

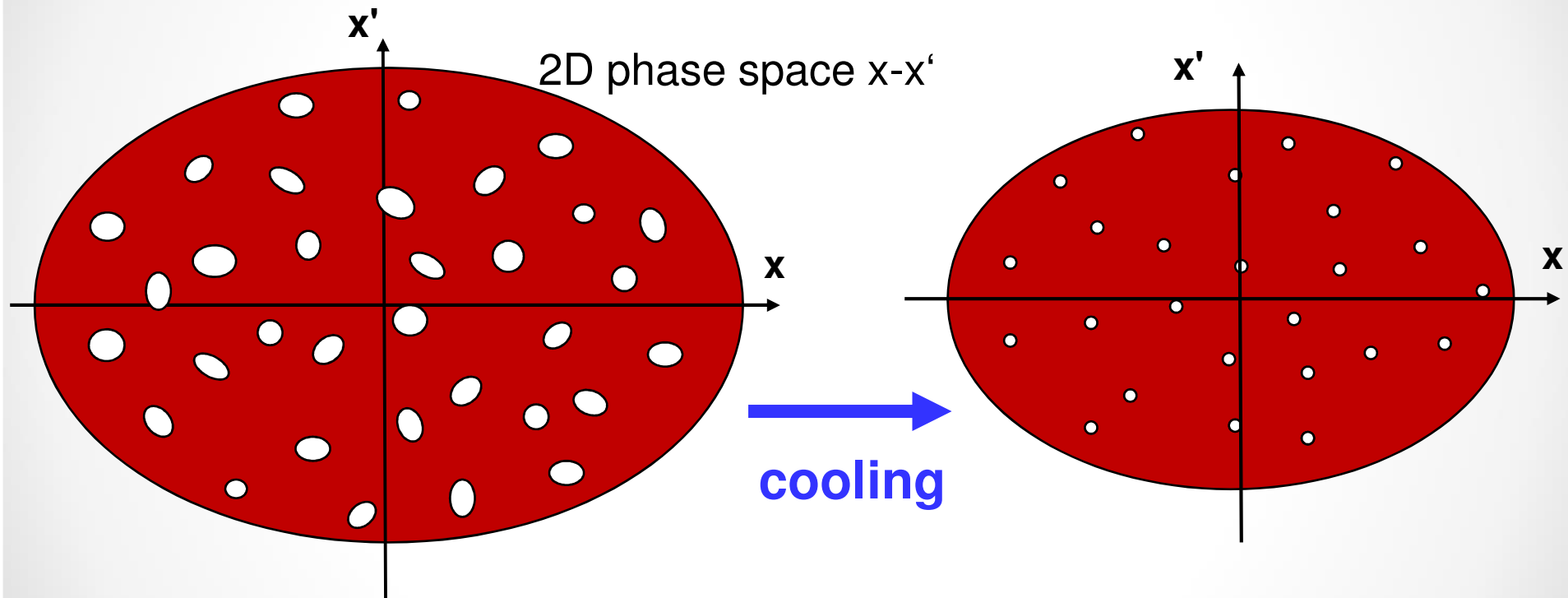
Stochastic Cooling

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**CAS Advanced Accelerator Physics,
Metalskolen, Slangerup, Denmark,
9 - 21 June 2019**

Fluctuations in Phase Space

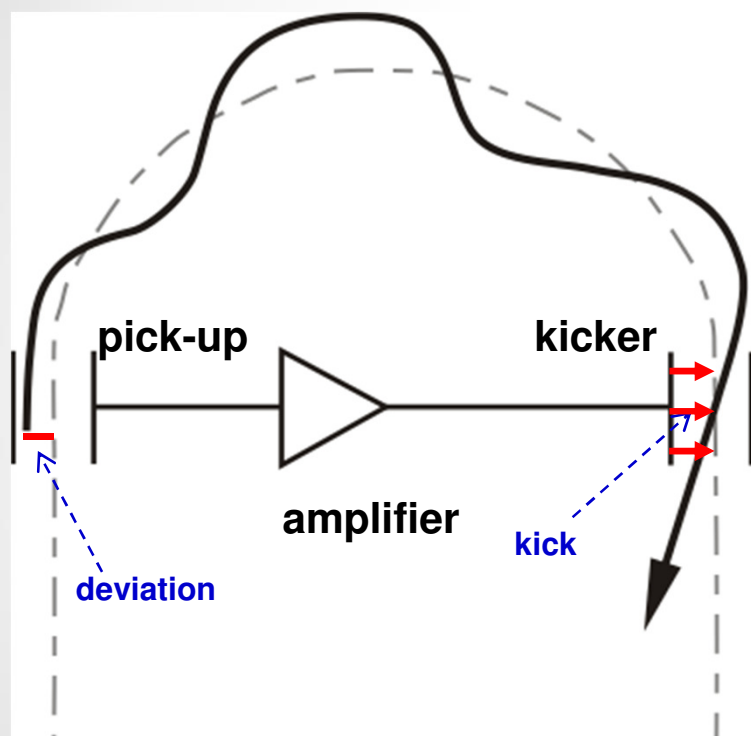
phase space is not homogeneously filled with particles
⇒ fluctuations of local particle density



compression of total phase space volume by reduction of locally empty phase space volume

Stochastic Cooling

First cooling method which was successfully used for beam preparation



S. van der Meer, D. Möhl, L. Thorndahl et al.
(1925 – 2011) (1936-2012)

Conditions:

Betatron motion phase advance
(pick-up to kicker): $(n + \frac{1}{2}) \pi$

Signal travel time = time of flight of particle
(between pick-up and kicker)

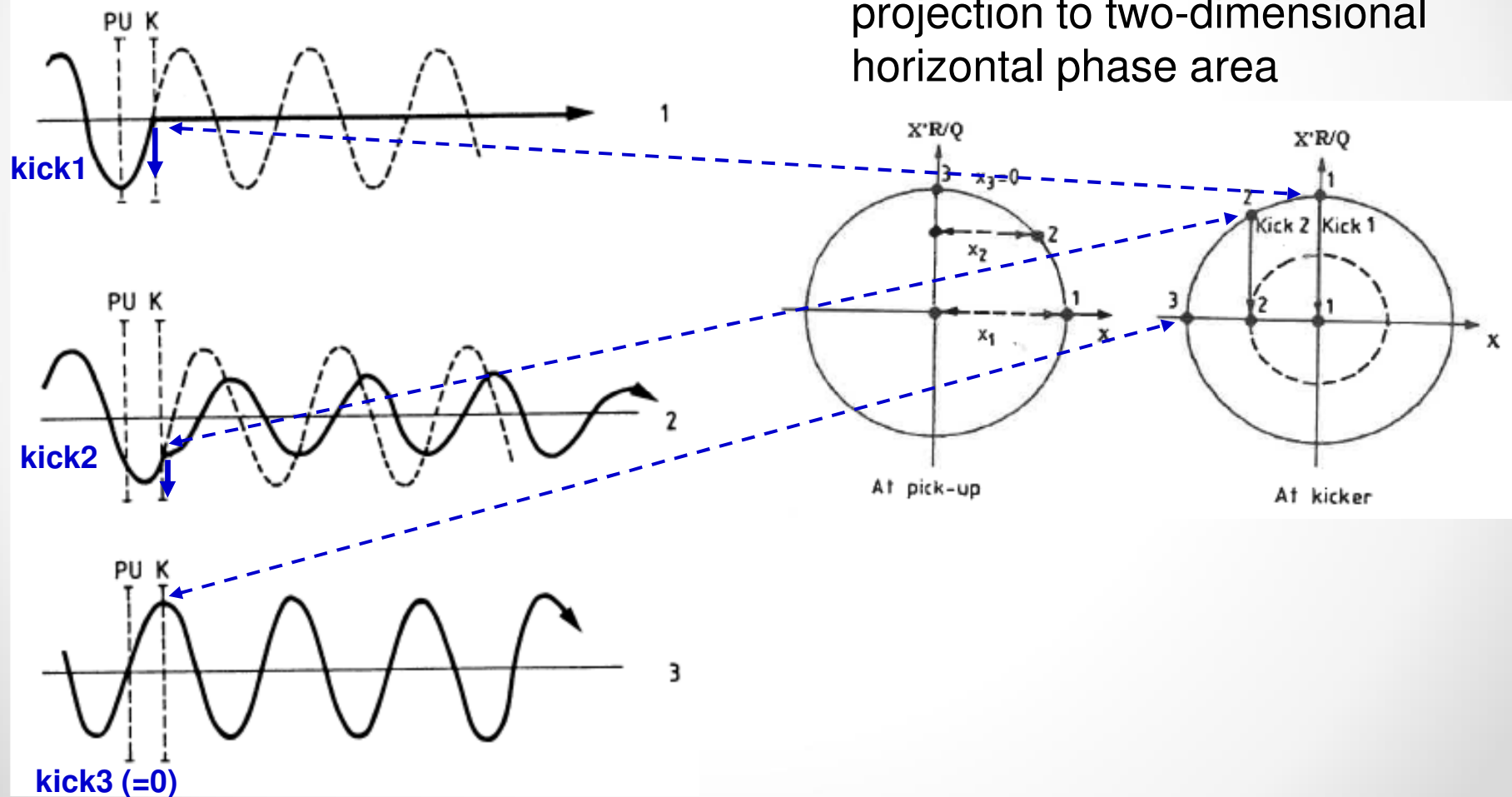
Sampling of sub-ensemble of total beam

Principle of transverse cooling:
measurement of deviation from ideal orbit
is used for correction kick (feedback)

Stochastic Cooling

single particle betatron motion
 along storage ring
 without (dashed) and with (full)
 correction **kick**

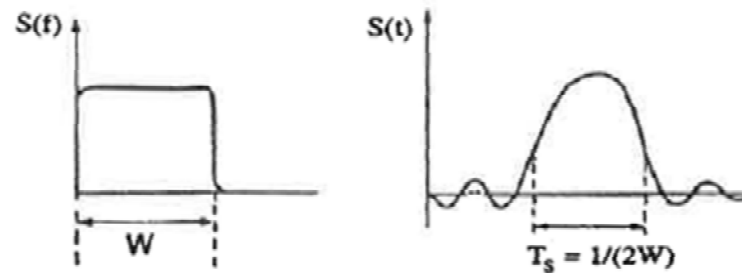
projection to two-dimensional
 horizontal phase area



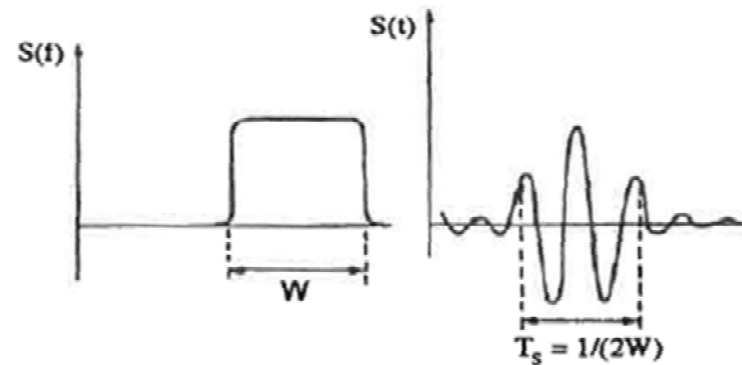
Stochastic Cooling

Nyquist theorem: a system with a band-width $\Delta f = W$ in frequency domain can resolve a minimum time duration $\Delta T = (2W)^{-1}$

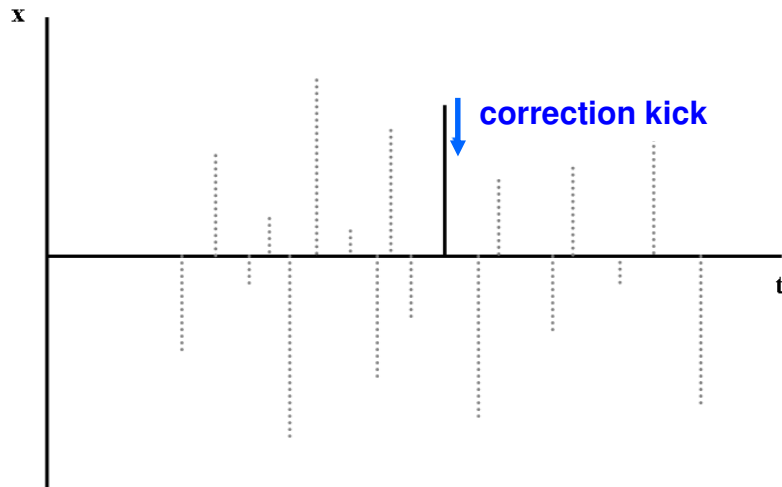
low pass



band pass



Stochastic Cooling

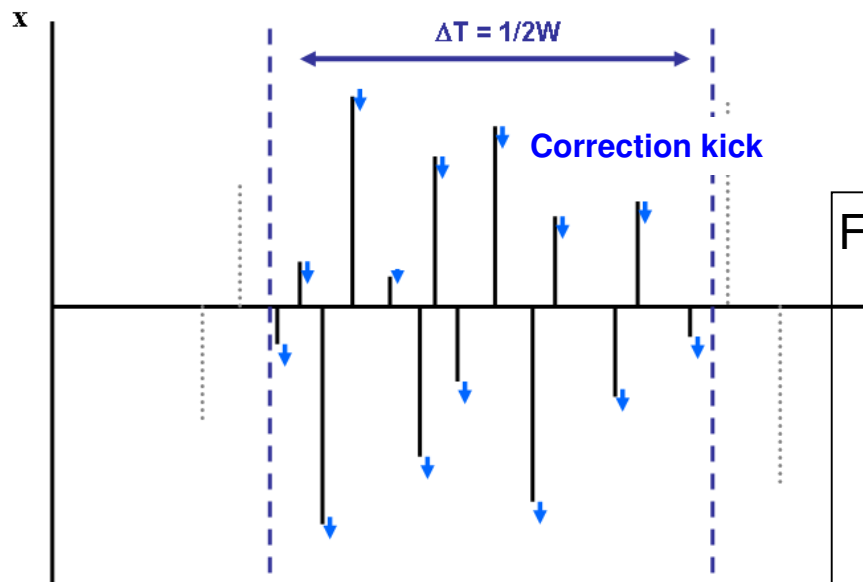


in time domain

correction kick
(unlimited time resolution)

$$-\Delta x = g \times x$$

Nyquist \Rightarrow the time resolution for a system of bandwidth W is $\Delta T = (2W)^{-1}$



correction kick with bandwidth W

$$-\Delta x = \frac{g}{N_s} \times \sum_{i=1..N_s} x_i, \quad N_s = N \frac{\Delta T}{T_0} = \frac{N}{2WT_0}$$

For exponential damping ($x(t) = x(t_0) \times e^{-(t-t_0)/\tau}$):

$$\tau^{-1} = T_0^{-1} \times \frac{\Delta x}{x} = \frac{g2W}{N}, \quad \text{if } \sum_{i=1..N_s} x_i = x$$

cooling rate

$$\tau^{-1} \leq \frac{2W}{N}, \quad \text{if } g \leq 1$$

Stochastic Cooling

some refinements of cooling rate formula

noise: thermal or electronic noise adds to the beam signal

mixing: change of relative longitudinal position of particles due to momentum spread

cooling rate $\lambda = \tau^{-1} = \frac{2W}{N} \left(\underbrace{2g}_{\text{cooling}} - \underbrace{g^2(M+U)}_{\text{heating}} \right)$ M mixing factor
U noise to signal ratio

maximum of cooling rate

$$\lambda_{max} = \frac{2W}{N} \frac{1}{M+U}$$

$$\frac{d\lambda}{dg} = 0 \Rightarrow g = \frac{1}{M+U}$$

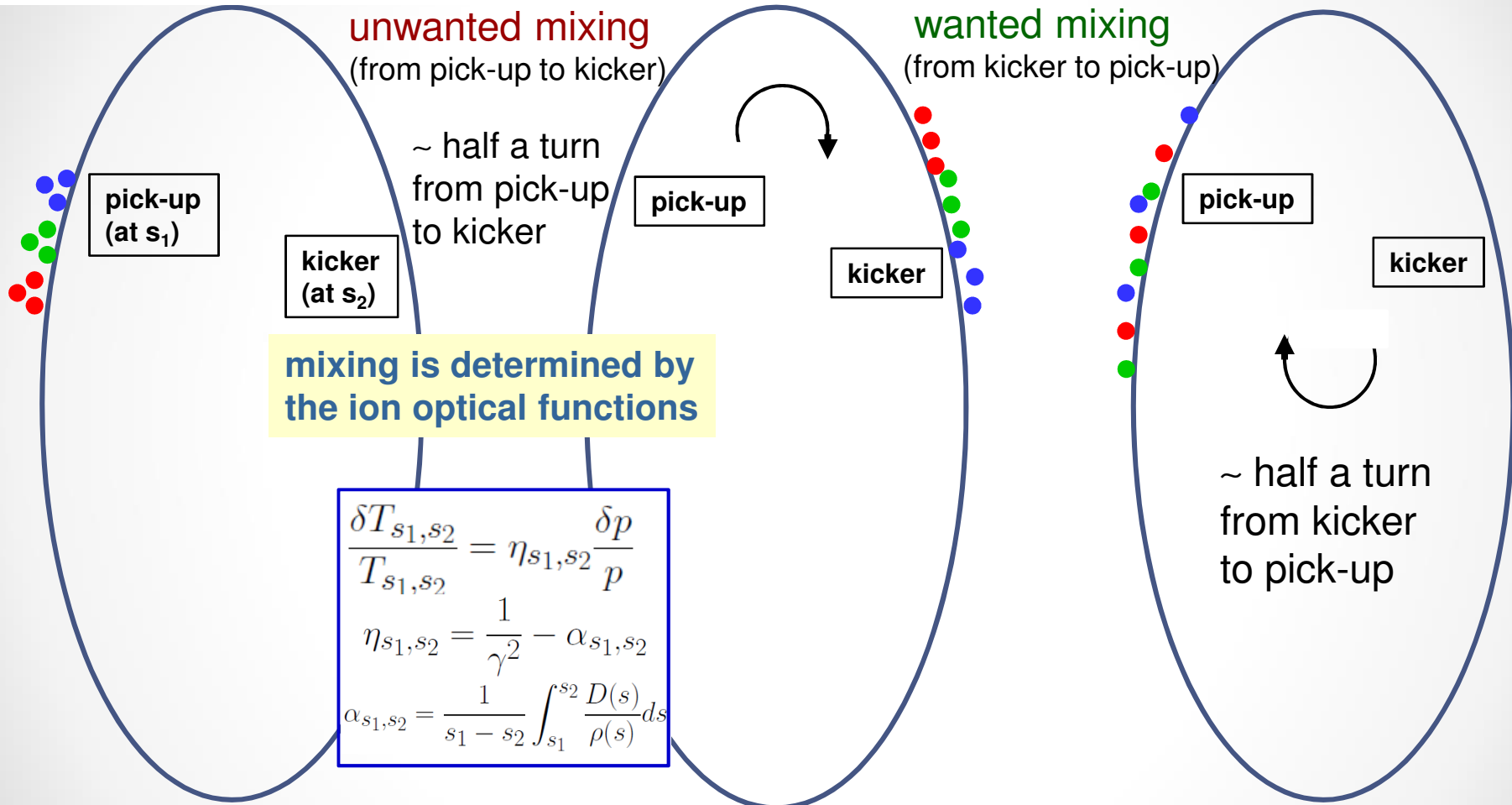
further refinement (wanted ↔ unwanted mixing):

with wanted mixing M (kicker to pick-up)
and unwanted mixing \tilde{M} (pick-up to kicker)

$$\lambda = \tau^{-1} = \frac{2W}{N} (2g(1 - \tilde{M}^{-2}) - g^2(M+U))$$

Mixing

$$\lambda = \tau^{-1} = \frac{2W}{N} (2g(1 - \tilde{M}^{-2}) - g^2(M + U))$$



$$1 - \tilde{M}^{-2} \approx \cos [0.5\pi \eta_{eff} n_{max} (\Delta p/p)_{rms}]$$

$$\Rightarrow \eta_{eff} \sim 0$$

$$M = (2WT\eta(\Delta p/p)_{rms})^{-1}$$

$$\Rightarrow \eta_{k-pu} > 0, (T\eta(\Delta p/p)_{rms})^{-1} \sim 1$$

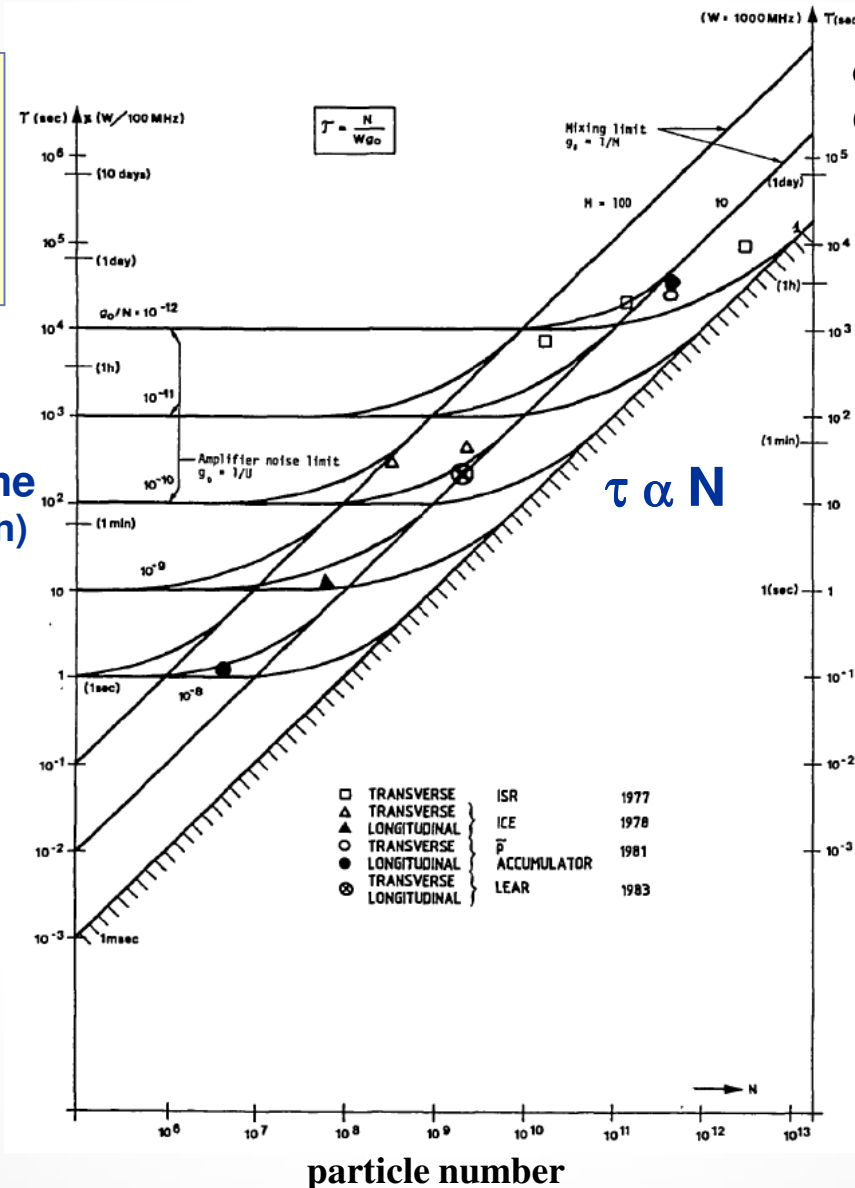
Basic Studies of Stochastic Cooling

summary of initial stochastic cooling studies at CERN with (anti-)protons

noise limit regime (depending on gain)

cooling time (normalized to 1 GHz bandwidth)

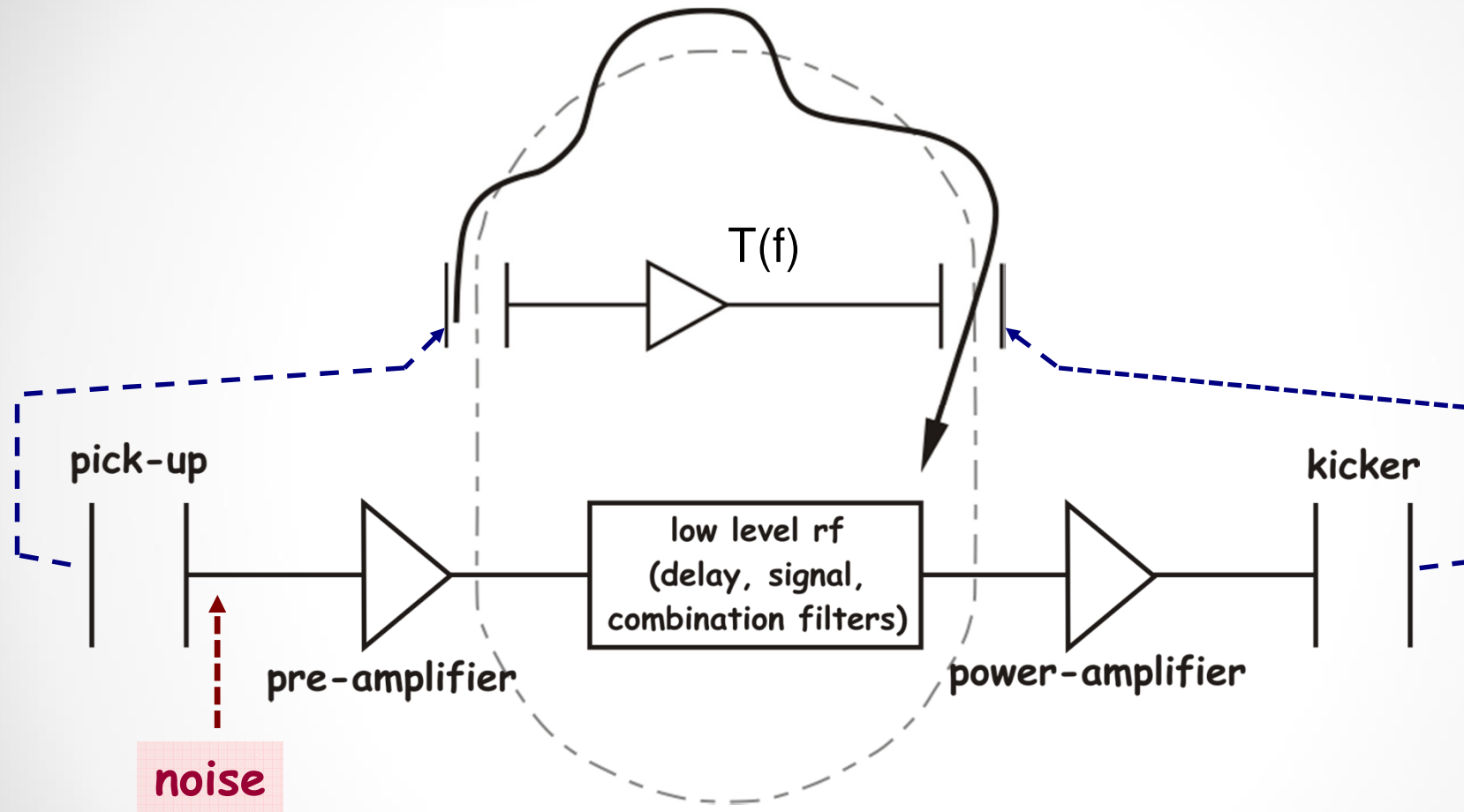
mixing limit regime



Requirements Stochastic Cooling

- **large bandwidth (typically one octave in the GHz range)**
- **good transfer function in gain and phase**
- **high sensitivity (high impedance) of pick-up and kickers**
- **low electronic noise (cold pick-ups, low noise amplifiers)**
- **large, but variable gain**
- **special ion optical properties of the ring**
 - betatron phase advance between transverse pick-up and kicker**
 - small momentum slip factor (large wanted and little unwanted mixing)**
 - for Palmer cooling: large dispersion value at pick-up**

Stochastic Cooling Circuit

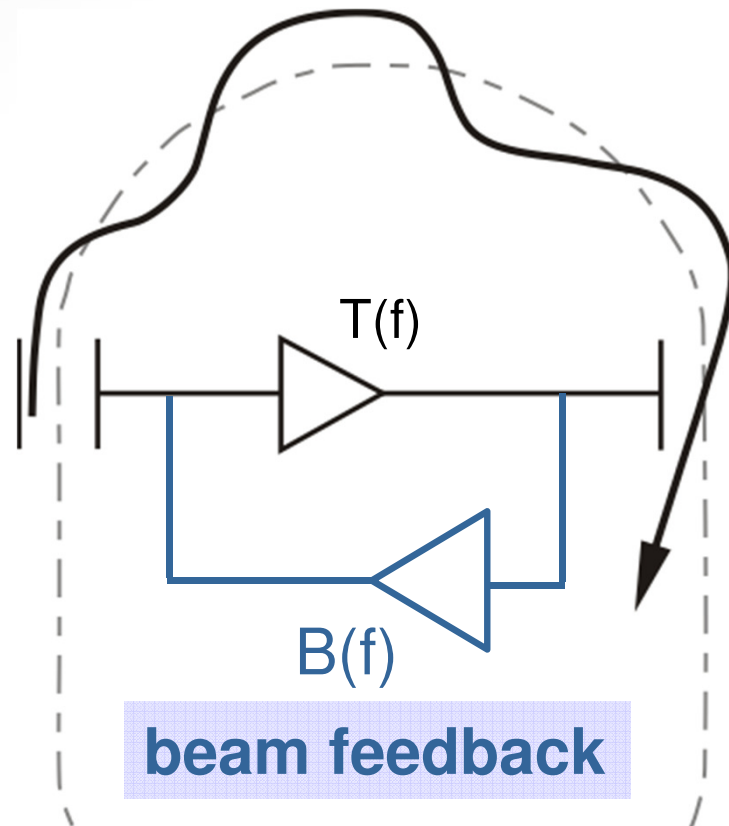


energy kick: $\delta E(f) = T(f) I_b(f)$

transfer function:

$$T(f) = Z_{pu} \cdot G_{pu}(f) \cdot H(t_{delay}) \cdot F(f) \cdot G_k(f) \cdot Z_{ki}$$

Stochastic Cooling Circuit



kick: $\delta E(f) = \frac{T(f)}{1 - B(f)T(f)} (I_b(f) + \Delta I(f)) \quad \Delta I(f) = B(f) \cdot \Delta E(f)$

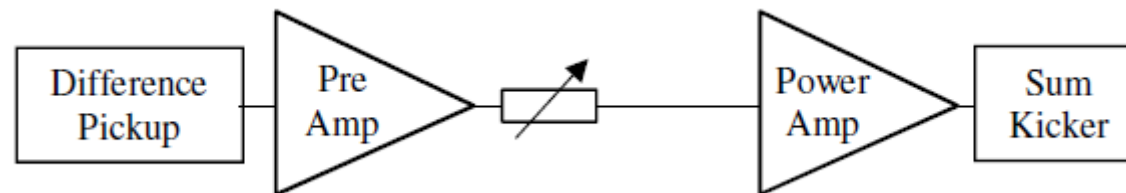
open loop gain: $S(f) = B(f) \cdot T(f)$

results in shielding and
a reduction of Schottky noise
⇒ reduction of gain

Longitudinal Stochastic Cooling

1) Palmer cooling

a pick-up in a dispersive section detects the horizontal position (sensitivity to the particle longitudinal momentum)



at the kicker the correction signal derived from the position results in an acceleration/deceleration kick which counteracts a momentum deviation

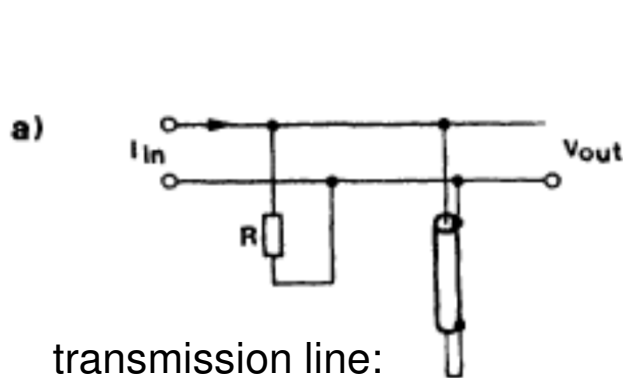
(coupling longitudinal-horizontal degree of freedom can cause heating \Rightarrow compensation by horizontal cooling system)

Longitudinal Stochastic Cooling

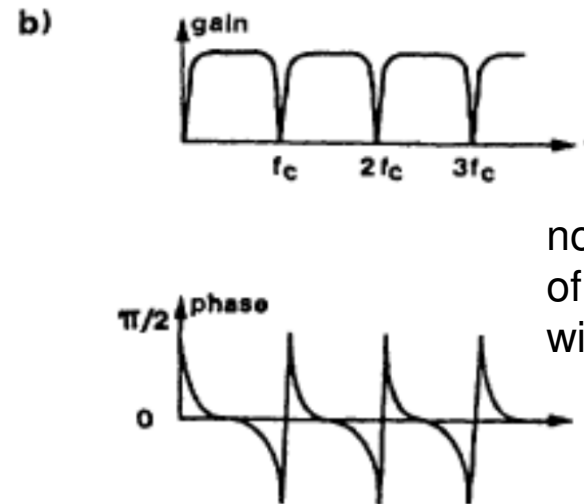
2) Notch filter cooling

filter creates notches at the harmonics of the nominal revolution frequency

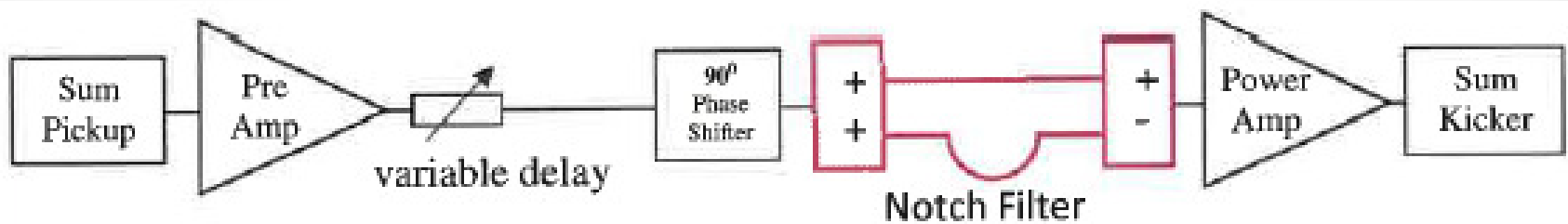
⇒ particles are forced to circulate at the nominal frequency



transmission line:
signal delay by one turn,
short circuit at all harmonics
of the revolution frequency



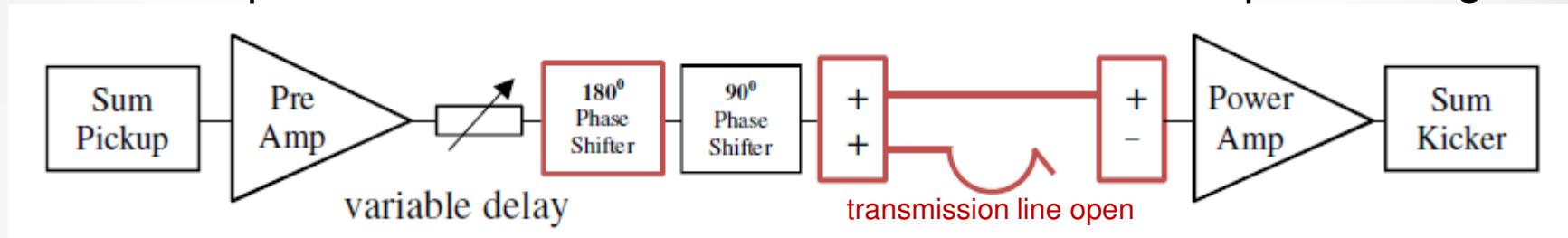
notches at harmonics
of the revolution frequency
with 180° phase jump



Longitudinal Stochastic Cooling

3) ToF cooling

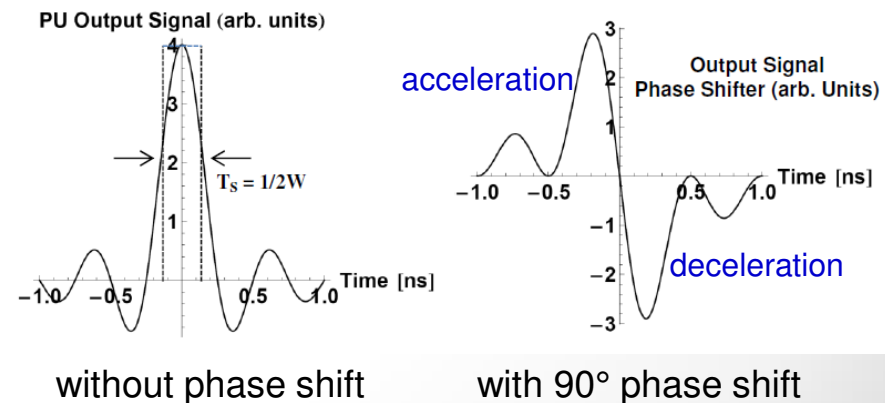
simplified scheme without notches allows efficient pre-cooling



compared to notch filter cooling the delay line is open and

a 90° phase shifter is added

⇒ differentiation of the signal



Fokker-Planck Equation

$$\frac{\partial \psi(\delta, t)}{\partial t} = -\frac{\partial}{\partial \delta} [F(\delta, t) \psi(\delta, t) - D(\delta, t) \frac{\partial}{\partial \delta} \psi(\delta, t)]$$

distribution function $\psi(\delta, t)$

coordinate $\delta = x, y, \delta p/p$

cooling term $F(\delta, t) = f_0 \delta$

diffusion term $D(\delta, t) = \frac{1}{2} f_0 \langle (\delta)^2 \rangle$

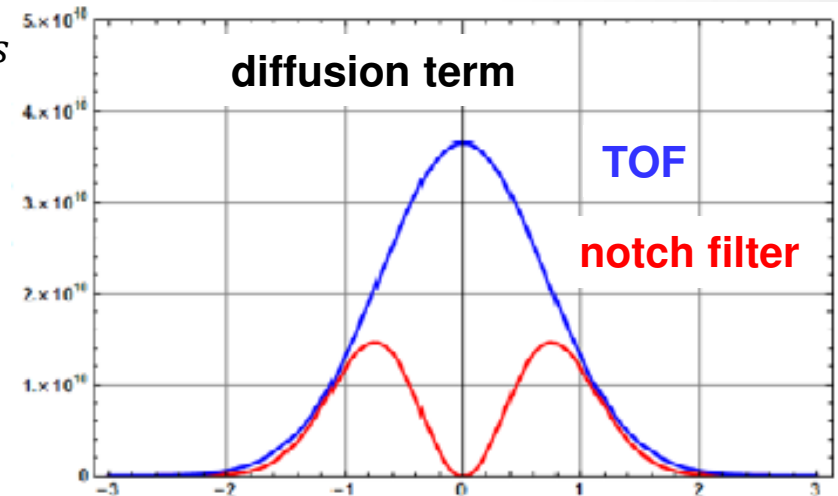
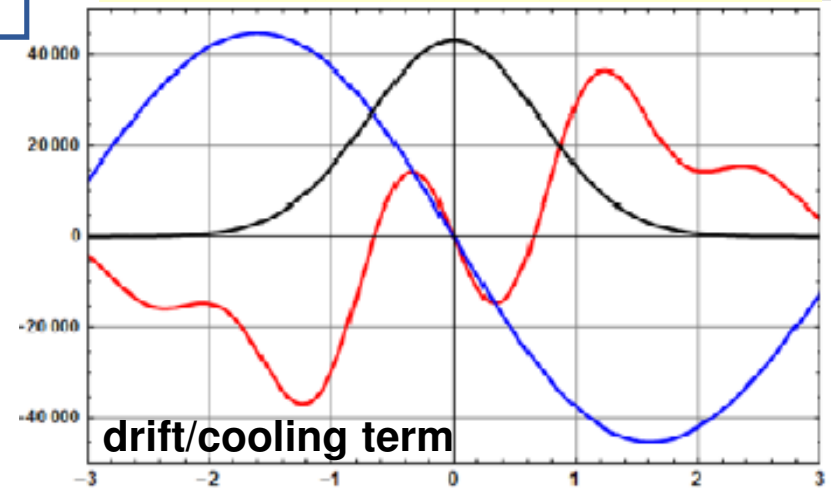
$$\Delta \delta = -g \frac{2W}{Nf_0} \delta \quad \langle (\Delta \delta)^2 \rangle = g^2 \delta_n^2 \text{rms}$$

equilibrium distribution ($\frac{\delta \psi}{\delta t} = 0$) is a Gaussian

$$\psi(\delta) = \frac{N}{\sqrt{2\pi}\sigma} \exp[-\delta^2 / (2\sigma^2)]$$

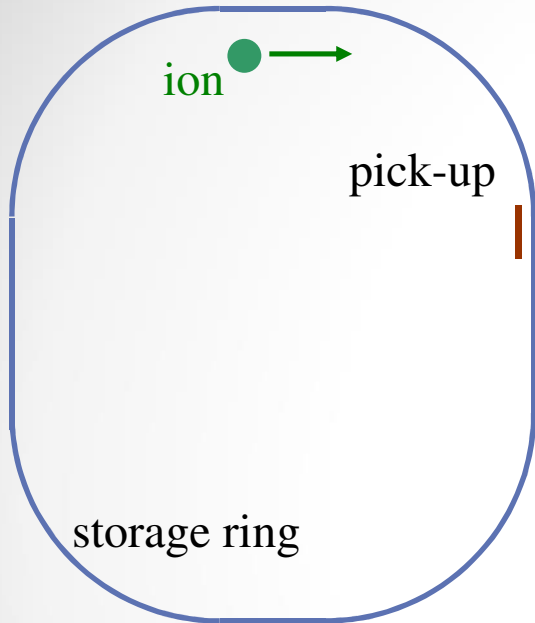
$$\sigma = \sqrt{\frac{D N}{g 2W}}$$

longitudinal cooling
TOF and notch filter method

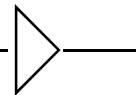


momentum deviation $\delta p/p [10^{-3}]$

Schottky Diagnostics



signal amplification

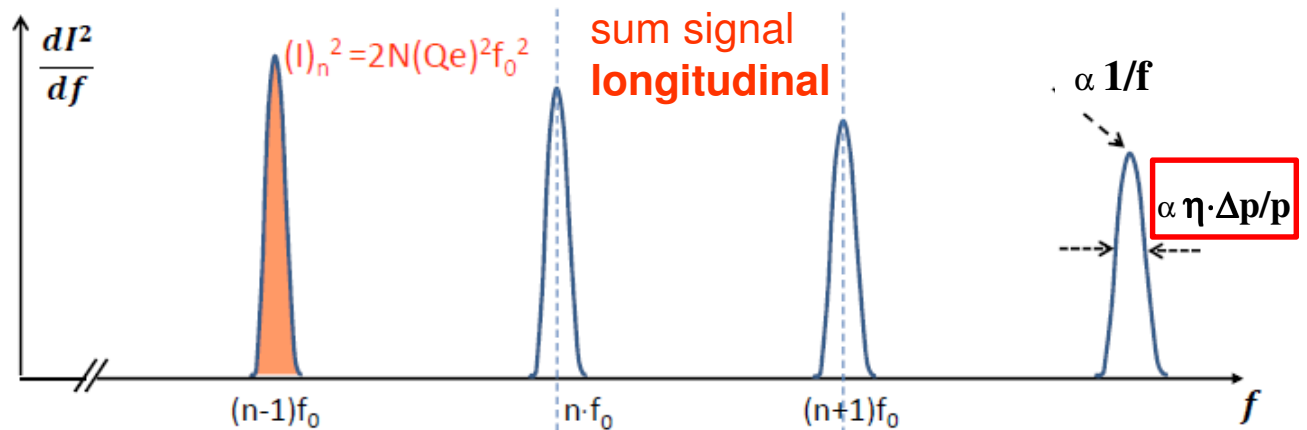


frequency analysis

momentum slip factor η

$$\eta = \frac{1}{\gamma^2} - \frac{1}{\gamma_t^2}$$

transition energy γ_t



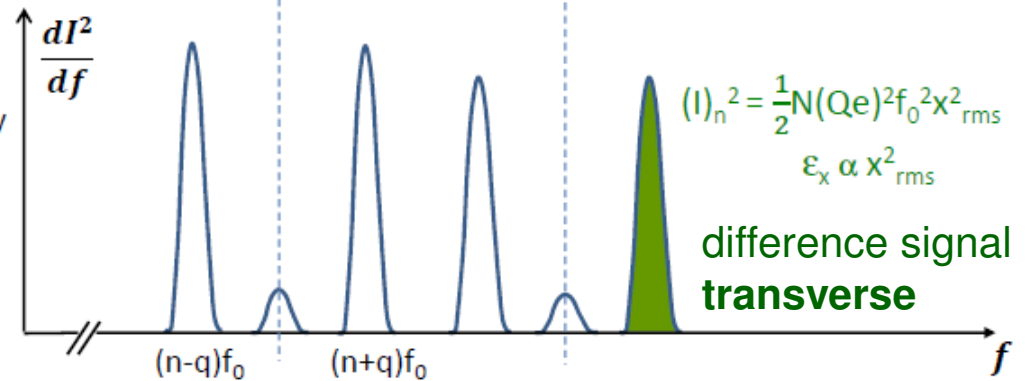
measurement of momentum spread

$$\frac{\Delta p}{p} = \frac{1}{\eta} \frac{\Delta f}{f}$$

measurement of transverse emittance

$$(I)_n^2 \propto \epsilon_x$$

N particle number
 f_0 revolution frequency
 Qe ion charge
 n harmonic number
 q non-integer tune



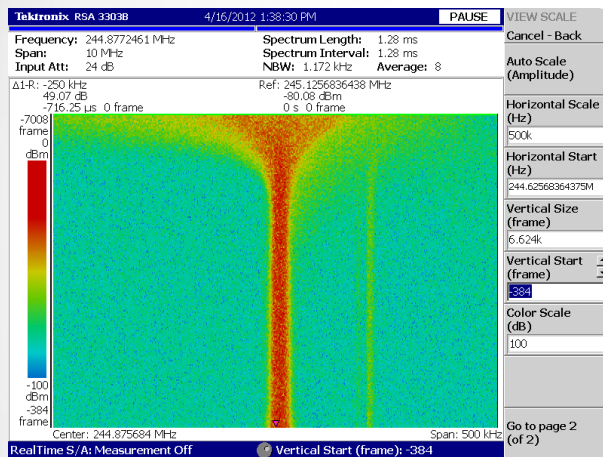
Comparison of Longitudinal Cooling Methods

Ar¹⁸⁺ 400 MeV/u

longitudinal momentum distribution versus time

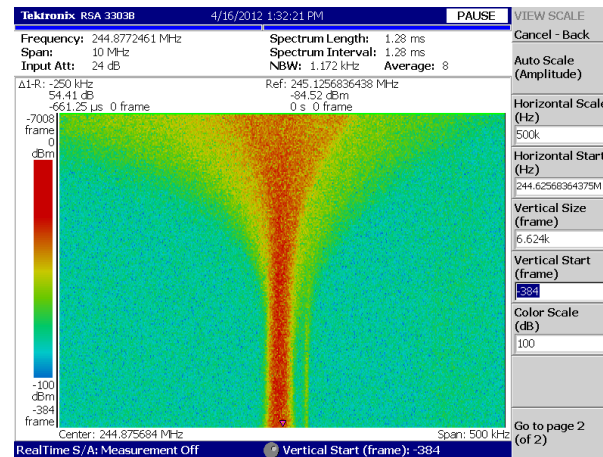
measured at the ESR
heavy ion storage ring
Schottky signal observed
at 245 MHz (h=124)

Palmer cooling



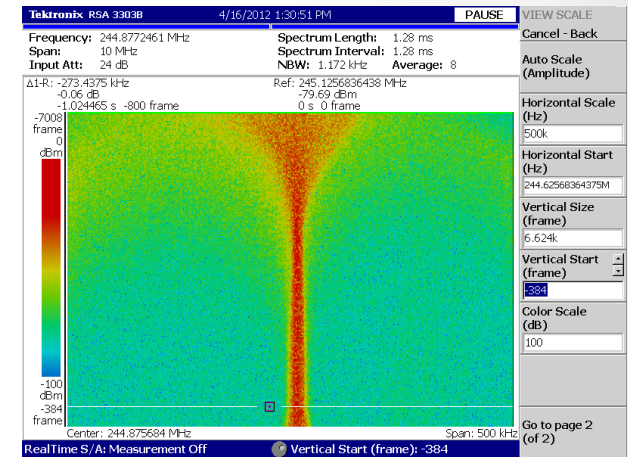
large momentum capture range
fast cooling
good final momentum spread
drawback: horizontal heating
needs to be compensated
by horizontal cooling

Time-of-Flight cooling



large momentum capture range
slower cooling
moderate final momentum spread
simple set-up
no special lattice requirement

Notch filter cooling

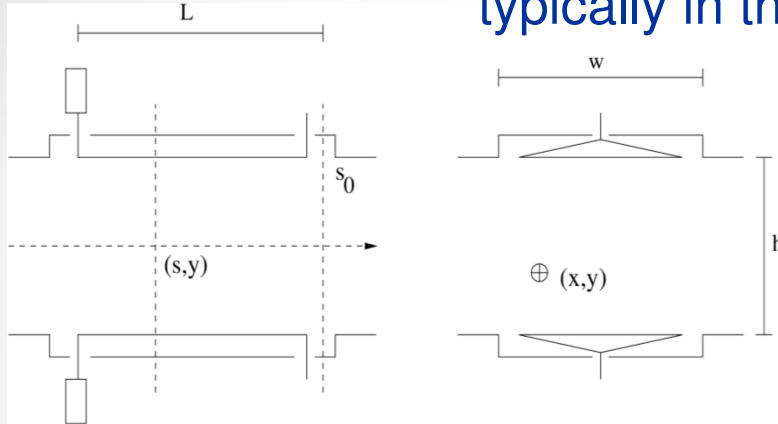


reduced momentum capture range
good cooling rate
smallest final momentum spread
most elaborate rf hardware
issue of notch filter stability

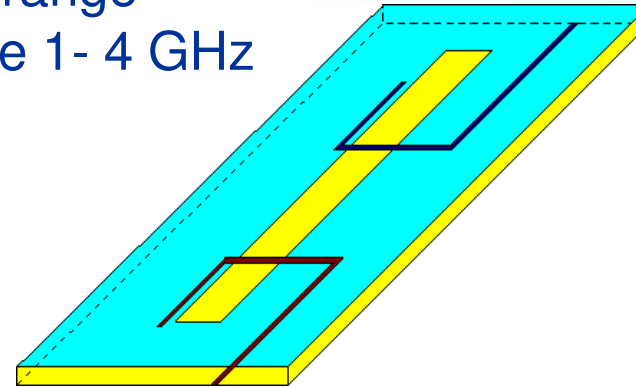
Electrode Structures

electrode size matched to the frequency range

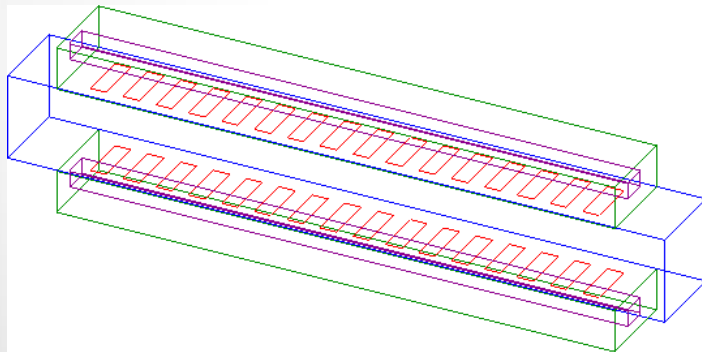
typically in the range 1- 4 GHz



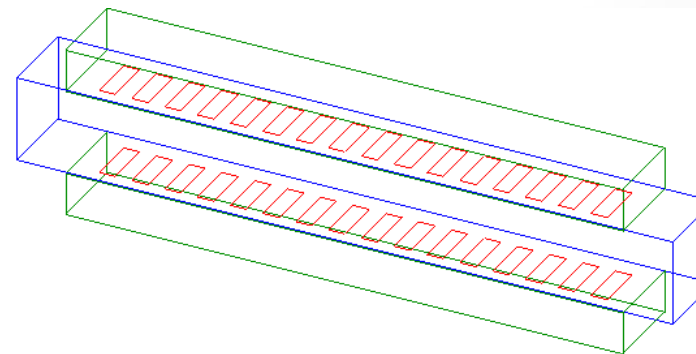
quarter wave pick-up
universal backward coupler



transverse slotline pick-up
*transverse microwave slotline
coupled to two microstrip lines*



Falin type structure
*travelling wave coaxial waveguide
with slot coupling*



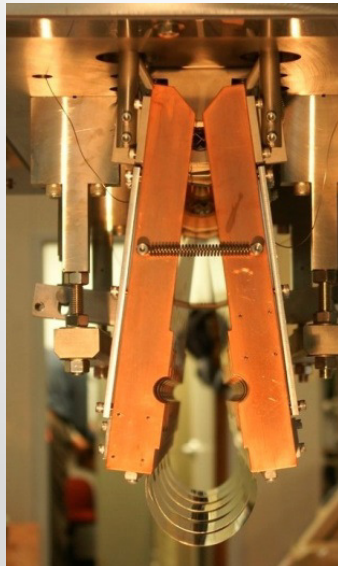
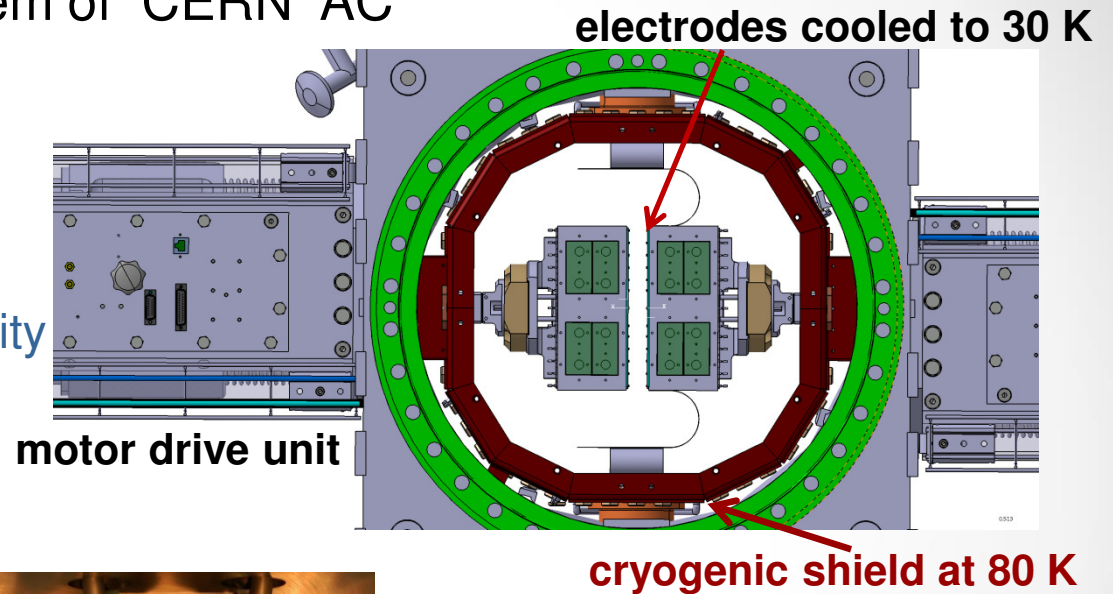
slotted waveguide structure
*travelling wave rectangular waveguide
with slot coupling*

Movable Electrodes

pioneered by the plunging system of CERN AC

more recently developed for:

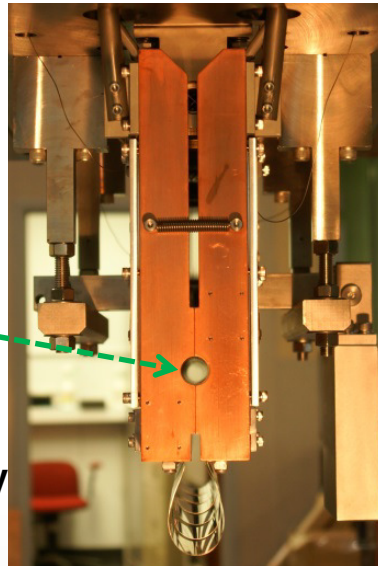
FAIR Collector Ring
stochastic cooling
improvement of sensitivity
repetition time down to 1 s
cooling during motion



← open position during injection and ramping

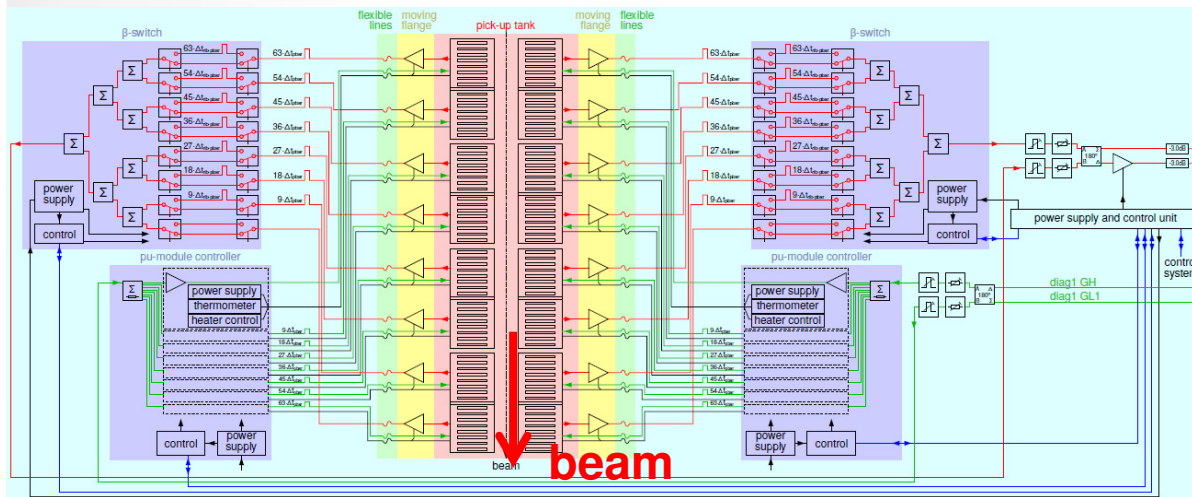
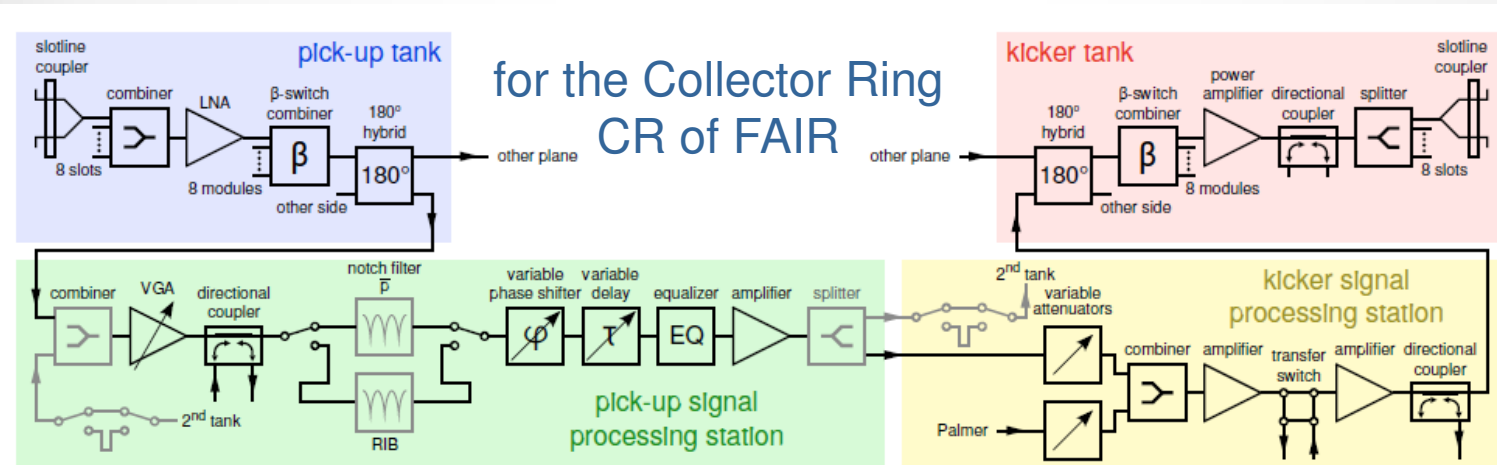
beam opening

→ closed for operation at the collision energy



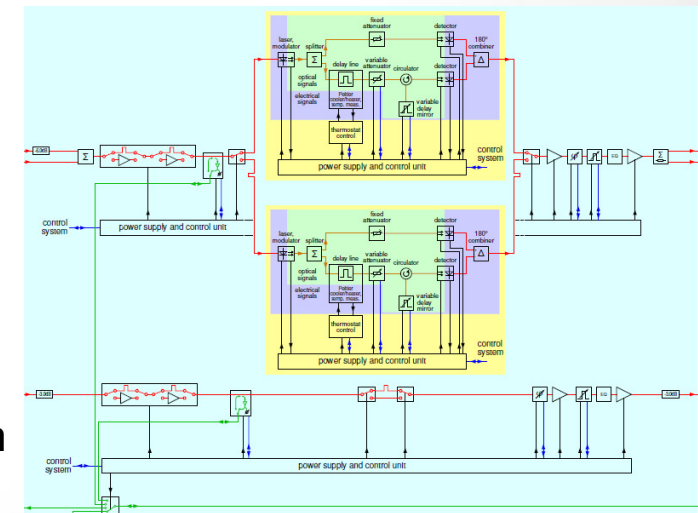
BNL RHIC Collider
operation after acceleration
in the collision mode
repetition time many hours
cooling after acceleration and closing

Stochastic Cooling RF Components



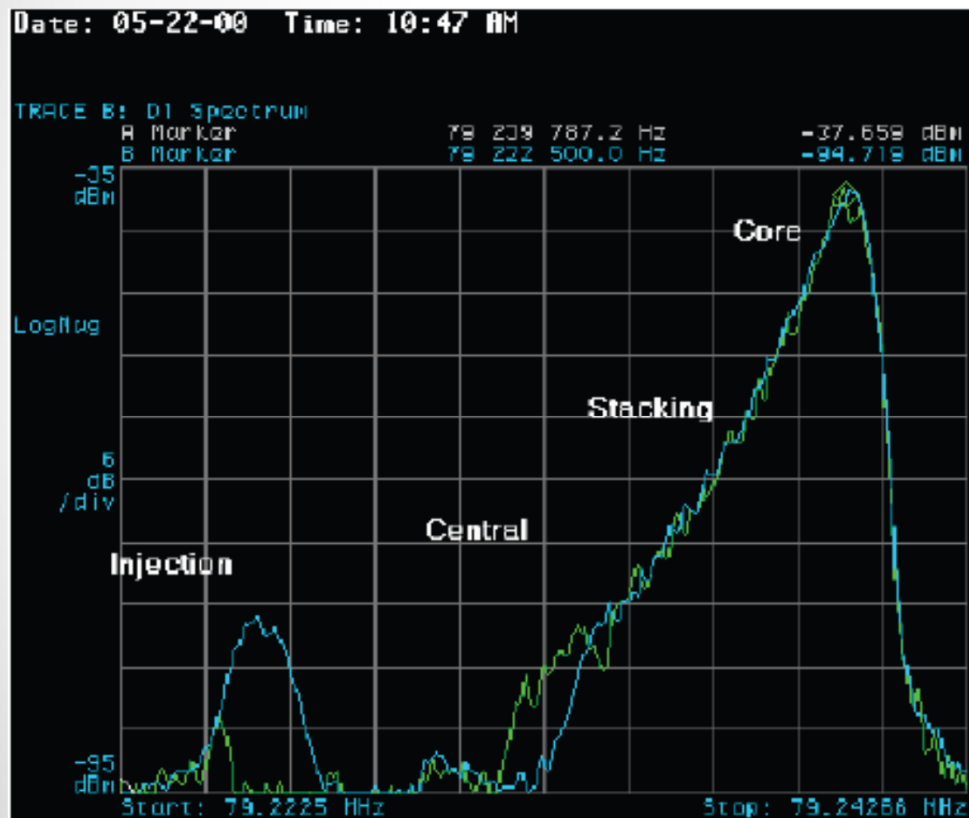
pick-up (kicker) tank
 summing of signals from different pick-ups along the beam
 with matched delay
 sum/difference of the two sides for longitudinal/transverse cooling

signal processing:
 delay, sum/difference,
 differentiation, filtering

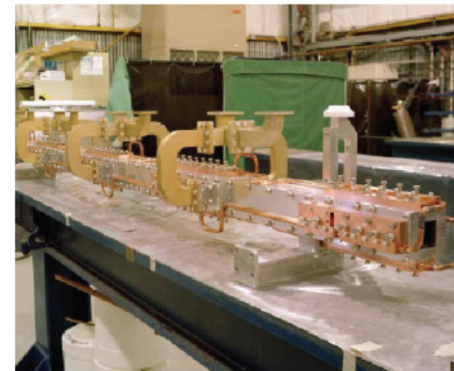


Antiproton Accumulation by Stochastic Cooling

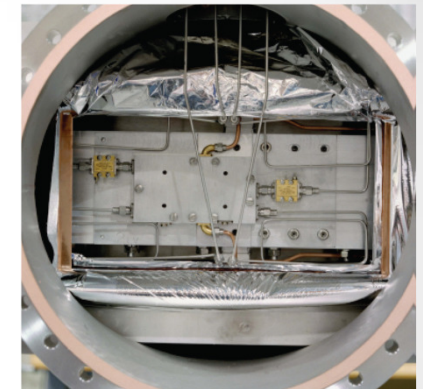
accumulation of 8 GeV antiprotons at accumulator ring, FNAL, shut down 09/2011
a similar facility AC/AA at CERN was operated until 11/1996



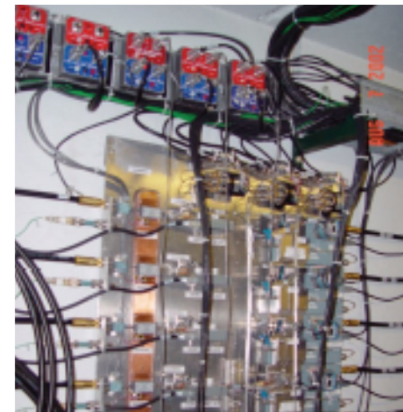
momentum distribution of accumulated
antiproton beam



kicker array



cryogenic microwave
amplifier



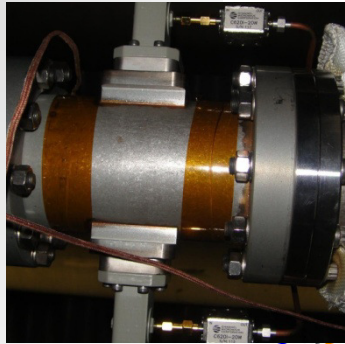
microwave electronics



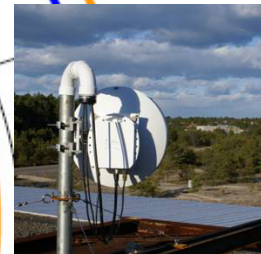
power amplifiers (TWTs)

RHIC – 3D stochastic cooling for heavy ions

longitudinal pickup



3 tanks with longitudinal (narrow band) kicker units

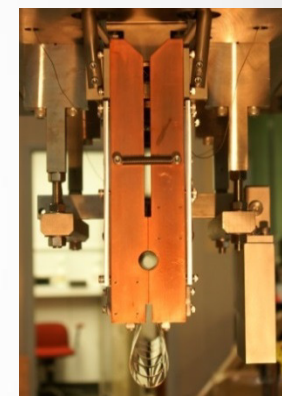
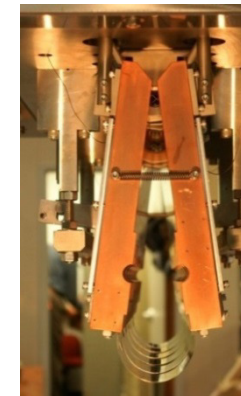


MicroWave Links, longitudinal

70 GHz carrier with 16 GHz local oscillator

Fiber Optic Links, transverse

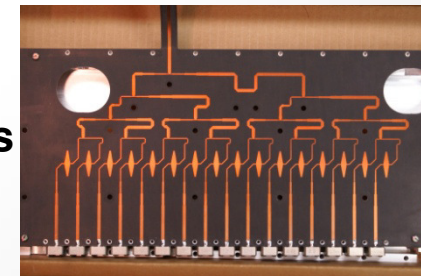
Transverse pickups, FO
Transverse kicker



longitudinal kicker open for injection and ramping (left), closed during cooling (right)

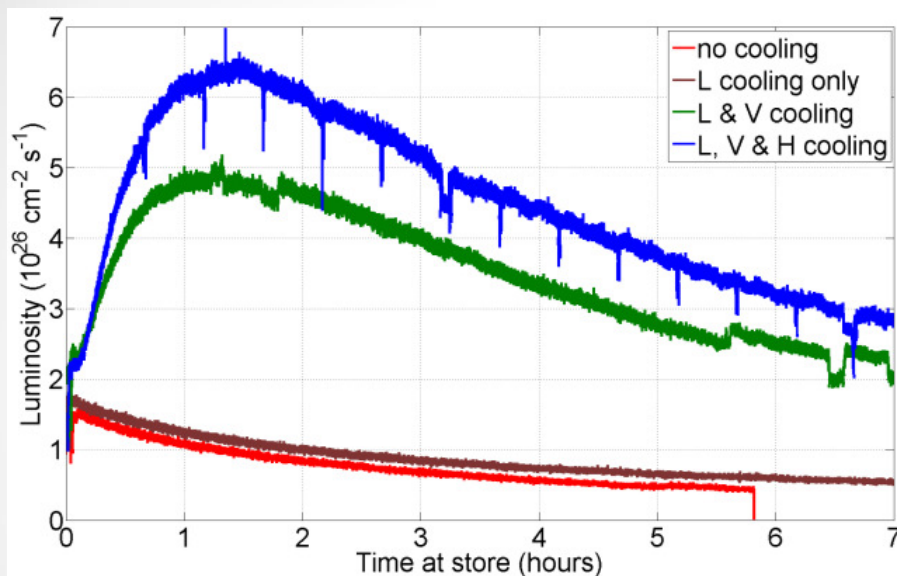


horizontal and vertical pickups



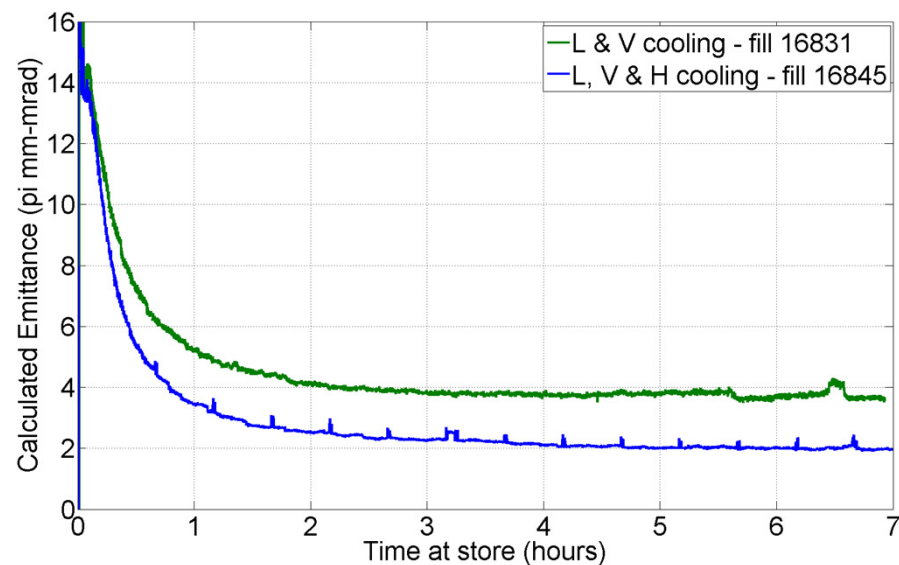
RHIC Luminosity production

luminosity with/without stochastic cooling



For Uranium-on-Uranium collisions the cooling increased the integrated luminosity per store by a factor of 5

beam emittance during store



The transverse emittances were reduced by x 4 with a cooling time of $\frac{1}{2}$ hour

M. Brennan et al.

Stochastic Cooling of Rare Isotopes at GSI

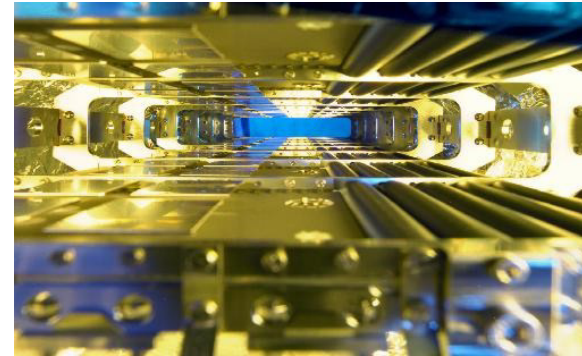
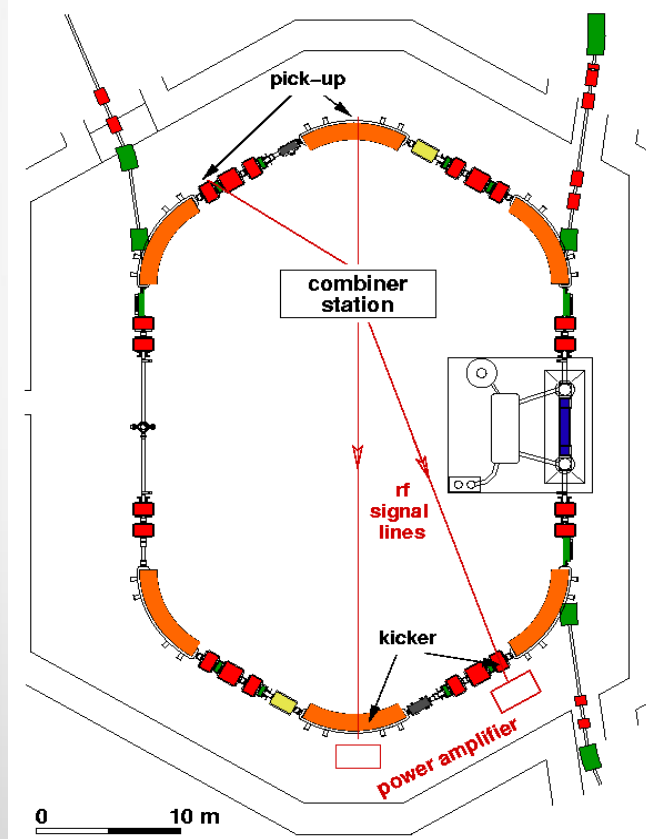
fast pre-cooling of hot rare isotopes

energy 400 (-550) MeV/u

bandwidth 0.8 GHz (range 0.9-1.7 GHz)

$\delta p/p = \pm 0.35\%$ \rightarrow $\delta p/p = \pm 0.01\%$

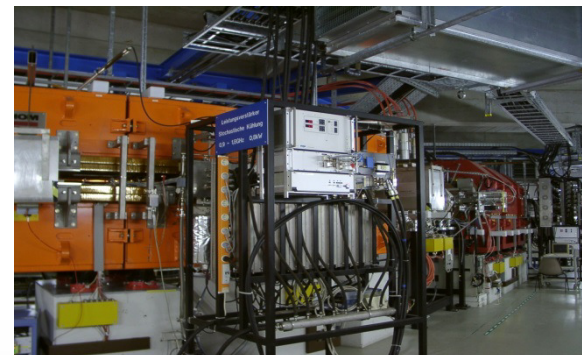
$\epsilon = 10 \times 10^{-6} \text{ m}$ \rightarrow $\epsilon = 2 \times 10^{-6} \text{ m}$



electrodes installed in the ultrahigh vacuum inside magnets



combination of signals from electrodes



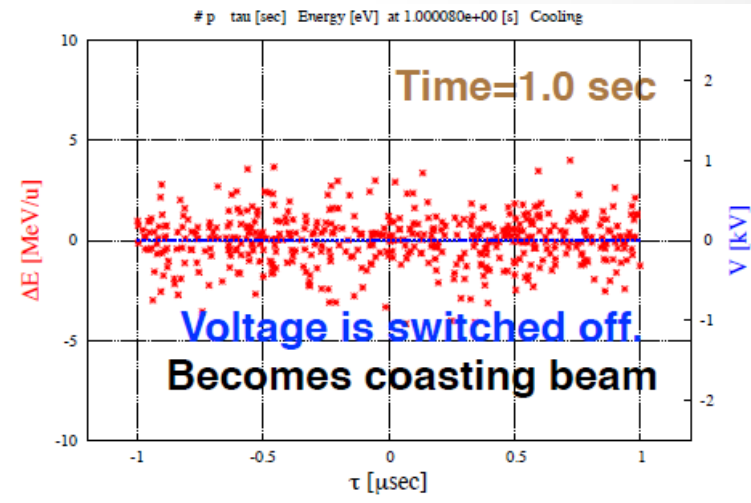
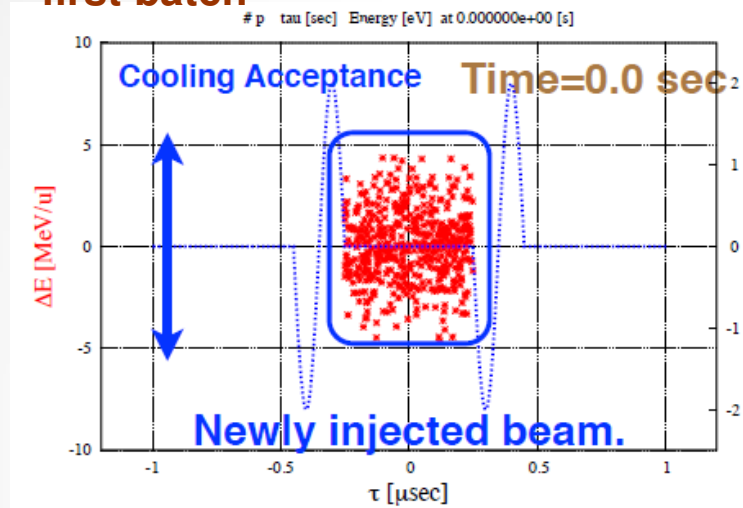
power amplifiers for generation of correction kicks

Barrier Bucket Accumulation by Stochastic Cooling

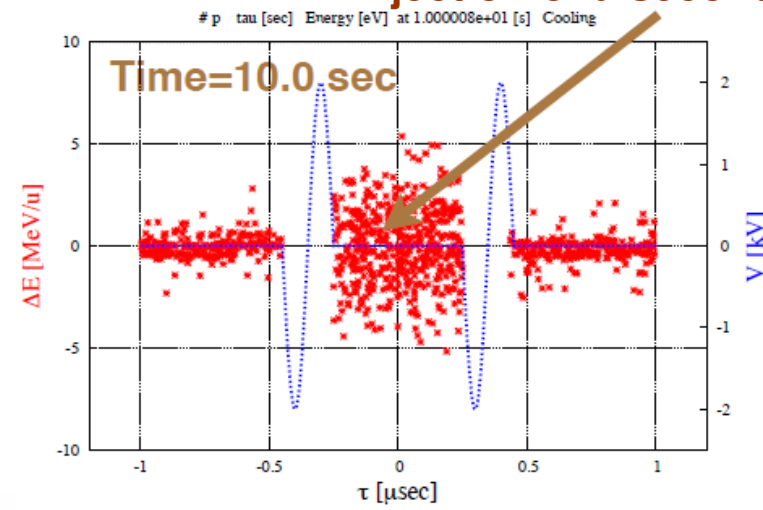
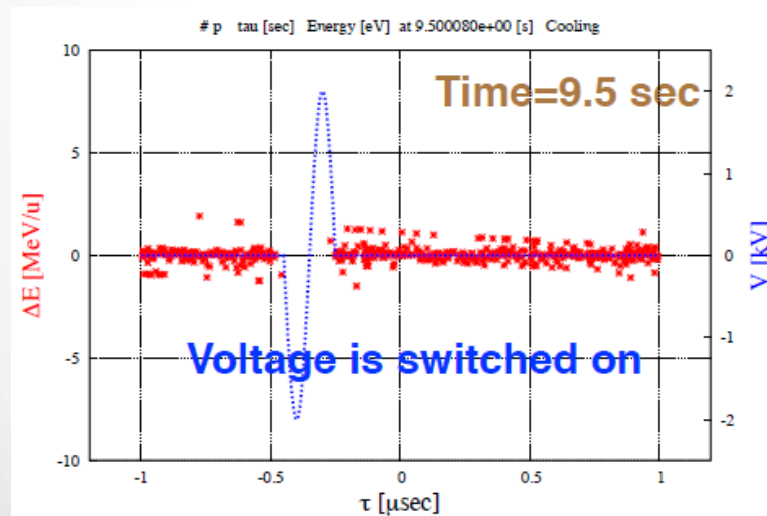
proposed for the accumulation of antiprotons in HESR

a similar method was applied in the Recycler (FNAL)

first batch



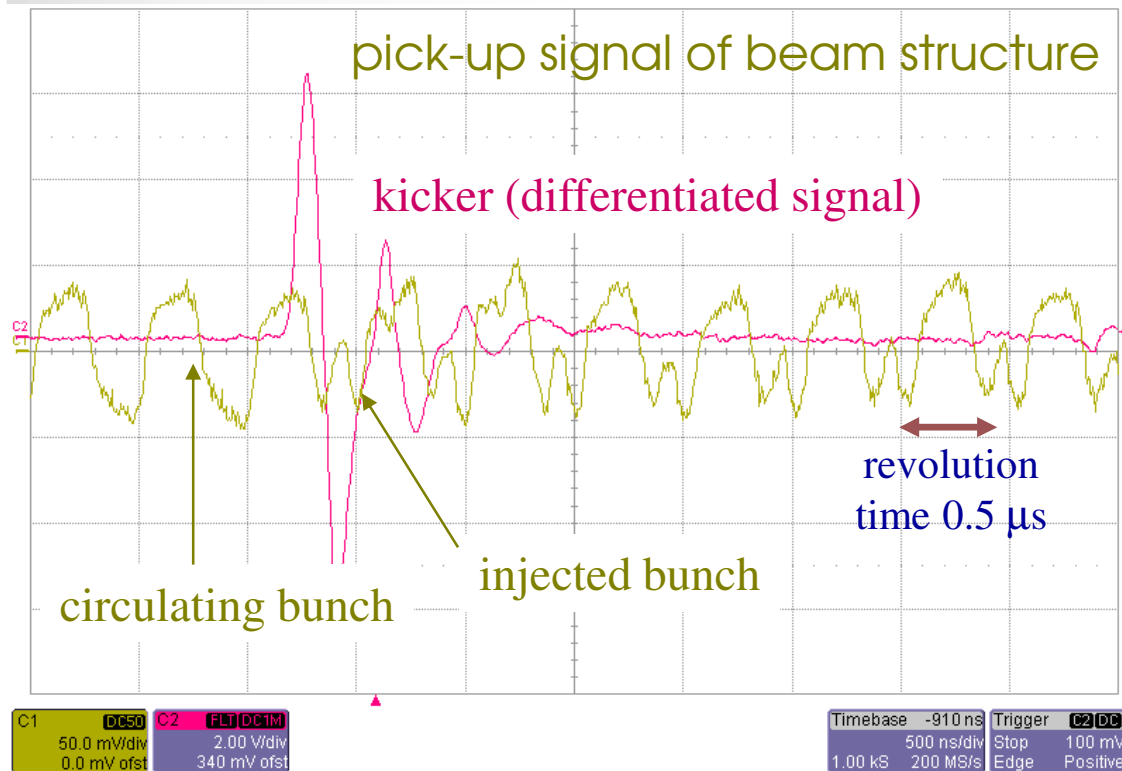
injection of a second batch



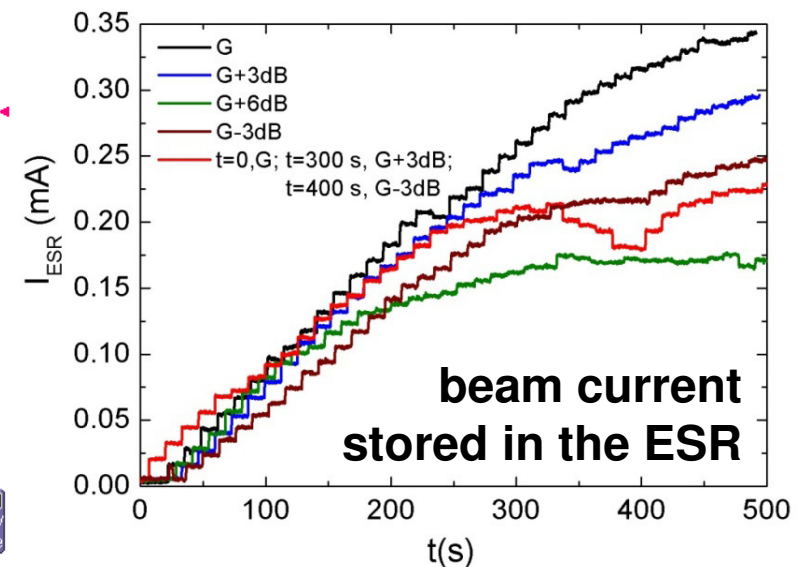
simulation by T. Katayama

Proof of Principle Experiment at ESR

Longitudinal Accumulation with Stochastic Cooling



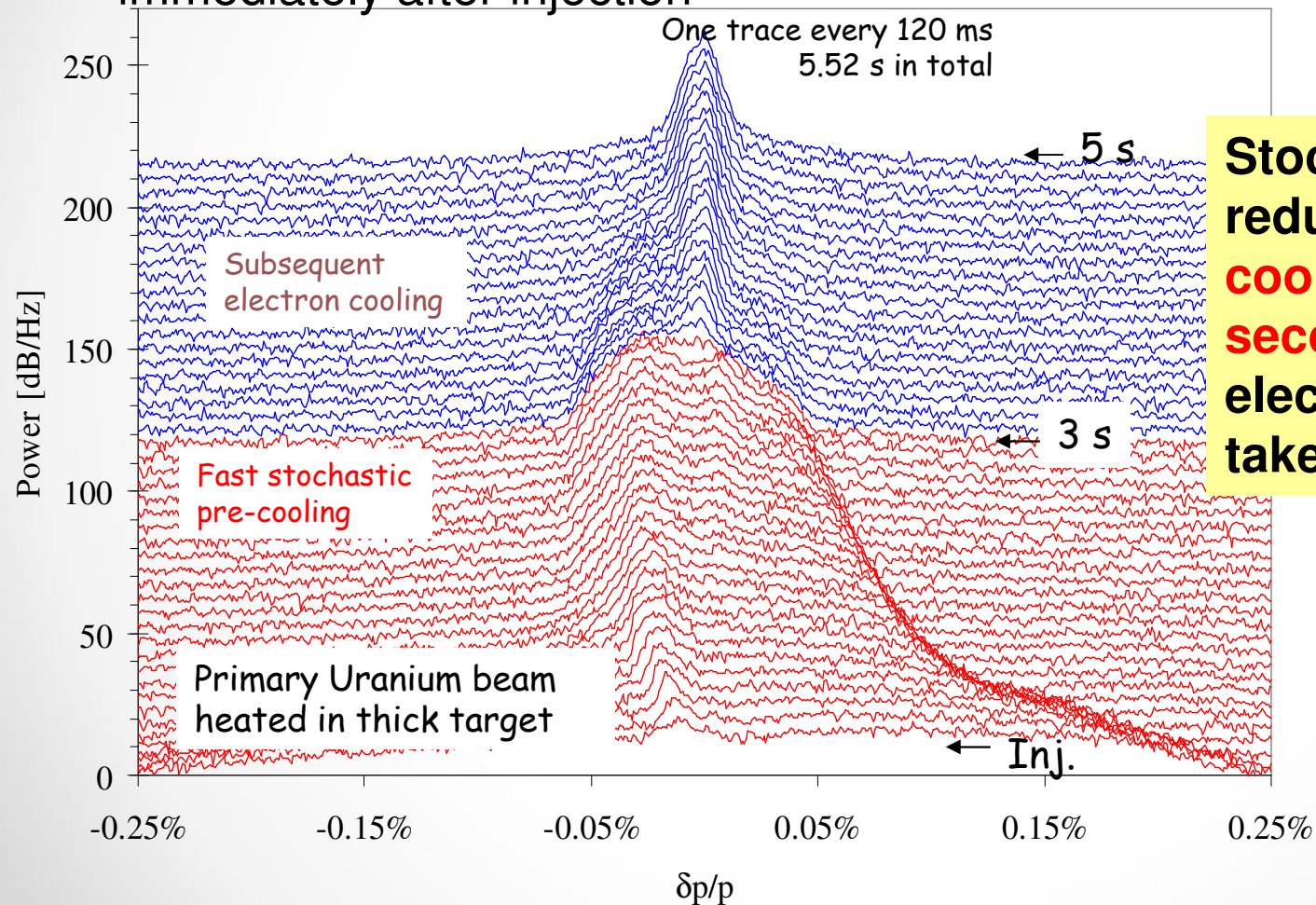
using a single bunch of Ar^{18+} at 400 MeV/u from SIS



at higher intensity and beam density heating can dominate
 \Rightarrow mitigate by variation of the system gain
 in the course of the cooling process

Combination of Stochastic and Electron Cooling

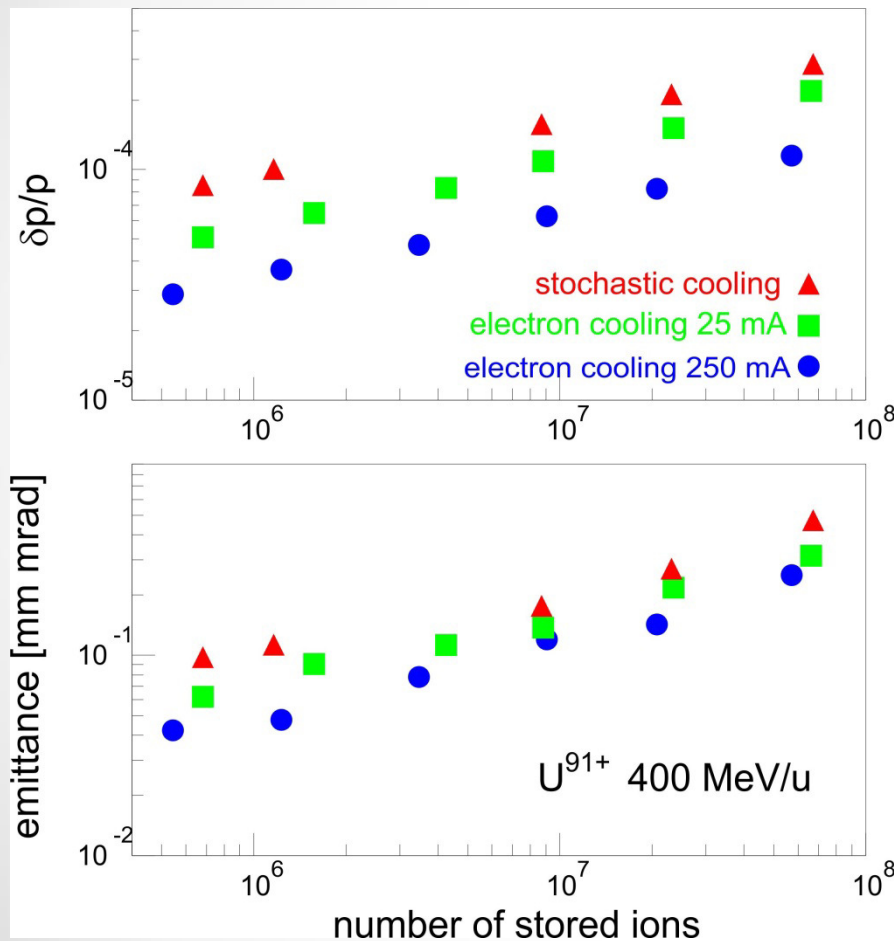
stochastic pre-cooling + final electron cooling
immediately after injection



Stochastic pre-cooling reduces the **total cooling time to a few seconds**, electron cooling only takes 10 - 60 s

lifetime due to nuclear decay of rare isotopes can be seconds or less

Equilibrium Beam Parameters of the Cooled Beam in the ESR



limited by Intrabeam Scattering

Electron cooling results in smaller momentum spread and smaller emittance.

The equilibrium is a balance between the cooling rate and the heating rate by intrabeam scattering.

calculated IBS-heating/cooling rate [s⁻¹]

	longit.	transv.
stoch. cool.	0.9 - 2.2	0.5 - 1.3
el. cool. [25 mA]	2.0 - 6.0	1.4 - 3.3
el. cool. [250 mA]	18 - 58	7 - 10

electron cooling is more powerful in producing cold beams, it provides higher cooling rate for cold beams

Stochastic Cooling Systems

CERN, Geneva, Switzerland

Intersecting Storage Ring (ISR) 1977
Initial Cooling Experiments (ICE) 1978
Antiproton Accumulator (AA) 1981
Low Energy Antiproton Ring (LEAR) 1983
Antiproton Collector (AC) 1987
Antiproton Decelerator (AD) 1999

FNAL, Chicago, USA

Test Ring 1979
Debuncher Ring 1985
Accumulator Ring 1985
Recycler Ring 1997

NAP-M, INP, Novosibirsk, Russia 1979

TARN, Tokyo, Japan 1983

ESR, GSI, Darmstadt, Germany 1997

COSY, FZJ, Jülich, Germany 1997

RHIC, BNL, Brookhaven, USA 2009

CSRe, IMP, Lanzhou, China 2016

decommissioned

in operation

Future Aspects of Stochastic Cooling

increased cooling rate:

- larger bandwidth of cooling system
- dedicated ring lattices

bunched beam cooling:

- increased luminosity in colliders

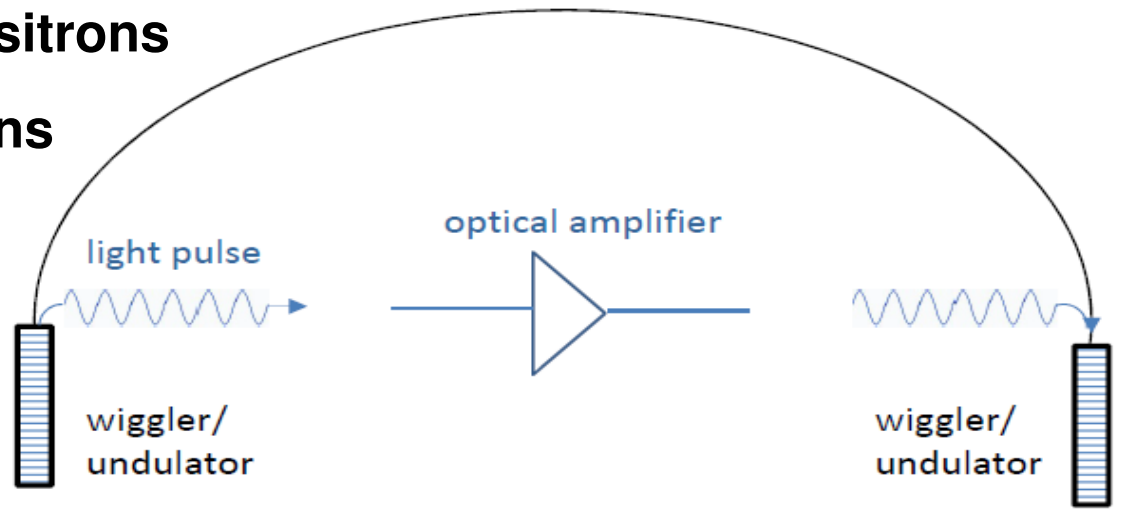
new accumulation schemes employing stochastic cooling

development of technologies

- e.g. optical components
- new rf components

Optical Stochastic Cooling

applicable to electrons/positrons
or very high energy hadrons

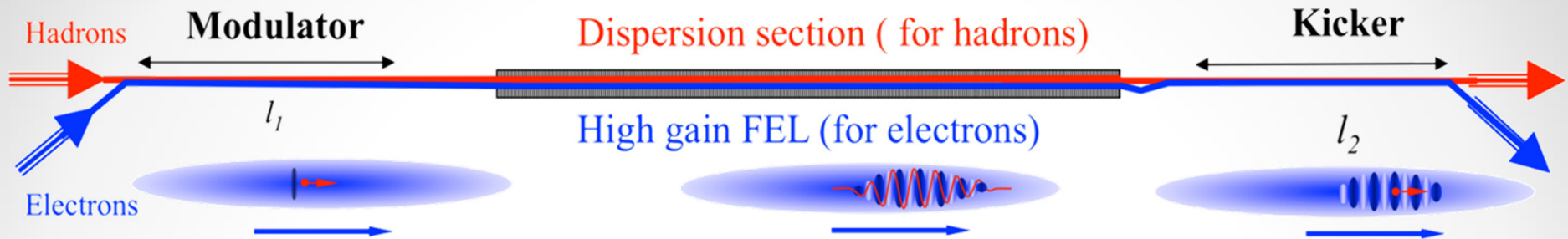


large bandwidth (up to THz) of optical system

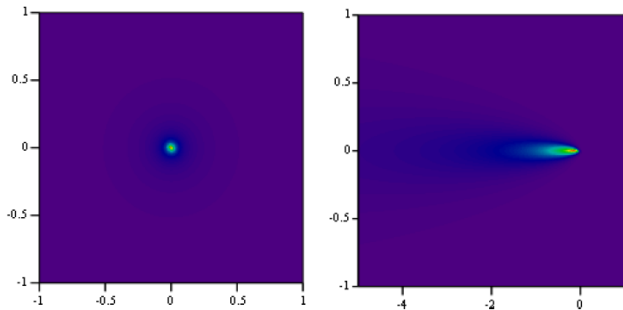
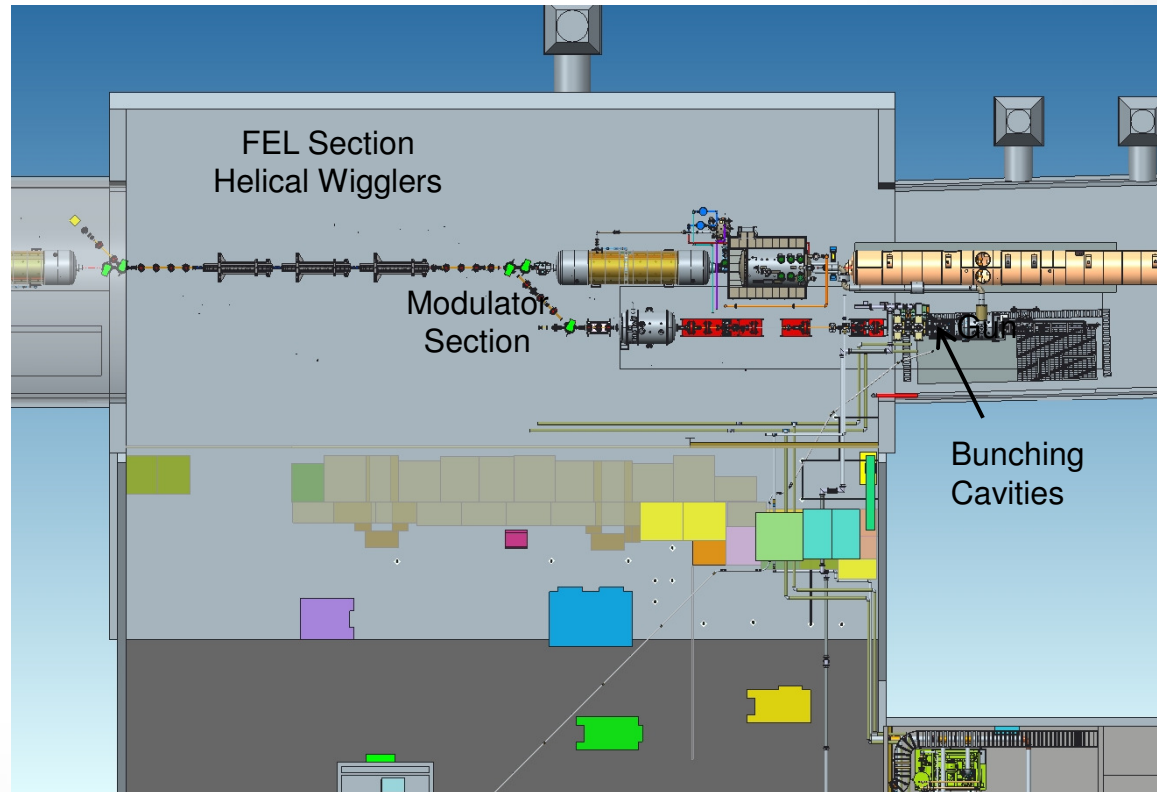
transverse cooling by longitudinal-transverse coupling

accelerator test facility **IOTA (Fermilab)** is preparing a demonstration of optical stochastic cooling

Coherent Electron Cooling



test experiment
proposed at
RHIC (Brookhaven)



simulations of an ion
in the electron plasma

Comparison of Cooling Methods

Stochastic Cooling

Useful for: low intensity beams
hot (secondary) beams
high charge
full 3D control

Limitations: high intensity beams
/problems beam quality limited
bunched beams

Electron Cooling

low energy
all intensities
warm beams (pre-cooled)
high charge
bunched beams

space charge effects
recombination losses
high energy

**laser cooling (of incompletely ionized ions)
and ionization cooling (of muons) are quite particular
and not general cooling methods**

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