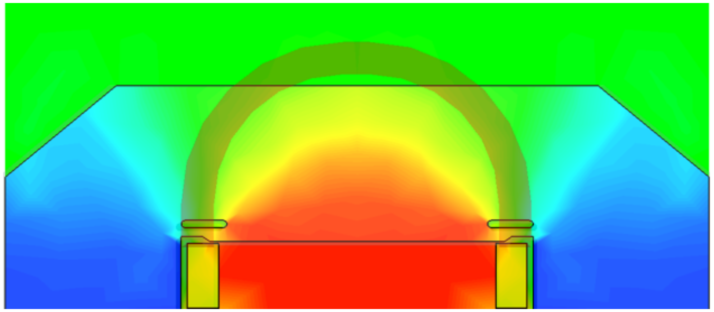
beam tube

- < 1mm thick

end-winding parts

- determine the eddy currents
  in the end plates





Challenge 2: Materials

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yoke iron:

- anisotropic (rolling & transverse direction)

$$\bar{\bar{\nu}}(\vec{B}) = R^T \begin{bmatrix} \nu_{\text{rol}} & & \\ & \nu_{\text{trans}} & \\ & & \nu_{\text{trans}} \end{bmatrix} R$$

ν_{rol} reluctivity in the rolling direction

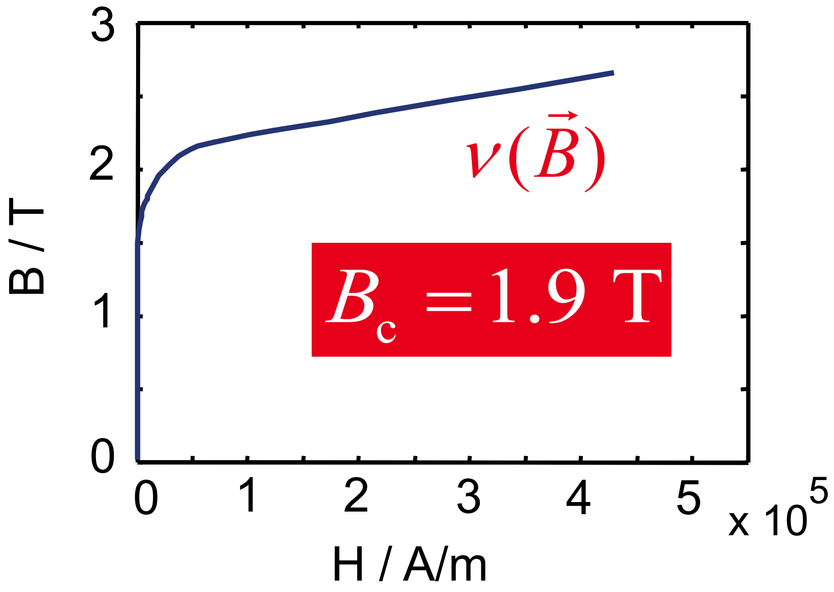
ν_{trans} reluctivity in the transversal direction

R local rotation matrix

Challenge 2: Materials

yoke iron:

- anisotropic (rolling & transverse direction)
- nonlinear (saturation)



Newton method

Challenge 2: Materials

yoke iron:

- anisotropic (rolling & transverse direction)
- nonlinear (saturation)
- hysteretic (remanent field)

Jiles-Atherton model

Preisach model

estimation of losses by Steinmetz-Bertotti

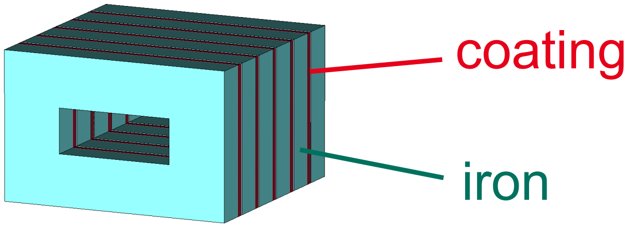
Challenge 2: Materials

yoke iron:

- anisotropic (rolling & transverse direction)
- nonlinear (saturation)
- hysteretic (remanent field)
- composite (lamination)

stacking factor

$$\gamma_{\mathrm{st}} \approx 0.95 \leq\sim 1$$



(simple) homogenisation along lamination direction

$$\frac{1}{\nu_{xy}} = \frac{\gamma_{\mathrm{st}}}{\nu_{\mathrm{Fe}}} + \frac{1-\gamma_{\mathrm{st}}}{\nu_0}$$

perpendicular to laminates

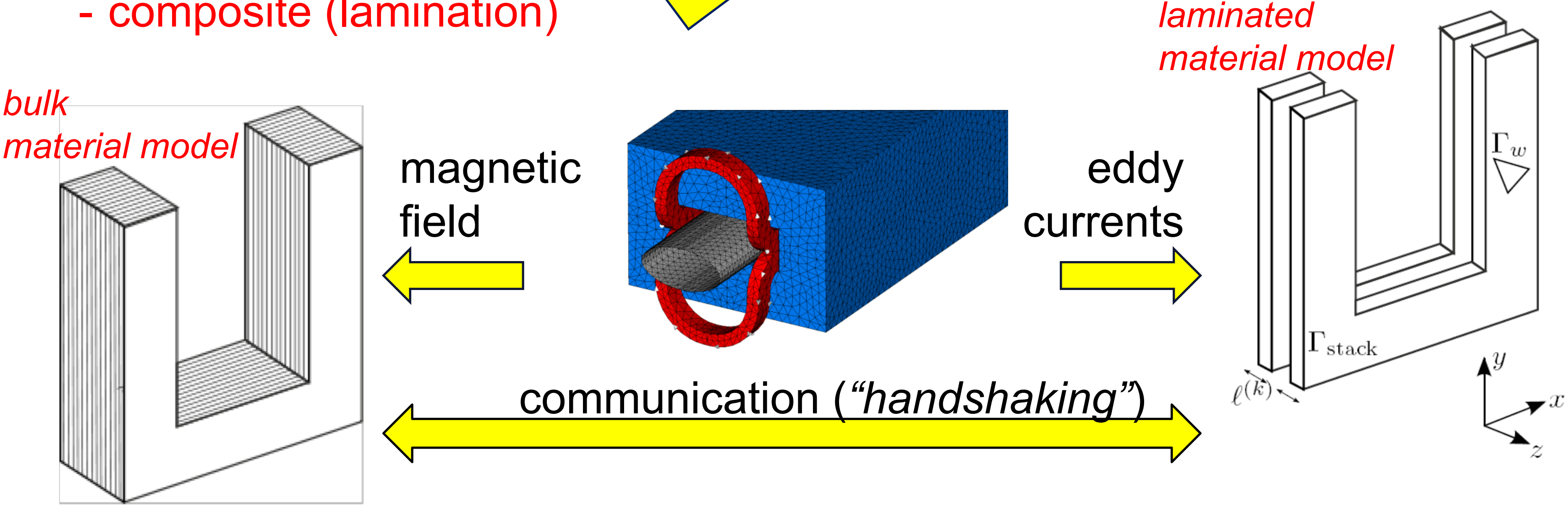
$$\nu_z = \gamma_{\mathrm{st}}\nu_{\mathrm{Fe}} + \left(1-\gamma_{\mathrm{st}}\right)\nu_0$$

Challenge 2: Materials

yoke iron:

- anisotropic (rolling & transverse direction)
- nonlinear (saturation)
- hysteretic (remanent field)
- composite (lamination)

multiscale simulation



Challenge 2: Materials

yoke iron:

- anisotropic (rolling & transverse direction)
- nonlinear (saturation)
- hysteretic (remanent field)
- composite (lamination)
- variability

→ stochastics, sensitivity

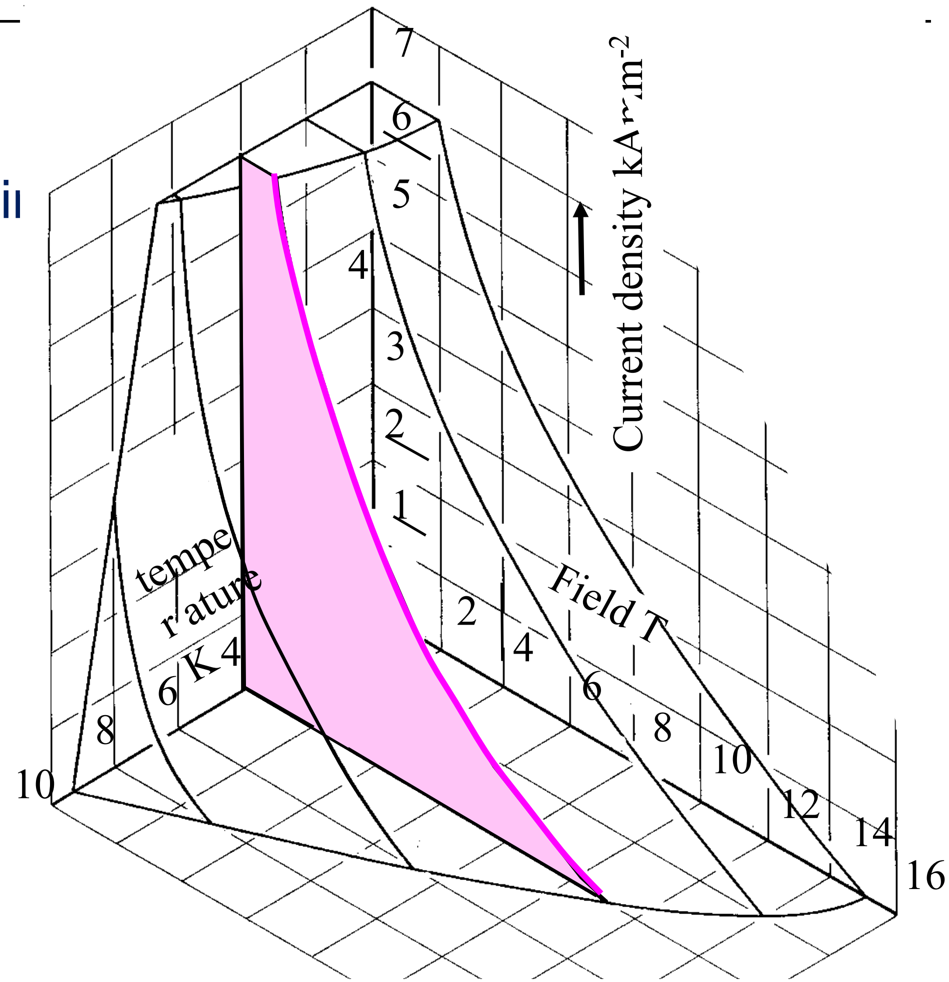
Challenge 2: Materials

yoke iron:

- anisotropic (rolling & transverse di
- nonlinear (saturation)
- hysteretic (remanent field)
- composite (lamination)
- variability

superconductor:

- critical current
- temperature
- magnetic field



Challenge 3: Transient phenomena

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lamination

- hysteresis + remanence

Jiles-Atherton model

Preisach model

estimation of the remanence
(based on data from material vendor)

Challenge 3: Transient phenomena

lamination

- hysteresis + remanence
- eddy currents

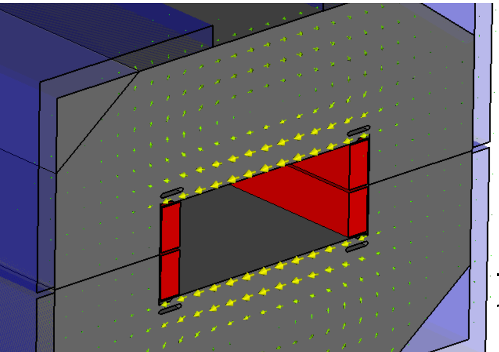
$$\nabla \times \left(\nu \nabla \times \vec{A} \right) + \sigma \frac{\partial \vec{A}}{\partial t} = \vec{J}_{\mathrm{s}}$$

eddy current term

+ (simple) homogenisation $\sigma_{xy} = \gamma_{\mathrm{st}} \sigma_{\mathrm{Fe}}$

$$\sigma_z = 0$$

or + multi-scale model (hand-shaking)



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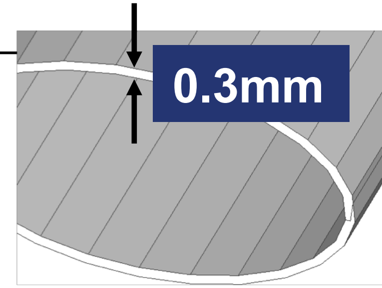
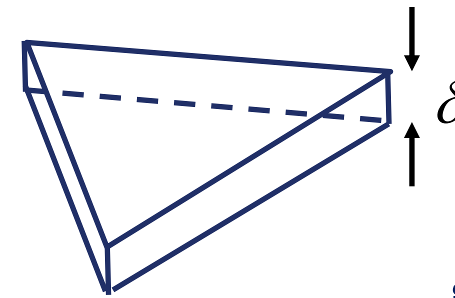
Challenge 3: Transient phenomena





lamination

- hysteresis + remanence
- eddy currents

beam tube

- eddy currents

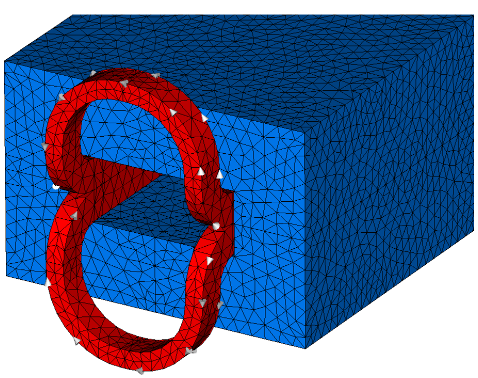
shell elements

additional matrix contributions $\mathbf{K}_\delta$ and $\mathbf{M}_\delta$

assembling into system matrix by $\mathbf{Q}$

$$\mathbf{K}_\nu + \sigma \mathbf{M}_\sigma \quad + \quad \mathbf{Q}^{\mathrm{T}} \left(\mathbf{K}_\delta + \alpha \mathbf{M}_\delta \right) \mathbf{Q} \quad = \quad \mathbf{K}_{\mathrm{full}} + \alpha \mathbf{M}_{\mathrm{full}}$$

+ Jens Trommler



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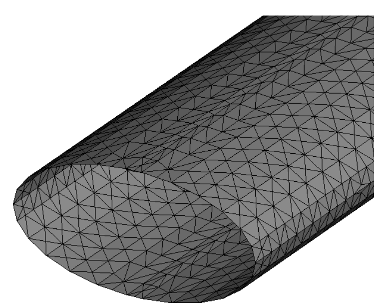

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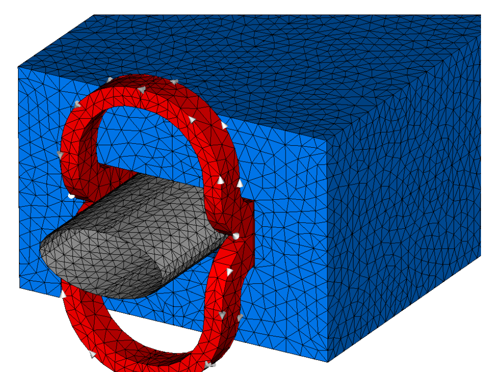


Challenge 3: Transient phenomena

lamination

- hysteresis + remanence
- eddy currents

beam tube

- eddy currents

superconductor

- persistent currents

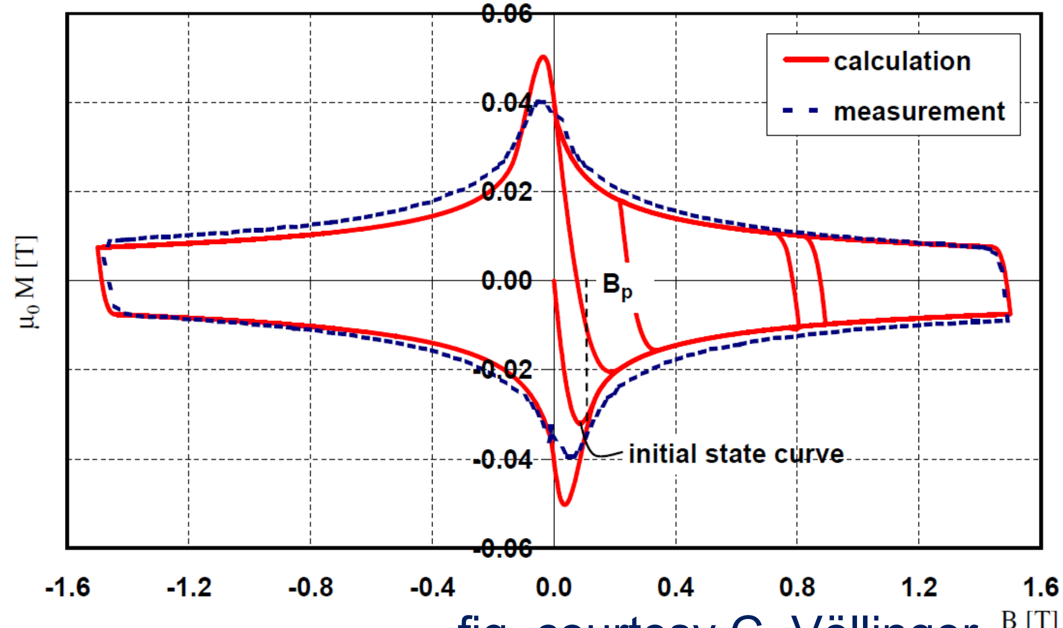


fig. courtesy C. Völlinger

Bean model → magnetisation (Christine Völlinger) implemented in ROXIE

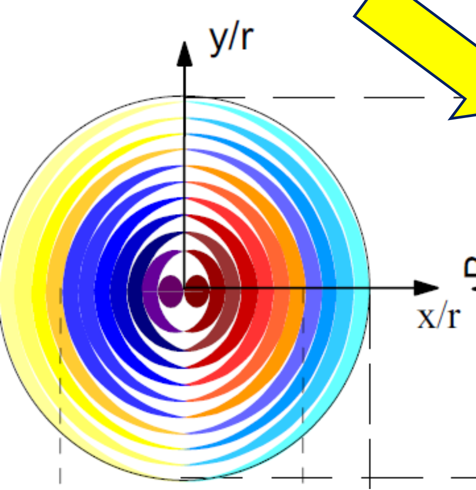


fig. courtesy C. Völlinger

Challenge 3: Transient phenomena

lamination

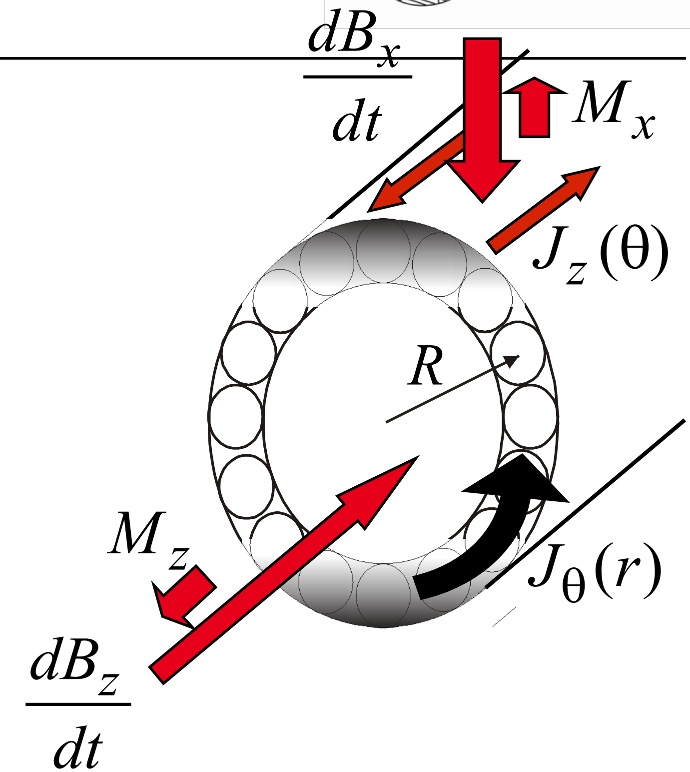
- hysteresis + remanence
- eddy currents

beam tube

- eddy currents

superconductor

- persistent currents
- coupling currents
- cable eddy currents



$$\nabla \times \left(\nu \nabla \times \vec{A}\right) + \sigma \frac{\partial \vec{A}}{\partial t} + \nabla \times \left(\nu_0 \bar{\bar{\tau}}_{\mathrm{cb}} \nabla \times \frac{\partial \vec{A}}{\partial t} \right) = \vec{J}_{\mathrm{s}}$$

additional magnetisation

Challenge 4: High accuracy requirements

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losses

- dimensioning of the cooling system
- hot spots
- quench

aperture field

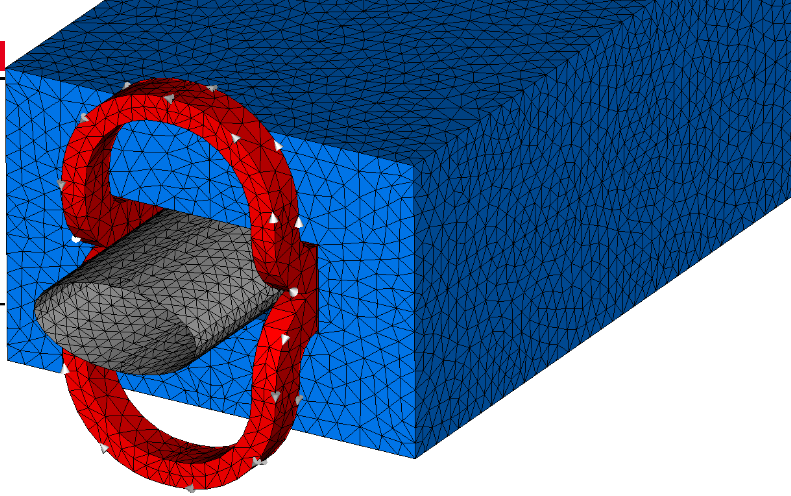
- multipoles during injection, ramping and extraction
- + influence of eddy currents

→

huge models

parallelisation, multi-core computers

Overview



- magnet simulation
  (standard 3D FE solver)
- challenges
  - geometrical details
  - materials
  - transient effects
  - high accuracy
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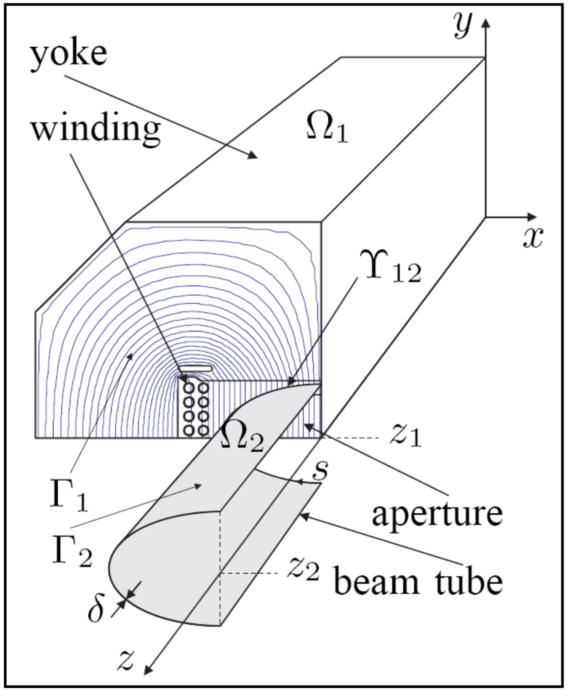
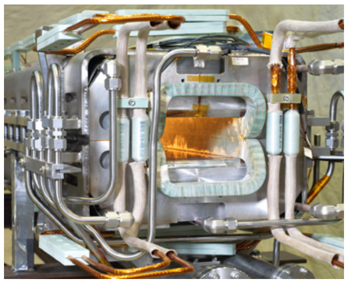
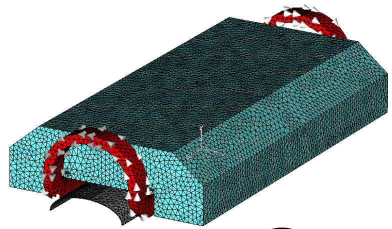
- stochastic models
- conclusions



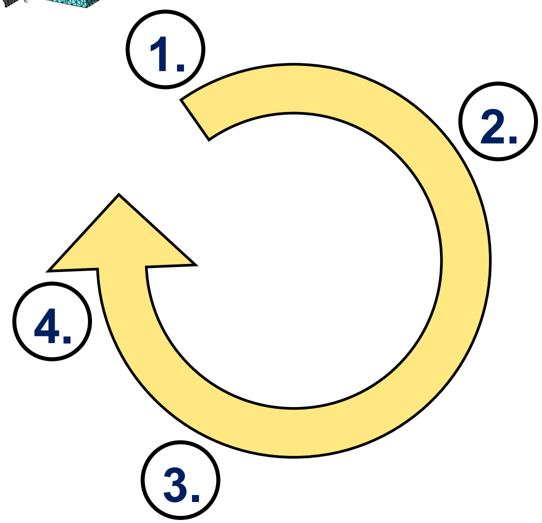
Dedicated Simulation Tool





FEMSTER, LLNL

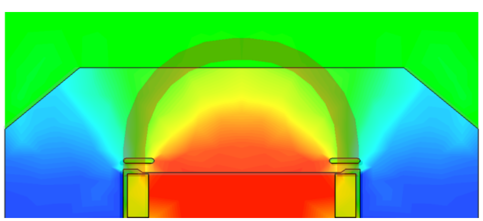
TRILINOS, Sandia Labs



CST Studio Suite®

- CAD modelling
- meshing

- visualisation



own software

- FE assembly (higher order FEs)
- transient solver
- nonlinear materials
- system solver

Matlab

- postprocessing
- visualisation

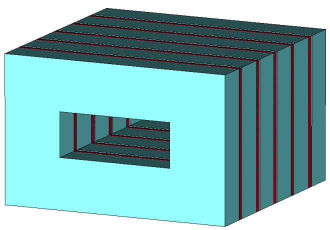
parallelisation

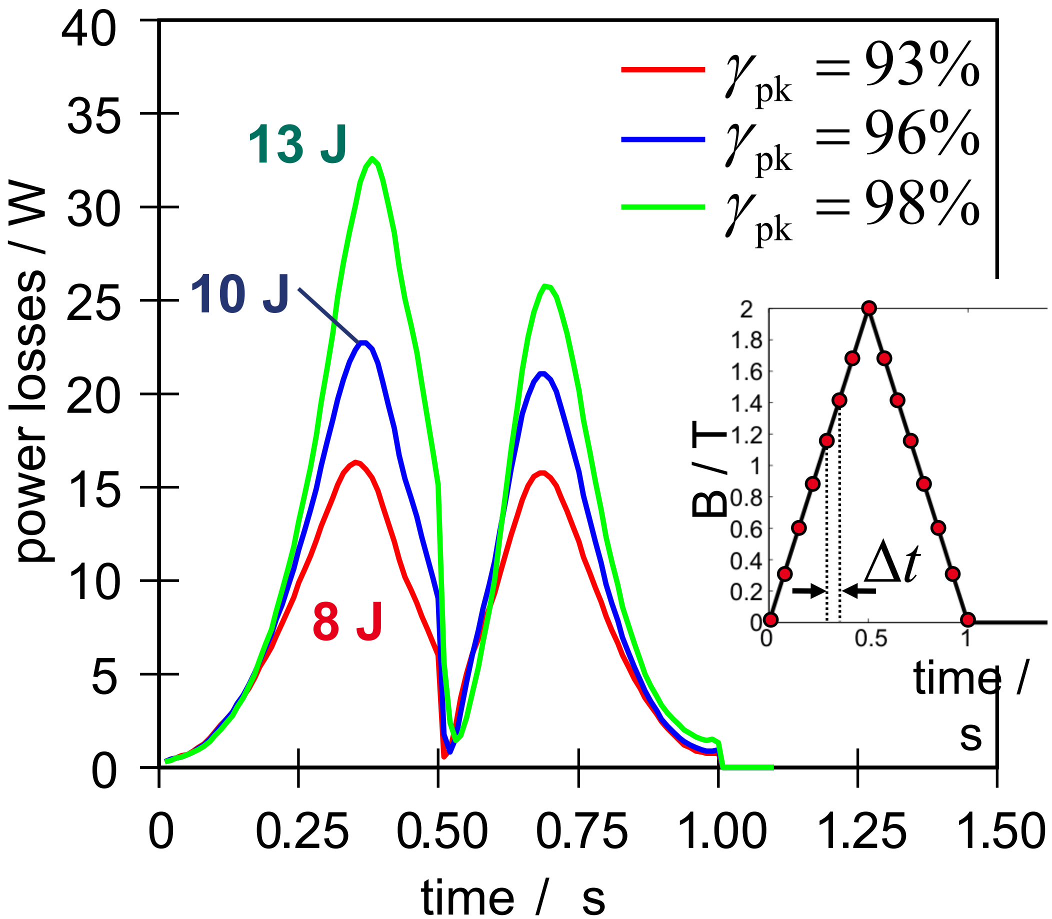
+ Stephan Koch, Jens Trommler

Results: Eddy-Current Losses

eddy-current losses over one cycle

for different stacking factors γ_{pk}





loss energy: $W = \int_0^T P \mathrm{d}t$

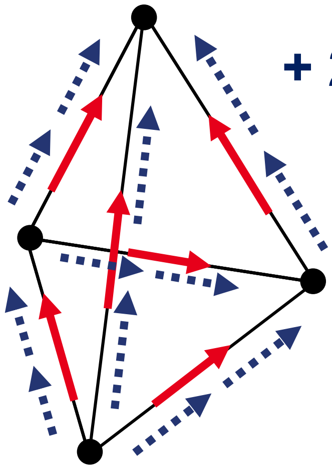
+ Stephan Koch, Jens Trommler

Results: Loss Energy

- discretization:
  - increase number of elements
  - increase order of approximation

$$\vec{A} \approx \vec{A}_{\mathrm{FE}} = \sum_j a_j \vec{w}_j^{\mathrm{tv}}$$

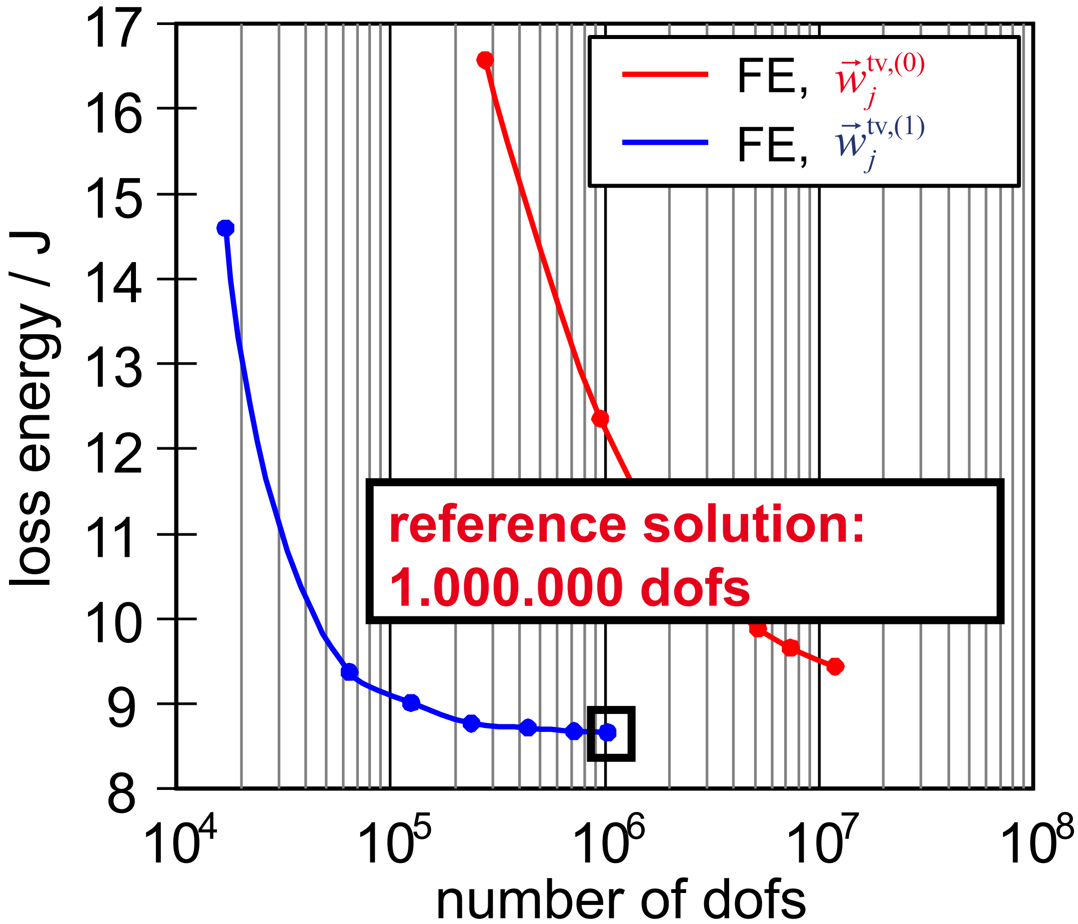
degrees of freedom:



+ 2 per face

$\vec{w}_j^{\mathrm{tv},(0)}$ $n_{\mathrm{dof}} = 6$

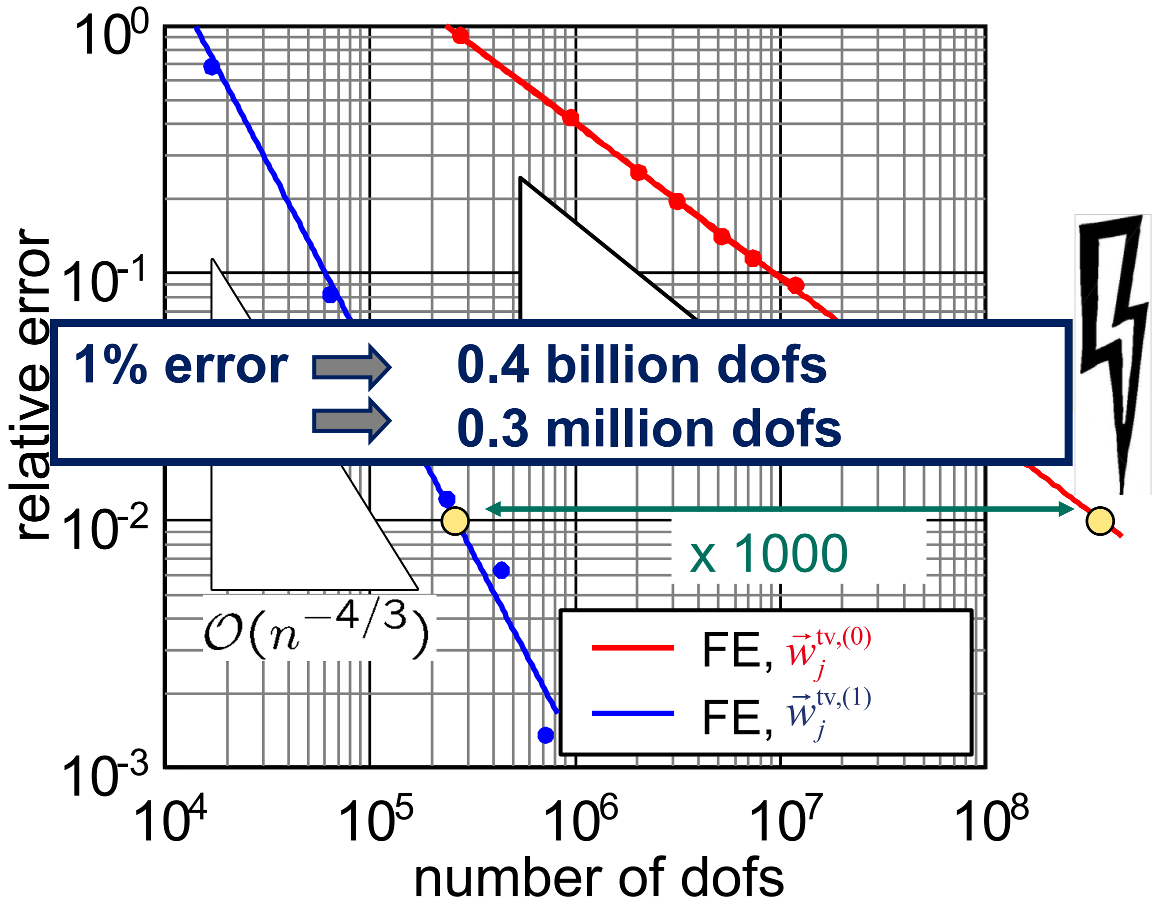
$\vec{w}_j^{\mathrm{tv},(1)}$ $n_{\mathrm{dof}} = 20$



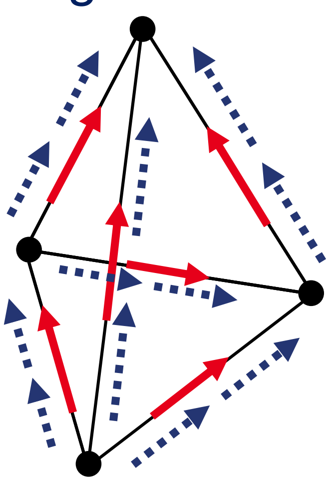
+ S. Koch, J. Trommler

Convergence: Loss Energy

- relative error with respect to reference solution



degrees of freedom:



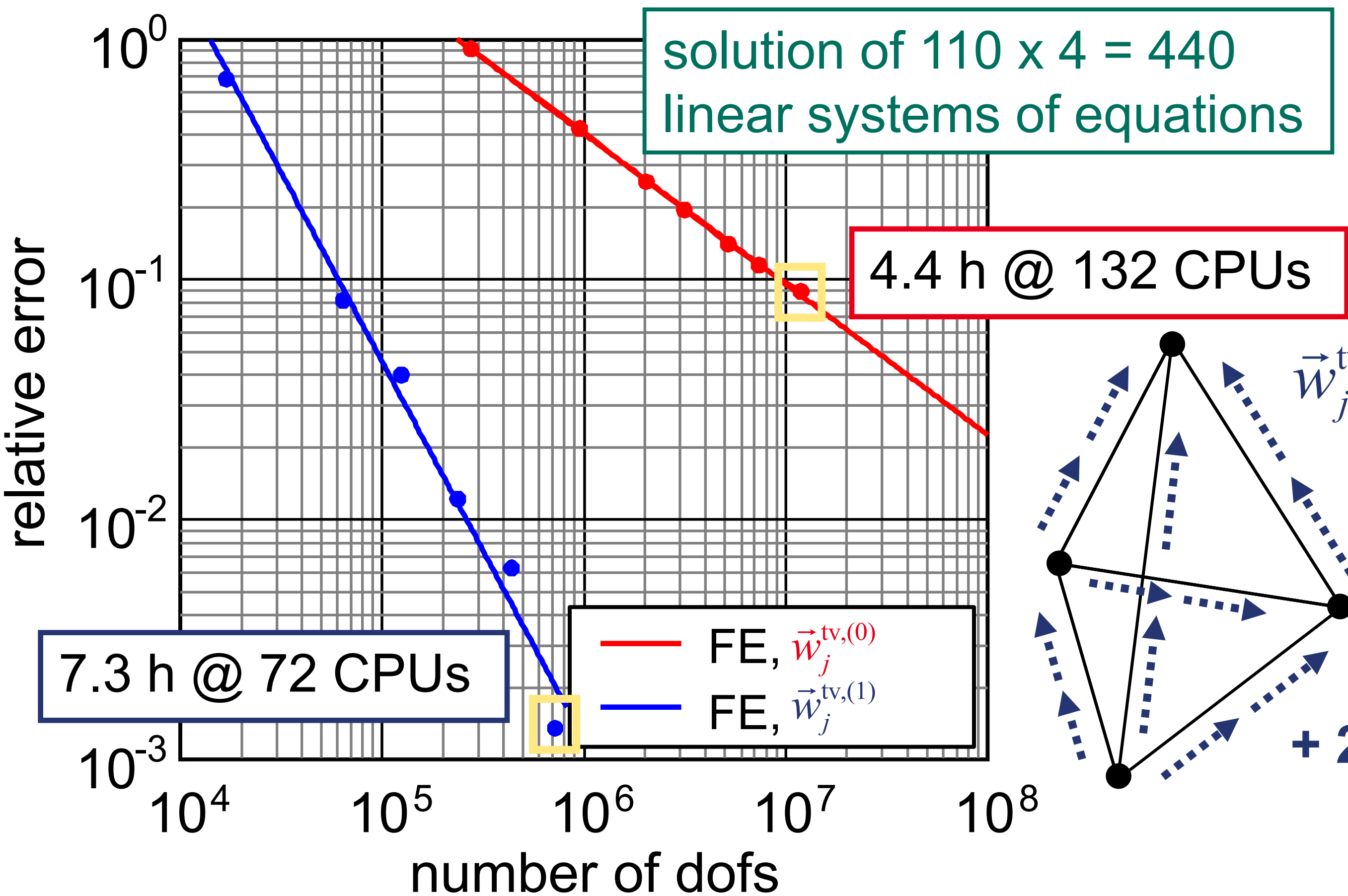
+ 2 per face

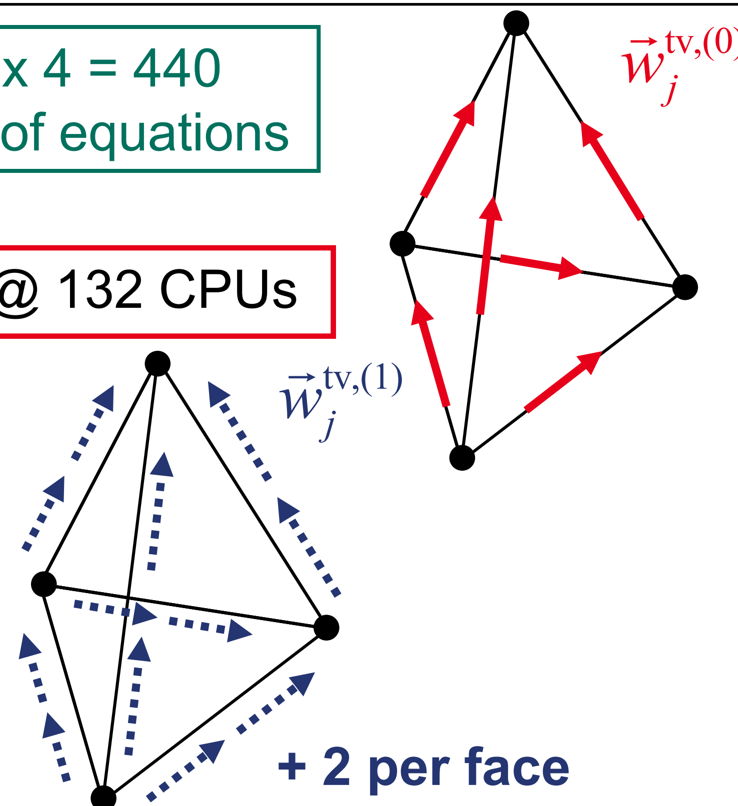
$\vec{w}_j^{\mathrm{tv},(0)}$

$\vec{w}_j^{\mathrm{tv},(1)}$

+ S. Koch, J. Trommler

Comparison: Shape Functions





+ S. Koch, J. Trommler

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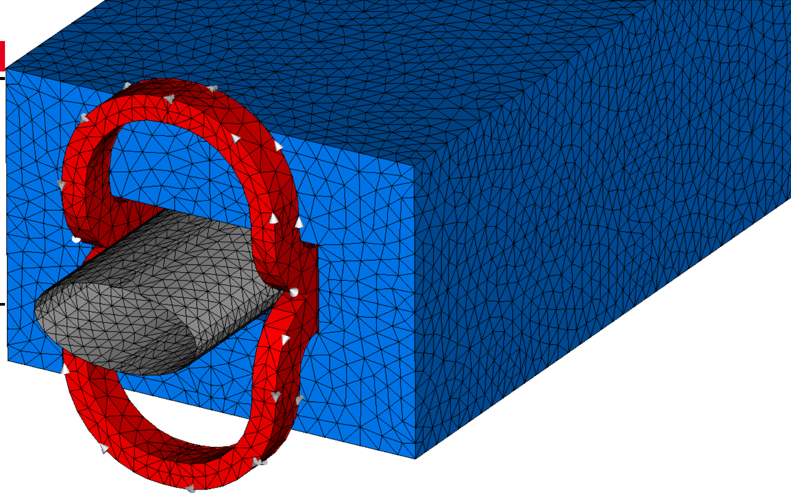

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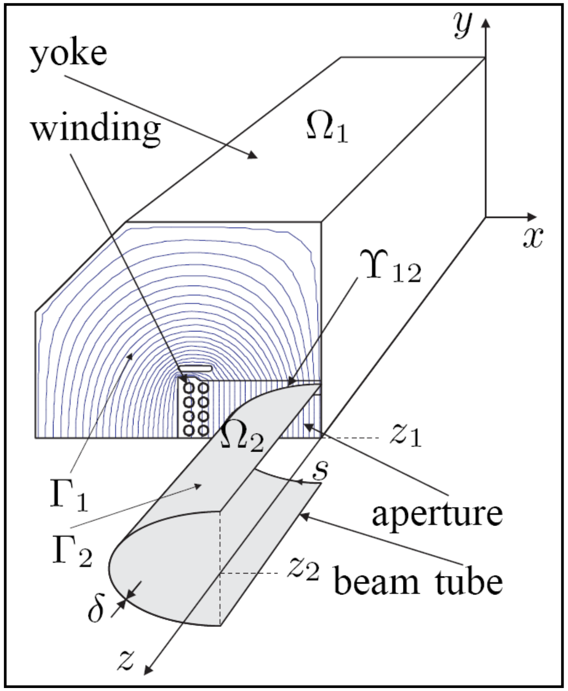
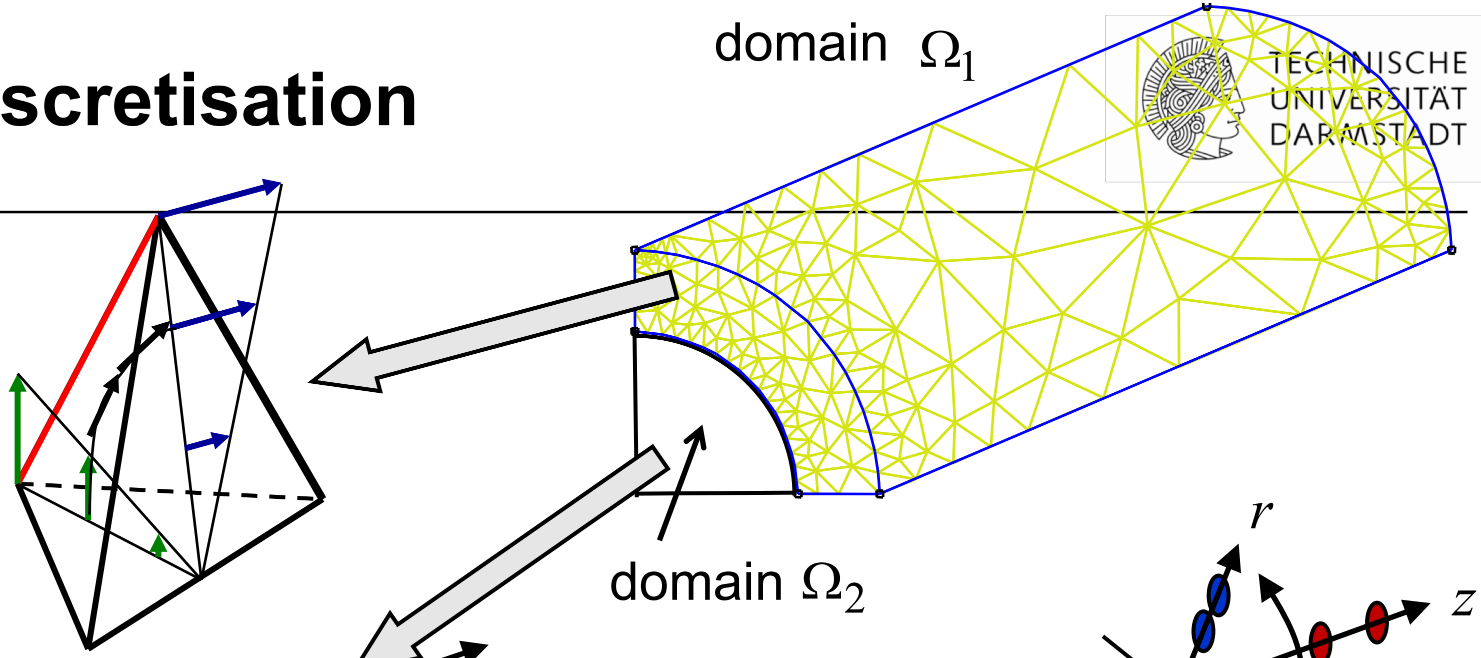
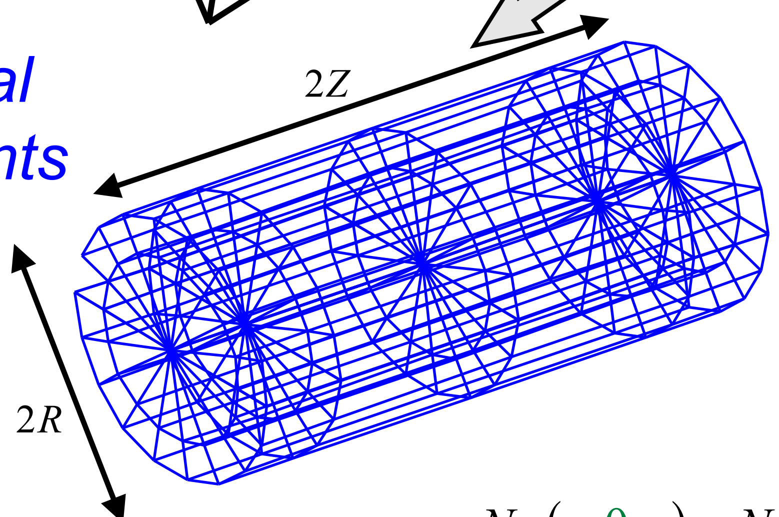


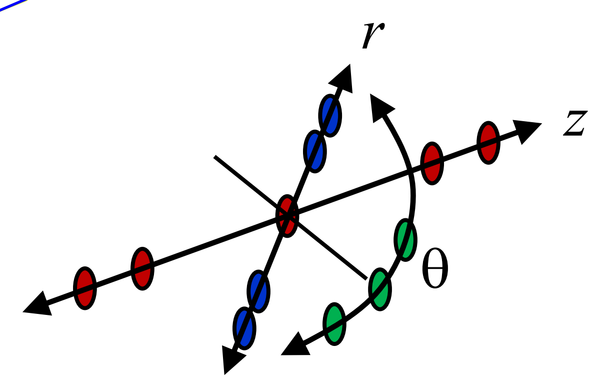
Hybrid discretisation

(edge) finite elements



spectral elements



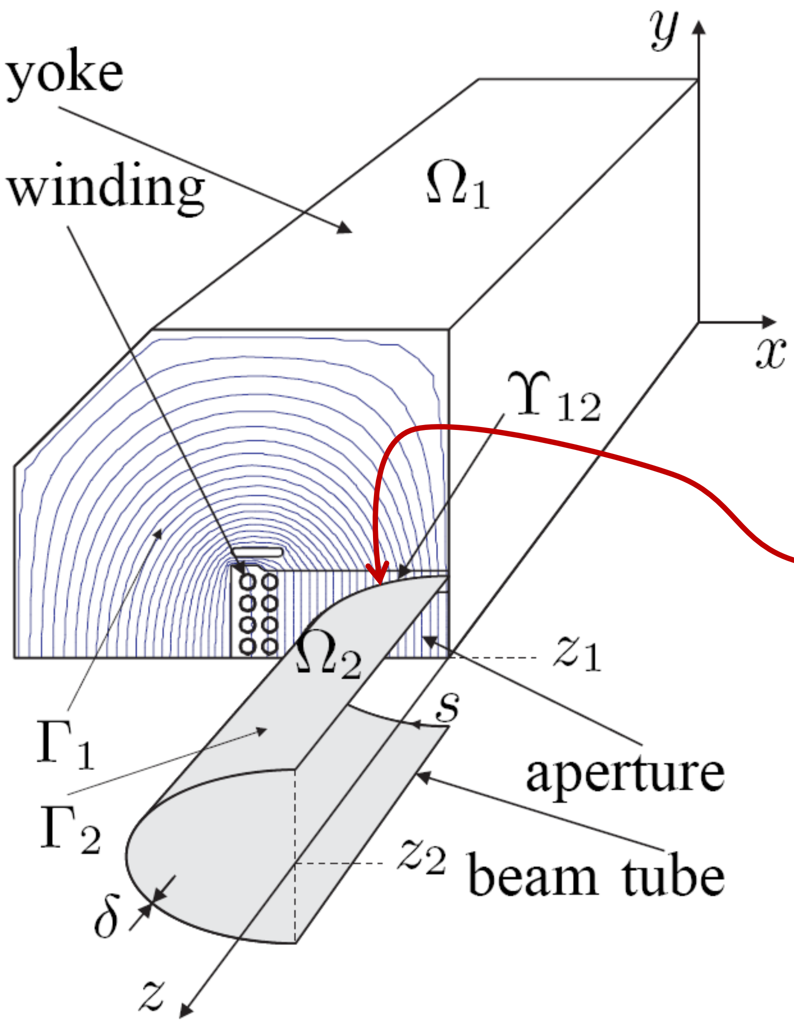


Legendre distribution in *r*
equidistant distribution in *θ*
Legendre distribution in *z*

$$N_q(r,\theta,z) = N_{q_1,q_2,\lambda}(r,\theta,z) = P_{q_1}\left(\frac{r}{R}\right)e^{-j\lambda_q\theta}P_{q_2}\left(\frac{z}{Z}\right)$$

+ Markus Clemens

Beam-tube end model



standard 2D model

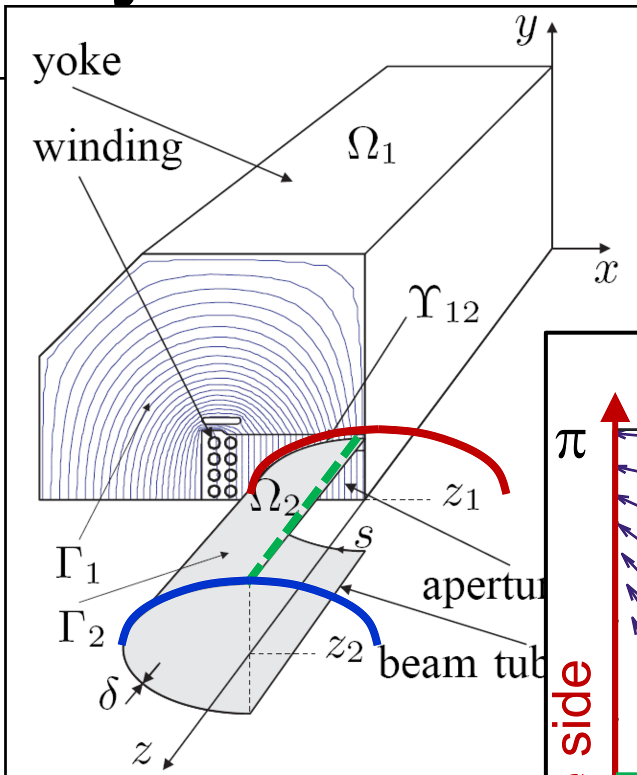
cross-section Γ_1
of volume Ω_1

common interface Υ_{12}

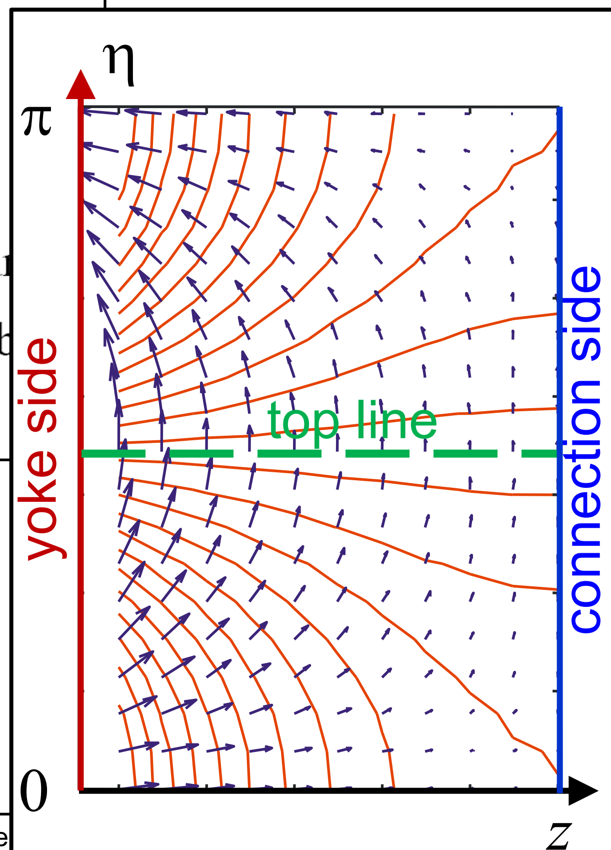
additional 2D model for the beam-tube end

cross-section Γ_2
of volume Ω_2

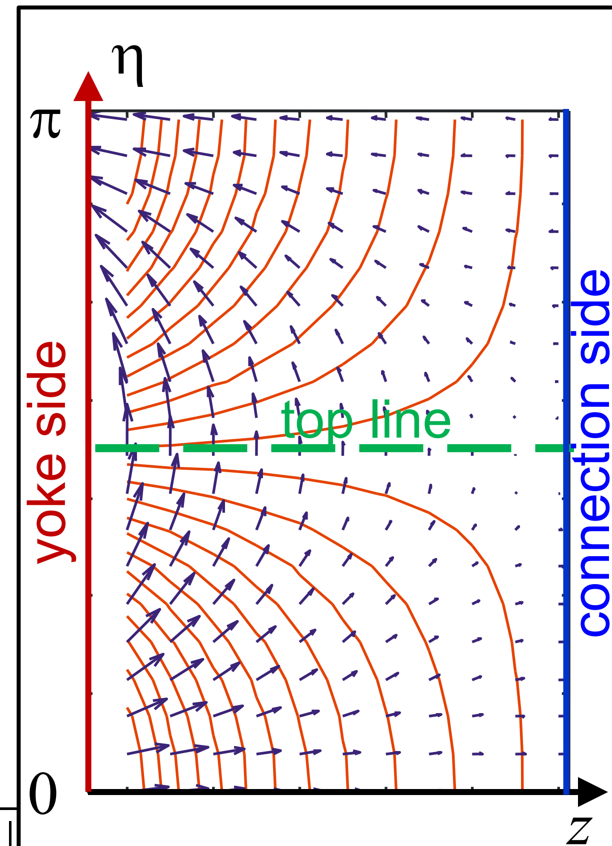
Eddy-current closing paths



connected beam tube



disconnected beam tube

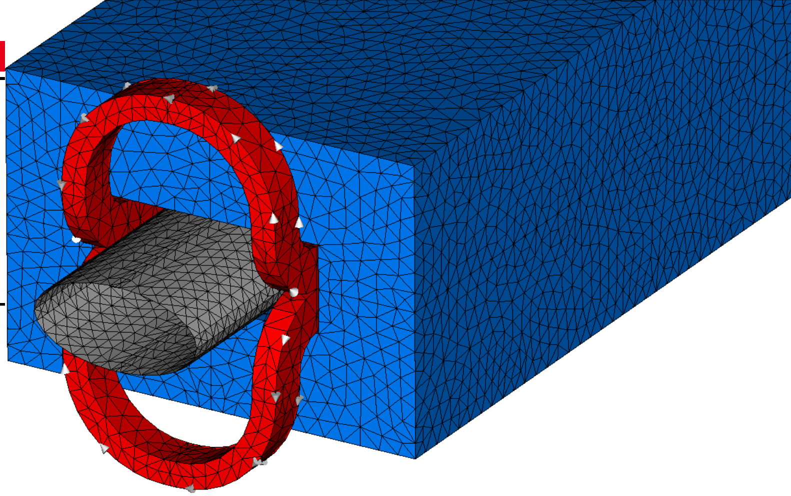


yoke side

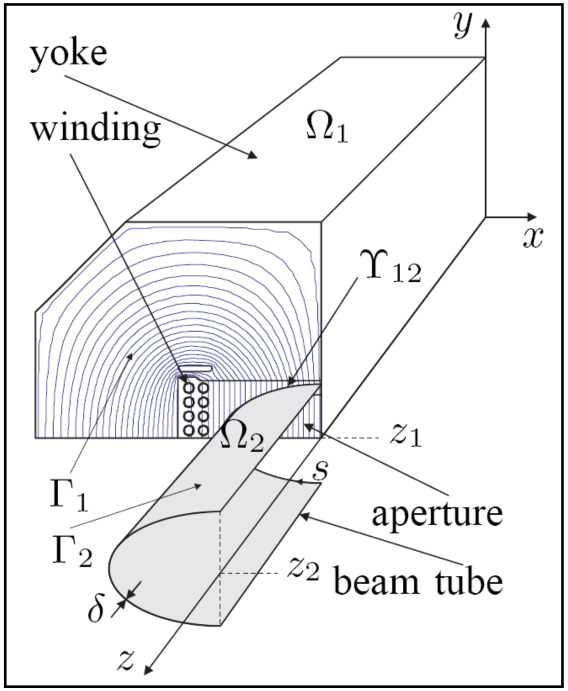
top line

connection side

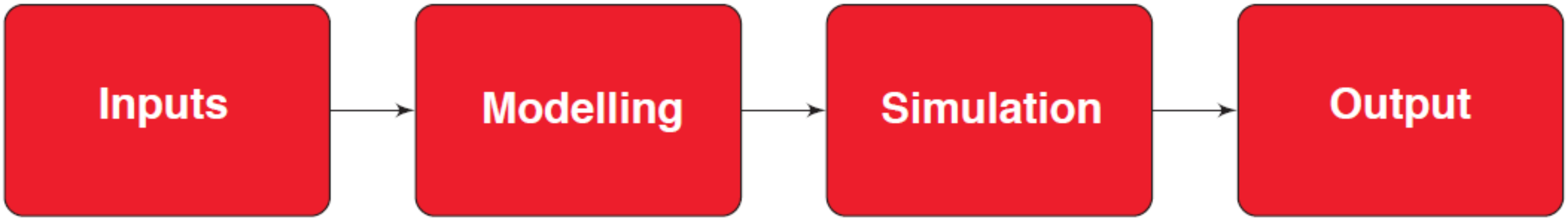
Overview

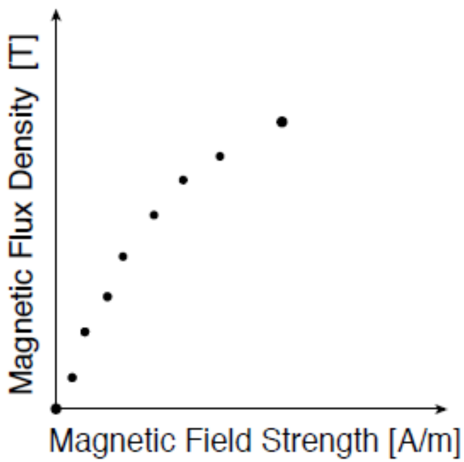


- magnet simulation (standard 3D FE solver)
- challenges
  - geometrical details
  - materials
  - transient effects
  - high accuracy
- magnet simulation (dedicated 3D FE solver)
- hybrid models
- stochastic models
- conclusions

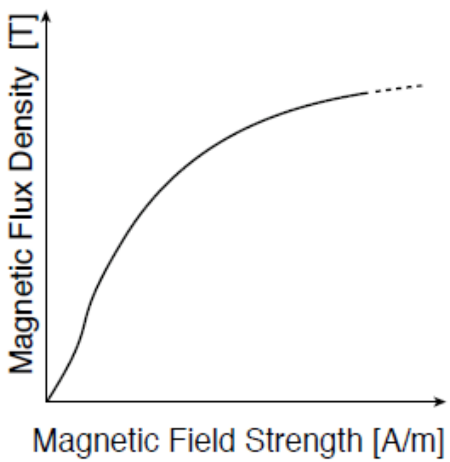


Uncertainty quantification

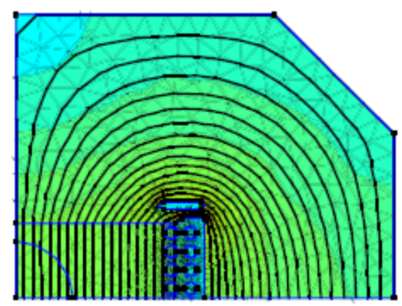




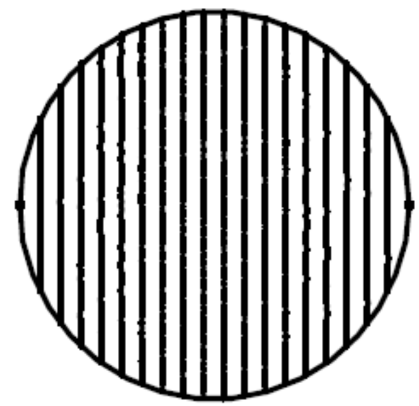
Measurement



Model of saturation



Accelerator Magnet



Multipoles b_i

+ Ulrich Römer, Sebastian Schöps

Overview

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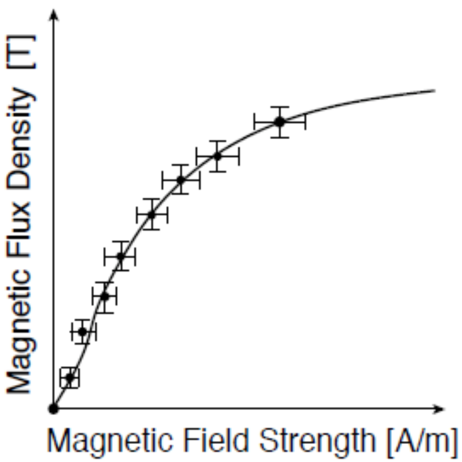
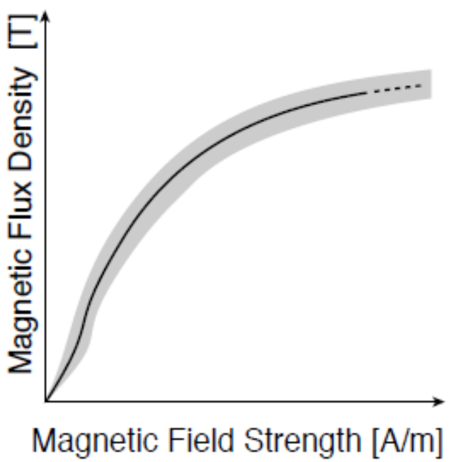
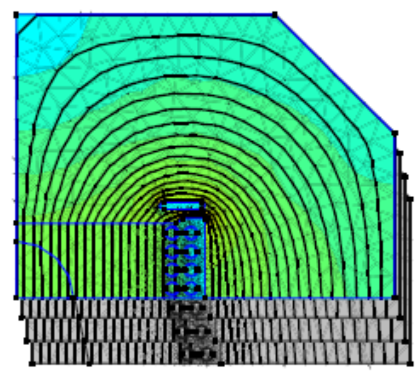
(Uncertain) Inputs → (Stochastic) Modelling → (Multiple) Simulations → (Uncertain) Output



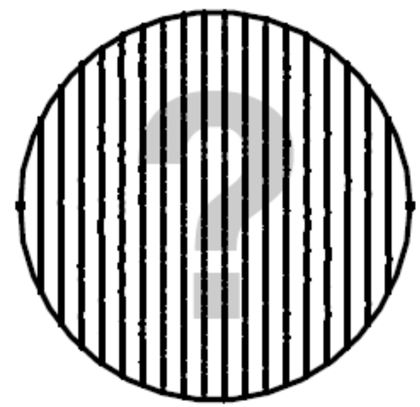
Measurement



Model of saturation



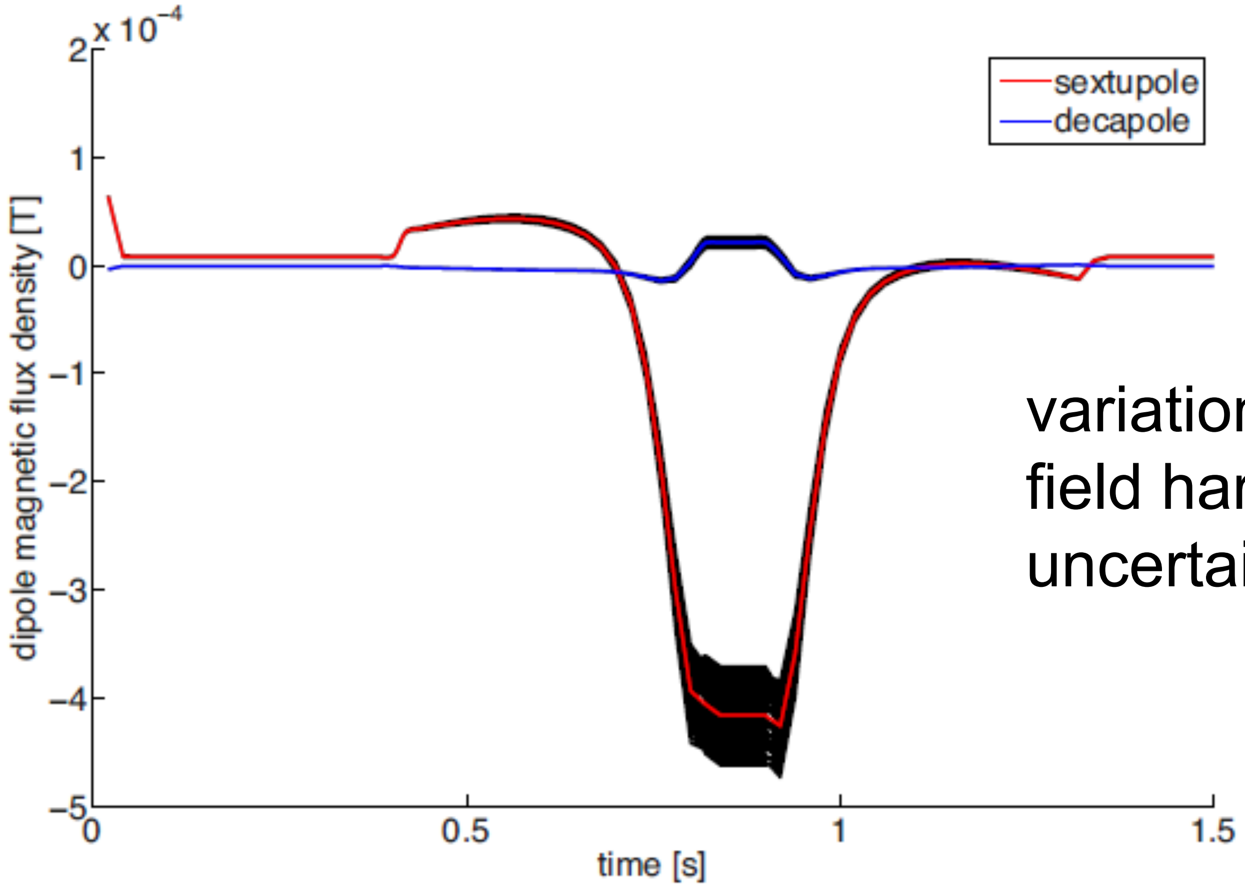
Accelerator Magnet



Multipoles b_i

+ Ulrich Römer, Sebastian Schöps

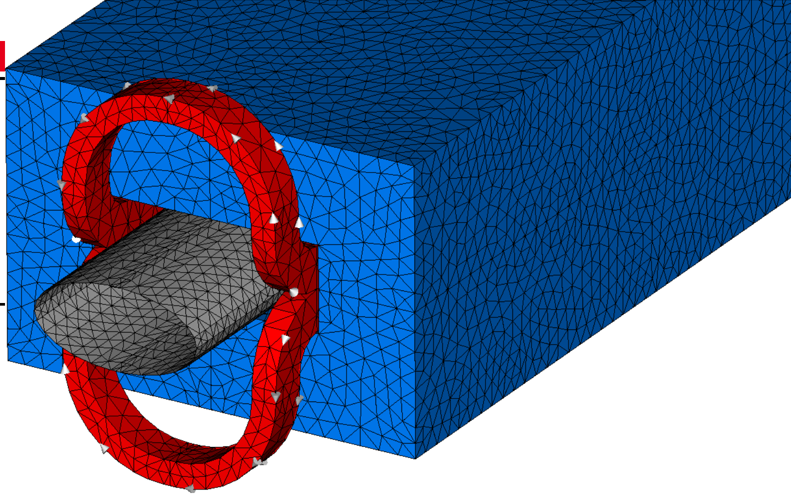
Uncertainty quantification



variation on the field harmonics due to uncertain BH-characteristic

+ Ulrich Römer, Sebastian Schöps

Conclusions



- nonlinear 3D transient magnetic simulation feasible with off-the-shell software
- challenges remain and are problem specific
  - geometrical details
  - materials
  - transient effects
  - high accuracy
- dedicated methods and software