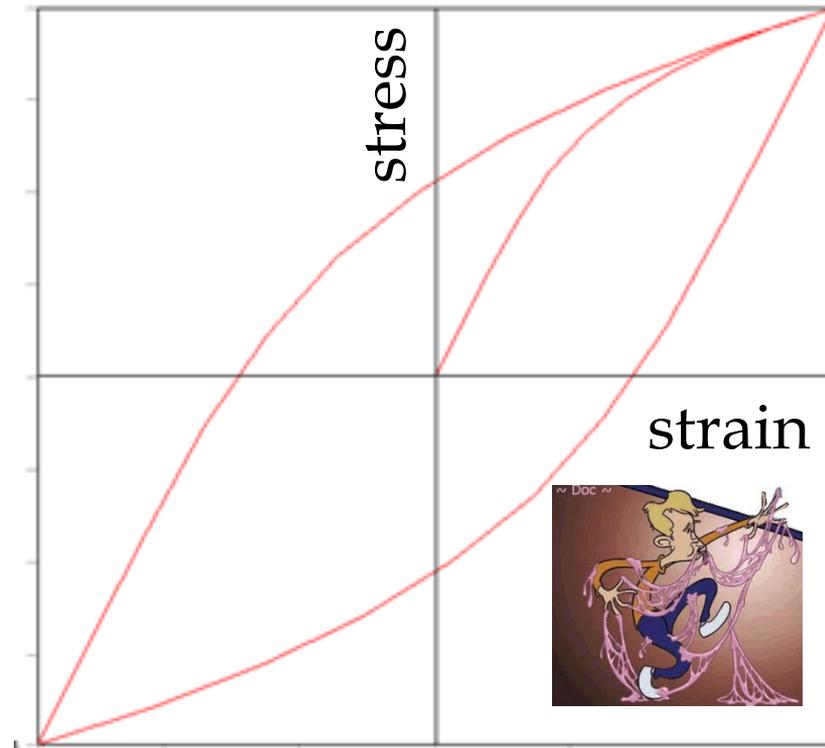


Davide Tommasini

CERN

-  Basic principles
-  Magnet types
-  Elementary design (dipole)
-  Manufacture
-  Resistive magnets in CERN accelerators

Basic principles : mechanics



To squeeze or elongate an object you need a press

An elongation or compression creates a force

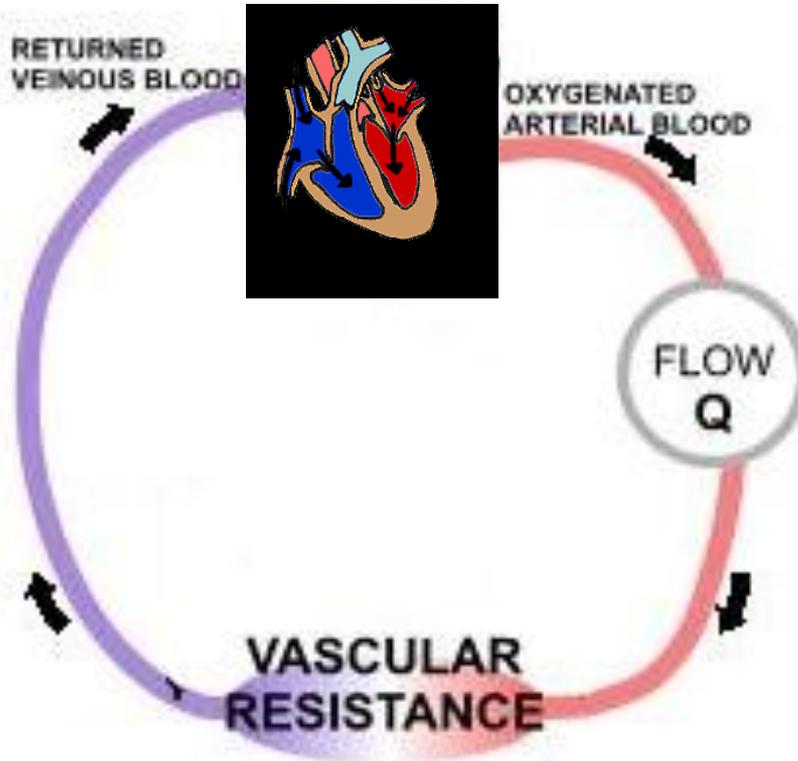
$$\text{FORCE} = \text{pressure} \times \text{section}$$

$$F = P \times A$$

$$\Delta L = (1/\mathcal{K}) \times F$$



Basic principles : hydraulic circuit



$$\Delta P = R \times Q$$

Little **pressure drop** across the main vessels, most is in tissues/organs

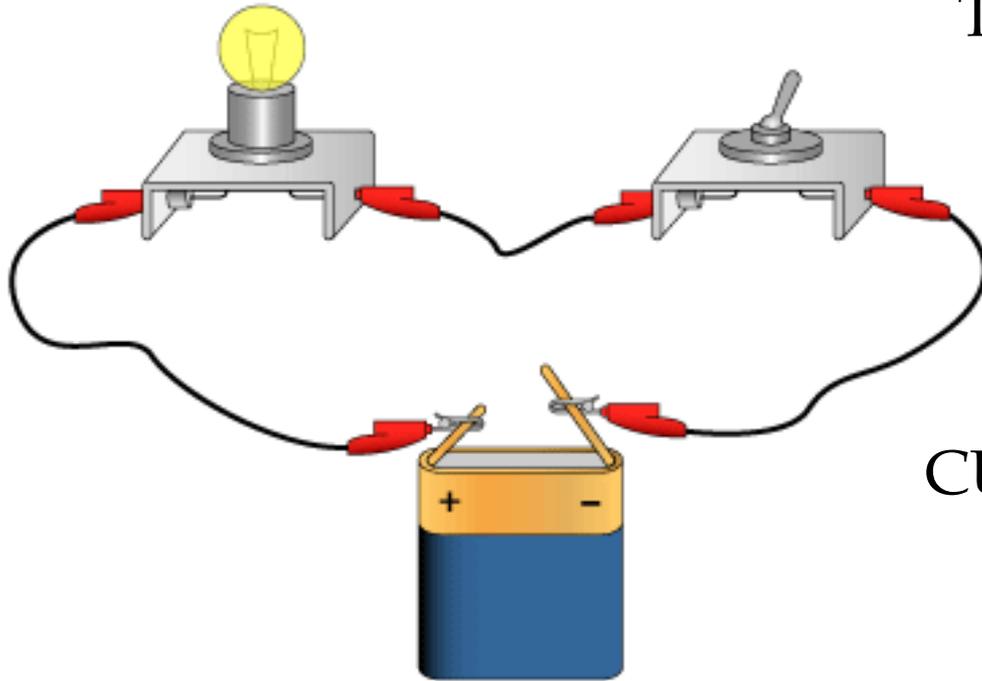
To make a fluid circulating you need a pump

A difference of pressure creates a flow

FLOW = speed x section
 $Q = v \times A$



Basic principles : electric circuit



$$\Delta V = R \times I$$

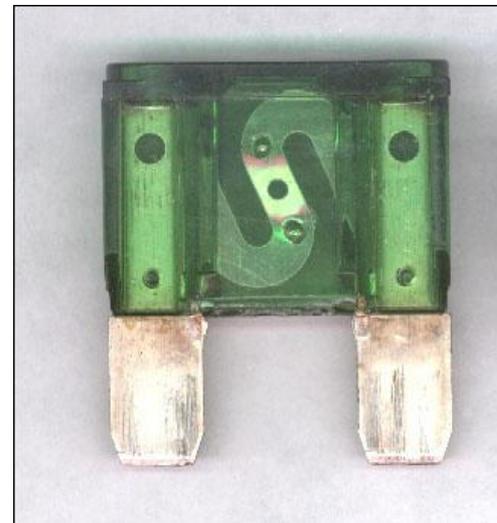
Little **voltage drop** across the wires, most is in the bulb

To produce electrical current you need a generator

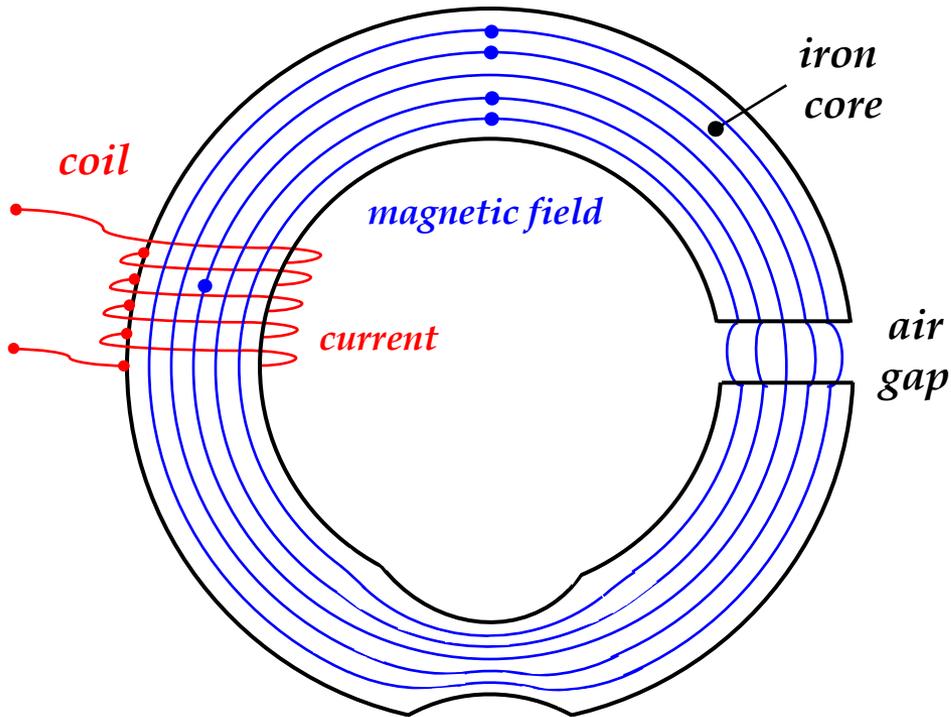
A difference of voltage creates a current flow

$$\text{CURRENT} = C_{\text{density}} \times \text{section}$$

$$I = J \times A$$



Basic principles : magnetic circuit



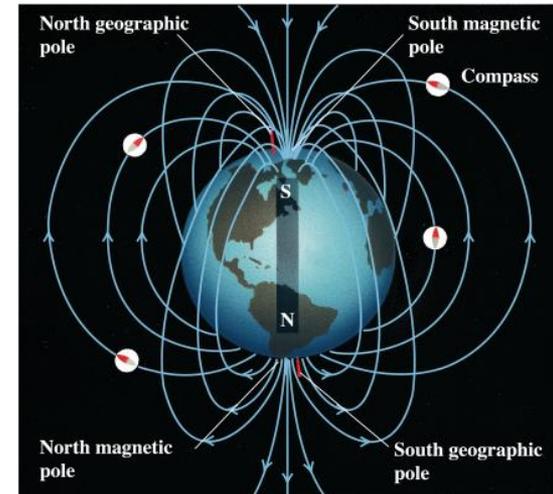
$$NI = \mathcal{R} \times \Phi$$

To produce a magnetic field you need a coil

A magnetomotive force creates a magnetic flux

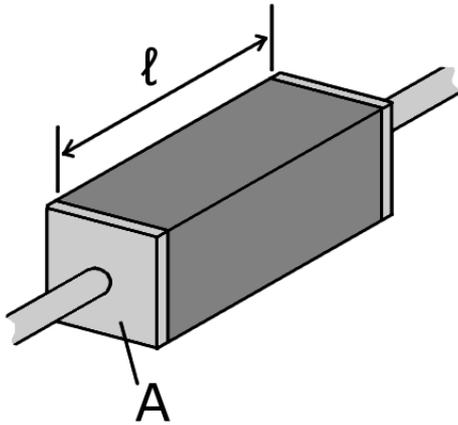
$$\text{FLUX} = \text{field} \times \text{section}$$

$$\Phi = B \times A$$



Little **magnetomotive force** is used in the iron, most is used in the air gap

Basic principles : constitutive equations



$$R = \text{length} / (\text{electrical conductivity} \times \text{section})$$

$$\mathcal{R} = \text{length} / (\text{magnetic permeability} \times \text{section})$$

$$R = \rho \frac{l}{A}$$

Electrical

$$\mathcal{R} = \frac{l}{\mu A}$$

Magnetic

$$B = \mu_0 \mu_r H$$

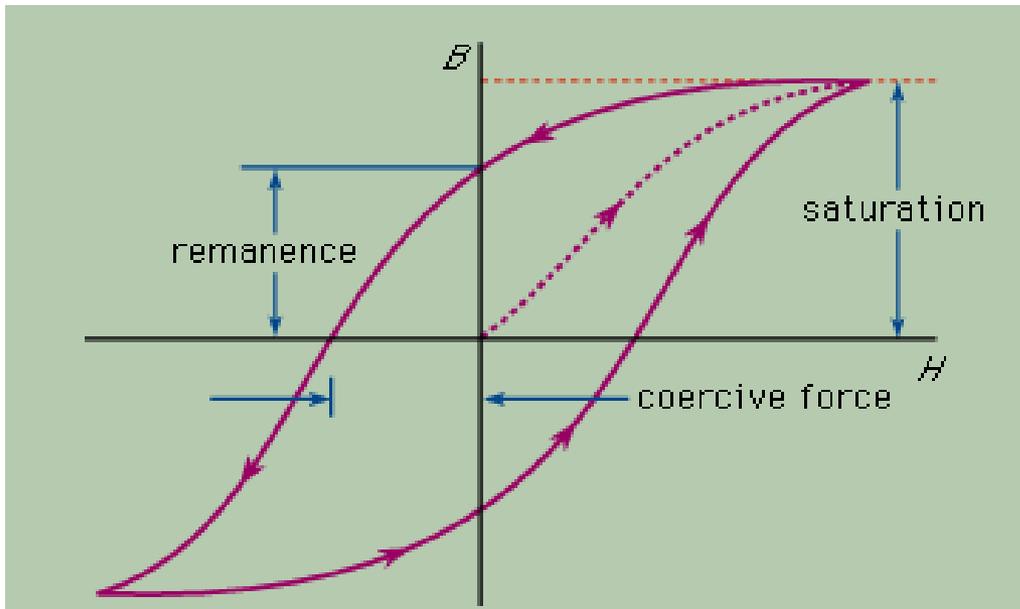
$$\mu_0 = 4\pi \cdot 10^{-7} \text{ Tm/A}$$

magnetomotive force is in reality
"magnetizing work density"

$$NI =$$

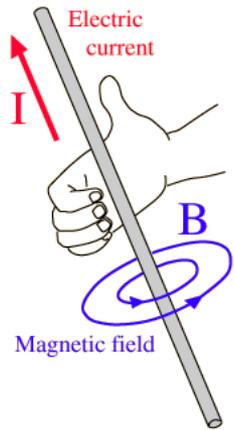
$$\oint \mathbf{H} \cdot d\mathbf{l} \text{ (Ampère's law)}$$

$$\mathcal{R} \times \Phi \text{ (Hopkinson's law)}$$

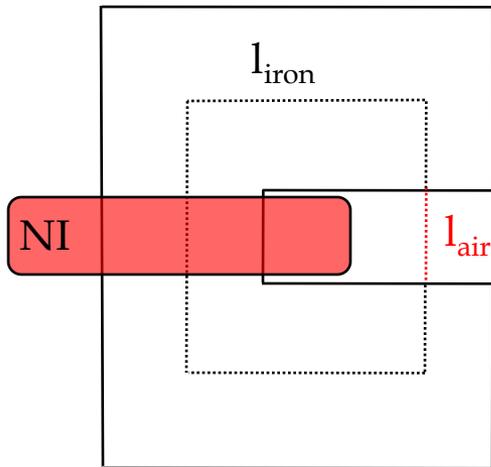


H can be interpreted as "magnetizing pressure"
In ferromagnetic materials small H creates high B

Basic principles : magnetic field generation



$$NI = \oint \vec{H} \cdot d\vec{l} = \frac{B}{\mu_0} 2\pi r$$



$$NI = H_{iron} \cdot l_{iron} + H_{air} \cdot l_{air}$$

~~$$NI = \frac{B}{\mu_0 \cdot \mu_r} \cdot l_{iron} + \frac{B}{\mu_0} \cdot l_{air}$$~~

Basic principles : forces



Work (energy) done by a force is :

$$W = \Delta E = \int \vec{F} \cdot d\vec{s}$$

In case of a uniform magnetic field

$$W_m = \frac{1}{2} B \cdot H \cdot V = \frac{1}{2} B \cdot H \cdot S \cdot x$$

$$F = dW/dx = \frac{1}{2} B \cdot H \cdot S$$

$$\text{in air } H = B / \mu_0$$

Magnetic force is then $\approx B^2 \cdot 4 \text{ kg}_f / \text{cm}^2$

A key (2 cm^2) in

$$B = 1\text{T} \Rightarrow F = 8 \text{ kg}_f$$

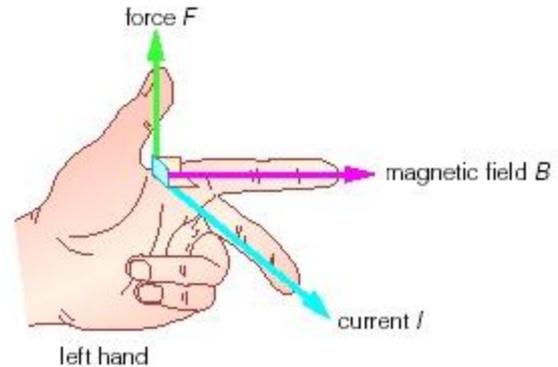
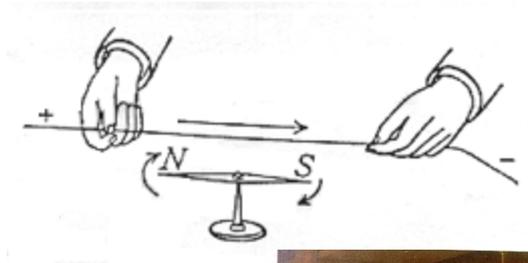
$$B = 2\text{T} \Rightarrow F = 32 \text{ kg}_f$$



Basic principles : forces

On a conductor immersed in magnetic field

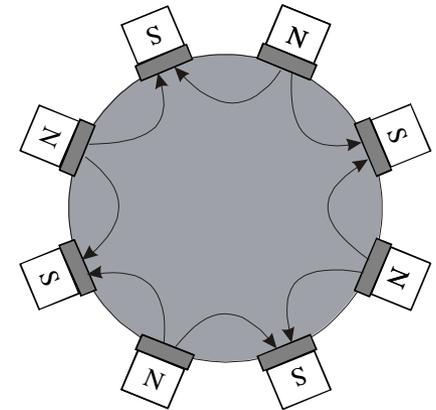
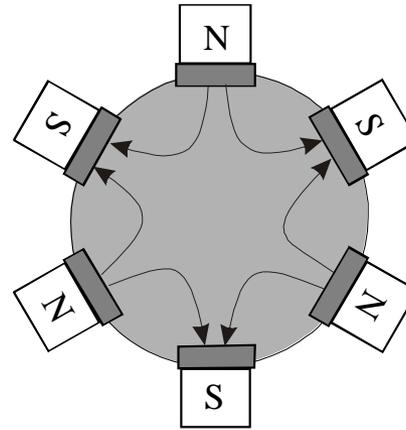
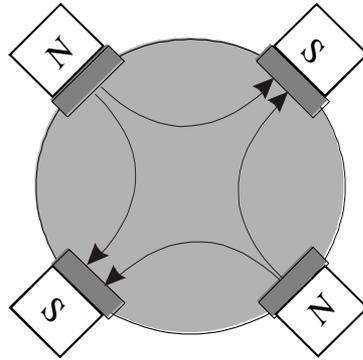
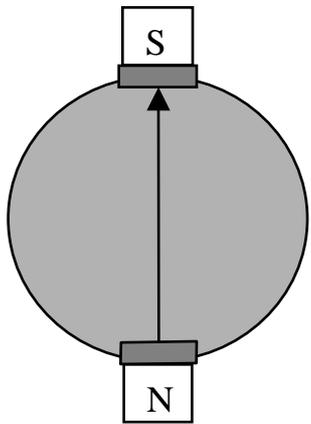
$$\mathbf{F} = \mathbf{I} \cdot \mathbf{L} \times \mathbf{B}$$



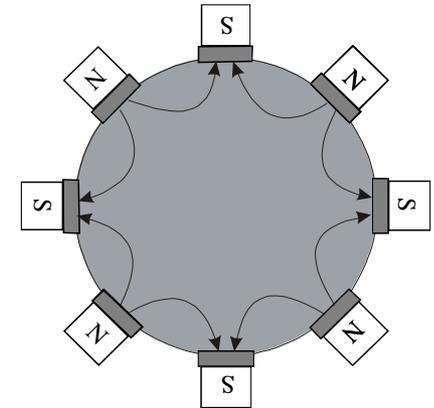
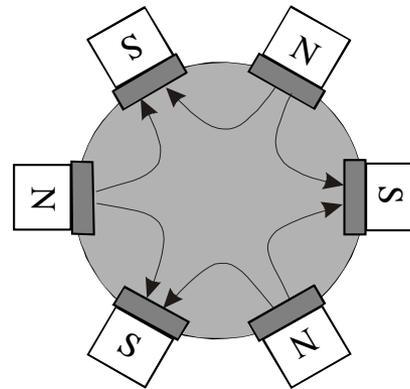
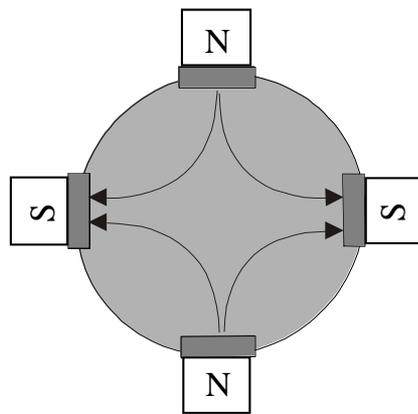
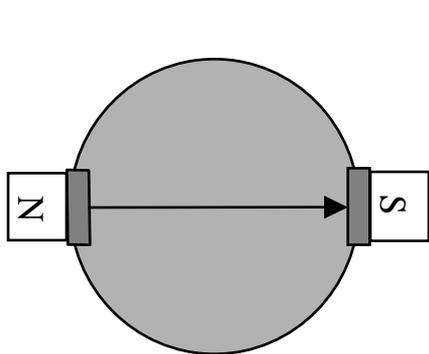
For example if a coil of 3 m length with $NI = 50\,000$ A is immersed in a perpendicular field of $B = 0.5$ T

$$F = 50000 \cdot 3 \cdot 0.5 = 75000 \text{ N} = 7.5 \text{ tons}_f$$

Magnet types : field harmonics



NORMAL : vertical field on mid-plane



SKREW : horizontal field on mid-plane

Magnet types : operation

Operation can be in steady state (DC), cycled, pulsed

A varying magnetic field produces a voltage difference (Faraday law)

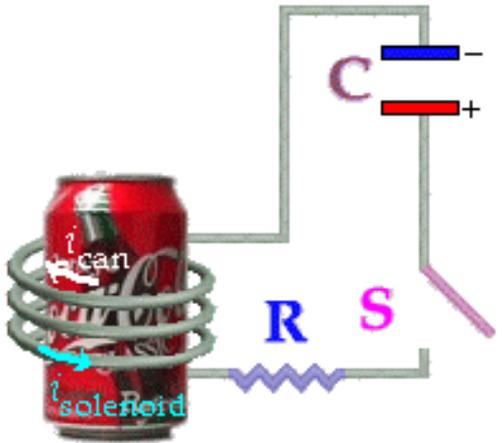
This effect acts against the variation (Lenz law)

$$V = - \partial\Phi / \partial t$$

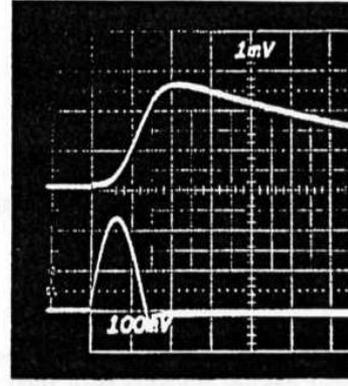
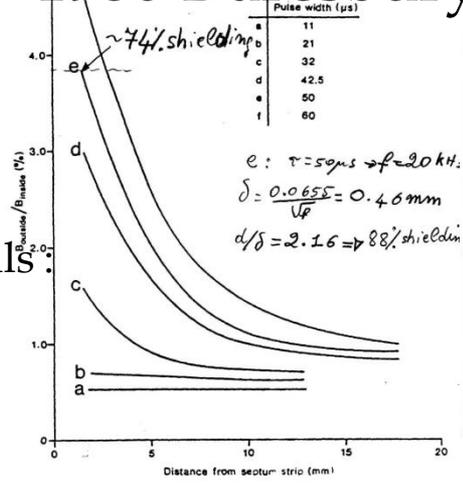
Currents are generated in electrical conducting materials:

- opposing to the penetration of the magnetic field
- producing losses

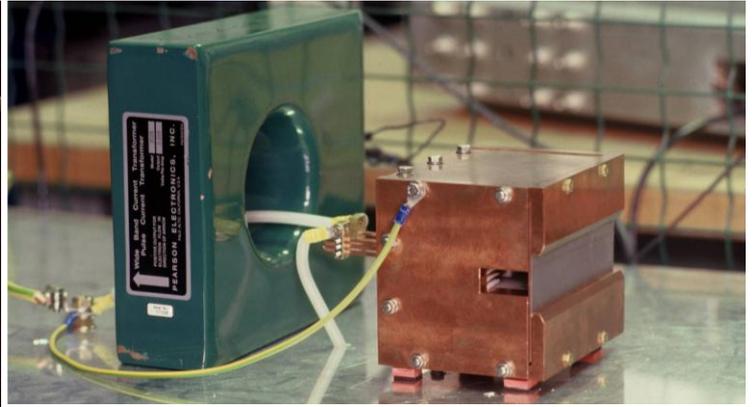
$$\delta = (\pi\mu\sigma f)^{-1/2}$$



1980 Daresbury 1990 ESRF

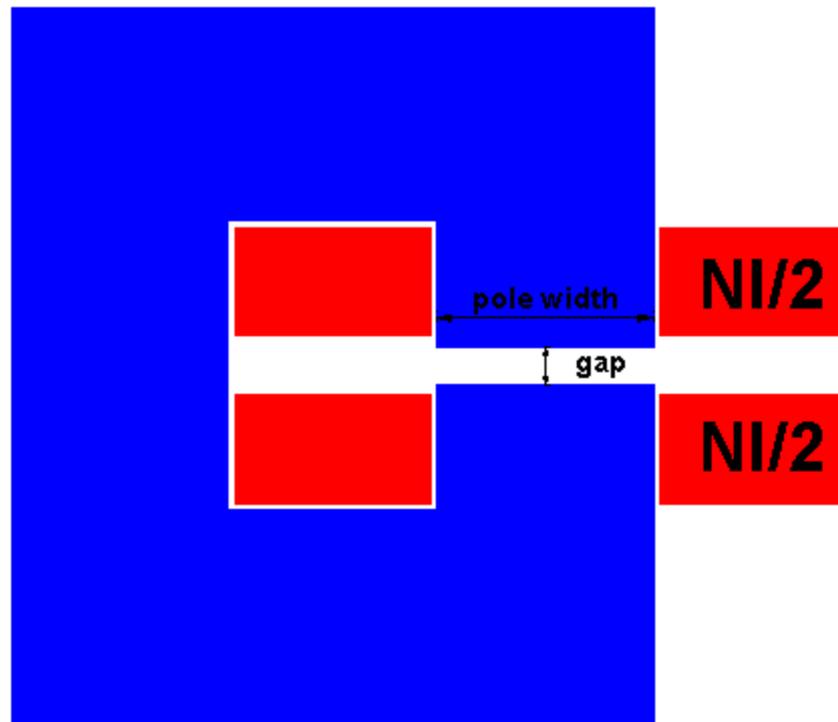


1990 ELETTRA



When magnetic field varies use laminations, possibly with silicon (1-4%) to increase resistivity

Elementary design : a C-dipole

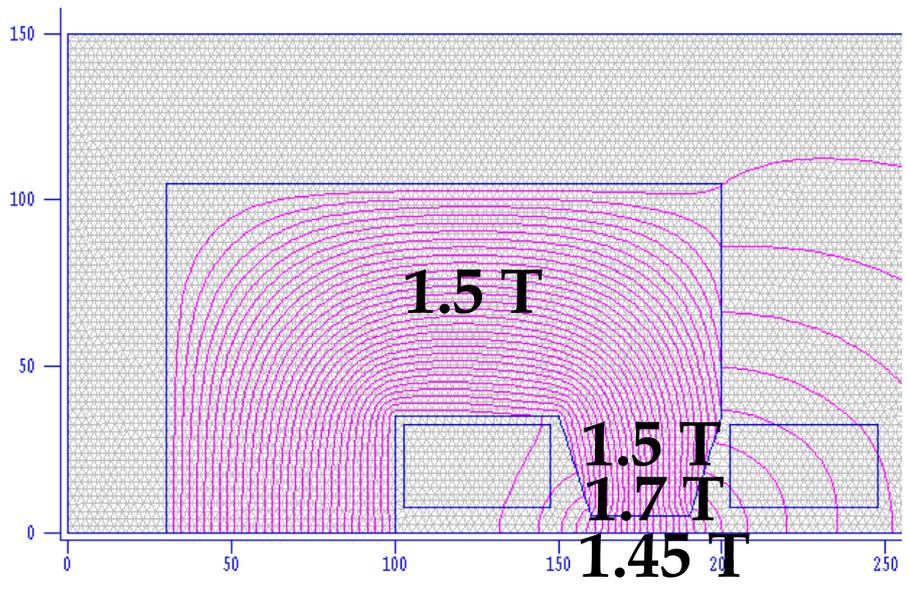
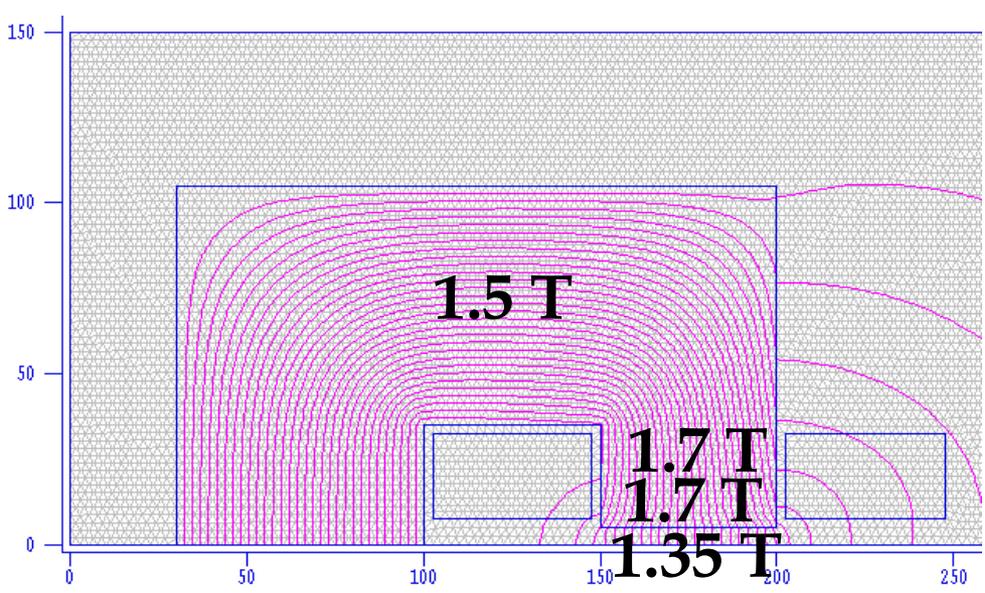
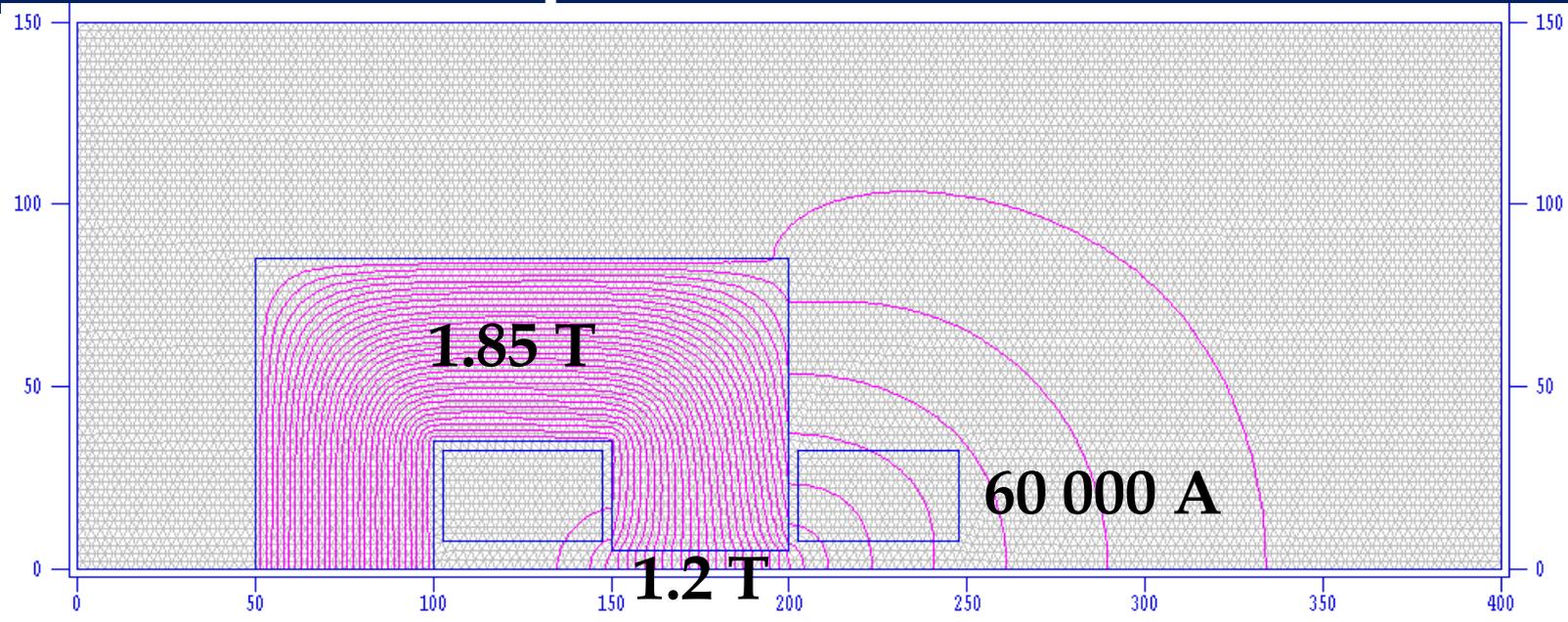


tentative pole width \sim good field region + $2.5 \cdot \text{gap}$

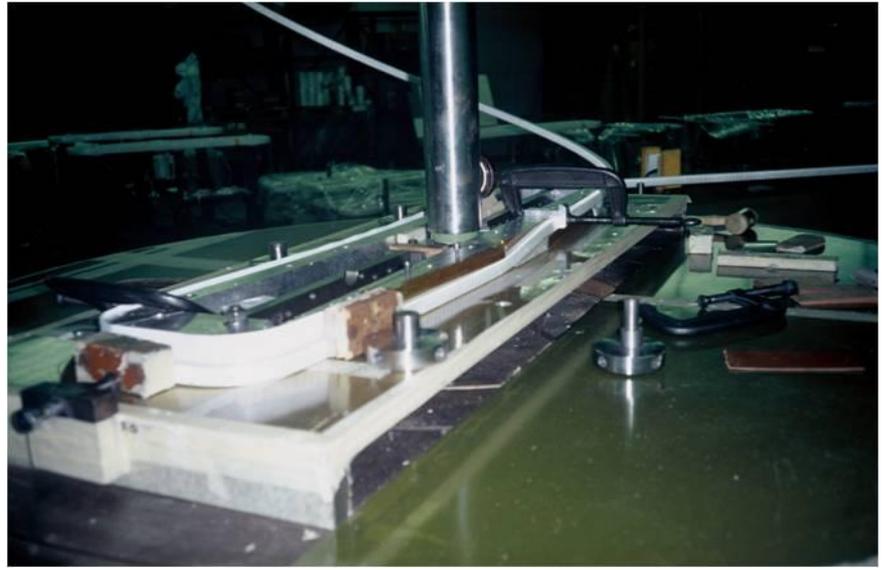
Considering the reluctance of iron negligible with respect to that of air, $NI = \mathcal{R} \times \Phi = [\text{gap}/(\mu_0 \times A)] \times (B \times A) = \text{gap} \cdot B / \mu_0$

$$B = 1.5 \text{ T}, \text{ gap} = 0.1 \text{ m} \Rightarrow NI = 120\,000 \text{ A}$$

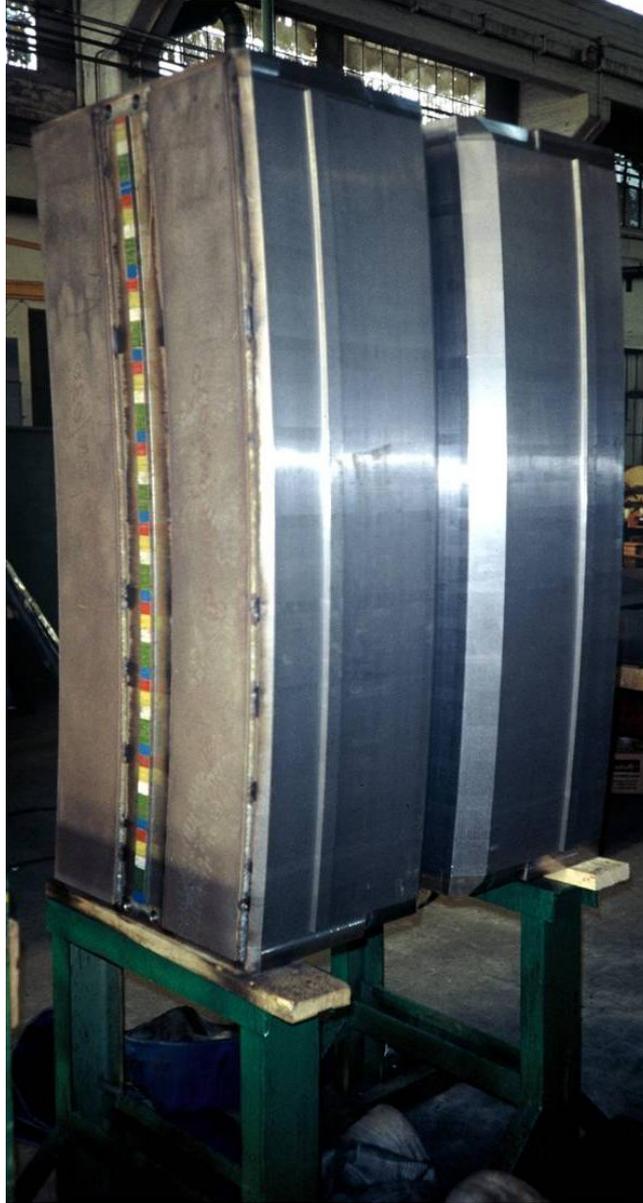
The C-dipole: saturation of iron



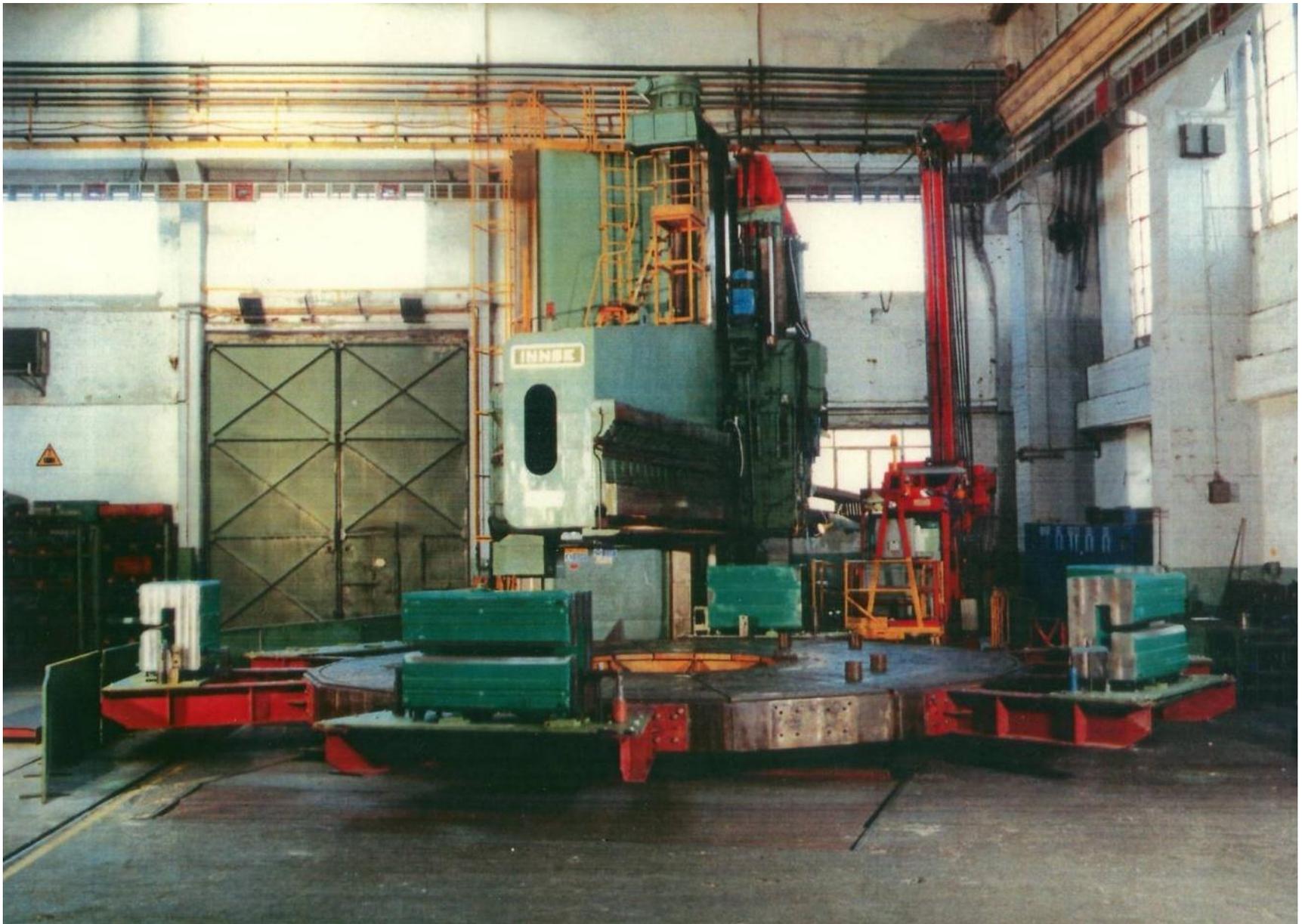
Manufacture : coils



Manufacture : yoke



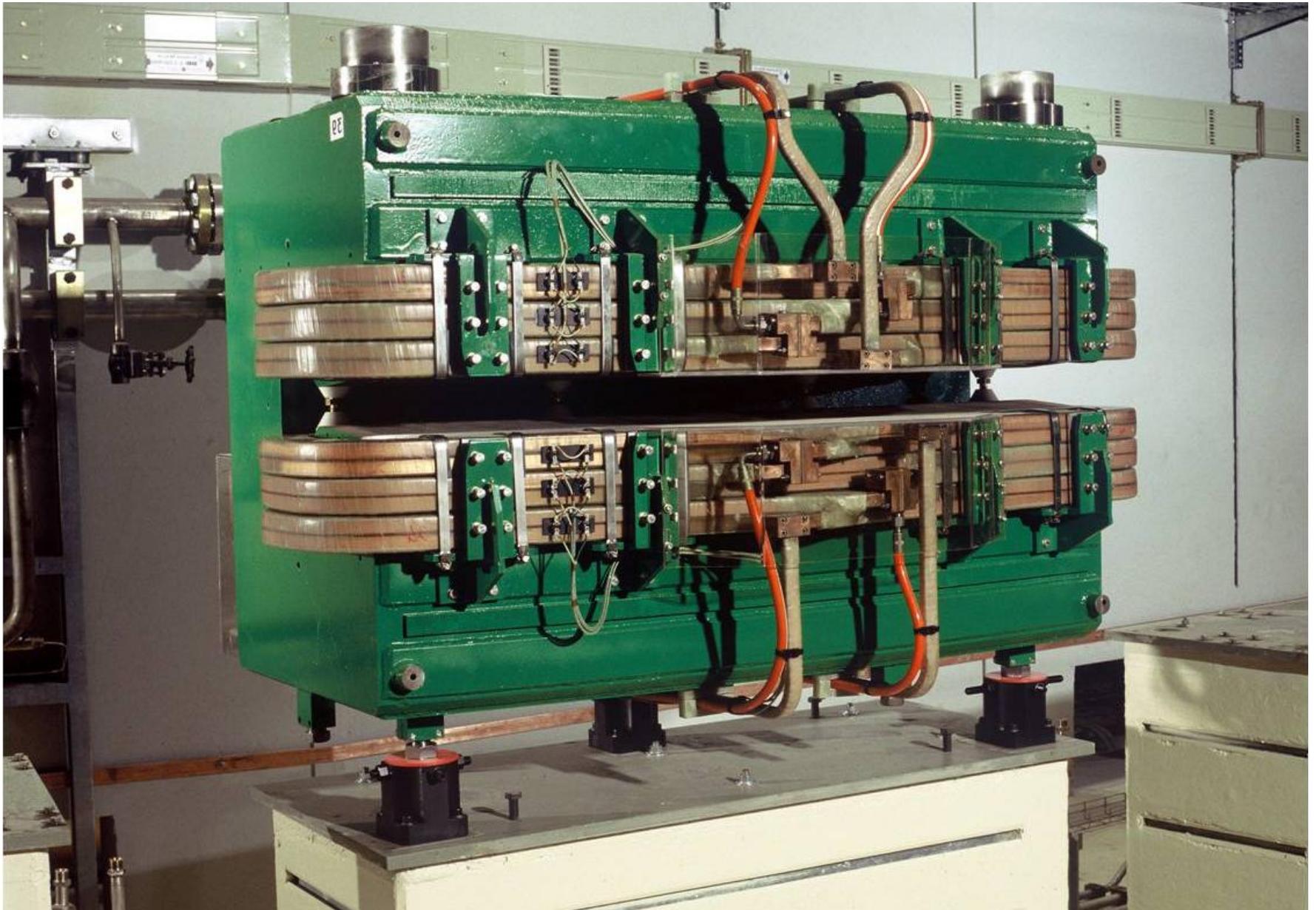
Manufacture : yoke



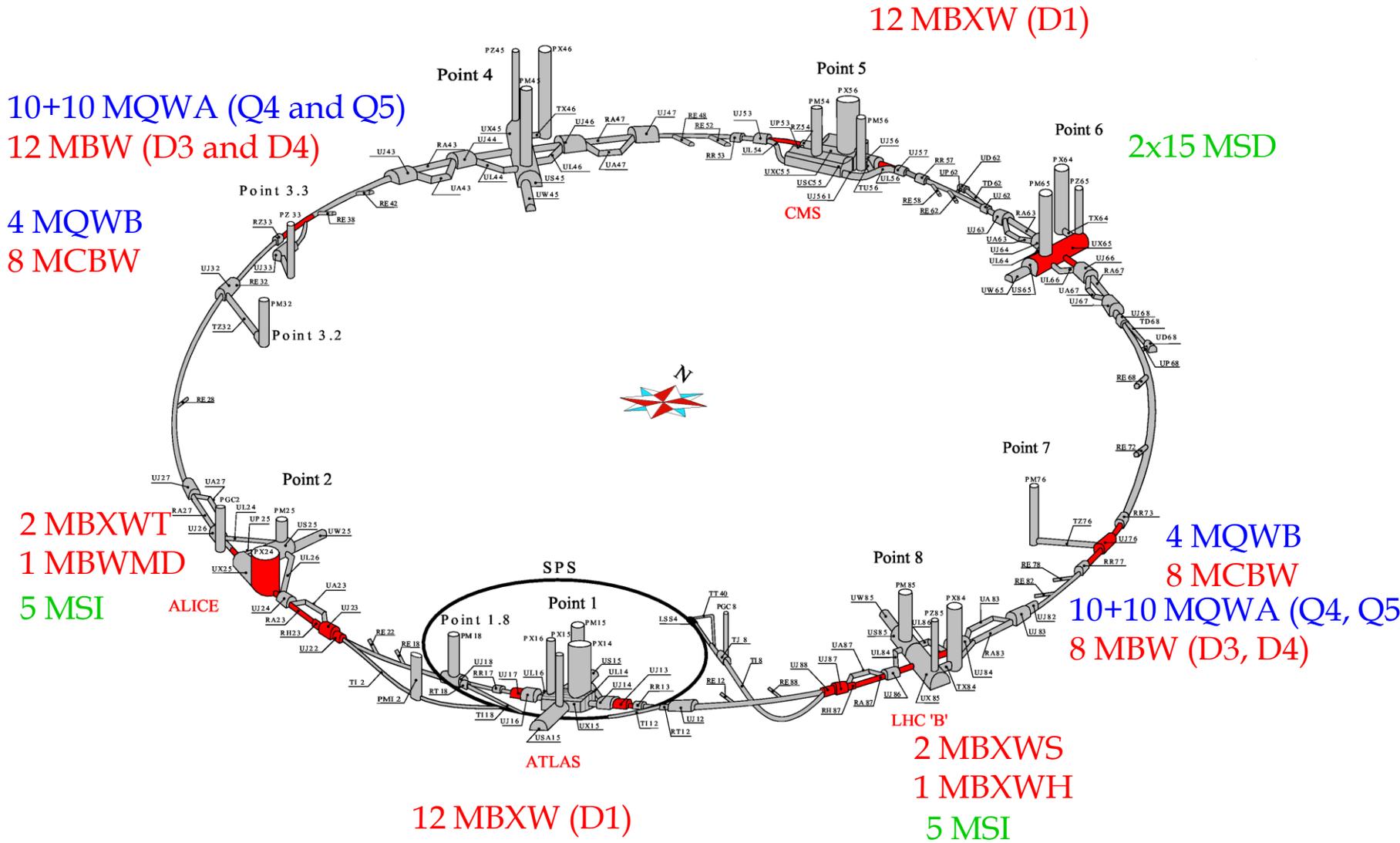
Manufacture : yoke



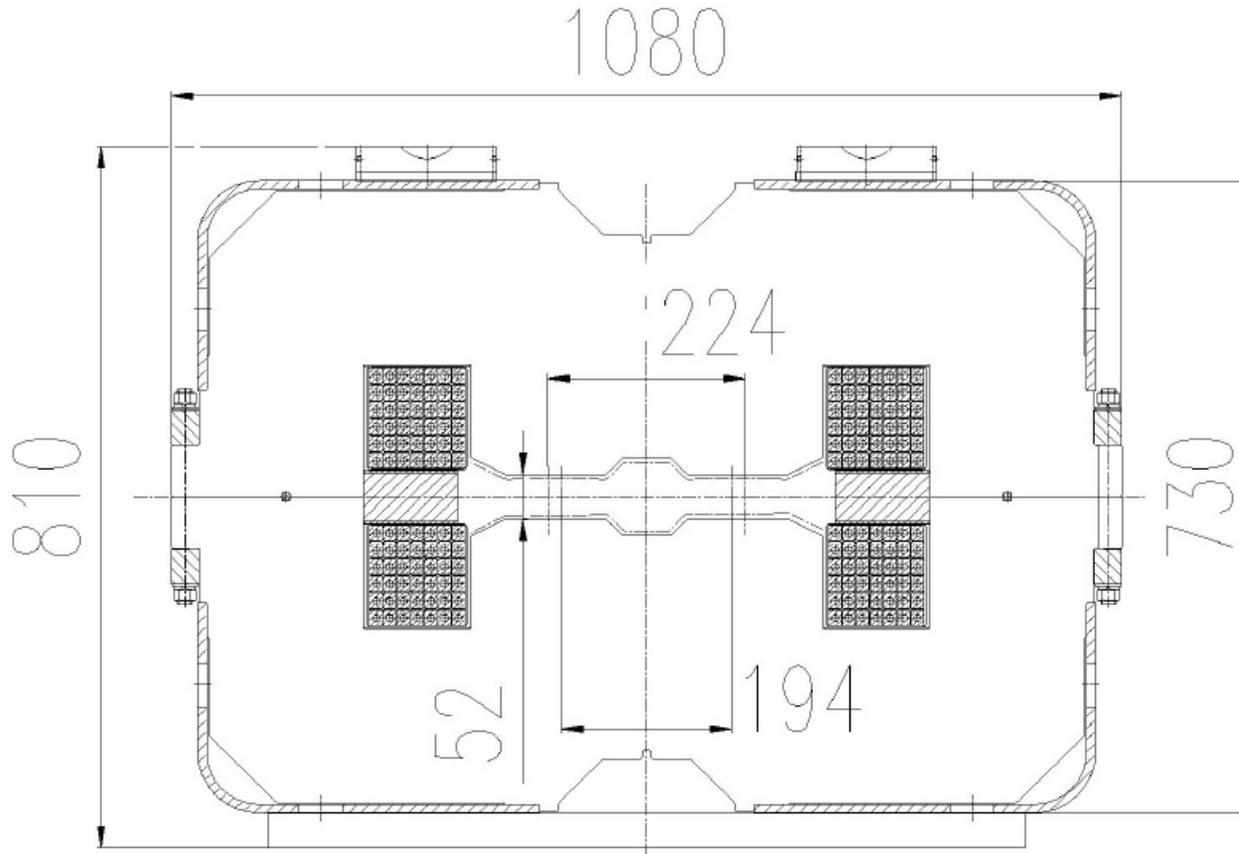
Manufacture : yoke



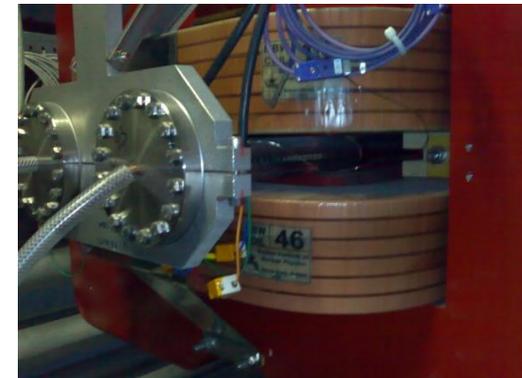
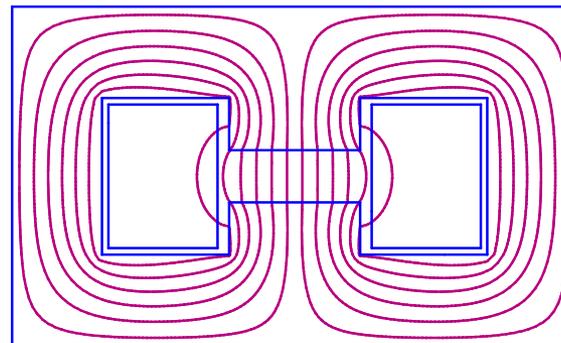
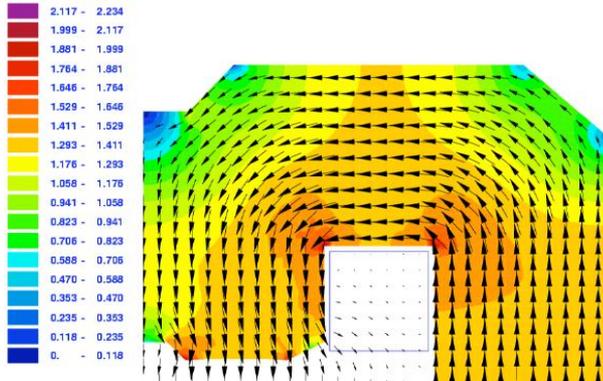
Normal Conducting LHC Magnets



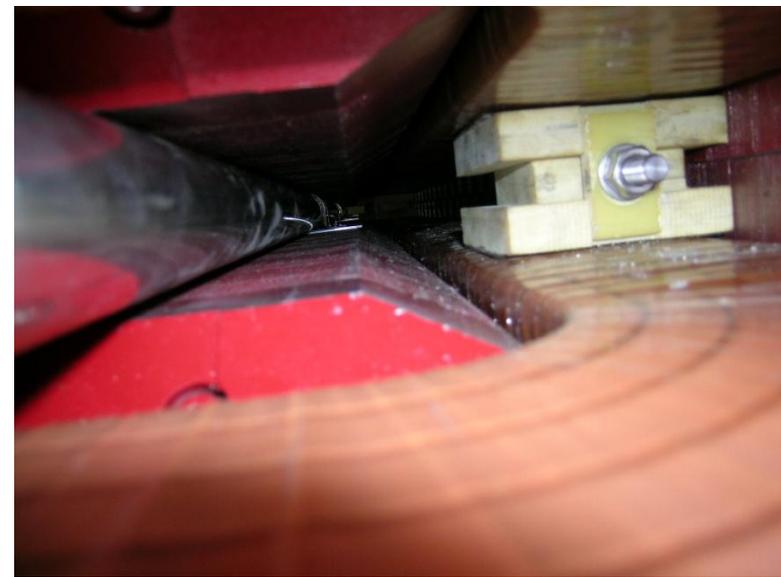
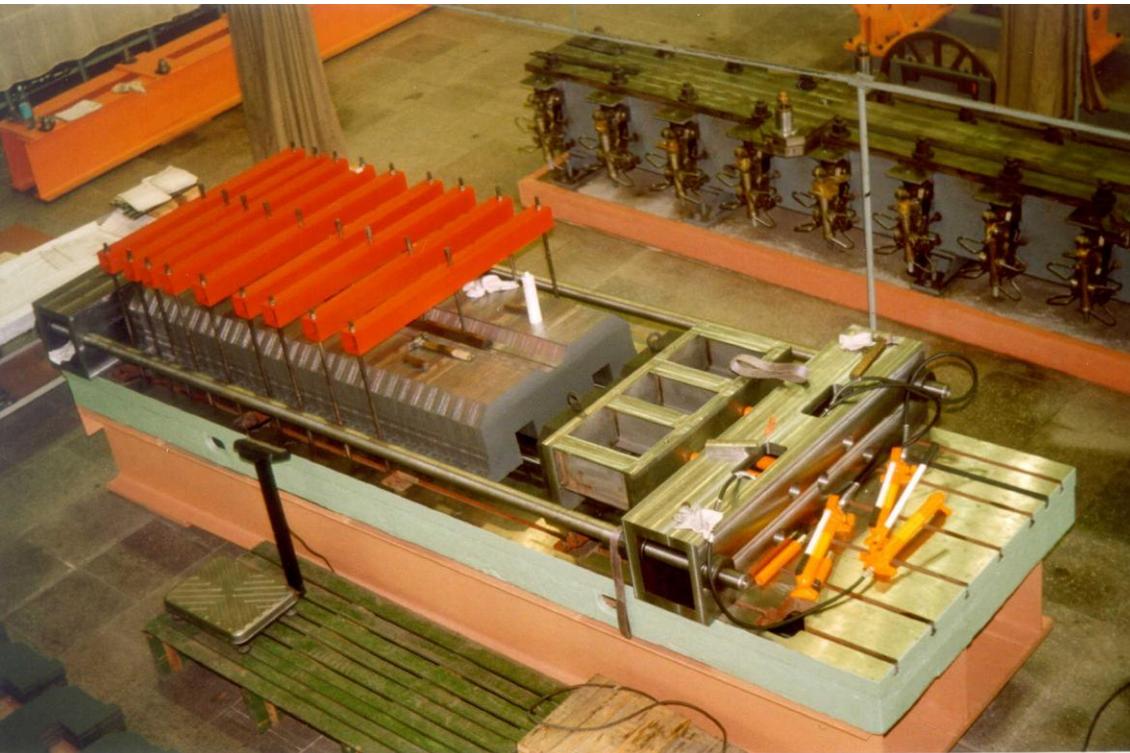
MBW in the LHC : H-type dipole / 1



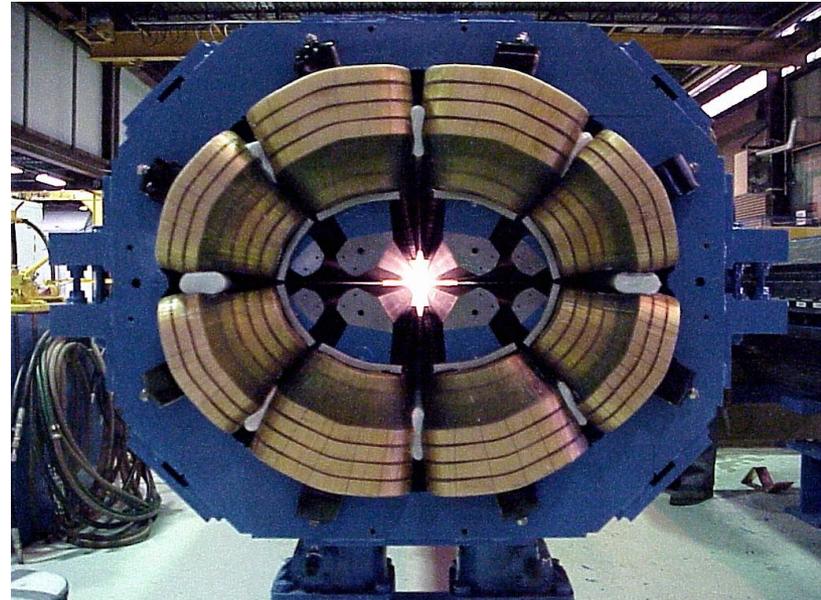
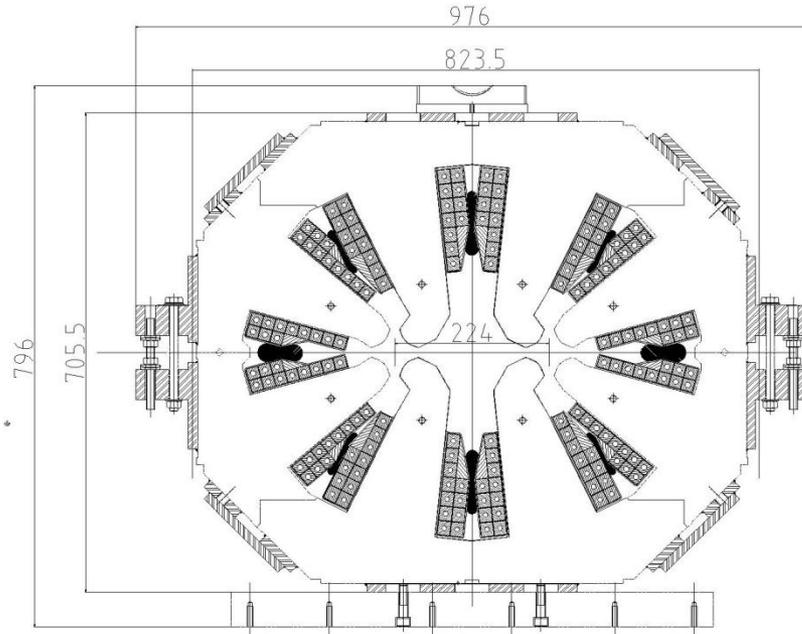
Parameter	Value
Aperture	52 mm
Nominal field	1.42 T
Magnetic length	3.4 m
Weight	18 t
Water flow	19 l/min
Power	29 kW



MBW in the LHC : H-type dipole / 2



MQW Magnets



LINAC-2 Quadrupoles

Type III



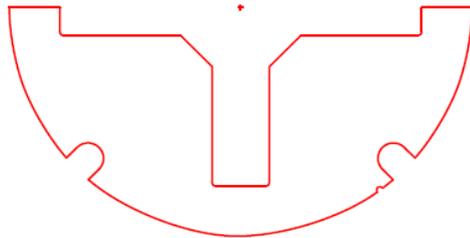
Type III - Assembly



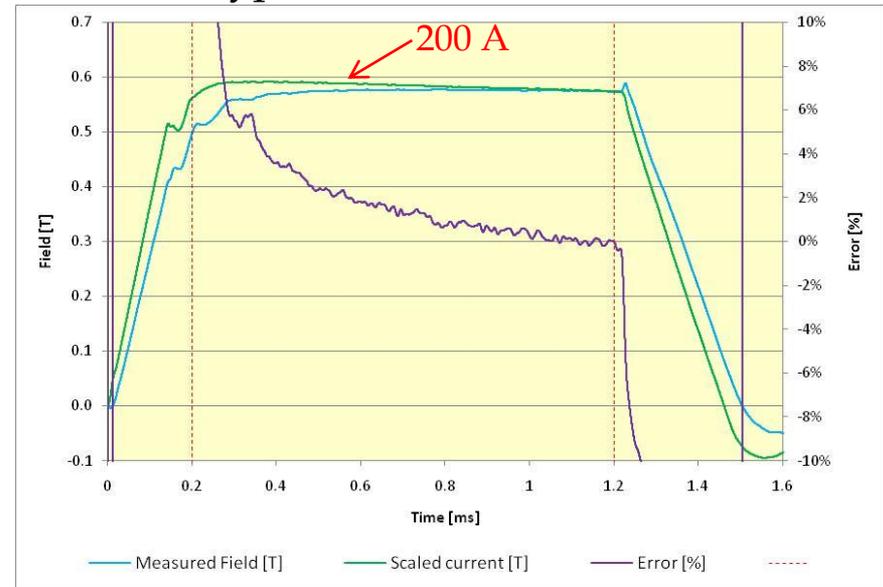
Type VII



Quadrupole Lamination



Type III - Field Measurement



Types - I to X

Core O.D. - 113 to 245 mm

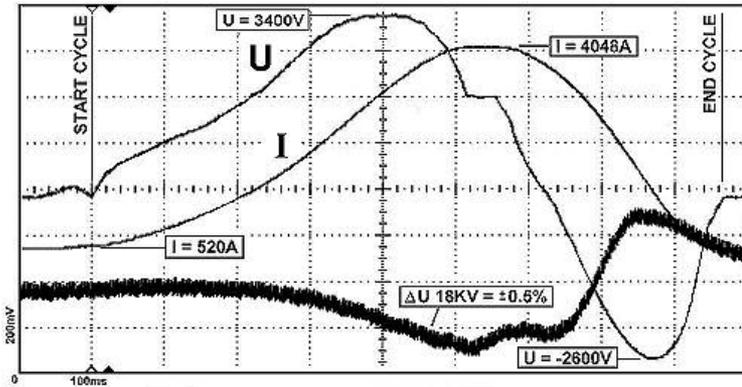
Core Length - 25 to 203 mm

Aperture Diameter - 22 to 103 mm

Yoke half - stacked and glued 0.65 mm laminations assembled with shrunk fit outer ring then potted.

PS Booster Dipoles

1.4 GeV Magnet Cycle



Spare Booster Dipole



Installed Booster Dipole



32 Dipole magnets for Booster Ring
 Magnet Weight - 12000 Kg
 Core Length - 1537 mm
 Aperture - 103 mm
 Magnetic flux @ 1.4 GeV operation 1.064 T

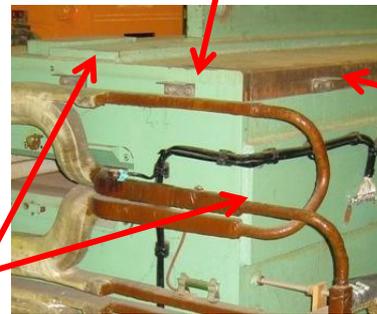
Yoke construction:
 Laminated core stacked between
 'thick' end plates assembled using
 external welded tie bars. Lamination
 insulation achieved through a
 phosphatizing process.

'Thick' End Plate

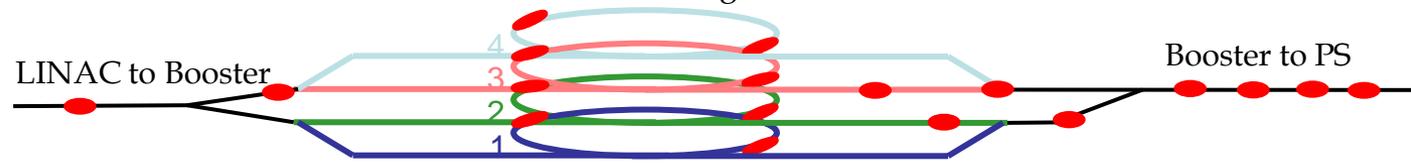
BDL correction Windings
 compensate the 1% difference between
 the inner and outer rings.

Laminations

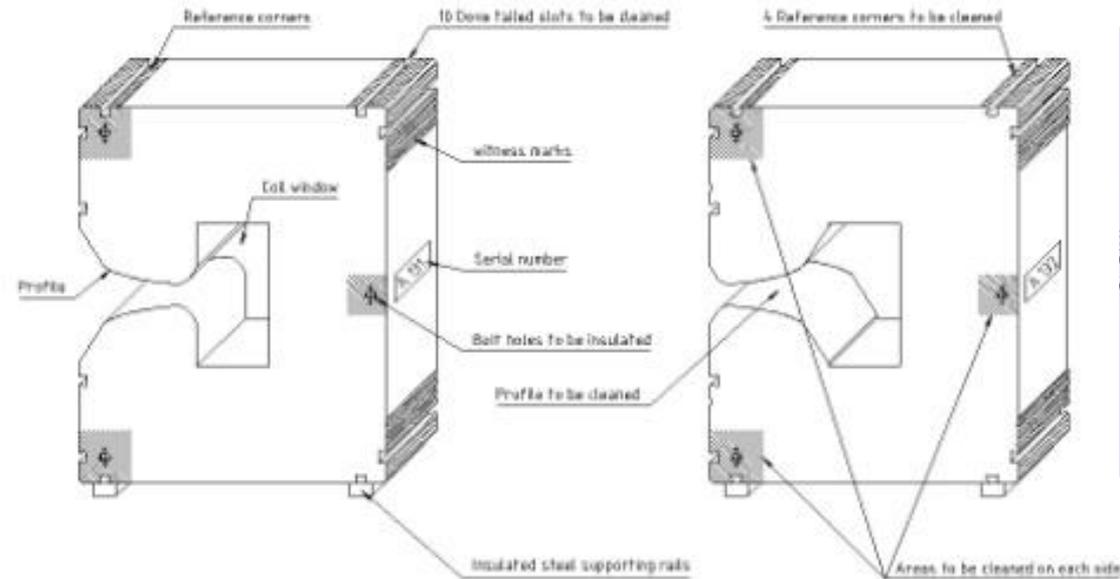
Welded tie Bars



Booster Ring

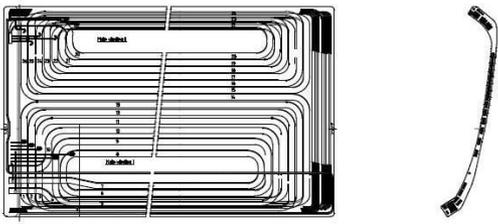


Main units PS, combined function

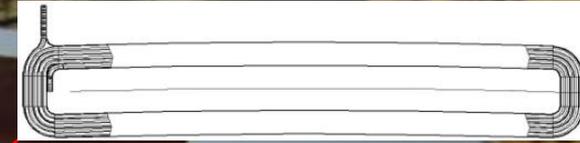


Typical "TSTLHC" cycle for LHC
1.256T, 900 ms, 25.08 GeV

Combined function dipole / quadrupole, PS machine



Pole Face Windings



Main coils (4) for dipole / quad. Field, Al, 20 turns total, 6000A max, 1.2T

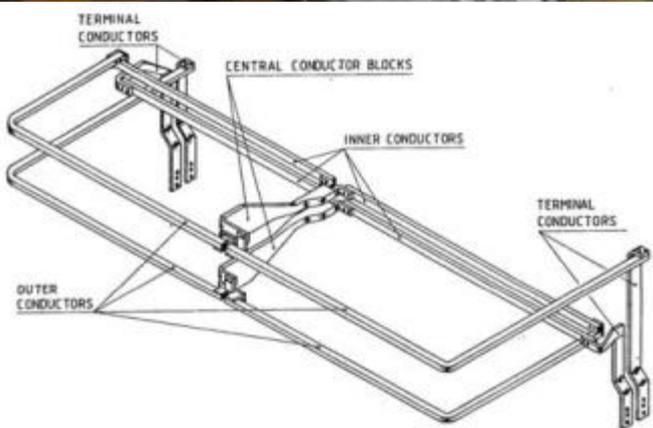
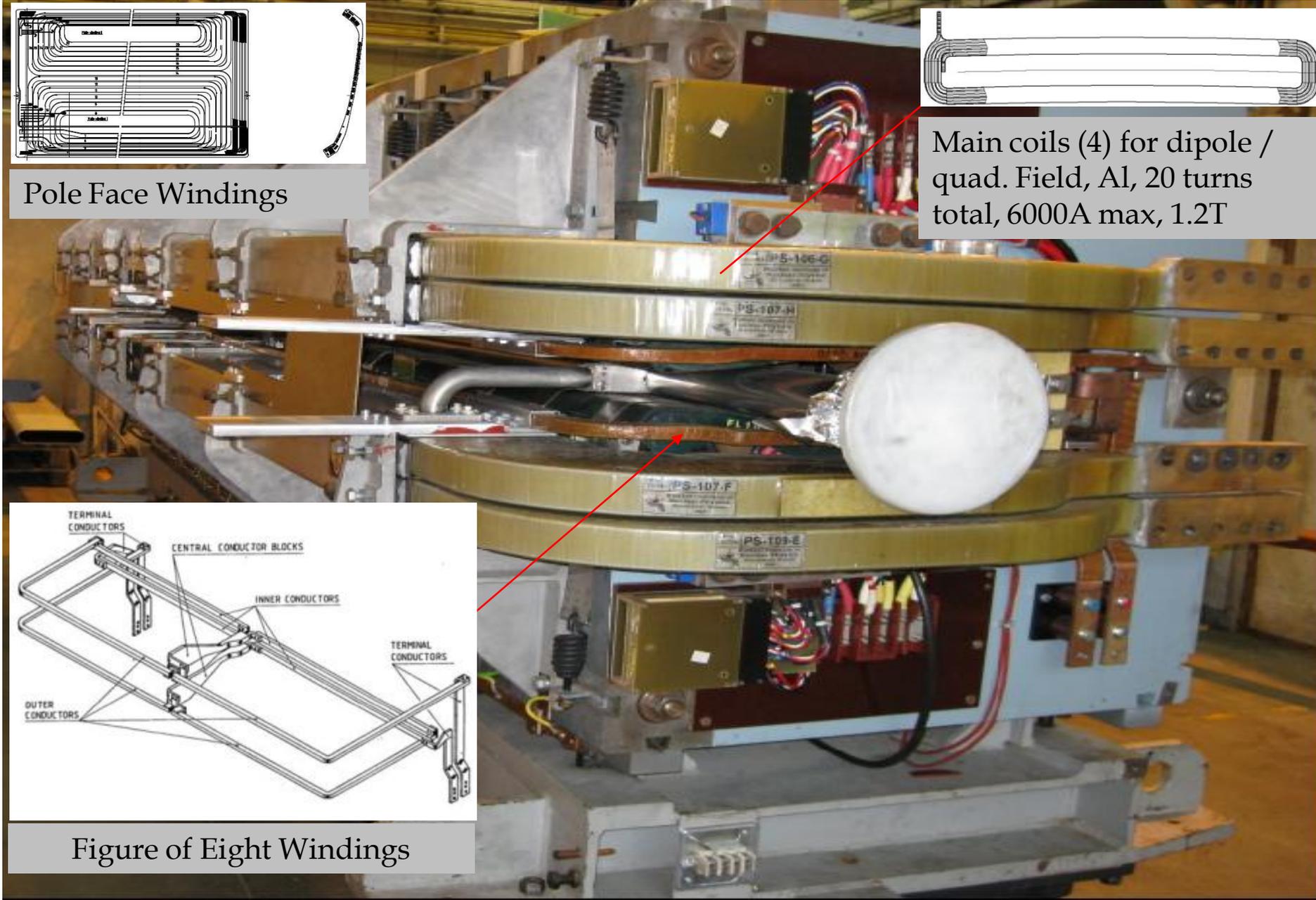
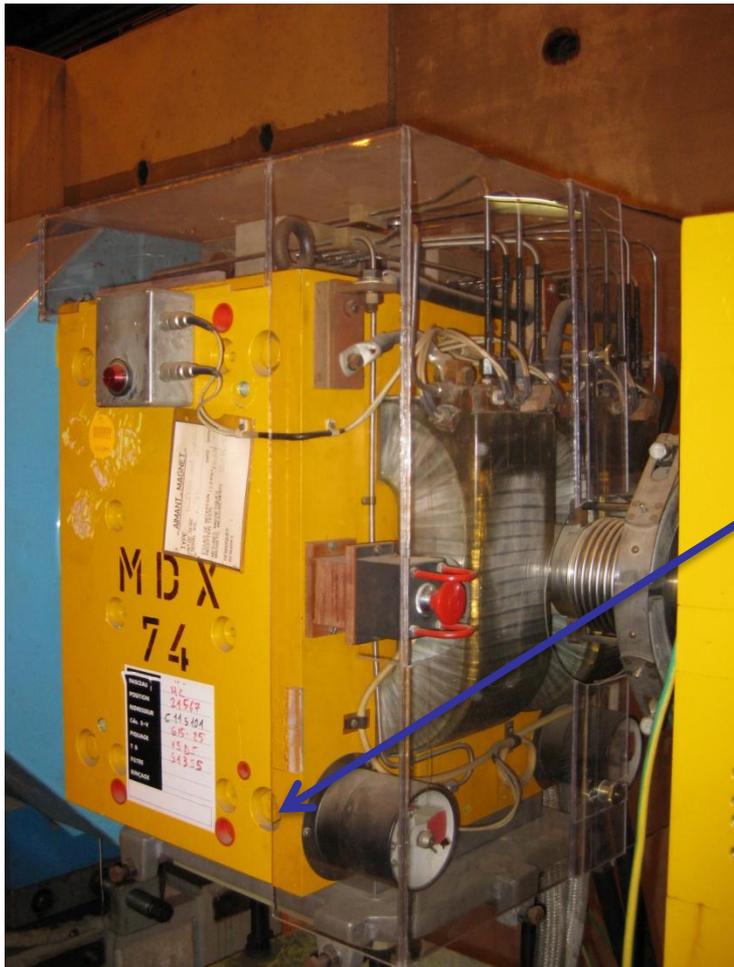


Figure of Eight Windings

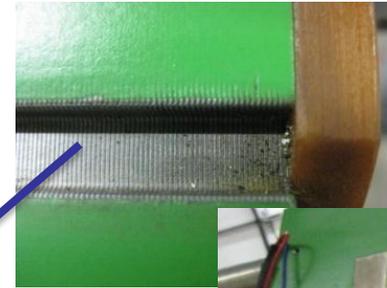
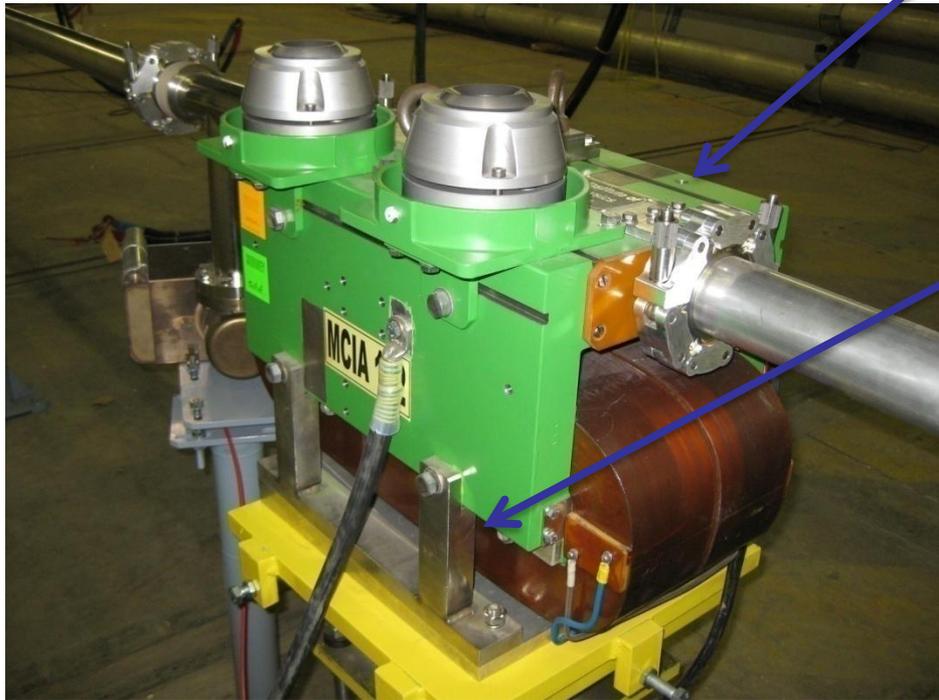
Magnet with solid yoke parts assembled with bolts.



Main parameters	
Name	MDX
Type	Vertical correcting dipole
Installation	SPS experimental area
Nominal peak field [T]	1.33
I_{\max} [A]	240
Résistance [Ω]	0.305
Inductance [H]	0.221
Yoke length [mm]	400
Gap [mm]	80
Total weight [kg]	1000

Corrector dipole in TI2 and TI8 LHC injection lines

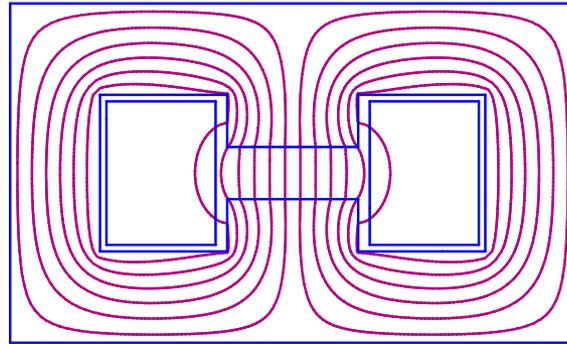
Magnet with glued laminated yokes assembled with bolts.



Main parameters	
Name	MCIA V
Type	Vertical correcting dipole
Nominal peak field [T]	0.26
I_{\max} [A]	3.5
N. Of turns	1014
Résistance [Ω]	13.9
Yoke lenght [mm]	450
Gap [mm]	32.5
Total weight [kg]	300

Main dipole in the SPS

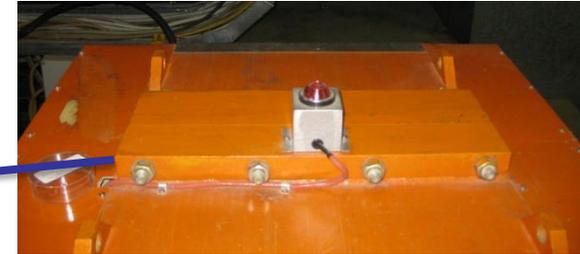
Magnet with laminations welded in a steel envelope
 H-type dipole, half-yokes assembled with welded plates



Main parameters	
Name	MBB
Type	Bending dipole
Nominal peak field [T]	1.8
I_{max} [A]	4900
N. Of turns	16
Résistance [Ω]	$4.46 \cdot 10^{-3}$
Inductance [H]	0.018
Yoke lenght [mm]	2225
Gap [mm]	52
Total weight [kg]	17400

Corrector dipole for E-Cloud experiment in SPS

Magnet with laminations welded in a steel envelope half-yokes assembled with bolts.



Main parameters	
Name	MDVW
Type	Vertical correcting dipole
Nominal peak field [T]	0.266
I_{\max} [A]	55
N. Of turns	2 x 50
Résistance [Ω]	1.76
Inductance [H]	1.12
Yoke lenght [mm]	429
Gap [mm]	200
Total weight [kg]	1100

Corrector dipole for BBLR experiment in SPS

Water-cooled magnet with plain conductor coils equipped with external water circuit.



Main parameters	
Name	MCVA
Type	Vertical correcting dipole
Nominal peak field [T]	0.059
I_{\max} [A]	5
Résistance [Ω]	12.5
Yoke length [mm]	400
Gap [mm]	170
Total weight [kg]	130

Air-cooled magnet



Main parameters	
Name	MCVA
Type	Vertical correcting dipole
Nominal peak field [T]	0.059
I_{\max} [A]	5
Résistance [Ω]	12.5
Yoke length [mm]	400
Gap [mm]	170
Total weight [kg]	130

Water-cooled magnet with insulators



Moulded insulating distributor



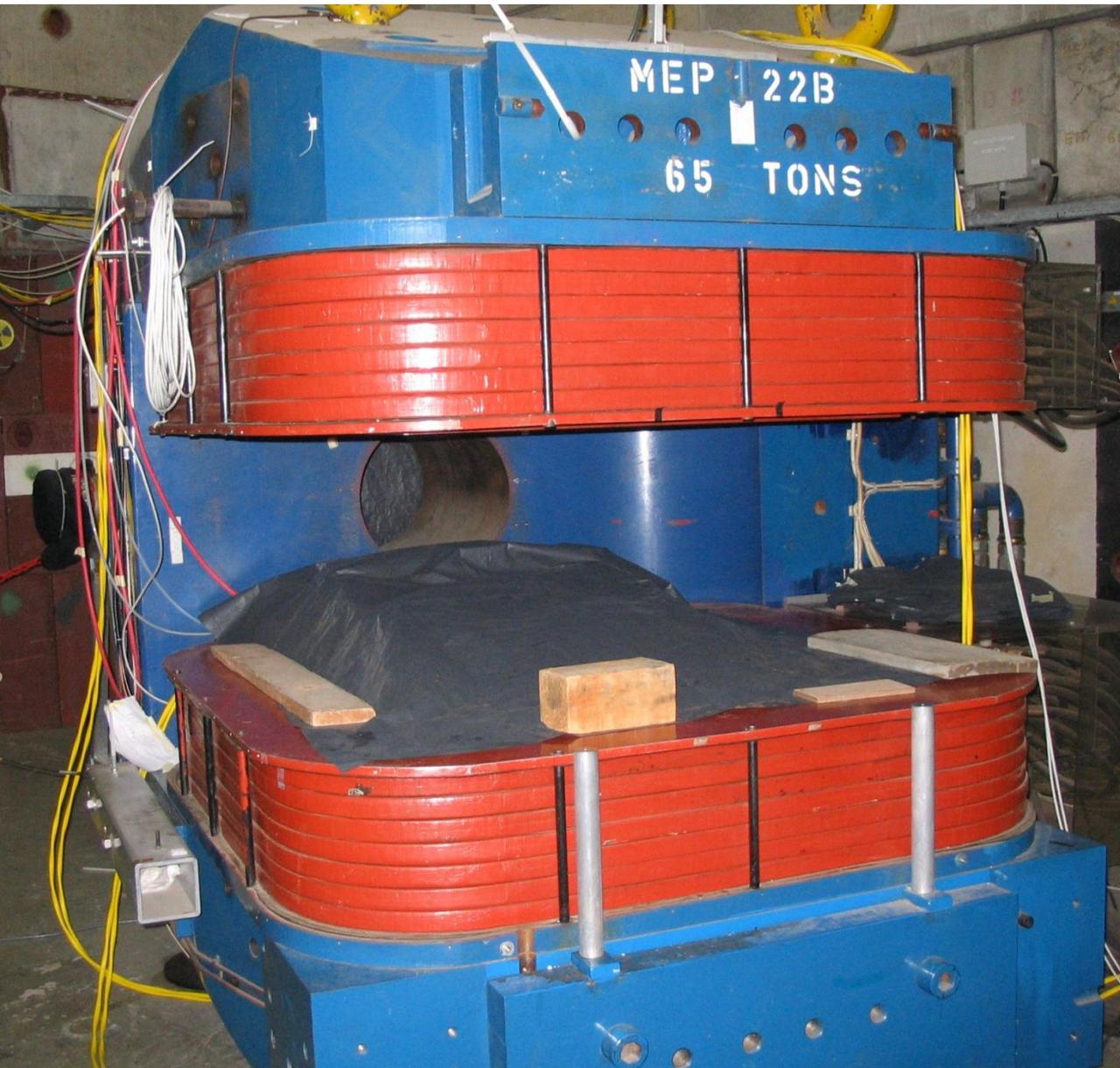
Separated insulators

Main parameters	
Name	QTL
Type	Quadrupole
Nominal gradient field [T/m]	24
I_{\max} [A]	416
N. Of turns	4 x 42
Résistance [Ω]	0.276
Inductance [H]	0.390
Yoke length [mm]	2990
Inscribed radius [mm]	80
Total weight [kg]	9900

Water-cooled magnet without insulators (insulating hoses).



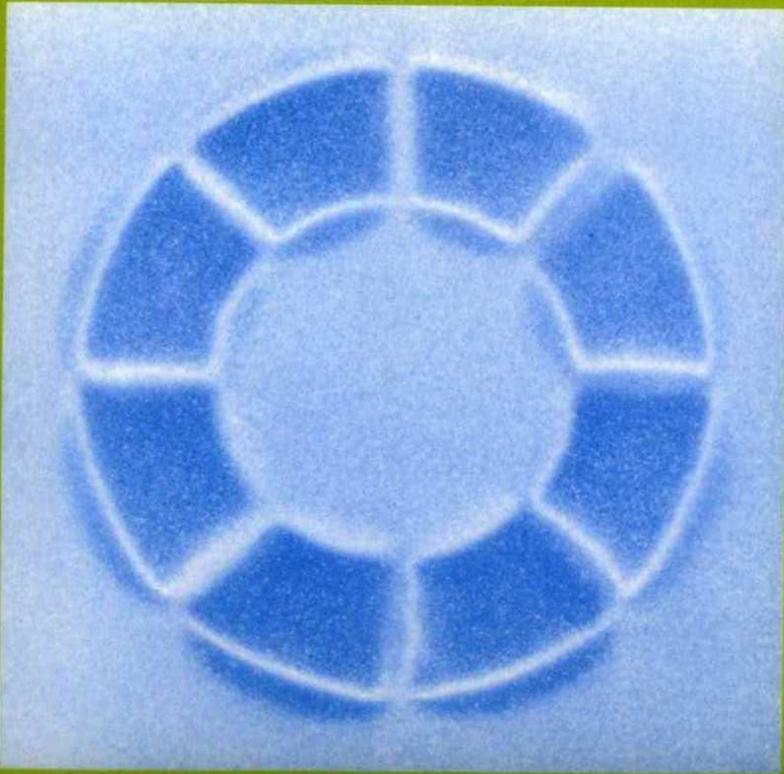
Main parameters	
Name	MQI
Type	Quadrupole
Nominal gradient field [T/m]	≥ 53.5
I_{\max} [A]	530
N. Of turns	4 x 11
Résistance [Ω]	0.036
Inductance [H]	0.013
Yoke length [mm]	1400
Inscribed radius [mm]	16
Total weight [kg]	1070



Parameter	Value
Aperture	500 mm
Nominal field	1.4 T
Pole width	1000 mm
Pole length	1000 mm
Weight	65 t
Power	750 kW

Permanent Magnet Materials and their Application

PETER CAMPBELL



$A_2 = \text{Re } C_2 z^2 = C_2(x^2 - y^2)$
 $V_2 = \text{Im } C_2 z^2 = 2C_2xy$

$A_3 = \text{Re } C_3 z^3 = C_3(x^3 - 3xy^2)$
 $V_3 = \text{Im } C_3 z^3 = C_3xy(3x^2y - y^3)$

Jack T. Tanabe

Iron Dominated Electromagnets

Design, Fabrication, Assembly and Measurements