

Beam-beam effects

(an introduction)

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(http://cern.ch/lhc-beam-beam/talks/Daresbury_beambeam.pdf)

BEAMS: moving charges

- Beam is a collection of charges
- Represent electromagnetic potential for other charges
- Forces on itself (**space charge**) and opposing beam (**beam-beam effects**)
- Main limit in past, present and future colliders
- Important for high density beams, i.e. high intensity and/or small beams:
for **high luminosity** !



Beam-beam effects

Remember:

$$\Rightarrow \mathcal{L} = \frac{N_1 N_2 f n_B}{4\pi \sigma_x \sigma_y} = \frac{N_1 N_2 f n_B}{4\pi \cdot \sigma_x \sigma_y}$$

- Overview: which effects are important for present and future machines (LEP, PEP, Tevatron, RHIC, LHC, ...)
- Qualitative and physical picture of the effects
- Mathematical derivations in:
Proceedings, Zeuthen 2003



Beam-beam effects

- A beam acts on particles like an electromagnetic lens, but:
 - Does not represent simple form, i.e. well defined multipoles
 - Very non-linear form of the forces, depending on distribution
 - Can change distribution as result of interaction (time dependent forces ..)
 - Results in many different effects and problems
-

Fields and Forces (I)

- Need fields \vec{E} and \vec{B} of opposing beam.
- In rest frame only electrostatic field: \vec{E}' , $\vec{B}' \equiv 0$
- Derive potential $U(x, y, z)$ from Poisson equation:

$$\Delta U(x, y, z) = -\frac{1}{\epsilon_0} \rho(x, y, z)$$

- The electrostatic fields become:

$$\vec{E}' = -\nabla U(x, y, z)$$



Fields and Forces (II)

- Transform into moving frame and calculate Lorentz force \vec{F} on particle with charge $q = Z_2 e$

$$E_{\parallel} = E'_{\parallel}, \quad E_{\perp} = \gamma \cdot E'_{\perp} \quad \text{with:} \quad \vec{B} = \vec{\beta} \times \vec{E}/c$$

$$\vec{F} = q(\vec{E} + \vec{\beta} \times \vec{B})$$

- Example Gaussian distribution:

$$\rho(x, y, z) = \frac{NZ_1e}{\sigma_x\sigma_y\sigma_z\sqrt{2\pi}^3} \exp\left(-\frac{x^2}{2\sigma_x^2} - \frac{y^2}{2\sigma_y^2} - \frac{z^2}{2\sigma_z^2}\right)$$


Simple example: Gaussian

- For 2D case the potential becomes
(see proceedings):

$$U(x, y, \sigma_x, \sigma_y) = \frac{NZ_1e}{4\pi\epsilon_0} \int_0^\infty \frac{\exp\left(-\frac{x^2}{2\sigma_x^2+q} - \frac{y^2}{2\sigma_y^2+q}\right)}{\sqrt{(2\sigma_x^2+q)(2\sigma_y^2+q)}} dq$$

- Can derive \vec{E} and \vec{B} fields and therefore forces
- For arbitrary distribution (non-Gaussian):
difficult (or impossible, numerical solution
required)

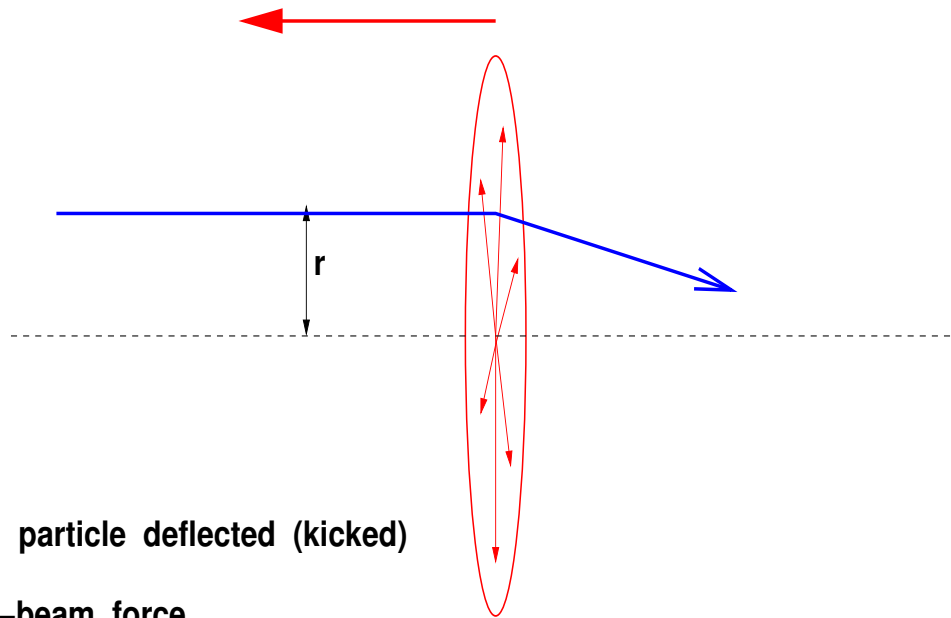
Simple example: Gaussian

- Round beams: $\sigma_x = \sigma_y = \sigma$, $Z_1 = -Z_2 = 1$
- Only components E_r and B_Φ are non-zero
- Force has only radial component, i.e. depends only on distance r from bunch centre
(where: $r^2 = x^2 + y^2$) (see proceedings)

$$F_r(r) = -\frac{Ne^2(1 + \beta^2)}{2\pi\epsilon_0 \cdot r} \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$

Beam-beam kick:

→ We need the deflection (kick) of the particle:



Beam-beam kick:

- Kick ($\Delta r'$): angle by which the particle is deflected during the passage
- Derived from force by integration over the collision (assume: $m_1=m_2$ and $Z_1=-Z_2=1$):

$$F_r(r, s, t) = -\frac{Ne^2(1 + \beta^2)}{\sqrt{(2\pi)^3\epsilon_0 r \sigma_s}} \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right] \cdot \left[\exp\left(-\frac{(s + vt)^2}{2\sigma_s^2}\right) \right]$$

with Newton's law :

$$\Delta r' = \frac{1}{mc\beta\gamma} \int_{-\infty}^{\infty} F_r(r, s, t) dt$$



Beam-beam kick:


→ Using the classical particle radius (implies $Z_1 = \pm Z_2$):

$$r_0 = e^2 / 4\pi\epsilon_0 mc^2$$

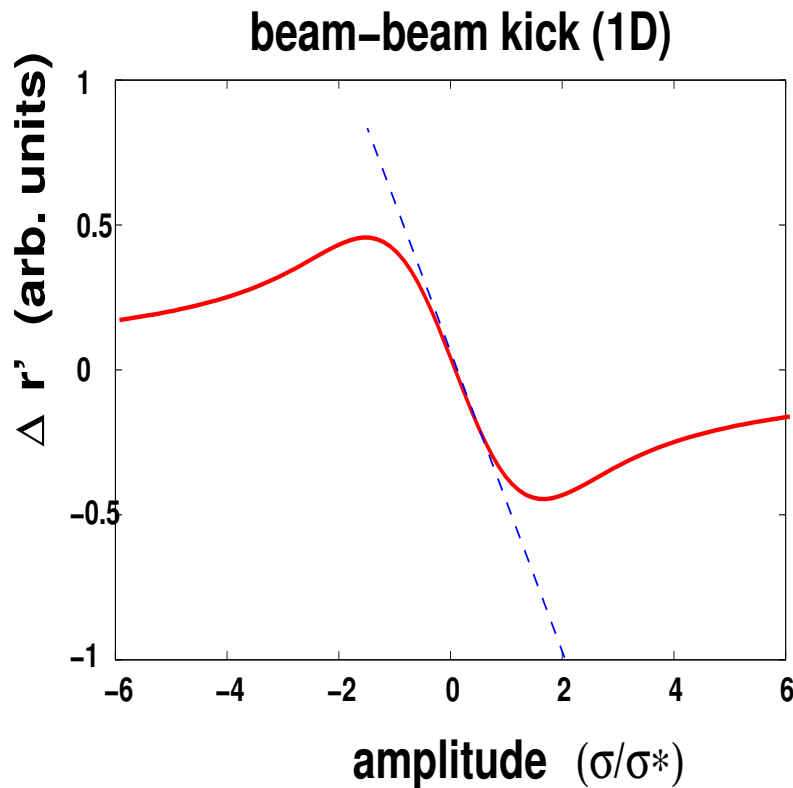
we have (radial kick and in Cartesian coordinates):

$$\Delta r' = -\frac{2Nr_0}{\gamma} \cdot \frac{r}{r^2} \cdot \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$

$$\Delta x' = -\frac{2Nr_0}{\gamma} \cdot \frac{x}{r^2} \cdot \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$

$$\Delta y' = -\frac{2Nr_0}{\gamma} \cdot \frac{y}{r^2} \cdot \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$


Beam-beam force/kick



- For small amplitudes: linear force
- ▶ amplitude independent tune change (like quadrupole)
- For large amplitudes: very non-linear
- ▶ amplitude dependent tune change (like non-linear fields)

Can we quantify the beam-beam strength ?

- Try the slope of force (kick $\Delta r'$) at zero amplitude
- This defines: beam-beam parameter ξ
- For head-on interactions and round beams ($\beta^* = \beta_x^* = \beta_y^*$) we get:

$$\xi = \frac{\beta^*}{4\pi} \cdot \frac{\delta(\Delta r')}{\delta r} = \frac{N \cdot r_0 \cdot \beta^*}{4\pi \gamma \sigma^2}$$

LEP - LHC

	LEP (e^+e^-)	LHC (pp)
Beam sizes	160 - 200 μm · 2 - 4 μm	16.6 μm · 16.6 μm
Intensity N	4.0 · 10 ¹¹ /bunch	1.15 · 10 ¹¹ /bunch
Energy	100 GeV	7000 GeV
β_x^* · β_y^*	1.25 m · 0.05 m	0.55 m · 0.55 m
Crossing angle	0.0	285 μrad
Beam-beam parameter(ξ)	(+) 0.0700	(-) 0.0034

Can we quantify the beam-beam strength ?

■ In general for non-round beams ($\beta_x^* \neq \beta_y^*$):

$$\xi_{x,y} = \frac{N \cdot r_o \cdot \beta_{x,y}^*}{2\pi\gamma\sigma_{x,y}(\sigma_x + \sigma_y)}$$

■ Proportional to (linear) tune shift ΔQ_{bb} from beam-beam interaction: $\Delta Q_{bb} \propto \pm \xi$

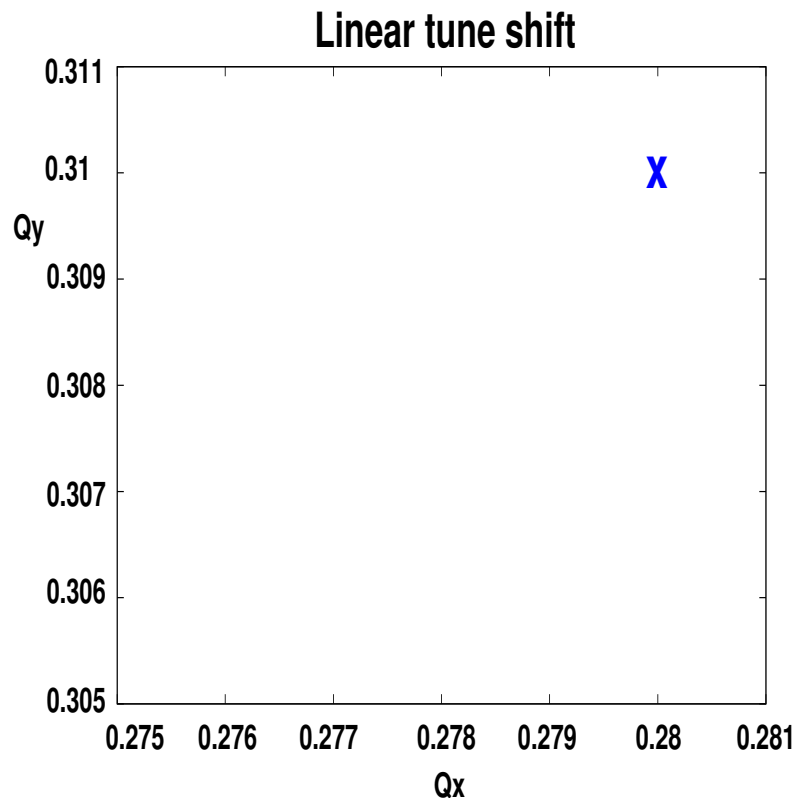
■ Good measure for strength of beam-beam interaction

■ BUT: does not describe

→ changes to optical functions

→ non-linear part of beam-beam force

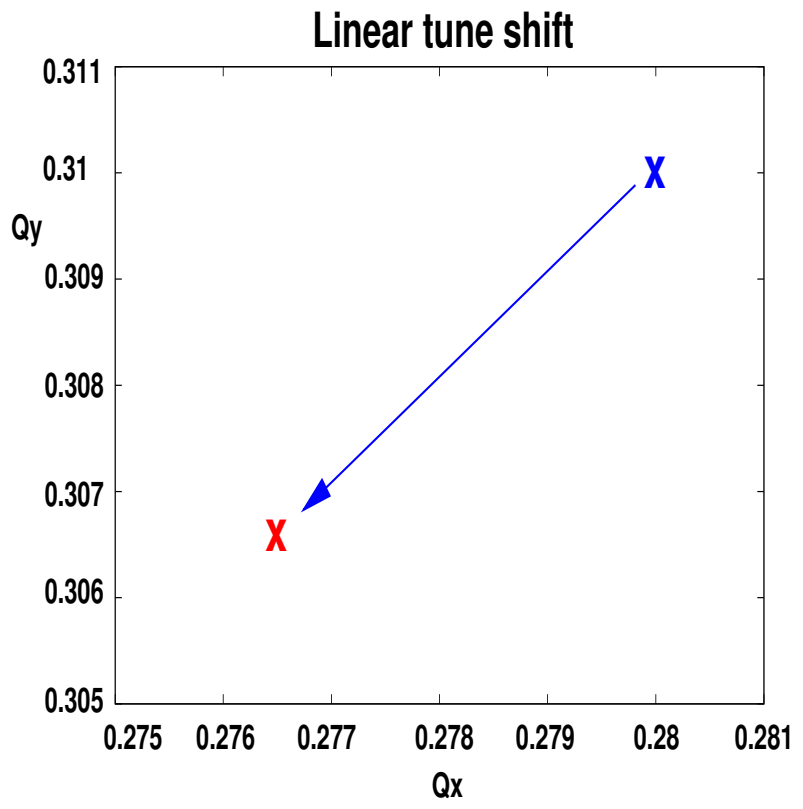
Linear tune shift - two dimensions



- Start with standard working point
- LHC (equally charged beams)
- Beam-beam shifts tune in both planes



Linear tune shift - two dimensions

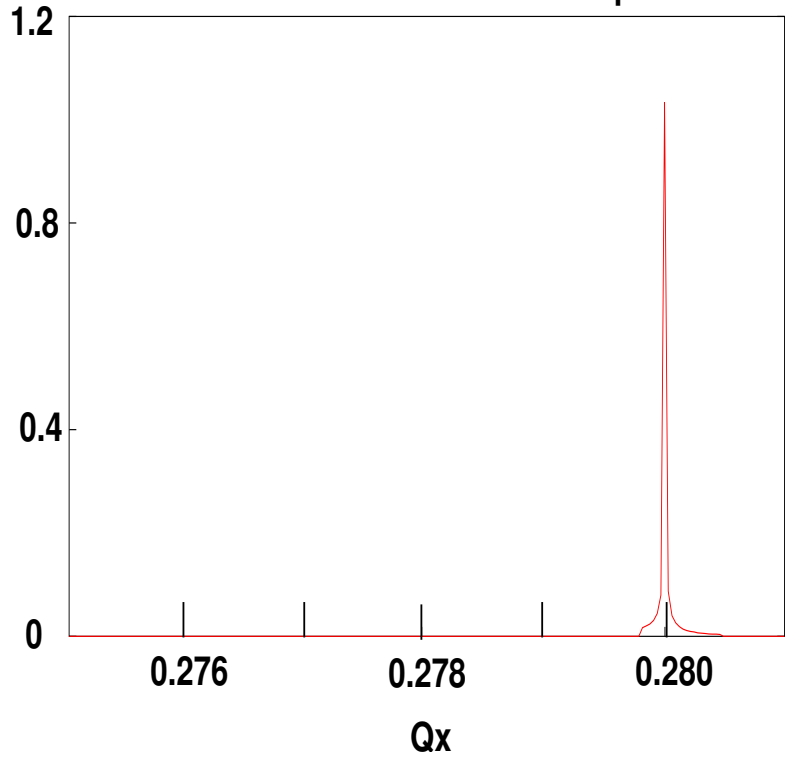




- Start with standard working point
- LHC (equally charged beams)
- Beam-beam shifts tune in both planes



Tune measurement: linear optics

Tune distribution for linear optics

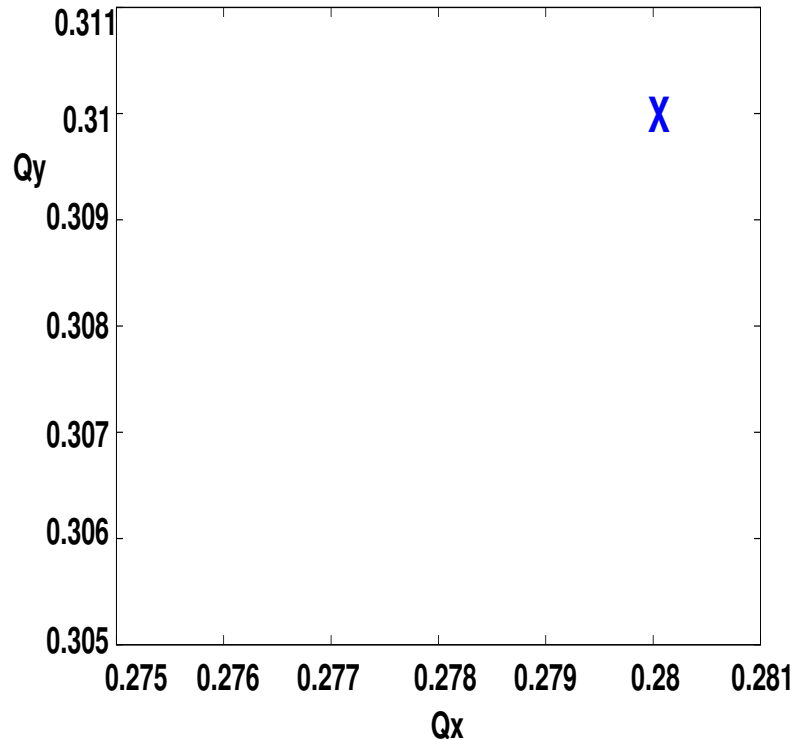


- Linear force: 
- all particles have same tune
- Only one frequency (tune) visible 



Non-linear tune shift - two dimensions

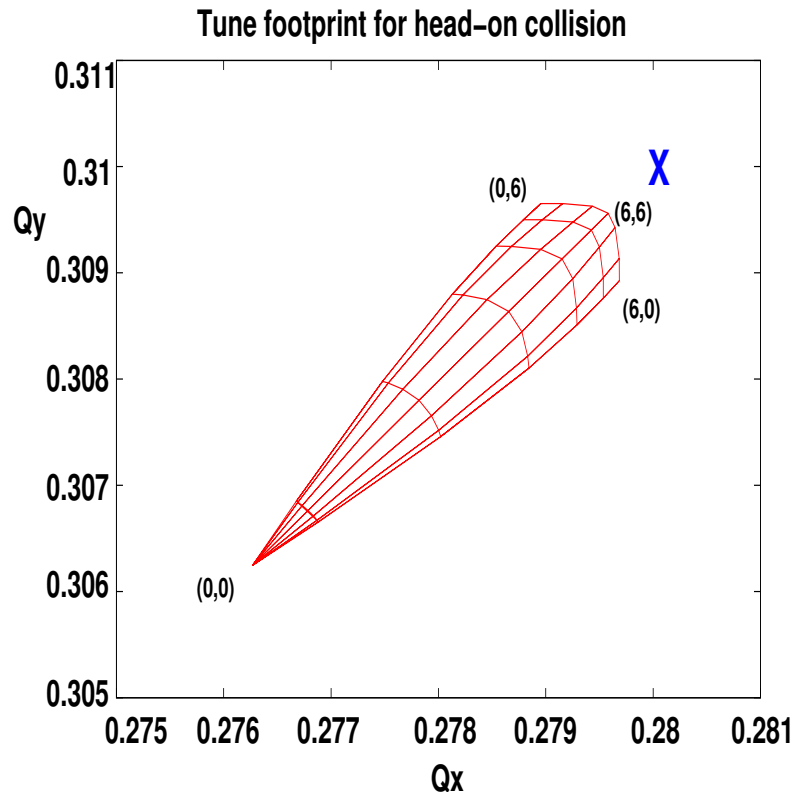
Tune footprint for head-on collision



- Tunes depend on x **and** y amplitudes
- No single tune in the beam
- Compute and plot for every amplitude (pair) the tunes in both planes
- In 2 dimensions:
plotted as **footprint**



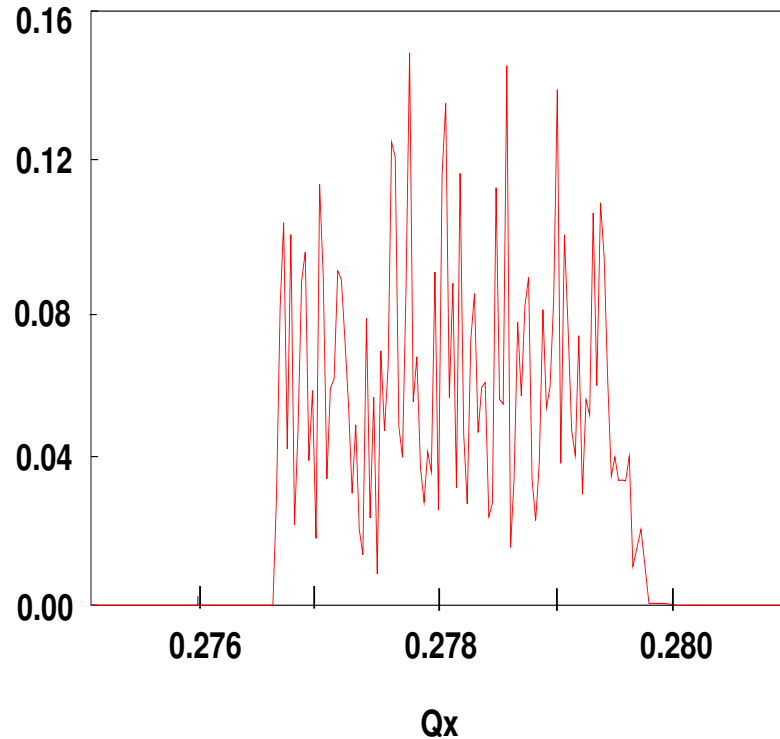
Non-linear tune shift - two dimensions



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Tune measurement: with beam-beam

Tune distribution for optics with beam-beam

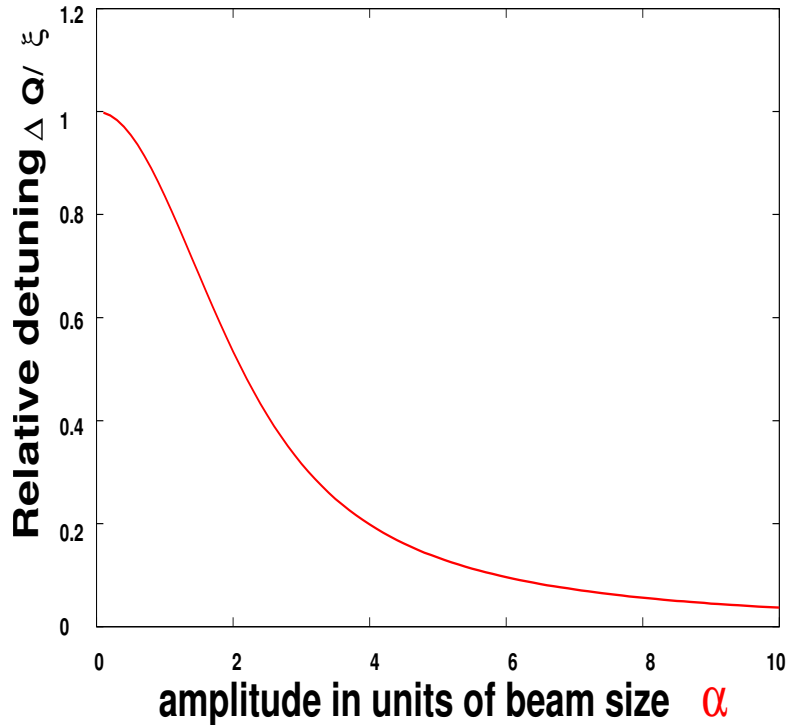


- Non-linear force: →
- particles with different amplitudes have different frequencies (tunes)
- ▶ We get frequency (tune) spectra
- ▶ Width of the spectra: about ξ



Amplitude detuning

Detuning with amplitude – round beams



■ Non-linear force: 
tune depends on amplitude

■ Largest effect for **small** amplitudes

▶ Calculation in the **proceedings**

→ with $\alpha = \frac{\sigma}{\sigma_*}$ we get:
$$\Delta Q/\xi = \frac{4}{\alpha^2} \left[1 - I_0\left(\frac{\alpha^2}{4}\right) \cdot e^{-\frac{\alpha^2}{4}} \right]$$

Weak-strong and strong-strong

- Both beams are very strong (**strong-strong**):
 - Both beams are affected and change due to beam-beam interaction
 - Examples: LHC, LEP, RHIC, ...
- One beam much stronger (**weak-strong**):
 - Only the weak beam is affected and changed due to beam-beam interaction
 - Examples: SPS collider, Tevatron, ...



Incoherent effects

(single particle effects)

- Single particle dynamics: treat as a particle through a static electromagnetic lens
- Basically non-linear dynamics
- All single particle effects observed:
 - Unstable and/or irregular motion
 - beam blow up or bad lifetime



Observations hadrons

- Non-linear motion can become chaotic
 - reduction of "dynamic aperture"
 - particle loss and bad lifetime
- Strong effects in the presence of noise or ripple
- Very bad: unequal beam sizes (studied at SPS, HERA)
- Evaluation is done by simulation



Observations leptons

Remember:

$$\Rightarrow \mathcal{L} = \frac{N_1 N_2 f n_B}{4\pi\sigma_x\sigma_y}$$

■ Luminosity should increase $\propto N_1 N_2$

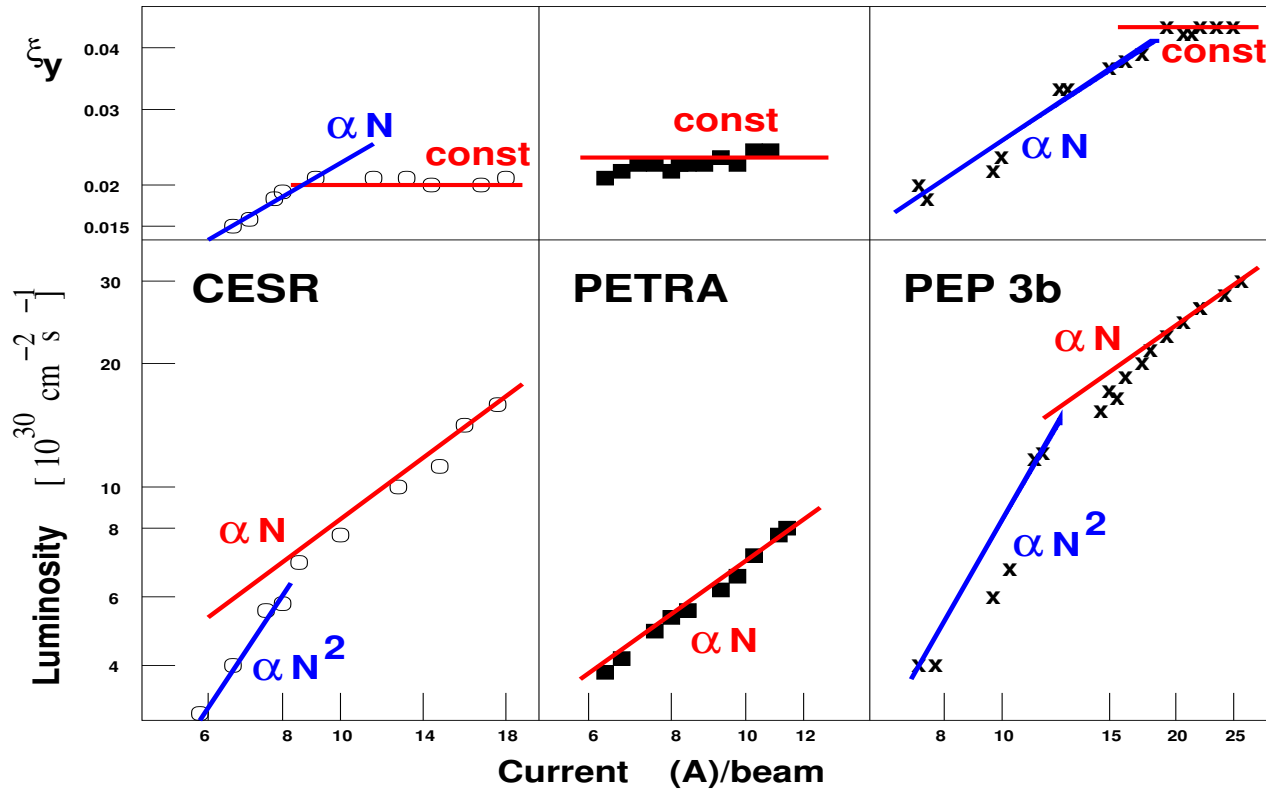
→ for: $N_1 = N_2 = N$ → $\propto N^2$

■ Beam-beam parameter should increase $\propto N$

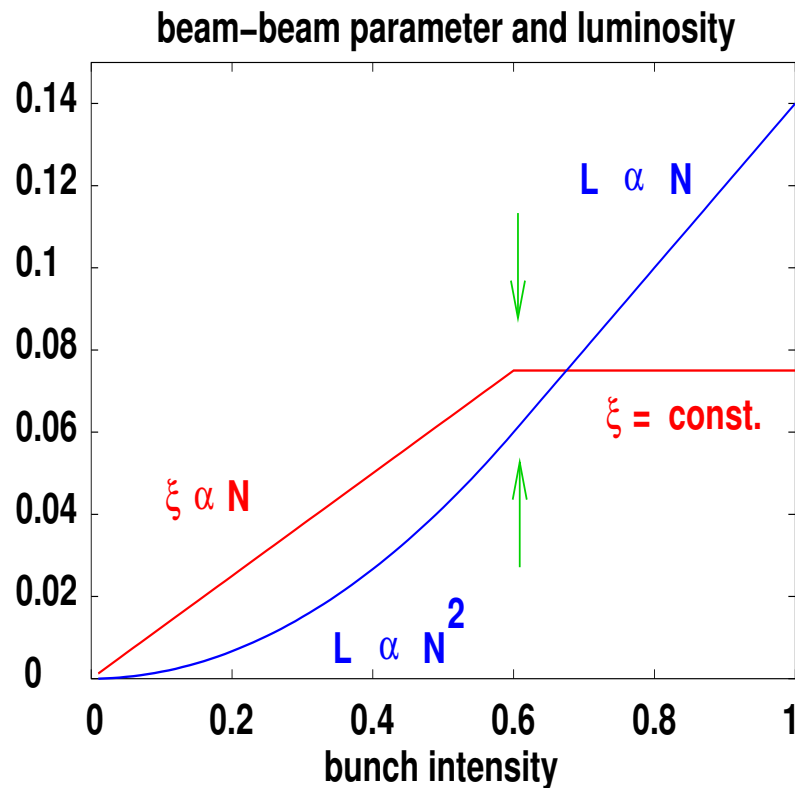
■ But:



Examples: beam-beam limit



Beam-beam limit (schematic)



■ Beam-beam parameter increases linearly with intensity

■ Saturation above some intensity

▶ Luminosity increases linearly

▶ So-called **beam-beam limit**

What is happening ?

we have
$$\xi_y = \frac{Nr_0\beta_y}{2\pi\gamma\sigma_y(\sigma_x + \sigma_y)} \quad (\sigma_x \gg \sigma_y) \quad \approx \quad \frac{r_0\beta_y}{2\pi\gamma(\sigma_x)} \cdot \frac{N}{\sigma_y}$$

and
$$\mathcal{L} = \frac{N^2fn_B}{4\pi\sigma_x\sigma_y} = \frac{Nfn_B}{4\pi\sigma_x} \cdot \frac{N}{\sigma_y}$$

- Above beam-beam limit: σ_y increases when N increases to keep ξ constant \rightarrow **equilibrium emittance !**
 - Therefore: $\mathcal{L} \propto N$ and $\xi \approx$ constant
 - ξ_{limit} is NOT a universal constant !
 - Difficult to predict
-

The next problem

Remember:

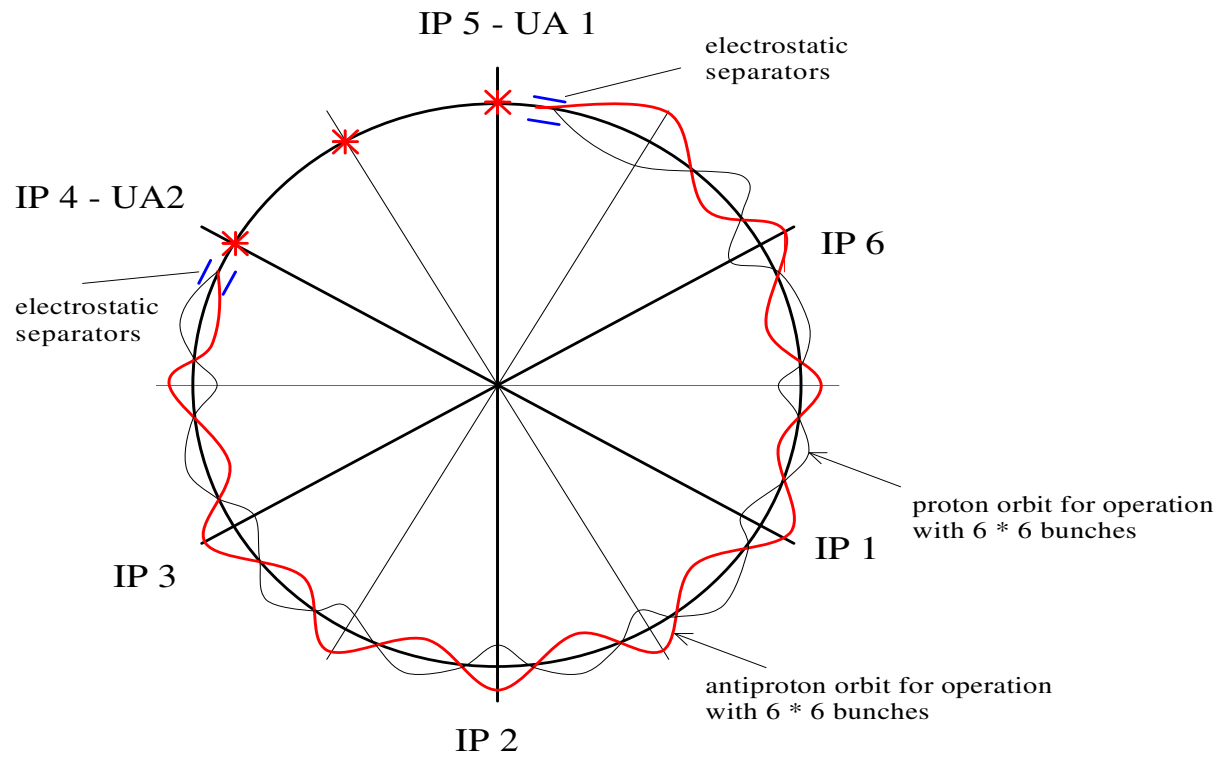
$$\Rightarrow \mathcal{L} = \frac{N_1 N_2 f \cdot n_B}{4\pi\sigma_x\sigma_y}$$

- How to collide many bunches (for high \mathcal{L}) ??
- Must avoid unwanted collisions !!
- Separation of the beams:
 - Pretzel scheme (SPS, LEP, Tevatron)
 - Bunch trains (LEP, PEP)
 - Crossing angle (LHC)

Separation: SPS

- \Rightarrow Few equidistant bunches
(6 against 6)
 - Beams travel in same beam pipe
(12 collision points !)
 - Two experimental areas
 - Need **global** separation
 - Horizontal pretzel around most of the circumference
-

Separation: SPS

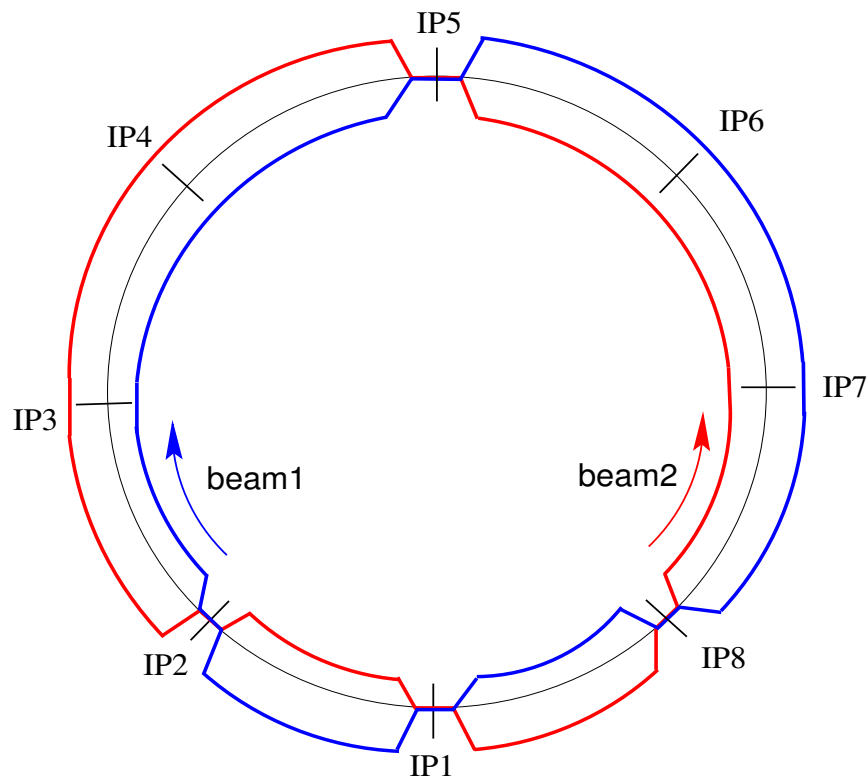


Separation: LHC

- \Rightarrow Many equidistant bunches
- Two beams in separate beam pipes except:
 - Four experimental areas
 - Need **local** separation
- Two horizontal and two vertical crossing angles

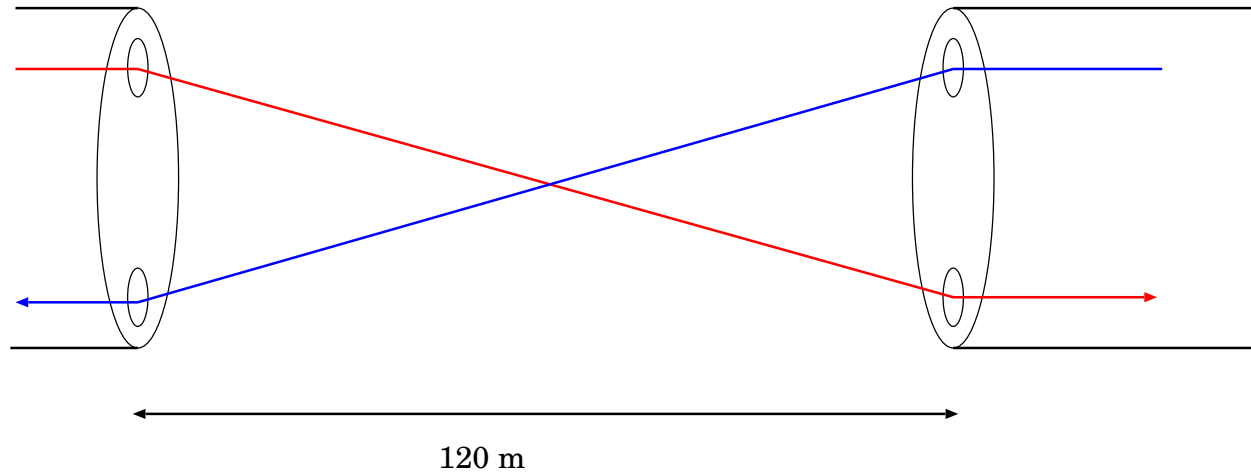


Layout of LHC



Example: LHC

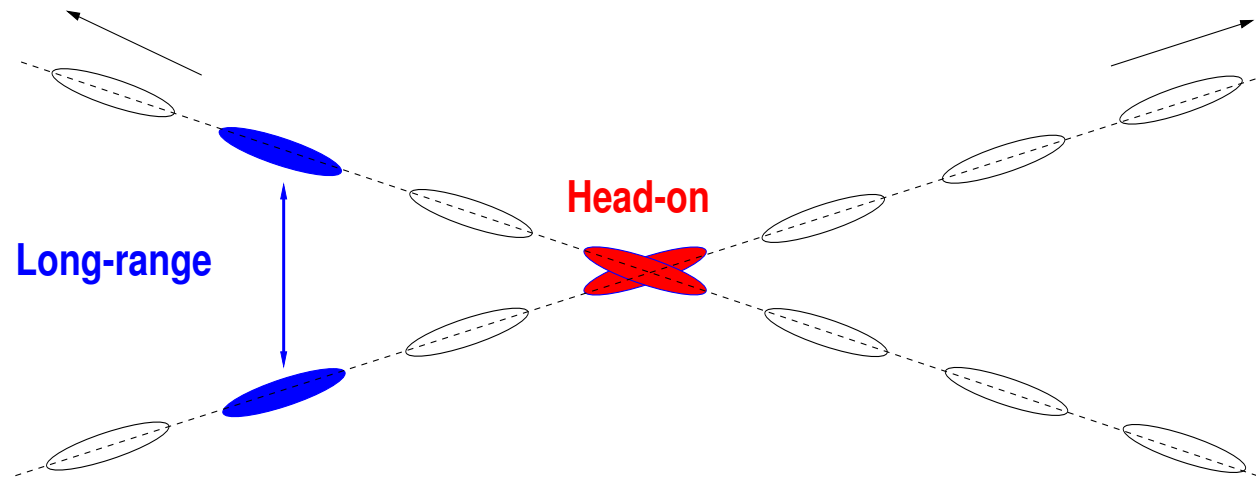
- Two beams, 2808 bunches each, every 25 ns
- In common chamber around experiments



- Over 120 m: about 30 parasitic interactions



Crossing angles (example LHC)



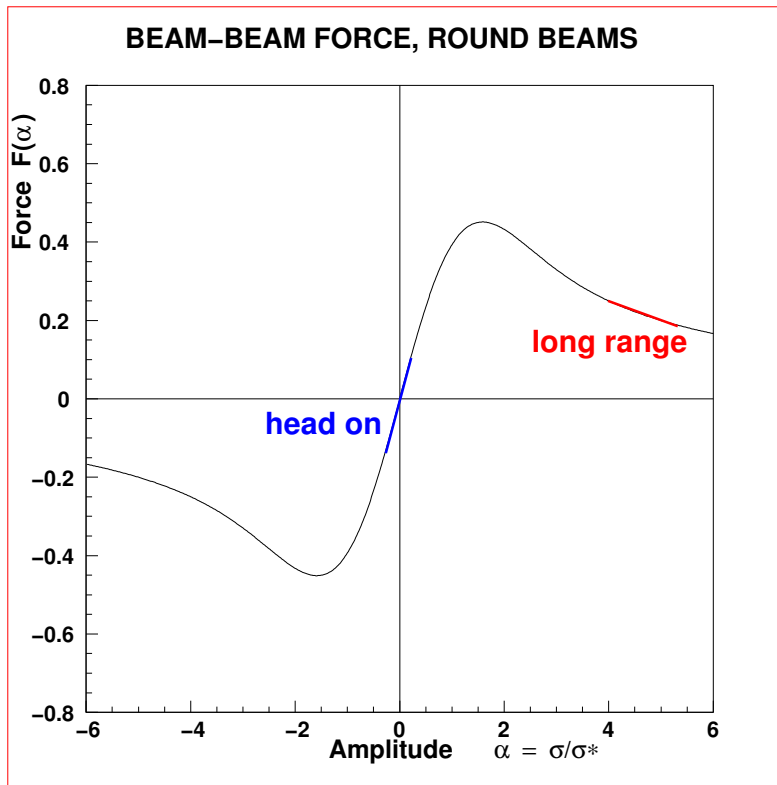
- Particles experience distant (weak) forces
- Separation typically $6 - 12 \sigma$
- We get so-called **long range interactions**

What is special about them ?

- Break symmetry between planes, also odd resonances
- Mostly affect particles at **large** amplitudes
- Cause effects on closed orbit
- PACMAN effects
- Tune shift has **opposite** sign in plane of separation

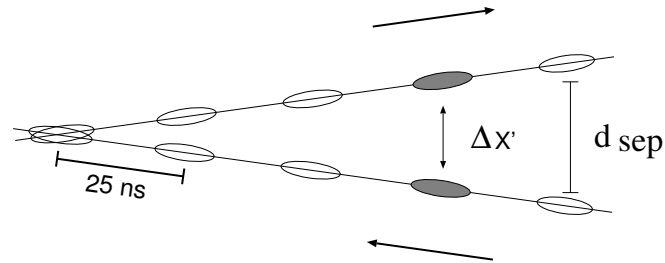


Why opposite tuneshift ???



- ▶ **Local** slope of force has opposite sign for large separation
- ▶ Opposite sign for focusing
- ▶ Used for partial compensation

Long range interactions (LHC)

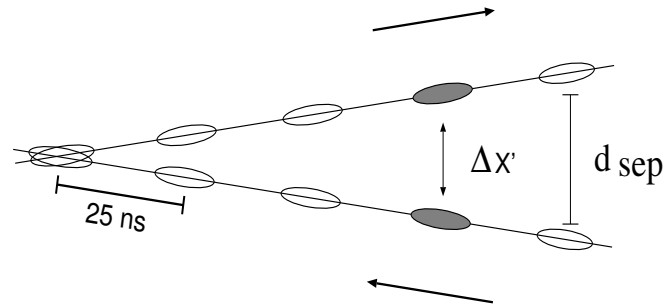


→ For horizontal separation d :

$$\Delta x'(x + d, y, r) = -\frac{2Nr_0}{\gamma} \cdot \frac{(x + d)}{r^2} \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$

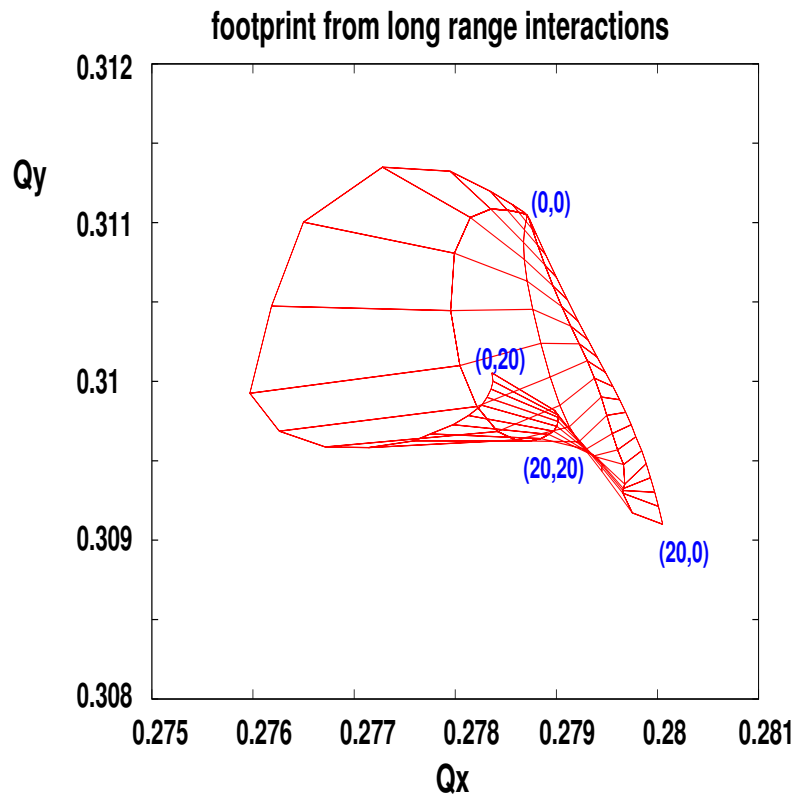
(with: $r^2 = (x + d)^2 + y^2$)

Long range interactions (LHC)



- Number of long range interactions depends on spacing and length of common part
- In LHC 15 collisions on each side, 120 in total !
- Effects depend on separation: $\Delta Q \propto -\frac{N}{d^2}$ (for large enough d !) footprints ??

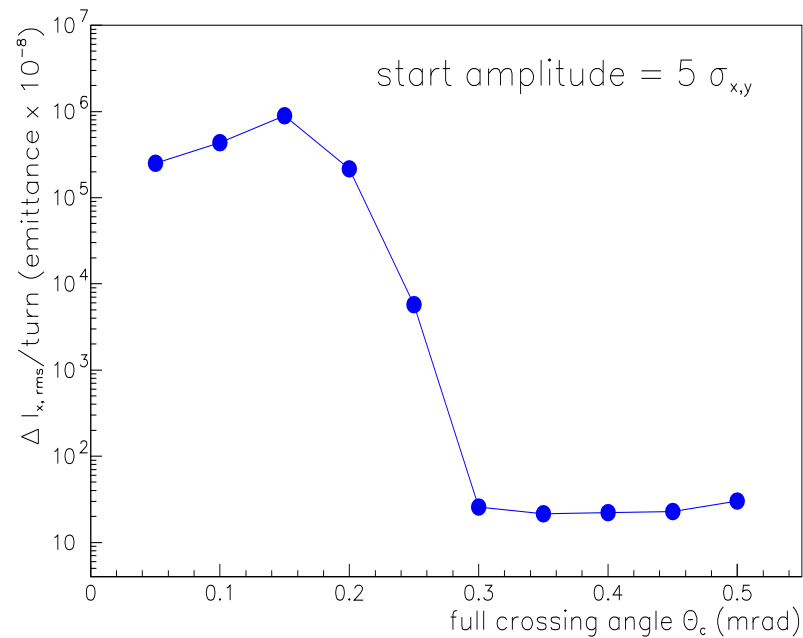
Footprints



- ▶ Large fo largest amplitudes where non-linearities are strong
- ▶ Size proportional to $\frac{1}{d^2}$
- ▶ Must expect problems at small separation
- ▶ Footprint very asymmetric

Particle losses

- Small crossing angle \iff small separation
- Small separation: particles become unstable and get lost



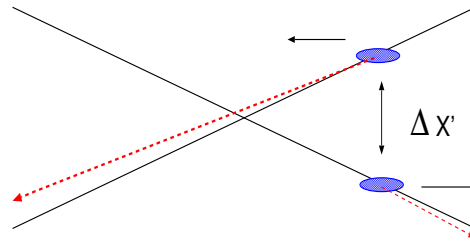
- Minimum crossing angle for LHC: $285 \mu\text{rad}$

Closed orbit effects

$$\Delta x'(x + d, y, r) = -\frac{2Nr_0}{\gamma} \cdot \frac{(x + d)}{r^2} \left[1 - \exp\left(-\frac{r^2}{2\sigma^2}\right) \right]$$

For well separated beams ($d \gg \sigma$) the force (kick) has an amplitude independent contribution: \rightarrow orbit kick

$$\Delta x' = \underbrace{\frac{\text{const.}}{d}} \cdot \left[1 - \frac{x}{d} + O\left(\frac{x^2}{d^2}\right) + \dots \right]$$

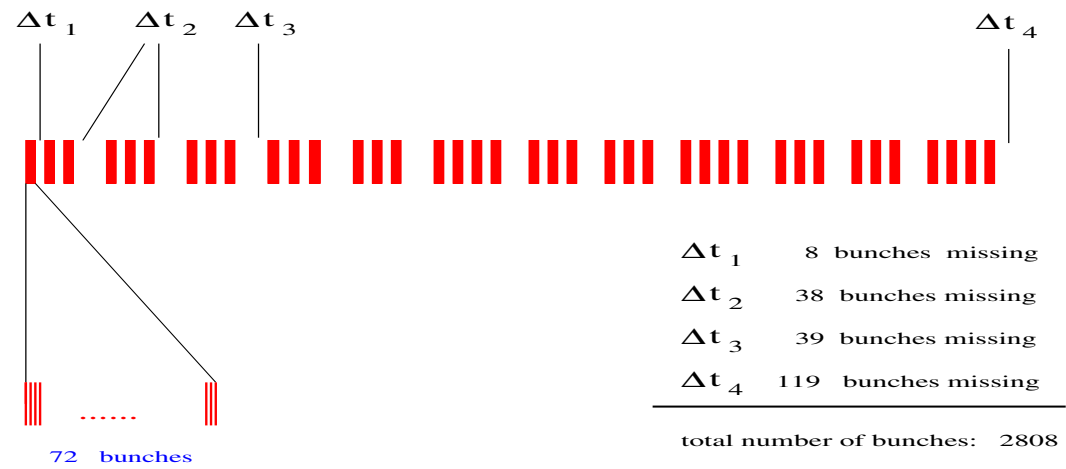


Closed orbit effects

- Beam-beam kick from long range interactions changes the orbit
 - Has been observed in LEP with bunch trains
 - Self-consistent calculation necessary
 - Effects can add up and become important
- Orbit can be corrected, **but:**



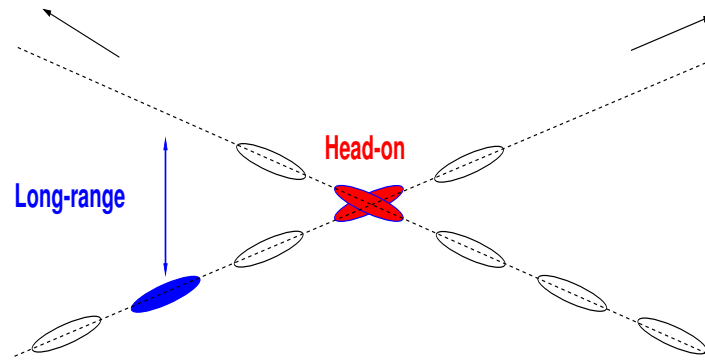
PACMAN bunches



- LHC bunch filling not continuous: holes for injection, extraction, dump ..
- 2808 of 3564 possible bunches → 1756 "holes"
- "Holes" meet "holes" at the interaction point
- But not always ...



Effect of holes



- A bunch can meet a hole (at beginning and end of bunch train)
- Results in left-right asymmetry
- Example LHC: between 120 (max) and 40 (min) long range collisions for different bunches



PACMAN bunches

■ When a bunch meets a "hole":

- Miss some long range interactions, PACMAN bunches
- They see fewer unwanted interactions in total
- Different integrated beam-beam effect

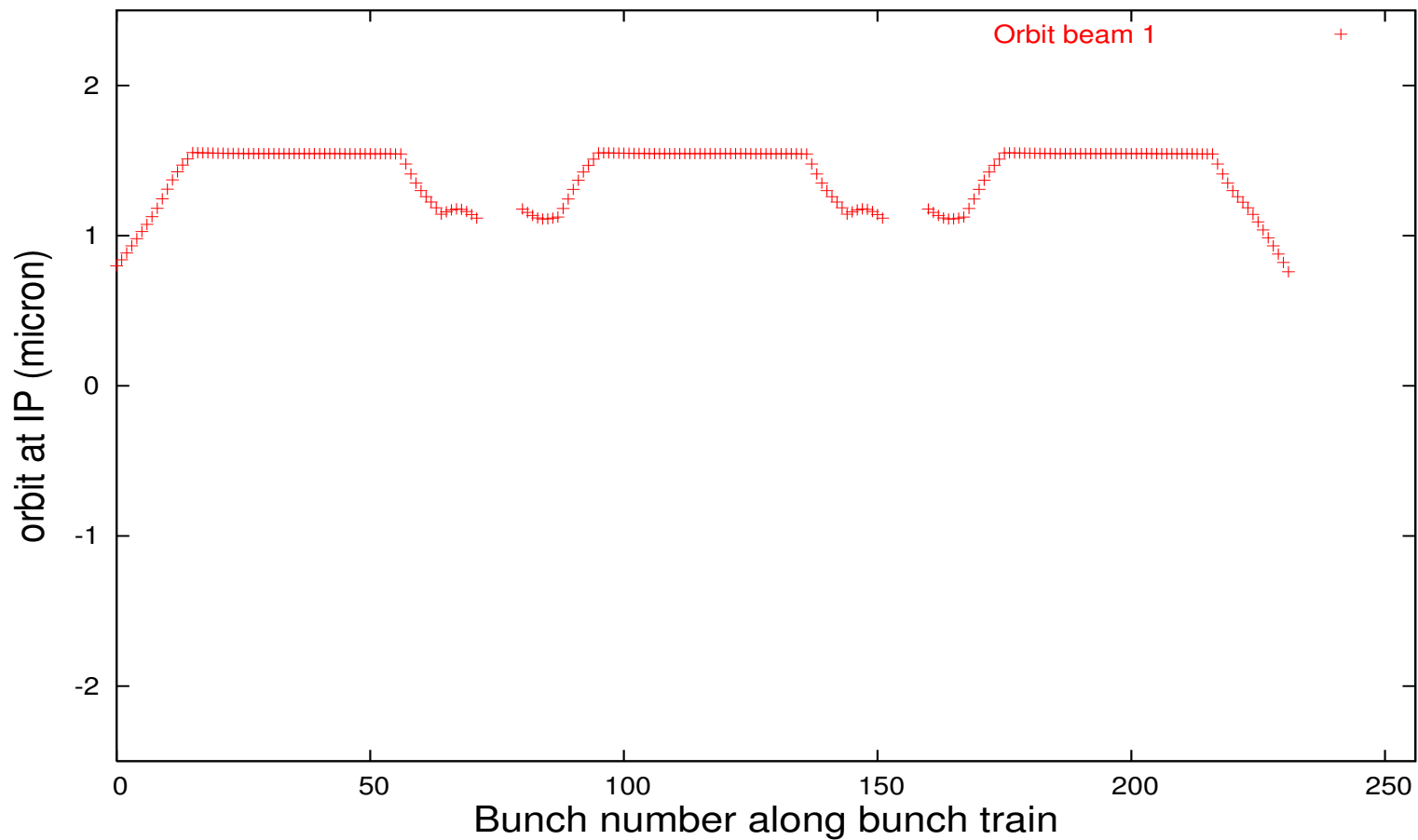
■ In general: when different bunches have different beam-beam effects

■ Example: orbit and tune effects



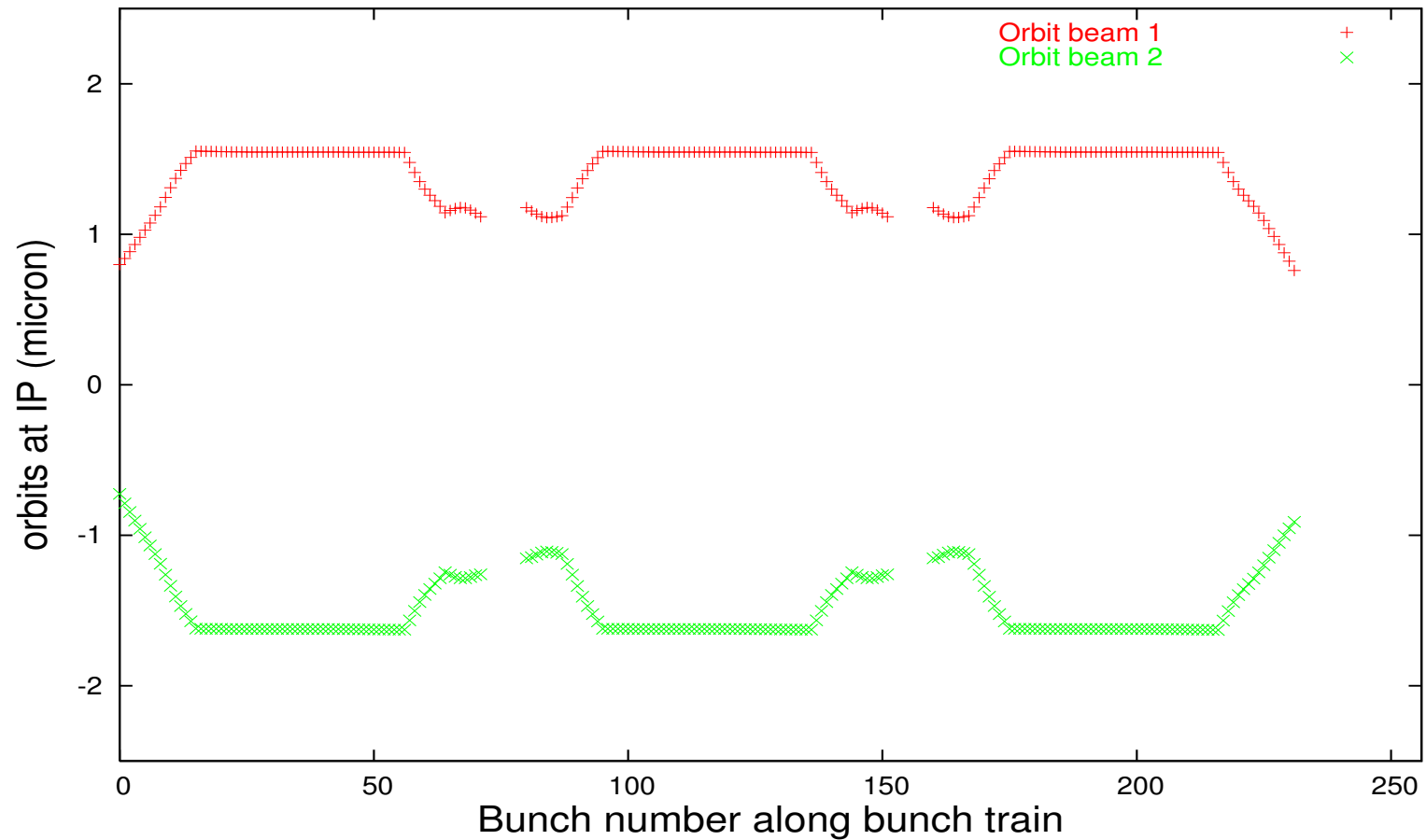
Orbit along LHC batches: beam 1

Orbit along bunches



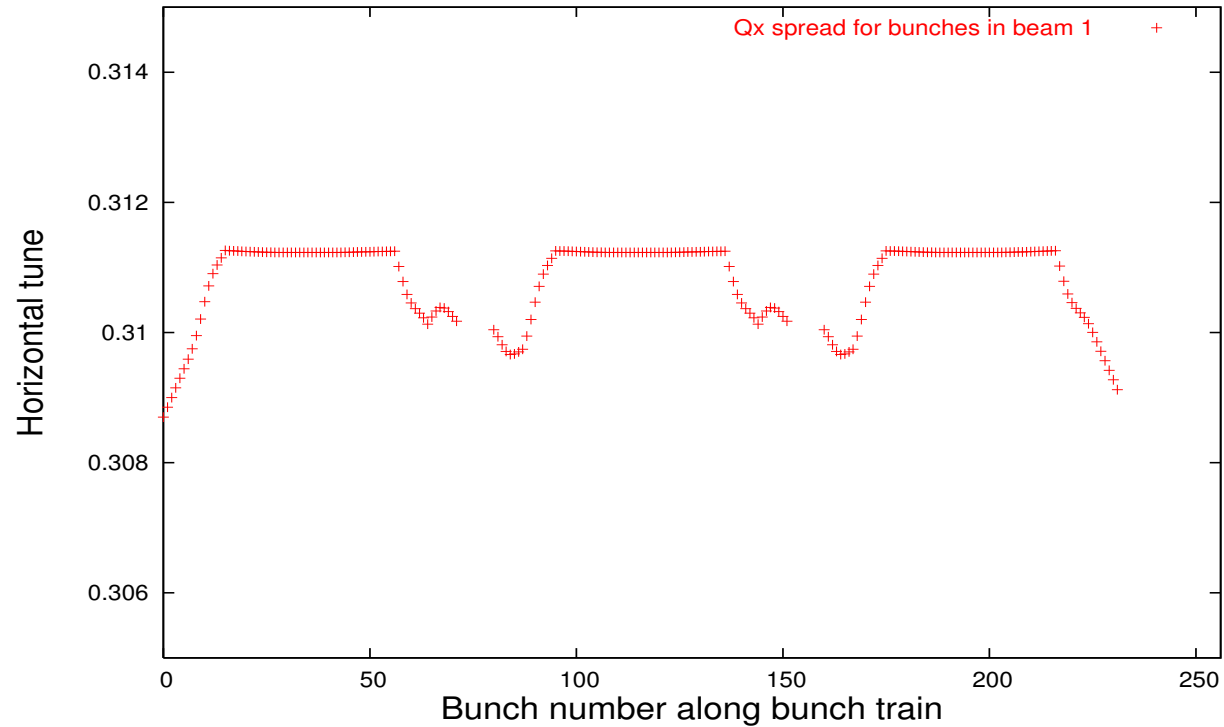
Orbit along LHC batches: **beam 1** and **beam 2**

Orbits along bunches



Tune along LHC batches

Tune along bunches



■ Spread is too large for safe operation

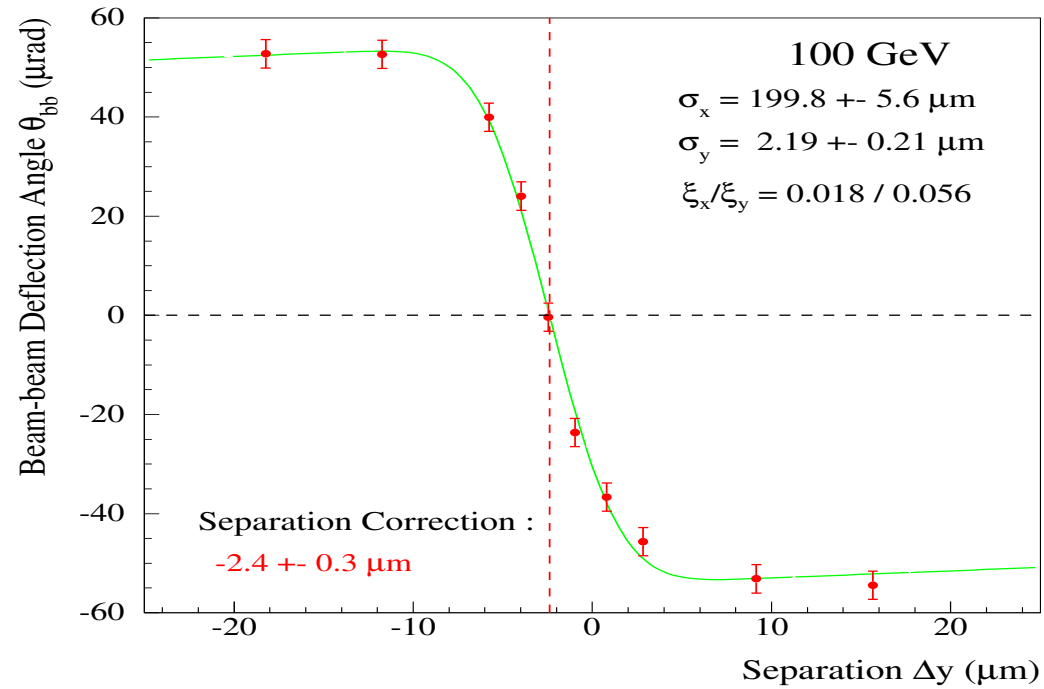


Beam-beam deflection scan

- The orbit effect can be useful when one has only a few bunches, i.e. not PACMAN effects
- Effect can be used to optimize luminosity
- Scanning two beams against each other
- Two beams get a orbit kick, depending on distance



Deflection scan (LEP measurement)



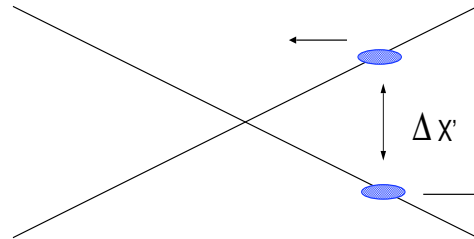
(Courtesy J. Wenniger)

Deflection scan

- Calculated kick from orbit follows the force function
- Allows to calculate parameters
- Allows to centre the beam
- Standard procedure at LEP



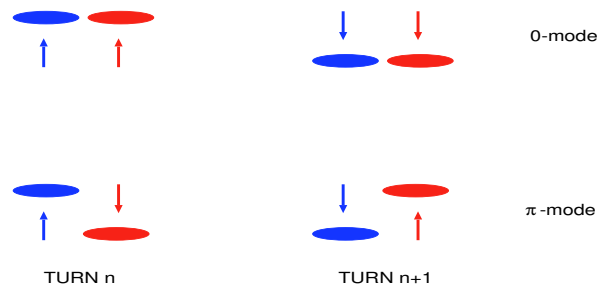
Coherent beam-beam effect



- Whole bunch sees a kick as an entity (coherent kick)
- The coherent kick of separated beams can excite coherent dipole oscillations
- All bunches couple together because each bunch "sees" many opposing bunches: many coherent modes possible !

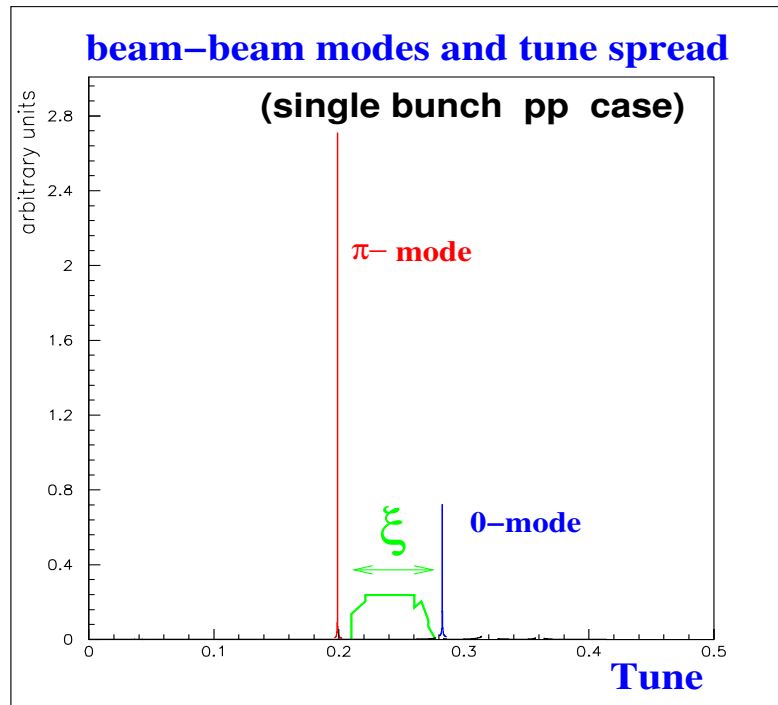
Coherent beam-beam effect

Simplest case: one bunch per beam:



- Coherent mode: two bunches are "locked" in a coherent oscillation
- 0-mode is stable (Mode with **NO** tune shift)
- π -mode can become unstable (Mode with **LARGEST** tune shift)

Coherent beam-beam frequencies (schematic)



▶ 0-mode is at unperturbed tune

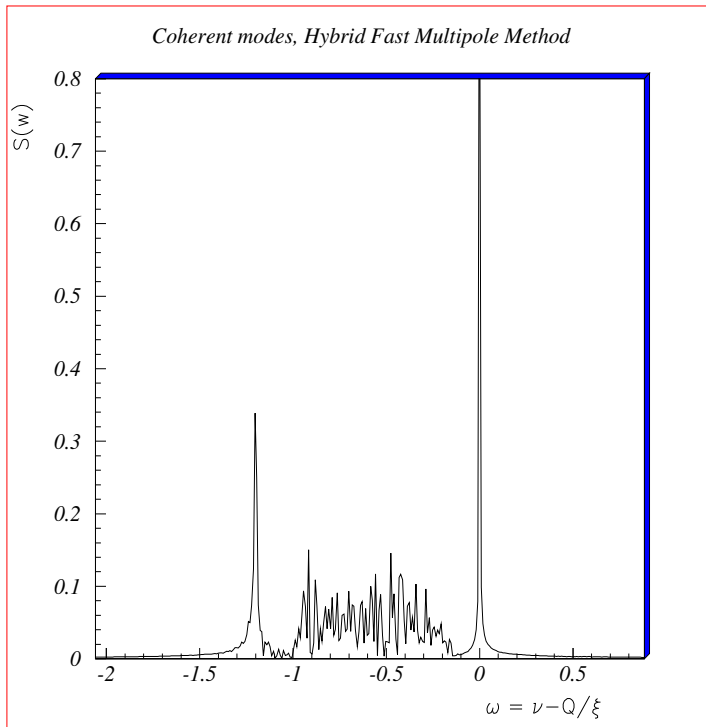
▶ π -mode is shifted by $1.1 - 1.3 \cdot \xi$

▶ Incoherent spread between $[0.0, 1.0] \cdot \xi$

➡ Strong-strong case: π -mode shifted outside tune spread

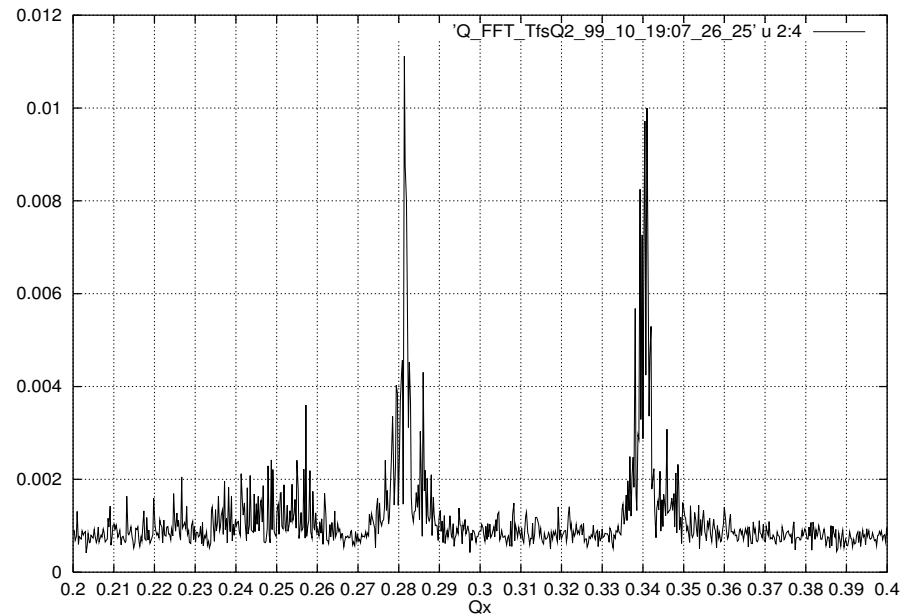
➡ No Landau damping possible

Simulation of coherent spectra



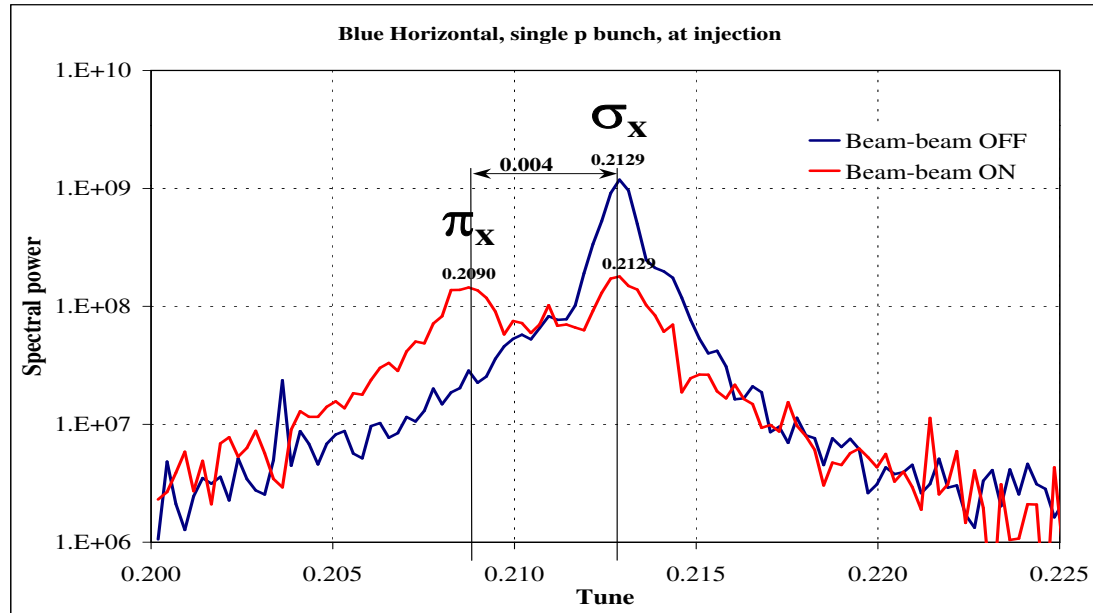
- ▶ Full simulation of both beams required
- ▶ Use up to 10^8 particles in simulations
- ▶ Must take into account changing fields
- ▶ Requires computation of arbitrary fields

What we measure: LEP



- Two modes clearly visible
- Can be distinguished by phase relation, i.e. sum and difference signals

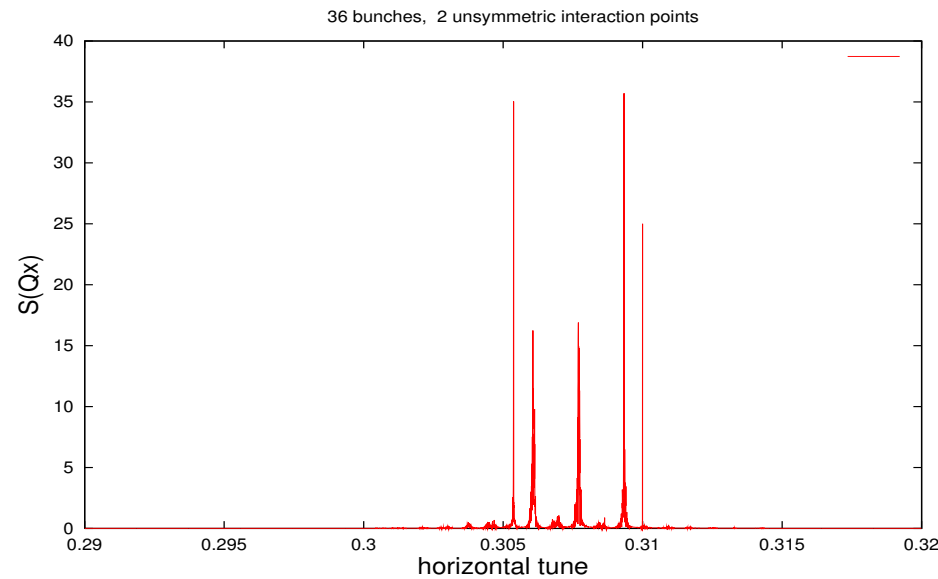
What we measure: RHIC



Courtesy W. Fischer (BNL)

- Compare spectra with and without beams : two modes visible with beams

Many bunches and more interaction points



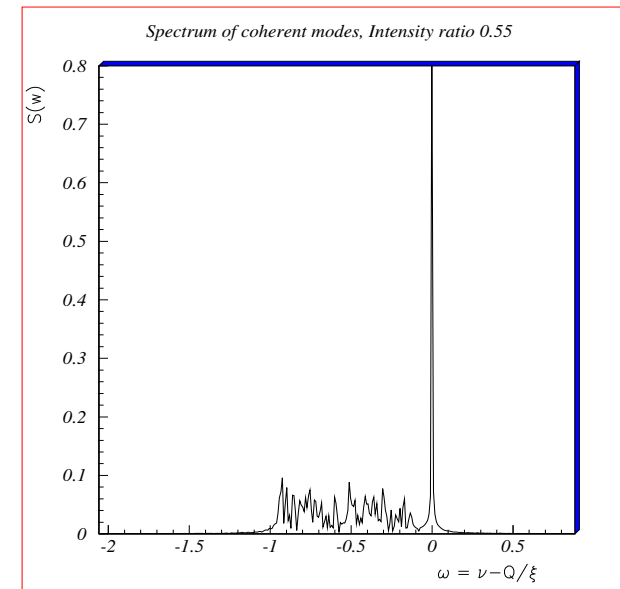
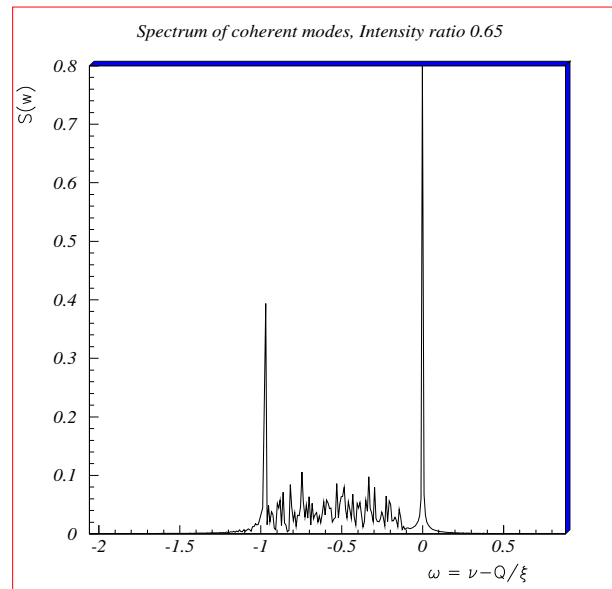
- Bunches couple via the beam-beam interaction
- Additional coherent modes become visible
- Potentially undesirable situation

What can be done to avoid problems ?

- Coherent motion requires 'organized' motion of many particles
- Therefore high degree of symmetry required
- Possible countermeasure: (symmetry breaking)
 - Different bunch intensity
 - Different tunes in the two beams

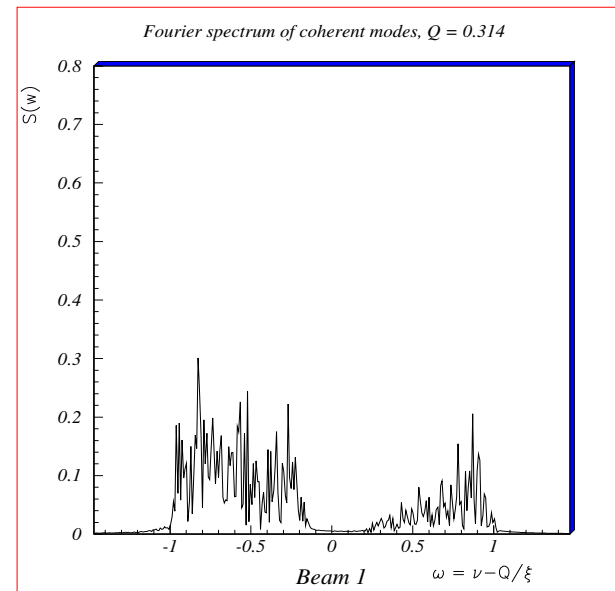
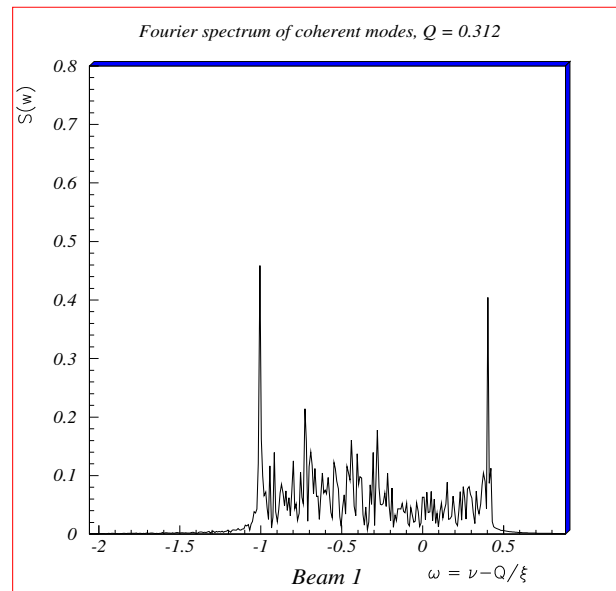


Beams with different intensity



→ Bunches with **different intensities** cannot maintain coherent motion

Beams with different tunes



→ Bunches with **different tunes** cannot maintain coherent motion

Can we suppress beam-beam effects ?

■ Find 'lenses' to correct beam-beam effects

● Head on effects:

- Linear "electron lens" to shift tunes
- Non-linear "electron lens" to reduce spread
- Tests in progress at FNAL

● Long range effects:

- At very large distance: force is $1/r$
- Same force as a wire !

■ So far: mixed success with **active** compensation

Others: Möbius lattice

■ Principle:

- Interchange horizontal and vertical plane each turn

■ Effects:

- Round beams (even for leptons)
- Some compensation effects for beam-beam interaction
- First test at CESR at Cornell



Not mentioned:

- Effects in linear colliders
- Asymmetric beams
- Coasting beams
- Beamstrahlung
- Synchrotron coupling
- Monochromatization
- Beam-beam experiments
- ... and many more



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