CERN Accelerator School

Chavannes de Bogis, Switzerland 8 November 2013

Beam-Beam Interactions

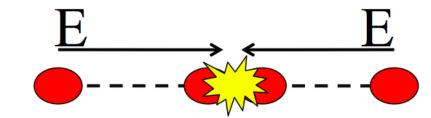
Tatiana Pieloni (BE-ABP-ICE)

Thanks to W. Herr



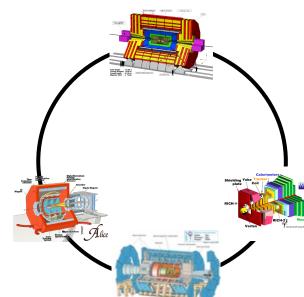
Hadron Circular Colliders

$$E^* \approx 2 \times E$$



$$N_{event/s} = L \cdot \sigma_{event}$$

$$L \propto \frac{N_p^2}{\sigma_x \sigma_y} \cdot n_b \cdot f_{rev}$$



Bunch intensity:

$$N_p = 1.15 - 1.65 \cdot 10^{11} \ ppb$$

Transverse Beam size:

$$\sigma_{x,y} = 16 - 30 \ \mu m$$

Number of bunches

$$1370 - 2808$$

Revolution frequency

When do we have beam-beam effects?

>They occur when two beams get closer and

collide

➤ Two types

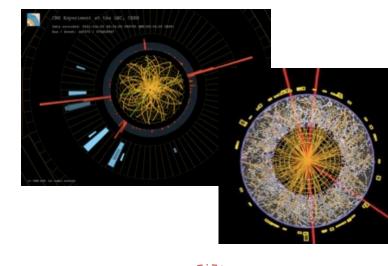
➤ High energy collisions between two particles (wanted)

➤ Distortions of beam by electromagnetic forces (unwanted)

➤ Unfortunately: usually both go together...

>0.001% (or less) of particles collide

> 99.999% (or more) of particles are distorted



 (X_2, Y_2)

 (X_1, Y_1)

Beam-beam effects: overview

- Circular Colliders: interaction occurs at every turn
 - Many effects and problems
 - Try to understand some of them

- Overview of effects (single particle and multi-particle effects)
- Qualitative and physical picture of effects
- Observations from the LHC
- Mathematical derivations and more info in References or at

Beam-beam webpage http://lhc-beam-beam.web.cern.ch/lhc-beam-beam/ And CAS Proceedings

References:

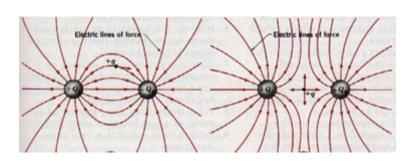
- [1] http://cern.ch/Werner.Herr/CAS2009/proceedings/bb_proc.pdf
- [2] V. Shiltsev et al, "Beam beam effects in the Tevatron", Phys. Rev. ST Accel. Beams 8, 101001 (2005)
- [3] Lyn Evans "The beam-beam interaction", CERN 84-15 (1984)
- [4] Alex Chao "Lie Algebra Techniques for Nonlinear Dynamics" SLAC-PUB-9574 (2002)
- [5] J. D. Jackson, "Classical Electrodynamics", John Wiley & Sons, NY, 1962.
- [6] H. Grote, F. Schmidt, L. H. A. Leunissen,"LHC Dynamic Aperture at Collision", LHC-Project-Note 197, (1999).
- [7] W. Herr,"Features and implications of different LHC crossing schemes", LHC-Project-Note 628, (2003).
- [8] A. Hofmann,"Beam-beam modes for two beams with unequal tunes", CERN-SL-99-039 (AP) (1999) p. 56.
- [9] Y. Alexahin, "On the Landau damping and decoherence of transverse dipole oscillations in colliding beams", Part. Acc. 59, 43 (1996).

...much more on the LHC Beam-beam webpage:

http://lhc-beam-beam.web.cern.ch/lhc-beam-beam/

Beams EM potential

- **▶** Beam is a collection of charges
- ➤ Beam is an electromagnetic potential for other charges



Force on itself (space charge) and opposing beam (beam-beam effects)

Single particle motion and whole bunch motion distorted

Focusing quadrupole Opposite Beam

A beam acts on particles like an electromagnetic lens, but...

Beam-beam Mathematics

General approach in electromagnetic problems Reference[5] already applied to beam-beam interactions in Reference[1,3, 4]

$$\Delta U = -\frac{1}{\epsilon_0} \rho(x, y, z)$$

Derive potential from Poisson equation for charges with distribution ρ

Solution of Poisson equation

$$U(x,y,z,\sigma_x,\sigma_y,\sigma_z) = \frac{1}{4\pi\epsilon_0} \int \int \int \frac{\rho(x_0,y_0,z_0) dx_0 dy_0 dz_0}{\sqrt{(x-x_0)^2 + (y-y_0)^2 + (z-z_0)^2)}}$$

$$\overrightarrow{E} = -\nabla U(x, y, z, \sigma_x, \sigma_y, \sigma_z)$$

Then compute the fields

$$\overrightarrow{F} = q(\overrightarrow{E} + \overrightarrow{v} \times \overrightarrow{B})$$

From Lorentz force one calculates the force acting on test particle with charge q

Making some assumptions we can simplify the problem and derive analytical formula for the force...

Round Gaussian distributions:

Gaussian distribution for charges:

Round beams:

Very relativistic, Force has only radial component:

$$\sigma_x = \sigma_y = \sigma$$

$$\beta \approx 1 \qquad r^2 = x^2 + y^2$$

$$F \propto \frac{N_p}{\sigma} \cdot \frac{1}{r} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

Beam-beam Force

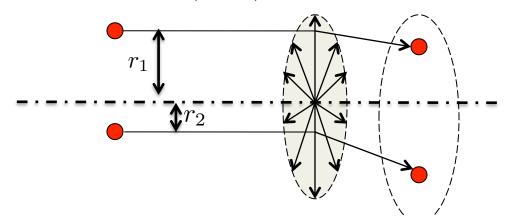
$$\Delta r' = \frac{1}{mc\beta\gamma} \int F_r(r, s, t) dt$$

$$\Delta r' = -\frac{N_p r_0}{r} \cdot \frac{r}{r^2} [1 - e^{-\frac{r^2}{2\sigma^2}}]$$

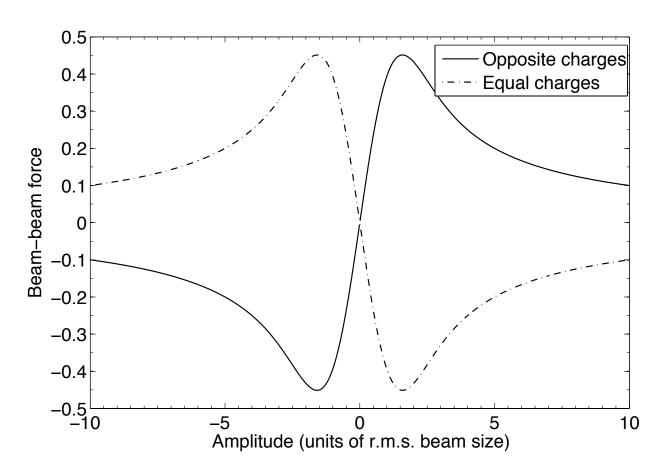
Beam-beam kick obtained integrating the force over the collision (i.e. time of passage)

Only radial component in relativistic case

How does this force looks like?



Beam-beam Force



$$F_r(r) = \pm \frac{ne^2(1+\beta_{rel}^2)}{2\pi\epsilon_0} \frac{1}{r} [1 - \exp(-\frac{r^2}{2\sigma^2})]$$

Why do we care?

Pushing for luminosity means stronger beam-beam effects

$$\mathcal{L} \propto rac{N_p^2}{\sigma_x \sigma_y} \cdot n_b$$

$$F \propto \frac{N_p}{\sigma} \cdot \frac{1}{r} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}} \right]$$

Physics fill lasts for many hours 10h – 24h

Strongest non-linearity in a collider YOU CANNOT AVOID!



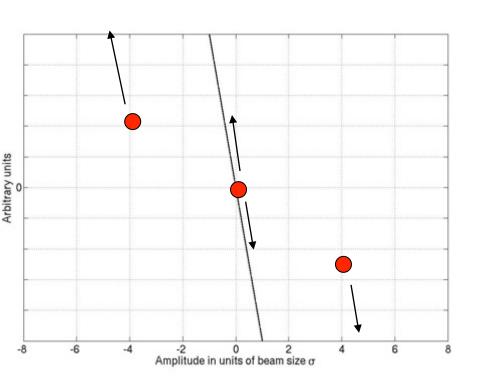
Two main questions:

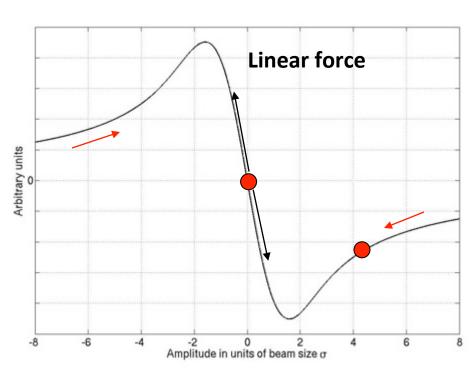
What happens to a single particle? What happens to the whole beam?

Beam-Beam Force: single particle...

Lattice defocusing quadrupole

Beam-beam force





$$F = -k \cdot r$$

$$F \propto \frac{N_p}{\sigma} \cdot \frac{1}{r} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}}\right]$$

For small amplitudes: linear force

For large amplitude: very non-linear

The beam will act as a strong non-linear electromagnetic lens!

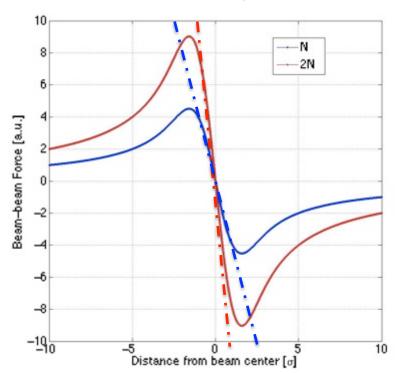
Can we quantify the beam-beam strenght?

Quantifies the strength of the force but does NOT reflect the nonlinear nature of the force

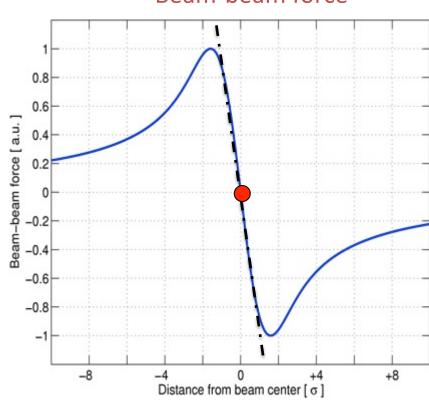
For small amplitudes: linear force

$$F \propto -\xi \cdot r$$

The slope of the force gives you the beam-beam parameter \mathcal{E}



Beam-beam force



$$\Delta r' = -\frac{N_p r_0}{r} \cdot \frac{r}{r^2} \cdot \left[1 - e^{-\frac{r^2}{2\sigma^2}}\right]$$

$$\Delta r' = \frac{2N_p r_0}{\gamma} \cdot \frac{1}{r} \cdot \left[1 - \left(1 - \frac{r^2}{2\sigma^2} + \dots \right) \right]$$

Colliders:

For round beams:

$$\xi = \frac{\beta^*}{4\pi} \cdot \frac{\delta(\Delta r')}{\delta r} = \frac{Nr_0\beta^*}{4\pi\gamma\sigma^2}$$

For non-round beams:

$$\xi_{x,y} = \frac{Nr_0 \beta_{x,y}^*}{2\pi \gamma \sigma_{x,y} (\sigma_x + \sigma_y)}$$

Examples:

Parameters	LHC nominal	LHC 2012	
Intensity N _{p,e} /bunch	1.15 10 ¹¹	1.6 10 ¹¹	
Energy GeV	7000	4000	
Beam emittance	3.75 μmrad	2.2-2.5 μmrad	
Crossing angle (μrad)	285	290	
$\beta_{x,y}^*$ (m)	1.25-0.05	0.60-0.60	
Luminosity	1 10 ³⁴	7.6 10 ³³	
ξ _{bb}	0.0034	0.006	

Linear Tune shift

For small amplitudes beam-beam can be approximated as linear force as a quadrupole

$$F \propto -\xi \cdot r$$

Focal length:

$$\frac{1}{f} = \frac{\Delta x'}{x} = \frac{Nr_0}{\gamma \sigma^2} = \frac{\xi \cdot 4\pi}{\beta^*}$$

Beam-beam matrix:

$$\begin{pmatrix} 1 & 0 \\ -\frac{\xi \cdot 4\pi}{\beta^*} & 1 \end{pmatrix}$$

Perturbed one turn matrix with perturbed tune $\triangle Q$ and beta function at the IP β^* :

$$\begin{pmatrix} cos(2\pi(Q + \Delta Q)) & \beta^* sin(2\pi(Q + \Delta Q)) \\ -\frac{1}{\beta^*} sin(2\pi(Q + \Delta Q)) & cos(2\pi(Q + \Delta Q)) \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 \\ -\frac{1}{2f} & 1 \end{pmatrix} \cdot \begin{pmatrix} \cos(2\pi Q) & \beta_0^* \sin(2\pi Q) \\ -\frac{1}{\beta_0^*} \sin(2\pi Q) & \cos(2\pi Q) \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 \\ -\frac{1}{2f} & 1 \end{pmatrix}$$

Linear tune

Solving the one turn matrix one can derive the tune shift ΔQ and the perturbed beta function at the IP β^* :

Tune is changed

$$\cos(2\pi(Q + \Delta Q)) = \cos(2\pi Q) - \frac{\beta_0^* \cdot 4\pi \xi}{\beta^*} \sin(2\pi Q)$$

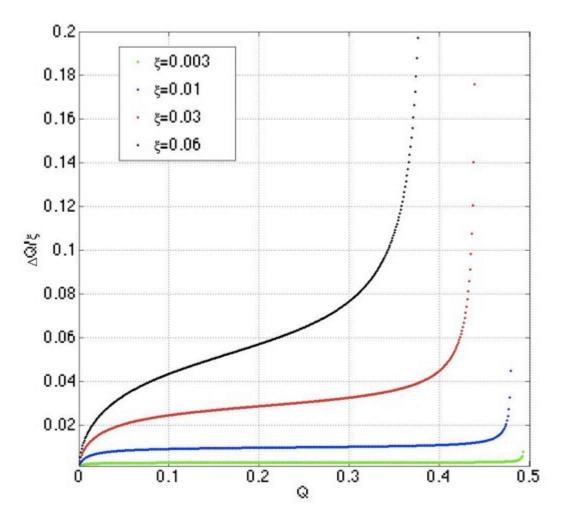
β -function is changed:

$$\frac{\beta^*}{\beta_0^*} = \frac{\sin(2\pi Q)}{\sin(2\pi(Q + \Delta Q))}$$

...how do they change?

Tune dependence of tune shift and dynamic beta

Tune shift as a function of tune



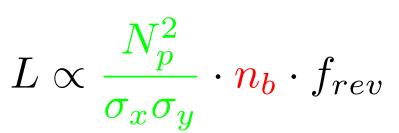
Larger ξ

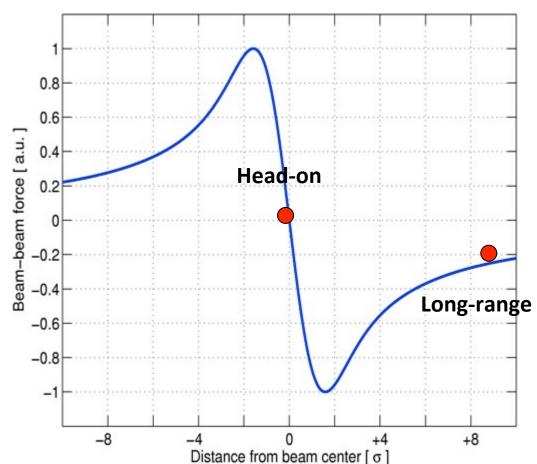


Strongest variation with Q

Head-on and Long-range interactions

Beam-beam force



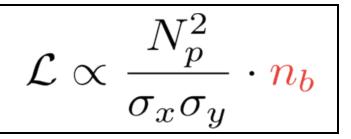


Other beam passing in the center force: **HEAD-ON** beam-beam interaction

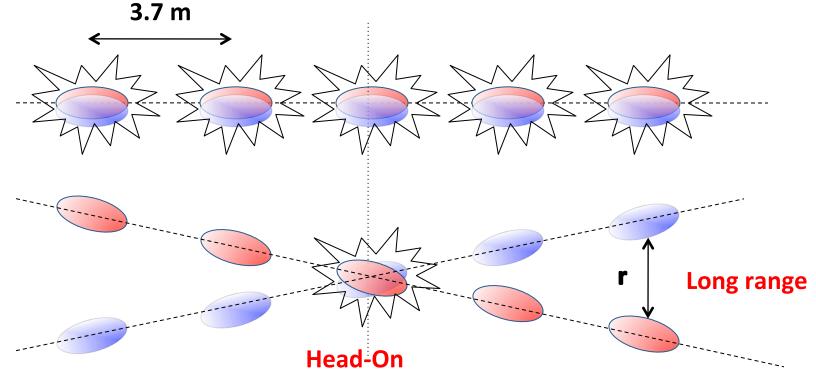
Other beam passing at an offset of the force: LONG-RANGE beam-beam interaction

Multiple bunch Complications

MANY INTERACTIONS



Num. of bunches : $n_b=2808$

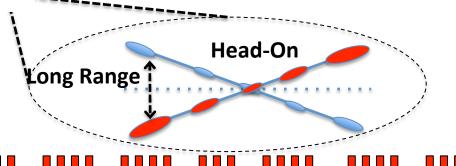


For 25ns case 124 BBIs per turn: 4 HO and 120 LR

LHC, KEKB... colliders



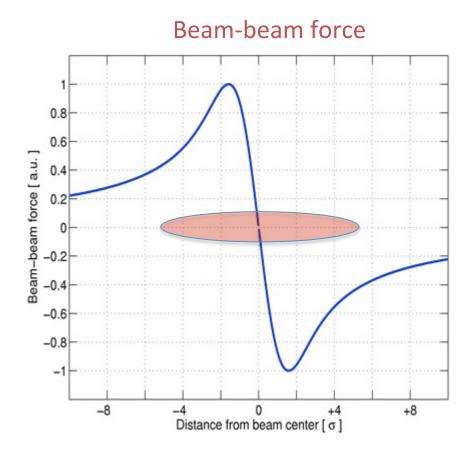
 High number of bunches in train structures



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	SppS	Tevatron	RHIC	LHC
Number Bunches	6	36	109	2808
LR interactions	9	70	0	120/40
Head-on interactions	3	2	2	4

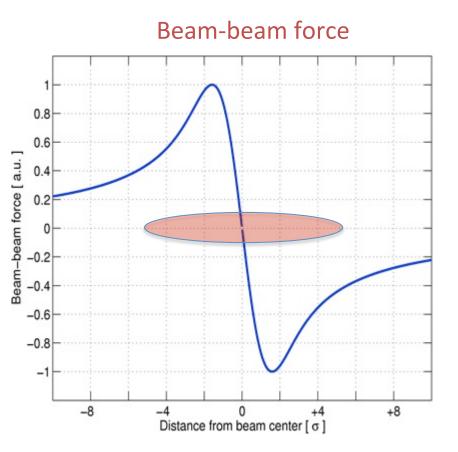
A beam is a collection of particles



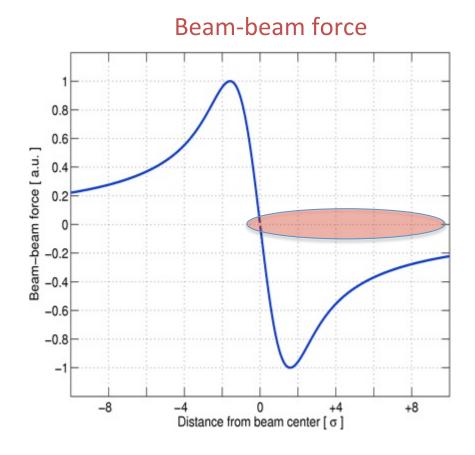
Beam 2 passing in the center of force produce by Beam 1
Particles of Beam 2 will experience different ranges of the beam-beam forces

Tune shift as a function of amplitude (detuning with amplitude or tune spread)

A beam will experience all the force range



Second beam passing in the center **HEAD-ON** beam-beam interaction

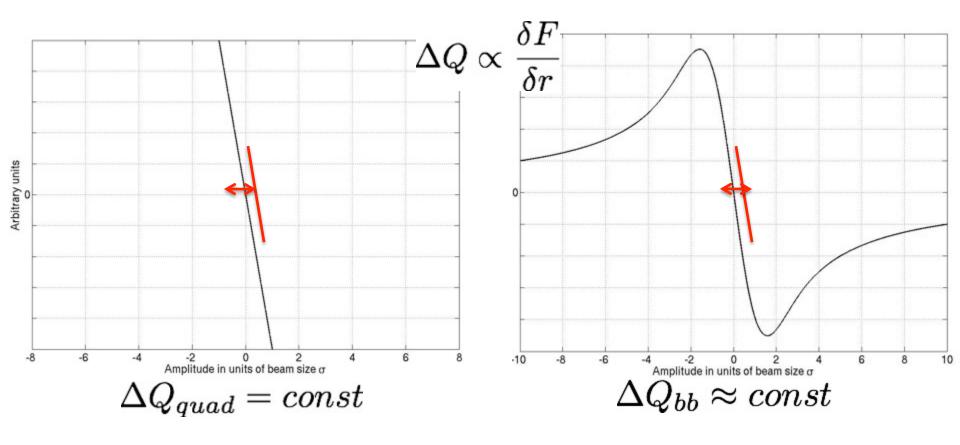


Second beam displaced offset LONG-RANGE beam-beam interaction

Different particles will see different force

Detuning with Amplitude for head-on

Instantaneous tune shift of test particle when it crosses the other beam is related to the derivative of the force with respect to the amplitude

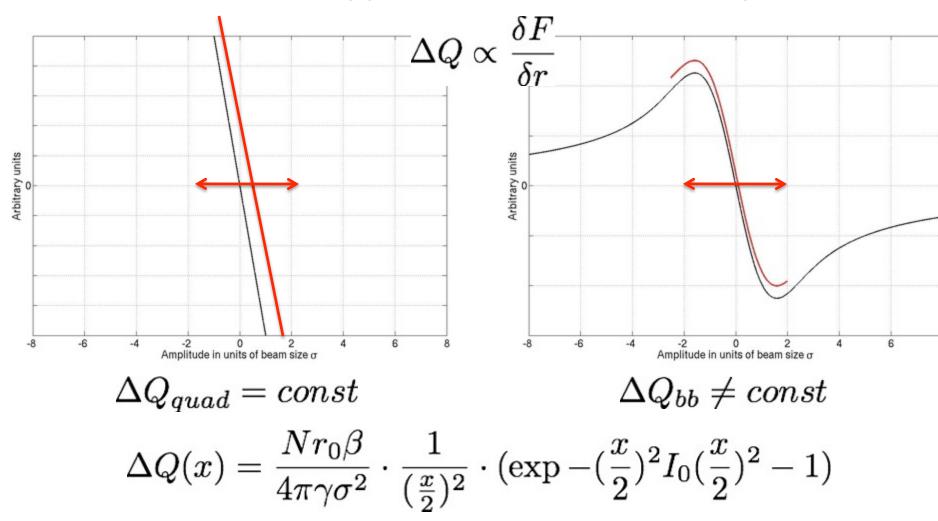


For small amplitude test particle linear tune shift

$$\lim_{r\to 0} \Delta Q(r) = -\frac{Nr_0\beta^*}{4\pi\gamma\sigma^2} = \xi$$

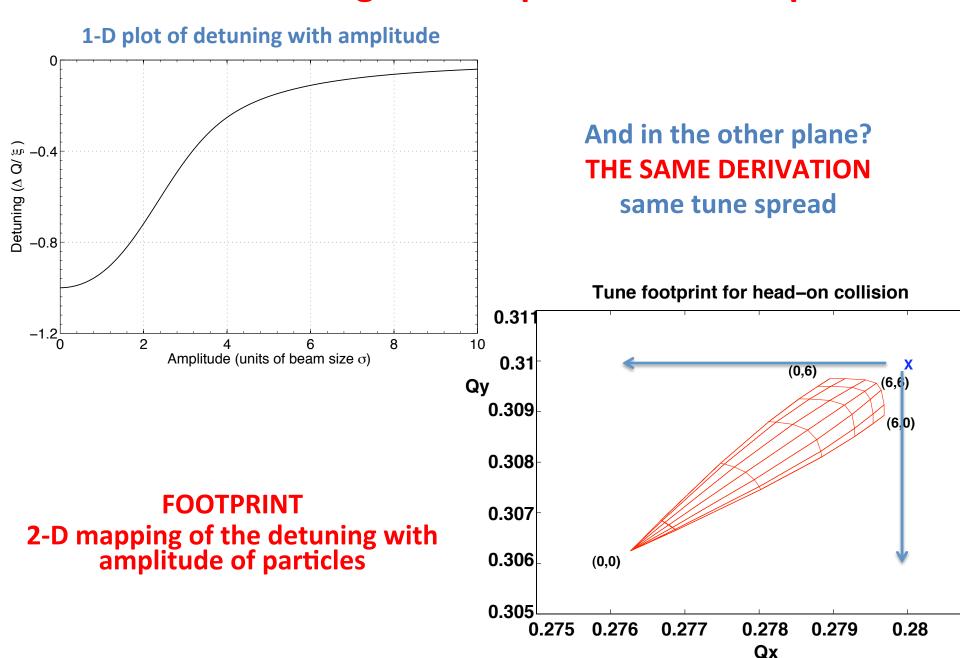
Detuning with Amplitude for head-on

Beam with many particles this results in a tune spread

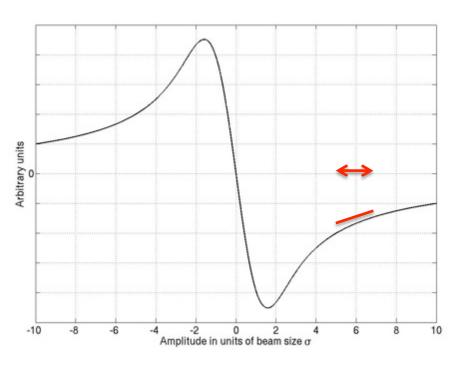


Mathematical derivation in Ref [3] using Hamiltonian formalism and in Ref [4] using Lie Algebra

Head-on detuning with amplitude and footprints



And for long-range interactions?

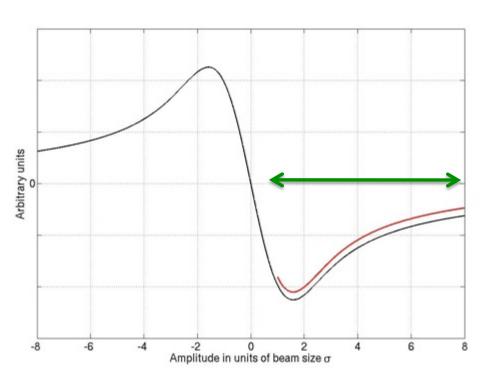


Second beam centered at d (i.e. 6σ)

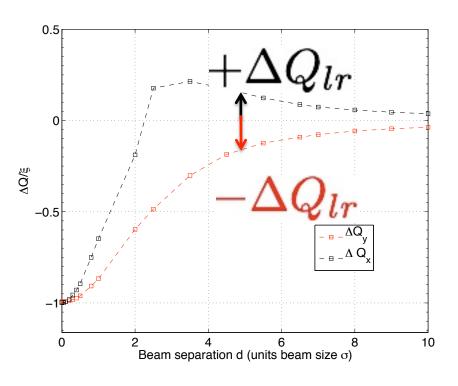
- •Small amplitude particles positive tune shifts
- Large amplitude can go to negative tune shifts

Long range tune shift scaling for distances $d>6\sigma$

$$\Delta Q_{lr} \propto -rac{N}{d^2}$$



Long-range footprints

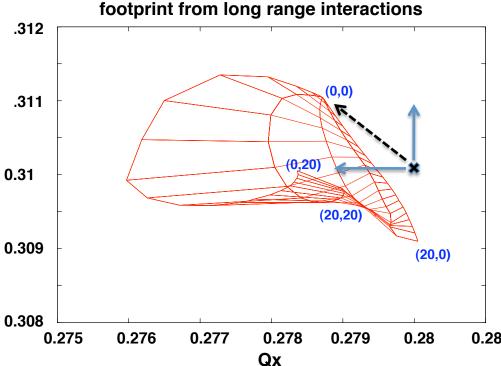


The picture is more complicated now the LARGE amplitude particles see the second beam and have larger tune shift

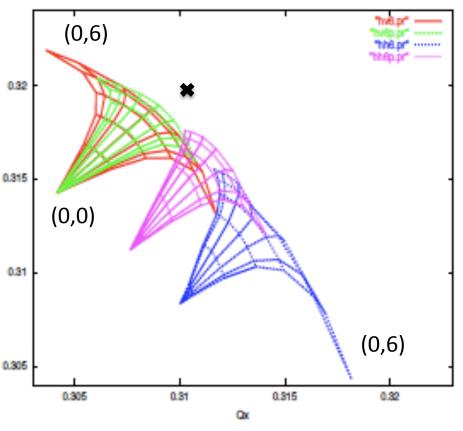
Separation in vertical plane!
And in horizontal plane?

The test particle is centered with the opposite beam

tune spread more like for head-on at large amplitudes



Beam-beam tune shift and spread



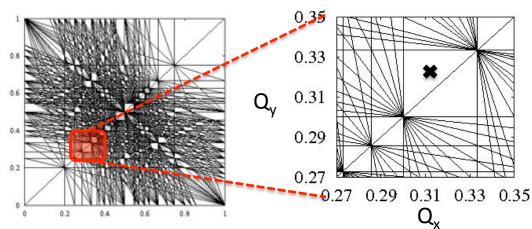
Footprints depend on:

- number of interactions
- Type (Head-on and long-range)
- Plane of interaction

When long-range effects become important footprint wings appear and alternating crossing important

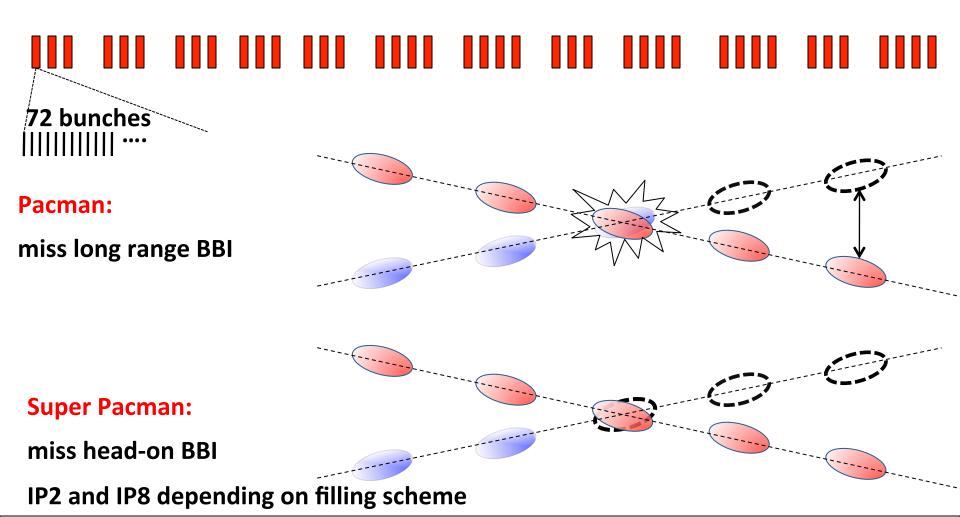
Aim to reduce the area as much as possible!

Passive compensation of tune shift Ref[7]



Complications

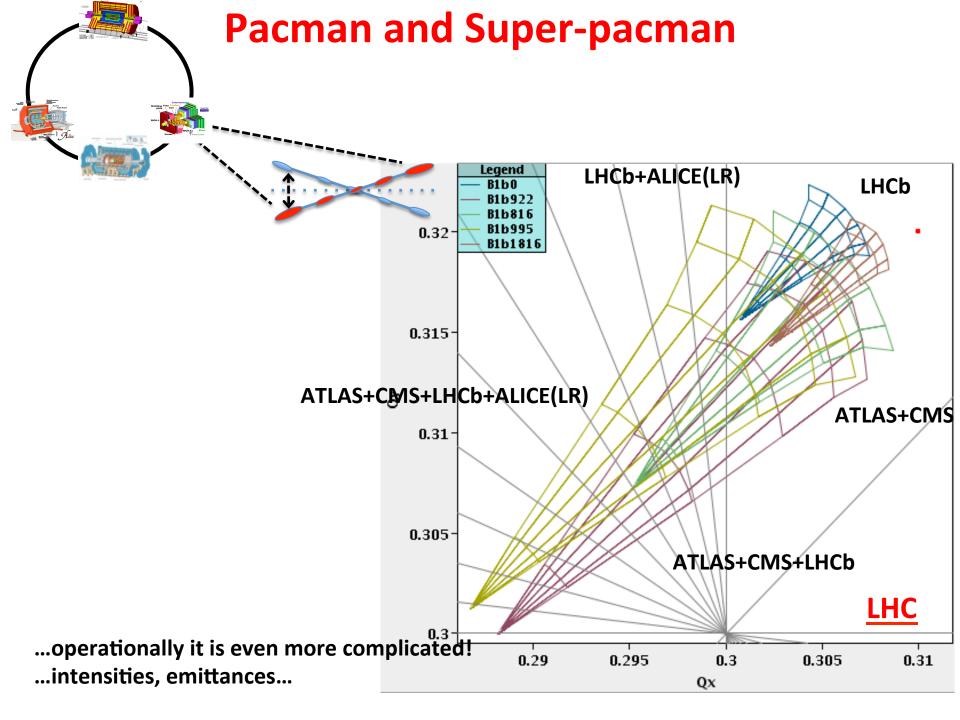
PACMAN and **SUPER PACMAN** bunches



Different bunch families: Pacman and Super Pacman

LHC Complications: filling schemes 72 bunches **SPS** extraction kicker PS extraction kicker **Abort Gap** Long-range Encounters IP1&IP5 **Nominal Bunches** 20 RF Bucket (ns)

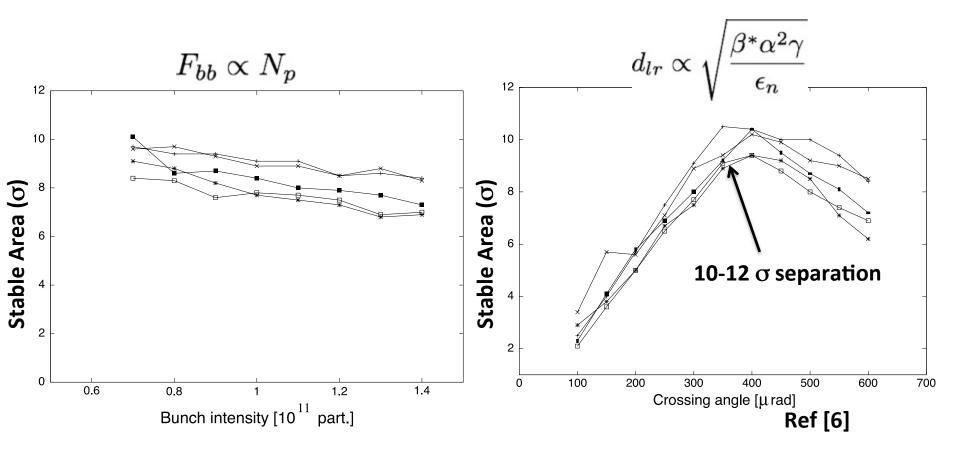
Pacman Bunche: different number of long-range interactions



Particle Losses

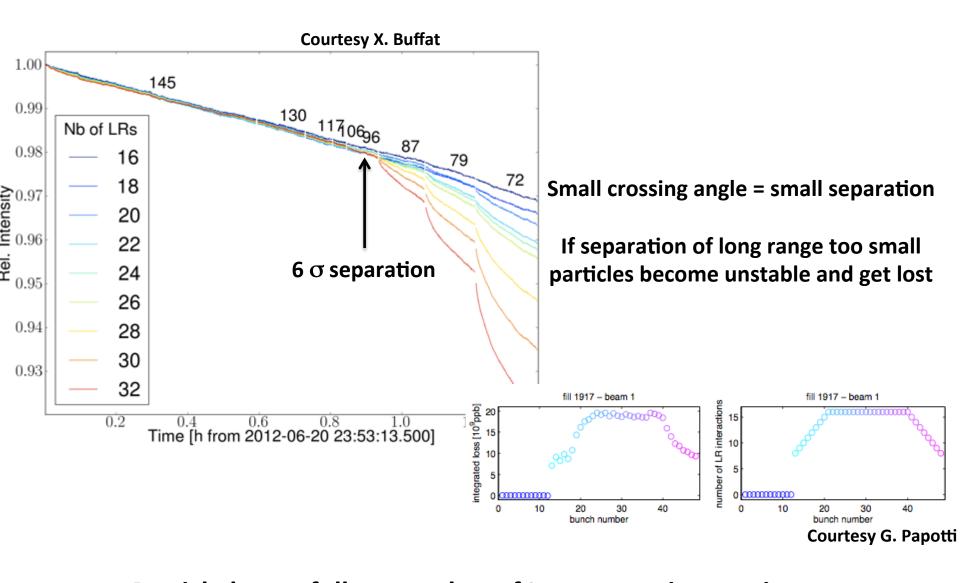
Dynamic Aperture: area in amplitude space with stable motion

Stable area of particles depends on beam intensity and crossing angle



Stable area depends on beam-beam interactions therefore the choice of running parameters (crossing angles, β^* , intensity) is the result of careful study of different effects!

DO we see the effects of LR in the LHC?



Particle losses follow number of Long range interactions

Nominal LHC will have twice the number of interactions

Long-range BB and Orbit Effects

Long Range Beam-beam interactions lead to orbit effects

Long range kick
$$\Delta x'(x+d,y,r) = -\frac{2Nr_0}{\gamma} \frac{(x+d)}{r^2} [1-\exp{(-\frac{r^2}{2\sigma^2})}]$$

For well separated beams

$$d \gg \sigma$$

The force has an amplitude independent contribution: ORBIT KICK

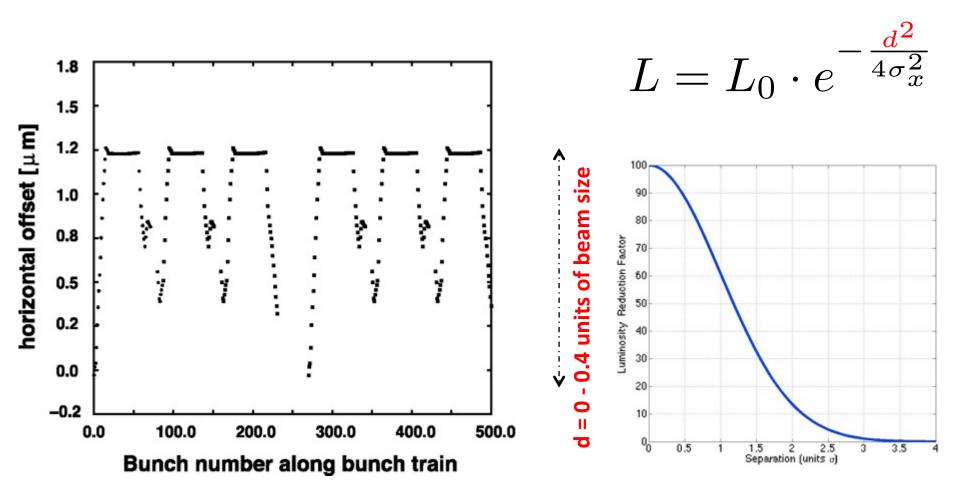
$$\Delta x' = \frac{const}{d} \left[1 - \frac{x}{d} + O(\frac{x^2}{d^2}) + \dots \right]$$

$$\Delta x'$$

Orbit can be corrected but we should remember PACMAN effects

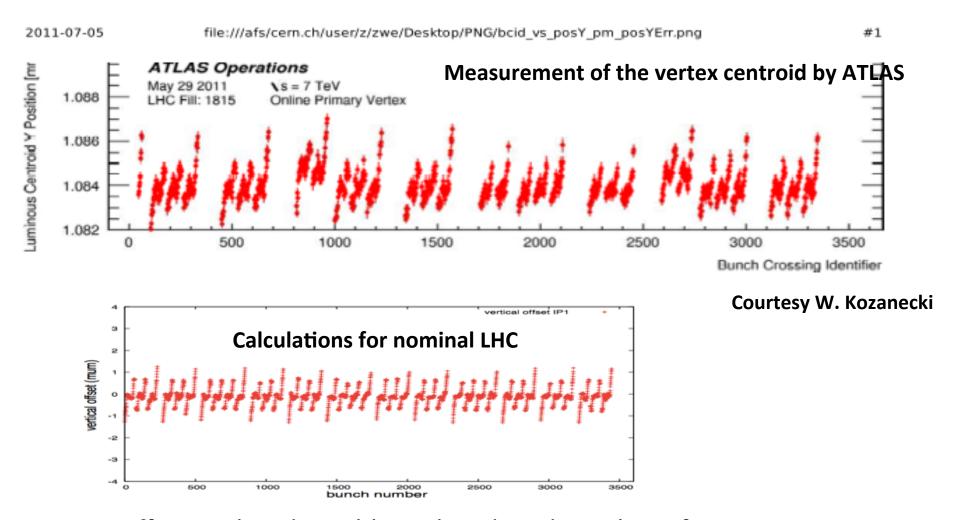
LHC orbit effects

Orbit effects different due to Pacman effects and the many long-range add up giving a non negligible effect



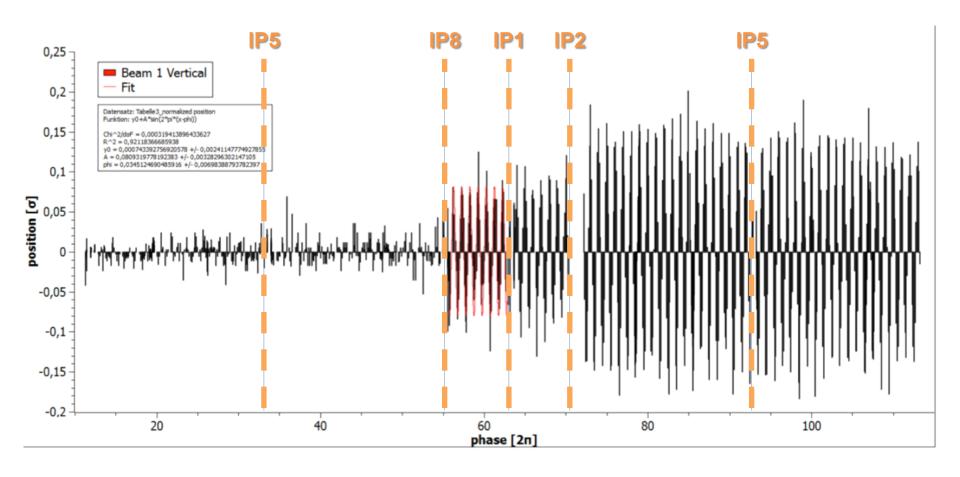
Long range orbit effect

Long range interactions leads to orbit offsets at the experiment a direct consequence is deterioration of the luminosity



Effect is already visible with reduced number of interactions

Long range orbit effect observations:



Courtesy T. Baer

Vertical oscillation starts when one beam is ejected and dumped

Coherent dipolar beam-beam modes

Coherent beam-beam effects arise from the forces which an exciting bunch exerts on a whole test bunch during collision

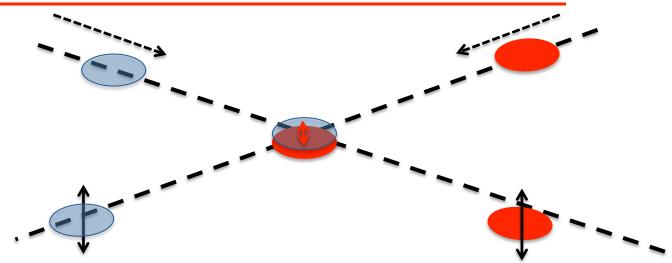
We study the collective behaviour of all particles of a bunch

Coherent motion requires an organized behaviour of all particles of the bunch

Coherent beam-beam force

- •Beam distributions Ψ_1 and Ψ_2 mutually changed by interaction
- Interaction depends on distributions
 - •Beam 1 Ψ_1 solution depends on beam 2 Ψ_2
 - •Beam 2 Ψ_2 solution depends on beam 1 Ψ_1
- Need a self-consistent solution

Coherent beam-beam effects



- Whole bunch sees a kick as an entity (coherent kick)
- Coherent kick seen by full bunch different from single particle kick
- •Requires integration of individual kick over particle distribution

$$\Delta r' = -\frac{N_p r_0}{r} \cdot \frac{r}{r^2} \cdot \left[1 - e^{-\frac{r^2}{4\sigma^2}}\right]$$

- •Coherent kick of separated beams can excite coherent dipolar oscillations
- •All bunches couple because each bunch "sees" many opposing bunches(LR): many coherent modes possible!

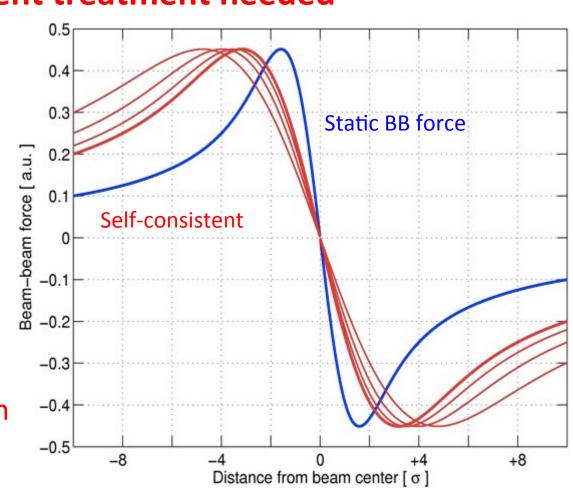
Coherent effects Self-consistent treatment needed

Perturbative methods

static source of distortion: example magnet

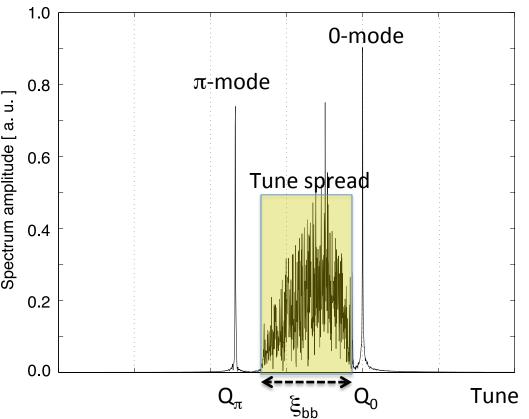
Self-consistent method

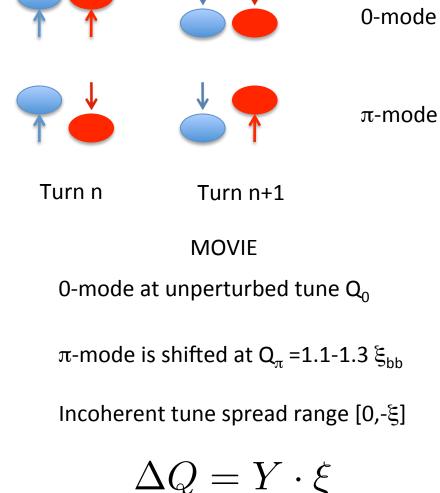
source of distortion changes as a result of the distortion



For a complete understanding of BB effect a self-consistent treatment should be used

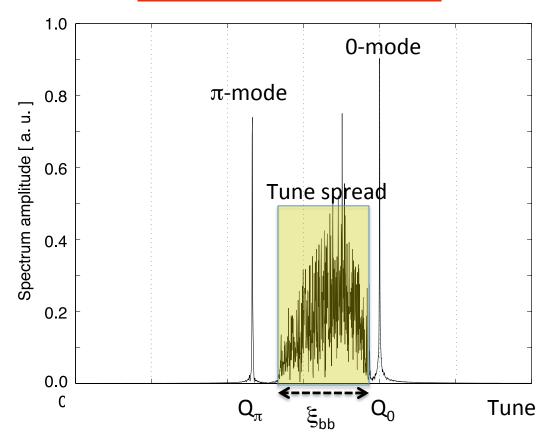
Simple case: one bunch per beam





- Coherent mode: two bunches are "locked" in a coherent oscillation
- 0-mode is stable (mode with NO tune shift)
- π -mode can become unstable (mode with largest tune shift)

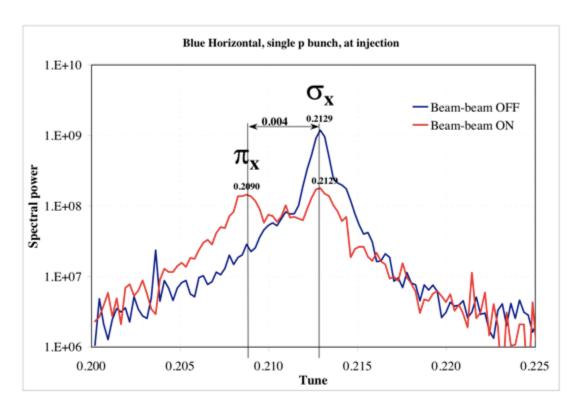
Simple case: one bunch per beam and Landau damping



Incoherent tune spread is the Landau damping region any mode with frequency laying in this range should not develop

• π -mode has frequency out of tune spread (Y) so it is not damped!

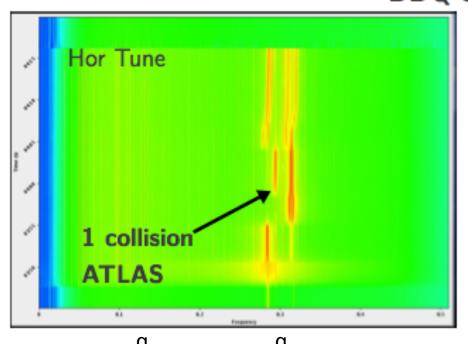
Coherent modes at RHIC

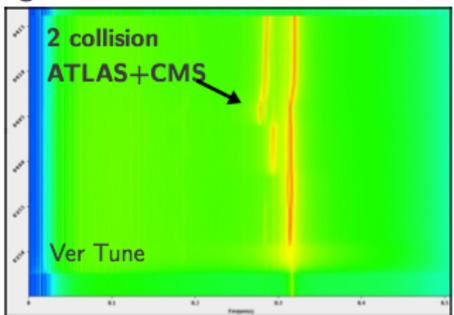


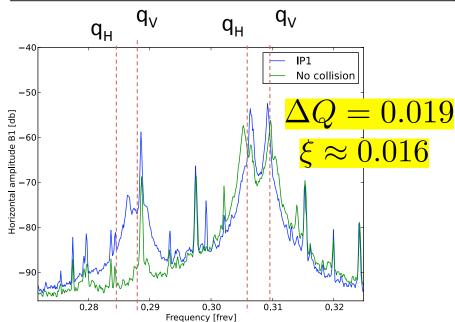
Courtesy W. Fischer (BNL)

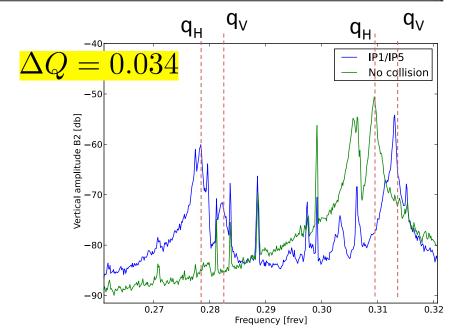
Tune spectra before collision and in collision two modes visible

Head-on beam-beam coherent mode: LHC BBQ Signals

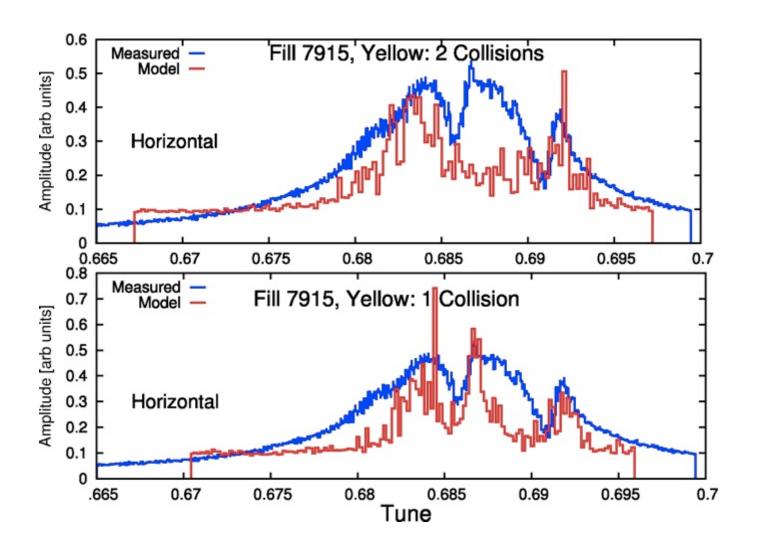






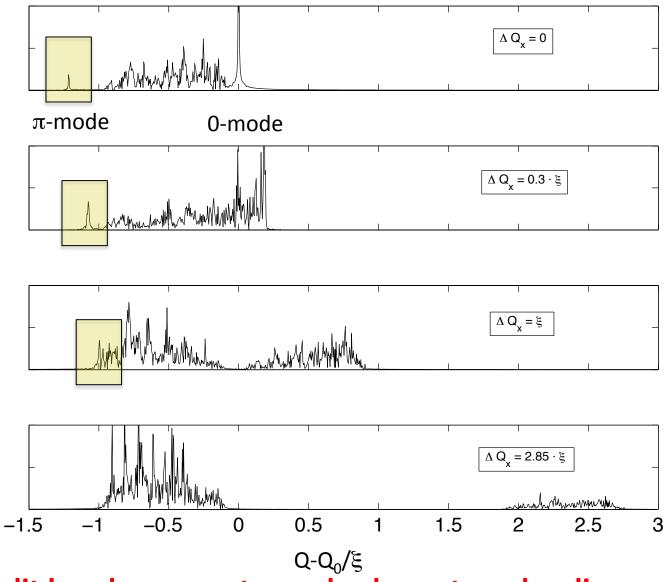


Beam-beam coherent modes and Landau Damping



Pacman effect on coherent modes Single bunch diagnostic so important

Different Tunes

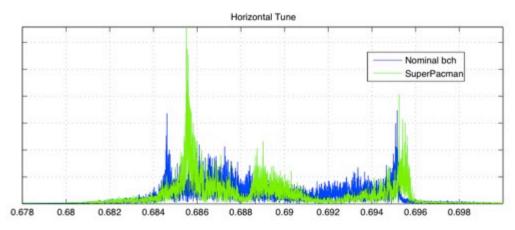


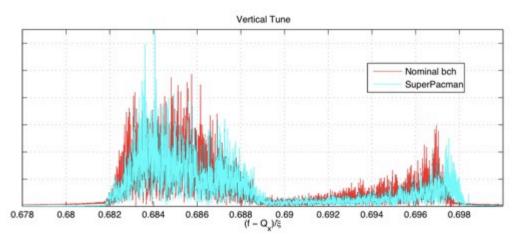
Tune split breaks symmetry and coherent modes disappear

Analytical calculations in Reference [8]

Different tunes or intensities

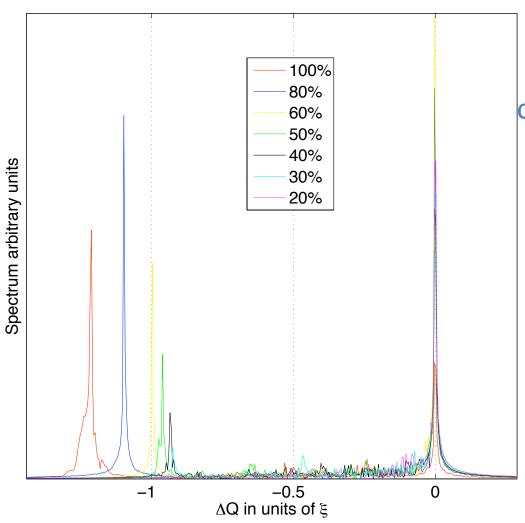
RHIC running with mirrored tune for years to break coherent oscillations





LHC has used a tune split to suppress coherent BB modes 2010 Physics Run

Different bunch intensities



For two bunches colliding head-on in one IP the coherent mode disappears if intensity ratio between bunches is 55% Reference[9]

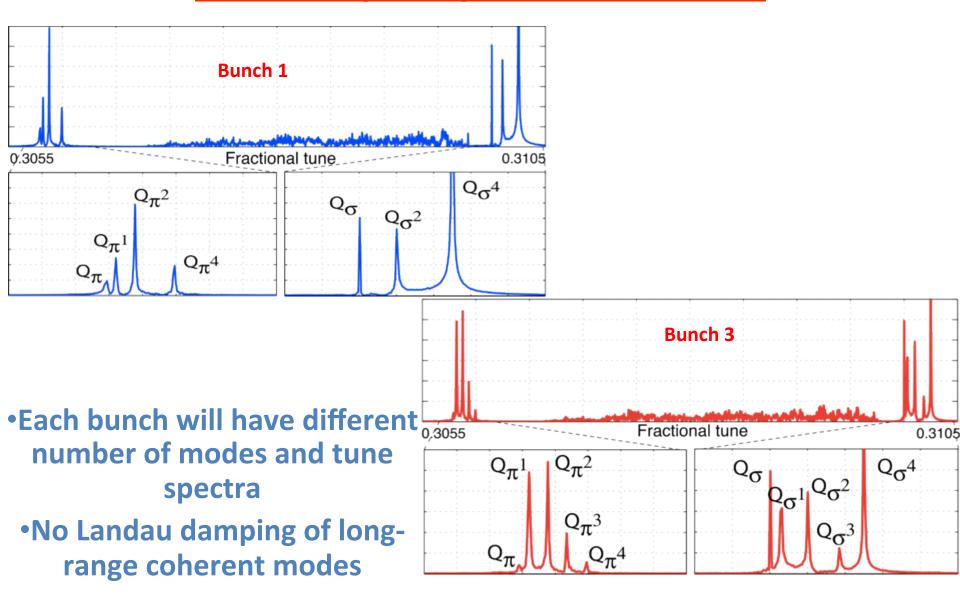
We assumed:

- equal emittances
- equal tunes
- NO PACMAN effects

(bunches will have different tunes)

For coherent modes the key is to break the simmetry in your coupled system...(tunes, intensities, collision patters...)

And Long range interactions?

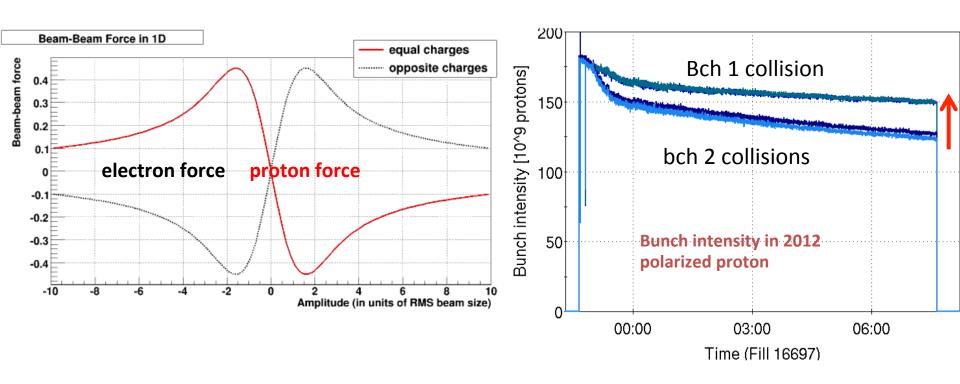


Single bunch diagnostic can make the difference

Beam-beam compensations:

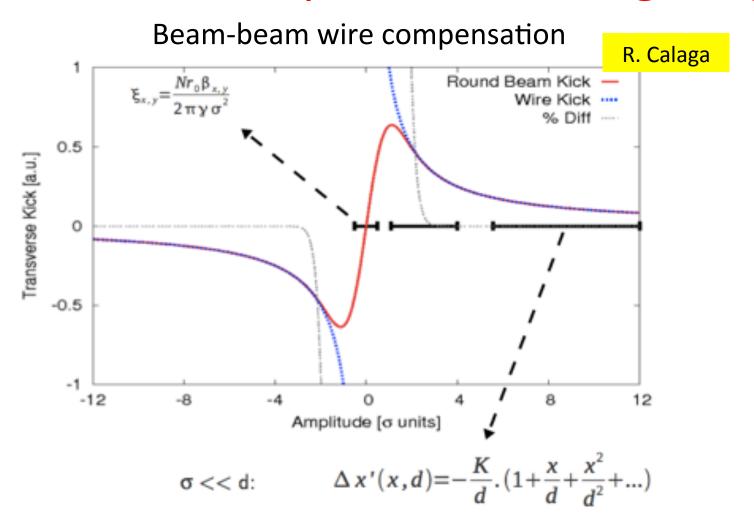
Head-on

- Linear e-lens, suppress shift
- Non-linear e-lens, suppress tune spread



- Past experience: at Tevatron linear and non-linear e-lenses, also hollow...
- Present: test for half compensation at RHIC with non-linear e-lens

Beam-beam compensations: long-range



- Past experience: at RHIC several tests till 2009...
- Present: simulation studies on-going for possible use in HL-LHC...

...not covered here...

- Linear colliders special issues
- Asymmetric beams effects
- Coasting beams
- Beamstrahlung
- Synchrobetatron coupling
- Beam-beam experiments
- Beam-beam and impedance

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Thank You!