Injection and extraction

- Introductory slides:
 - Kickers, septa and normalised phase-space
- Injection methods
 - Single-turn hadron injection
 - Injection errors, filamentation and blow-up
 - Multi-turn hadron injection
 - Charge-exchange H- injection
 - Lepton injection
- Extraction methods
 - Single-turn (fast) extraction
 - Non-resonant and resonant multi-turn (fast) extraction
 - Resonant multi-turn (slow) extraction

Matthew Fraser, CERN (TE-ABT-BTP) based on lectures by Brennan Goddard

Injection and extraction

ALICE

TI2

n (neutrons)

- An accelerator has limited dynamic range
- Chain of stages needed to reach high energy
- Periodic re-filling of storage rings, like LHC
- External facilities and experiments:

p (protons)

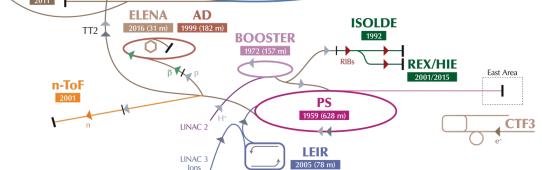
ions

 e.g. ISOLDE, HIRADMAT, AWAKE...

Beam transfer (into, out of, and between machines) is necessary.

RIBs (Radioactive Ion Beams)

CERN Accelerator Complex CMS LHC North Area 2008 (27 km) LHCb TT20 TT40 TT41 **SPS** 1976 (7 km) TI8 **AWAKE** TT10 ATLAS 2016 **HiRadMat** TT60 2011



+++- proton/antiproton conversion

LHC Large Hadron Collider SPS Super Proton Synchrotron PS Proton Synchrotron AD Antiproton Decelerator CTF3 Clic Test Facility

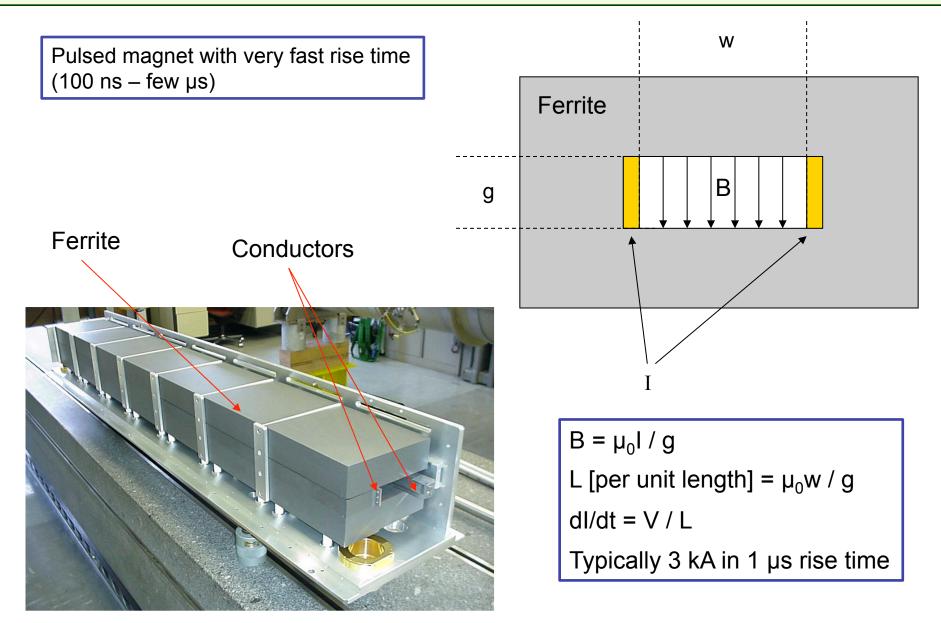
p (antiprotons)

AWAKE Advanced WAKefield Experiment ISOLDE Isotope Separator OnLine REX/HIE Radioactive EXperiment/High Intensity and Energy ISOLDE

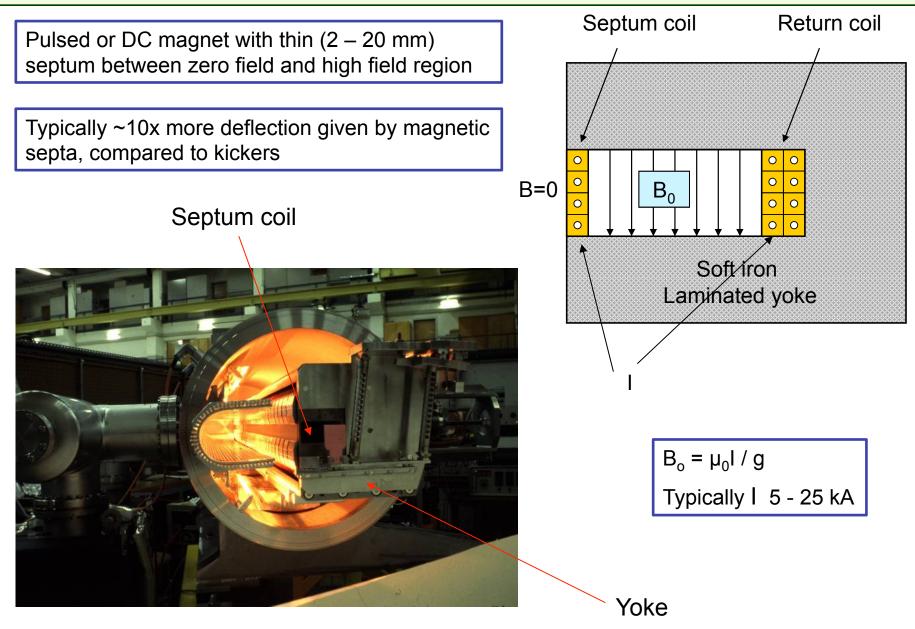
• e⁻ (electrons)

LEIR Low Energy Ion Ring LINAC LINear ACcelerator n-ToF Neutrons Time Of Flight HiRadMat High-Radiation to Materials

Kicker magnet

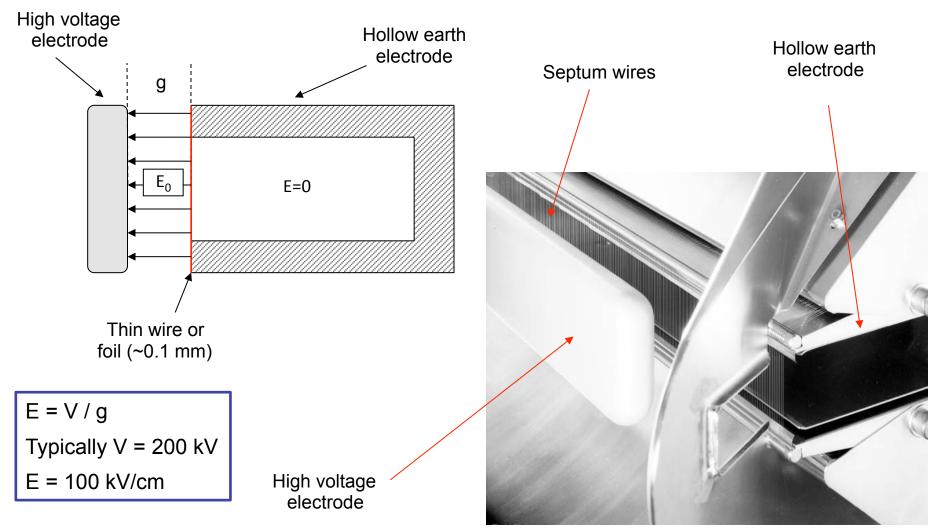


Magnetic septum



Electrostatic septum

DC electrostatic device with very thin septum between zero field and high field region



Normalised phase space

• Transform real transverse coordinates (*x*, *x'*, *s*) to normalised co-ordinates (\bar{X}, \bar{X}', μ) where the independent variable becomes the phase advance μ :

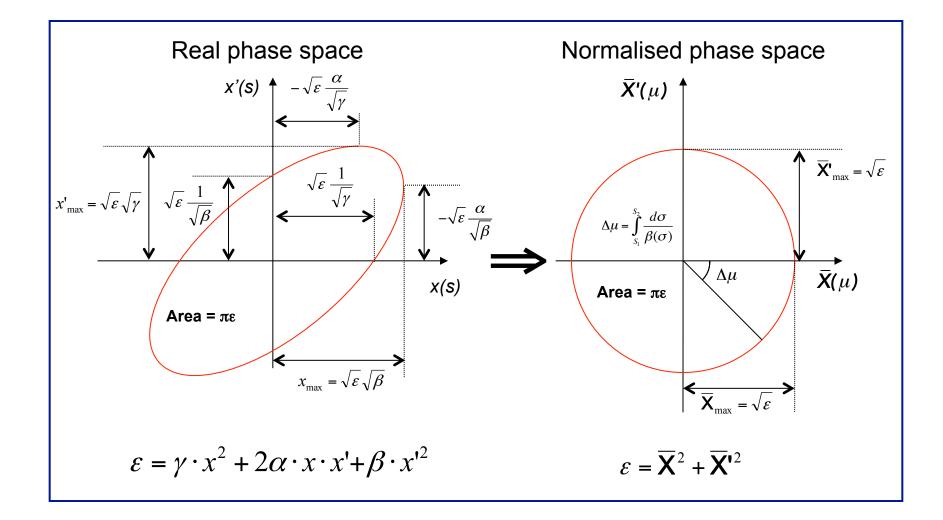
$$\begin{bmatrix} \bar{\mathbf{X}} \\ \bar{\mathbf{X}'} \end{bmatrix} = \mathbf{N} \cdot \begin{bmatrix} x \\ x' \end{bmatrix} = \sqrt{\frac{1}{\beta(s)}} \cdot \begin{bmatrix} 1 & 0 \\ \alpha(s) & \beta(s) \end{bmatrix} \cdot \begin{bmatrix} x \\ x' \end{bmatrix}$$

$$x(s) = \sqrt{\varepsilon} \sqrt{\beta(s)} \cos[\mu(s) + \mu_0]$$

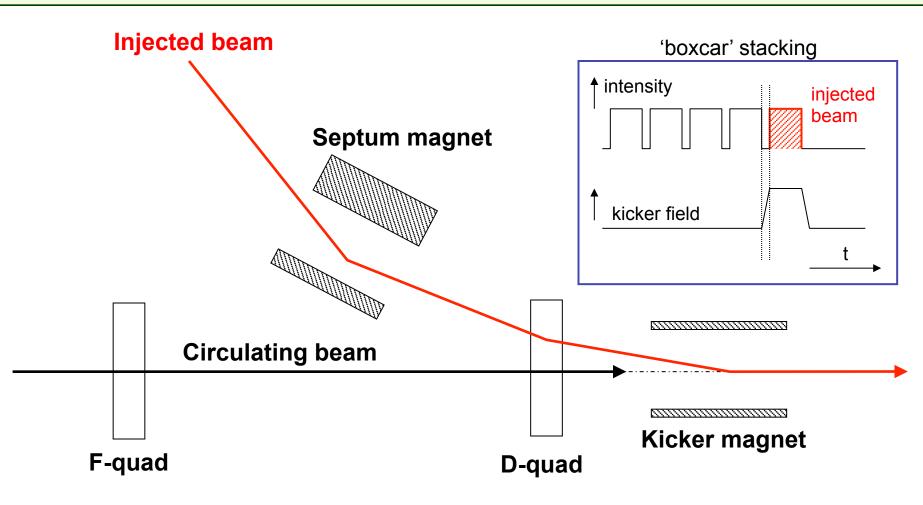
$$\mu(s) = \int_{0}^{s} \frac{d\sigma}{\beta(\sigma)}$$

$$\bar{\mathbf{X}}(\mu) = \sqrt{\frac{1}{\beta(s)}} \cdot x = \sqrt{\varepsilon} \cos[\mu + \mu_0]$$
$$\bar{\mathbf{X}}'(\mu) = \sqrt{\frac{1}{\beta(s)}} \cdot \alpha(s)x + \sqrt{\beta(s)}x' = -\sqrt{\varepsilon} \sin[\mu + \mu_0] = \frac{d\bar{\mathbf{X}}}{d\mu}$$

Normalised phase space

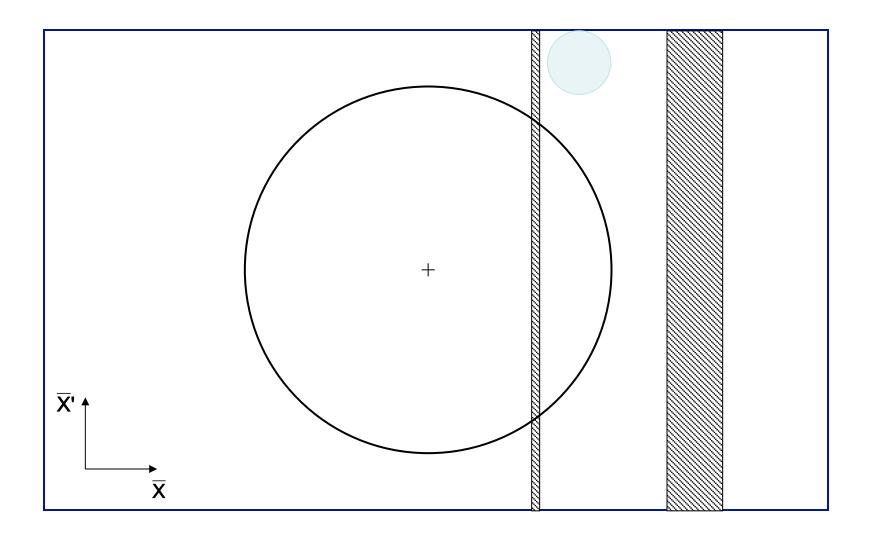


Single-turn injection – same plane

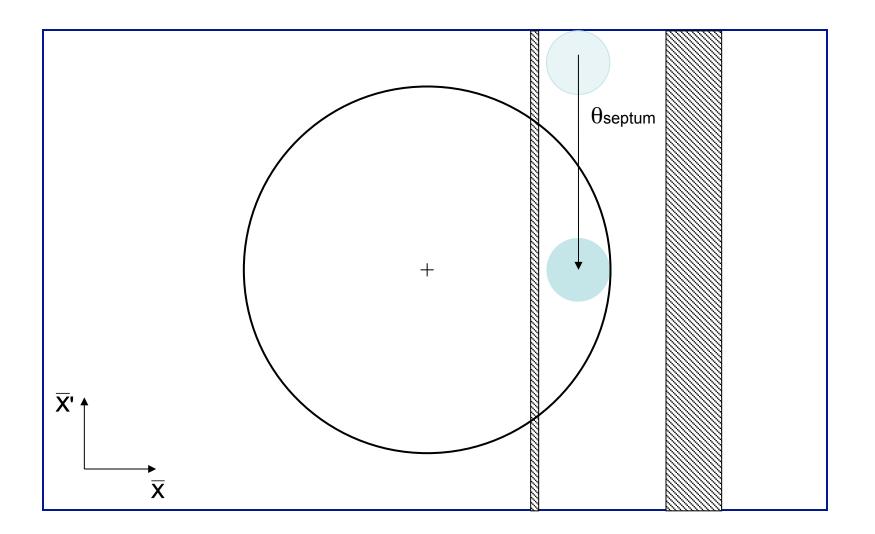


- Septum deflects the beam onto the closed orbit at the centre of the kicker
- Kicker compensates for the remaining angle
- Septum and kicker either side of D quad to minimise kicker strength

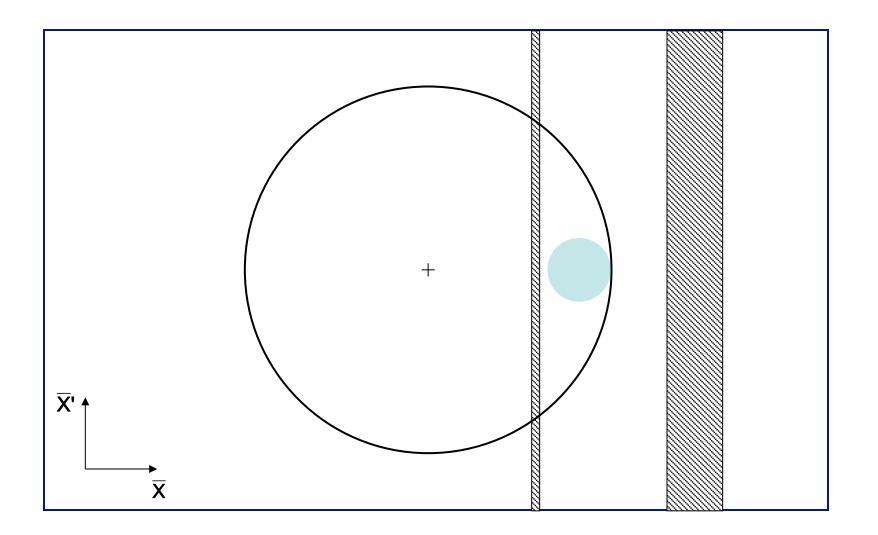
Normalised phase space at centre of idealised septum



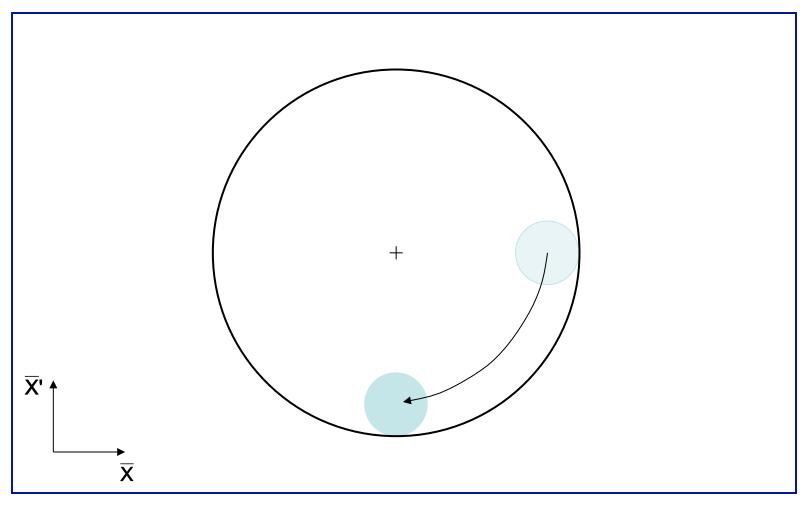
Normalised phase space at centre of idealised septum



Normalised phase space at centre of idealised septum

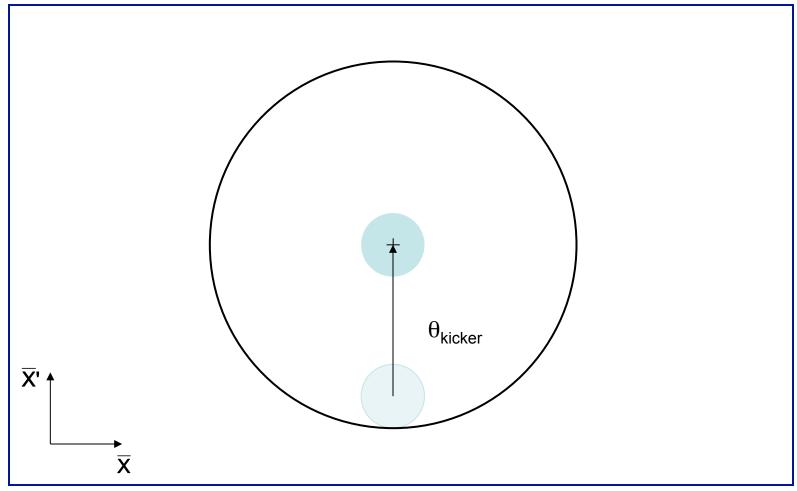


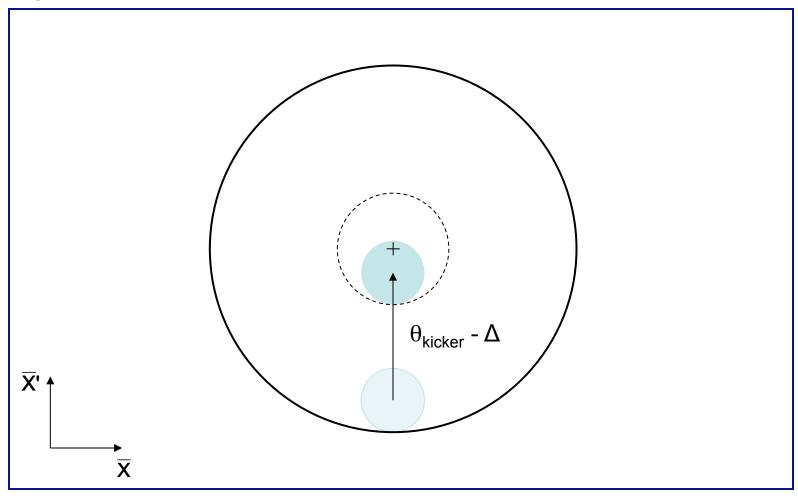
 $\mu/2$ phase advance to kicker location

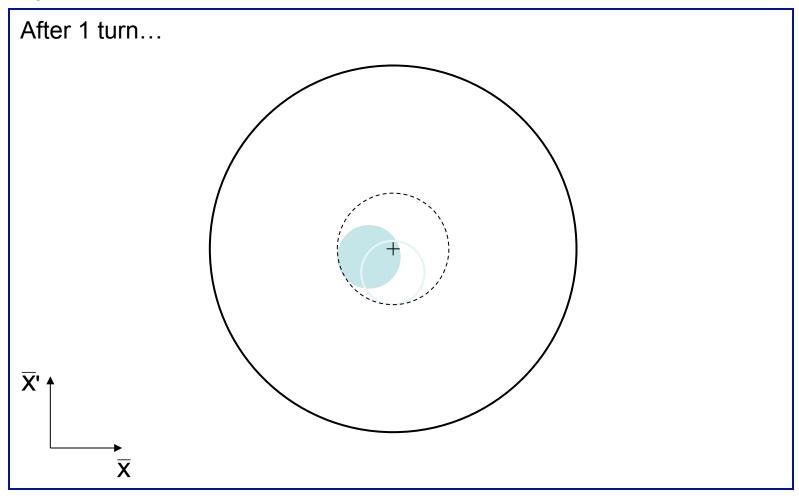


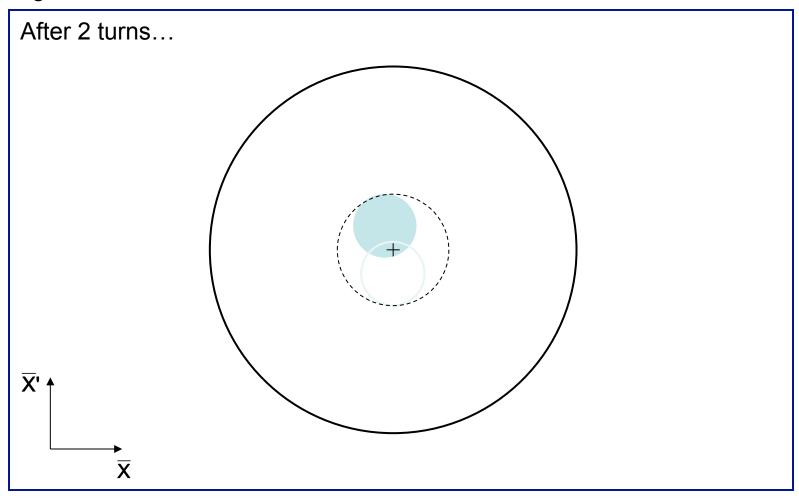
Normalised phase space at centre of idealised kicker

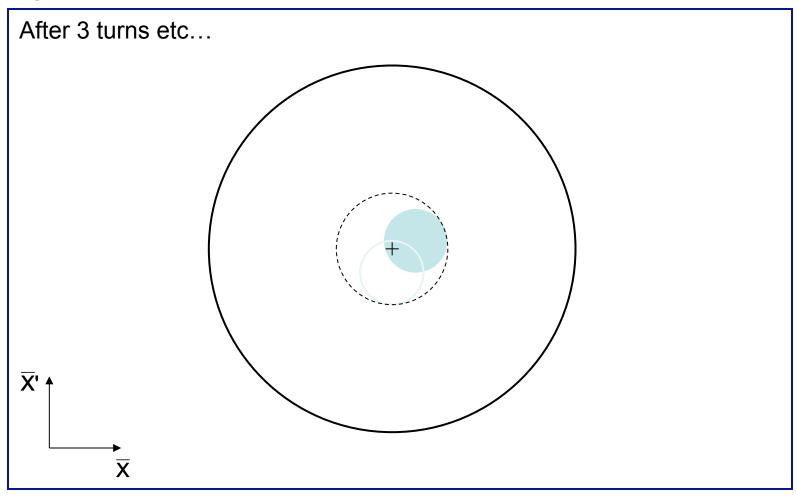
Kicker deflection places beam on central orbit:







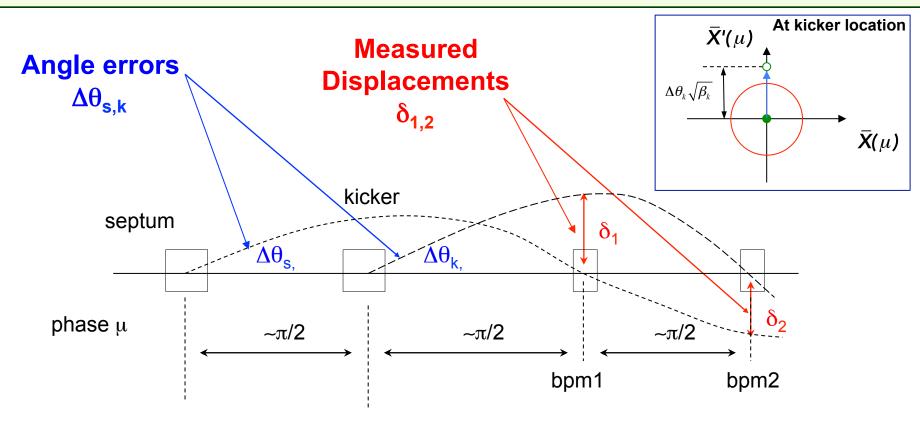




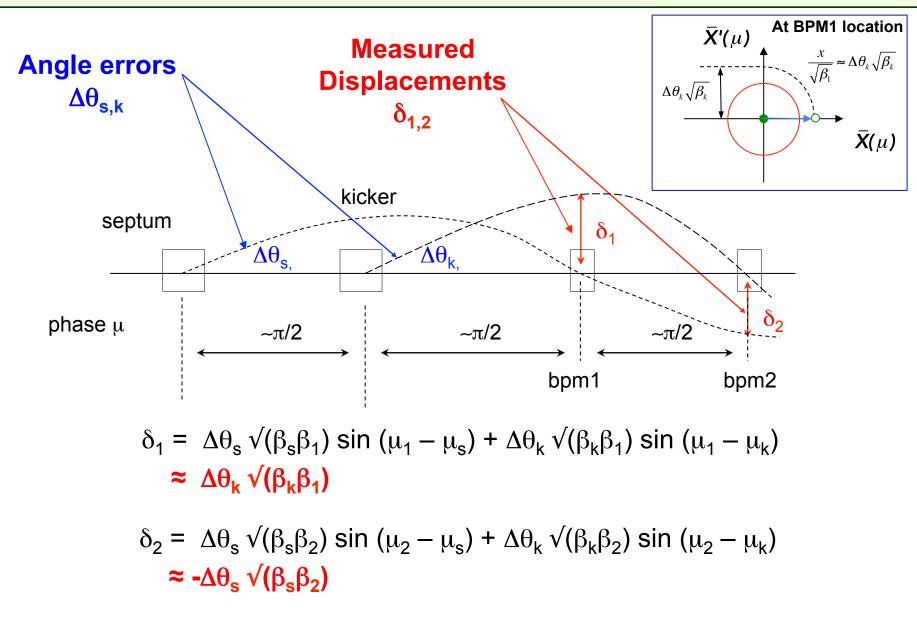
• Betatron oscillations with respect to the Closed Orbit:



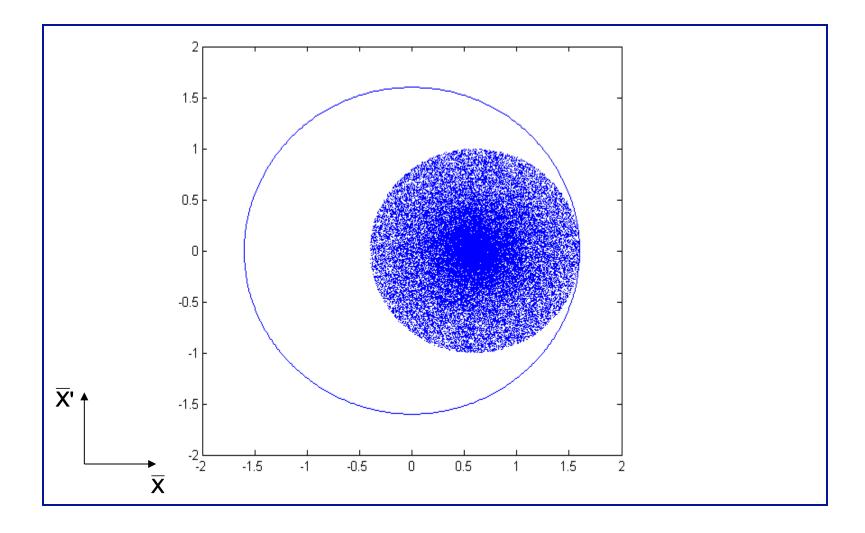
Injection errors

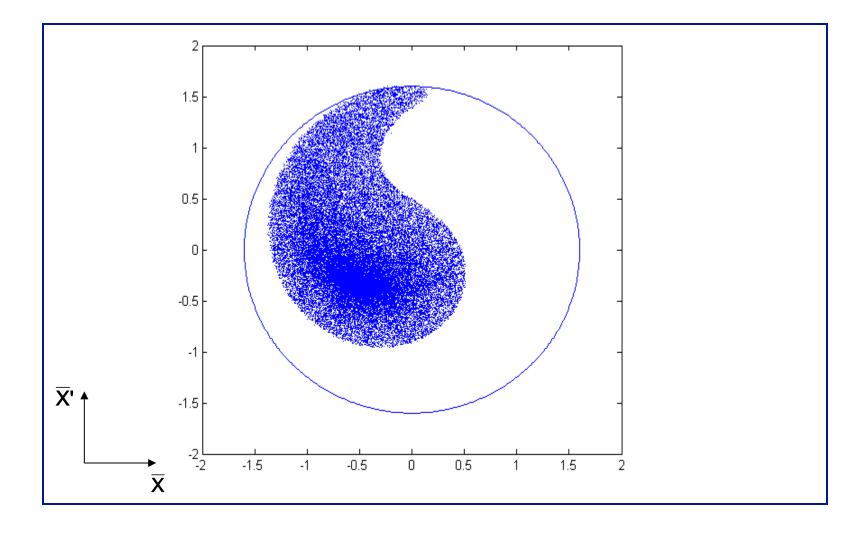


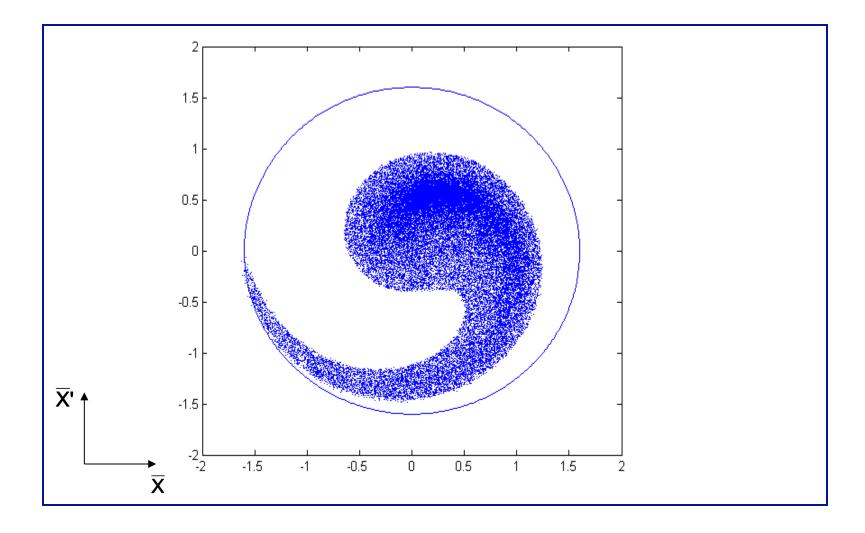
Injection errors

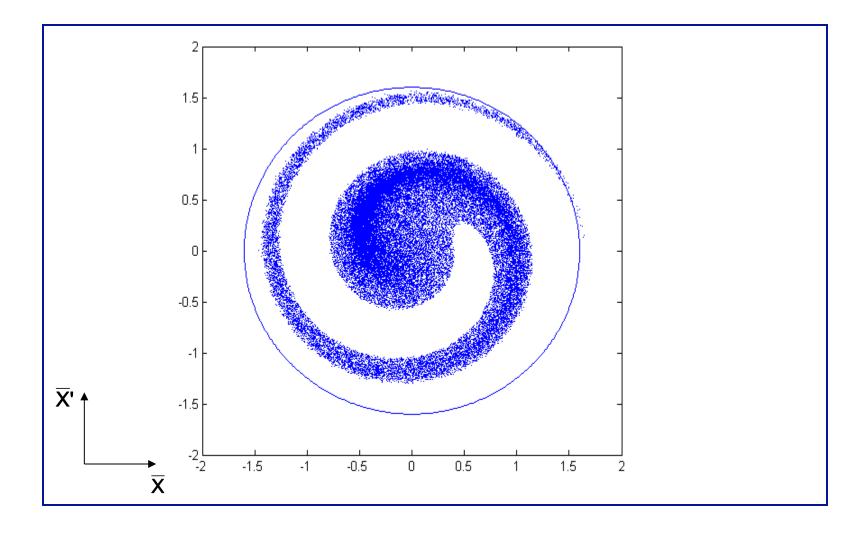


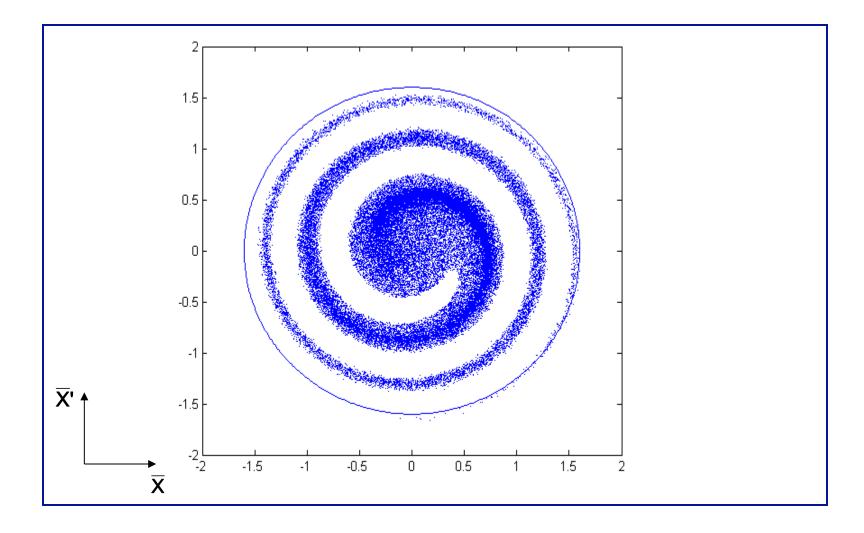
- Non-linear effects (e.g. higher-order field components) introduce amplitude-dependent effects into particle motion
- Over many turns, a phase-space oscillation is transformed into an emittance increase
- So any residual transverse oscillation will lead to an emittance blow-up through filamentation
 - Chromaticity coupled with a non-zero momentum spread at injection can also cause filmentation, often termed *chromatic decoherence*
 - "Transverse damper" systems are used to damp injection oscillations bunch position measured by a pick-up, which is linked to a kicker

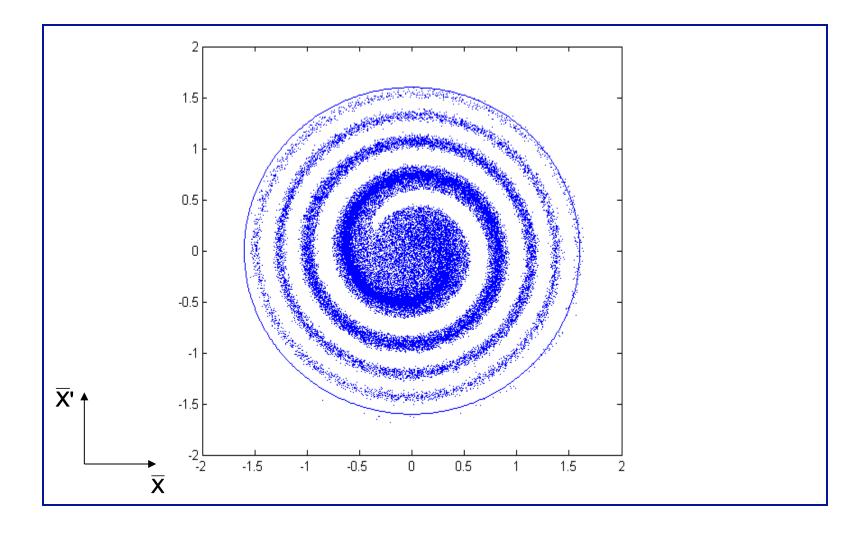


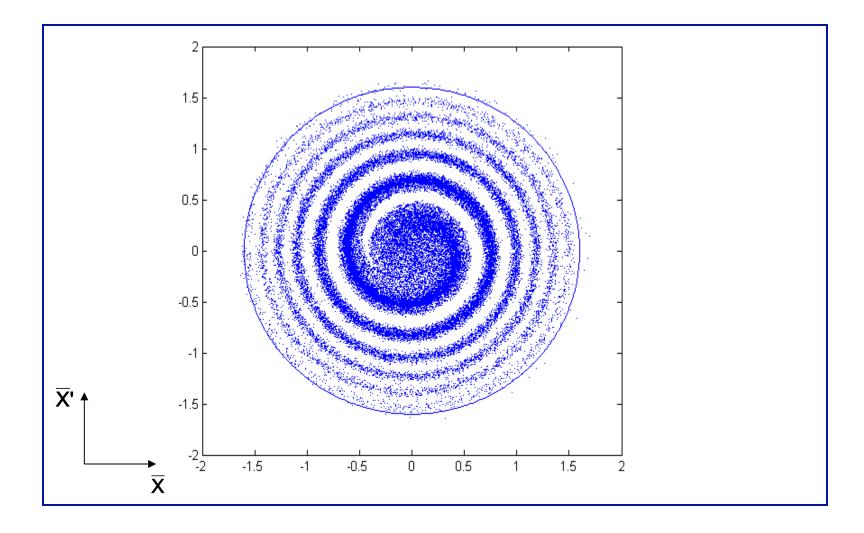


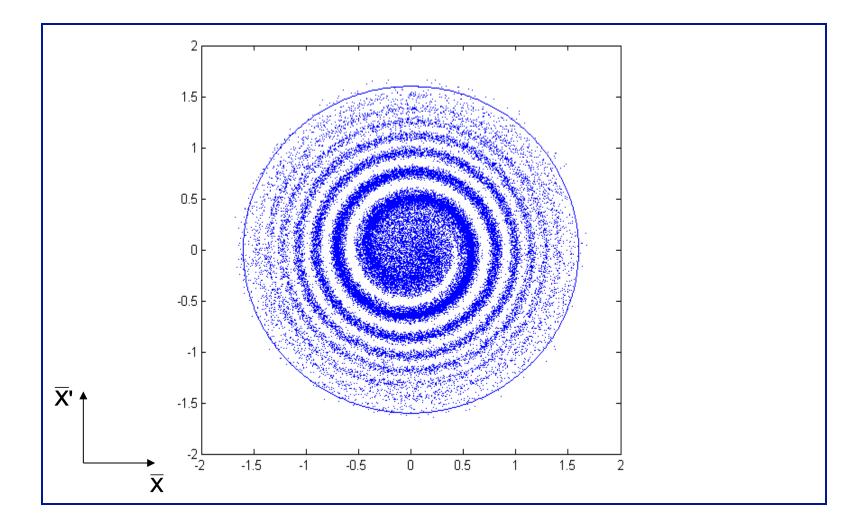


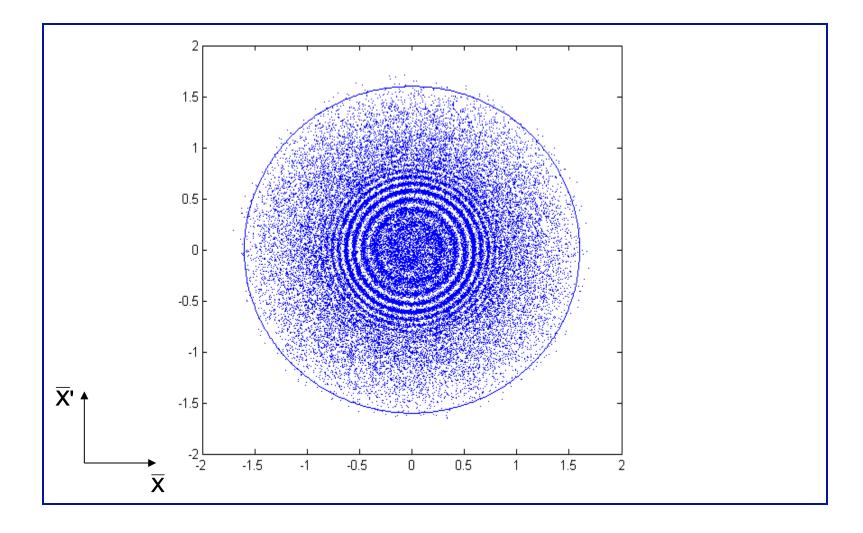


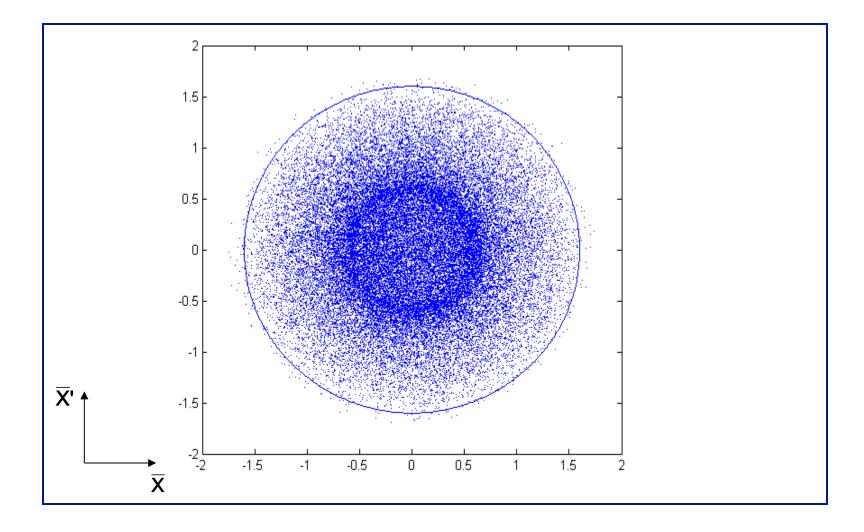




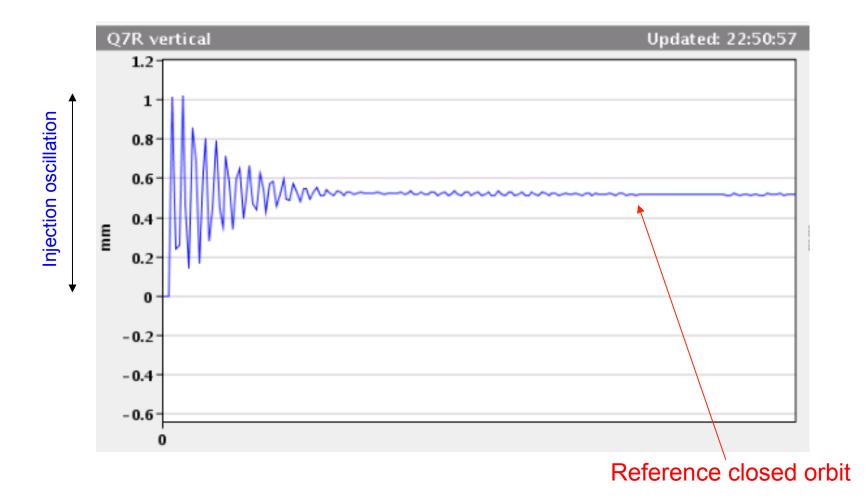




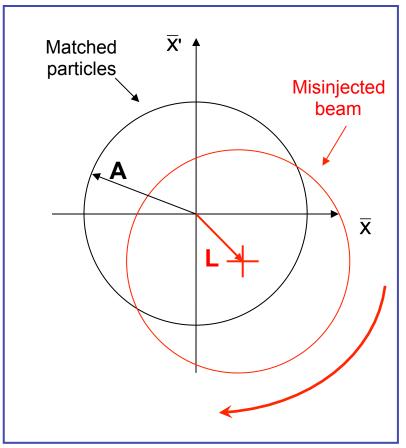




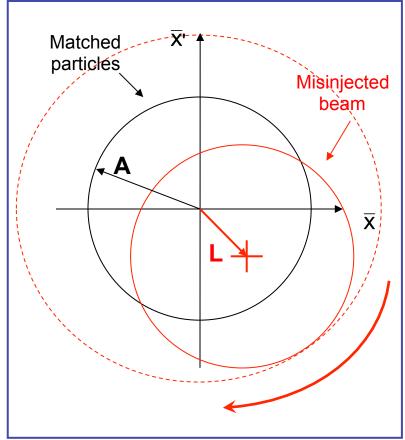
• Residual transverse oscillations lead to an *effective* emittance blowup through filamentation:



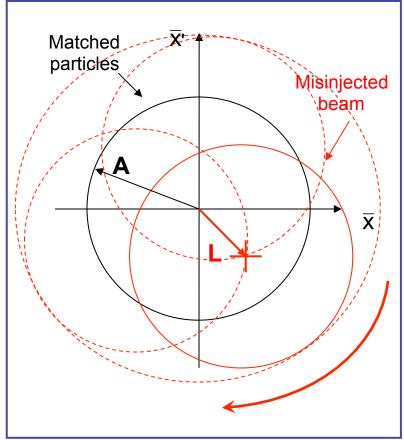
- Consider a collection of particles with max. amplitudes A
- The beam can be injected with an error in angle and position
- For an injection error Δa , in units of $\sigma = \sqrt{(\beta \epsilon)}$, the mis-injected beam is offset in normalised phase space by an amplitude L = $\Delta a \sqrt{\epsilon}$



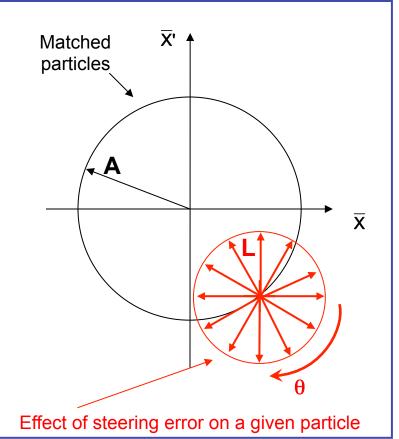
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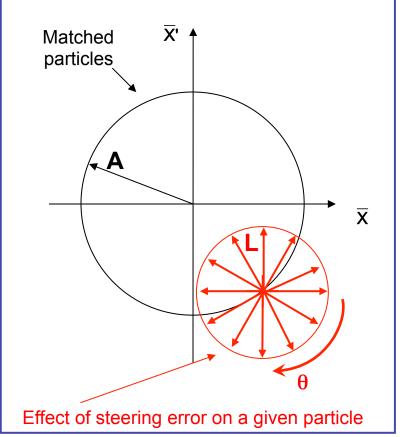
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- Any given point on the matched ellipse is randomised over all phases after filamentation due to the steering error:



Blow-up from steering error

- Consider a collection of particles with max. amplitudes A
- The beam can be injected with an error in angle and position.
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- Any given point on the matched ellipse is randomised over all phases after filamentation due to the steering error
- For a general particle distribution, where A_i denotes amplitude in normalised phase of particle i:

$$\varepsilon_{matched} = \left\langle \mathbf{A}_i^2 \right\rangle / 2$$



Blow-up from steering error

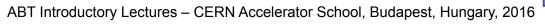
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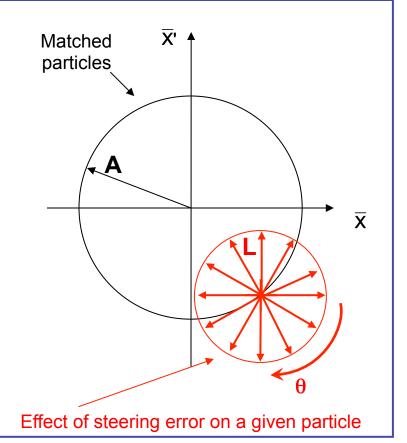
$$\varepsilon_{matched} = \left\langle \mathbf{A}_i^2 \right\rangle / 2$$

• After filamentation:

$$\varepsilon_{diluted} = \varepsilon_{matched} + \frac{L^2}{2}$$

See appendix for derivation





Blow-up from steering error

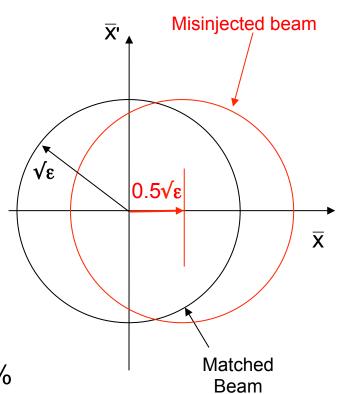
- A numerical example....
- Consider an offset $\Delta a = 0.5\sigma$ for injected beam:

$$L = \Delta a \sqrt{\varepsilon_{matched}}$$

$$\varepsilon_{diluted} = \varepsilon_{matched} + \frac{L^2}{2}$$
$$= \varepsilon_{matched} \left[1 + \frac{\Delta a^2}{2} \right]$$
$$= \varepsilon_{matched} \left[1.125 \right]$$

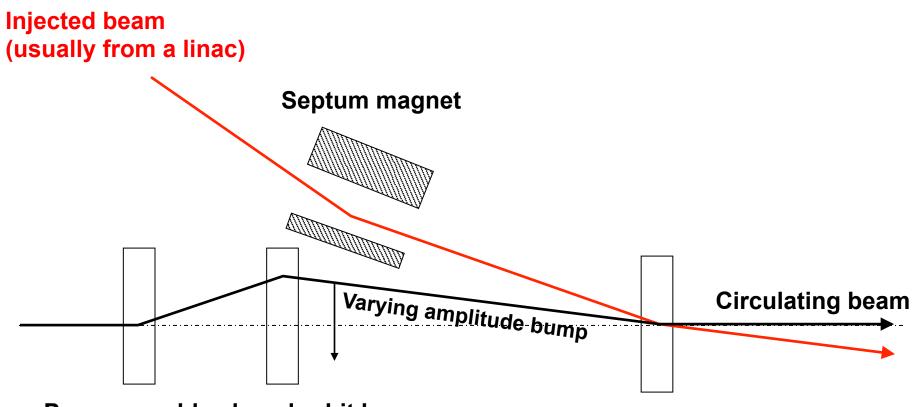
• For nominal LHC beam:

...allowed growth through LHC cycle ~10 %



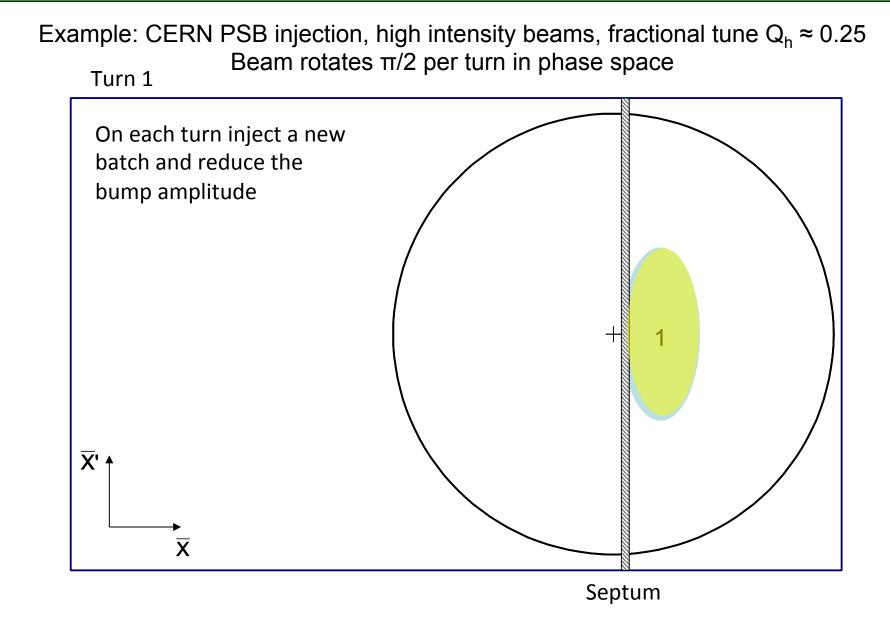
Multi-turn injection

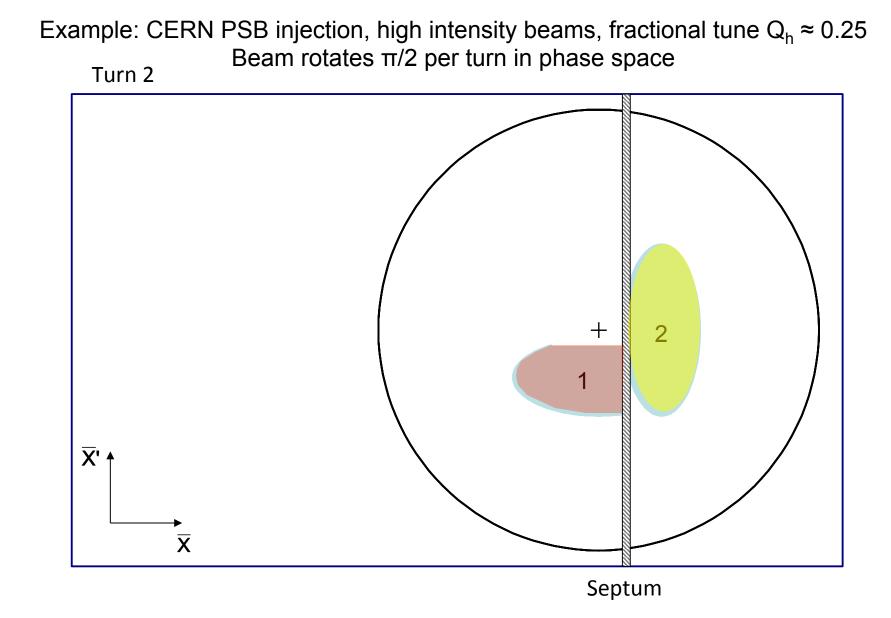
- For hadrons the beam density at injection can be limited either by space charge effects or by the injector capacity
- If we cannot increase charge density, we can sometimes fill the horizontal phase space to increase overall injected intensity.
 - If the acceptance of the receiving machine is larger than the delivered beam emittance we can accumulate intensity



Programmable closed orbit bump

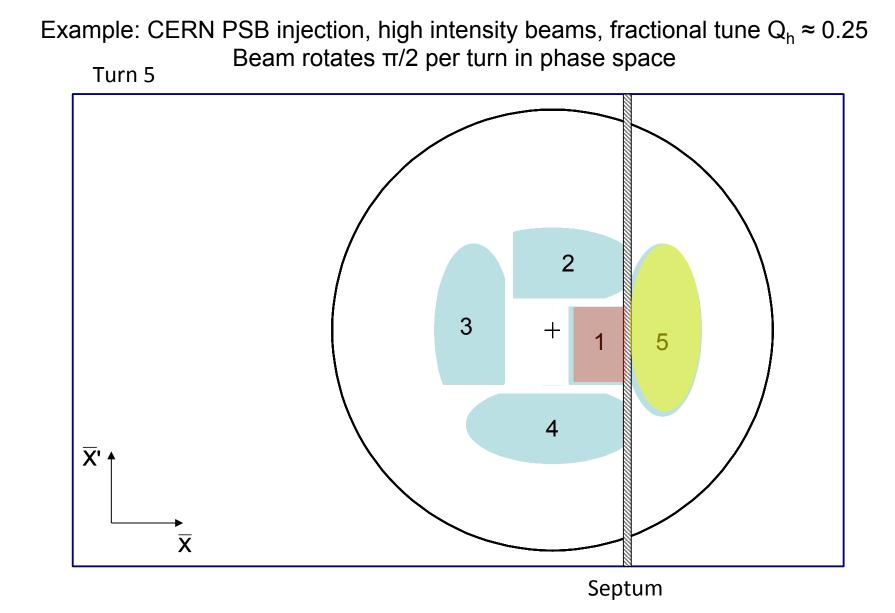
- No kicker but fast programmable bumpers
- Bump amplitude decreases and a new batch injected turn-by-turn
- Phase-space "painting"

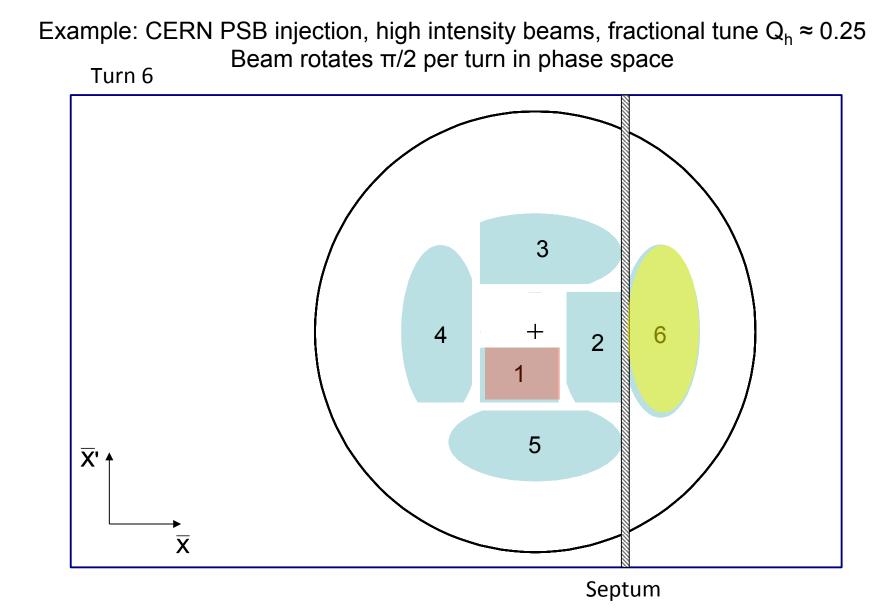


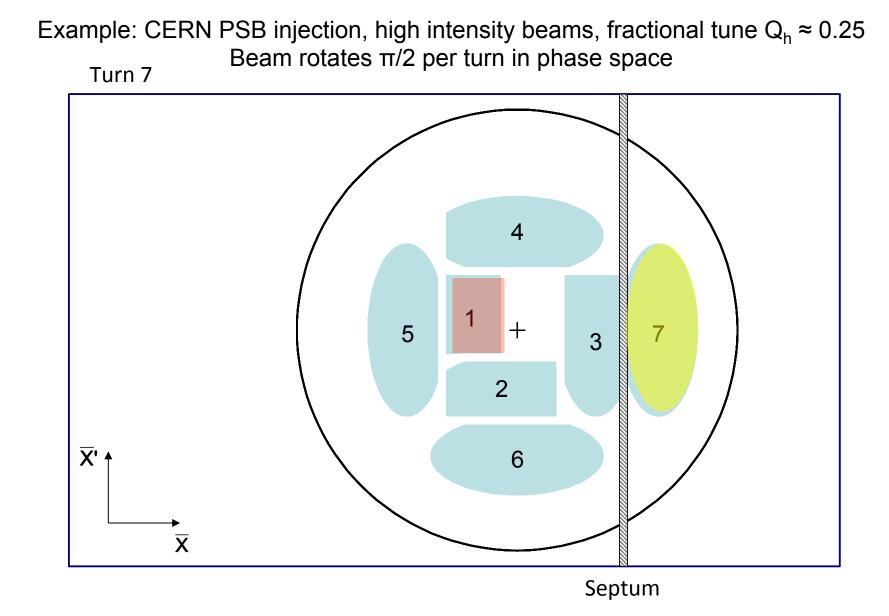


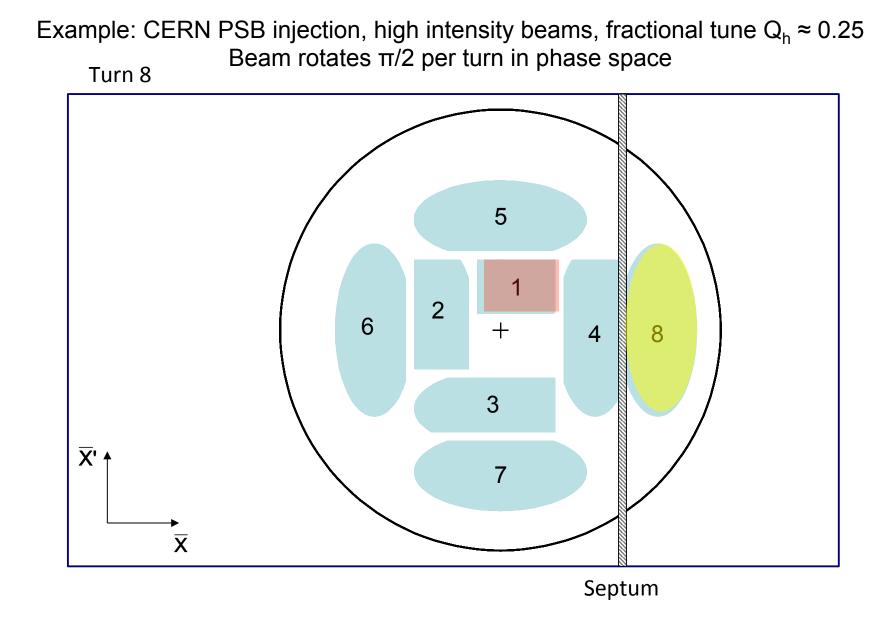
Example: CERN PSB injection, high intensity beams, fractional tune $Q_h \approx 0.25$ Beam rotates $\pi/2$ per turn in phase space Turn 3 +3 2 <u>X</u>' 4 $\overline{\mathbf{X}}$ Septum

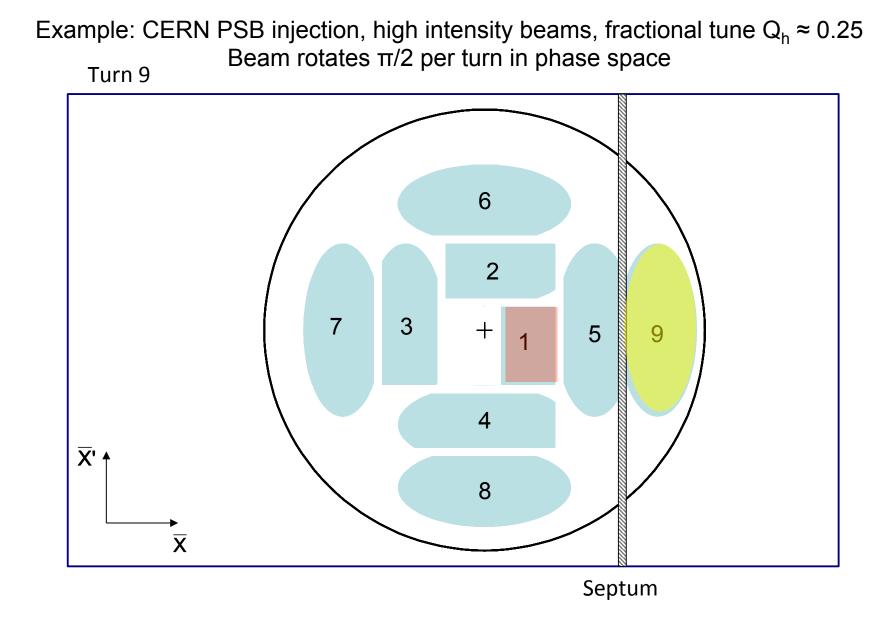
Example: CERN PSB injection, high intensity beams, fractional tune $Q_h \approx 0.25$ Beam rotates $\pi/2$ per turn in phase space Turn 4 2 +4 3 <u>X</u>' 4 $\overline{\mathbf{X}}$ Septum

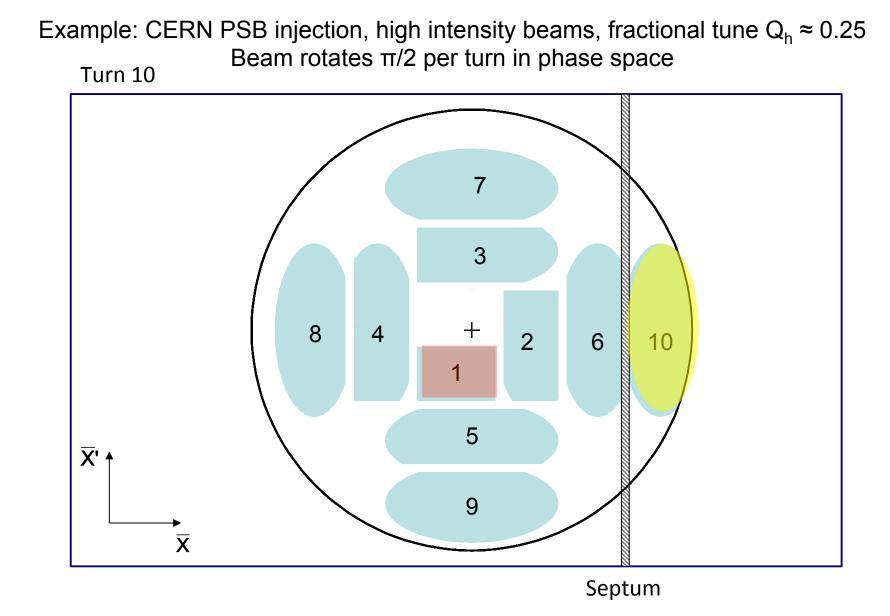


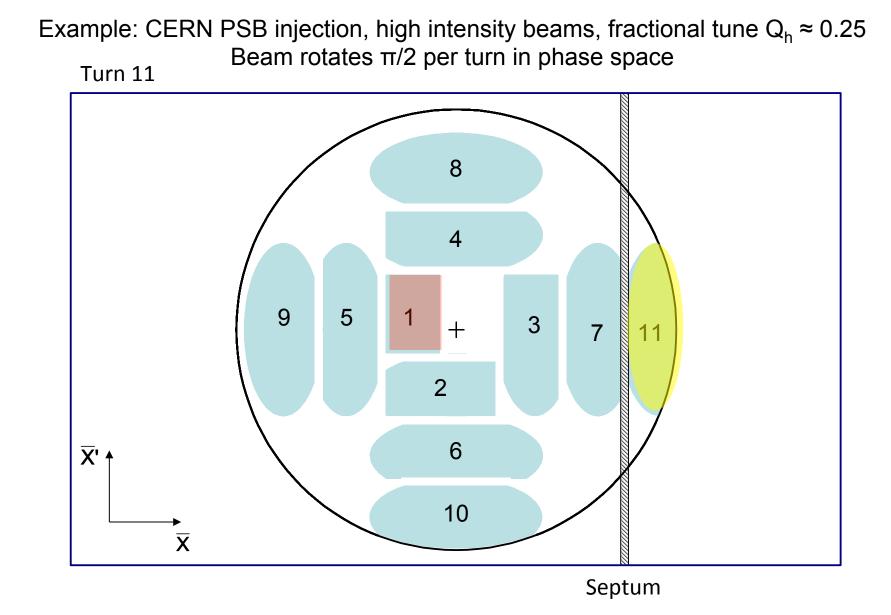










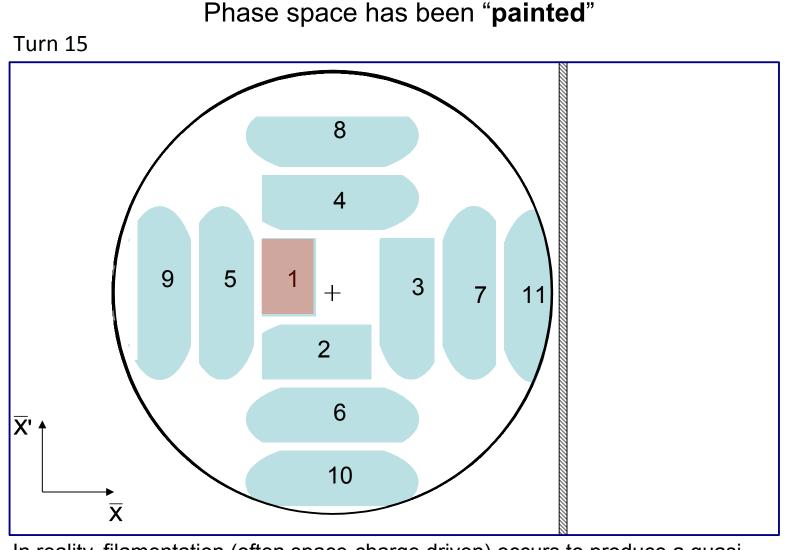


Example: CERN PSB injection, high intensity beams, fractional tune $Q_h \approx 0.25$ Beam rotates $\pi/2$ per turn in phase space Turn 12 9 5 2 10 6 +8 4 3 <u>X</u>' 7 11 $\overline{\mathbf{X}}$ Septum

Example: CERN PSB injection, high intensity beams, fractional tune $Q_h \approx 0.25$ Beam rotates $\pi/2$ per turn in phase space Turn 13 10 6 2 11 7 3 +5 9 4 <u>X</u>' 8 $\overline{\mathbf{X}}$ Septum

Example: CERN PSB injection, high intensity beams, fractional tune $Q_h \approx 0.25$ Beam rotates $\pi/2$ per turn in phase space Turn 14 11 7 3 8 4 +2 6 10 5 <u>X</u>' 9 $\overline{\mathbf{X}}$

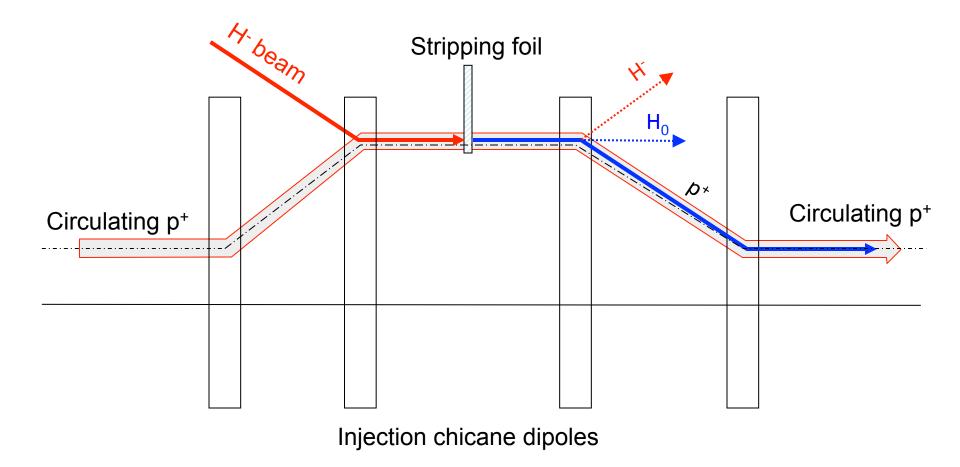
Septum



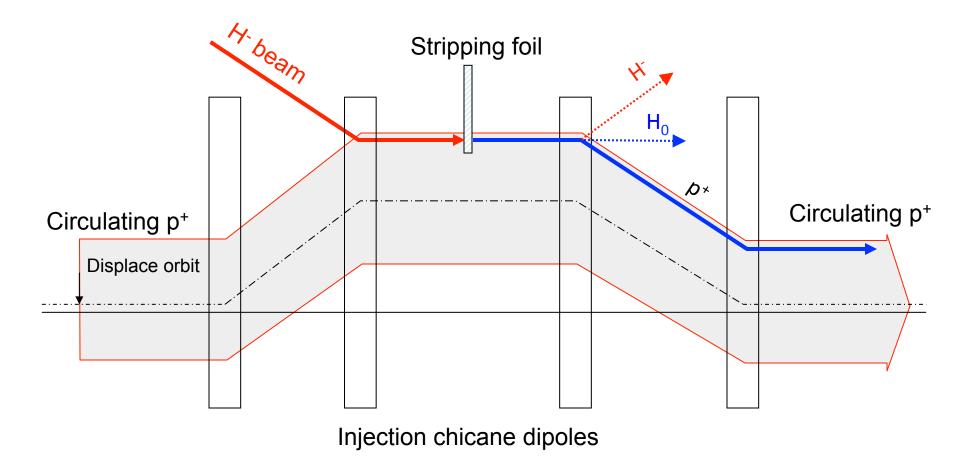
In reality, filamentation (often space-charge driven) occurs to produce a quasiuniform beam

- Multi-turn injection is essential to accumulate high intensity
- Disadvantages inherent in using an injection septum:
 - Width of several mm reduces aperture
 - Beam losses from circulating beam hitting septum:
 - typically 30 40 % for the CERN PSB injection at 50 MeV
 - Limits number of injected turns to 10 20
- Charge-exchange injection provides elegant alternative
 - Possible to "cheat" Liouville's theorem, which says that emittance is conserved....
 - Convert H⁻ to p⁺ using a thin stripping foil, allowing injection <u>into the</u> <u>same phase space area</u>

Start of injection process

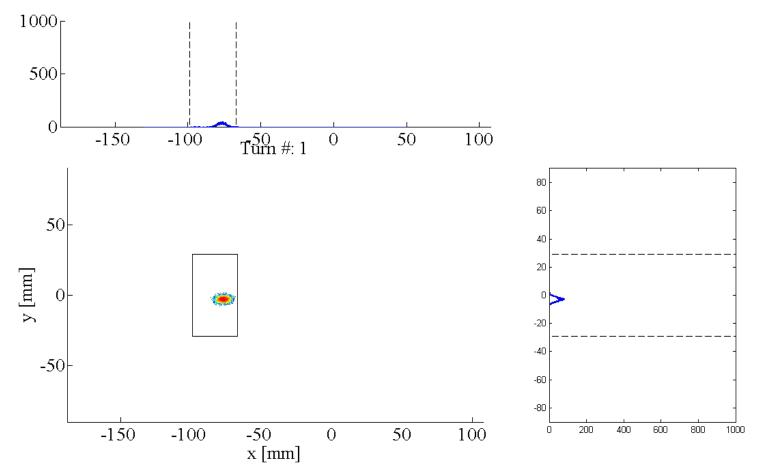


End of injection process with painting



Accumulation process on foil

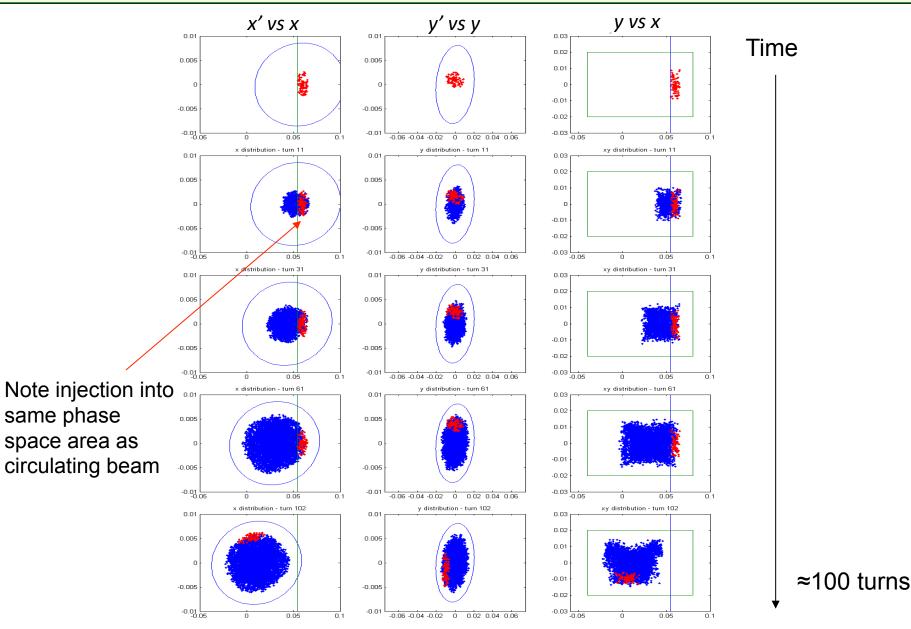
- Linac4 connection to the PS booster at 160 MeV:
 - H⁻ stripped to p⁺ with an estimated efficiency ≈98 % with C foil 200 μ g.cm⁻²



V. Forte, Performance of the CERN PSB at 160 MeV with H- charge exchange injection, PhD thesis – CERN and Université Blaise Pascal

- Paint uniform transverse phase space density by modifying closed orbit bump and steering injected beam
- Foil thickness calculated to double-strip most ions (≈99%)
 - 50 MeV 50 μg.cm⁻²
 - 800 MeV 200 µg.cm⁻² (≈ 1 µm of C!)
- Carbon foils generally used very fragile
- Injection chicane reduced or switched off after injection, to avoid excessive foil heating and beam blow-up
- Longitudinal phase space can also be painted turn-by-turn:
 - Variation of the injected beam energy turn-by-turn (linac voltage scaled)
 - Chopper system in linac to match length of injected batch to bucket

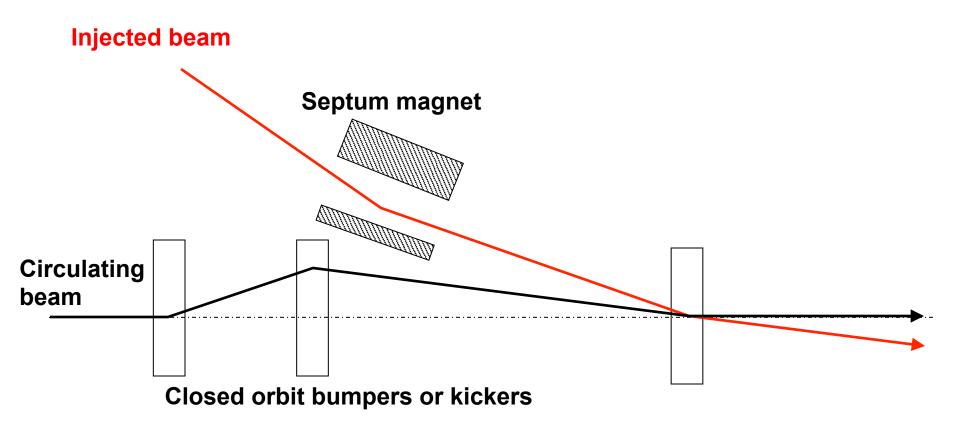
H- injection - painting



Lepton injection

- Single-turn injection can be used as for hadrons; however, lepton motion is <u>strongly damped</u> (different with respect to proton or ion injection).
 - Synchrotron radiation
 - see Electron Beam Dynamics lectures by L. Rivkin
- Can use transverse or longitudinal damping:
 - Transverse Betatron accumulation
 - Longitudinal Synchrotron accumulation

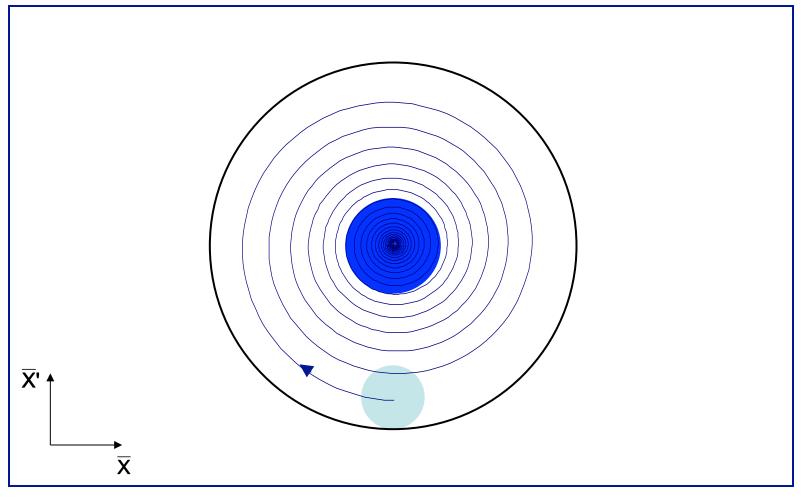
Betatron lepton injection



- Beam is injected with an angle with respect to the closed orbit
- Injected beam performs <u>damped</u> betatron oscillations about the closed orbit

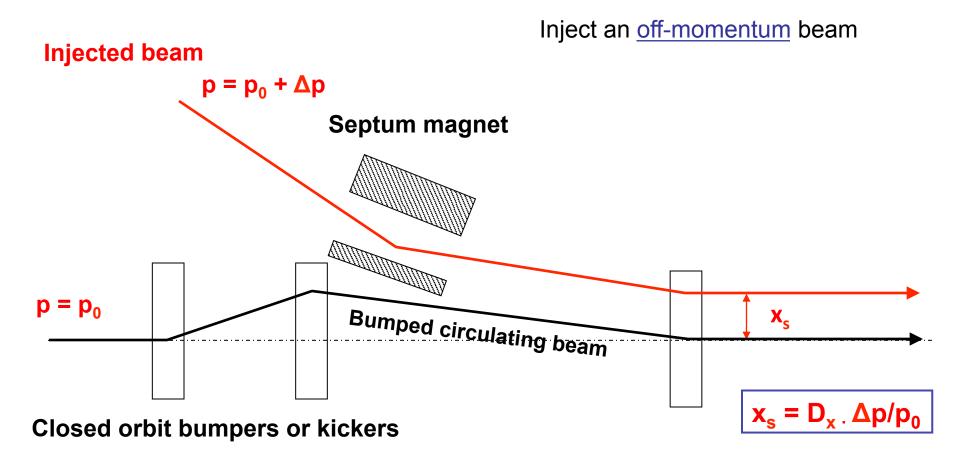
Betatron lepton injection

Injected bunch performs damped betatron oscillations



In LEP at 20 GeV, the damping time was about 6'000 turns (0.6 seconds)

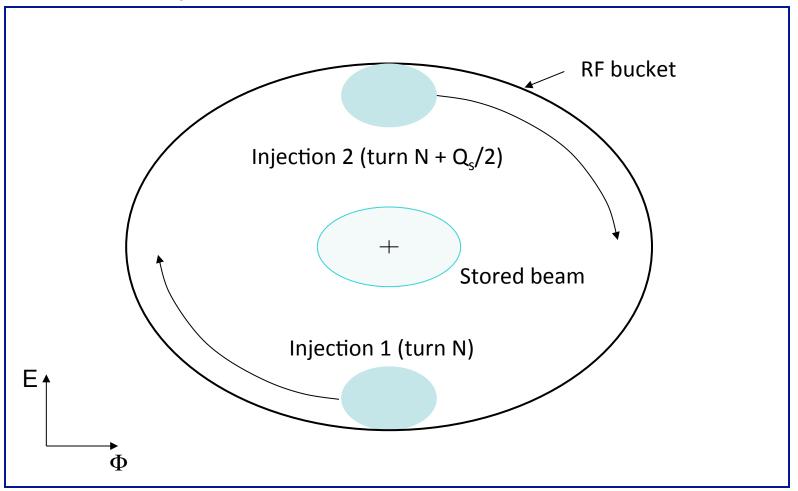
Synchrotron lepton injection



- Beam injected parallel to circulating beam, onto dispersion orbit of a particle having the same momentum offset $\Delta p/p$
- Injected beam makes damped synchrotron oscillations at Q_s but does not perform betatron oscillations

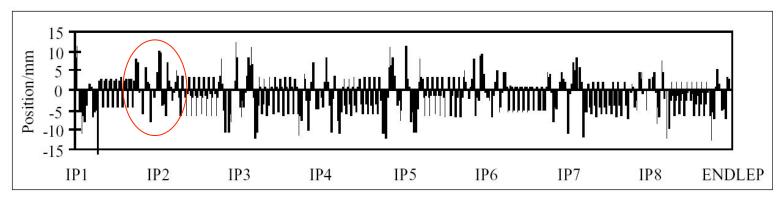
Synchrotron lepton injection

Double batch injection possible....

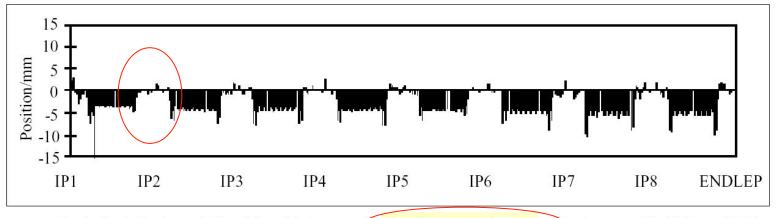


Longitudinal damping time in LEP was ~3'000 turns (2x faster than transverse)

Synchrotron lepton injection in LEP



Optimized Horizontal First Turn Trajectory for Betatron Injection of Positrons into LEP.



Optimized Horizontal First Turn Trajectory for Synchrotron Injection of Positrons with $\Delta P/P$ at -0.6%

Synchrotron injection in LEP gave improved background for LEP experiments due to small orbit offsets in <u>zero dispersion straight sections</u>

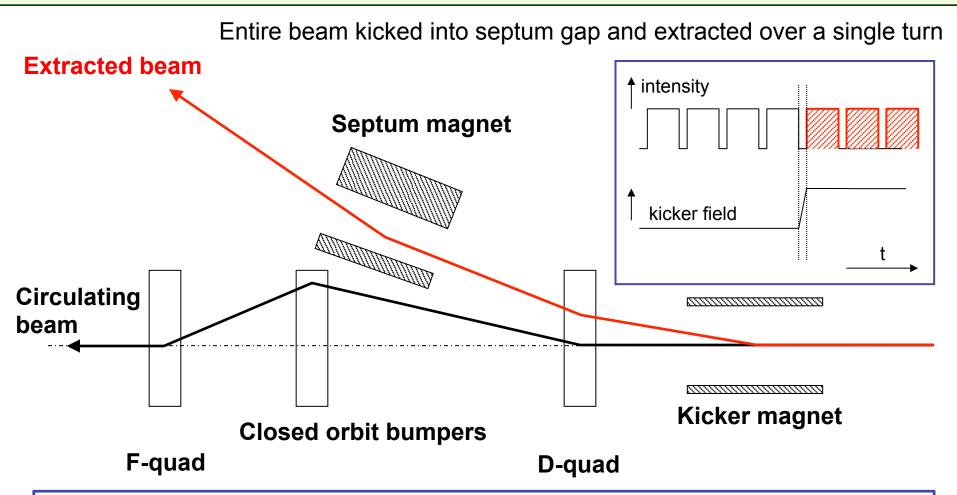
Injection - summary

- Several different techniques using kickers, septa and bumpers:
 - Single-turn injection for hadrons
 - Boxcar stacking: transfer between machines in accelerator chain
 - Angle / position errors \Rightarrow injection oscillations
 - Uncorrected errors \Rightarrow filamentation \Rightarrow emittance increase
 - Multi-turn injection for hadrons
 - Phase space painting to increase intensity
 - H- injection allows injection into same phase space area
 - Lepton injection: take advantage of damping
 - Less concerned about injection precision and matching

Extraction

- Different extraction techniques exist, depending on requirements
 - <u>Fast extraction</u>: ≤1 turn
 - <u>Non-resonant (fast) multi-turn extraction</u>: few turns
 - <u>Resonant low-loss (fast) multi-turn extraction</u>: few turns
 - Resonant multi-turn extraction: many thousands of turns
- Usually higher energy than injection \Rightarrow stronger elements ($\int B.dl$)
 - At high energies many kicker and septum modules may be required
 - To reduce kicker and septum strength, beam can be moved near to septum by closed orbit bump

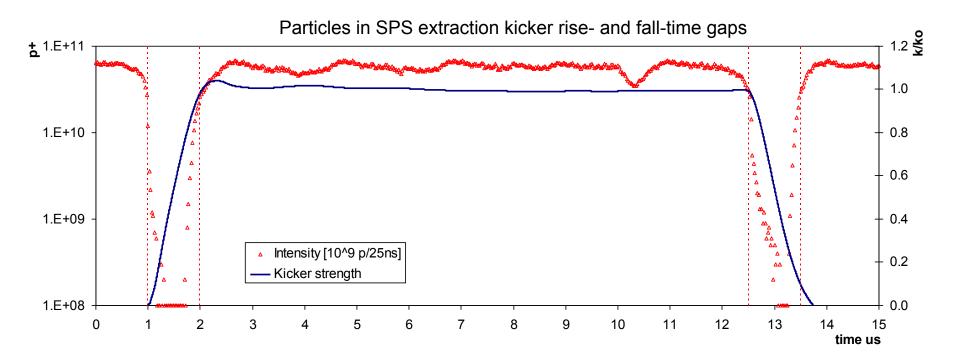
Fast single turn extraction



- Bumpers move circulating beam close to septum to reduce kicker strength
- Kicker deflects the entire beam into the septum in a single turn
- Most efficient (lowest deflection angles required) for $\pi/2$ phase advance between kicker and septum

Fast single turn extraction

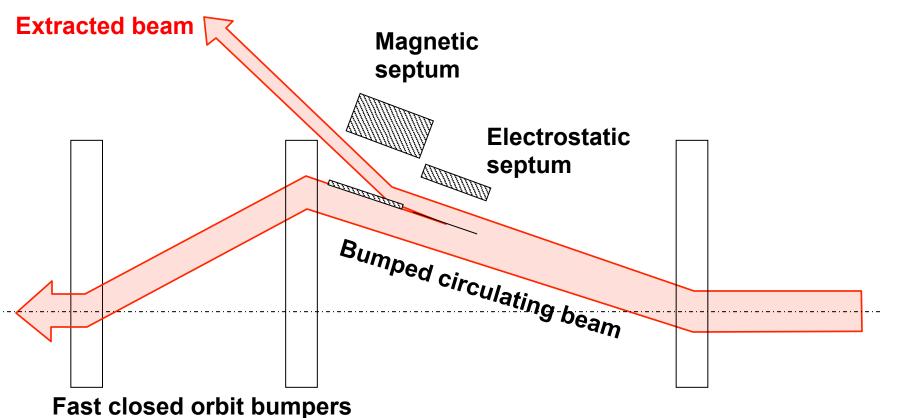
- For transfer of beams between accelerators in an injector chain
- For secondary particle production
 - e.g. neutrinos, radioactive beams
- Losses from transverse scraping or from particles in extraction gap:
 - Fast extraction from SPS to CNGS:



Multi-turn extraction

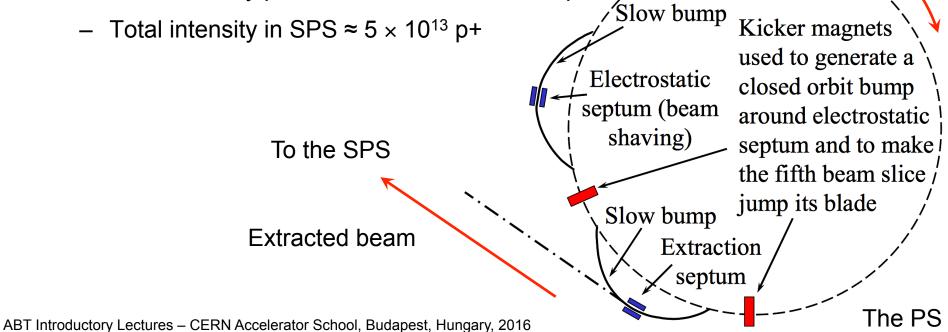
- Some filling schemes require a beam to be injected in several turns to a larger machine...
- And very commonly Fixed Target physics experiments and medical accelerators often need a quasi-continuous flux of particles...
- Multi-turn extraction...
 - Fast: Non-resonant and resonant multi-turn ejection (few turns) for filling
 - e.g. PS to SPS at CERN for high intensity proton beams (>2.5 10¹³ protons)
 - Slow: Resonant extraction (ms to hours) for experiments

Beam bumped to septum; part of beam 'shaved' off each turn

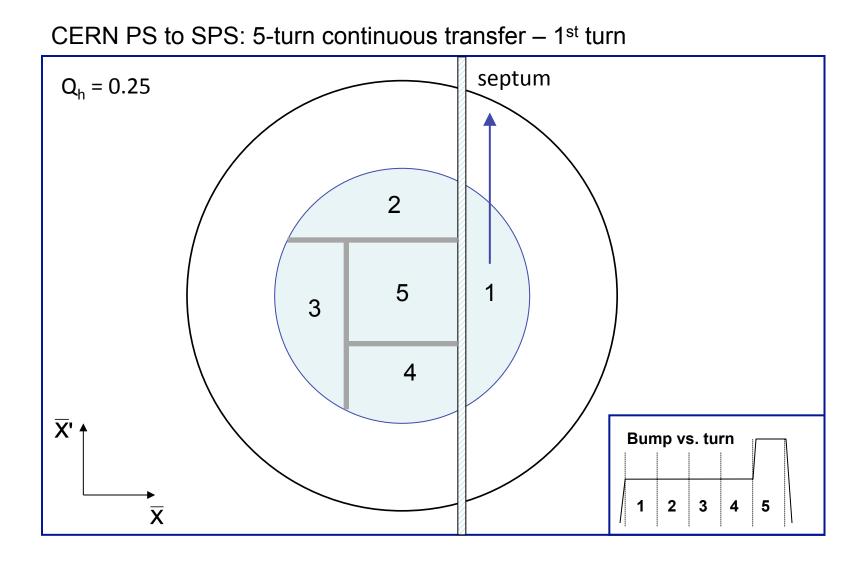


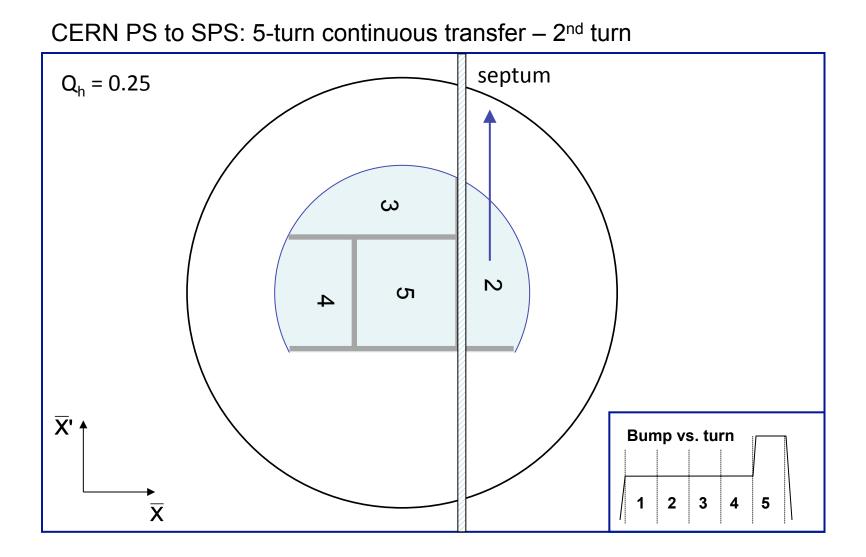
- Fast bumper deflects the whole beam onto the septum
- Beam extracted in a few turns, with the machine tune rotating the beam
- Intrinsically a high-loss process: thin septum essential
- Often combine thin electrostatic septa with magnetic septa

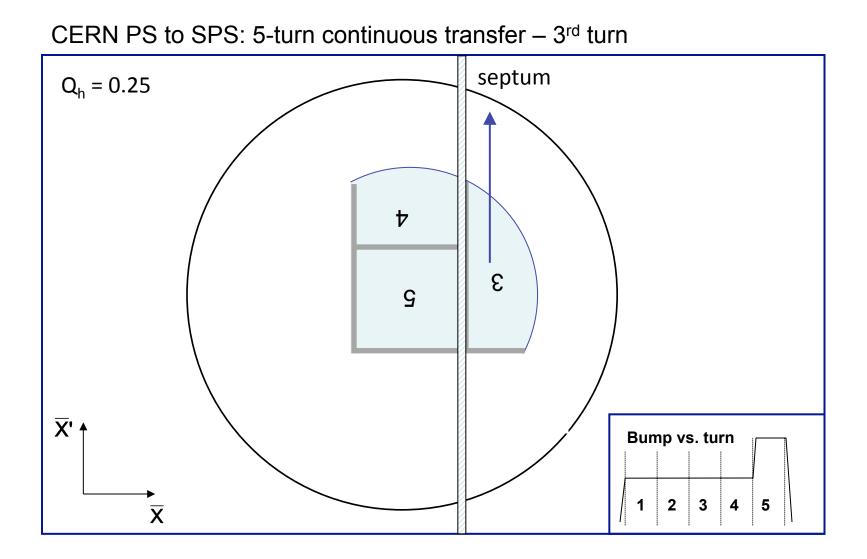
- Example system: CERN PS to SPS Fixed-Target 'continuous transfer'.
 - Accelerate beam in PS to 14 GeV/c
 - Empty PS machine (2.1 µs long) in 5 turns into SPS
 - Do it again
 - Fill SPS machine (23 µs long)
 - Quasi-continuous beam in SPS (2 x 1 µs gaps)
 - − Total intensity per PS extraction $\approx 3 \times 10^{13}$ p+

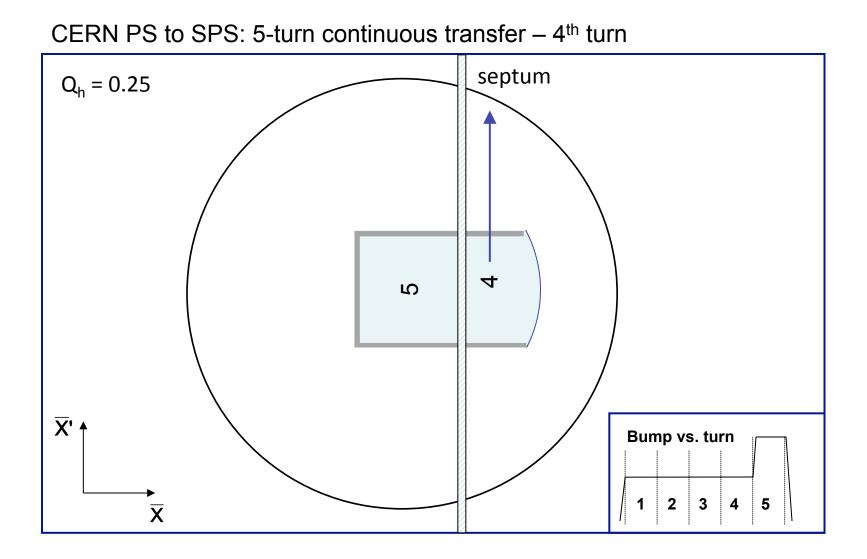


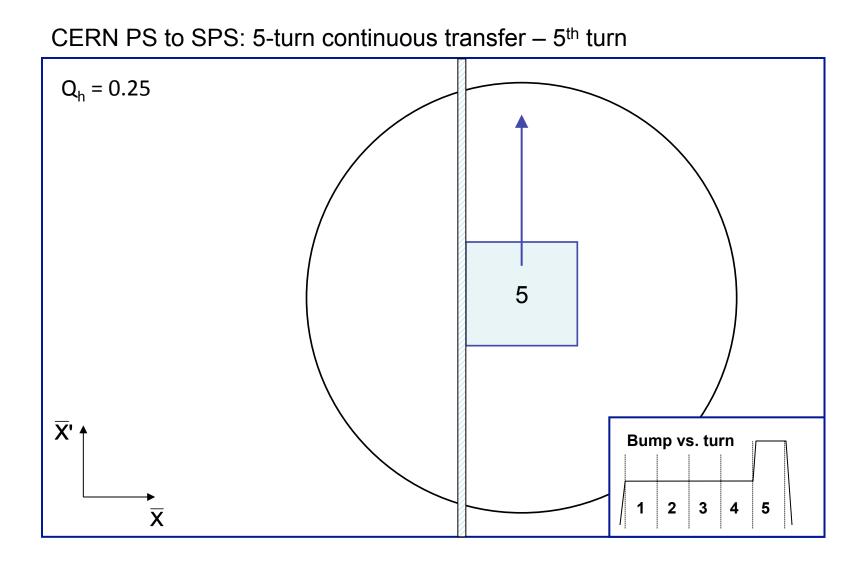
beam









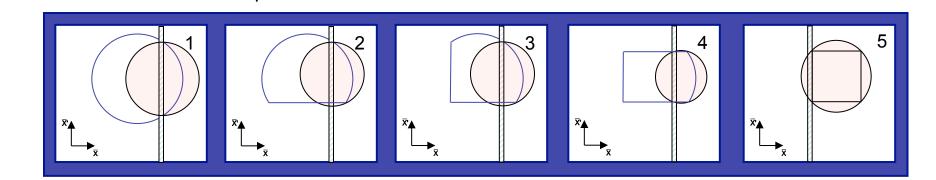


- CERN PS to SPS: 5-turn continuous transfer
 - Losses impose thin (ES) septum...

...a second magnetic septum is needed

- Still about 15 % of beam lost in PS-SPS CT
- Difficult to get equal intensities per turn
- Different trajectories for each turn





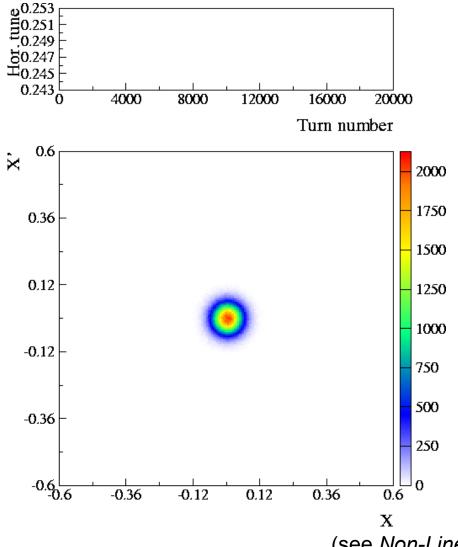
2

5

Resonant multi-turn (fast) extraction

- Adiabatic capture of beam in stable "islands"
 - Use non-linear fields (sextupoles and octupoles) to create islands of stability in phase space
 - A slow (adiabatic) tune variation to cross a resonance and to drive particles into the islands (capture) with the help of transverse excitation (using damper)
 - Variation of field strengths to separate the islands in phase space
- Several big advantages:
 - Losses reduced significantly (no particles at the septum in transverse plane)
 - Phase space matching improved with respect to existing non-resonant multi-turn extraction - 'beamlets' have similar emittance and optical parameters

Resonant multi-turn (fast) extraction

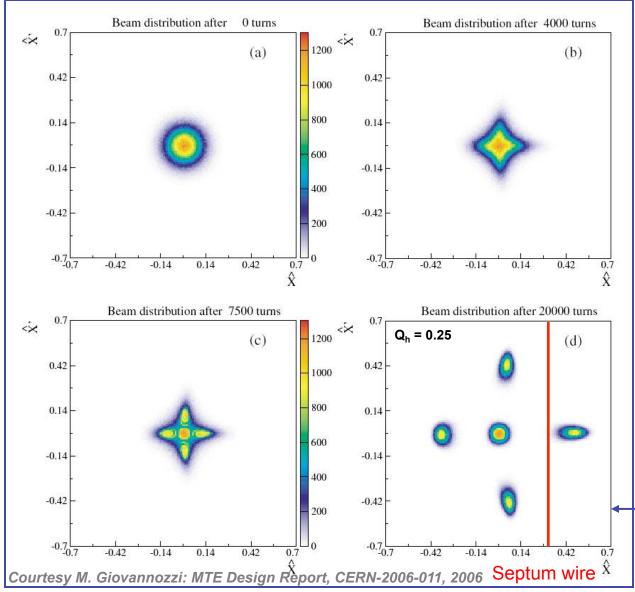


- a. Unperturbed beam
- b. Increasing non-linear fields
- c. Beam captured in stable islands
- d. Islands separated and beam bumped across septum – extracted in 5 turns

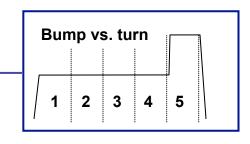
(see Non-Linear Beam Dynamics lectures by A. Wolski)

Courtesy M. Giovannozzi: MTE Design Report, CERN-2006-011, 2006

Resonant multi-turn (fast) extraction

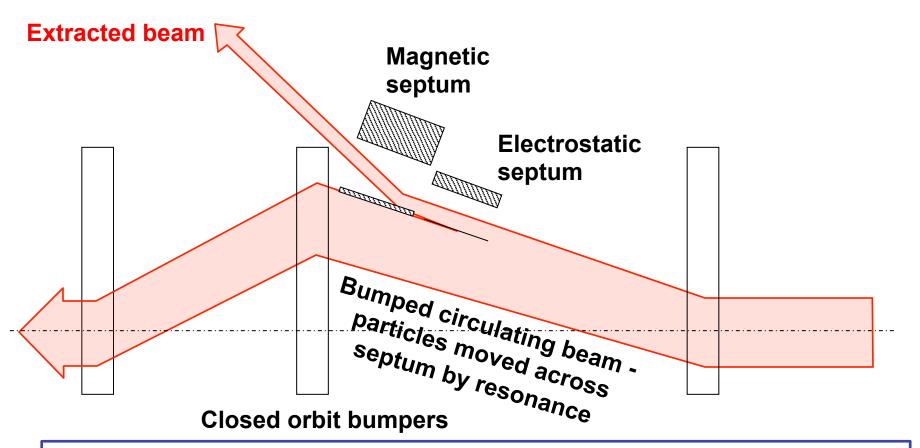


- a. Unperturbed beam
- b. Increasing non-linear fields
- c. Beam captured in stable islands
- d. Islands separated and beam bumped across septum – extracted in 5 turns



Resonant multi-turn (slow) extraction

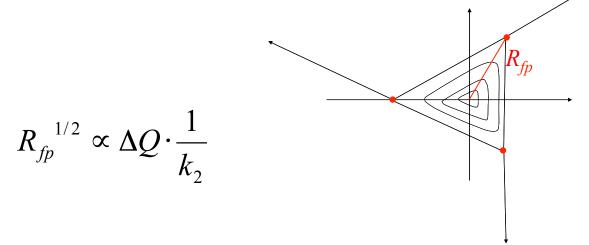
Non-linear fields excite resonances that drive the beam slowly across the septum



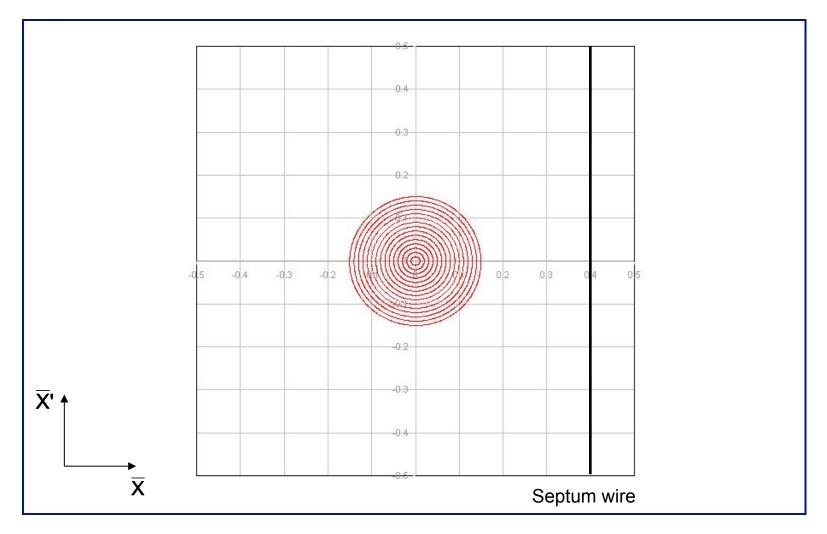
- Slow bumpers move the beam near the septum
- Tune adjusted close to nth order betatron resonance
- Multipole magnets excited to define stable area in phase space, size depends on $\Delta Q = Q Q_r$

Resonant multi-turn (slow) extraction

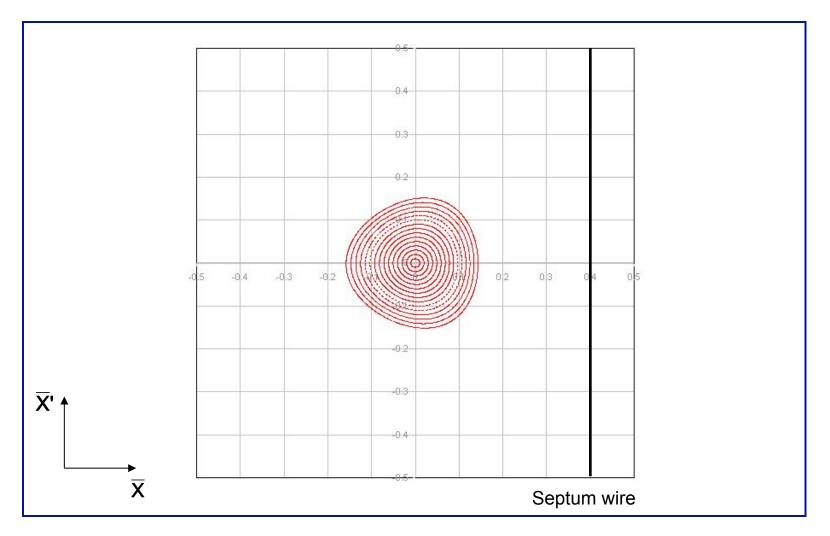
- 3rd order resonances see *lectures by A. Wolski*
 - Sextupole fields distort the circular normalised phase space particle trajectories.
 - Stable area defined, delimited by unstable Fixed Points.



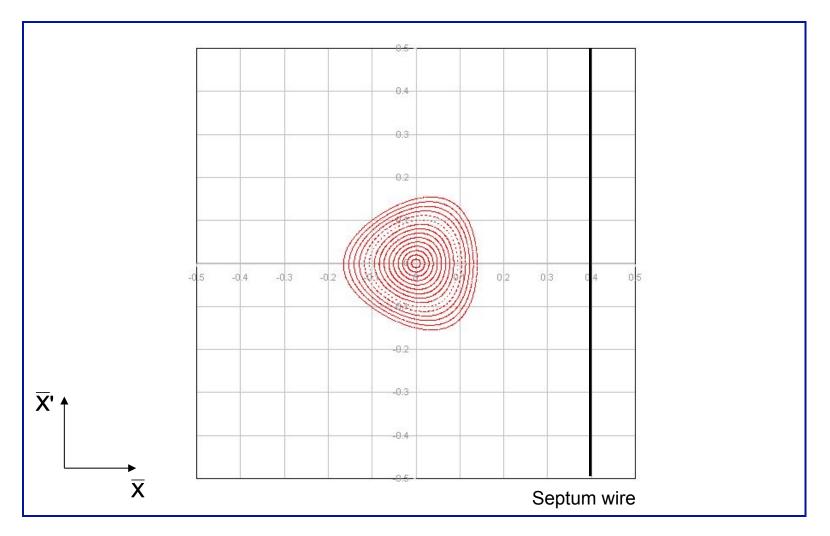
- Sextupole magnets arranged to produce suitable phase space orientation of the stable triangle at thin electrostatic septum
- Stable area can be reduced by...
 - Increasing the sextupole strength, or...
 - Fixing the sextupole strength and scanning the machine tune Q_h (and therefore the resonance) through the tune spread of the beam
 - Large tune spread created with RF gymnastics (large momentum spread) and large chromaticity



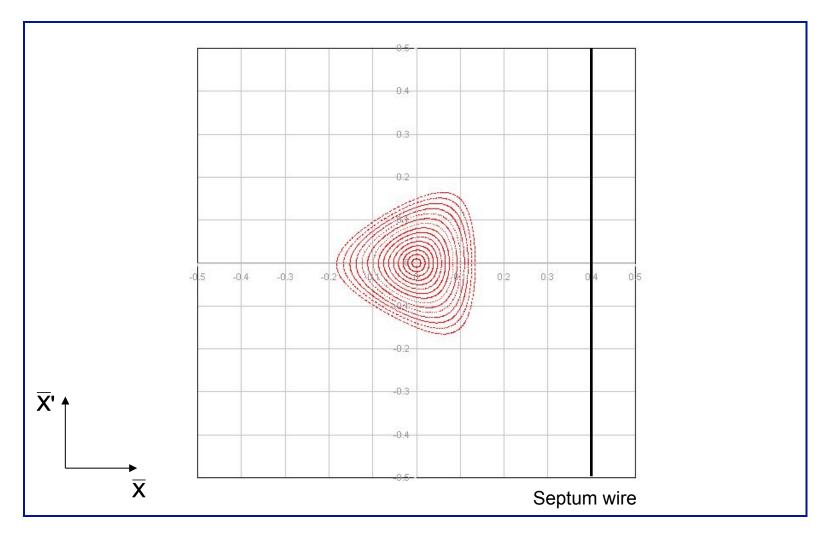
- Particles distributed on emittance contours
- ΔQ large no phase space distortion



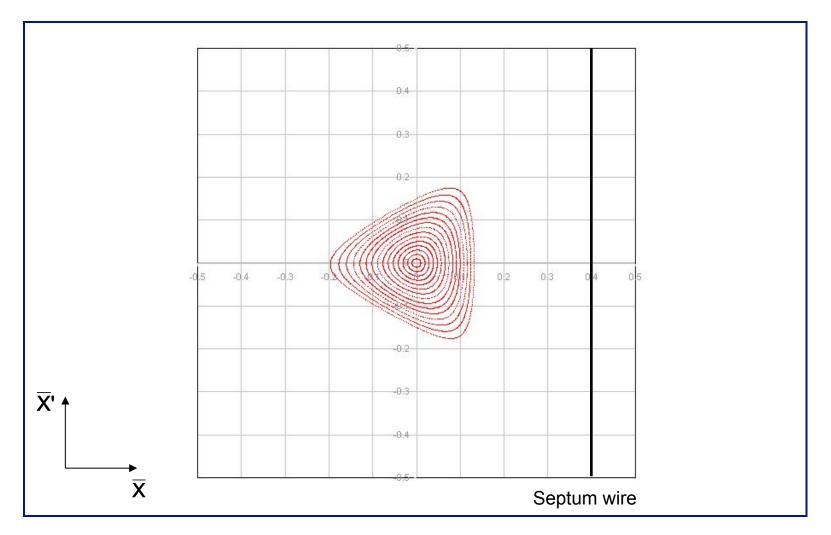
- Sextupole magnets produce a triangular stable area in phase space
- ΔQ decreasing phase space distortion for largest amplitudes



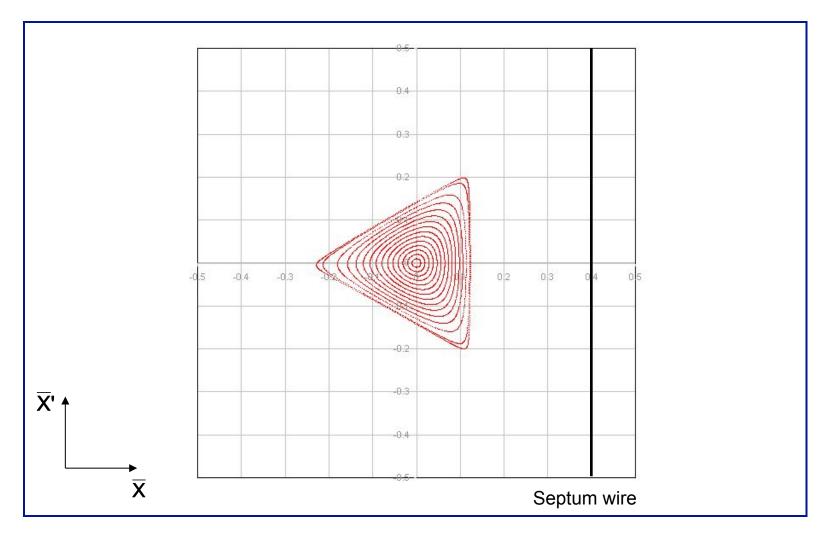
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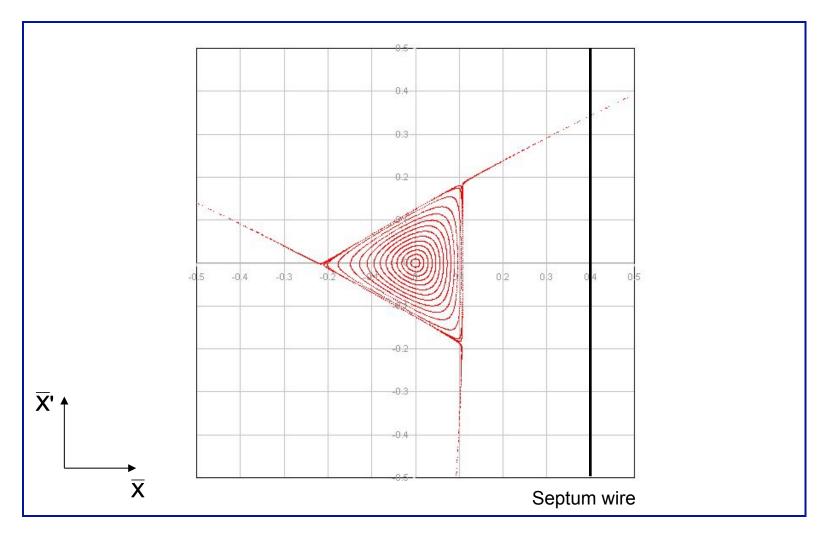
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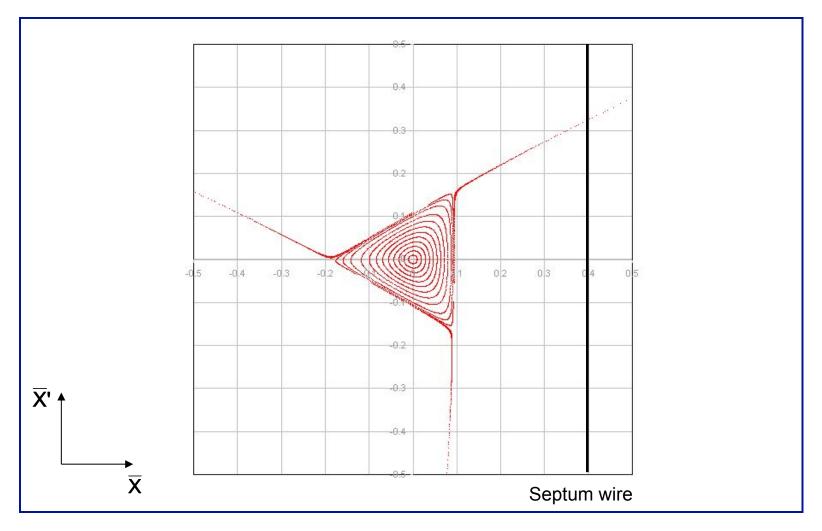
- Sextupole magnets produce a triangular stable area in phase space
- ΔQ decreasing phase space distortion for largest amplitudes



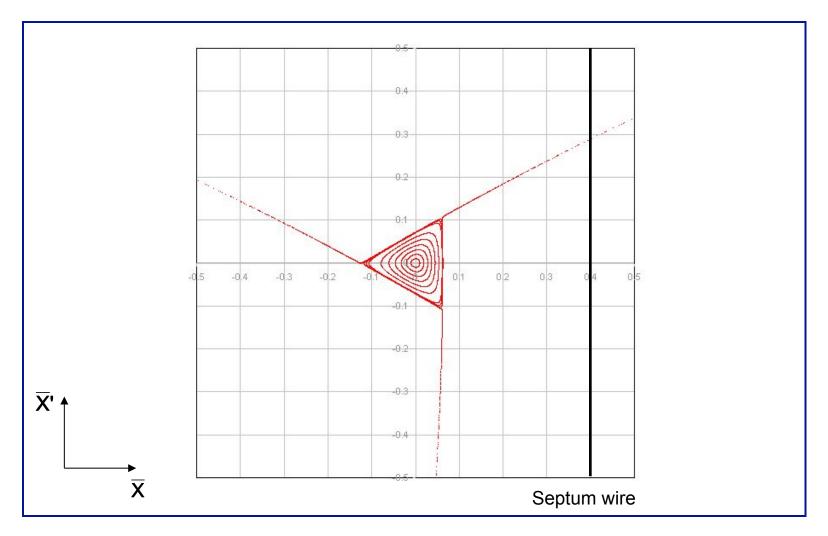
- Largest amplitude particle trajectories are significantly distorted
- Locations of fixed points discernable at extremities of phase space triangle



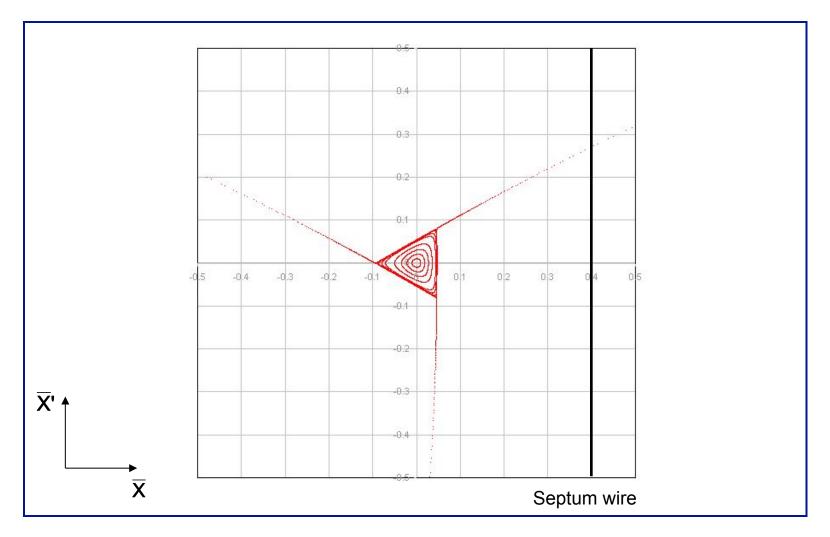
- ΔQ small enough that largest amplitude particle trajectories are unstable
- Unstable particles follow separatrix branches as they increase in amplitude



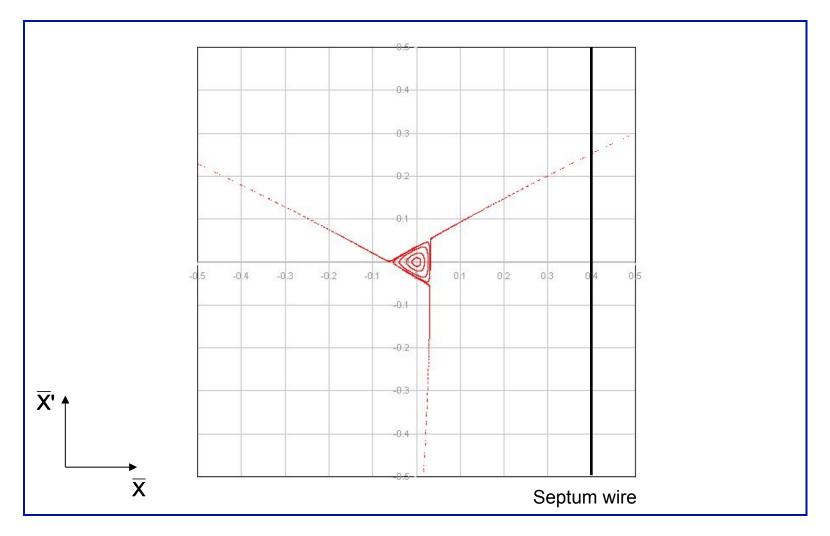
• Stable area shrinks as ΔQ becomes smaller



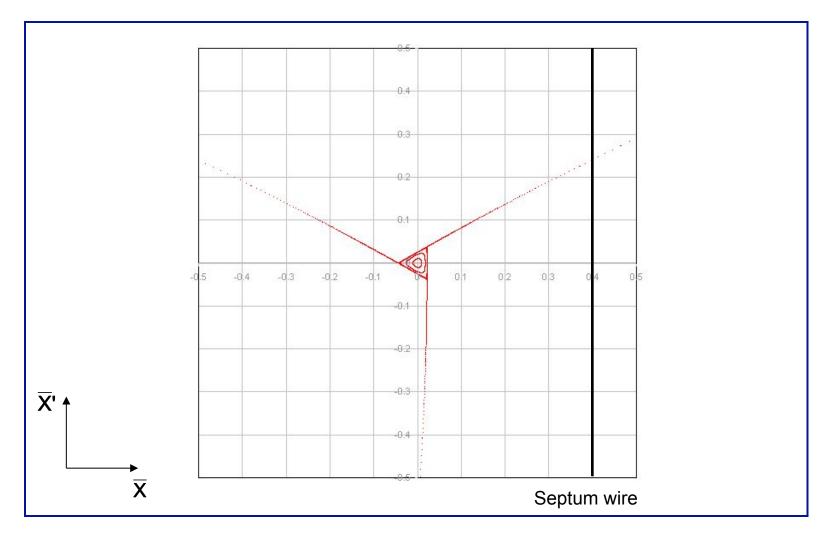
• Separatrix position in phase space shifts as the stable area shrinks



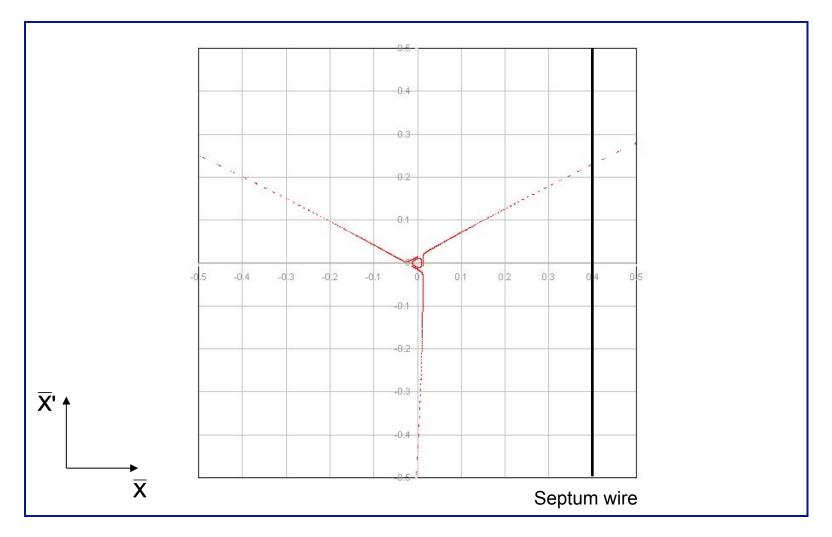
 As the stable area shrinks, the circulating beam intensity drops since particles are being continuously extracted



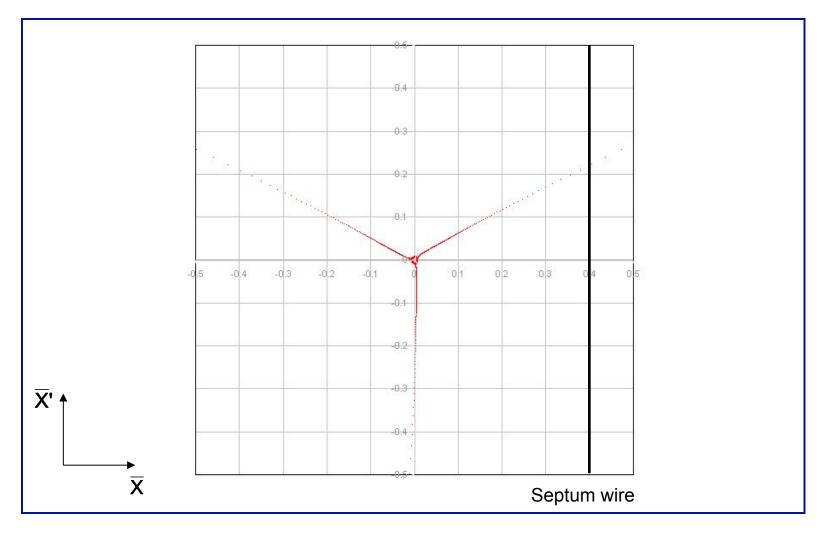
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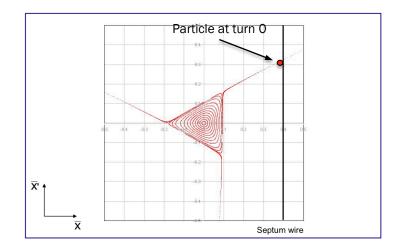
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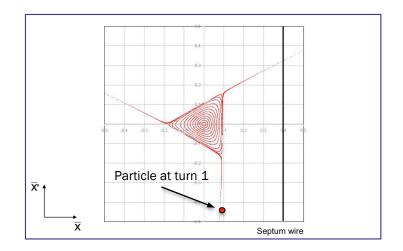


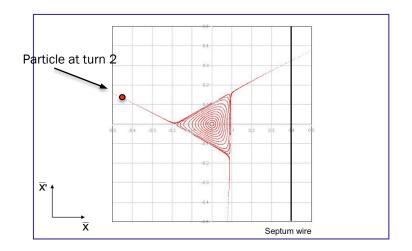
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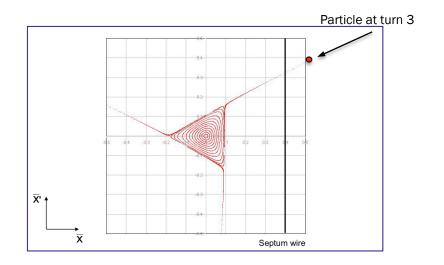


 As ΔQ approaches zero, the particles with very small amplitude are extracted





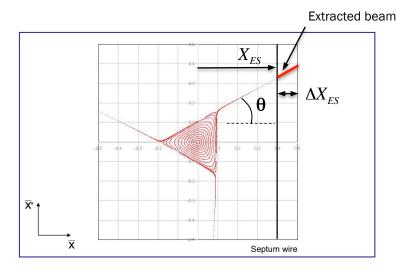




- On resonance, sextupole kicks add-up driving particles over septum
 - Distance travelled in these final three turns is termed the "spiral step," ΔX_{ES}

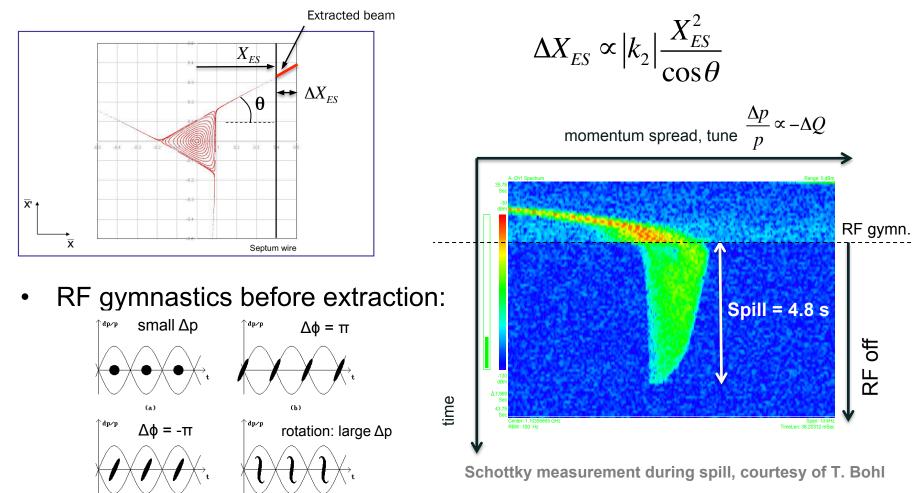
 $\Delta X_{ES} \propto \left| k_2 \right| \frac{X_{ES}^2}{\cos \theta}$

- Extraction bump trimmed in the machine to adjust the spiral step

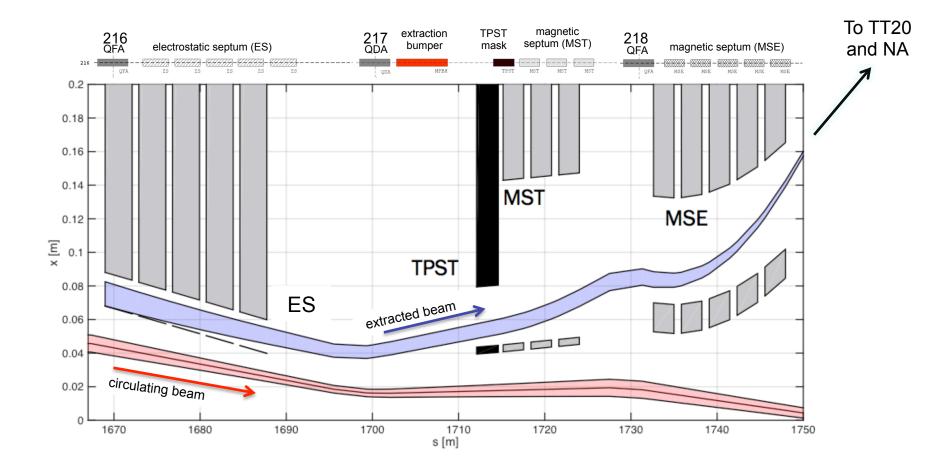


ABT

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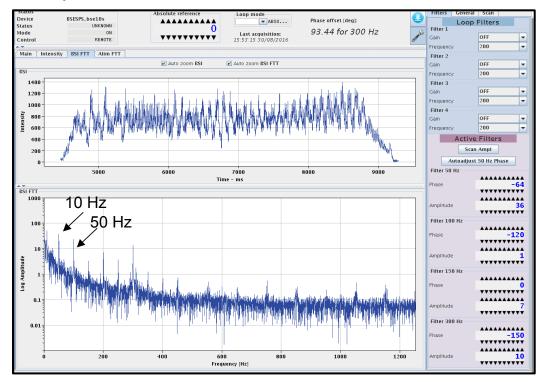


Slow extraction channel: SPS



Slow extracted spill quality

- The slow-extraction is a resonant process and it amplifies the smallest imperfections in the machine:
 - e.g. spill intensity variations can be explained by ripples in the current of the quads (mains: n x 50 Hz) at the level of a few ppm!
 - Injection of *n* x 50 Hz signals in counter-phase on dedicated quads can be used to compensate

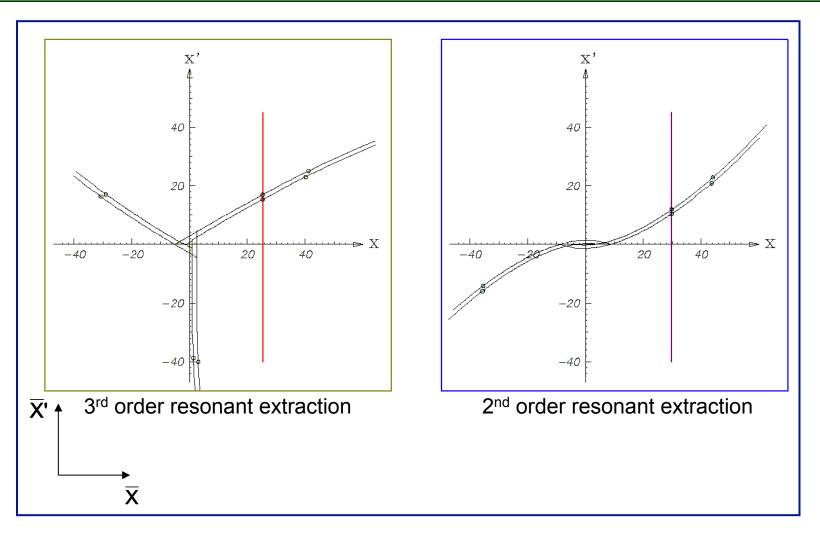


A recent example of a spill at SPS to the North Area with large n x 50 Hz components and another noise source at 10 Hz

Second-order resonant extraction

- An extraction can also be made over a few hundred turns
- 2nd and 4th order resonances
 - Octupole fields distort the regular phase space particle trajectories
 - Stable area defined, delimited by two unstable Fixed Points
 - Beam tune brought across a 2^{nd} order resonance (Q $\rightarrow 0.5$)
 - Particle amplitudes quickly grow and beam is extracted in a few hundred turns

Resonant extraction separatrices



- Amplitude growth for 2nd order resonance much faster than 3rd shorter spills (≈milliseconds vs. seconds)
- Used where intense pulses are required on target e.g. neutrino production

Extraction - summary

- Several different techniques:
 - Single-turn fast extraction:
 - for Boxcar stacking (transfer between machines in accelerator chain), beam abort
 - Non-resonant (fast) multi-turn extraction
 - slice beam into equal parts for transfer between machine over a few turns.
 - Resonant low-loss (fast) multi-turn extraction
 - create stable islands in phase space: slice off over a few turns.
 - Resonant (slow) multi-turn extraction
 - create stable area in phase space ⇒ slowly drive particles into resonance ⇒ long spill over many thousand turns.

Thank you for your attention

Appendix

Blow-up from steering error

• The new particle coordinates in normalised phase space are:

$$\overline{X}_{error} = \overline{X}_0 + L\cos\theta$$

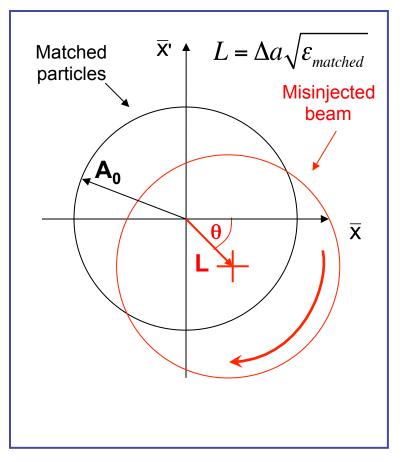
$$\overline{X}'_{error} = \overline{X}'_0 + L\sin\theta$$

 For a general particle distribution, where A_i denotes amplitude in normalised phase of particle i:

$$\mathbf{A}_{i}^{2} = \bar{X}_{0,i}^{2} + \bar{X}'_{0,i}^{2}$$

• The emittance of the distribution is:

$$\varepsilon_{matched} = \left\langle \mathbf{A}_i^2 \right\rangle / 2$$



Blow-up from steering error

• So we plug in the new coordinates:

