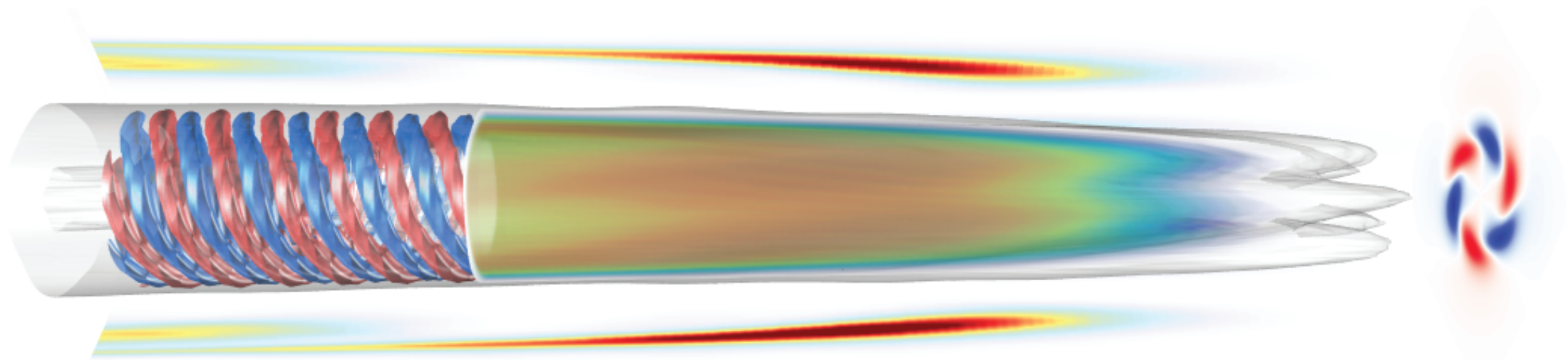


Plasma accelerators driven by exotic light beams

Jorge Vieira

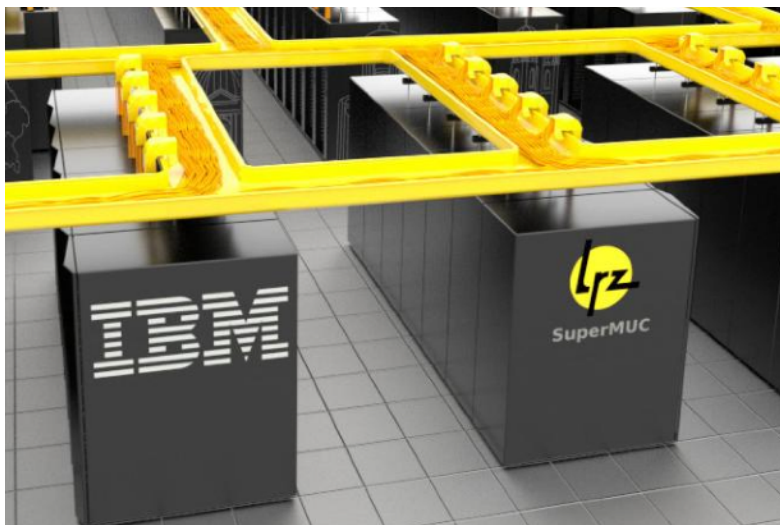
GoLP / IPFN, Instituto Superior Técnico, Lisbon, Portugal



Work in collaboration with:

M. Pardal, J.T. Mendonça, R.A. Fonseca, L.O. Silva (IST); **E.P.Alves** (SLAC)
F. Quéré (CEA); **R. Bingham, R. Trines** (RAL,STFC), **Y. Shi, R. Kingham** (Imperial College)

Simulation results obtained at the SuperMUC supercomputer in Garching, Germany.





Committed to open science

Open-access model

- 40+ research groups worldwide are using OSIRIS
- 300+ publications in leading scientific journals
- Large developer and user community
- Detailed documentation and sample inputs files available

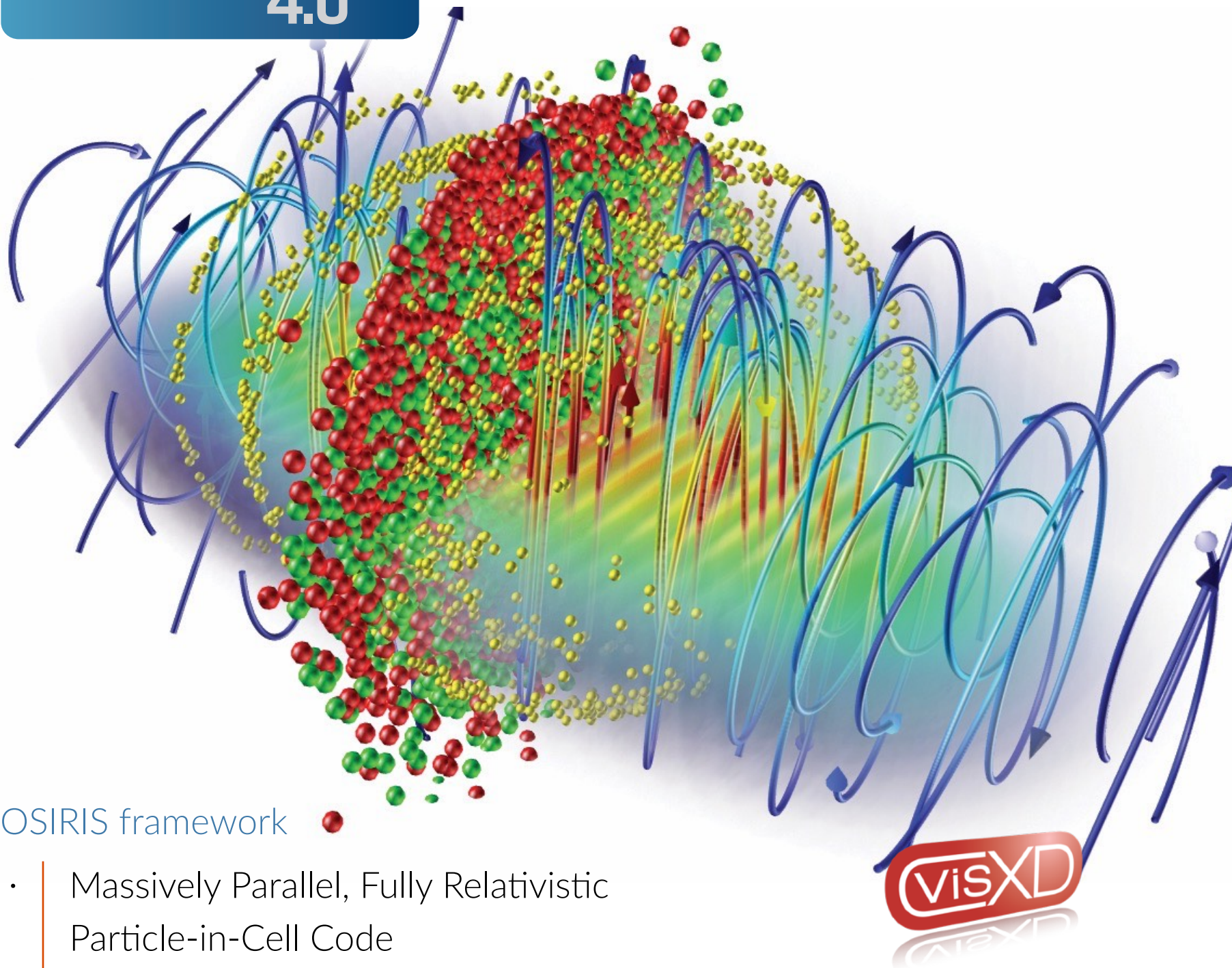
Using OSIRIS 4.0

- The code can be used freely by research institutions after signing an MoU
- Find out more at:

<http://epp.tecnico.ulisboa.pt/osiris>

OSIRIS framework

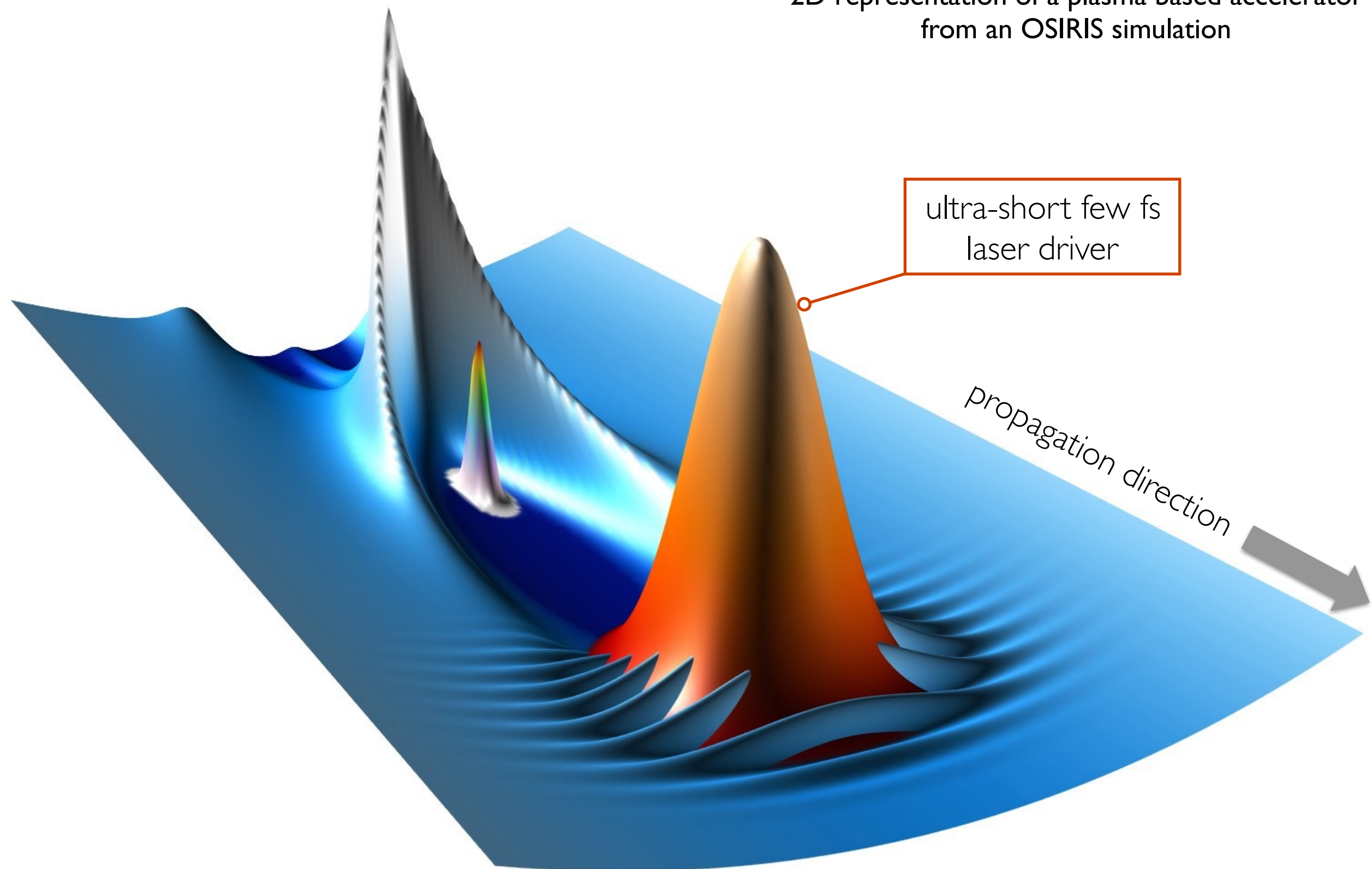
- Massively Parallel, Fully Relativistic Particle-in-Cell Code
- Parallel scalability to 2 M cores
- Explicit SSE / AVX / QPX / Xeon Phi / CUDA support
- Extended simulation/physics models



Ricardo Fonseca: ricardo.fonseca@tecnico.ulisboa.pt

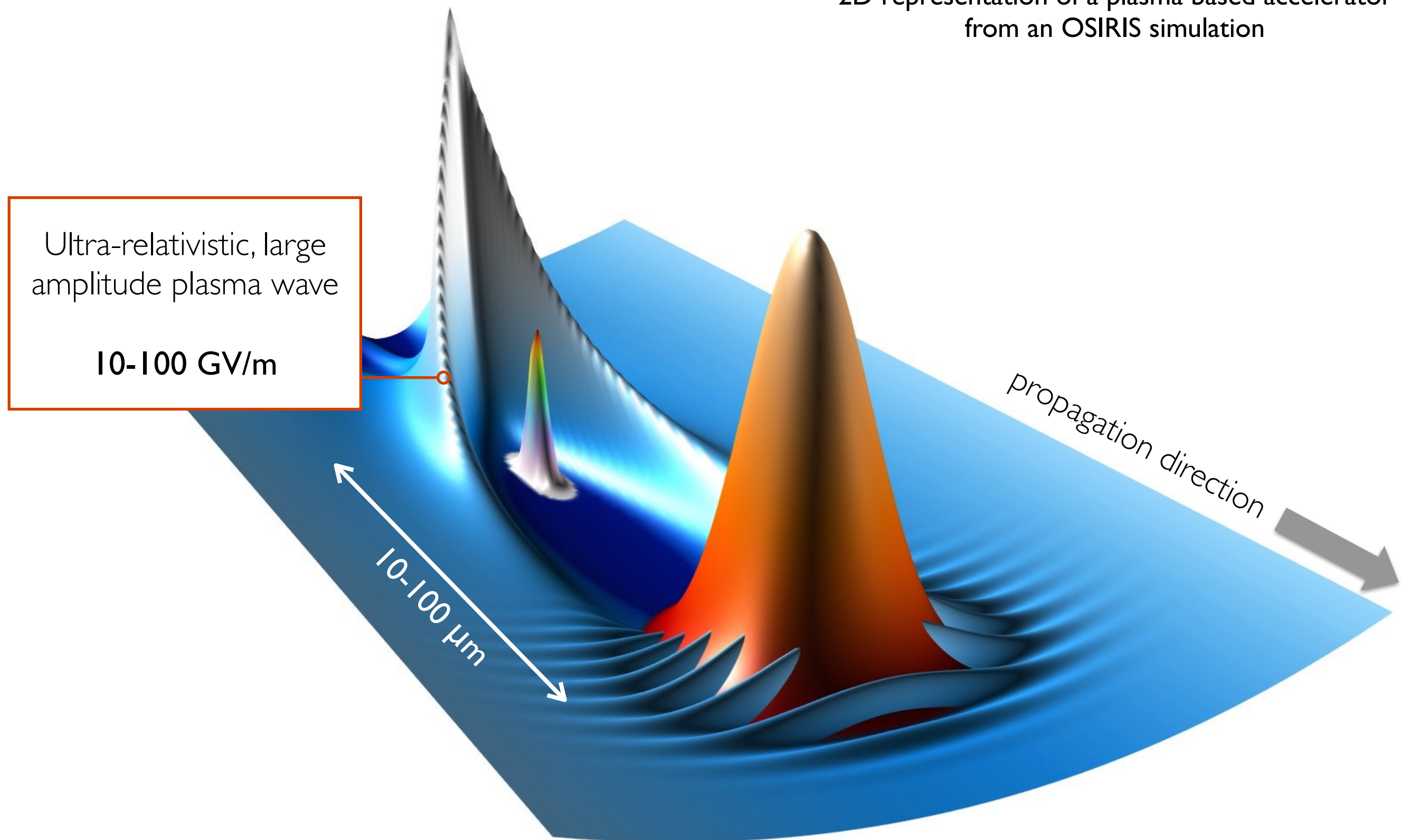
How do plasma accelerators work?

2D representation of a plasma based accelerator
from an OSIRIS simulation



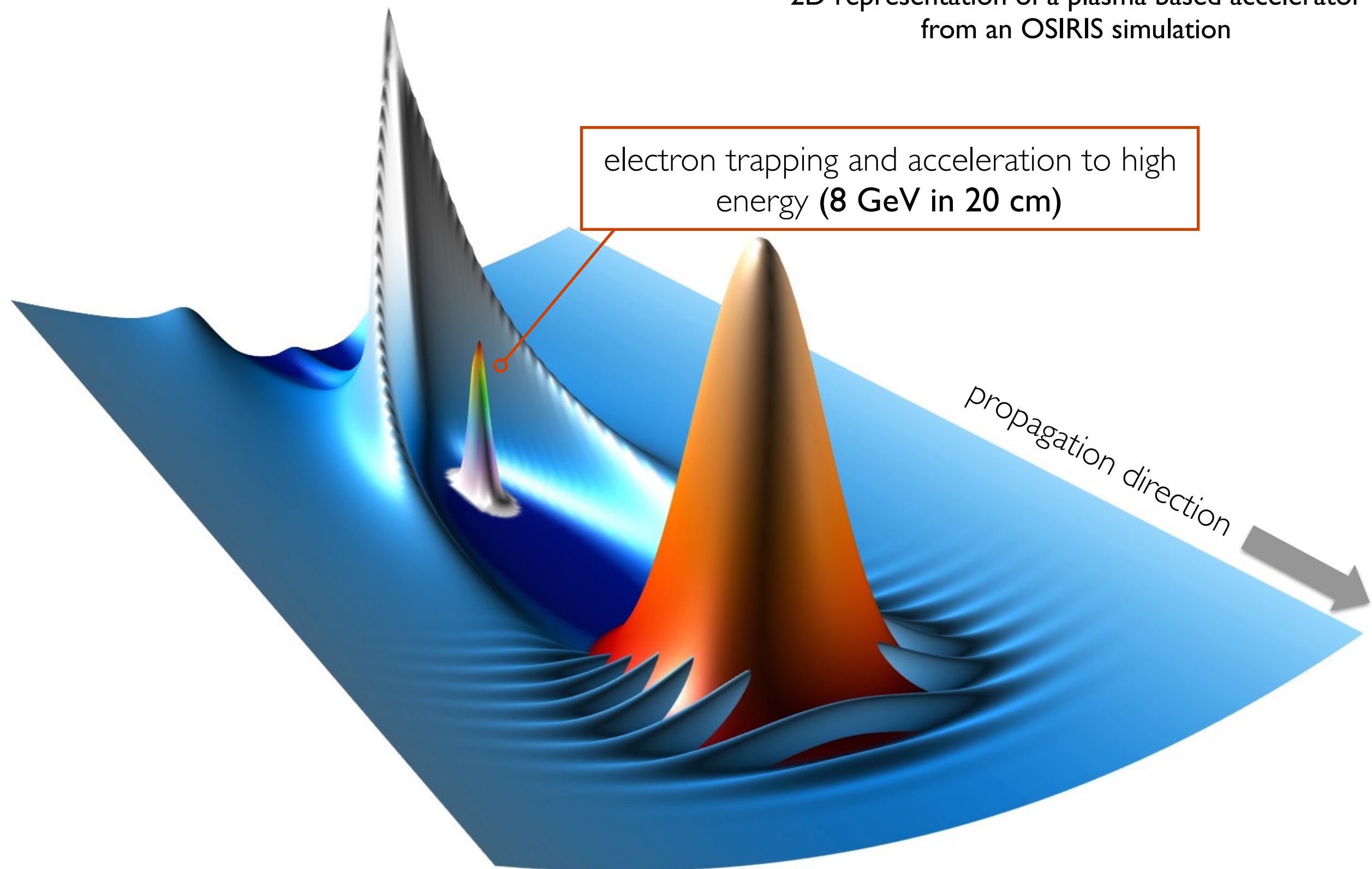
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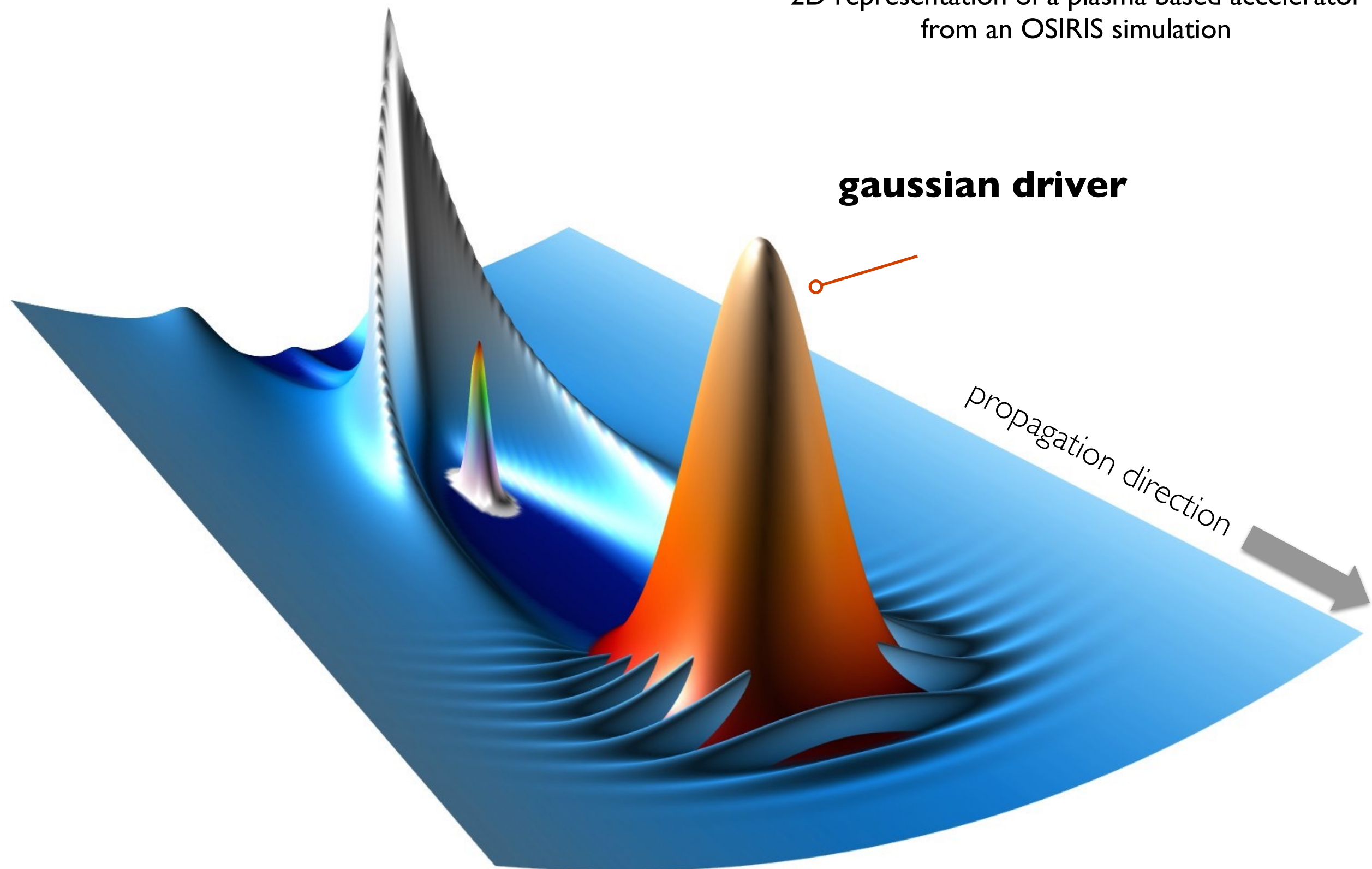
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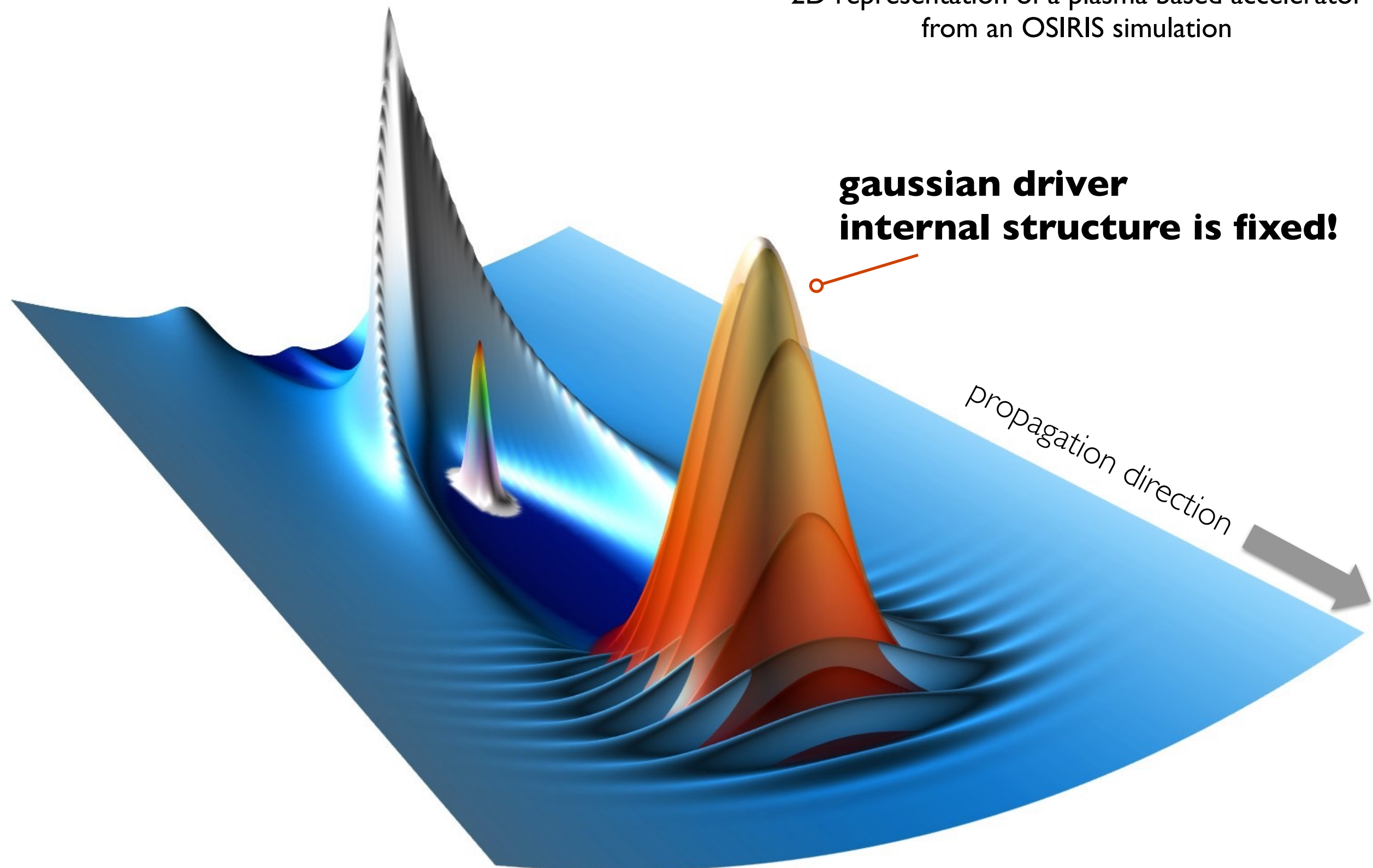
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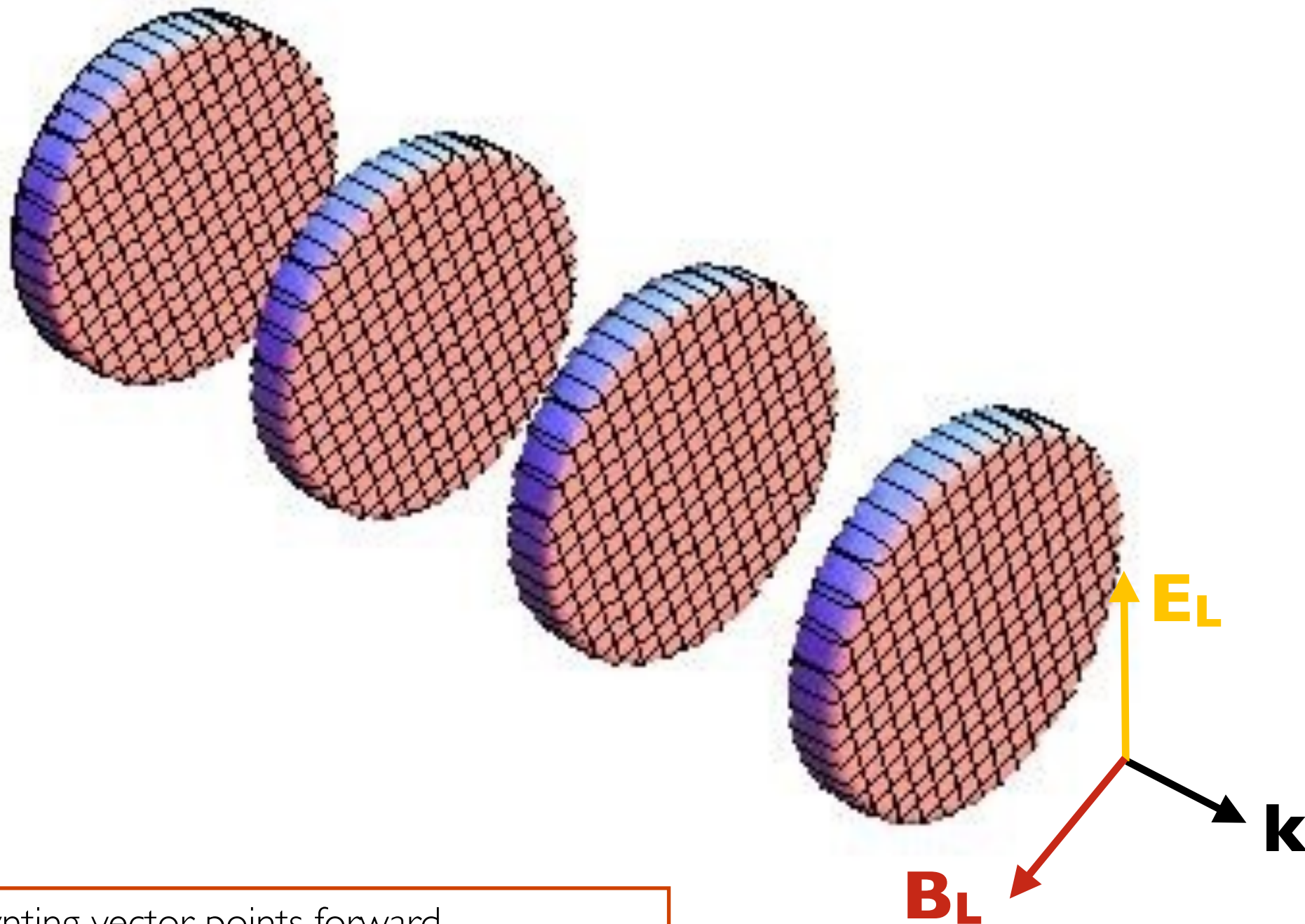
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The Orbital Angular Momentum (OAM) of light

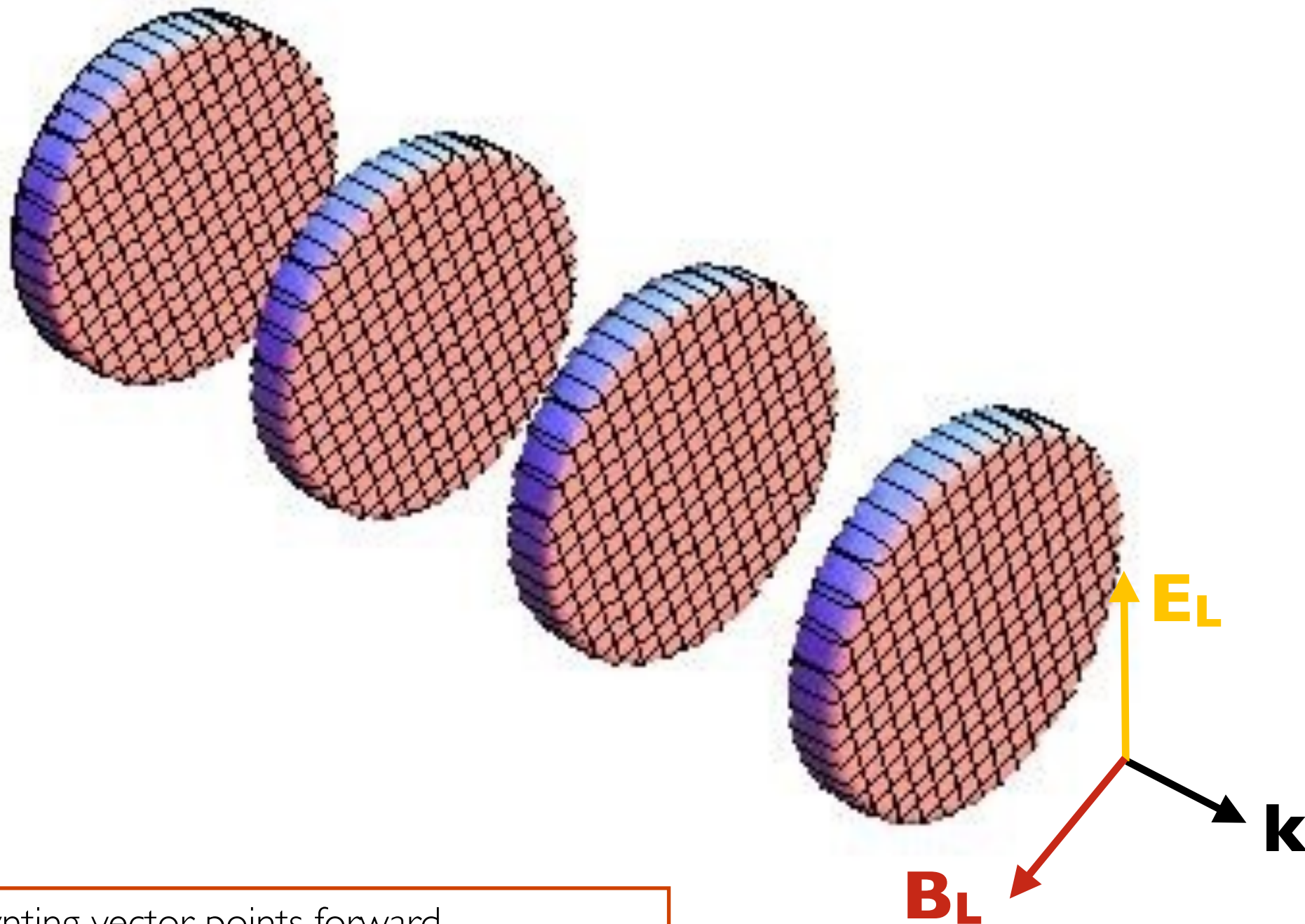
representation of a *plane wave*



Poynting vector points forward
Transfer *linear* momentum to matter: **optical tweezers**

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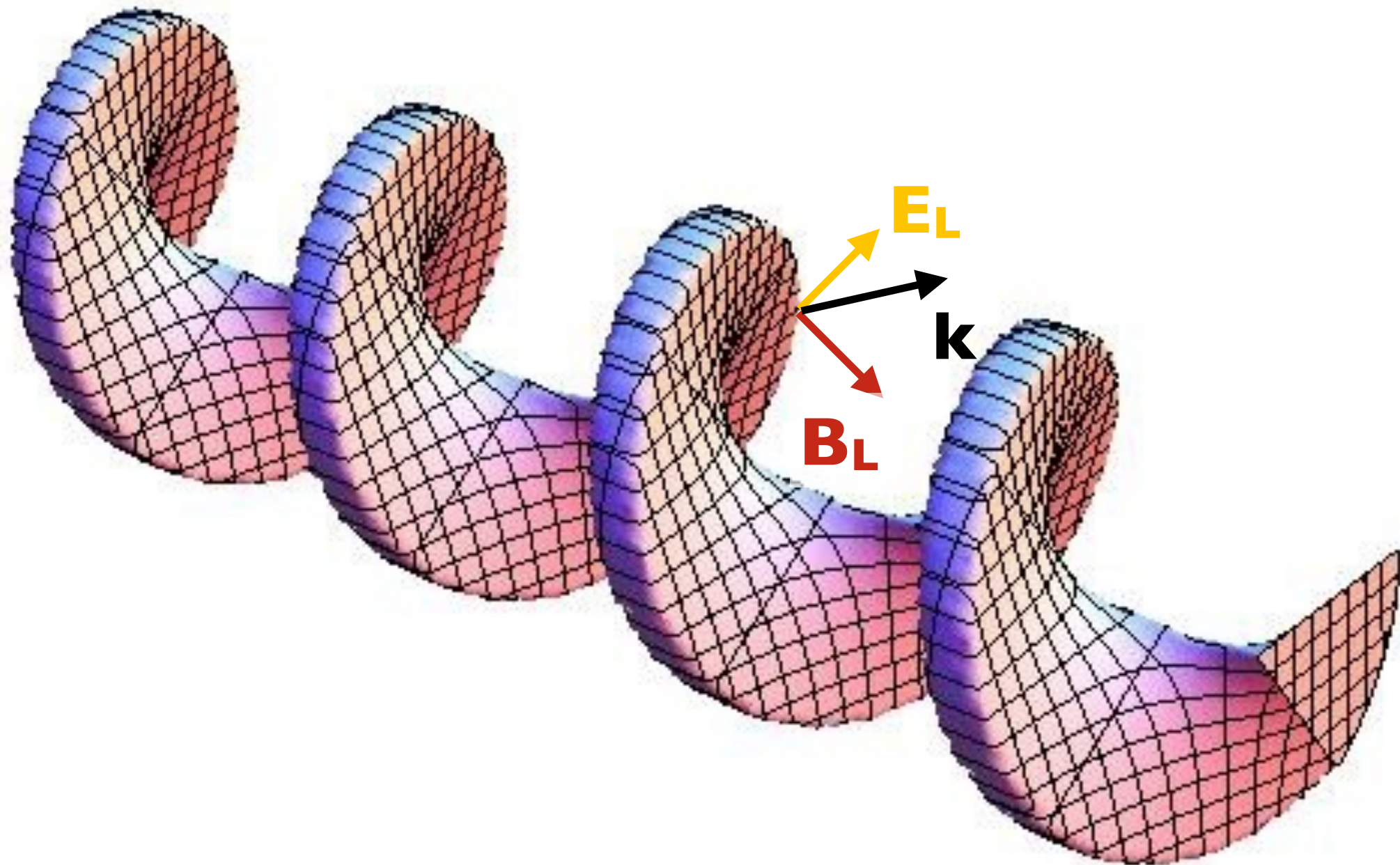
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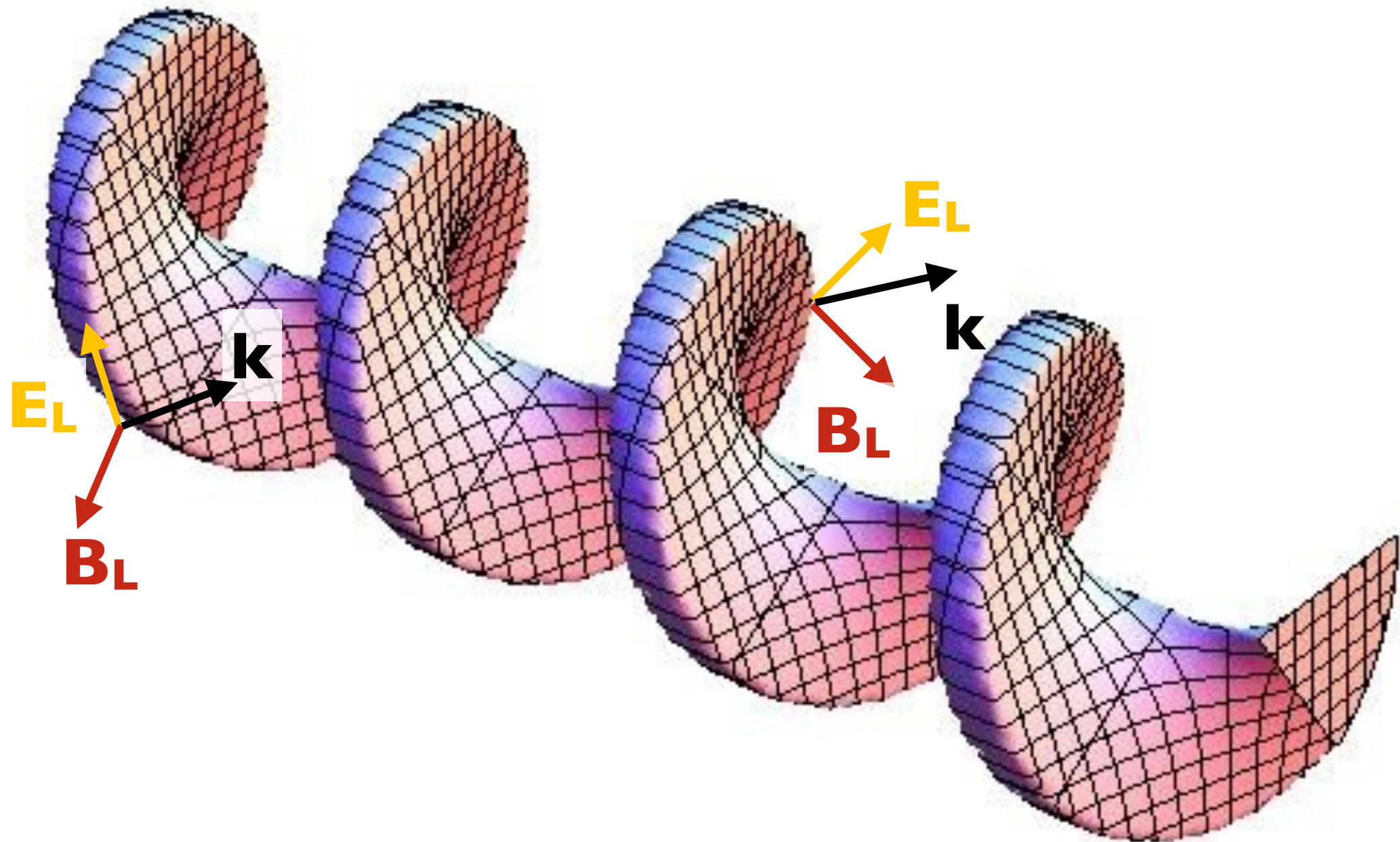
The Orbital Angular Momentum (OAM) of light

representation of a *twisted* wave



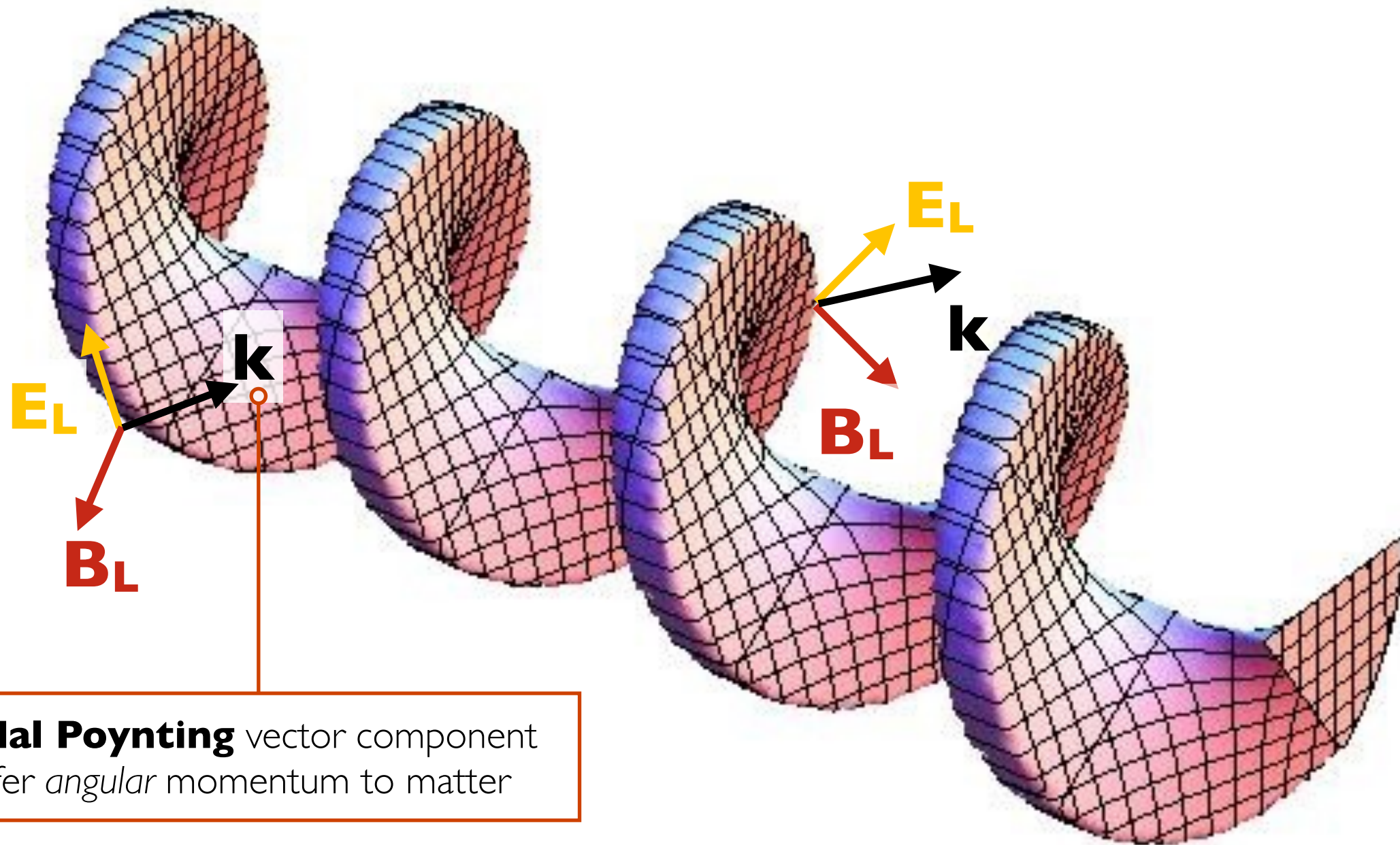
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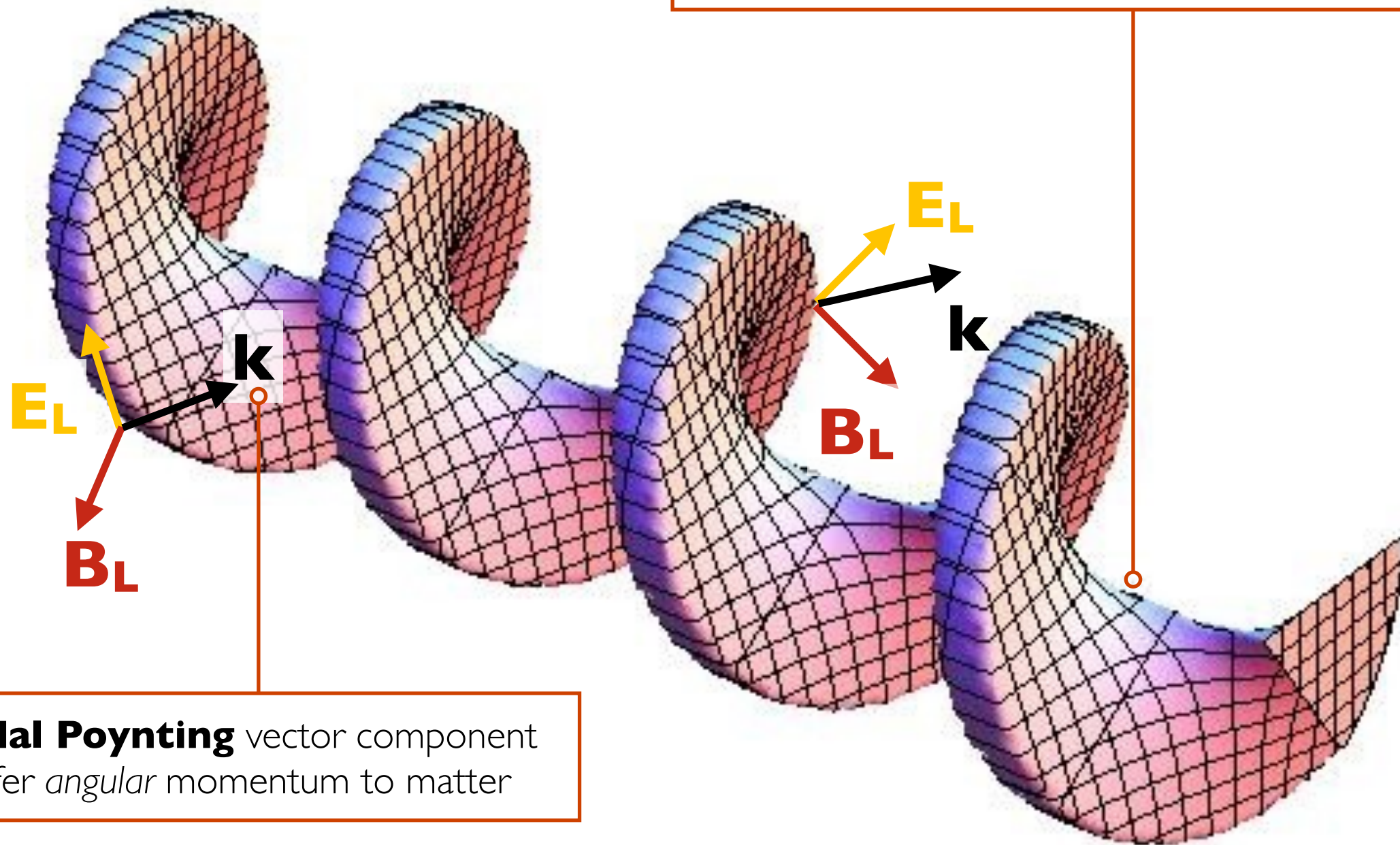
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The Orbital Angular Momentum (OAM) of light

representation of a *twisted* wave

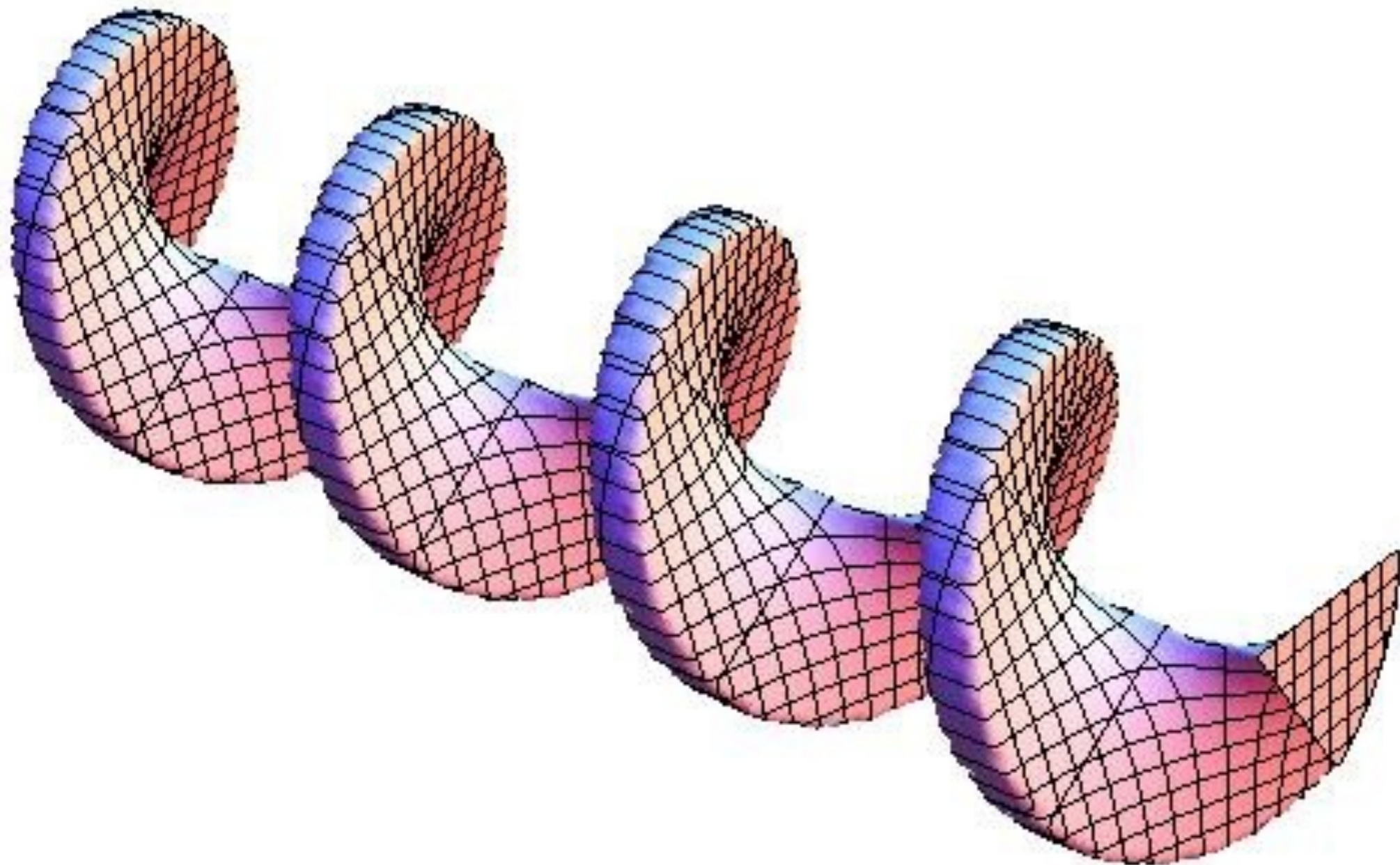
Phase singularity on axis - doughnut intensity profile
Higher order Laguerre-Gaussian modes



Poloidal Poynting vector component
Transfer *angular* momentum to matter

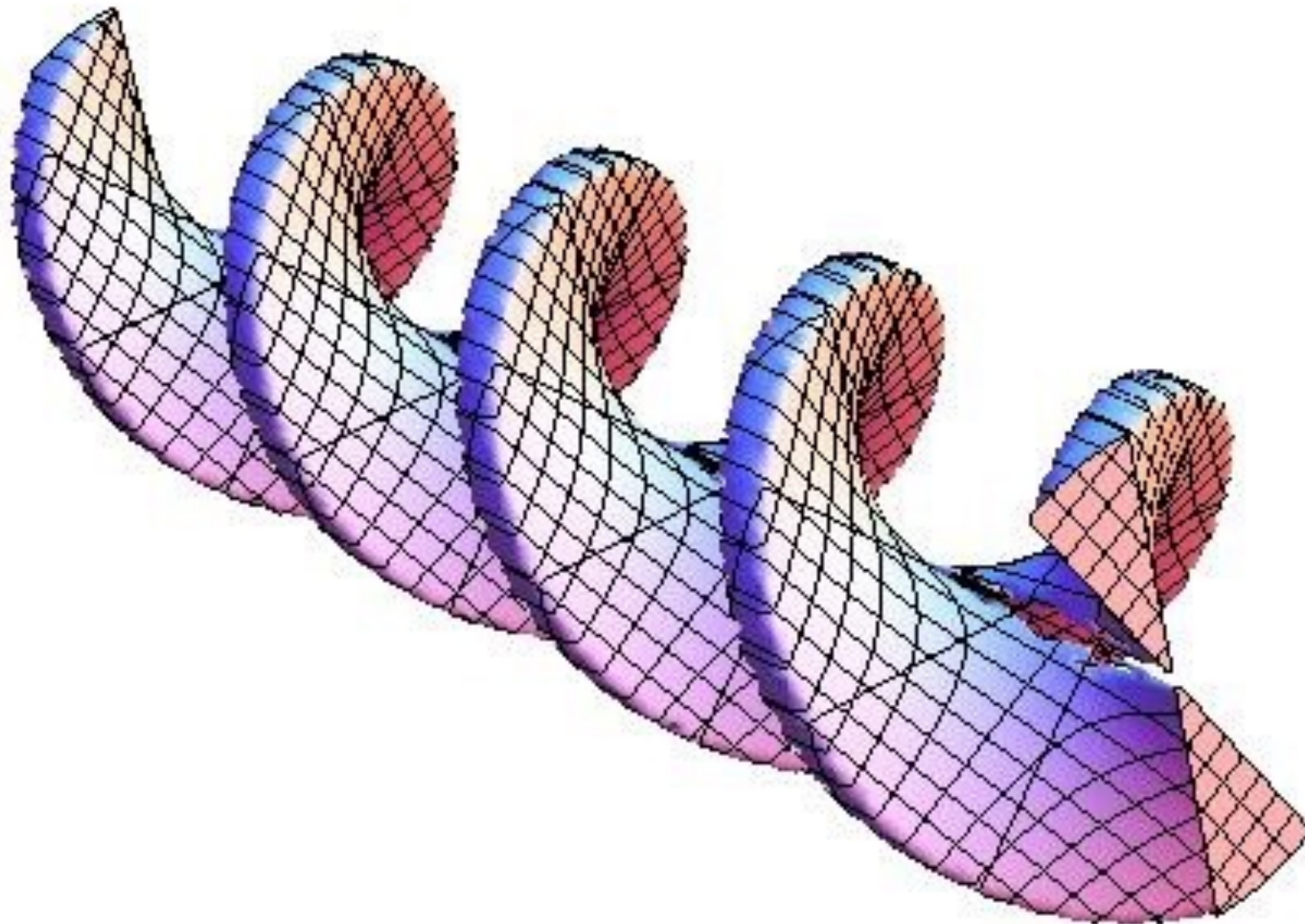
The Orbital Angular Momentum (OAM) of light

representation of a *twisted* wave **I helix - OAM (ℓ) is I**



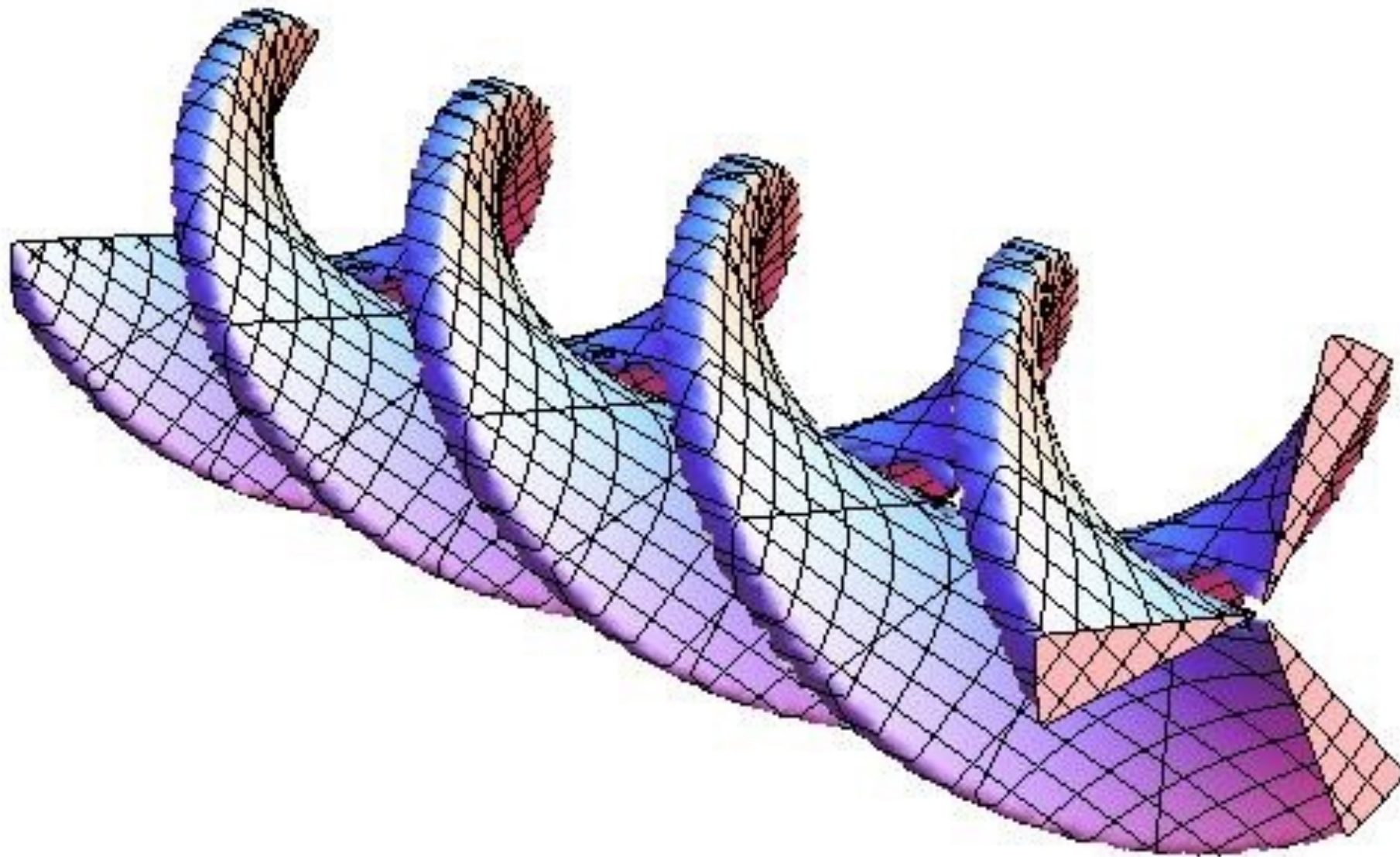
The orbital angular momentum of light

representation of a *twisted* wave **2 helixes - OAM (ℓ) is 2**



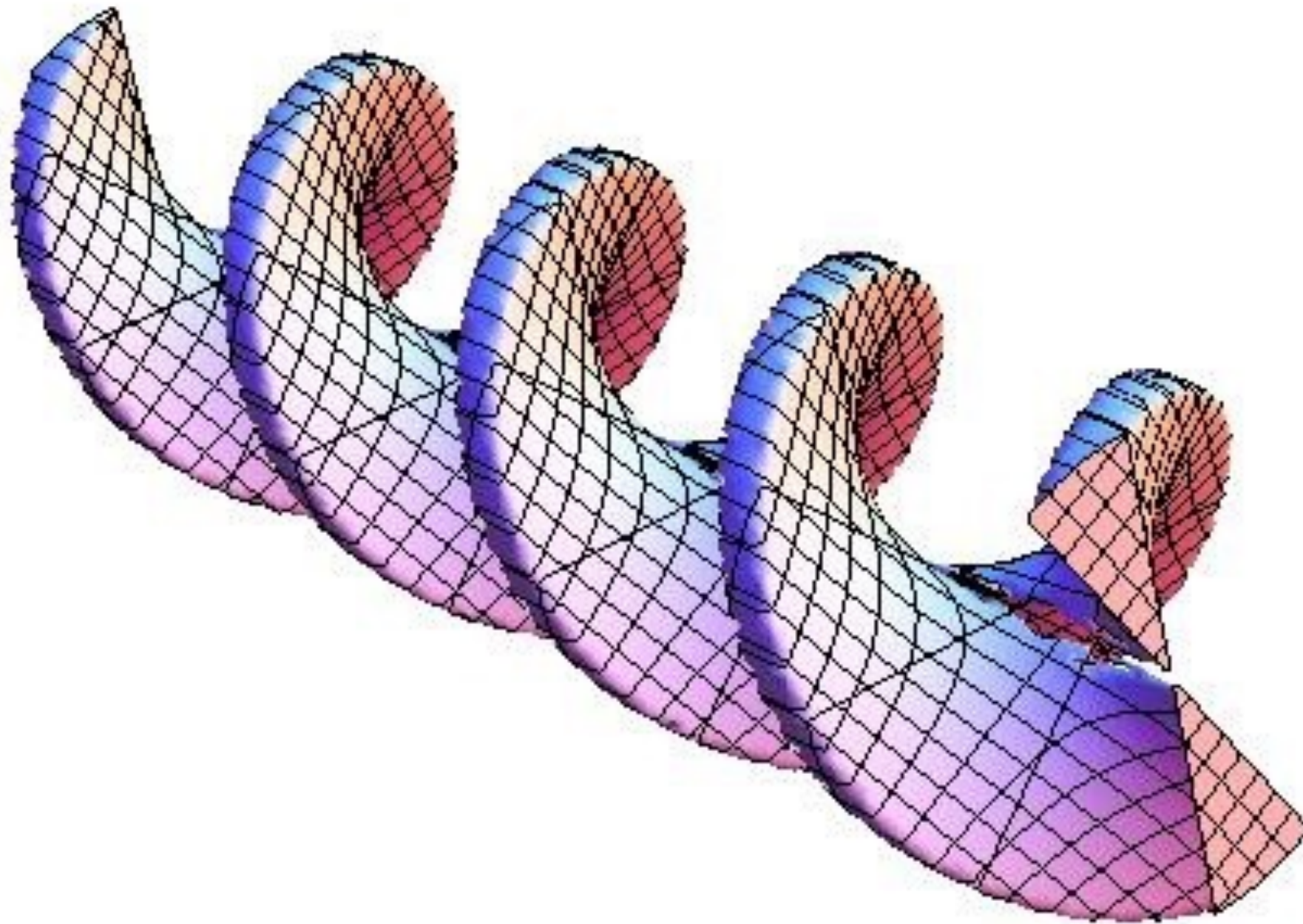
The orbital angular momentum of light

representation of a *twisted* wave **3 helixes - OAM (ℓ) is 3**



The orbital angular momentum of light

representation of a *twisted* wave **2 helixes - OAM (ℓ) is 2**



Interesting examples of double helixes

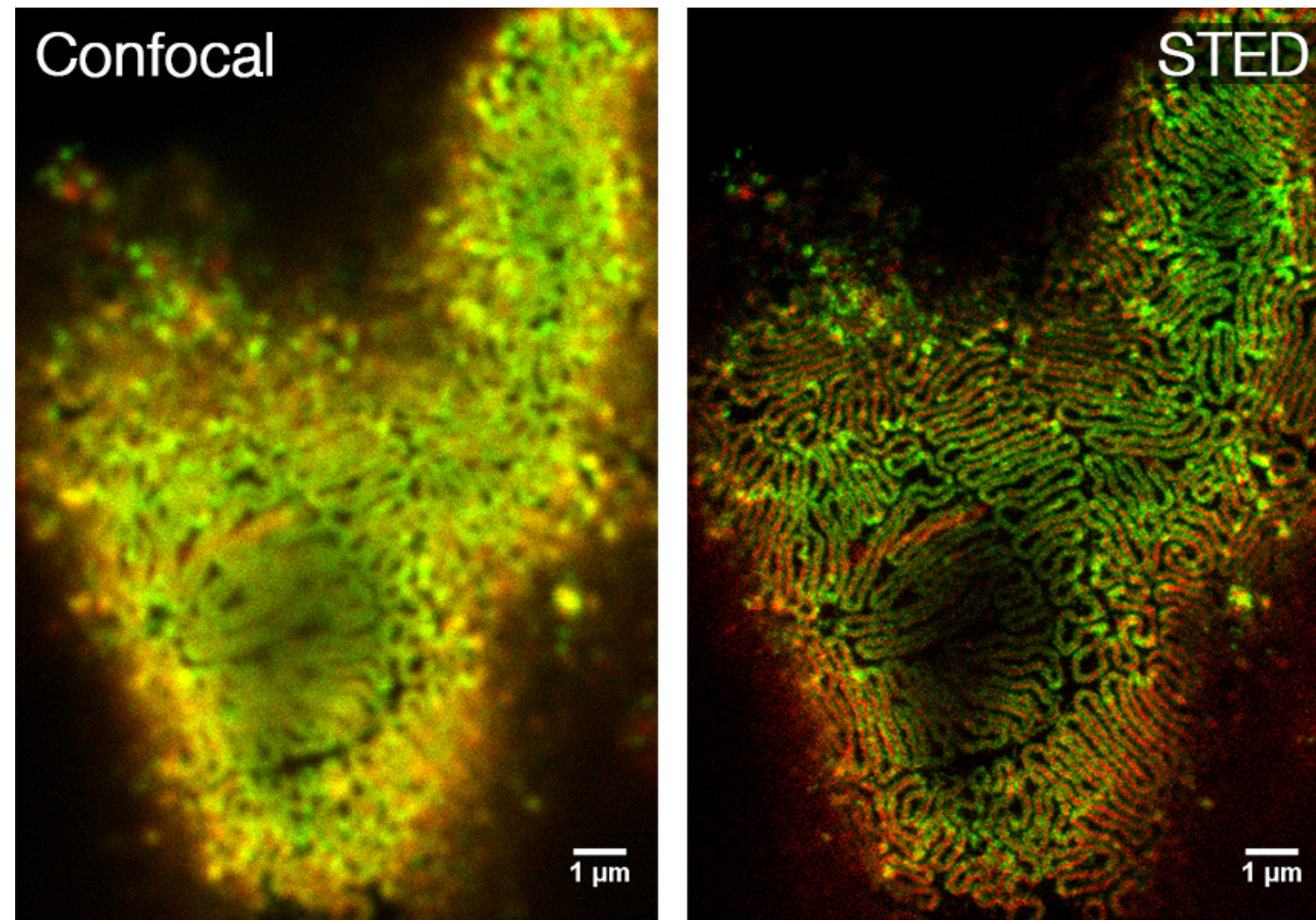
Interesting examples of double helixes



Interesting examples of double helixes

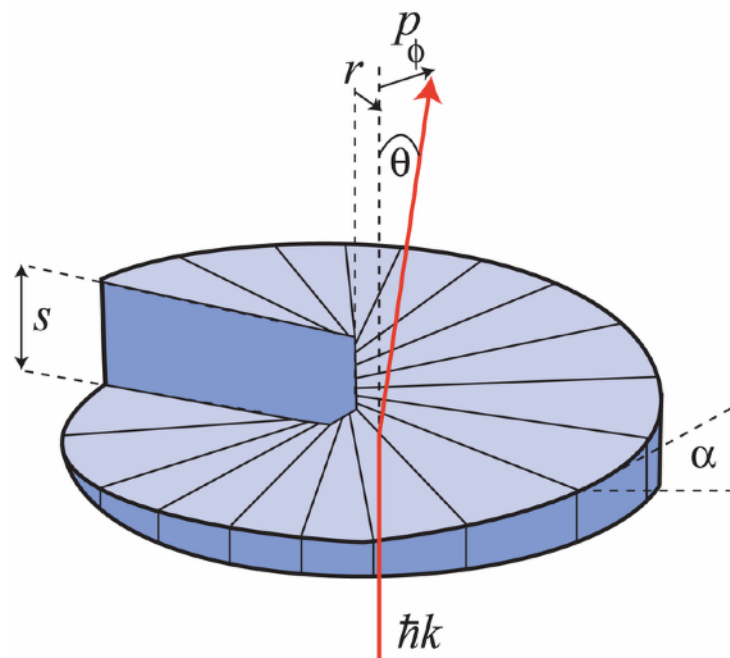


Super-resolution microscopy is a notable example where OAM beams revolutionised science and technology [S. Hell et al. Optics Lett. 19, 780-782 (1994)]

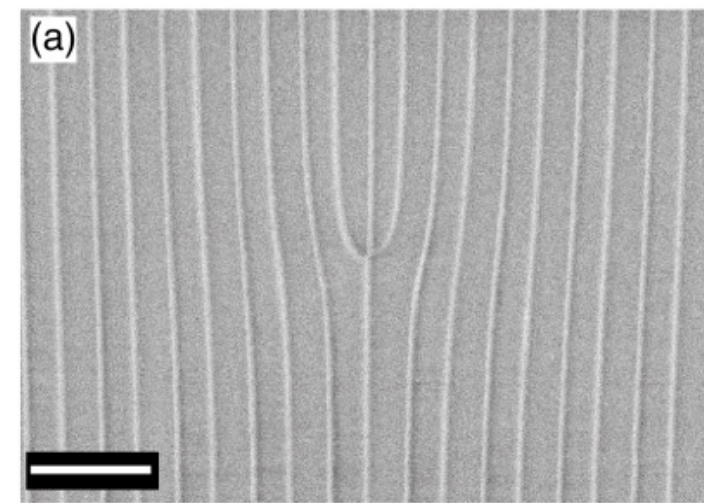


- **Optical communications** TB/s data transfer in free space [J. Wang et al. Nat. Ph. 6 488 (2012)]
- **Quantum computing** Very large base of entangled states [A. Mair et al., Nature 412, 313 (2001)]

Spiral phase plate

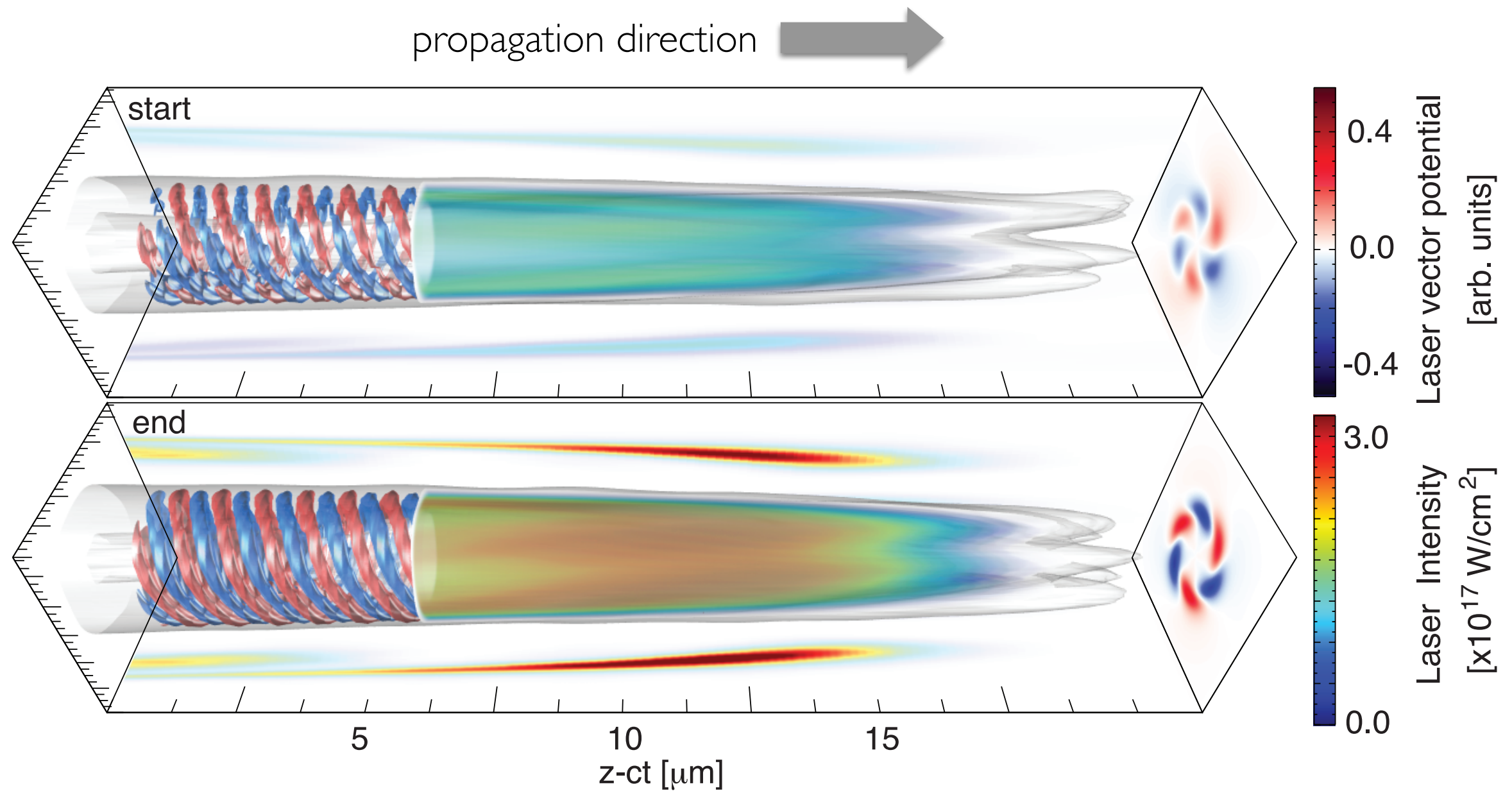


Computer generated hologram



Ultra-fast spatiotemporal beam shaping

Producing these beams at ultra-high intensity is the goal of several experimental teams



J. Vieira et al PRL 117, 265001 (2016); Nat. Comms 7:10371 (2016).

What are the key properties of **plasma wakefields driven by twisted lasers**? Can we address major open challenges with this new approach?

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Conclusions and future directions

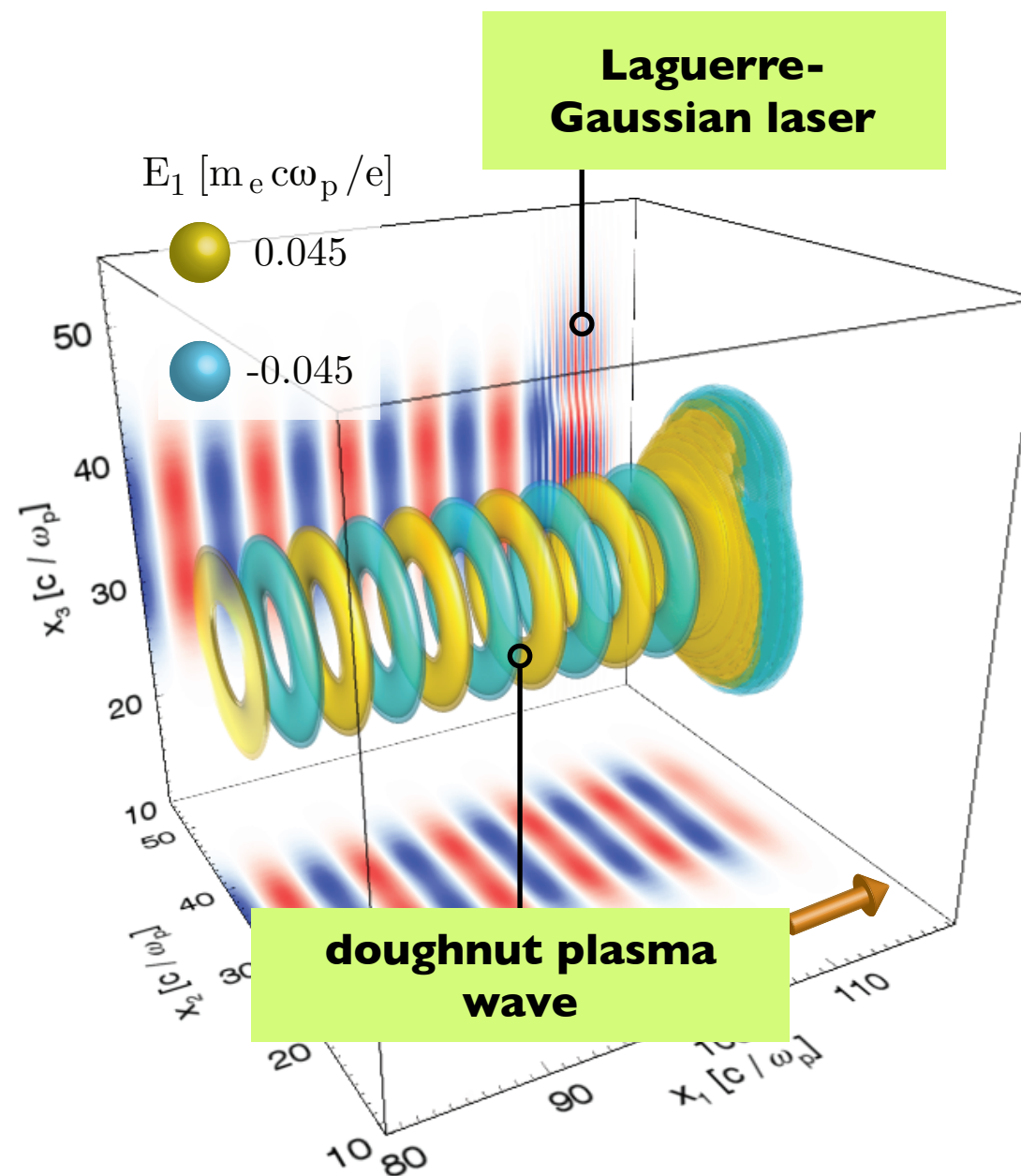
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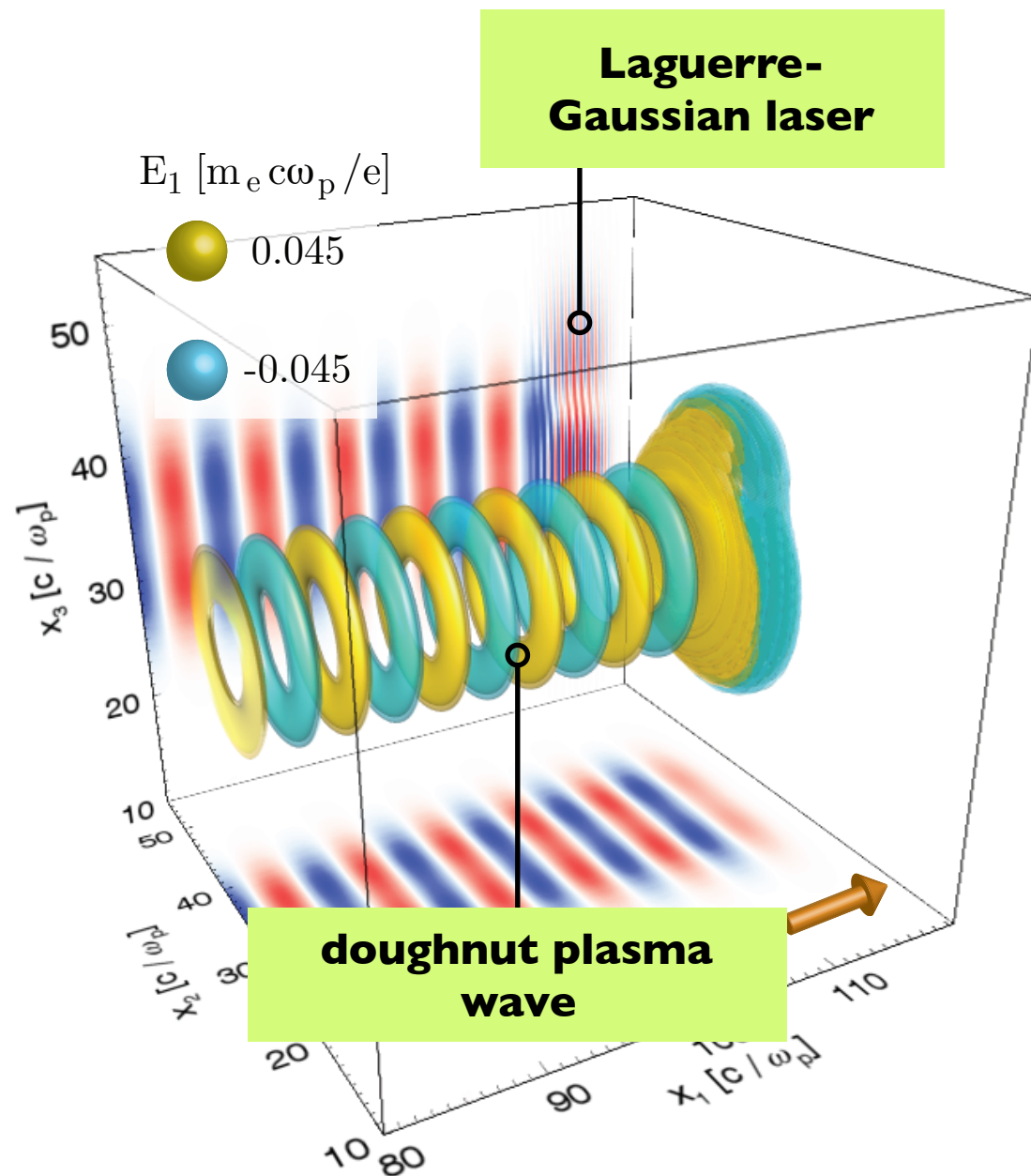
Conclusions and future directions

Linear doughnut wakefields



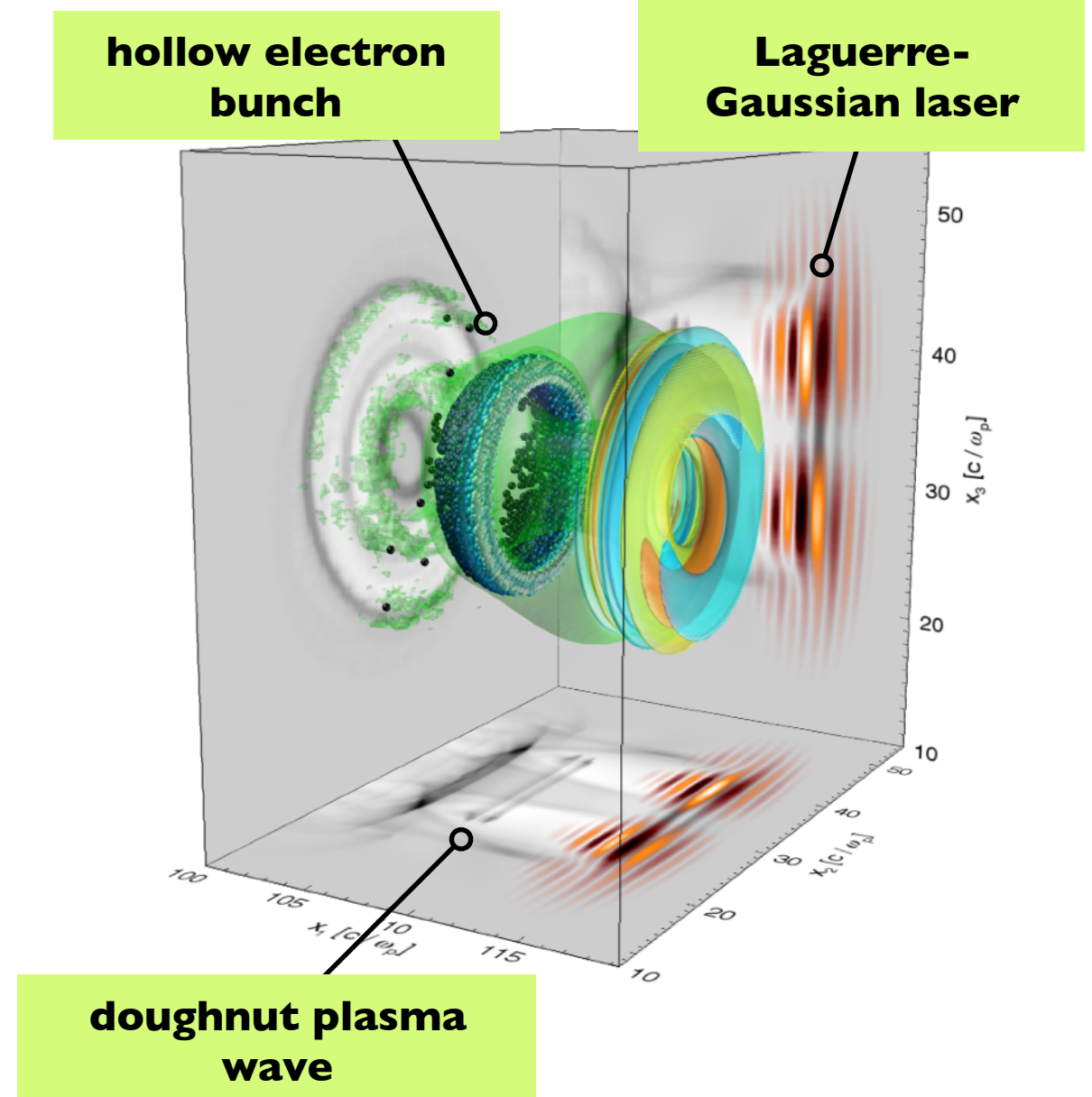
J.T. Mendonça and J.Vieira, PoP 21, 033107 (2014)

Linear doughnut wakefields



J.T. Mendonça and J.Vieira, PoP 21, 033107 (2014)

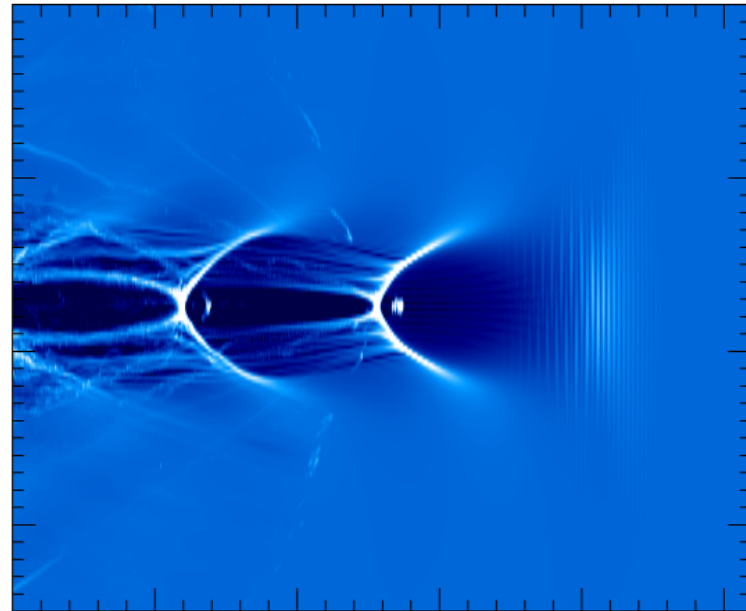
Non-linear doughnut blowout



J.Vieira and J.T. Mendonça PRL 112, 215001 (2014)

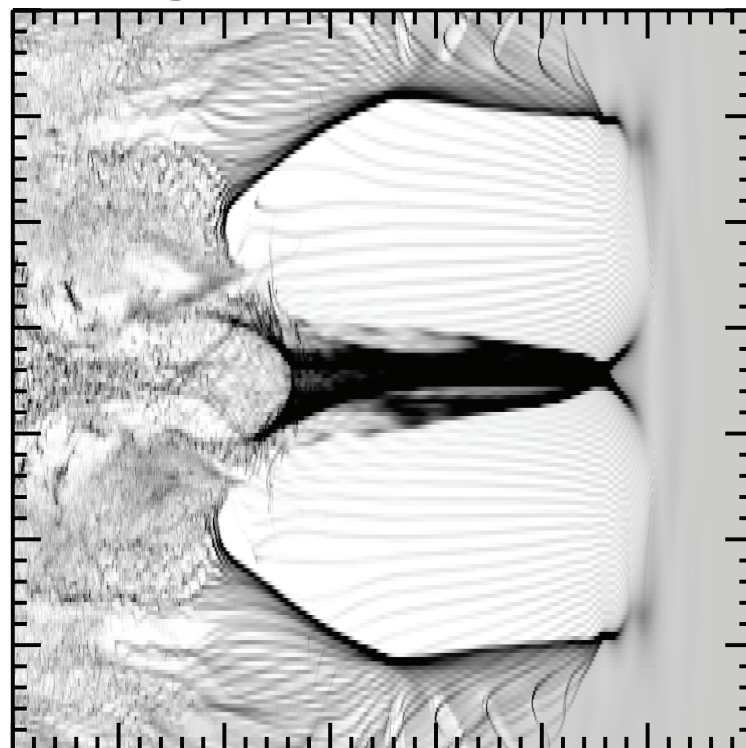
Why doughnut plasma waves are interesting: Positron acceleration in the non-linear blowout regime

conventional blowout regime



- laser expels electrons outwards
- pure ion channel focuses electrons
- positron acceleration *not possible*

doughnut plasma wave

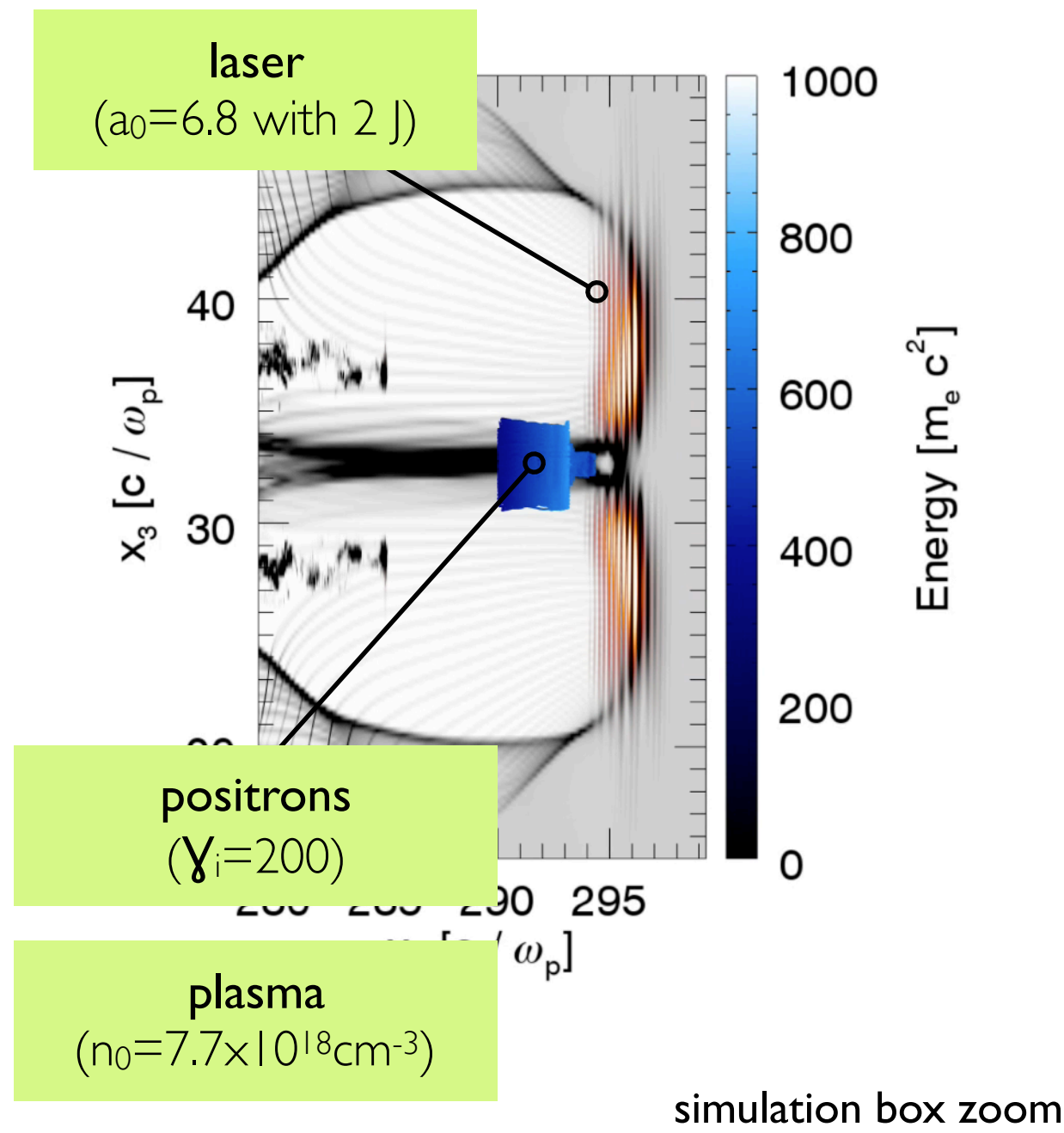


- laser pushes electrons inwards
- electron filament focuses positrons
- positron acceleration *is possible*

3D simulations show positron acceleration in strongly non-linear regimes

3D simulation of positron acceleration

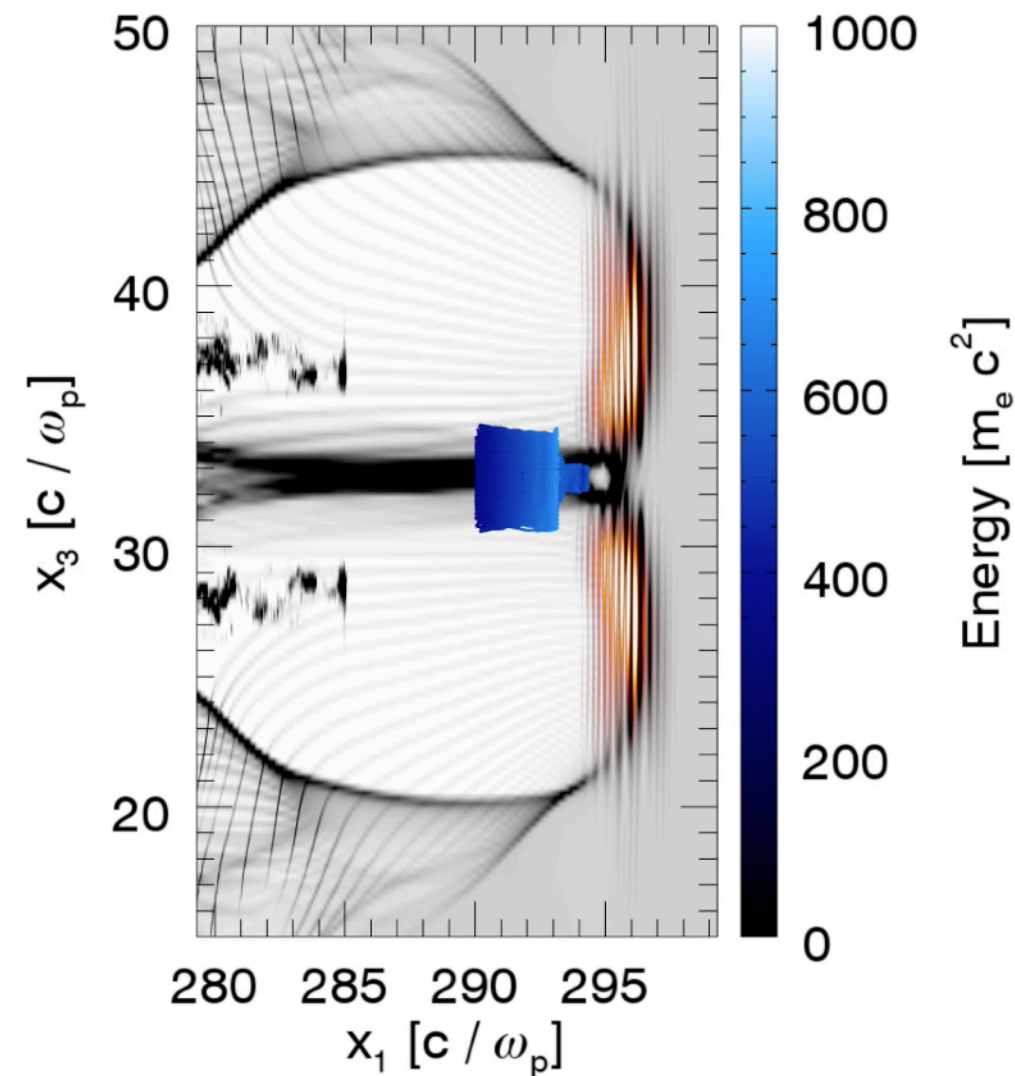
**laser and plasma parameters
within experimental reach**



3D simulations show positron acceleration in strongly non-linear regimes

3D simulation of positron acceleration

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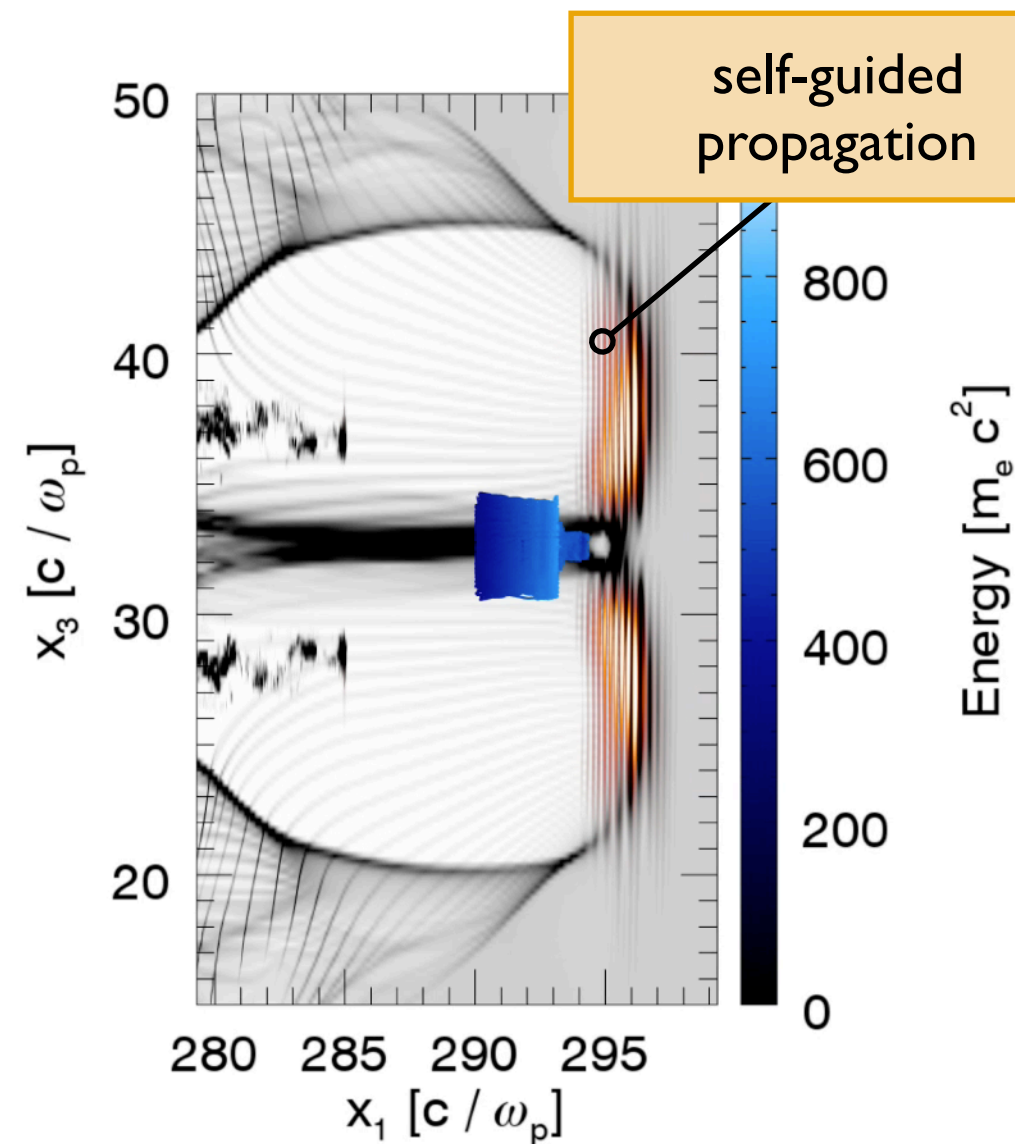


simulation box zoom

3D simulations show positron acceleration in strongly non-linear regimes

3D simulation of positron acceleration

**laser and plasma parameters
within experimental reach**

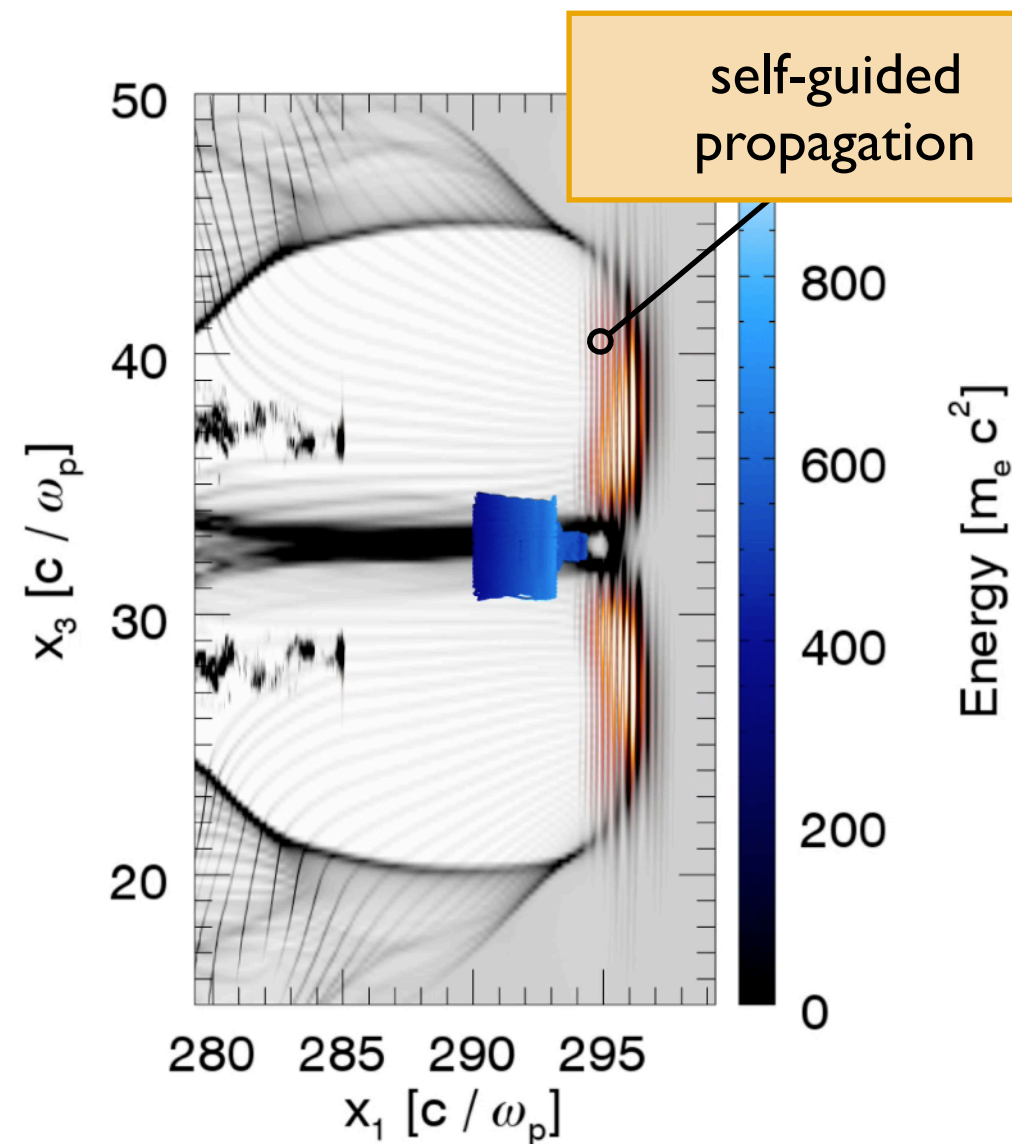


simulation box zoom

3D simulations show positron acceleration in strongly non-linear regimes

3D simulation of positron acceleration

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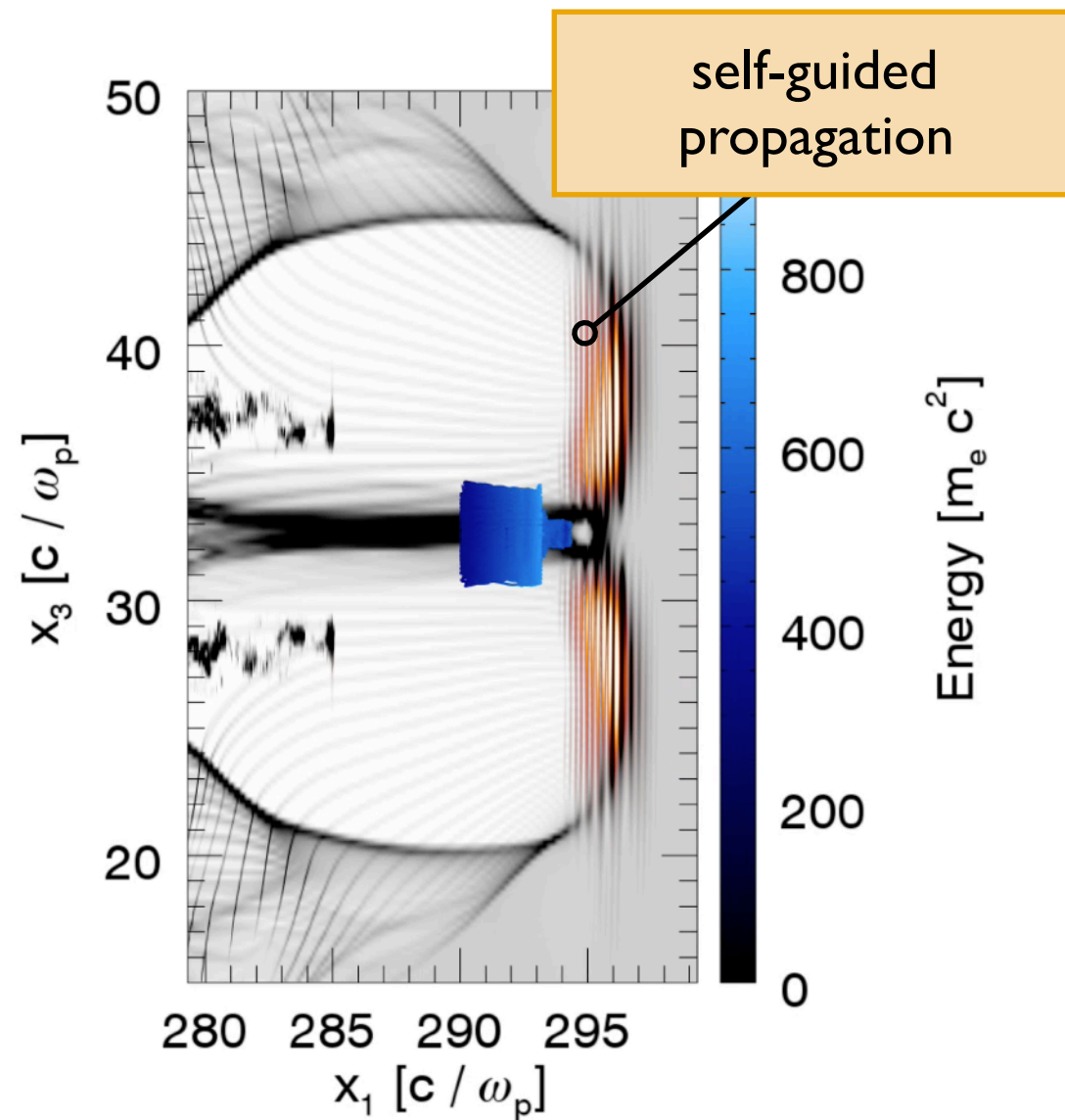


simulation box zoom

3D simulations show positron acceleration in strongly non-linear regimes

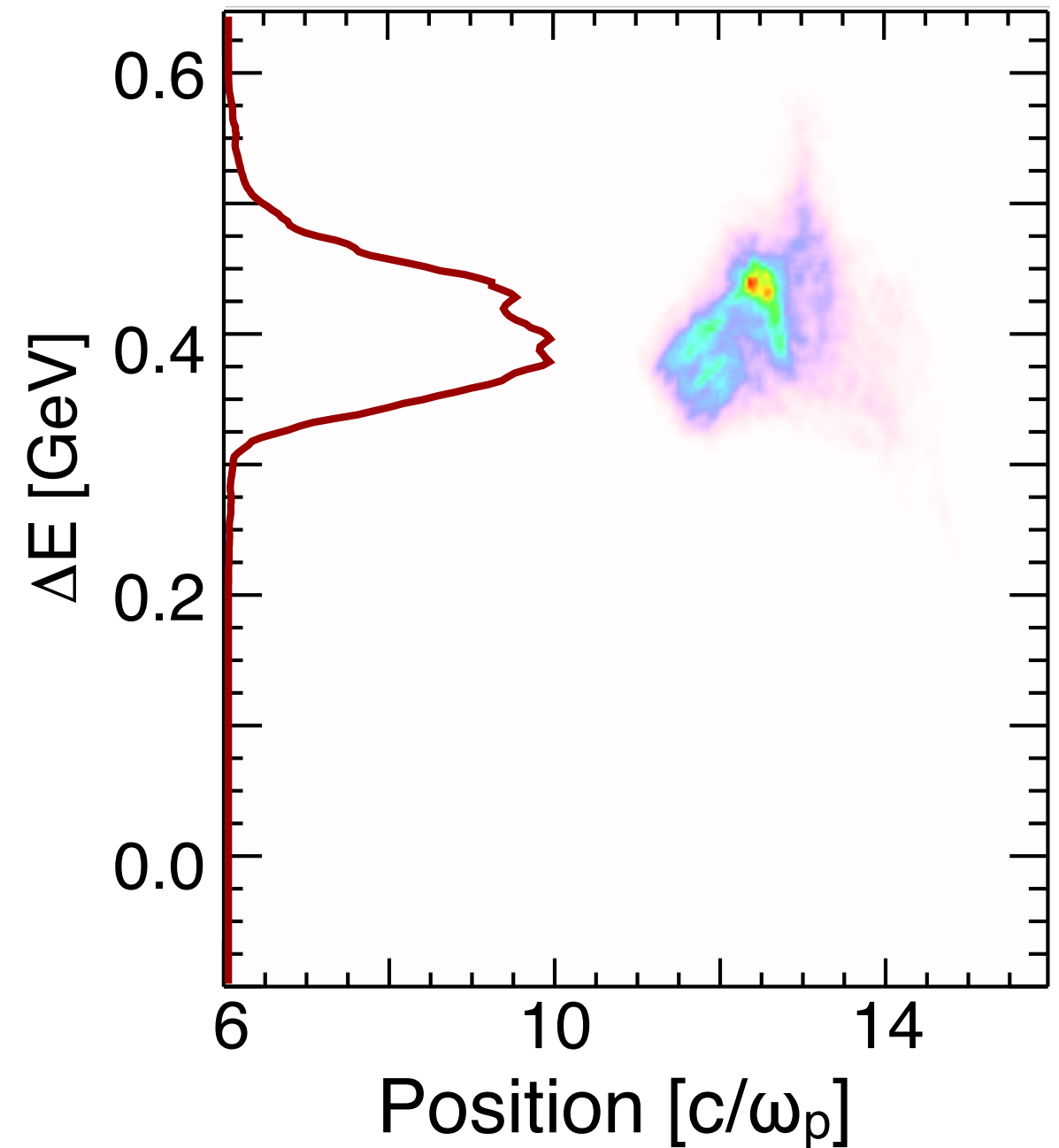
3D simulation of positron acceleration

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simulation box zoom

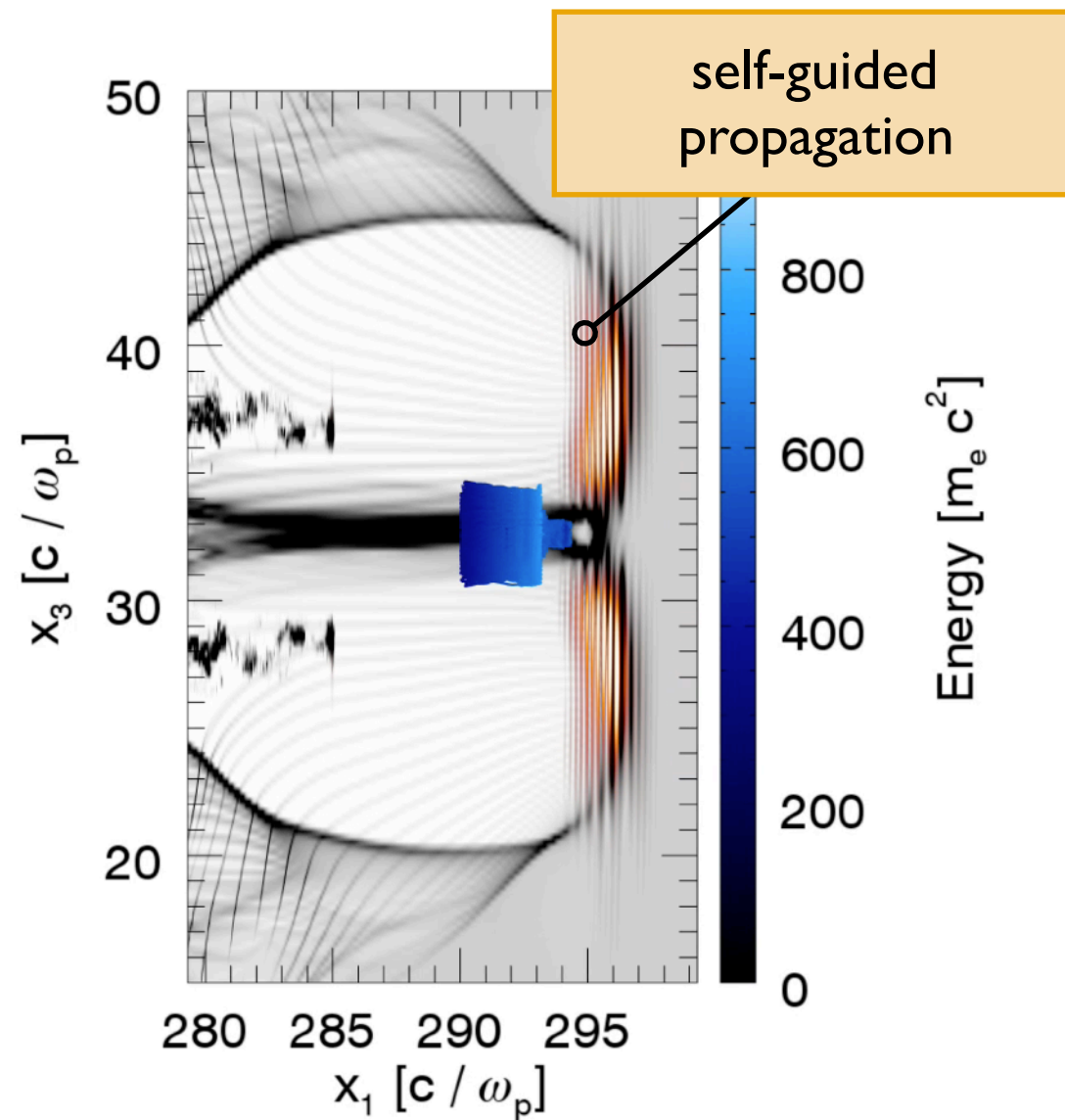
Positron bunch is quasimonoenergetic



3D simulations show positron acceleration in strongly non-linear regimes

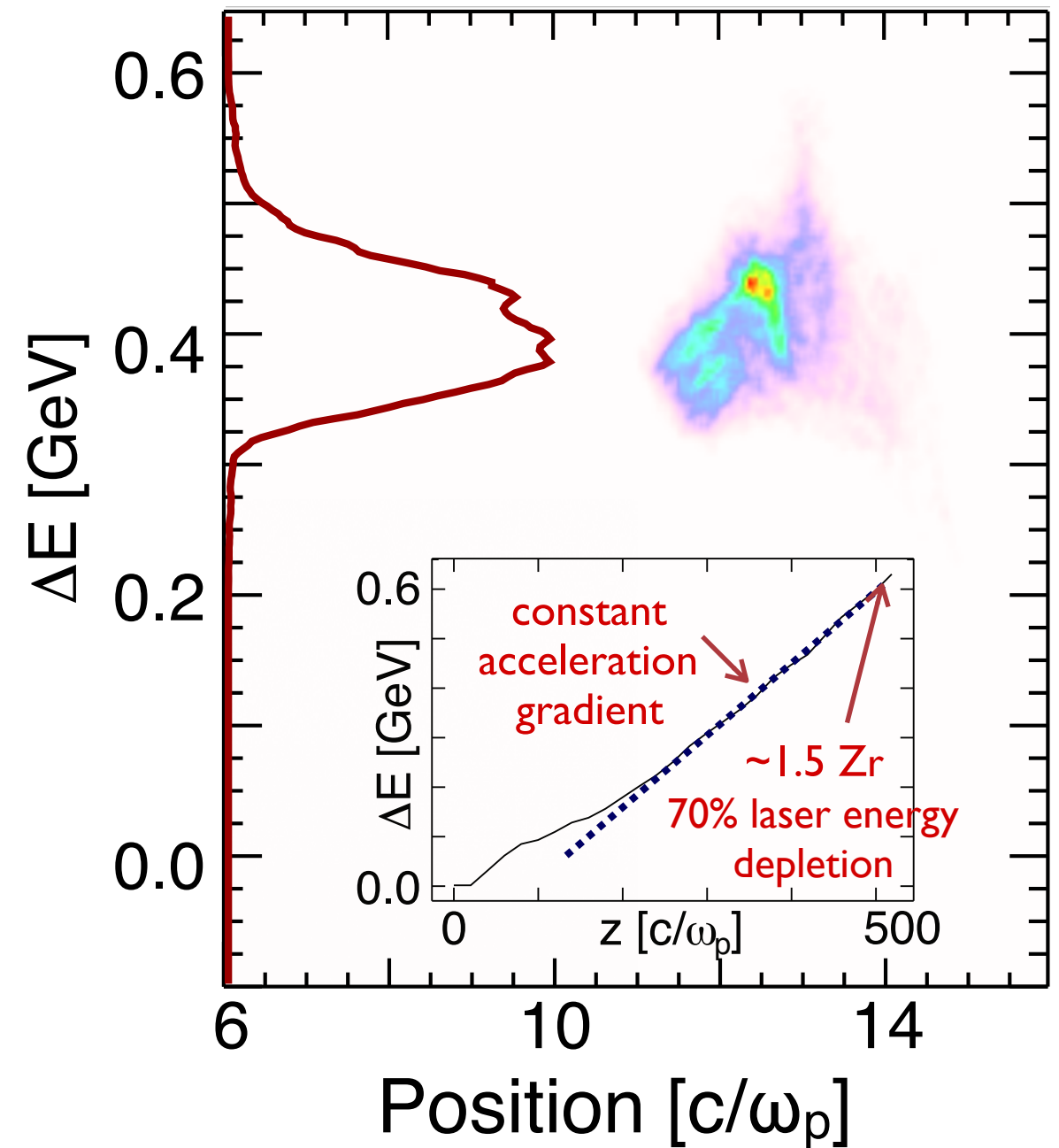
3D simulation of positron acceleration

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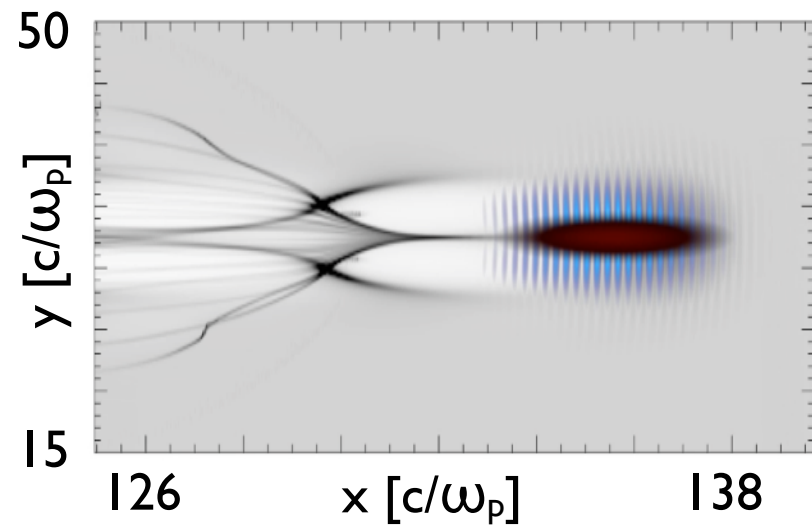
simulation box zoom

Positron bunch is quasimonoenergetic



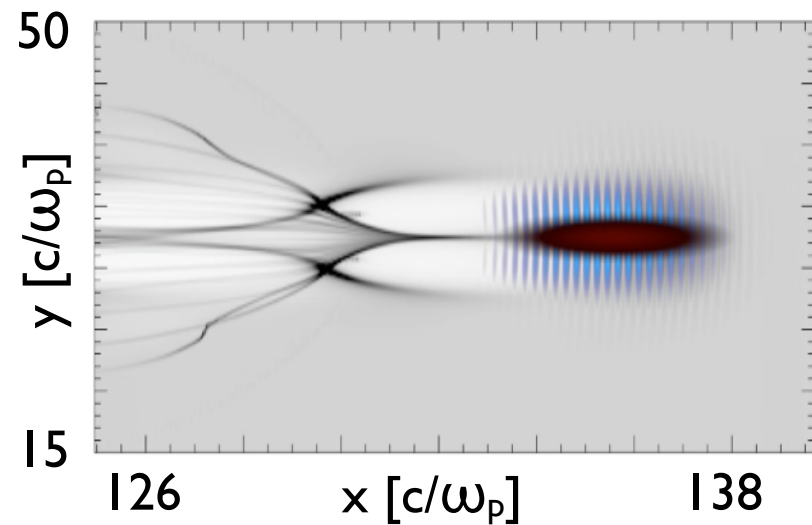
On-axis filament

positrons attract e^-
towards the axis



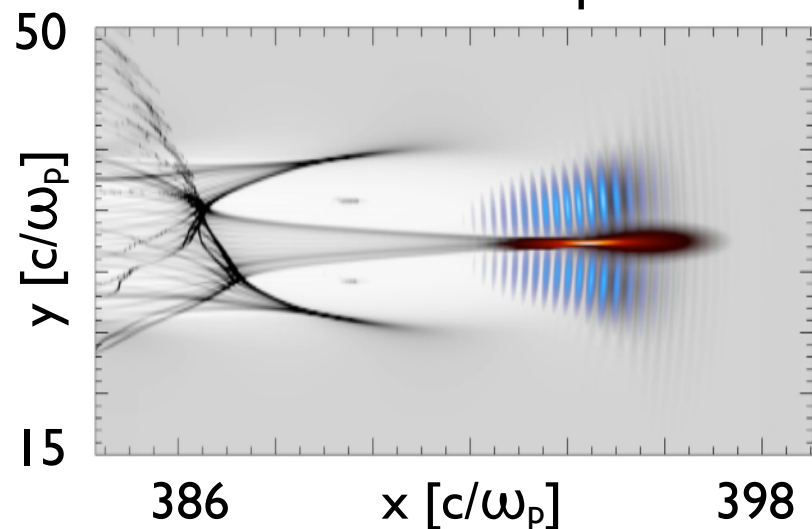
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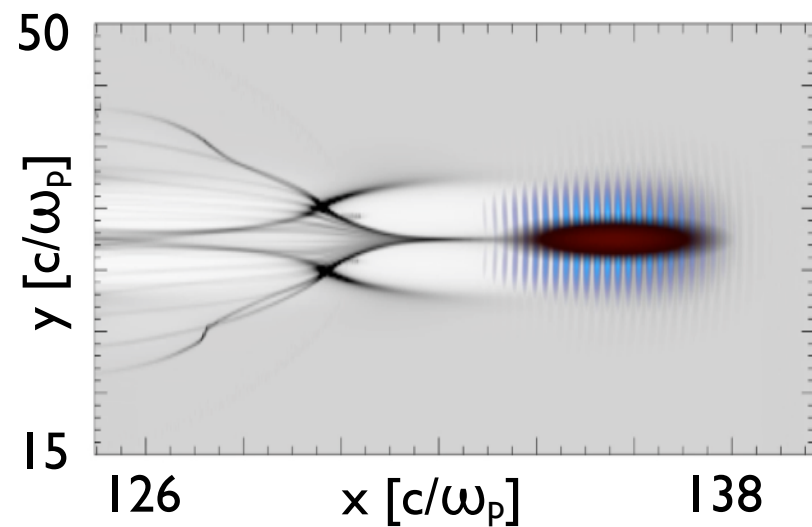
Doughnut laser

plasma refractive index gradients
modulate laser pulse



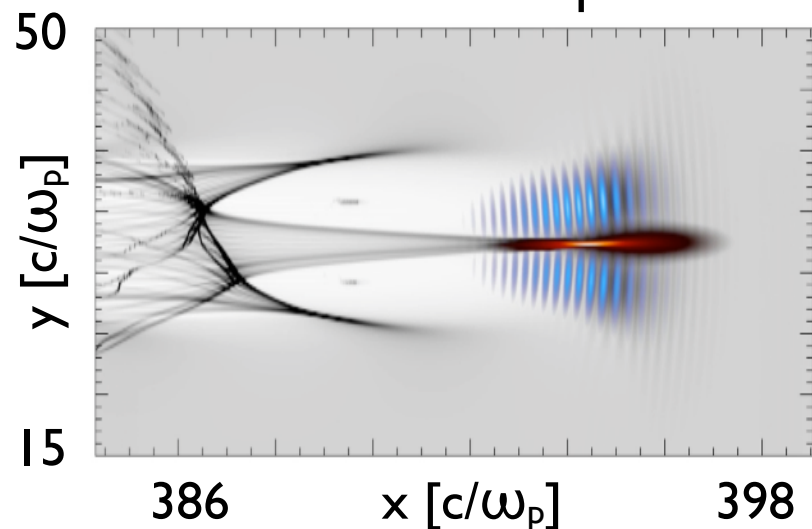
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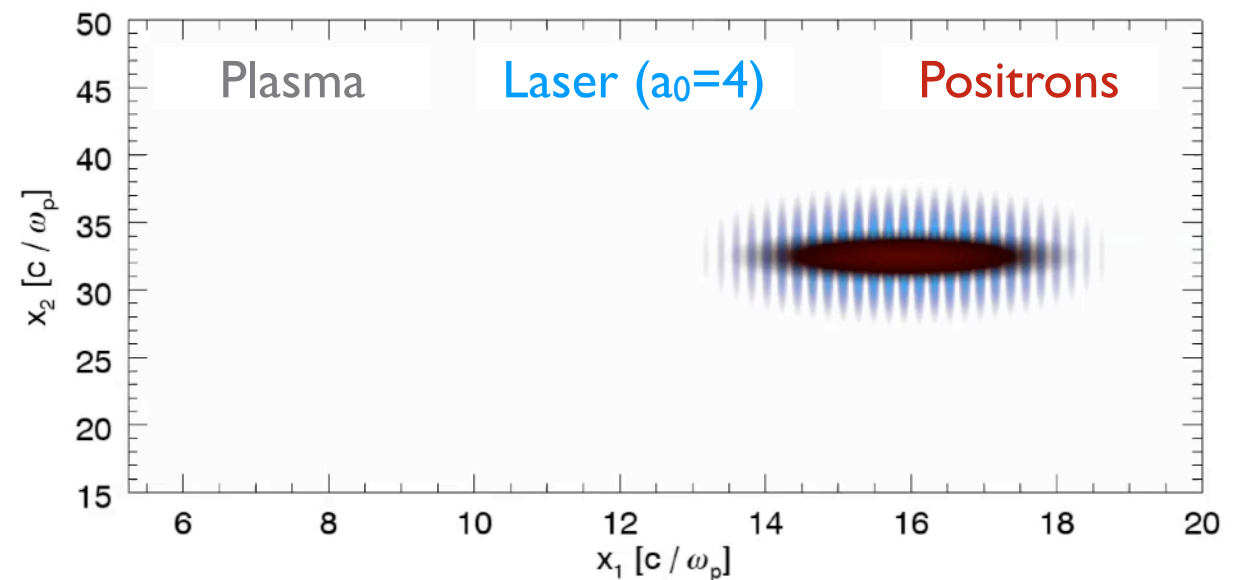
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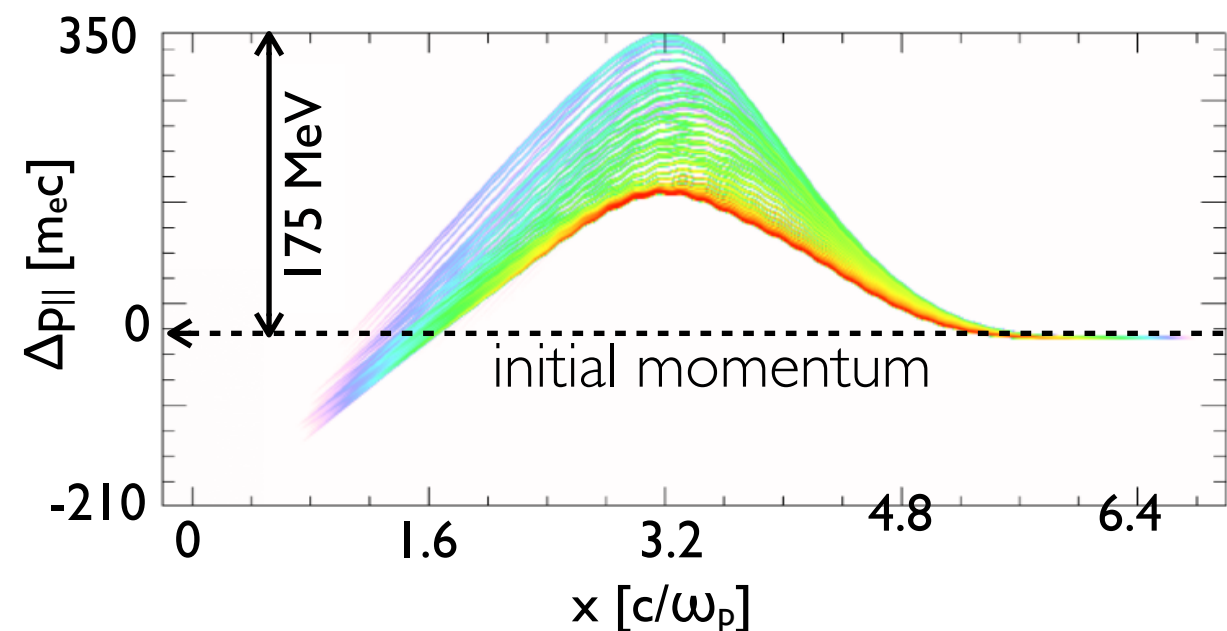
Proof-of-concept simulations

Positron beam loading required



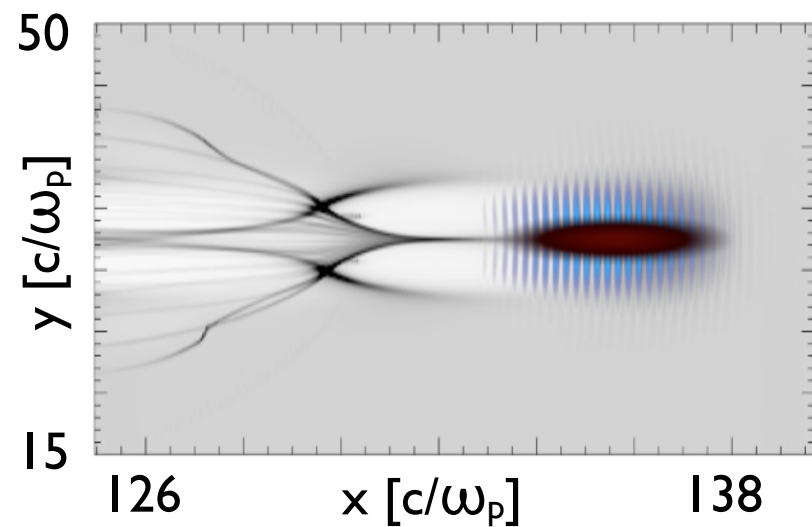
balance laser ponderomotive force with positron attraction

Positrons extract energy from wakefield



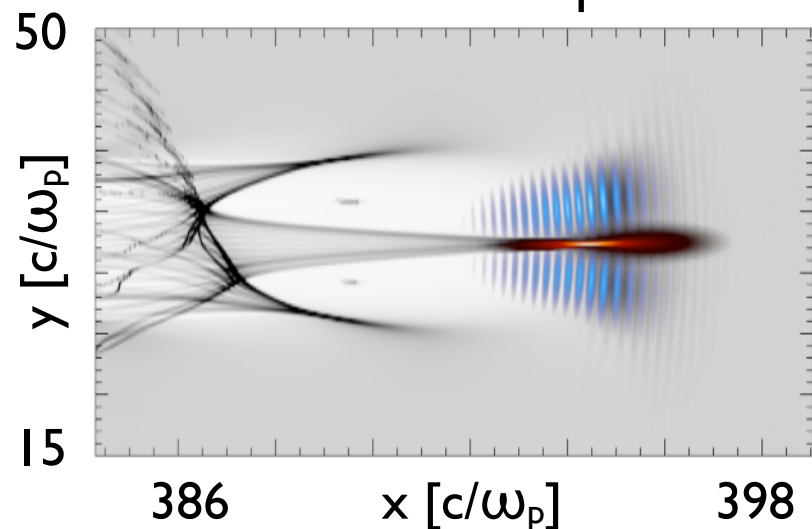
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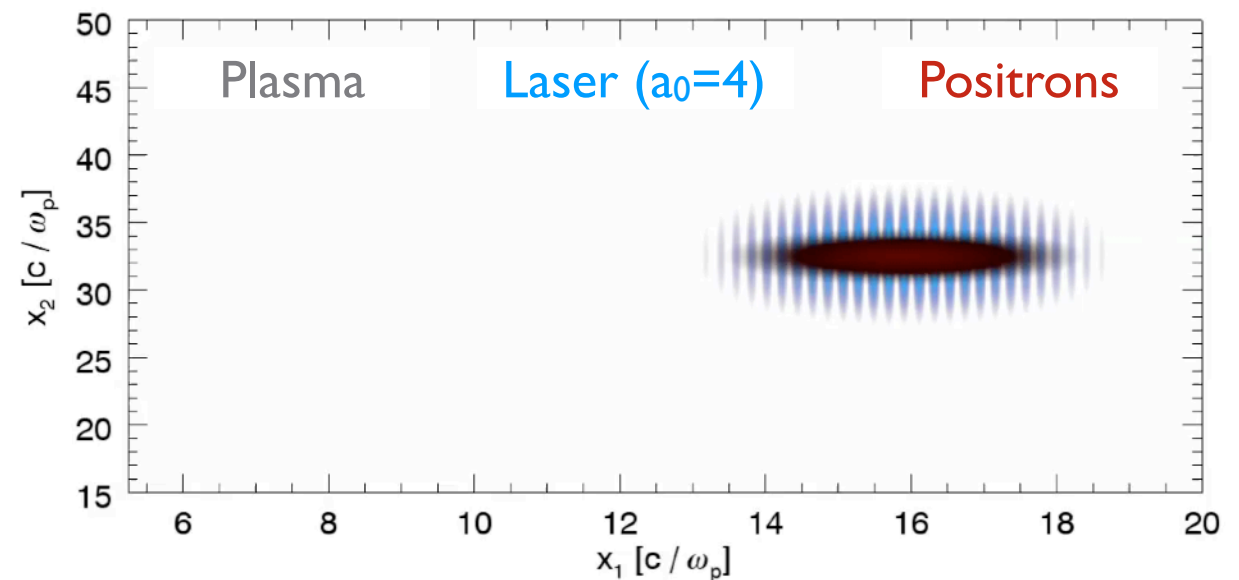
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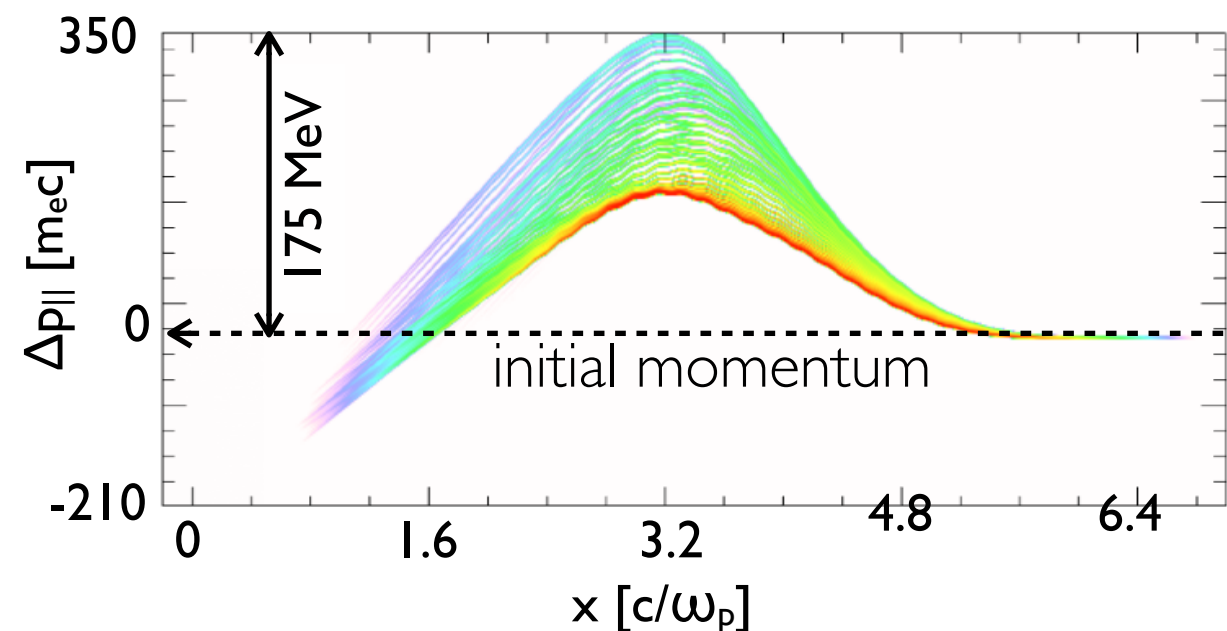
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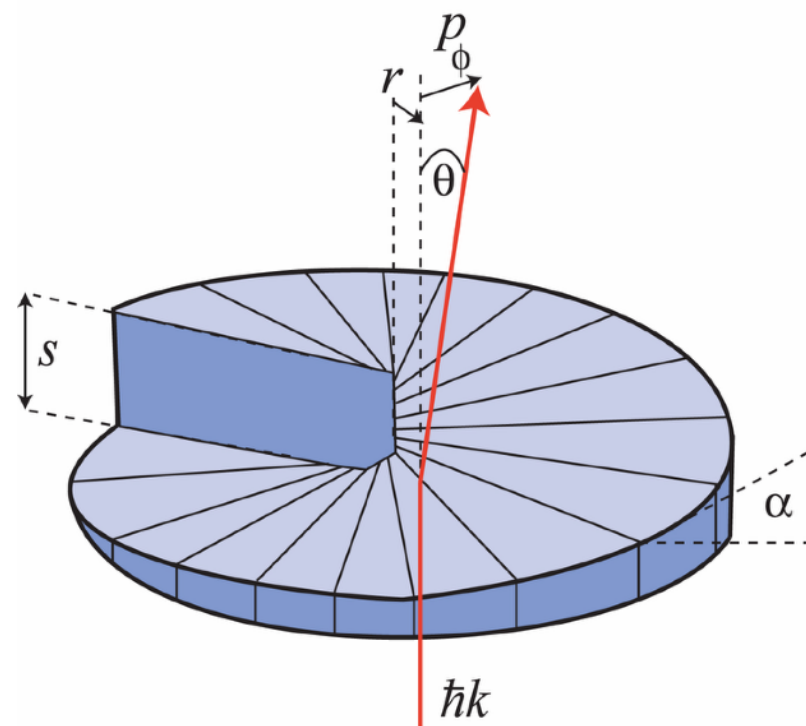
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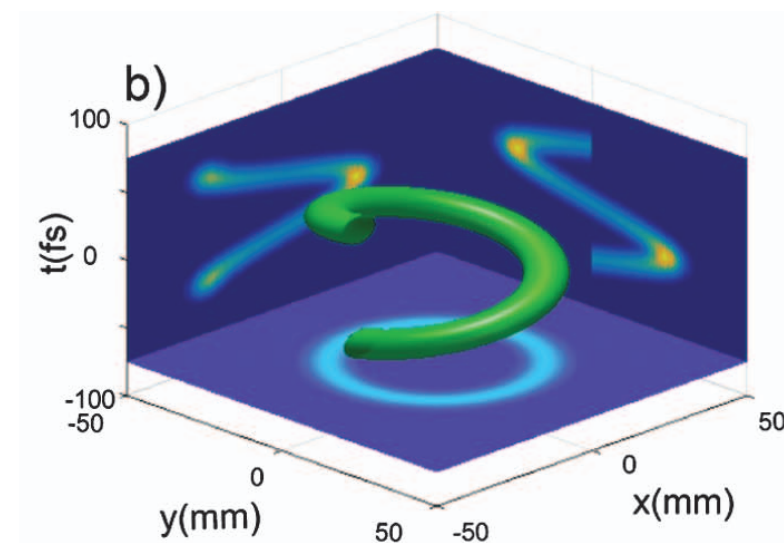
Conclusions and future directions

Experimental realisation*

spiral phase plate



Light spring forms when
thickness $\approx$ laser duration

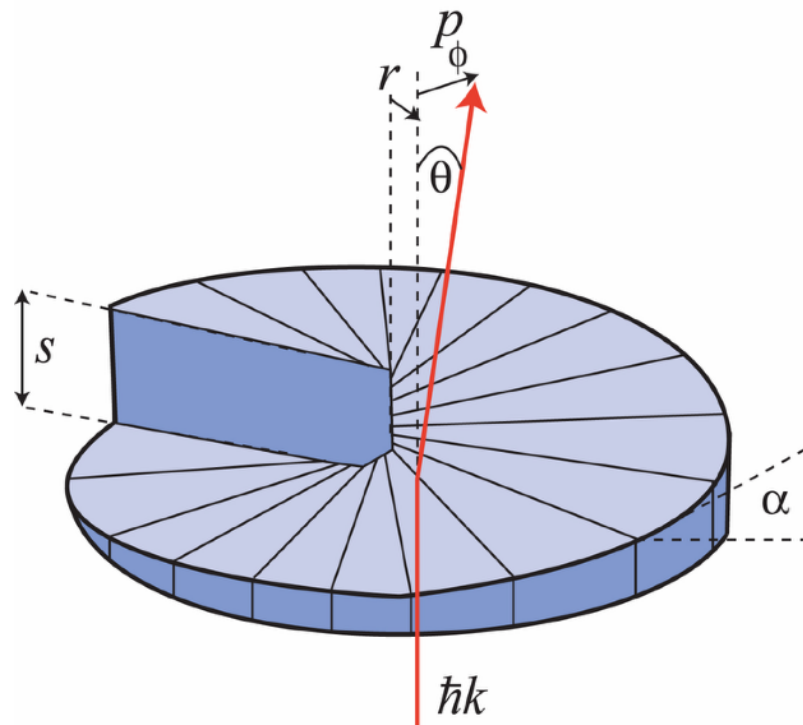


angular dependent group
velocity dispersion

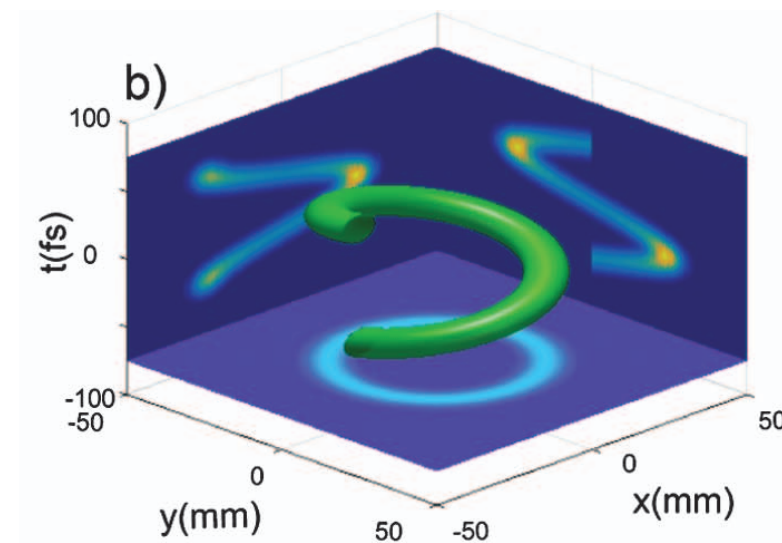
*G. Pariente, F. Quéré, Optics Letters **40** 2037 (2015)

Experimental realisation*

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Mathematical model for simulations and theory

Beating two Laguerre-Gaussian modes

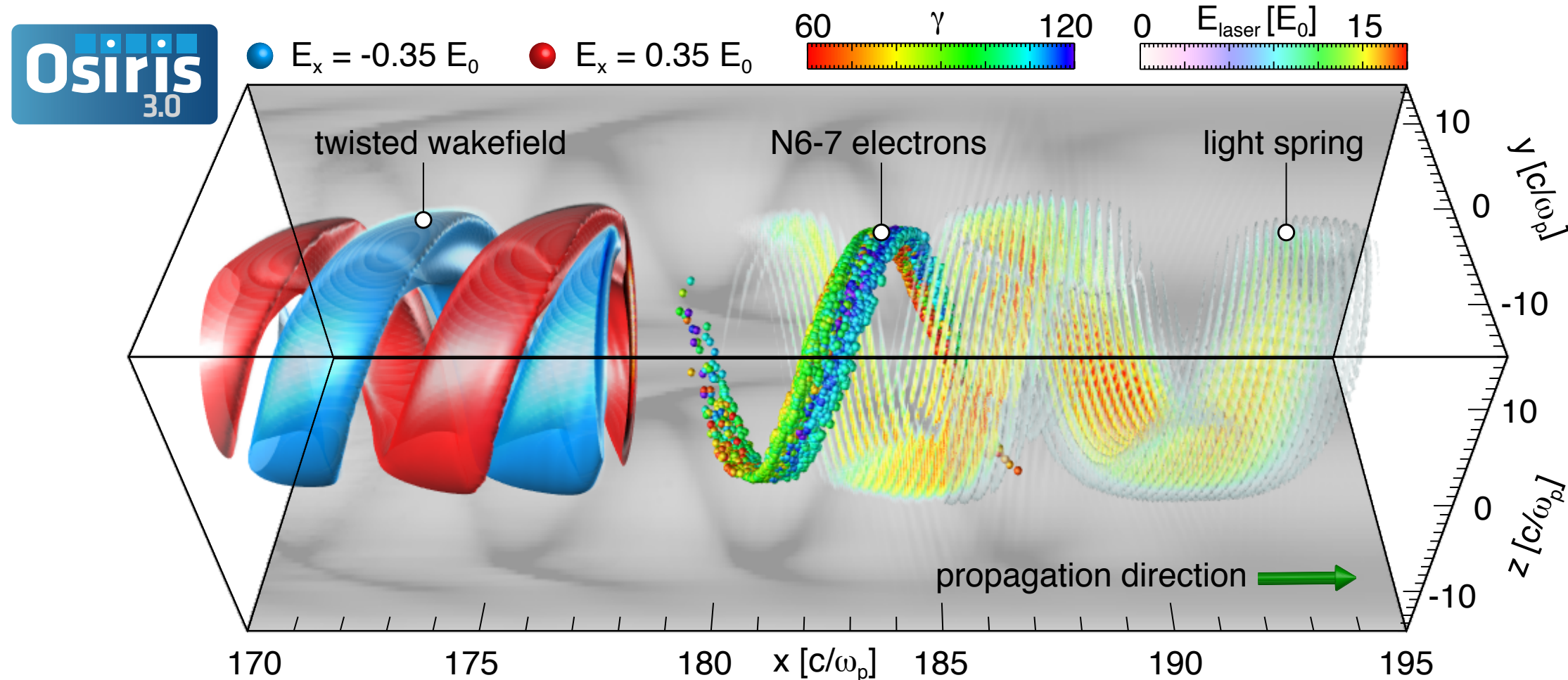
$$a^2 \propto a_{r,l}^2 + a_{r,l+\Delta l}^2 + 2a_{r,l}a_{r,l+\Delta l} \cos [\Delta k(ct - x) + \Delta l\theta + \Delta\varphi(x)]$$

Δl is the OAM difference between the two modes

Δk is the wavenumber difference

$\Delta\varphi$ is a phase difference

*G. Pariente, F. Quéré, Optics Letters **40** 2037 (2015)



Panofsky-Wenzel theorem

Transverse force acting on relativistic particle

$$\nabla_{\perp} E_x = \frac{\partial \mathbf{W}_{\perp}}{\partial \xi}$$

Transverse wakefield

$$\mathbf{W}_{\perp} = \mathbf{E}_{\perp} + (\mathbf{e}_x \times \mathbf{B})_{\perp}$$

OAM wakefield

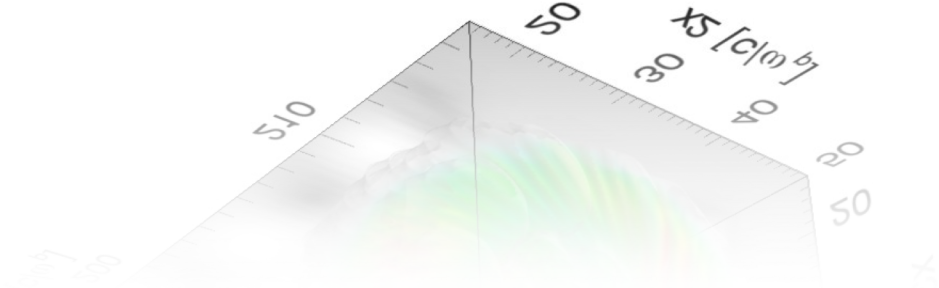
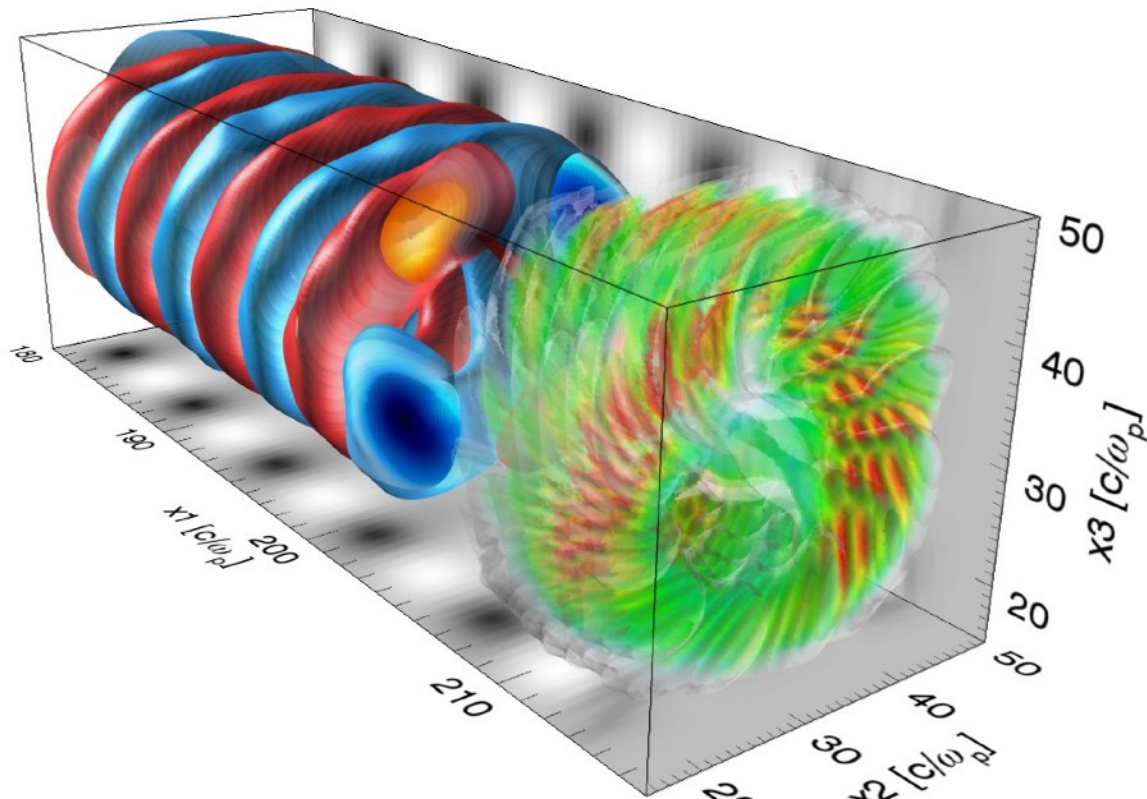
Radial focusing (betatron motion)

$$\frac{\partial E_x}{\partial r} = \frac{\partial W_r}{\partial \xi} \propto \frac{\partial \phi}{\partial r}$$

Azimuthal force **new!**

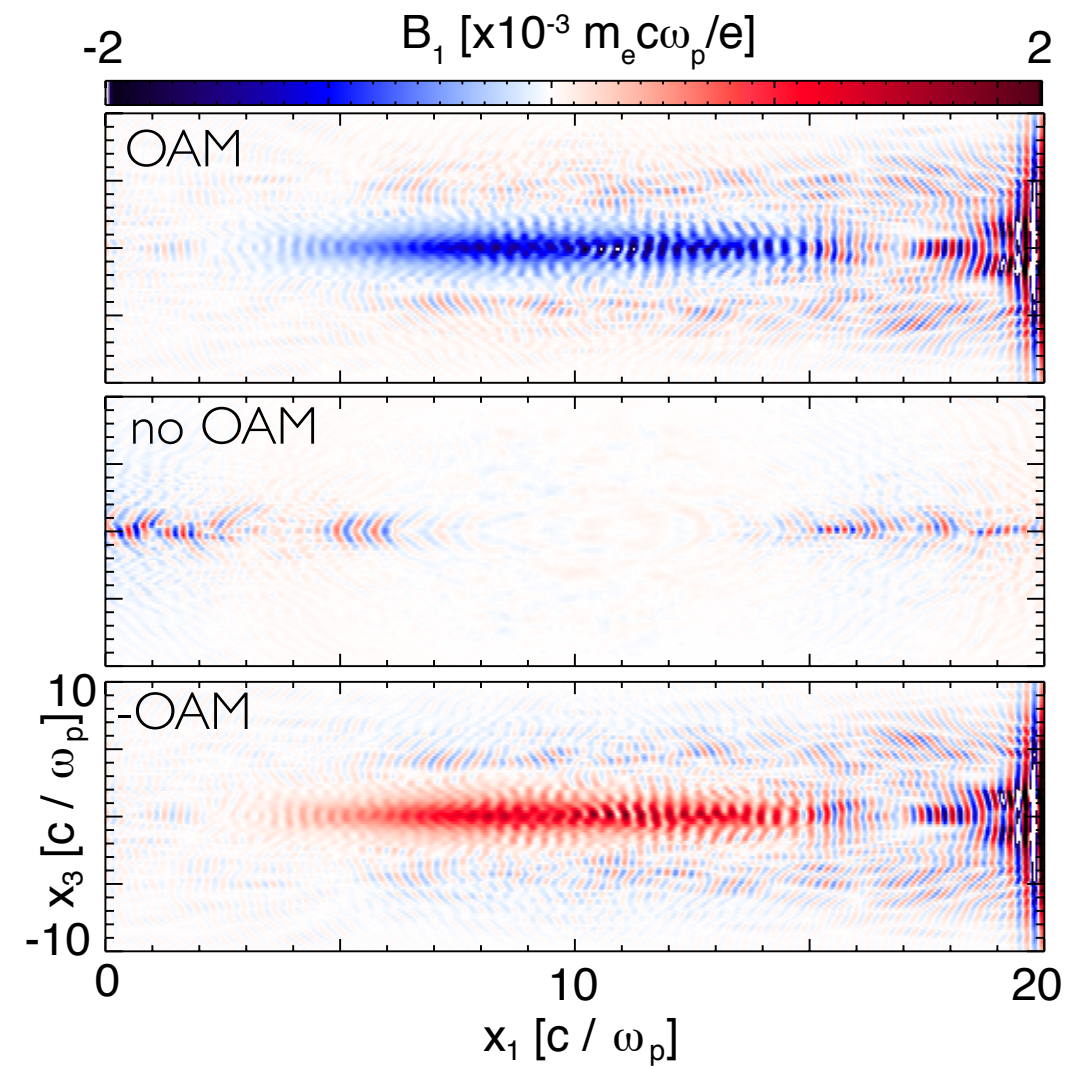
$$\frac{1}{r} \frac{\partial E_x}{\partial \theta} = \frac{\partial W_{\theta}}{\partial \xi} \propto \frac{\ell_p}{r} \phi$$

Simulations confirm new field components



Longitudinal B fields

A new longitudinal B fields appear when wakefields become nonlinear



(OAM plasma wave driven in a Raman backscatter configuration)

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Hamiltonian formulation

Hamiltonian of a charged particle

$$\mathcal{H} = m_e c^2 \gamma + e\phi(r, \theta, \xi)$$

Twisted wakefield structure

$$\phi = \phi(v_\phi t - x + \ell_p \theta) = \phi(u)$$

Hamilton's equations

$$\frac{d\mathcal{P}_x}{dt} \simeq \frac{dp_x}{dt} = -\frac{\partial \mathcal{H}}{\partial x} = \phi'(u)$$

$$\frac{d\mathcal{P}_\theta}{dt} \simeq \frac{dL_x}{dt} = -\frac{\partial \mathcal{H}}{\partial \theta} = -\ell_p \phi'$$

$$\frac{d\mathcal{H}}{dt} = \frac{\partial \mathcal{H}}{\partial t} = v_g \phi'$$

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Constants of motion

$$\text{Energy} \quad \gamma (1 - v_\phi v_x / c^2) = 1 + \Delta\phi / m_e c^2$$

$$\text{Ratio of angular momentum flux to energy} \quad \frac{\Delta L_x}{\Delta p_x} = \frac{\ell_p}{k_p} \Rightarrow \frac{\Delta L_x}{E} = \frac{\ell_p}{\omega_p}$$

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Angular momentum is quantised.

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$$\frac{d\mathcal{P}_\theta}{dt} \simeq \frac{dL_x}{dt} = -\frac{\partial \mathcal{H}}{\partial \theta} = -\ell_p \phi'$$

$$\frac{d\mathcal{H}}{dt} = \frac{\partial \mathcal{H}}{\partial t} = v_g \phi'$$

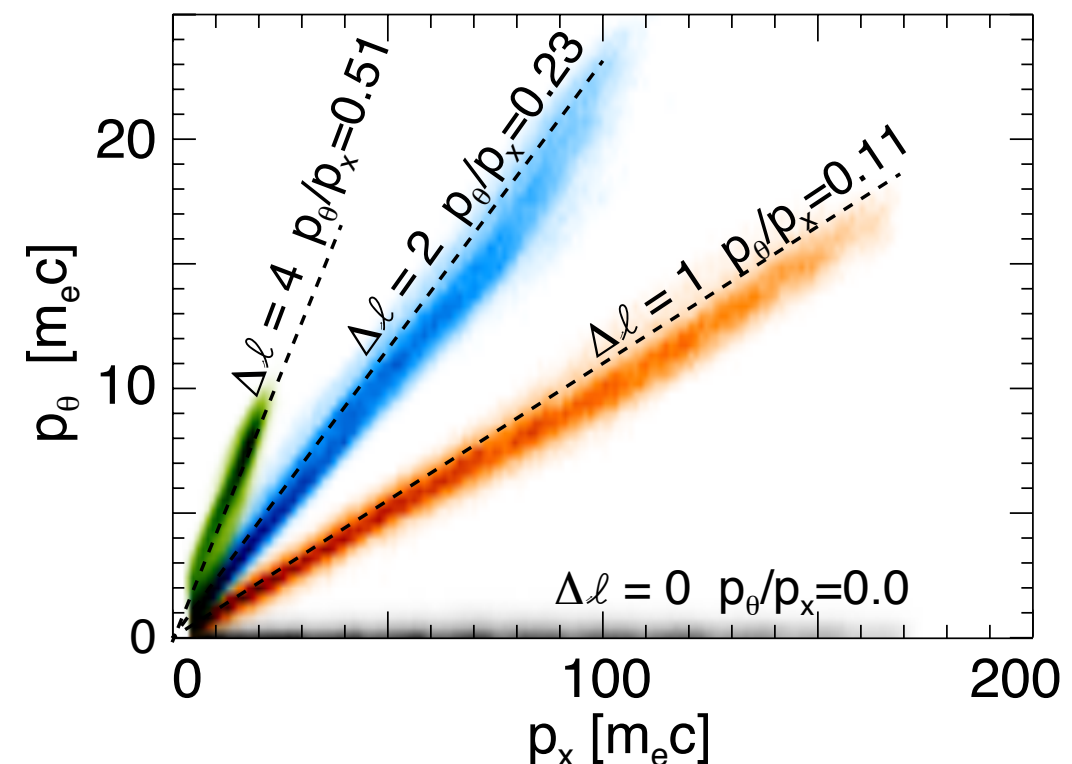
Constants of motion

Energy $\gamma (1 - v_\phi v_x / c^2) = 1 + \Delta\phi / m_e c^2$

Ratio of angular momentum flux to energy $\frac{\Delta L_x}{\Delta p_x} = \frac{\ell_p}{k_p} \Rightarrow \frac{\Delta L_x}{E} = \frac{\ell_p}{\omega_p}$

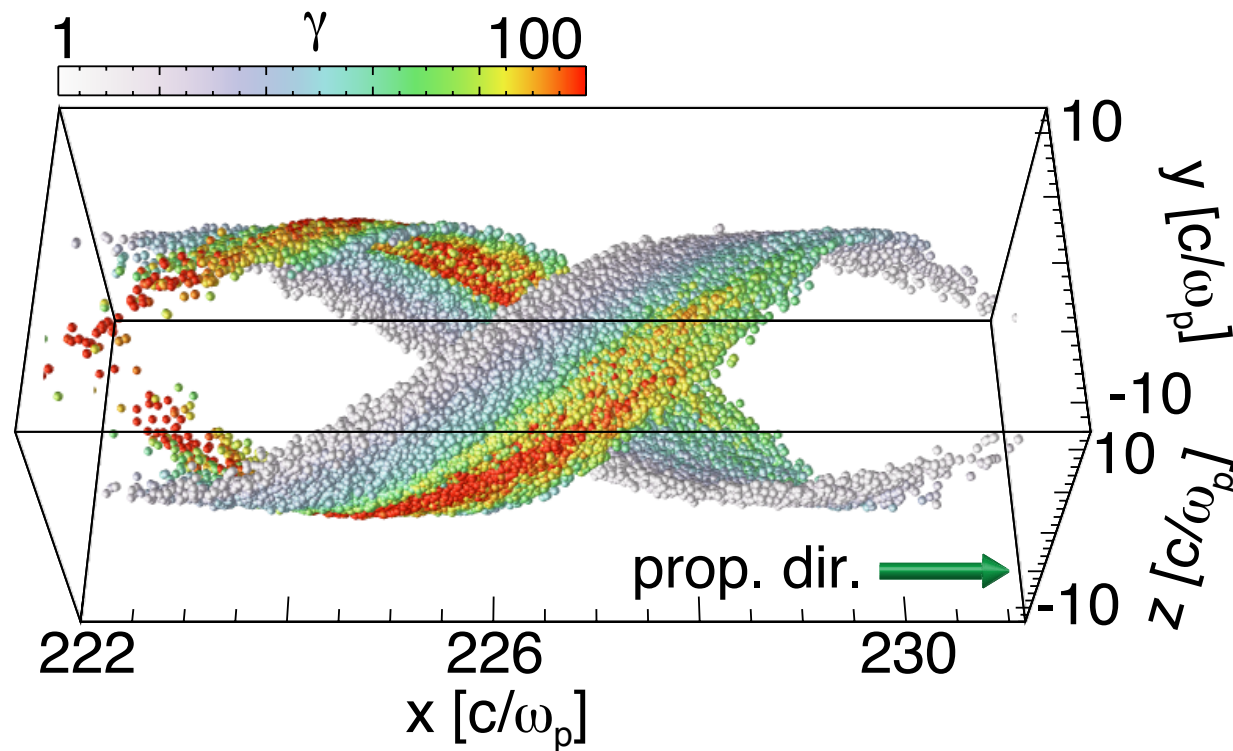
Angular momentum is quantised.

Simulations confirm OAM quantisation



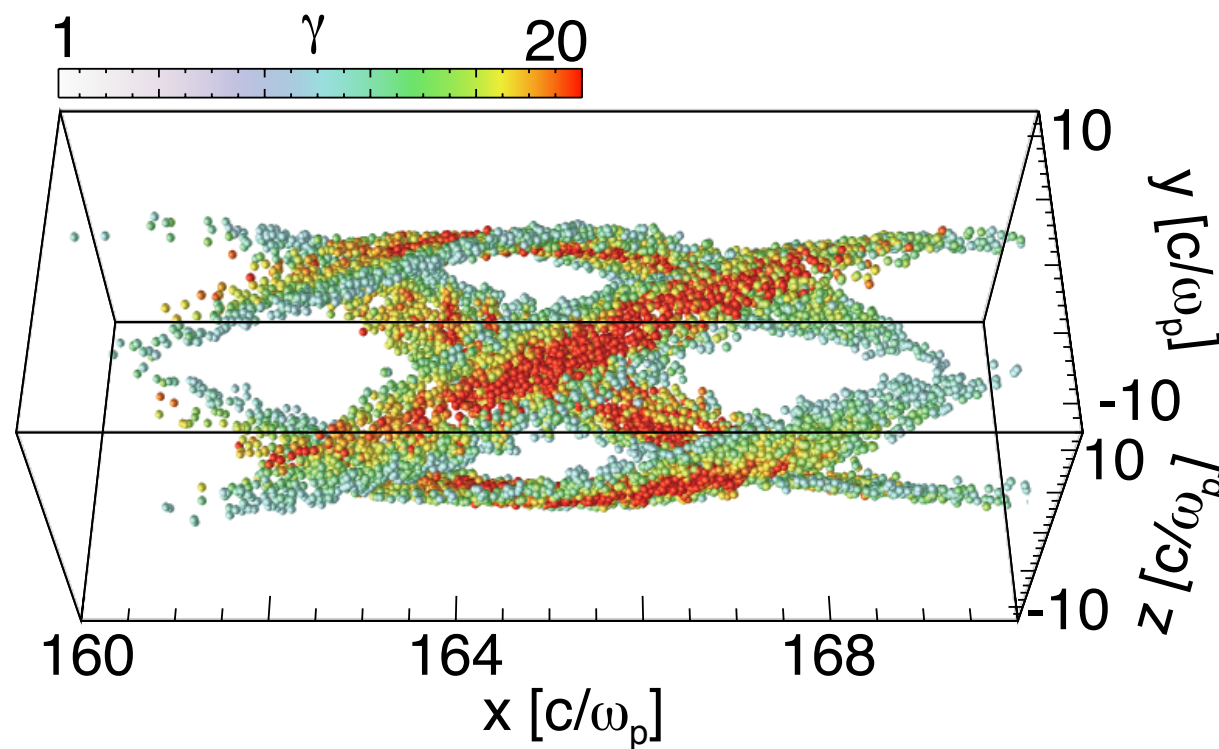
Relativistic bunches have a vortex spatial structure

$\ell = 2$



double start helix

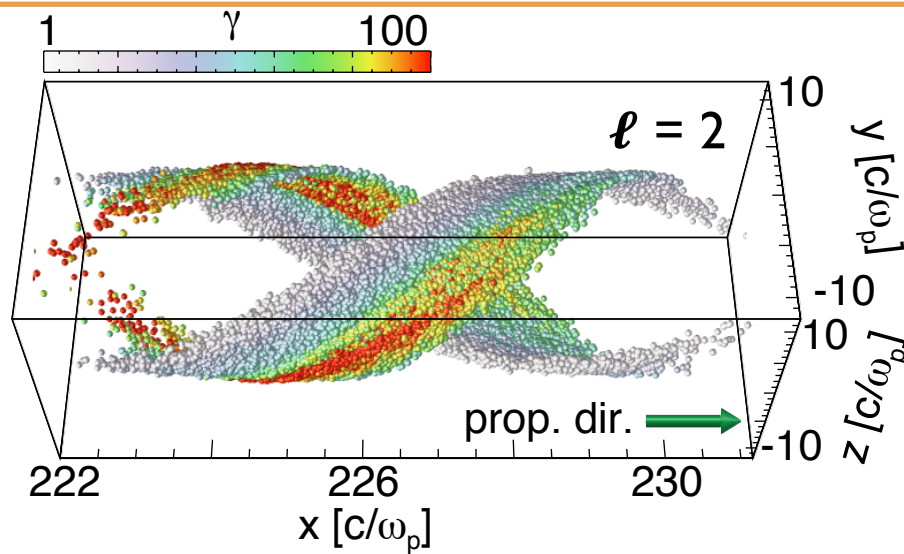
$\ell = 4$



four intertwined helices

Beams have a vortex density structure

Classical

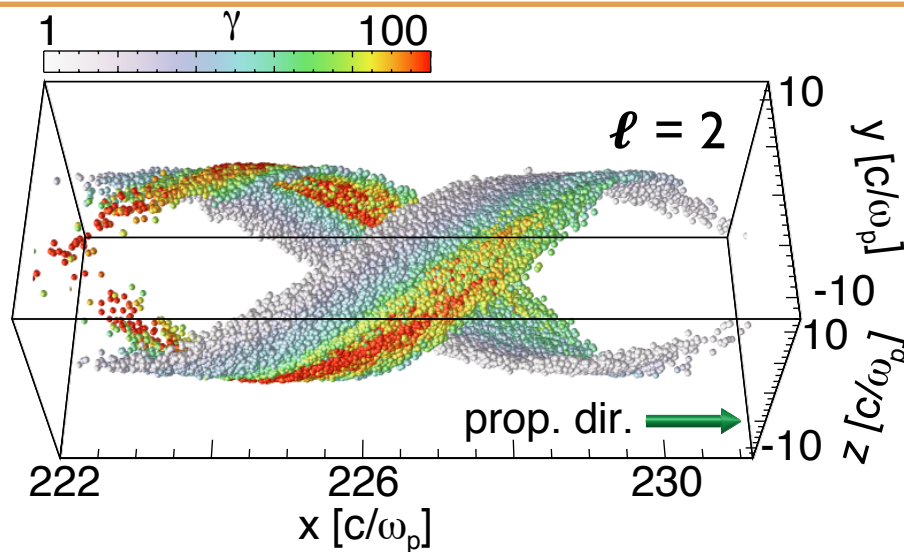


Ratio of angular momentum
to energy gain

$$\frac{\Delta L_x}{E} = \frac{\ell}{\omega_p}$$

Beams have a vortex density structure

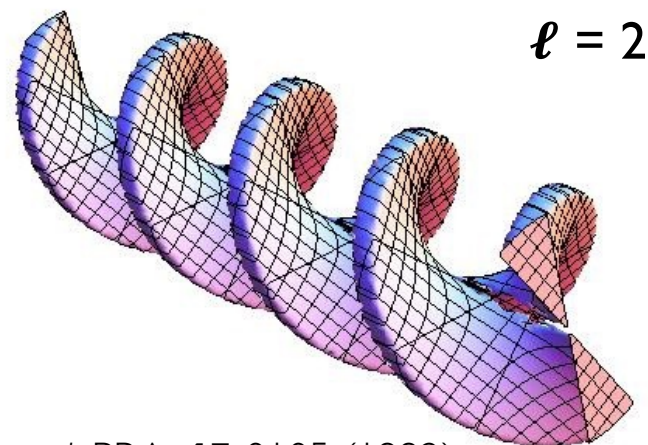
Classical



Ratio of angular momentum
to energy gain

$$\frac{\Delta L_x}{E} = \frac{\ell}{\omega_p}$$

Light



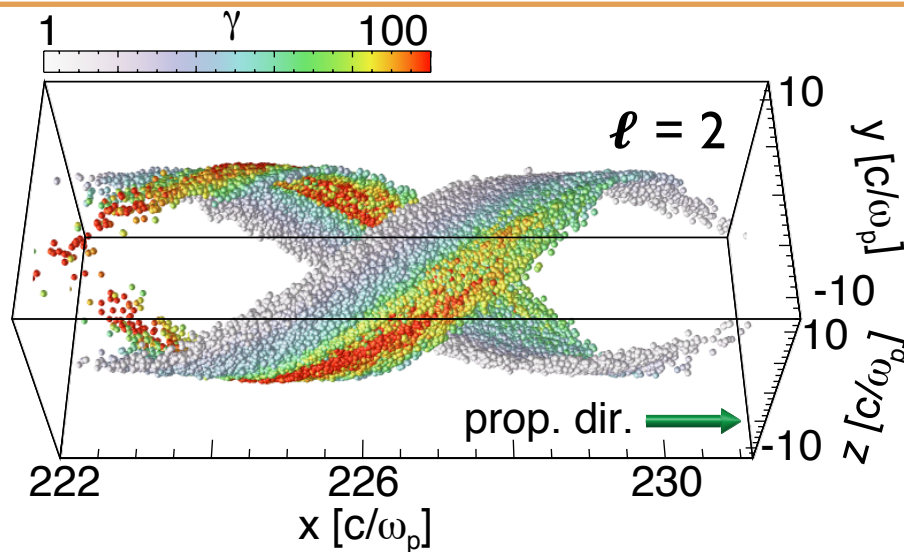
Ratio of angular momentum flux
to energy flux for the vortex
beams*

$$\frac{\mathbf{J}}{c\mathbf{P}} = \frac{\ell}{\omega_0}$$

*L. Allen et al. PRA, **45** 8185 (1992)

Beams have a vortex density structure

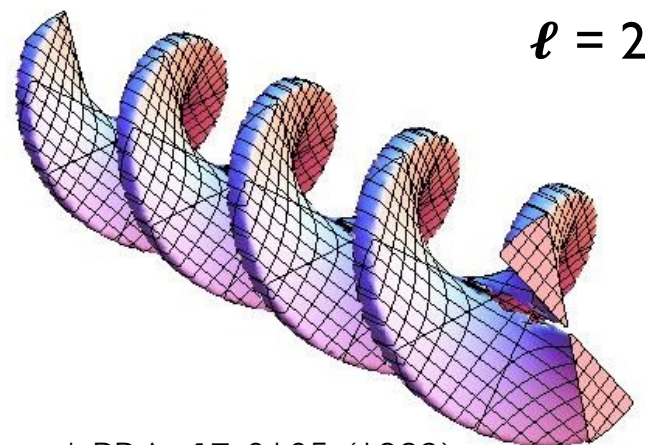
Classical



Ratio of angular momentum
to energy gain

$$\frac{\Delta L_x}{E} = \frac{\ell}{\omega_p}$$

Light

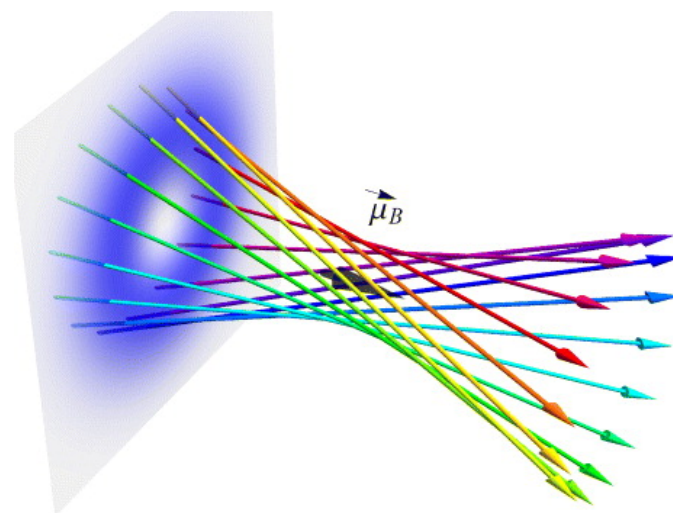


*L. Allen et al. PRA, **45** 8185 (1992)

Ratio of angular momentum flux
to energy flux for the vortex
beams*

$$\frac{\mathbf{J}}{c\mathbf{P}} = \frac{\ell}{\omega_0}$$

Quantum



Ratio of wave packet
angular momentum flux to longitudinal momentum

$$\frac{L_z}{p_z} = \frac{\ell}{k_z}$$

What are the key properties of **plasma wakefields driven by twisted lasers**? Can we address major open challenges with this new approach?

Is it possible to **transfer light's orbital angular momentum to** a new type of **plasma waves** carrying angular momentum themselves?

Is it possible to **transfer the angular momentum** of these plasma waves **to relativistic vortex electron (positron) bunches**?

Conclusions and future directions

Twisted light provides new degrees of freedom to control plasma acceleration

positron acceleration and beam phase space manipulation

Positron acceleration in the non-linear blowout regime

on-axis positron focusing force in doughnut shaped plasma waves

Generation of vortex electron bunches

electrons with quantised orbital angular momentum levels in twisted plasma waves