



UNIVERSITÉ
DE GENÈVE

FACULTÉ DES SCIENCES

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Superconductors for magnets

From the materials to the technical conductors

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Outline

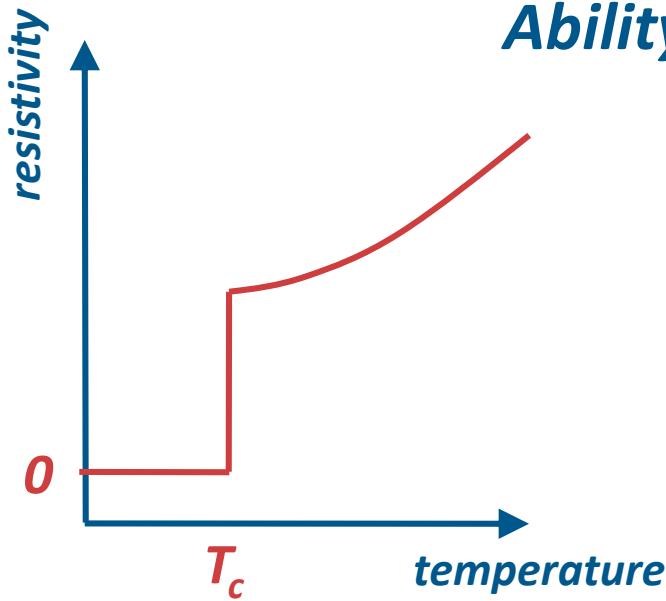
A short introduction to superconductivity

- *Type-I vs. Type-II – why Type-II is better?*
- *Vortex pinning and critical current*

From the materials to the technical conductors

- *LTS : Nb_3Sn properties and wire technology*
- *HTS : YBCO properties and wire technology*

Discovery of Superconductivity in 1911



Ability to carry a current without dissipation

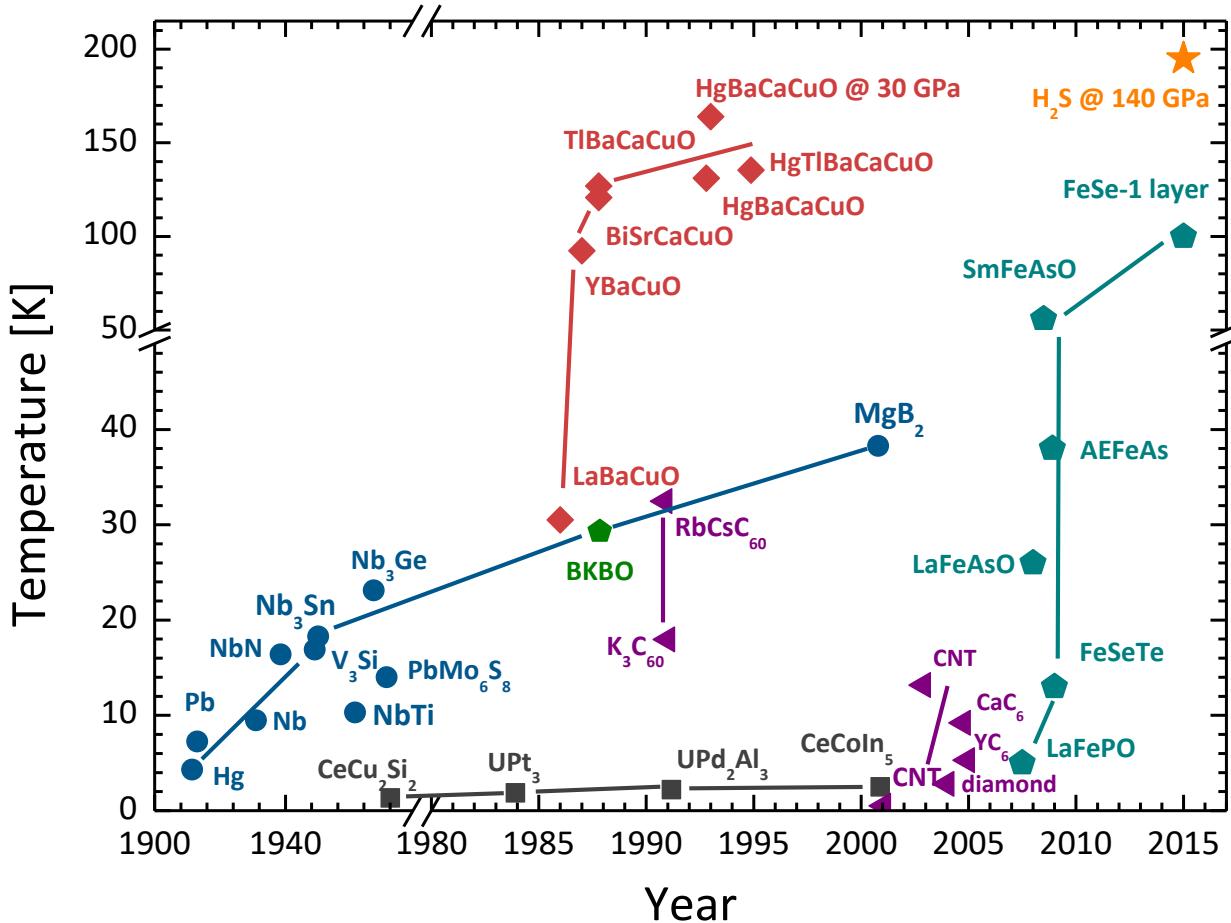
- *Transport of energy*
- *Generation of high magnetic fields*

Drawbacks:

Loss-less currents cannot exceed the critical current I_c

1000+ superconducting compounds, very few for practical use

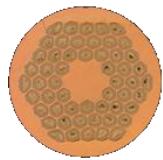
Superconductors History



NbTi



Nb₃Sn



MgB₂



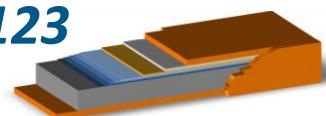
Bi2223



Bi2212



Y123



Night on
the Moon

Liquid nitrogen

Surface of Pluto

Liquid neon

Liquid hydrogen

Liquid helium

Key facts about superconductors

1) There are two characteristic lengths in a superconductor

$$\xi = \frac{\hbar}{\sqrt{2m^* |\alpha|}}$$

coherence length

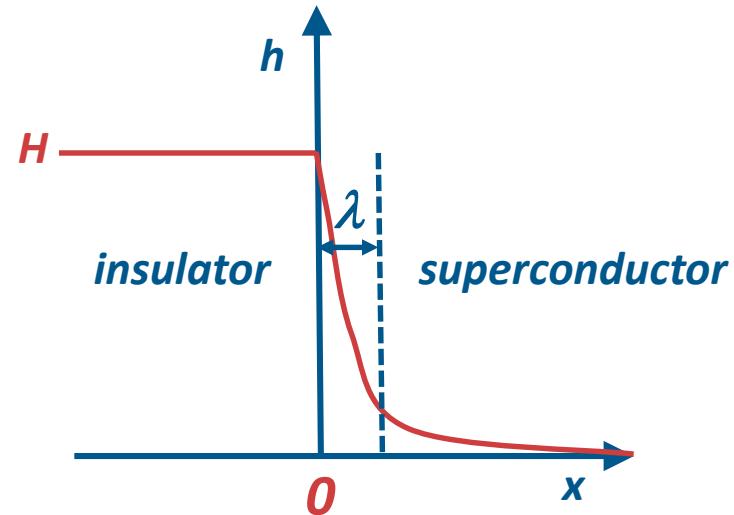
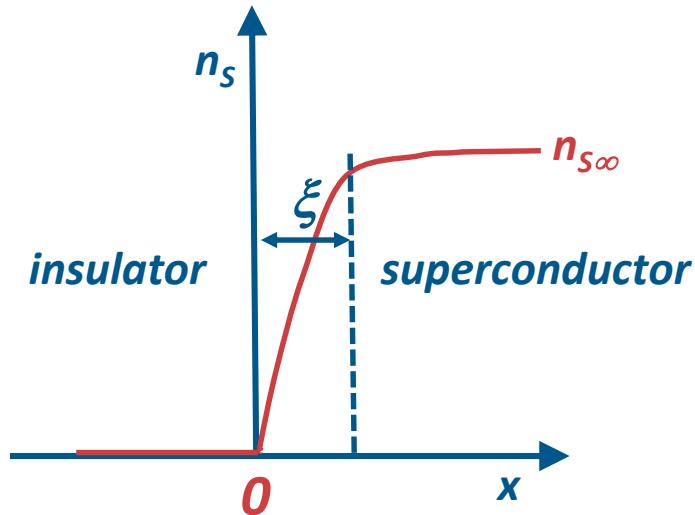
and

$$\lambda = \sqrt{\frac{m^* c^2}{4\pi n_s^2 e^*}}$$

penetration depth

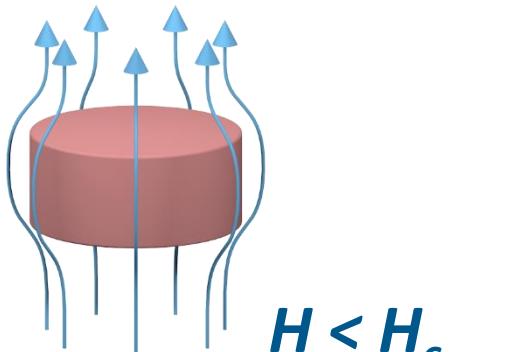
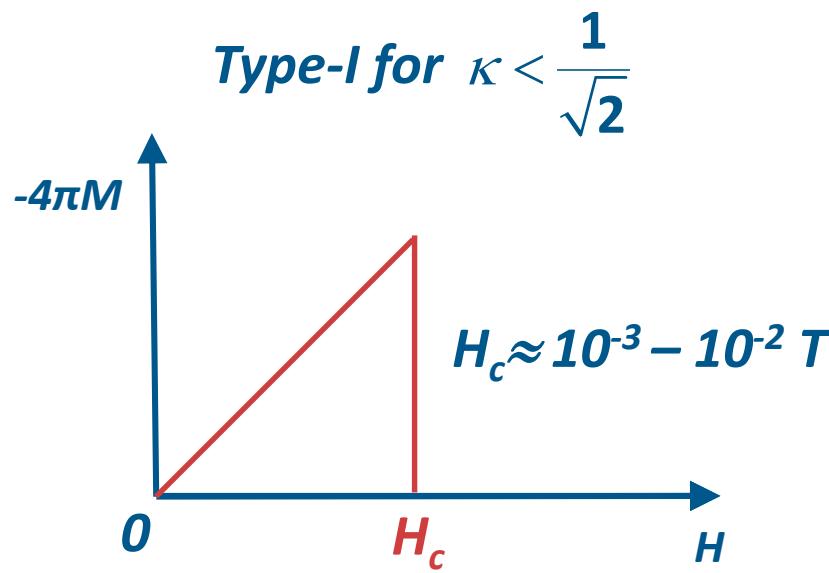
ξ defines the space modulation of the “superelectron” density n_s

λ characterizes the distance to which a magnetic field penetrates into a superconductor

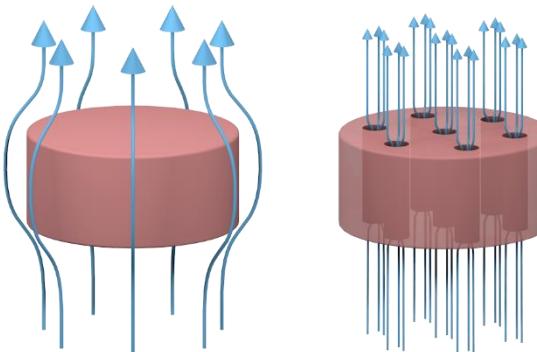
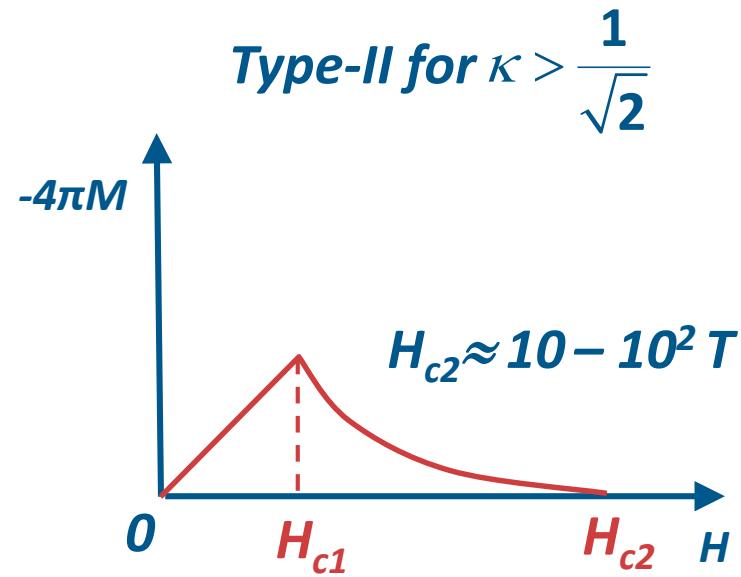


Key facts about superconductors

2) There are two types of superconductors, depending on $\kappa = \frac{\lambda}{\xi}$
Ginzburg-Landau parameter



$H < H_c$
The Meissner Effect



$H < H_{c1}$ $H_{c1} < H < H_{c2}$

$$-4\pi M = H - B$$

Key facts about superconductors

- 3) *In a type-I superconductor, superconducting currents are confined to the surface in a λ -thick layer*

- 4) *In a type-II superconductor, the critical fields are related to the characteristic lengths*

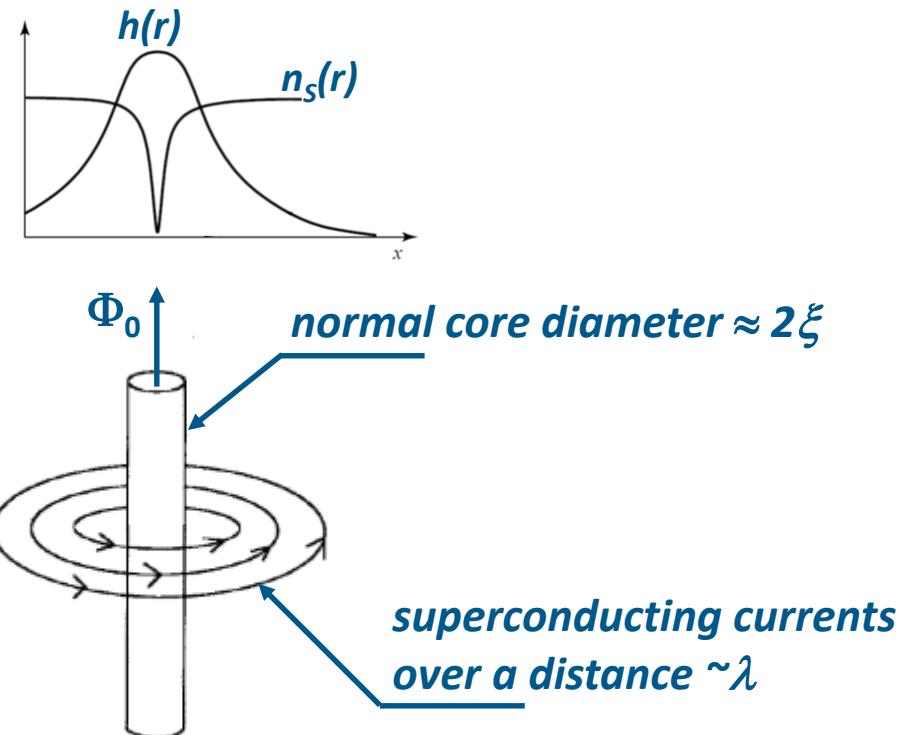
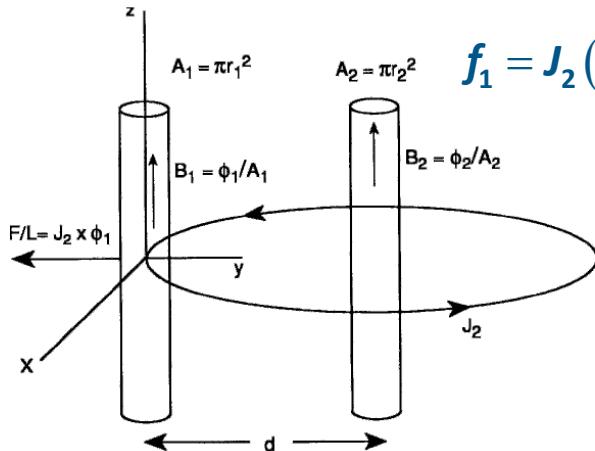
$$H_{c1} = \frac{\Phi_0}{4\pi\lambda^2} \ln \kappa = \frac{H_c}{\sqrt{2}\kappa} \ln \kappa \quad H_{c2} = \frac{\Phi_0}{2\pi\xi^2} = \sqrt{2}\kappa H_c$$

- 5) *In a type-II superconductor, magnetic flux penetrates beyond H_{c1} . The entering flux is fractionated in vortices, each one carrying a flux quantum $\Phi_0 = hc/2e$*

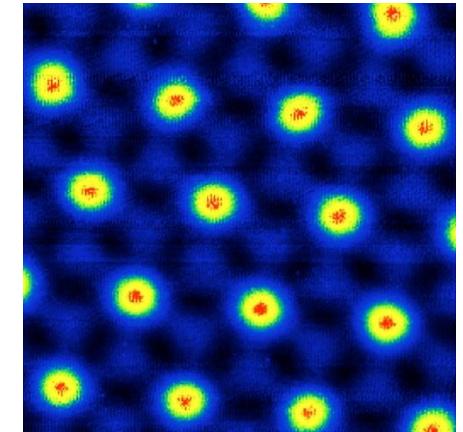
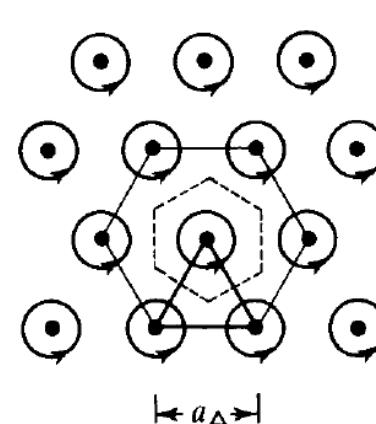
What is a vortex?



Vortices repel each other...



The Abrikosov lattice
... and arrange on a regular lattice



Vortex motion and dissipation: the Flux Flow

Let's focus on the effects of a transport current density J

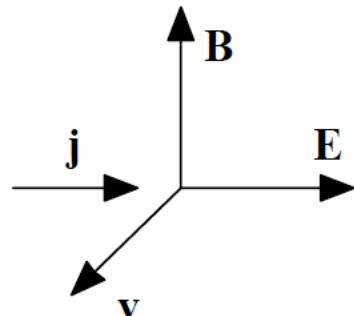
On a single vortex

$$\mathbf{f} = \mathbf{J} \times \frac{\Phi_0}{c} \hat{\mathbf{z}}$$

On the vortex lattice

$$\mathbf{F} = \sum \mathbf{f} = n_v \mathbf{f} = \mathbf{J} \times n_v \frac{\Phi_0}{c} \hat{\mathbf{z}} = \mathbf{J} \times \frac{\mathbf{B}}{c}$$

Therefore, vortices tend to move transverse to \mathbf{J} . If v is their velocity



$$\mathbf{E} = \mathbf{B} \times \frac{\mathbf{v}}{c}$$

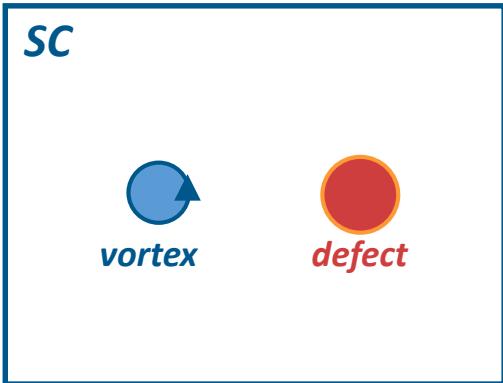
DISSIPATION !!

The Flux Flow resistivity

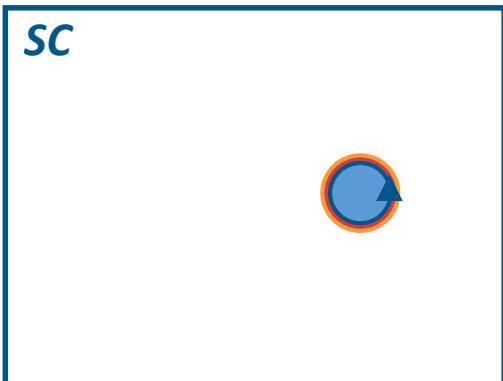
$$\rho_{ff} = \rho_n \frac{B}{B_{c2}}$$

Vortex-defect interaction

Let's consider defects – precipitates, grain boundaries, etc. – whose size is comparable with the coherence length ξ



$$\Delta G = \underbrace{\Delta G_{\text{condensation}}(\text{defect}) + \Delta G_{\text{condensation}}(\text{vortex})}_{\text{energy loss}} - \underbrace{\Delta G_{\text{mag}}}_{\text{energy gain}}$$



$$\Delta G = \underbrace{\Delta G_{\text{condensation}}(\text{defect})}_{\text{energy loss}} - \underbrace{\Delta G_{\text{mag}}}_{\text{energy gain}}$$

The defect acts as a potential well $U(r)$

The vortex is pinned at the defect position

The force to extract the vortex from the defect is $f_p = -\nabla U(r)$

Vortex-defect interaction

$$\mathbf{f} = \mathbf{J} \times \frac{\Phi_0}{c} \hat{\mathbf{z}}$$

Force exerted from J

$$f_p = J_c \times \frac{\Phi_0}{c} \hat{\mathbf{z}}$$

*Pinning Force exerted
from defects*

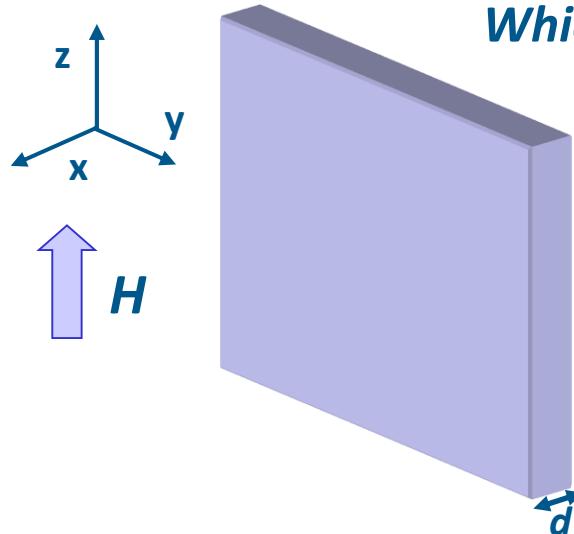
J_c is the critical current density

If $f < f_p$ then $v = 0$ and $\rho = 0$

If $f > f_p$ then $v \neq 0$ and $\rho \neq 0$

Only superconductors with defects are truly superconducting ($\rho = 0$) !!

Vortex pinning and critical state: the Bean model

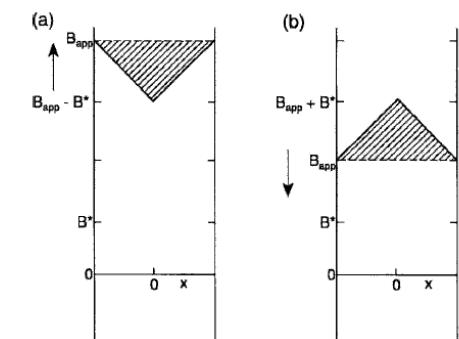
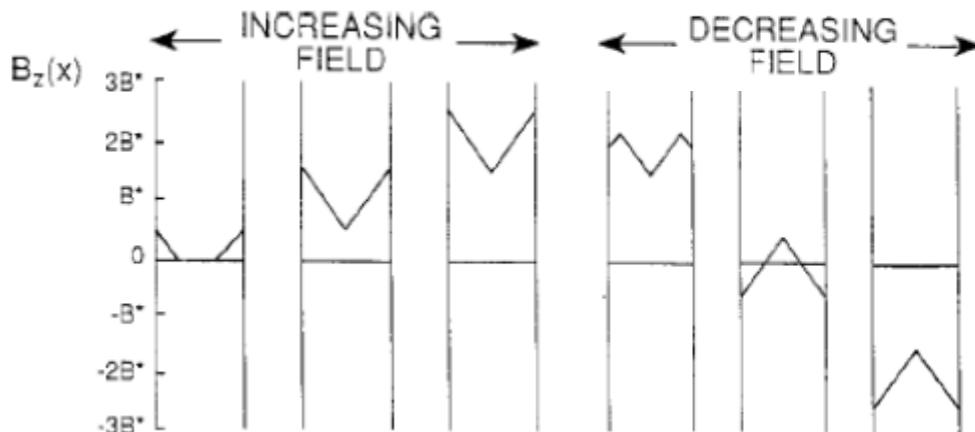


Which is the shape of the field profile in the superconductor?

$$1) \quad \nabla \times H = \frac{4\pi}{c} J$$

$$2) \quad F = \frac{JB}{c} = \frac{1}{4\pi} B \frac{dB}{dx} \leq F_p = \frac{J_c B}{c}$$

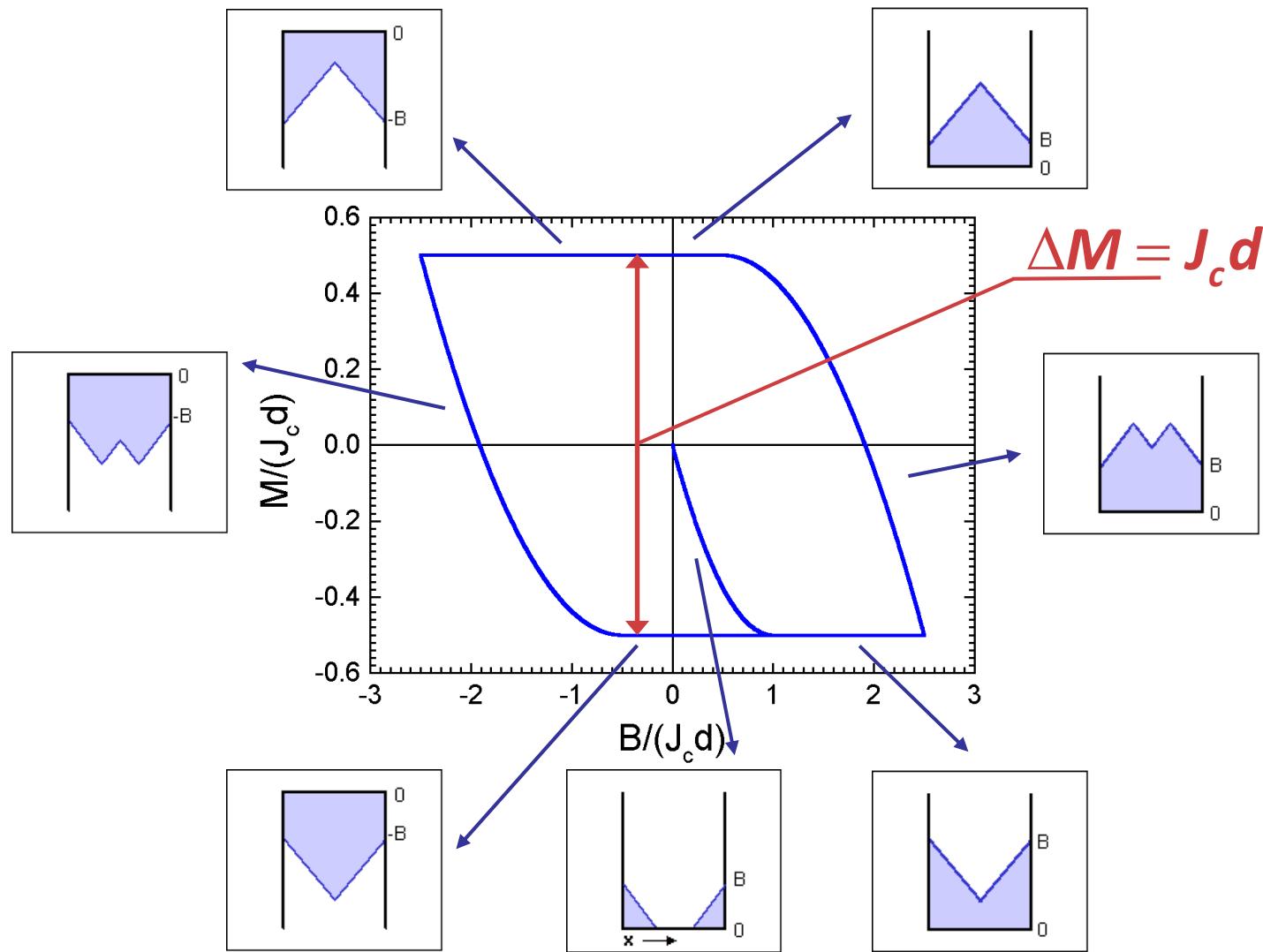
The assumption of the Bean model is $F = F_p \Rightarrow \frac{dB}{dx} = \frac{4\pi}{c} J_c$



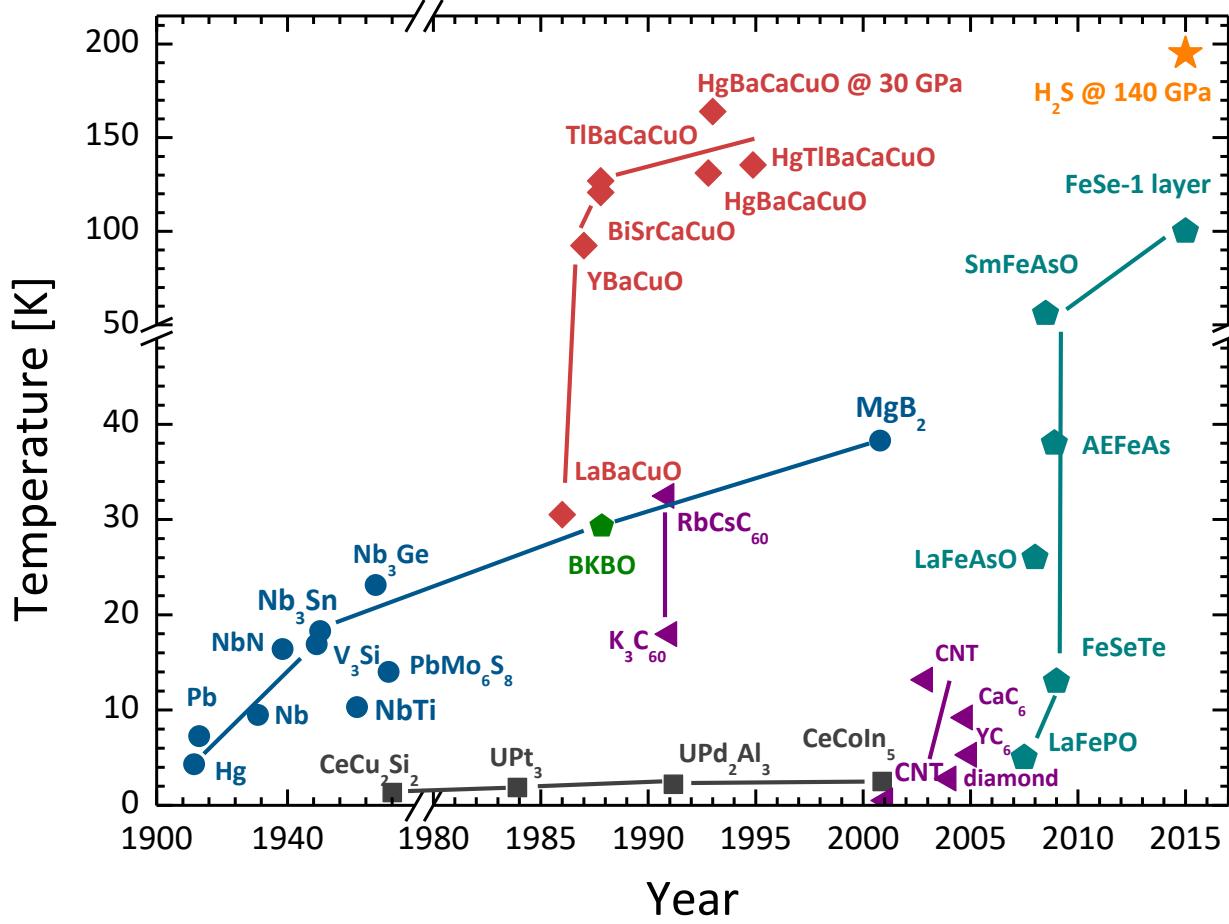
The triangle area is the magnetization of the sample

Critical state: Hysteresis loop

Hysteresis = LOSSES



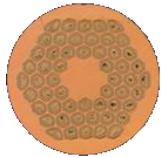
Superconductors History



$NbTi$



Nb_3Sn



MgB_2



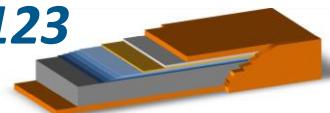
$Bi2223$



$Bi2212$

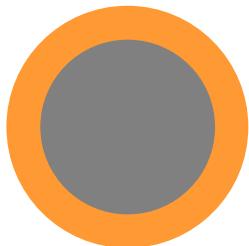


$Y123$



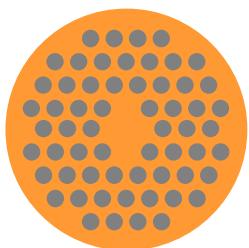
Why superconducting wires are (almost) all multifilamentary ?

Why superconducting wires are all multifilamentary ?



$$\Delta M \propto J_c d$$

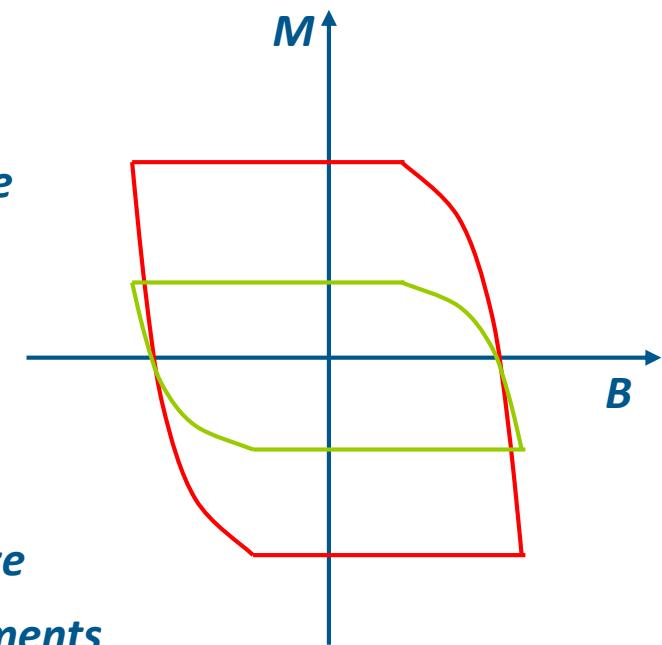
d is the filament size



$$\Delta M \propto n J_c d$$

d is the filament size

n is the number of filaments



With the subdivision of the superconducting layer in filaments, hysteretic losses are reduced but the critical current $I_c = J_c A_{SC}$ is unchanged

... but this is not the only reason ...

Flux jumps and Thermal instabilities

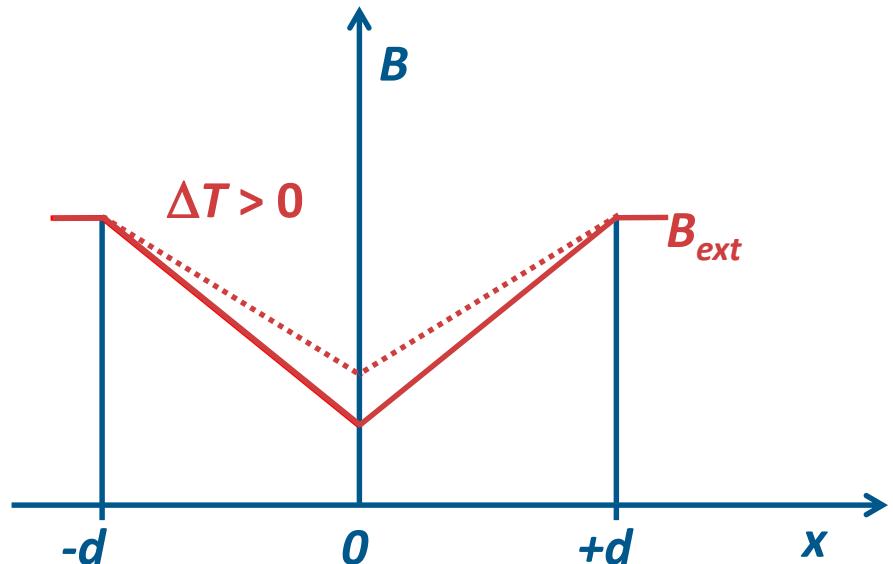
In the adiabatic approximation

$$\Delta T > 0 \quad \Rightarrow \quad \Delta J_c < 0$$

↑

$$\Delta Q > 0 \quad \Leftarrow \quad \Delta E > 0$$

↓



If ΔQ_{ext} is the initial perturbation, the heat balance for the slab is

$$c\Delta T = \Delta Q_{ext} + \frac{\mu_0 J_c^2 d^2}{3(T_c - T_{op})} \Delta T$$

Because of the energy stored in the current, the effective specific heat is

$$c_{eff} = \frac{\Delta Q_{ext}}{\Delta T} = c - \frac{\mu_0 J_c^2 d^2}{3(T_c - T_{op})}$$

c_{eff} can become zero \Rightarrow ultimate thermal catastrophe !!

Flux jumps and Thermal instabilities

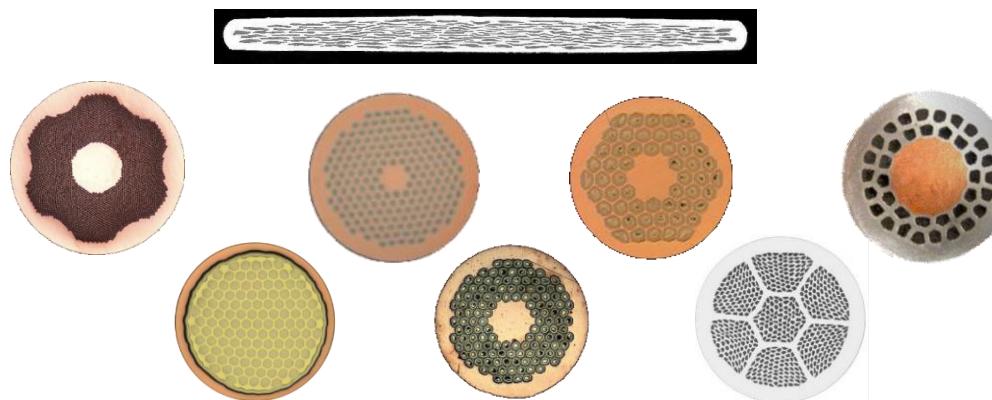
The stability condition is

$$c_{eff} = c - \frac{\mu_0 J_c^2 d^2}{3(T_c - T_{op})} > 0$$

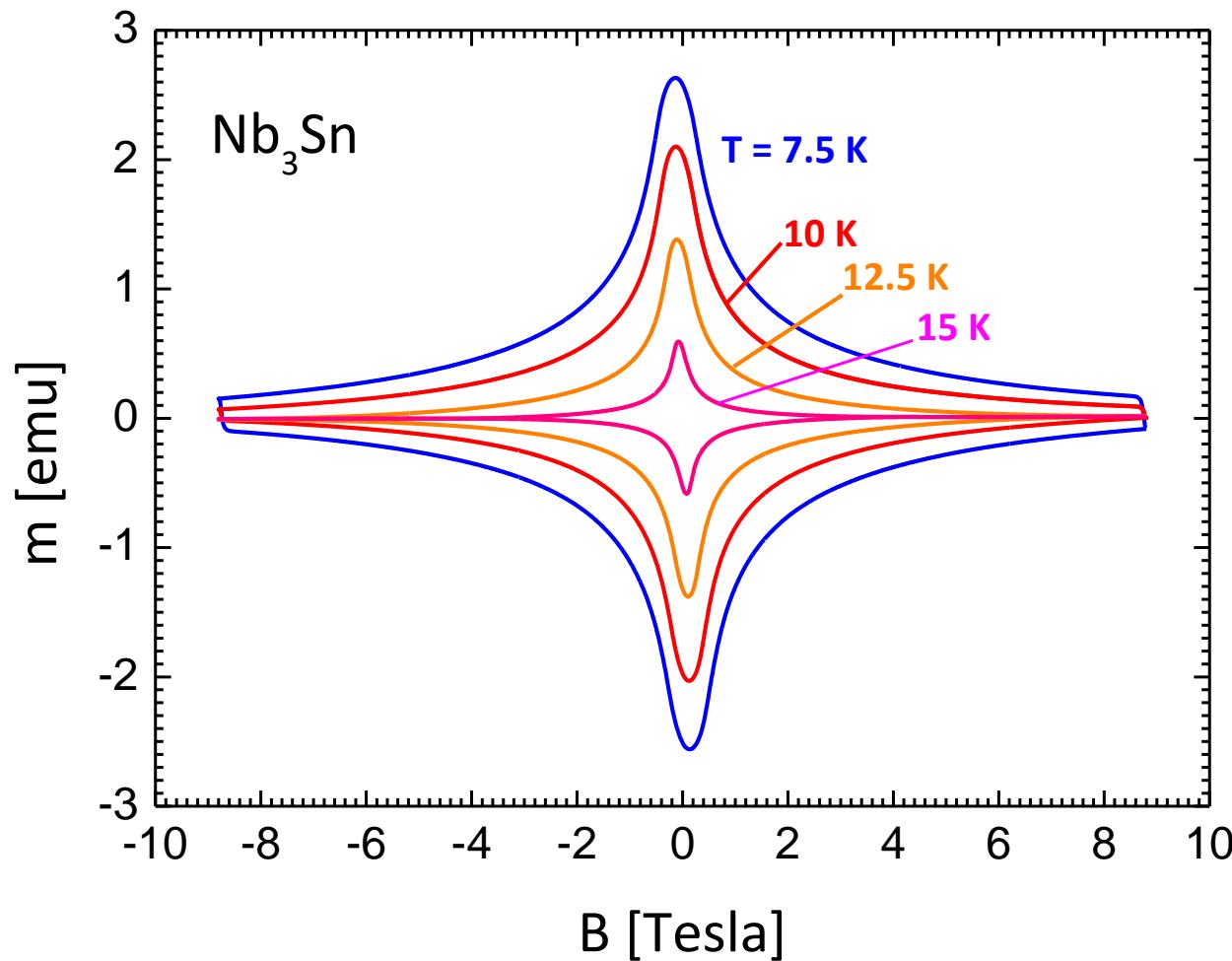
A superconducting wire must be designed in such a way that

$$\frac{\mu_0 J_c^2 d^2}{c(T_c - T_{op})} < 3$$

And this demands the subdivision of the superconductor in fine filaments

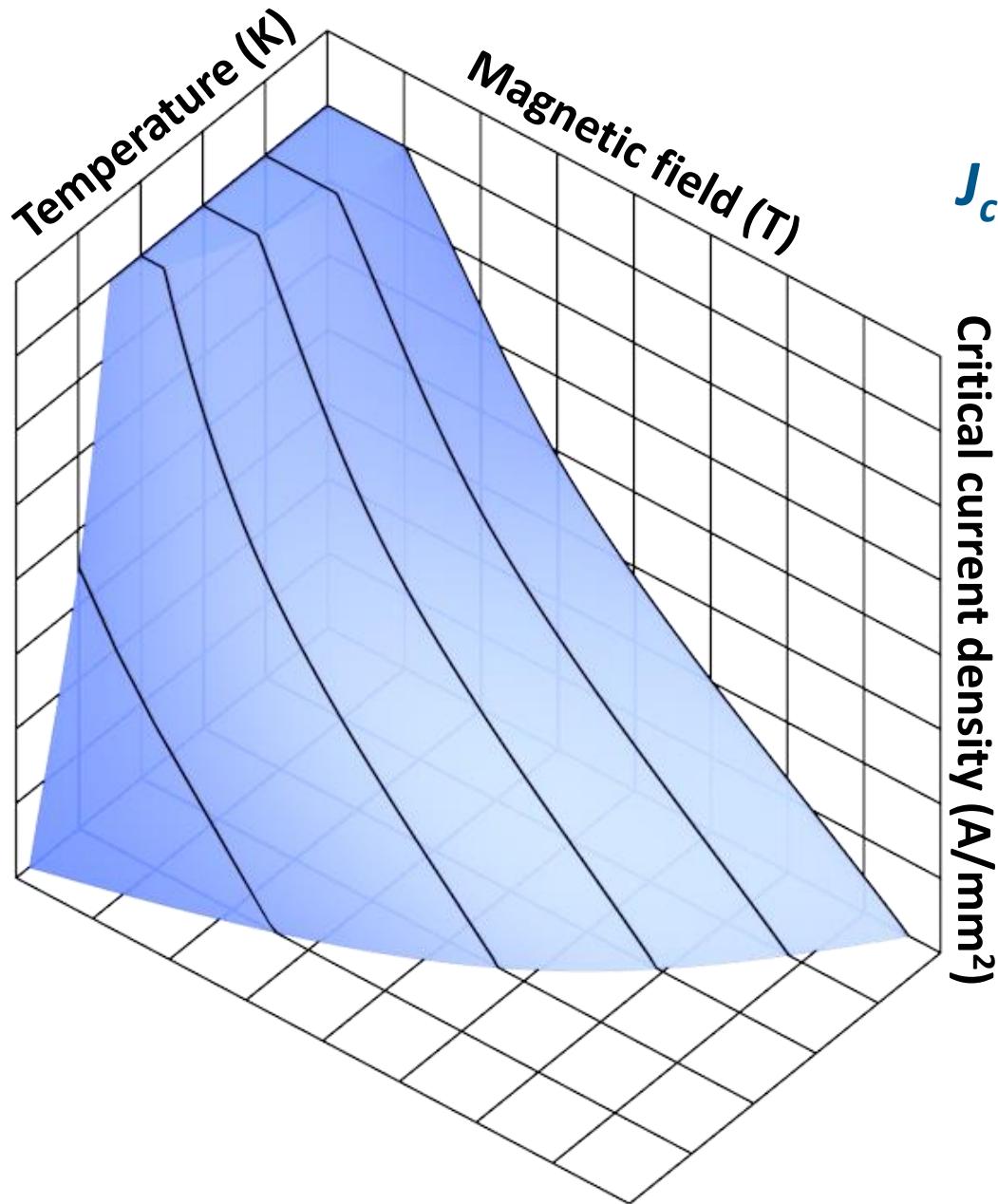


Field and temperature dependence of J_c



$$\Delta\mathbf{M} = \Delta\mathbf{M}(B, T) \Rightarrow J_c = J_c(B, T)$$

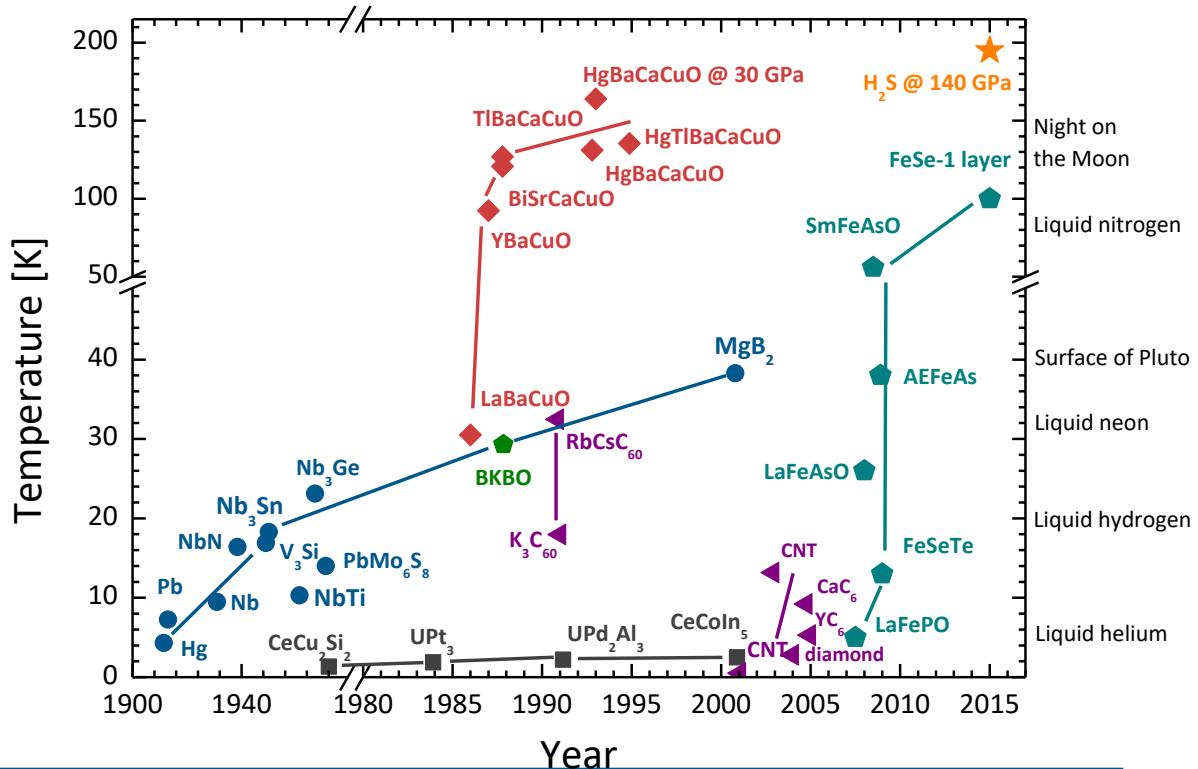
The critical surface $J_c(B,T,\dots)$



J_c depends also on:

- *the applied stress*
- *the magnetic field orientation (only for anisotropic superconductors)*

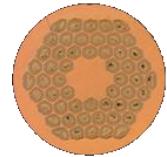
From superconducting materials... ...to technical superconductors



NbTi



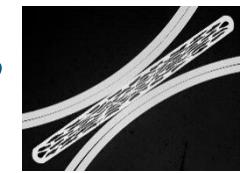
Nb₃Sn



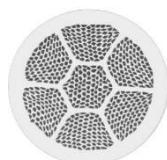
MgB₂



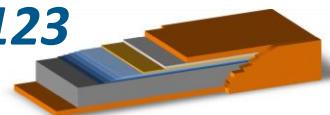
Bi2223



Bi2212



Y123



- | | |
|---|---------------|
| 1. <i>Superconducting ?</i> | 10'000 |
| 2. <i>T_c>4.2K & B_{c2}>10T ?</i> | 100 |
| 3. <i>J_c>1000 A/mm² ?</i> | ~10 |

In the following...



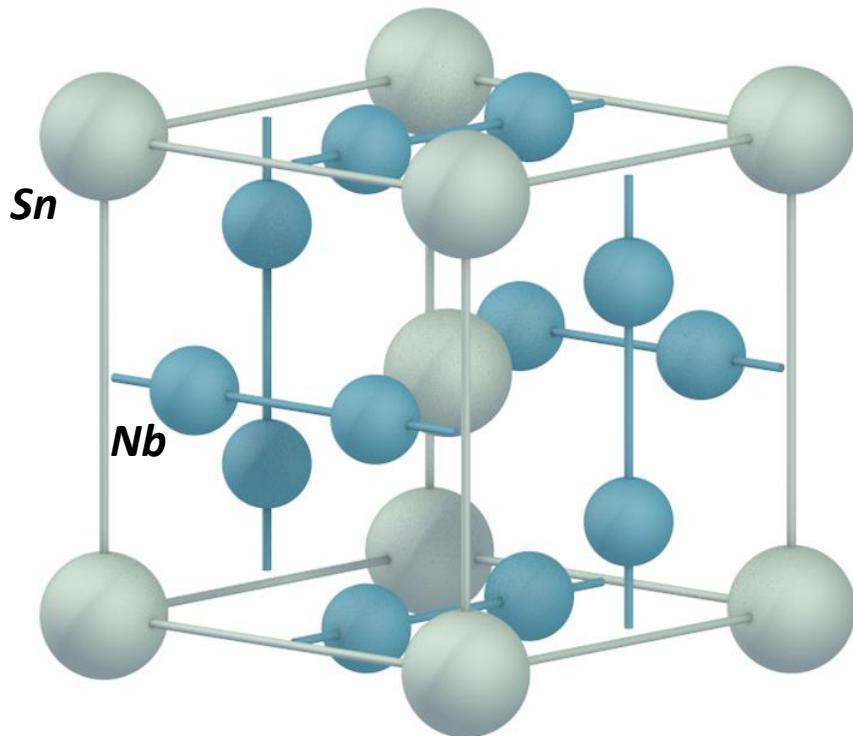
Nb₃Sn → the HiLumi HL-LHC PROJECT superconductor and only candidate material for the 16 T dipoles of



YBCO → the way to get 20 T dipoles and beyond



Introduction to Nb_3Sn



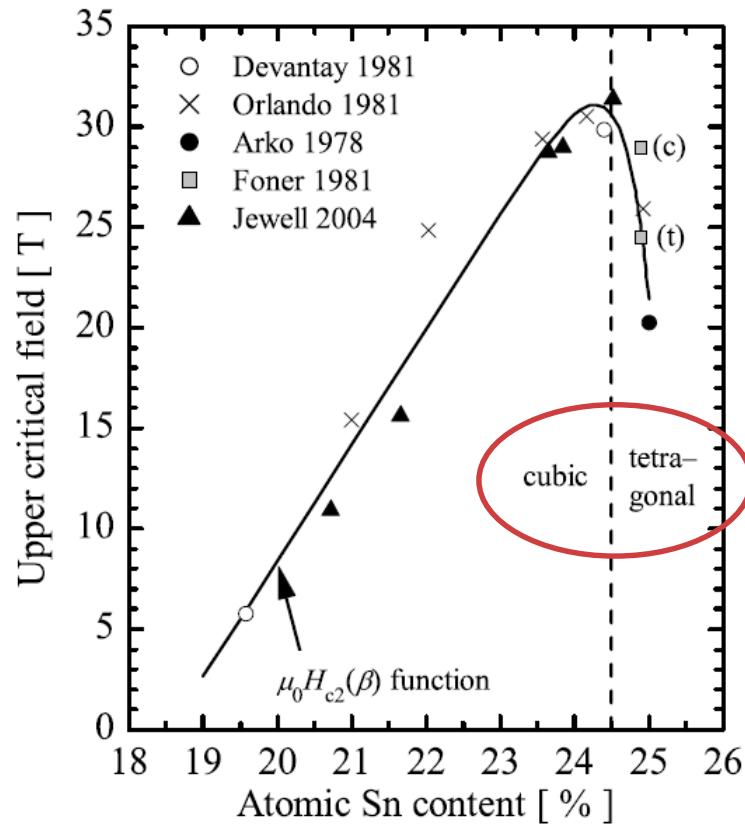
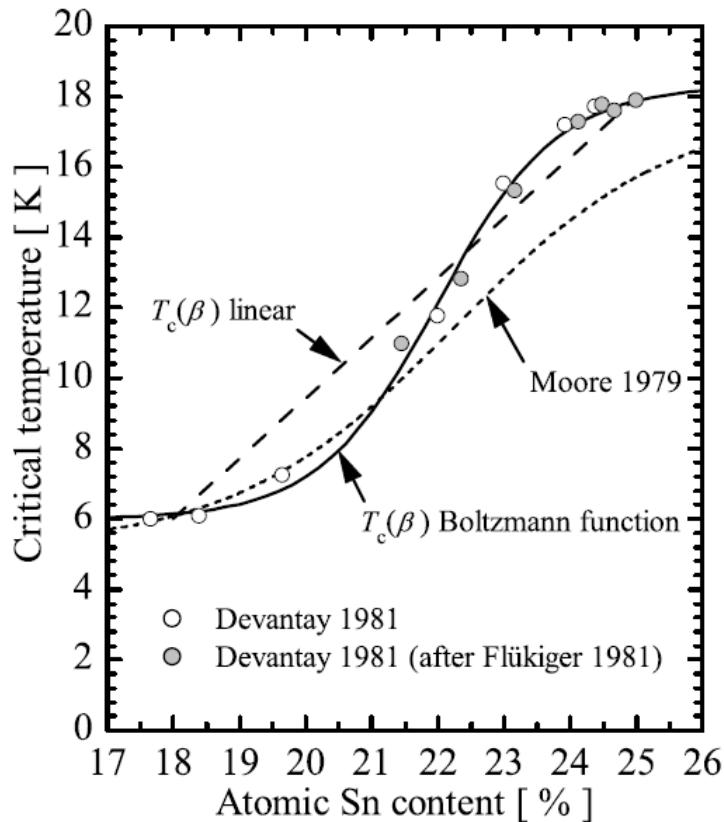
Nb_3Sn is the prototype of A15 superconductors

B.T. Matthias et al., PR 95 (1954) 1435

B \ A ₃	Ti	Zr	V	Nb	Ta	Cr	Mo
	4	4	5	5	5	6	6
Al 3				11.8	18.8		0.6
Ga 3				16.8	20.3		0.8
In 3				13.9	9.2		
Tl 3					9		
Si 4				17.1	19		1.7
Ge 4				11.2	23.2	8.0	1.2
Sn 4	5.8	0.9	7.0	18.0	8.4		
Pb 4		0.8		8.0	17		
As 5				0.2			
Sb 5	5.8			0.8	2.2	0.7	
Bi 5			3.4		4.5		
Tc 7							15.0
Re 7							15.0
Ru 8						3.4	10.6
Os 8				5.7	1.1	4.7	12.7
Rh 9				1.0	2.6	10.0	0.3
Ir 9	5.4			1.7	3.2	6.6	0.8
Pd 10				0.08			
Pt 10	0.5			3.7	10.9	0.4	
Au 11		0.9	3.2	11.5	16.0		8.8

A15 are intermetallic compounds with A_3B formula

Nb₃Sn : the Superconductor for high fields (today)



	T_c [K]	B_{c2} [T]
Nb_3Sn	18.0	30+

Nb_{3+x}Sn_{1-x} is superconducting also when deviates from stoichiometry

How to rise H_{c2} – Let's play it dirty

For a clean, ordered superconductor

$$H_{c2} = \frac{\Phi_0}{2\pi\xi^2}$$

Disorder reduces the electron mean free path ℓ , which in turn leads to decrease of ξ

$$\frac{1}{\xi(\ell)} = \frac{1}{\xi(\infty)} + \frac{1}{\ell}$$

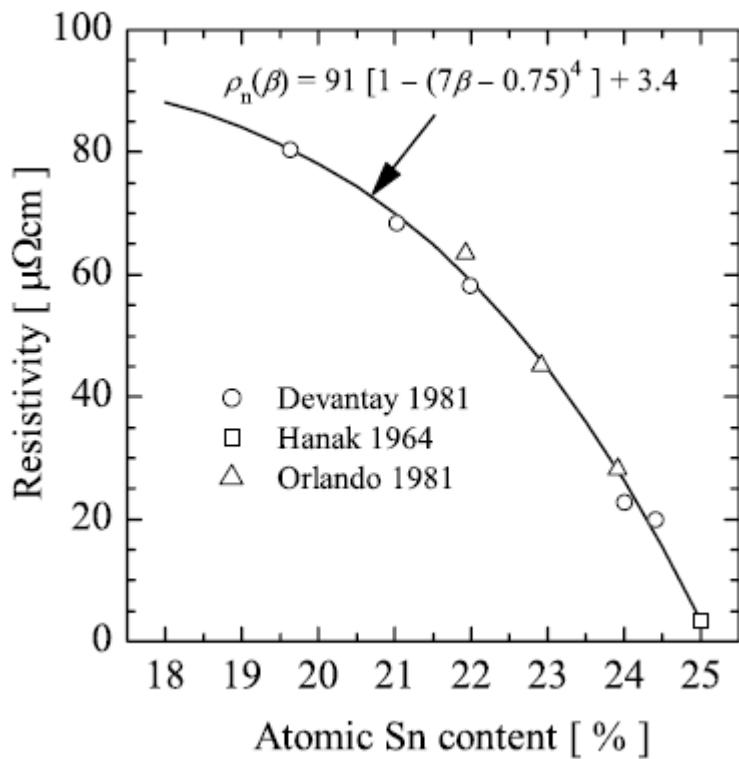
An useful expression of H_{c2} in the dirty limit

$$H_{c2}(T=0) \approx \frac{k_B e}{\mu_0} N(E_F) \rho_n T_c \propto \gamma \rho_n T_c$$

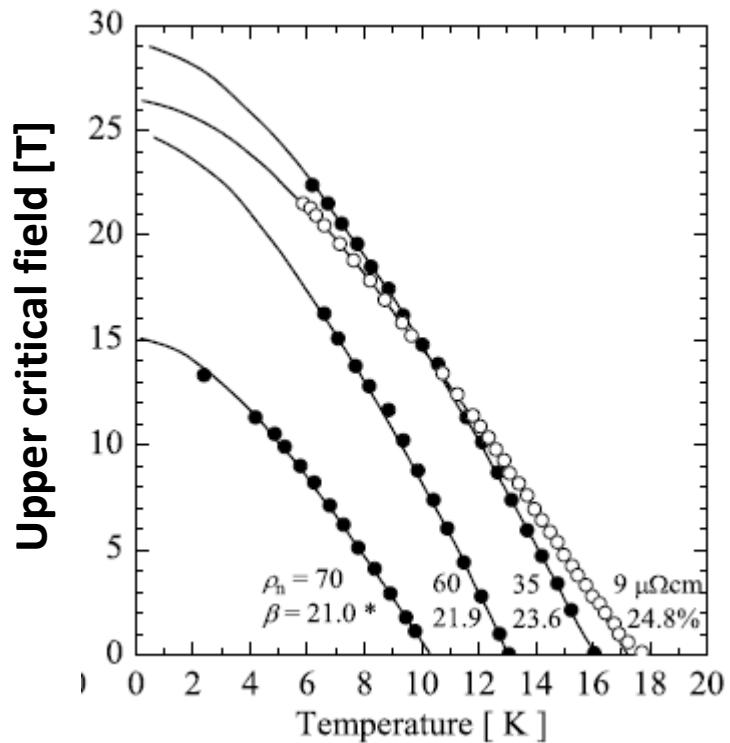
How to rise H_{c2} in Nb_3Sn

$$H_{c2} \propto \gamma \rho_n T_c$$

Resistivity vs. Sn at.%



H_{c2} vs. T at various Sn at.%

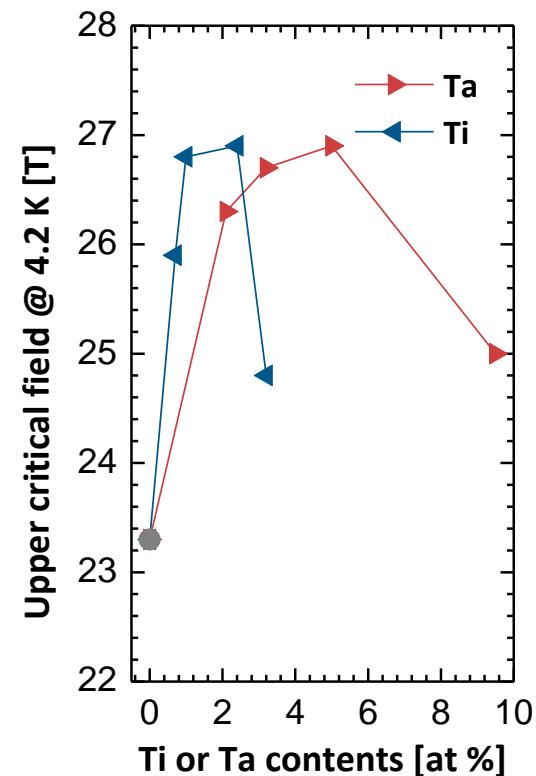
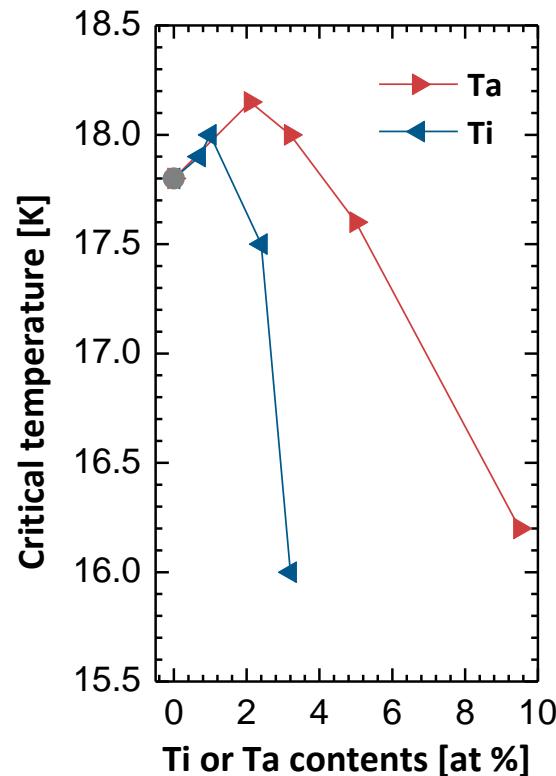
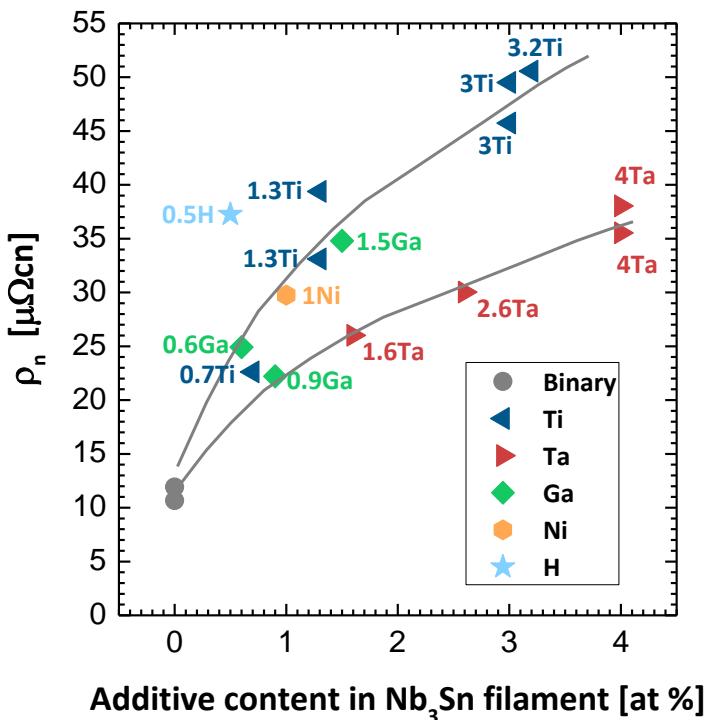


Reducing Sn content rises ρ_n , but reduces T_c . Other ideas ?

Alloying (doping) Nb_3Sn to rise H_{c2}

$$H_{c2} \propto \gamma \rho_n T_c$$

The additions of Ta and Ti are particularly beneficial



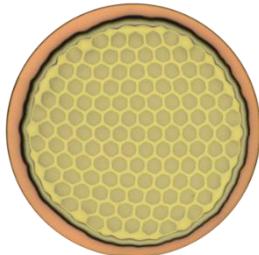
$(Nb,Ta)_3Sn$ and $Nb_3(Sn,Ti)$

$$\frac{H_{c2}(4.2\text{ K})}{H_{c2}(0\text{ K})} = 0.89$$

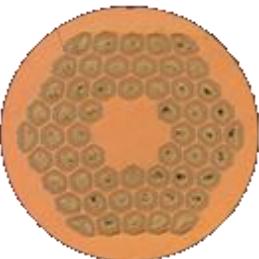
M. Suenaga et al., JAP 59 (1986) 840
R. Flükiger et al., Cryogenics 48 (2008) 293

Industrial fabrication of Nb_3Sn wires

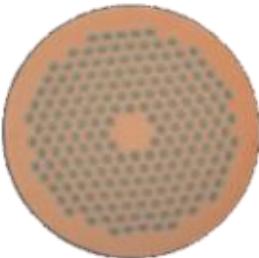
Three technologies have been developed at industrial scale



- *Bronze route*



- *Internal Sn diffusion*



- *Powder in tube*

*The Sn source is
the main difference*

Presently produced by



LUVATA

Western Superconducting
Technologies Co.,Ltd.



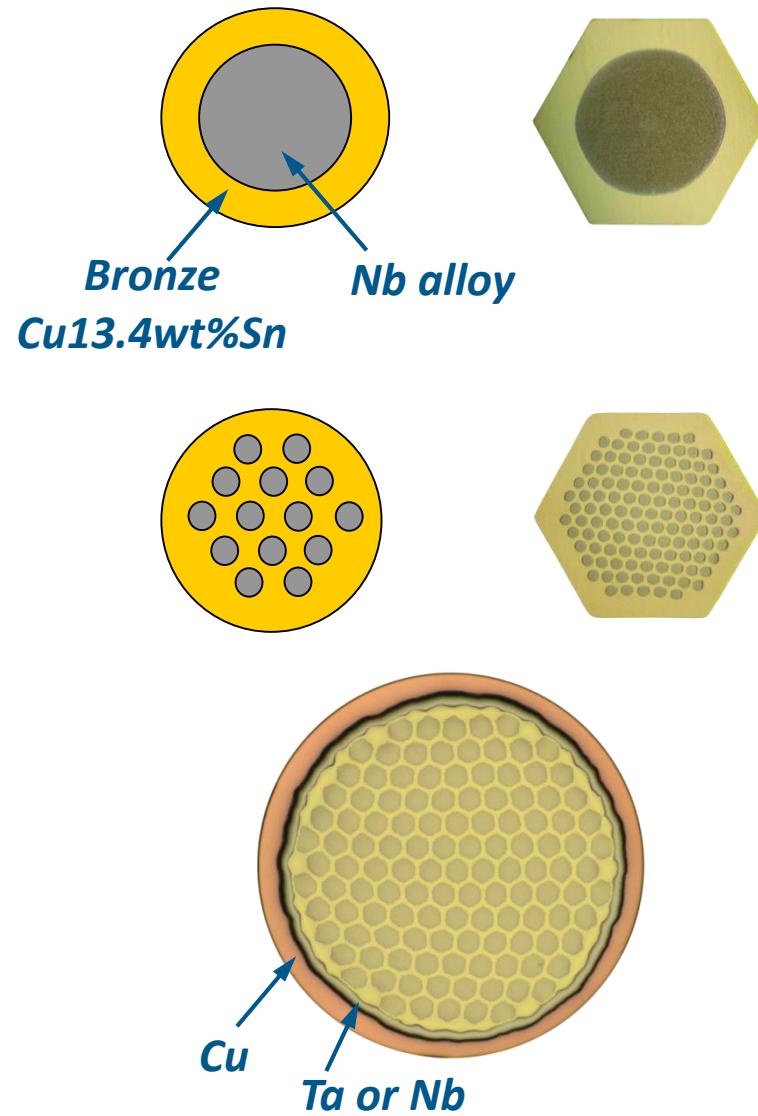
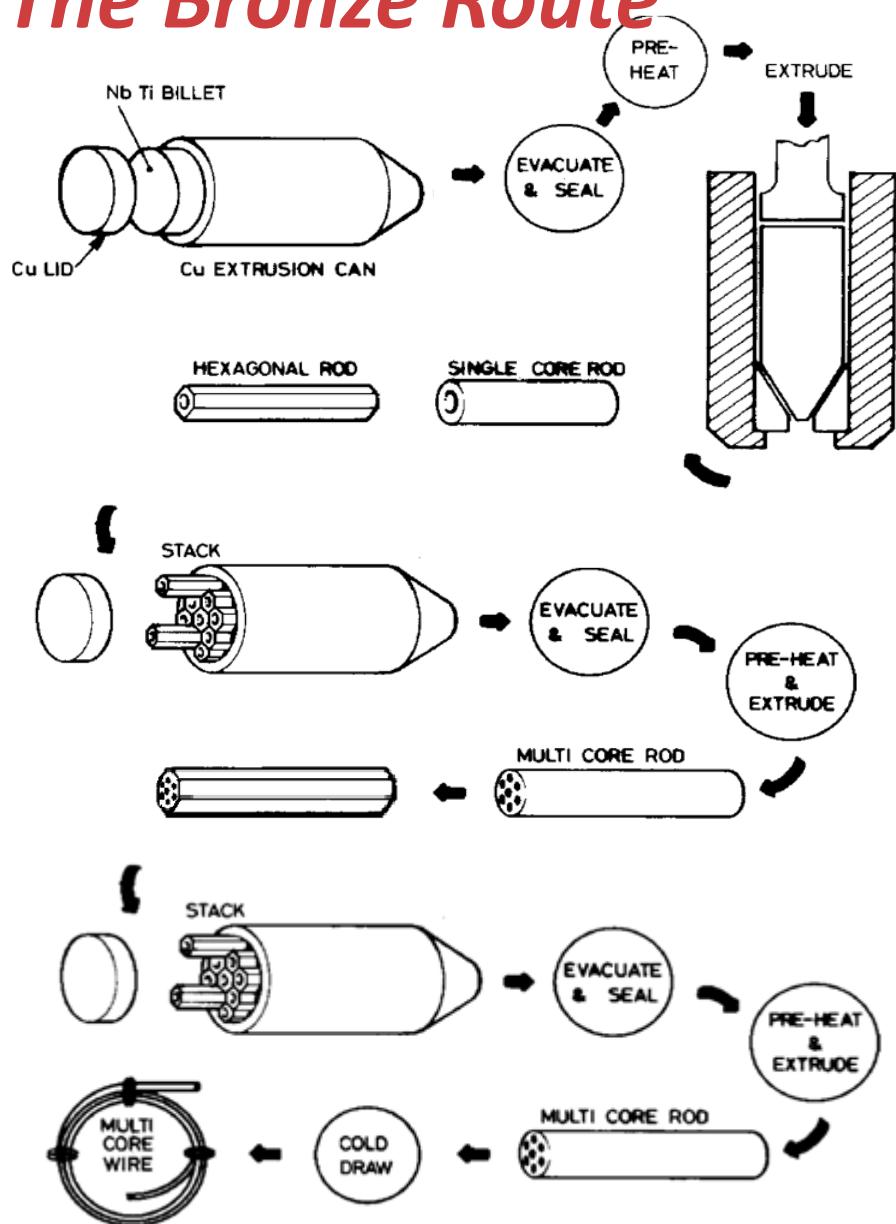
BOCHVAR INSTITUTE OF
INORGANIC MATERIALS
JSC VNIINM



KOBELCO
KOBE STEEL, LTD.



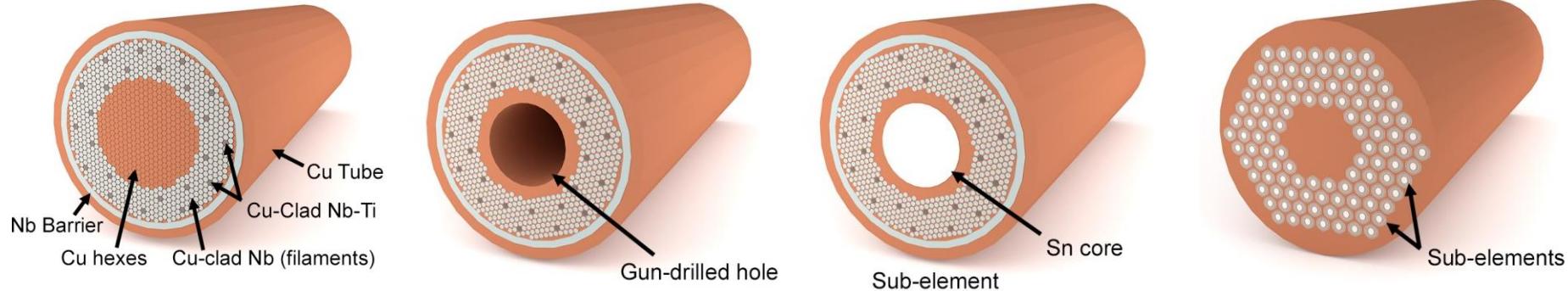
The Bronze Route



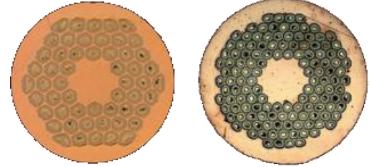
**Cu-Sn bronze is used as Sn source
The final filament size is ~5 μm**

Wires are then reacted at ~650°C for >100 hours to form Nb₃Sn

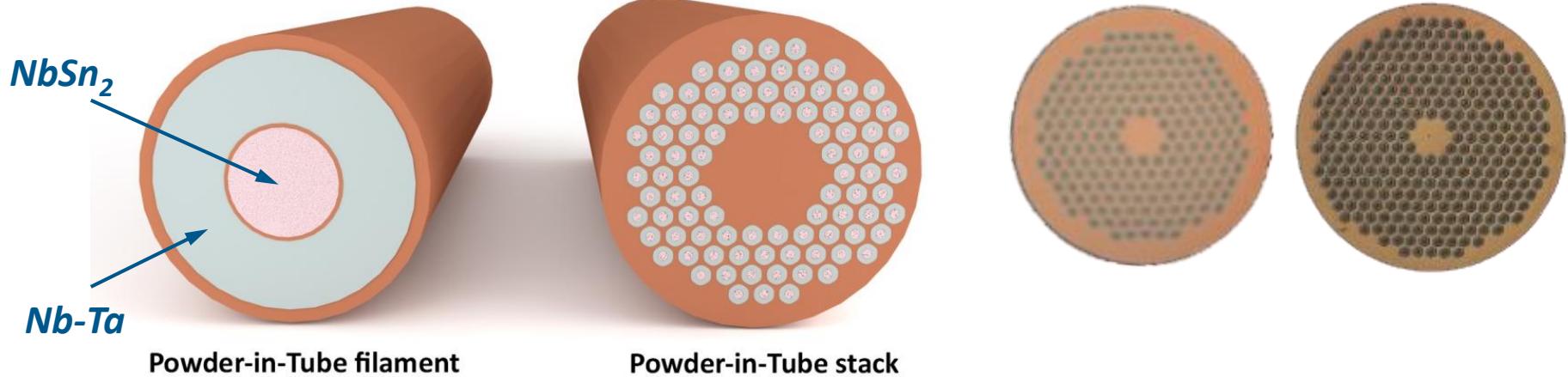
The Internal Sn diffusion process



- *A Sn rod is inserted in the subelement core*
- *After the insertion of Sn, only cold deformations are possible*
- *Subelement size ranges between 20 and 100 μm*
- *A long-duration multistep reaction schedule is required to form Nb_3Sn*

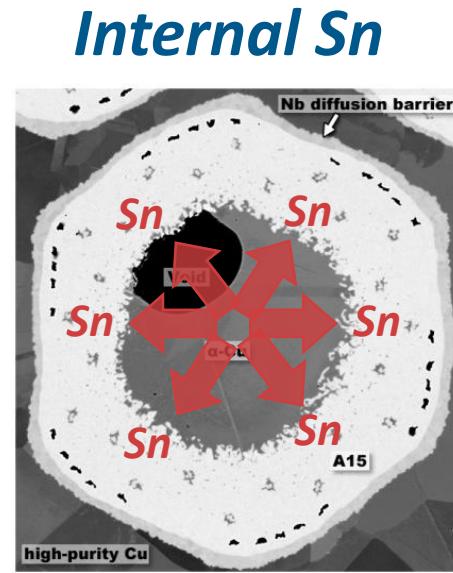
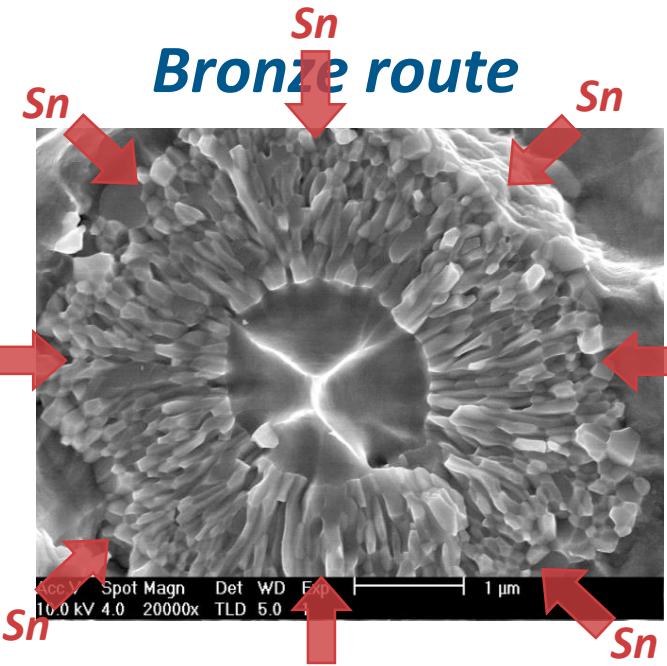


The Powder-In-Tube method

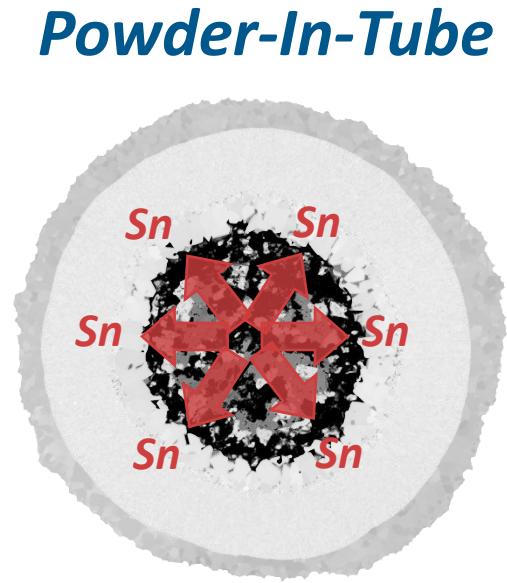


- *$NbSn_2$ and Sn powders are used as Sn source*
- *Subelement size ranges between 20 and 100 μm*
- *A long-duration multistep reaction schedule is required to form Nb_3Sn*

Microstructure of the A15 phase after reaction



Subelement size ~50 μm



Filament size ~50 μm

High Sn content & appropriate Ta/Ti doping to get high B_{c2} and thus high in-field J_c

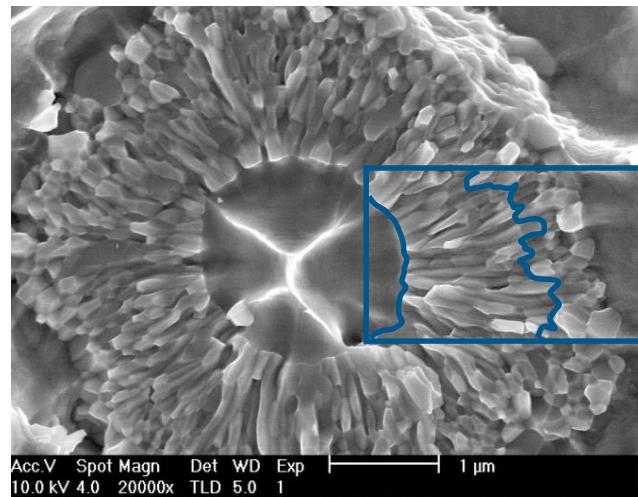
Also microstructure is directly related to the J_c performance

Grain boundaries act as the main vortex pinning centers

Small grain size implies high grain boundary density and thus high J_c

Microstructure of the A15 phase after reaction

Bronze route



Filament size ~5 μm

Outer region

Equiaxed grains ~ 150 nm

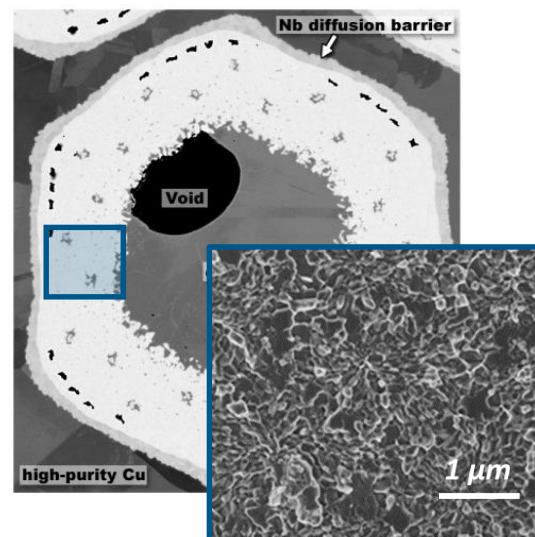
21-25 at.% Sn

Inner region

Columnar grains ~ 400 nm

18-21 at.% Sn

Internal Sn



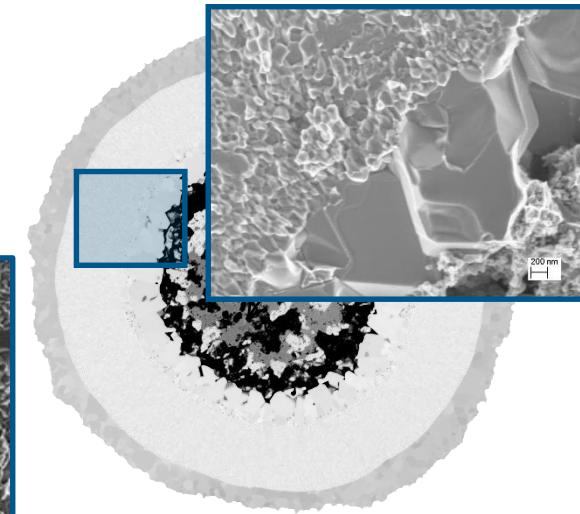
Subelement size ~50 μm

Almost everywhere

Fine grains ~ 150 nm

24-25 at.% Sn

Powder-In-Tube



Filament size ~50 μm

Outer region

Fine grains ~ 150 nm

23-24 at.% Sn

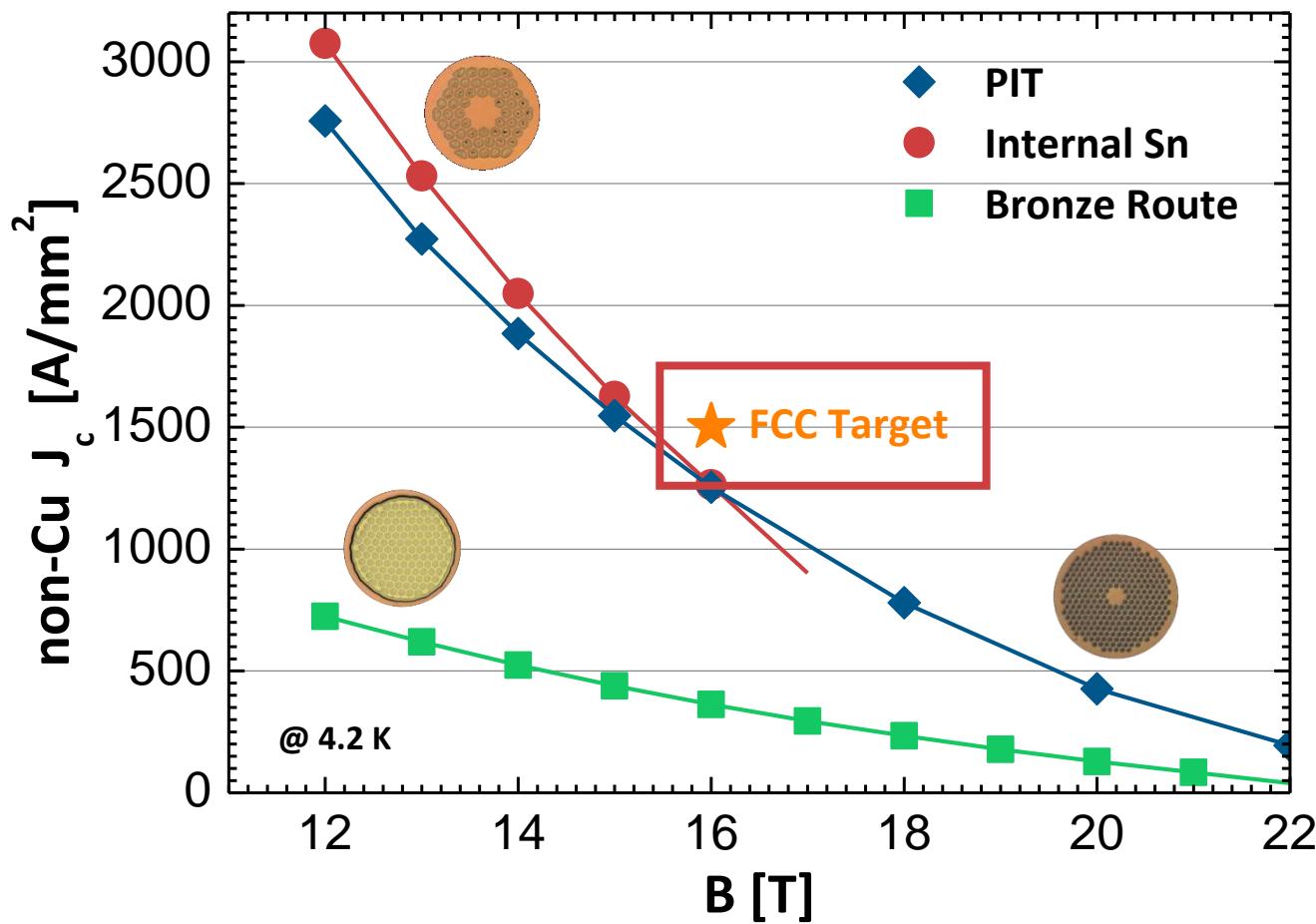
Inner region

Large grains ~ 1 μm

25 at.% Sn

Critical current density vs. magnetic field

Best performance achieved so far in industrial wires



How do we get the ultimate Nb_3Sn ?

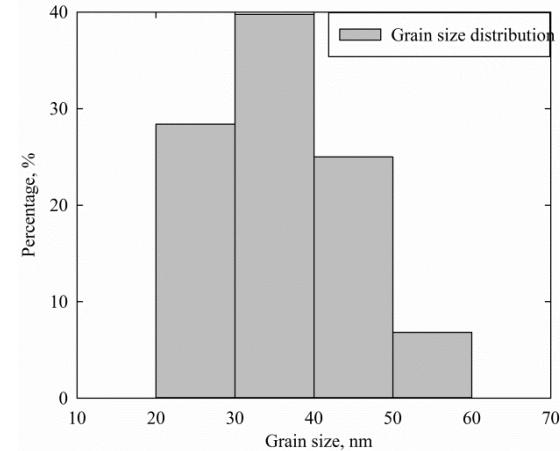
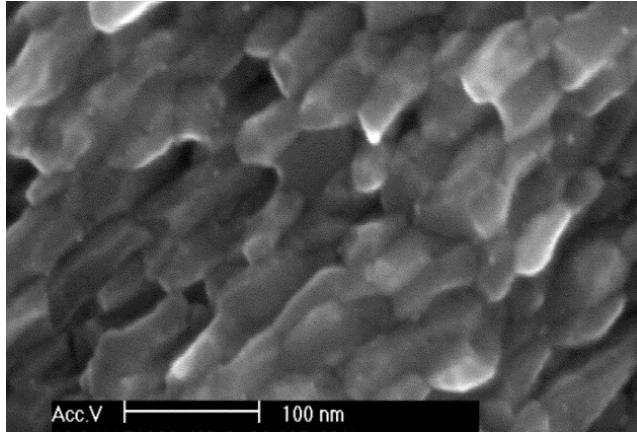
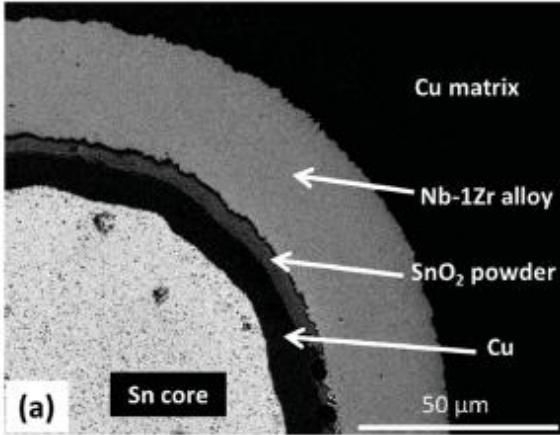
Internal oxidation and grain refinement in Nb_3Sn

@ Ohio State University

Idea to form fine precipitates in Nb to impede the A15 grain growth

Use of a Nb-Zr alloy: Zr has stronger affinity to oxygen than Nb

Oxygen supply added to the composite: oxidation of Zr and formation of nano- ZrO_2



X. Xu et al., APL 104 (2014) 082602

X. Xu et al., Adv. Mat. 27 (2015) 1346

Average grain size is reduced down to 36 nm

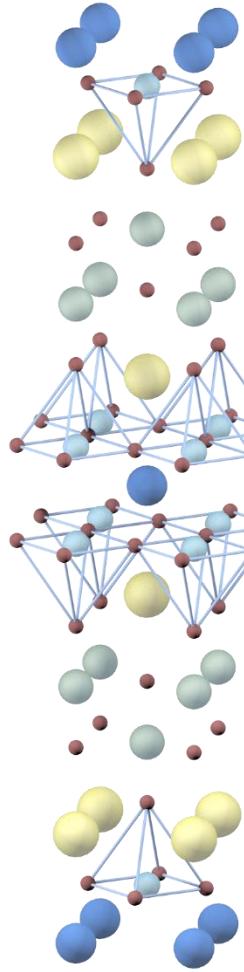
Greatly enhanced pinning in binary Nb_3Sn

Result need to be transferred to Ti- and Ta- alloyed Nb_3Sn

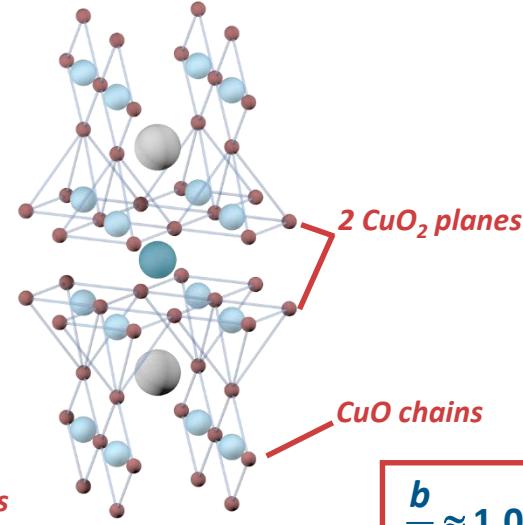
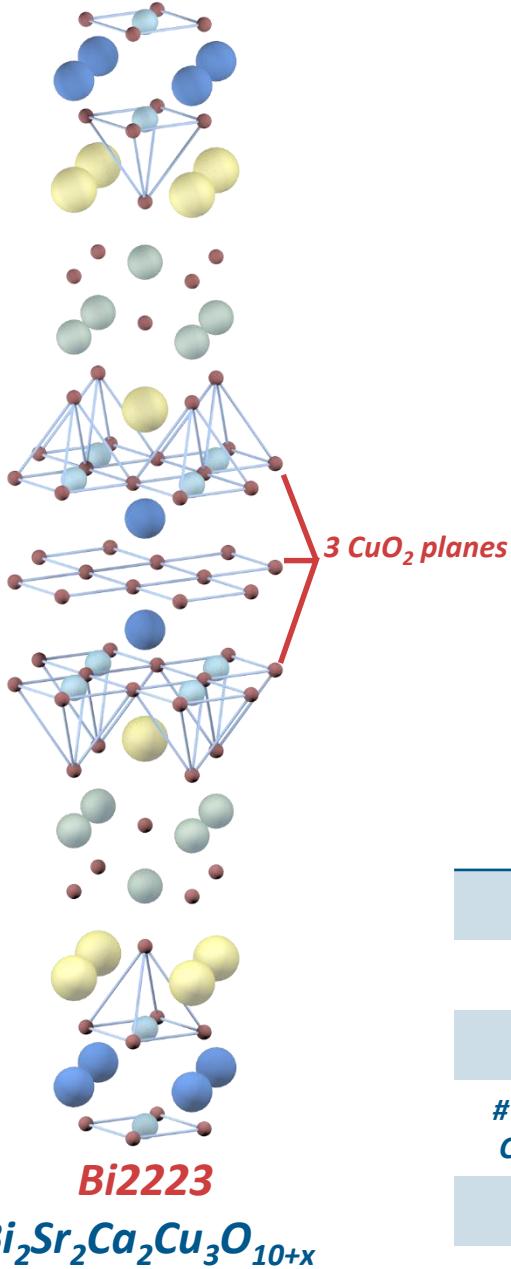
*High Temperature Superconductors are
different animals ...*



HTS materials for applications



- O
- Ca
- Cu
- Sr
- Bi



Y123

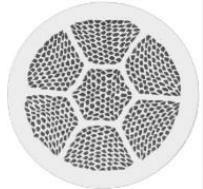
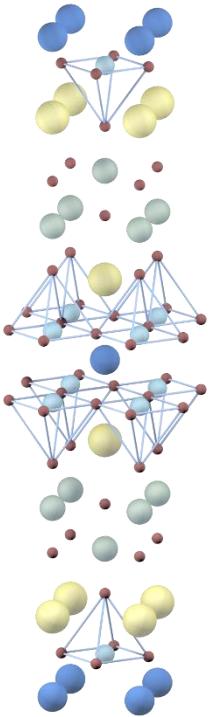
$\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$

$$\frac{b}{a} \approx 1.001 \text{ in BSCCO}$$

$$\frac{b}{a} \approx 1.02 \text{ in YBCO}$$

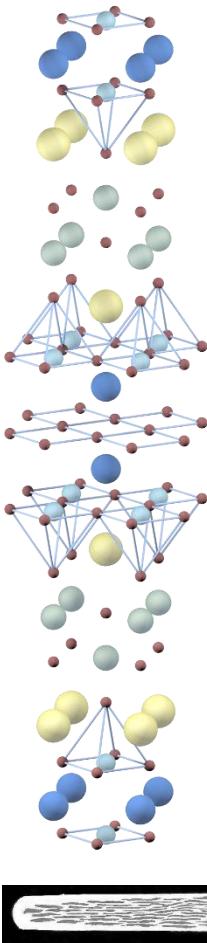
	Bi2212	Bi2223	Y123
a [Å]	5.415	5.413	3.8227
b [Å]	5.421	5.421	3.8872
c [Å]	30.880	37.010	11.680
# of adjacent CuO_2 planes	2	3	2
T_c [K]	91	110	92

The evolution to the present wires and tapes

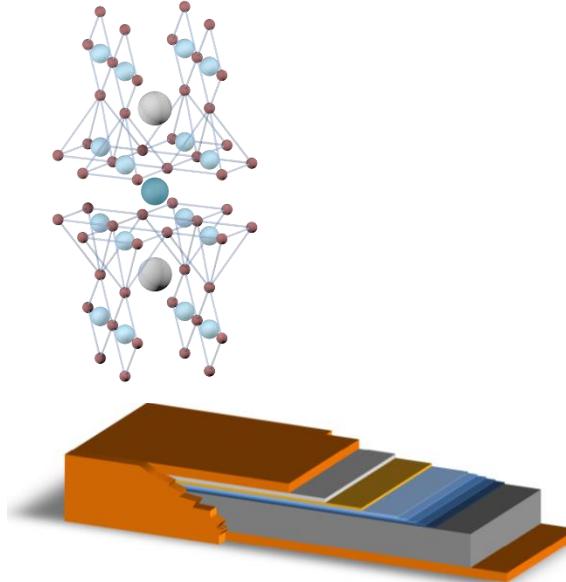


Bi2212

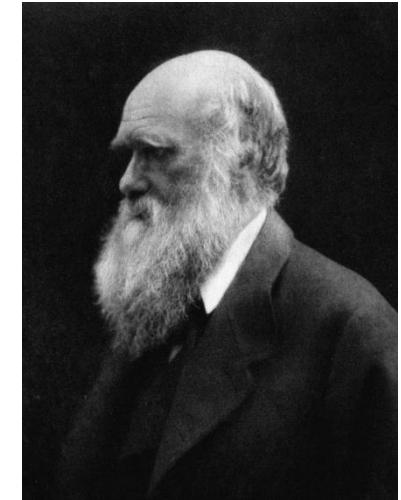
Powder-In-Tube wire



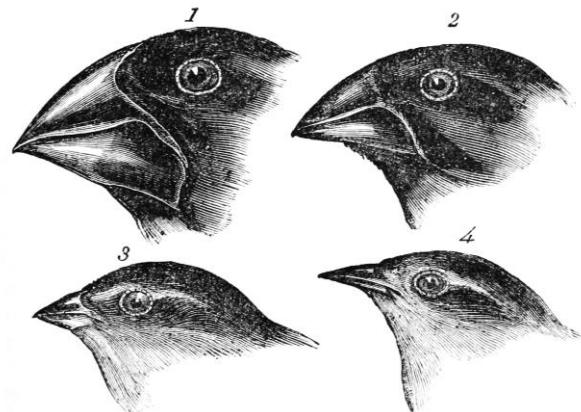
Bi2223 Powder-In-Tube tape



Y123 Coated Conductor



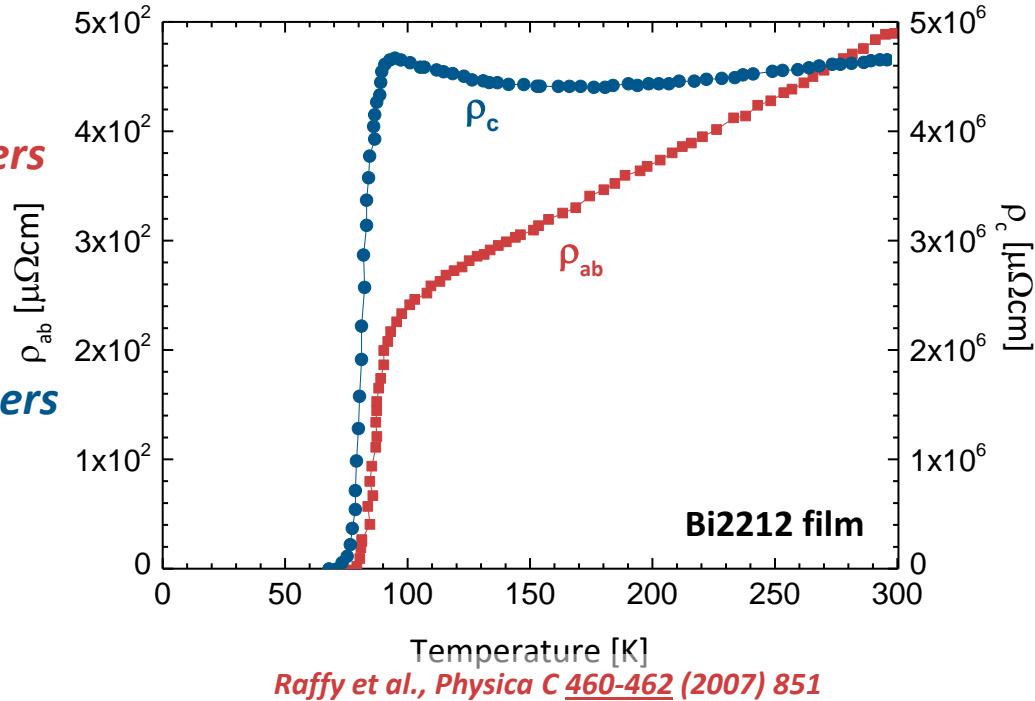
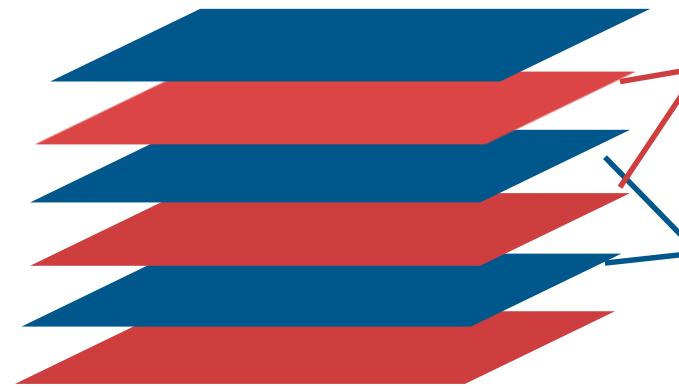
Darwin's finches



1. *Geospiza magnirostris*.
3. *Geospiza parvula*.

2. *Geospiza fortis*.
4. *Certhidea olivacea*.

Layered structure and Anisotropy

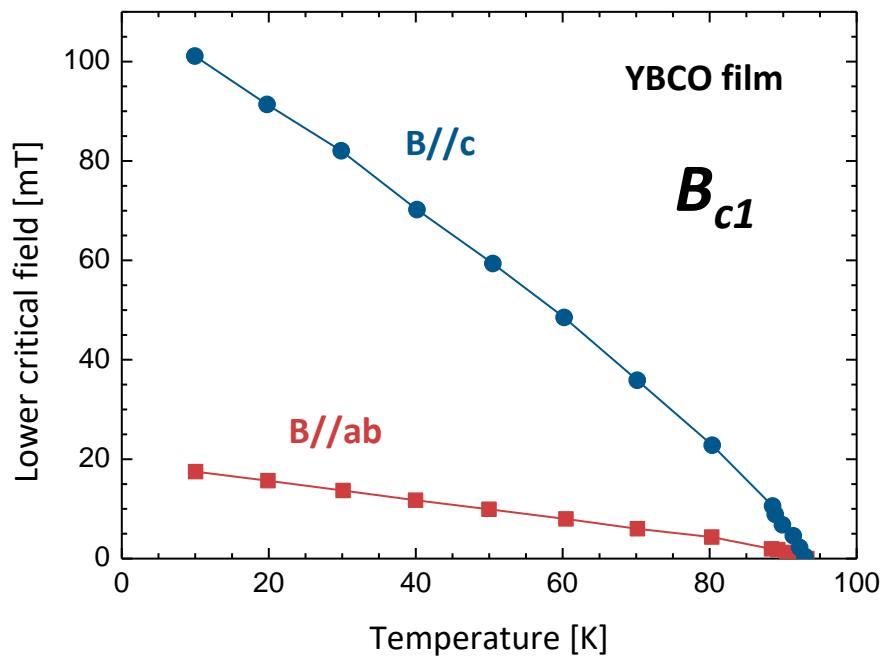


Charge carriers have effective masses that depend on the crystallographic orientation

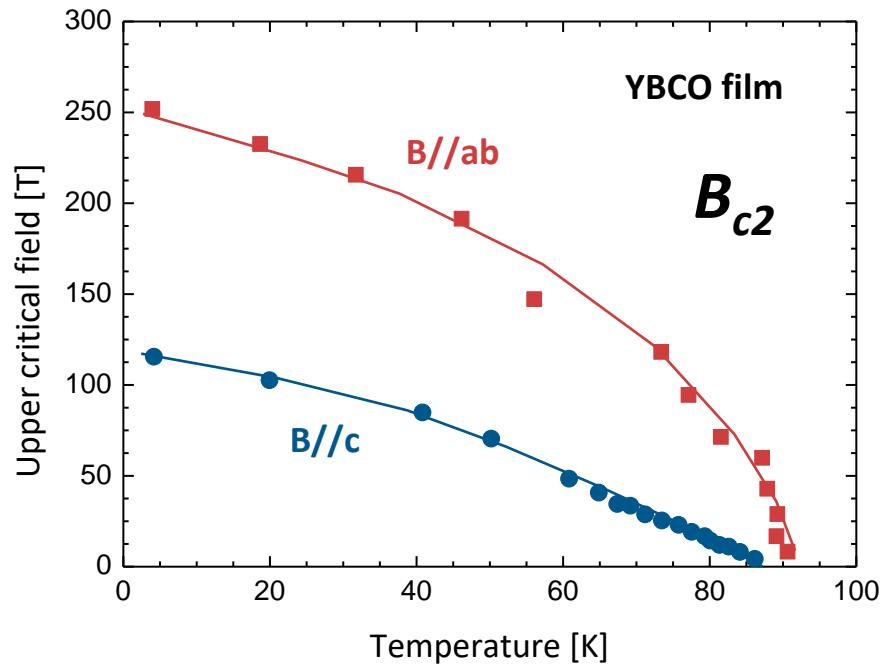
$\frac{m_c}{m_{ab}}$ ranges between 50 and 10'000 in cuprates

The superconductor lengths depend on the carrier mass: $\xi \propto \frac{1}{\sqrt{m}}$ and $\lambda \propto \sqrt{m}$

Anisotropy of the critical fields B_{c1} and B_{c2}



Liang et al., PRB 50 (1994) 4212



Nagakawa et al., JPCM 10 (1998) 11571

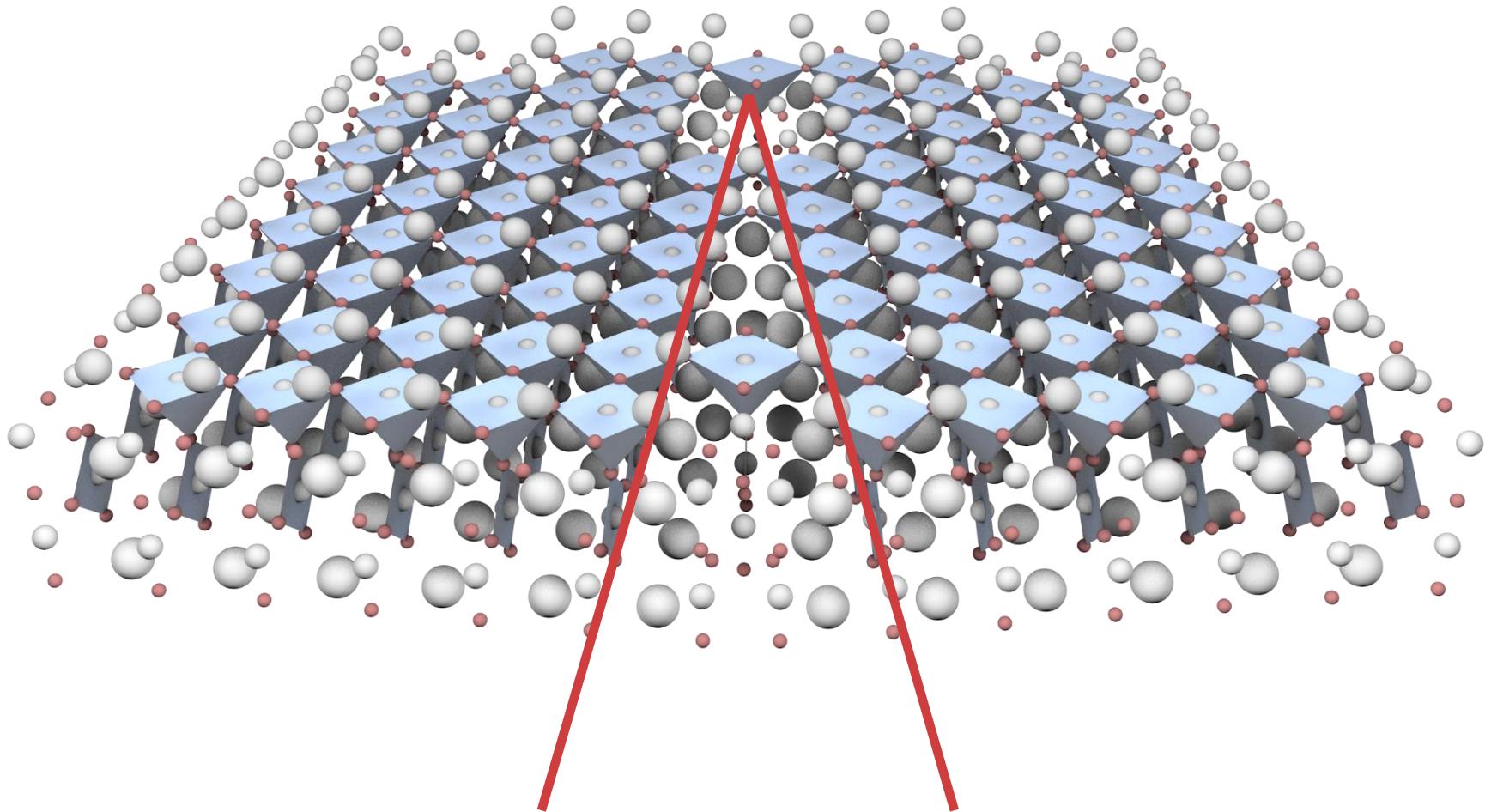
Sekitani et al., NJP 9 (2007) 47

The superconductor anisotropy parameter

$$\gamma = \sqrt{\frac{m_c}{m_{ab}}} = \frac{\lambda_c}{\lambda_{ab}} = \frac{\xi_{ab}}{\xi_c}$$

	Bi2212	Bi2223	Y123
γ	~ 150	~ 30	~ 7

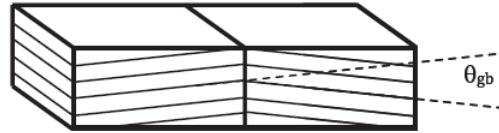
Grain Boundaries in HTS



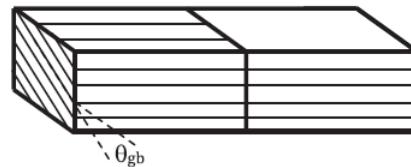
Grain boundaries in Y123 (YBCO)



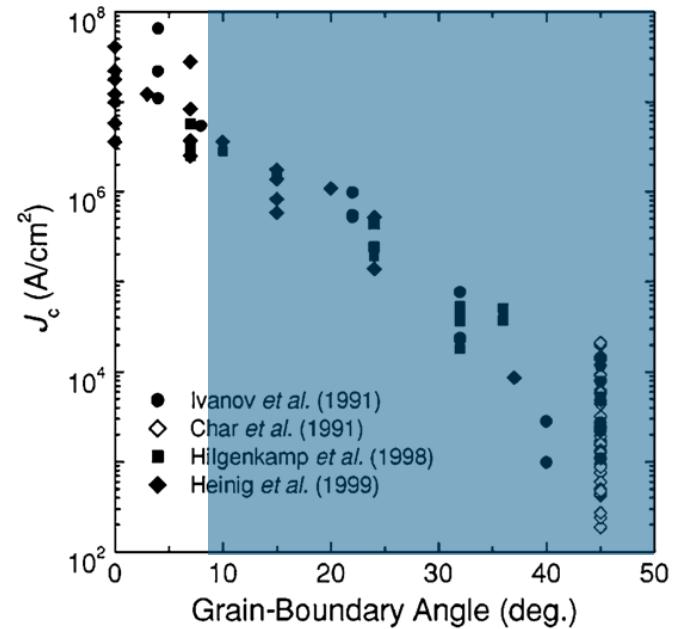
[001] tilt boundary



[100] tilt boundary



[100] twist boundary



Hilgenkamp and Mannhart, RMP 74 (2002) 485

For angles above 8-10°, the J_c^{GB} is reduced by a factor >100 !!

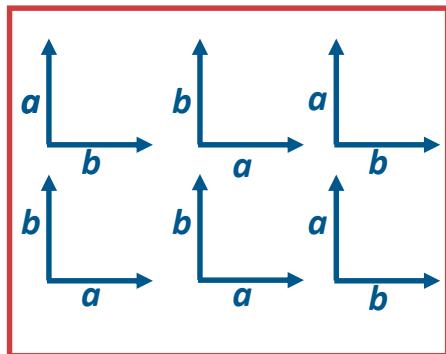
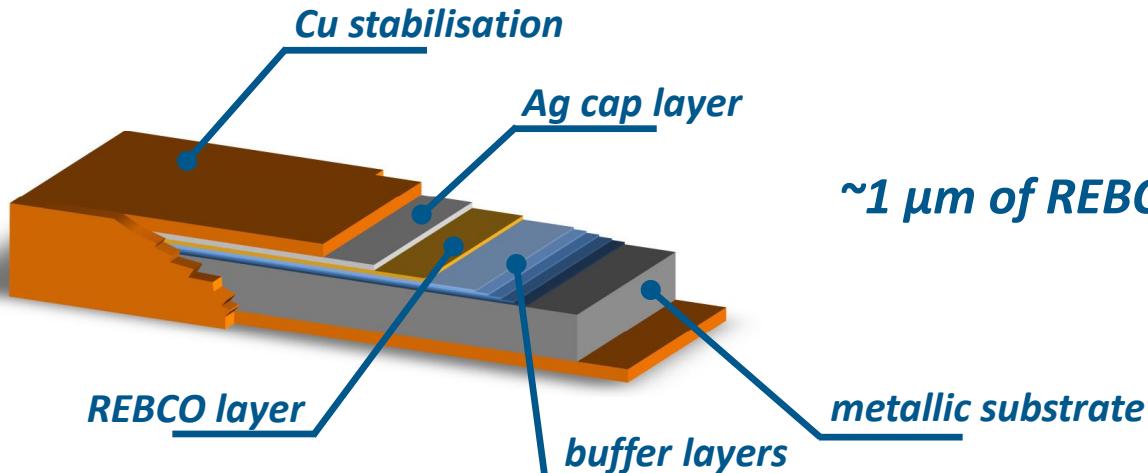
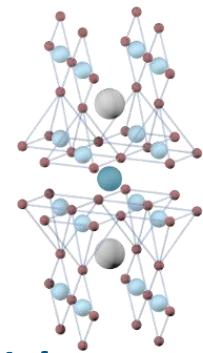
In order to get high J_c in the conductor, biaxial texturing is needed

Alignment of the grains is needed in all crystallographic orientations

RE = Rare Earth

YBCO (REBCO) coated conductors

Iijima et al., APL 60 (1992) 769
Goyal et al., APL 69 (1996) 1795



Looking from above

Presently produced by



The technology of REBCO coated conductors

Alternative approaches for growing epitaxial REBCO on flexible metallic substrates in km-lengths

Substrate texturing

RABiTS : Rolling-Assisted, Biaxially Textured Substrates
Texture is created in NiW by a rolling-and-recrystallization process

IBAD : Ion Beam Assisted Deposition
A biaxially textured MgO layer is grown on polycrystalline Hastelloy

Physical routes

PLD Pulsed Laser Deposition

RCE Reactive Co-Evaporation

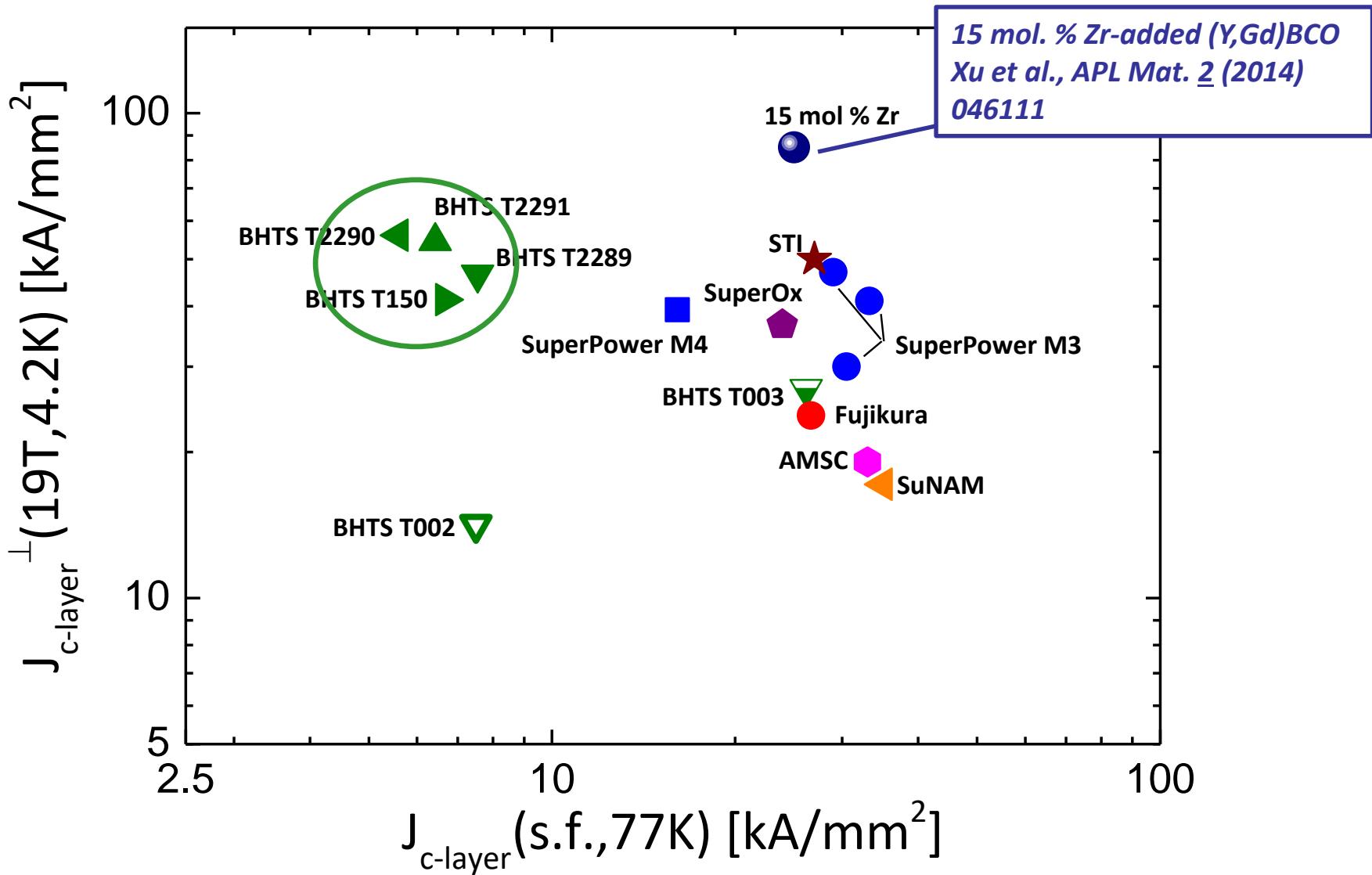
REBCO layer deposition

Chemical routes

MOD Metal-Organic Deposition

MOCVD Metal-Organic Chemical Vapor Dep.

Performance overview: J_c (s.f., 77K) vs. J_c^\perp (19T, 4.2K)

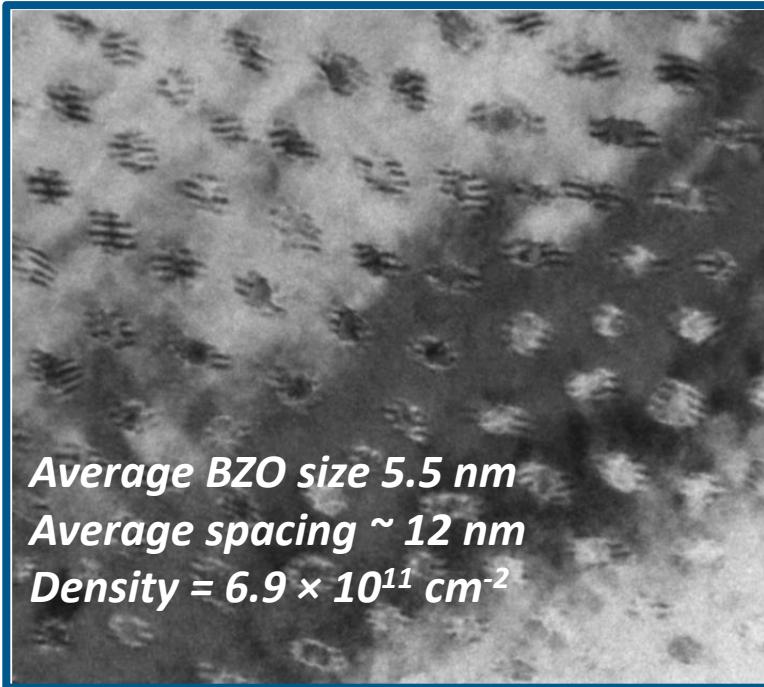


Artificial pinning: “genetically-modified” REBCO

Introduction of artificial nano-defects to control vortex pinning, reduce anisotropy and enhance performance

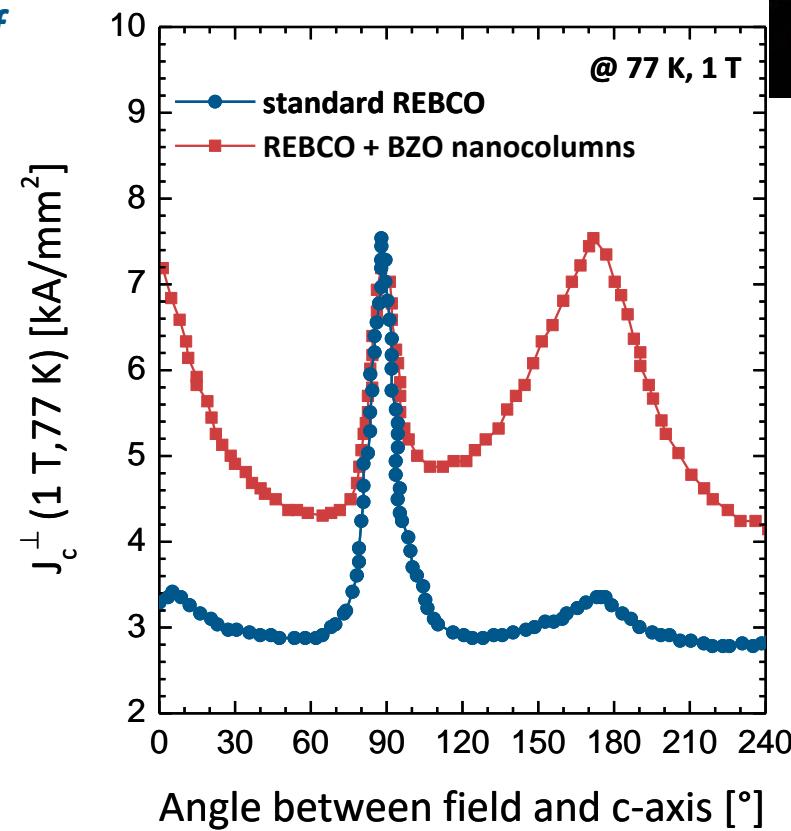


BaZrO₃ (BZO) precipitates are in form of nano-columns oriented along the c-axis



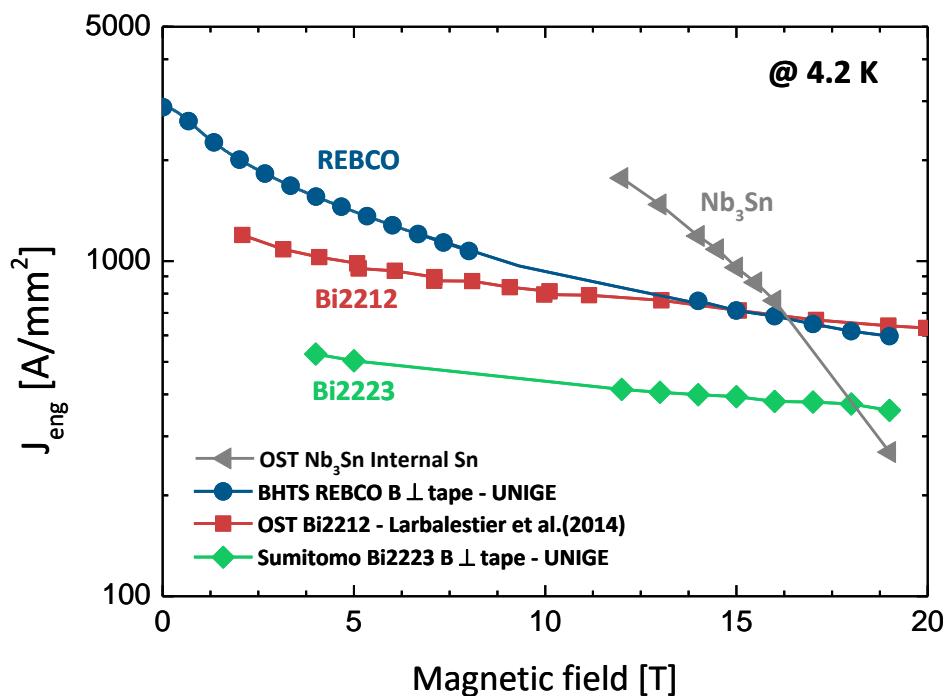
Average BZO size 5.5 nm
Average spacing ~ 12 nm
Density = $6.9 \times 10^{11} \text{ cm}^{-2}$

Selvamanickam et al., *APL* **106** (2015) 032601

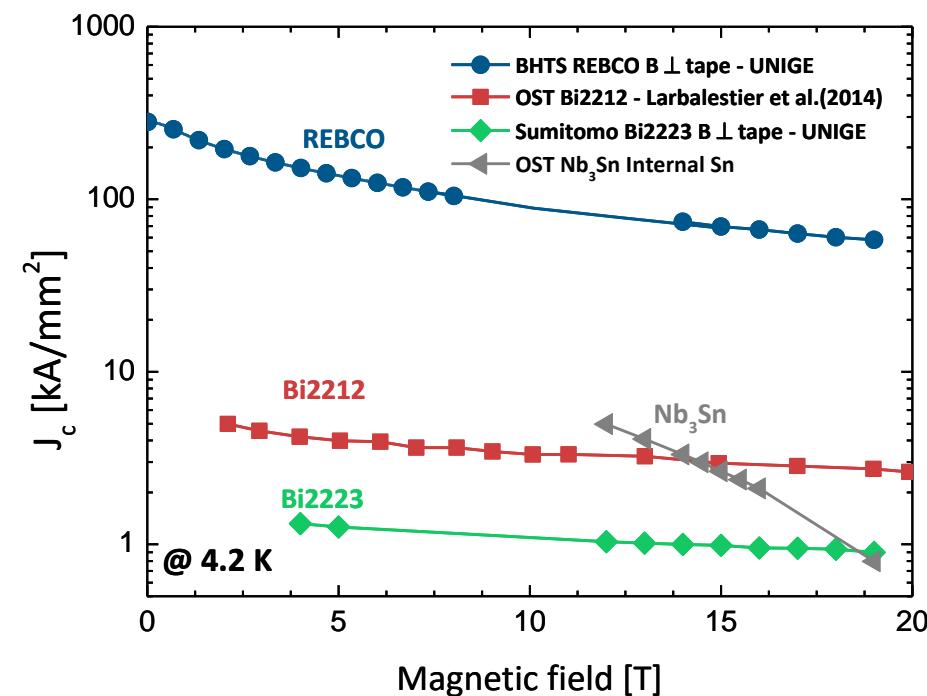


Selvamanickam et al., *IEEE TASC* **21** (2011) 3049

Engineering vs. superconducting layer performance



Engineering current density



Critical current density

REBCO and Bi2223 tapes retain the anisotropic properties of the superconductor

Data shown here correspond to the unfavorable orientation wrt the field

The in-field properties of Bi2212 wires are fully isotropic

*Operate at high current density is a necessary condition,
but it is not sufficient*

Other crucial requirements:

- *Have high tolerance to stress* Magnetic forces
- *Be safe in case of magnet quench* Quench detection, NZPV
- *Have low magnetization* Applications to NMR, MRI, HEP magnets
- *Have a persistent joint technology* Applications to NMR, MRI

Conductor contest: Nb_3Sn vs REBCO

	Nb_3Sn	REBCO
<i>Geometry</i>	round wire	tape
<i>SC fraction</i>	~35%	~1%
<i>In-field Anisotropy</i>	1, Isotropic	~5
<i>Multifilamentary</i>	Yes, twisted	No, single layer
<i>Operation boundaries</i>	2.2 K, 23.5 T * 4.2 K, 19 T *	4.2 K, UHF 77 K, ~3 T
<i>Mechanical properties</i>	Some issues with transversal loads	Almost OK, but delamination issues
<i>Disadvantages</i>	Still margin to improve the performance? Cost!!	Long lengths under development Cost!!

* in solenoidal coils

Practical conductors for accelerator magnets : Why cables ?

Superconducting wires have current capability of few hundred Amps

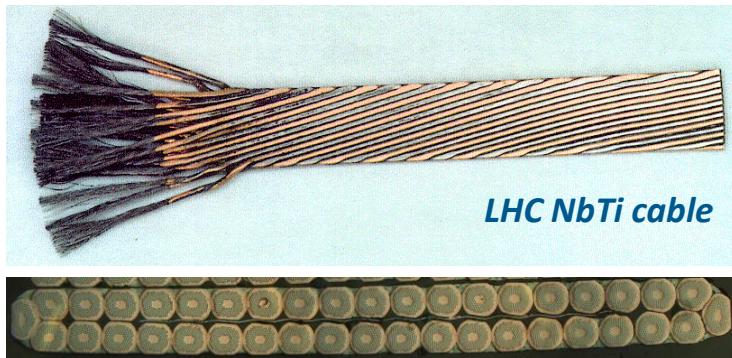
Dipoles and quadrupoles require large operating currents $\sim 10 \text{ kA}$

- *To keep the inductance low*
- *To lower the charging voltage*
- *To ease magnet protection*

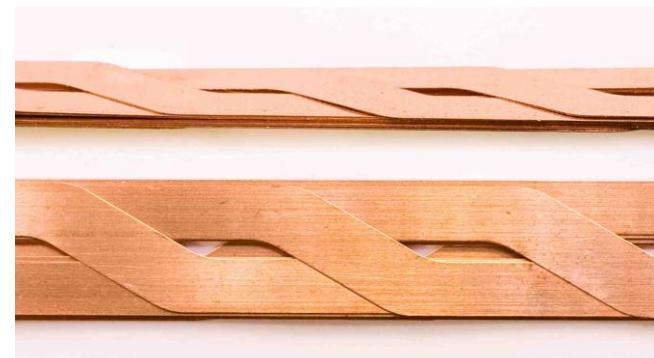
$$E = \frac{1}{2} L I^2 \quad V = L \frac{I}{t} = \frac{2E}{It}$$

$$V(I_{op} = 250\text{A}) = 40 \times V(I_{op} = 10\text{kA})$$

Round wires → Rutherford cables



REBCO tapes → Roebel cables



Both are fully transposed cables. Transposition length and number of wires or tapes can be adapted to the needs of the application

Summary

What we have learned

- *How to carry a current without dissipation*
Why just being a superconductor is not enough
- *How to enhance the critical current*
Avoid perfection → Defects to pin vortices
- *How to make a superconducting wire*
“classical” metallurgy and Nb_3Sn
thin film technology and REBCO coated conductors

Thank you for the attention !

...time for questions...

Carmine SENATORE

carmine.senatore@unige.ch

<http://supra.unige.ch>

If you want to know more about applied superconductivity in Geneva, visit <http://supra.unige.ch>

The screenshot shows a web browser window with the URL <http://dqmp.unige.ch/senatore/>. The page title is "Home - Group of Applied Su...". The main content area features a large image of a blue superconducting magnet. Below it, text reads: "The research of the Group of Applied Superconductivity is driven by the challenge to understand and control the basic properties required for the practical implementation of superconducting materials. This includes all the material aspects that play a role in tuning the superconductor properties as well as innovative approaches to the processing of superconducting wires and tapes." Another section states: "Our activities focus on the development of both low- and high-T_c superconductors for applications in various fields, from the high field magnets for NMR/MRI systems and particle accelerators to the emerging applications in the electric power infrastructure." At the bottom, it says: "The activities of the laboratory are supported by the following institutions:" followed by logos for FNSNF, Swiss Confederation, European Union, and Federal Department of Economic Affairs.

GROUP OF APPLIED SUPERCONDUCTIVITY
Prof. Carmine Senatore

UNIVERSITÉ DE GENÈVE
FACULTÉ DES SCIENCES
Section de physique

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Home

The research of the Group of Applied Superconductivity is driven by the challenge to understand and control the basic properties required for the practical implementation of superconducting materials. This includes all the material aspects that play a role in tuning the superconductor properties as well as innovative approaches to the processing of superconducting wires and tapes.

Our activities focus on the development of both low- and high-T_c superconductors for applications in various fields, from the high field magnets for NMR/MRI systems and particle accelerators to the emerging applications in the electric power infrastructure.

The activities of the laboratory are supported by the following institutions:

LATEST NEWS

EUCAS 2017

EUCAS 2017 in Geneva!
From 17th to 21st of September 2017 Geneva is hosting... [Read more →](#)

FCC week 2017

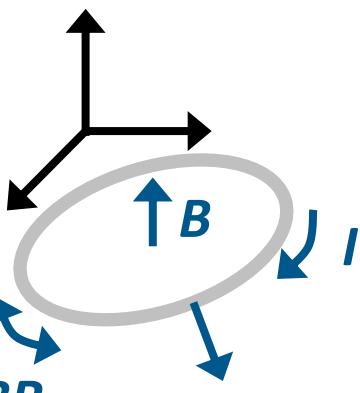
FCC week 2017 in Berlin
The 3rd Annual Meeting of the Future Circular Collider Study...
[Read more →](#)

*Operate at high current density is a necessary condition,
but it is not sufficient*

Other crucial requirements:

- *Have high tolerance to stress* Magnetic forces
- *Be safe in case of magnet quench* Quench detection, NZPV
- *Have low magnetization* Applications to NMR, MRI, HEP magnets
- *Have a persistent joint technology* Applications to NMR, MRI

Magnetic stresses in the winding

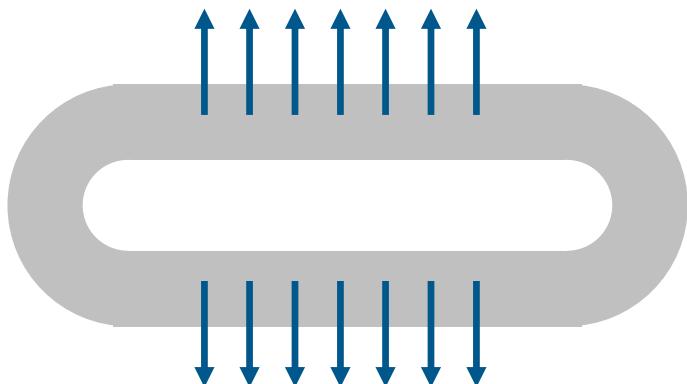

$$\sigma_{hoop} = \frac{I}{S_{wire}} BR$$

The diagram shows a single circular loop of wire. A current I flows clockwise through the loop. A magnetic field B is shown pointing vertically upwards from the center of the loop. A force vector $F = I \times B$ is shown at the bottom right, perpendicular to both I and B .

Hoop stress levels **above 100 MPa** are common

As an example, the NHMFL 32 T magnet will operate at **400 MPa**

In a real winding adjacent turns press on each other and develop 3-D stresses

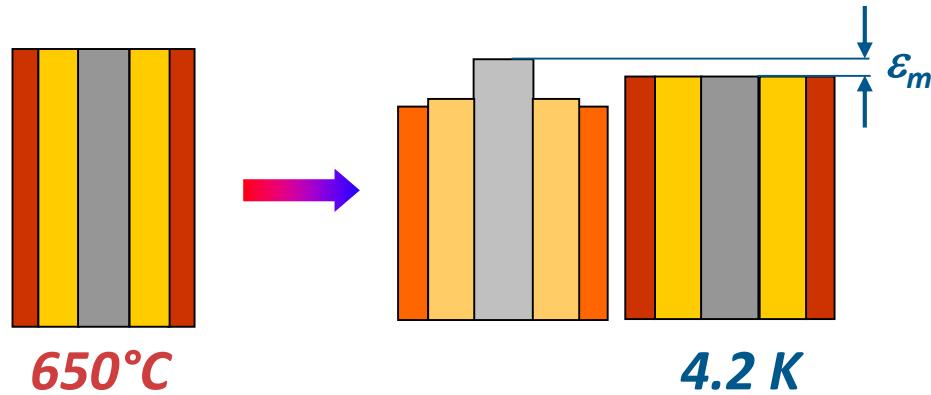


In straight-sided coils such as accelerator magnet, the conductor experiences large transverse forces

$F = 175 \text{ ton/m}$ in a LHC dipole

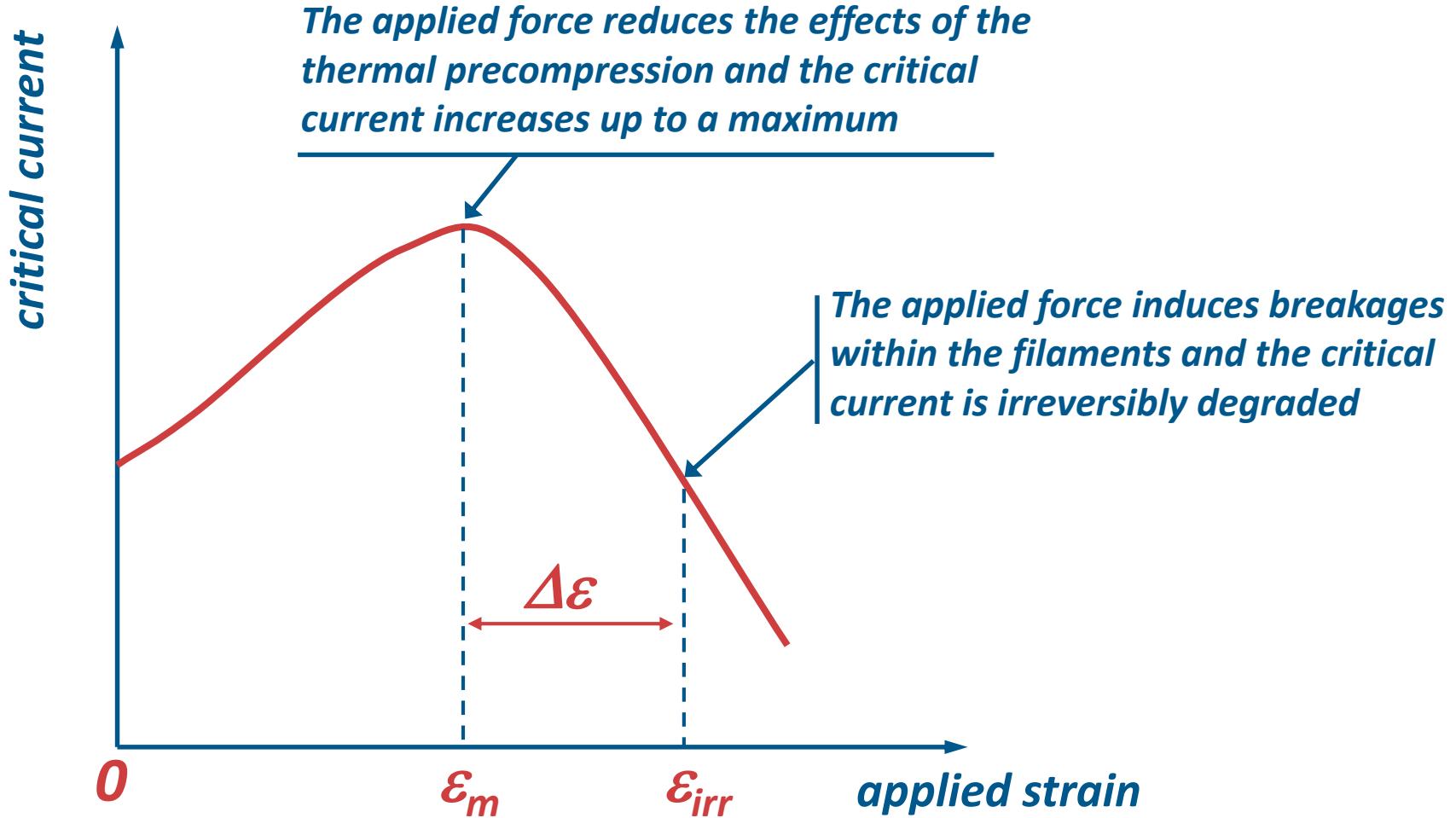
And also thermal stresses

Mismatch in thermal contraction at the cooldown



Strain-induced changes in the critical current

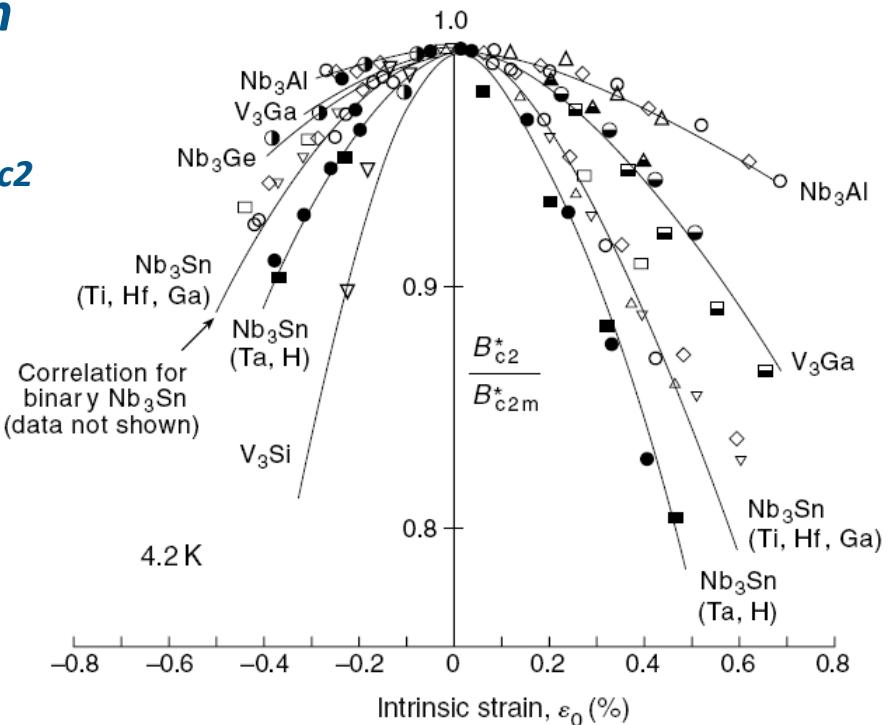
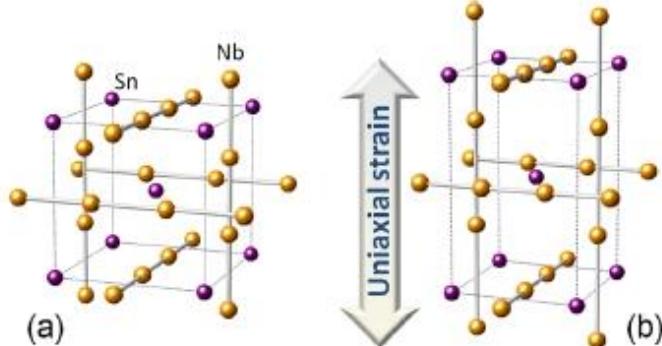
The case of Nb₃Sn



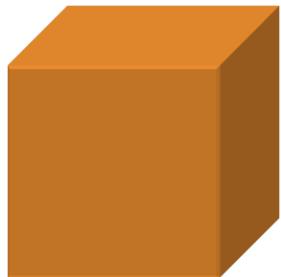
Reversible strain effects

Why superconducting properties depend on strain

Under strain the crystal structure deforms and this induces change both in the phonon spectrum and the electronic bands and thus on T_c and B_{c2}

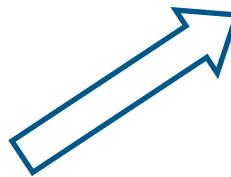


Reversible strain effects in Nb_3Sn wires

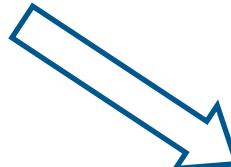
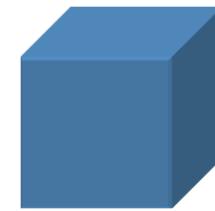


*Cubic-shaped stress-free
cell for Nb_3Sn*

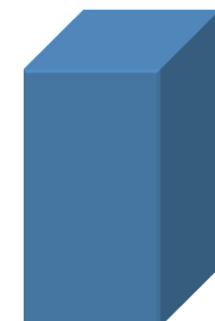
*Precompression induced by
cooling to low temperature
has two components*



HYDROSTATIC
Change of the cell volume

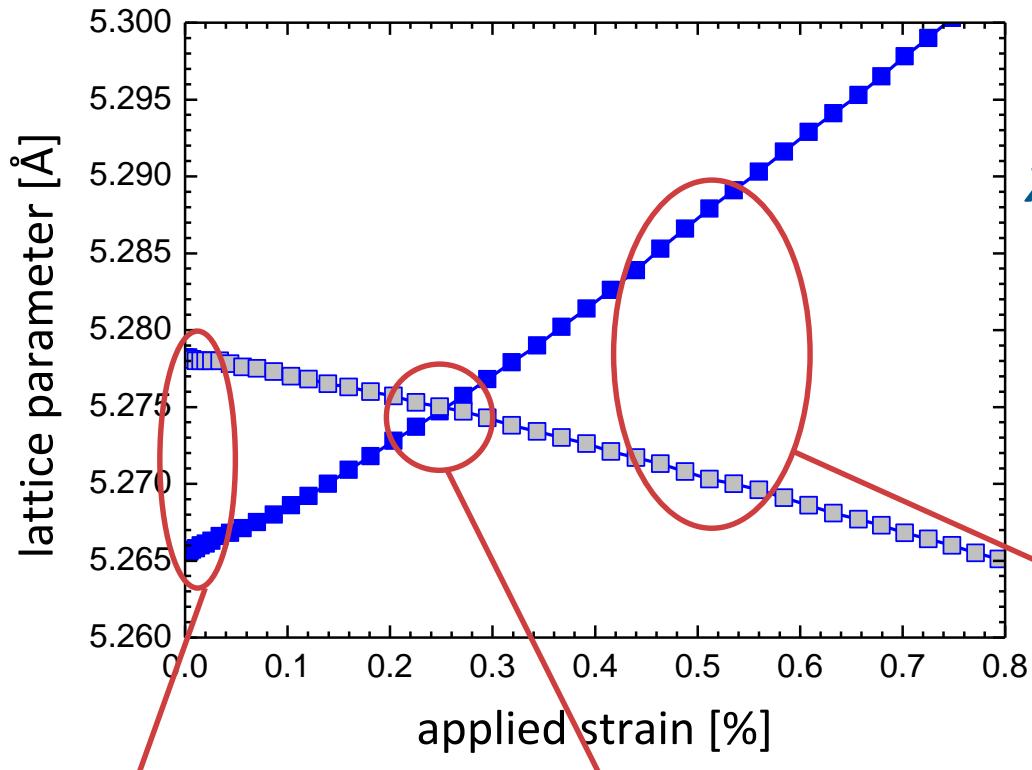


DEVIATORIC
Change of the cell shape



Reversible strain effects in Nb_3Sn wires: lattice parameters

Bronze route wire: Nb_3Sn lattice parameters vs axial strain @ 4.2K



XRD experiments @ ESRF Grenoble

C. Scheuerlein et al., IEEE TAS 19 (2009) 2653

L. Muzzi et al., SUST 25 (2012) 054006

HIGH APPLIED STRAIN
Again Hydrostatic+Deviatoric

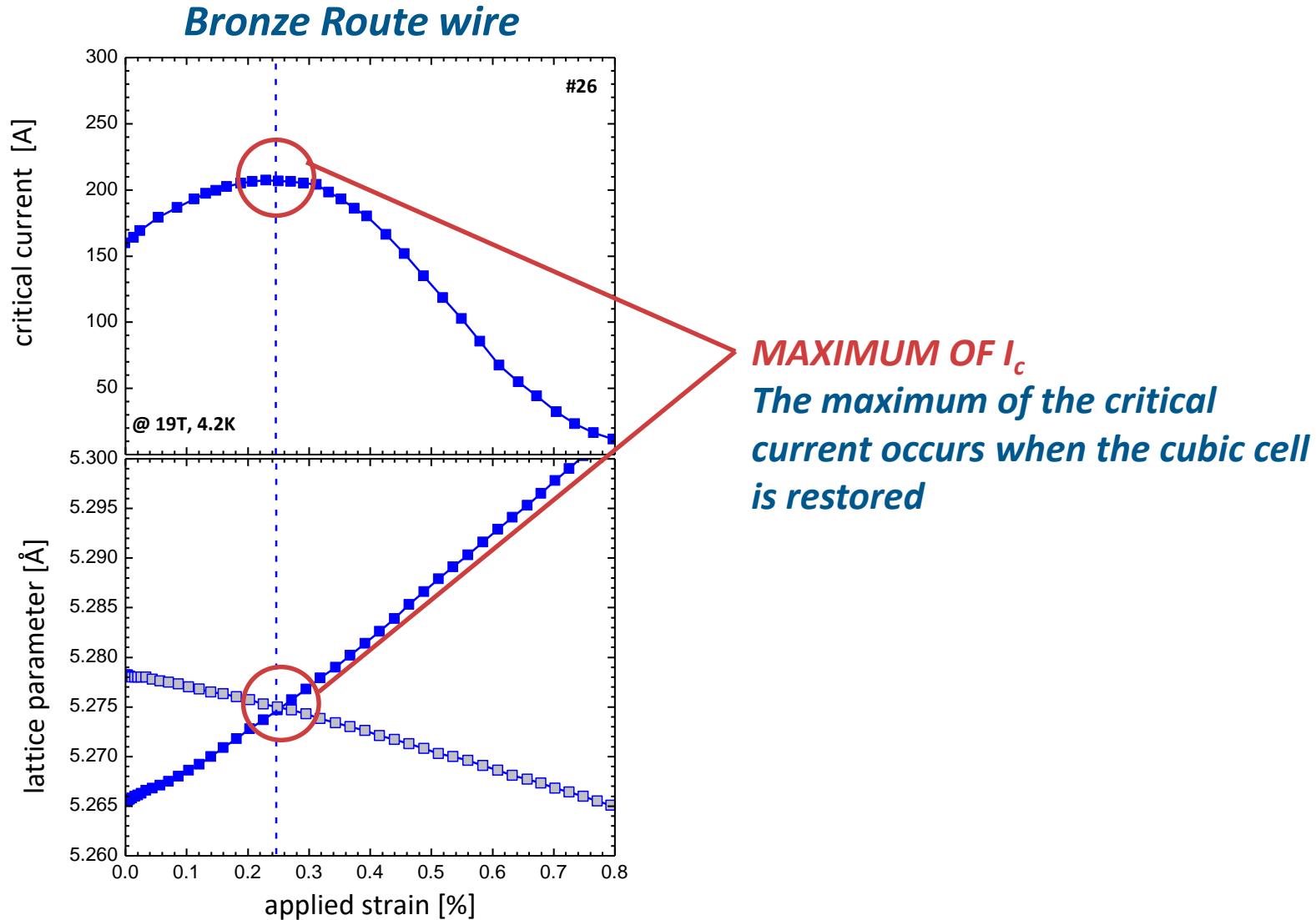
ZERO APPLIED STRAIN

Nb_3Sn is precompressed
Hydrostatic+Deviatoric

CROSSING POINT

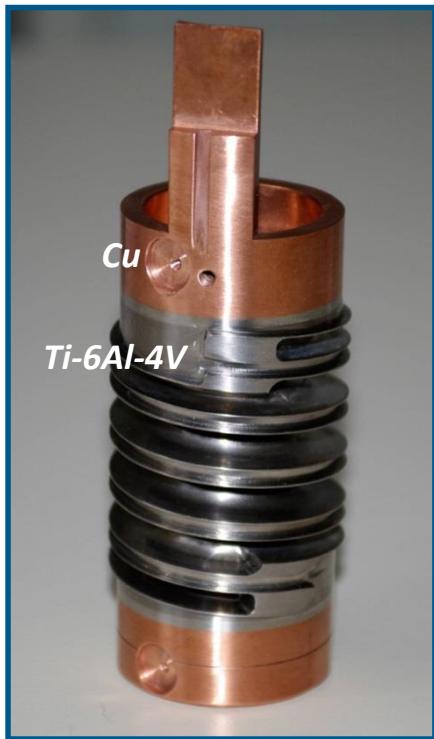
Cubic cell recovered
Hydrostatic component still
present

Lattice parameters and I_c under axial strain

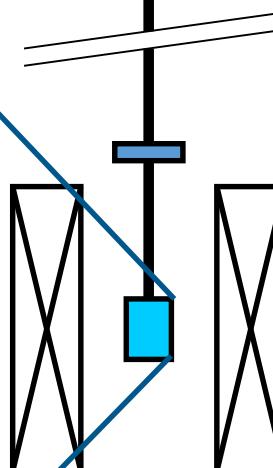


How to mesure I_c vs. axial strain

The WASP (Walters Spring) probe



Motor @ room temperature

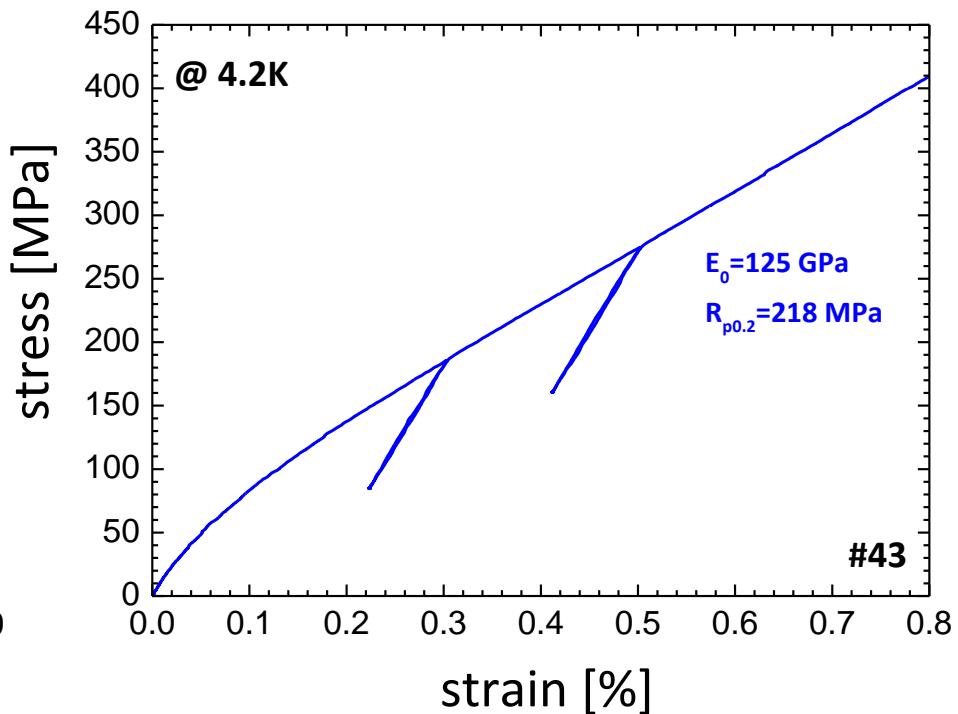
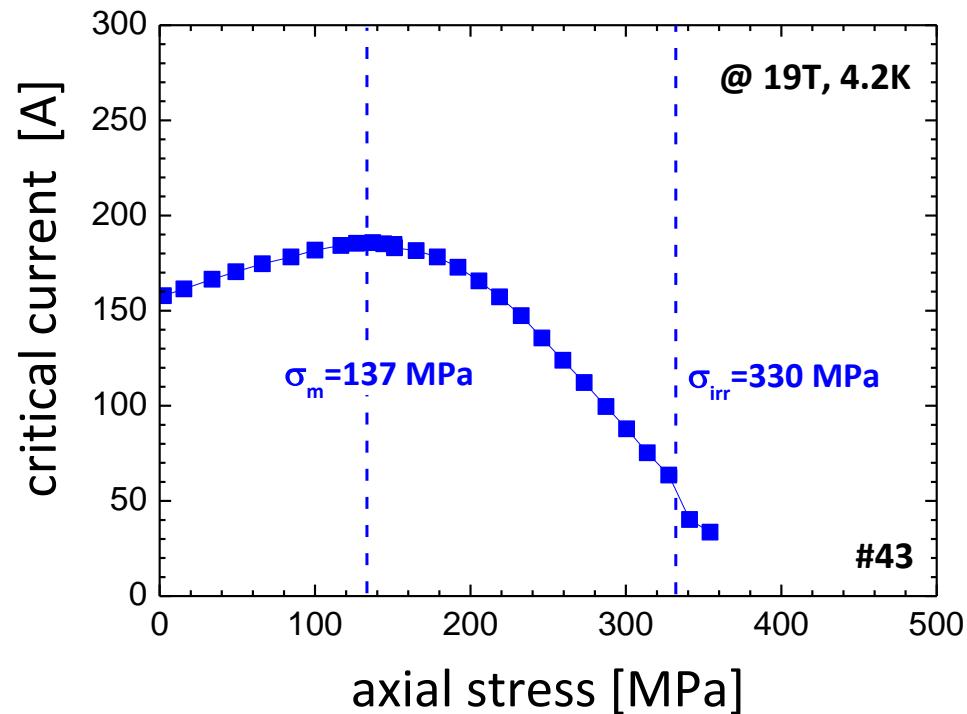


B. Seeber et al., Rev. Sci. Instr. 76 (2005) 093901

<i>Max current</i>	<i>1000 A</i>
<i>Sample length</i>	<i>1.1 meter</i>
<i>Voltage taps distance</i>	<i>126 mm</i>
<i>Electrical field criterion</i>	<i>0.01 μV/cm</i>
<i>Strain (ϵ)</i>	<i>up to $\pm 1.2\%$</i>

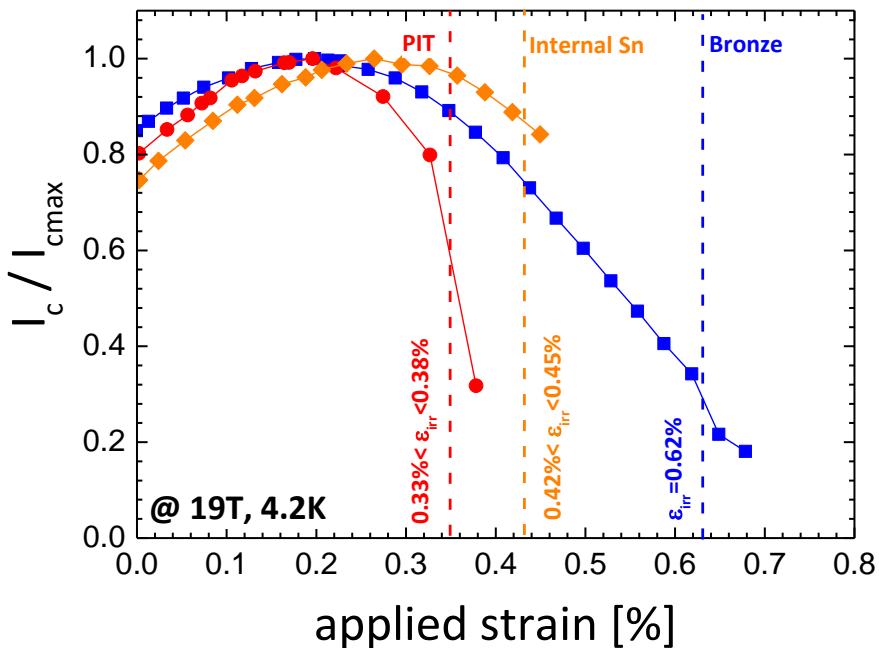
From I_c vs. strain to I_c vs. stress

Bronze Route wire

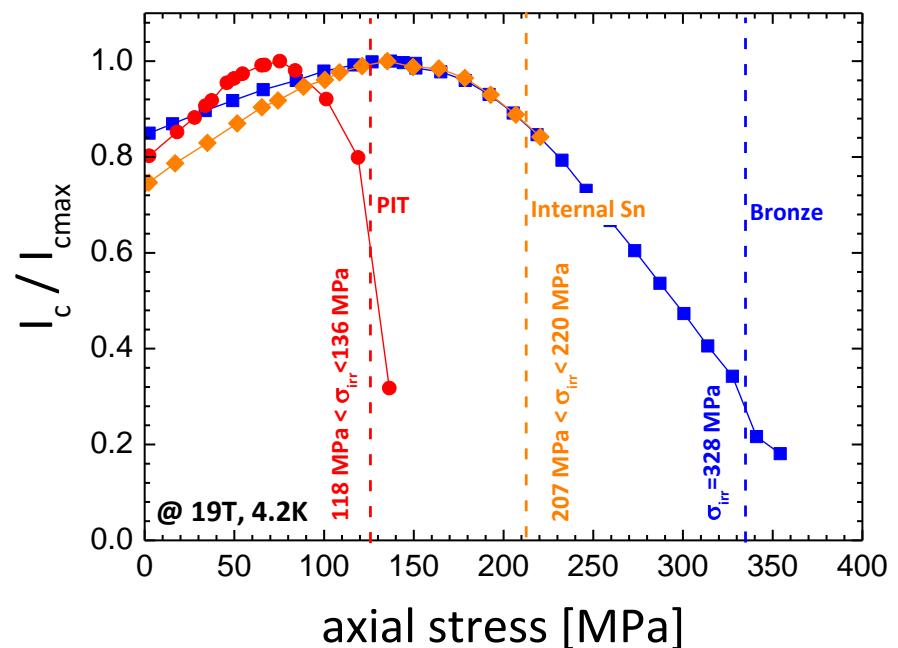


Bronze Route, Internal Sn and PIT: a comparison

I_c vs. axial strain



I_c vs. axial stress



Technology

σ_{irr}

Bronze Route

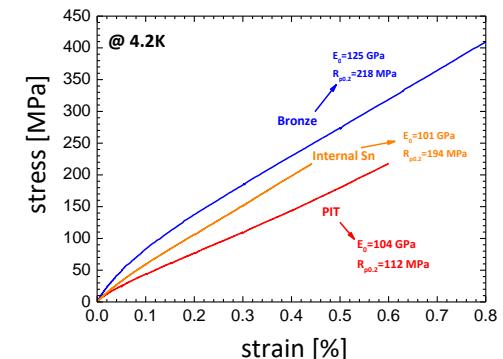
330 MPa

Internal Sn

210 MPa

Powder-In-Tube

120 MPa



Degradation upon transverse loads

High field dipoles based on high J_c Nb_3Sn Rutherford cables require coil pre-stresses larger than 100 MPa, with peak stress of ~ 200 MPa at operation

Are the Nb_3Sn wires in the cable able to withstand such a high stress level? Which degradation is tolerable?

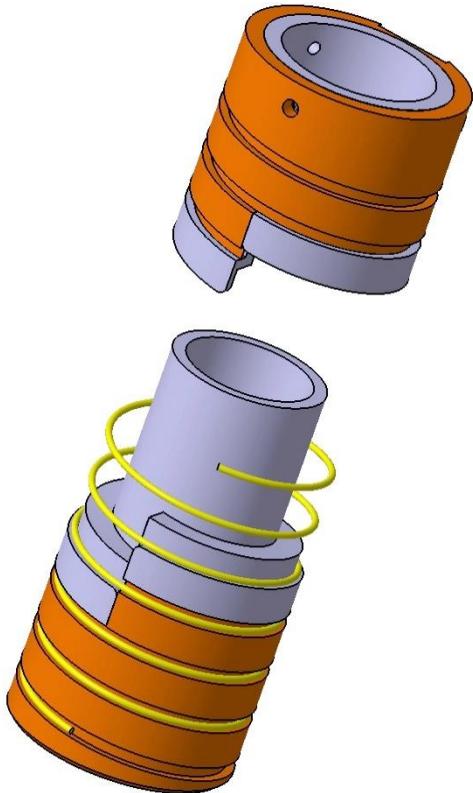


Nb₃Sn Rutherford cable for HL-LHC, 40 strands

- *Nb₃Sn wires are deformed during cabling*
- *Cables are braided with glass fiber*
- *The winding is impregnated with resin*

Is it possible to extrapolate the behaviour of the cable from a single wire experiment?

The WASP concept for l_c vs. transverse stress



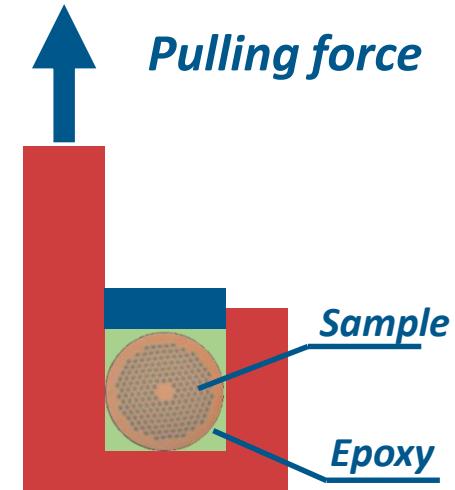
3 groove widths

1.30 mm

1.15 mm

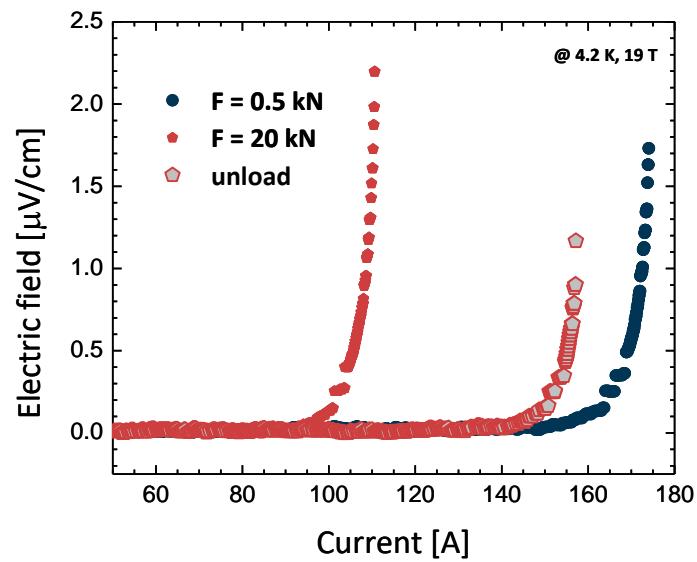
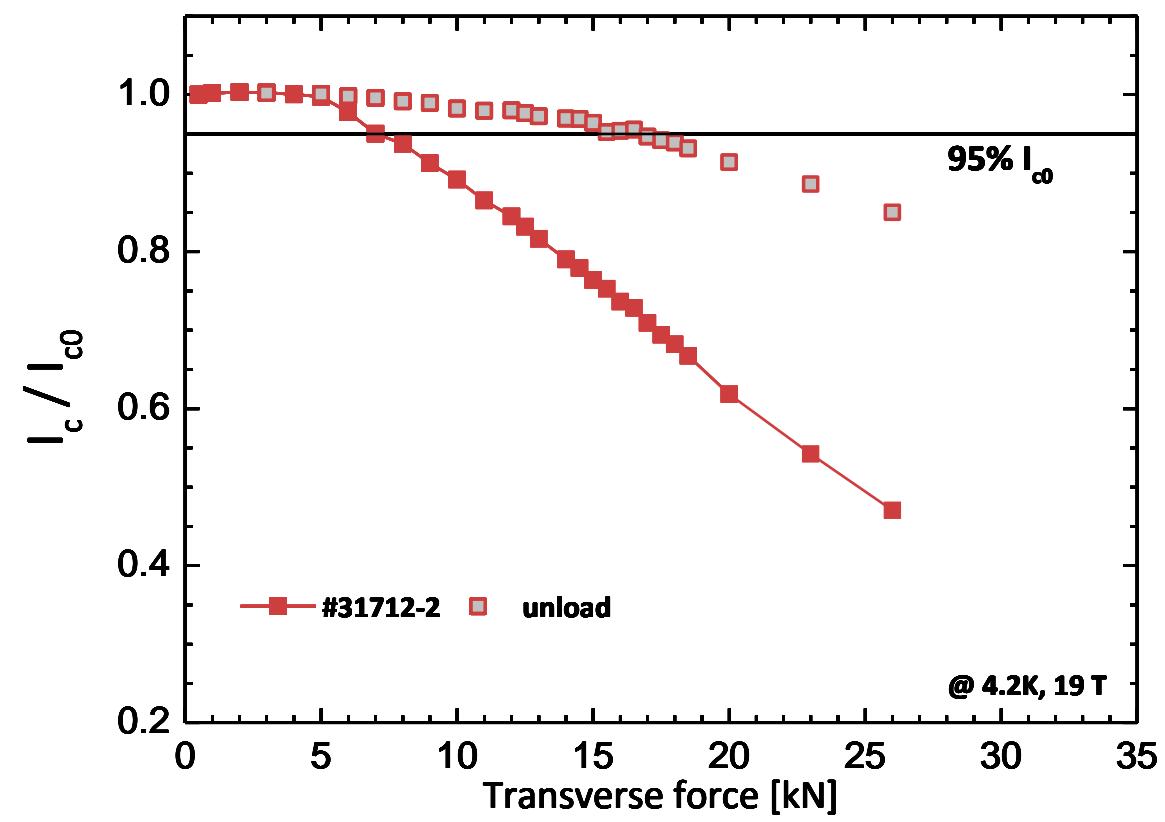
1.00 mm

4-WALL + impregnation



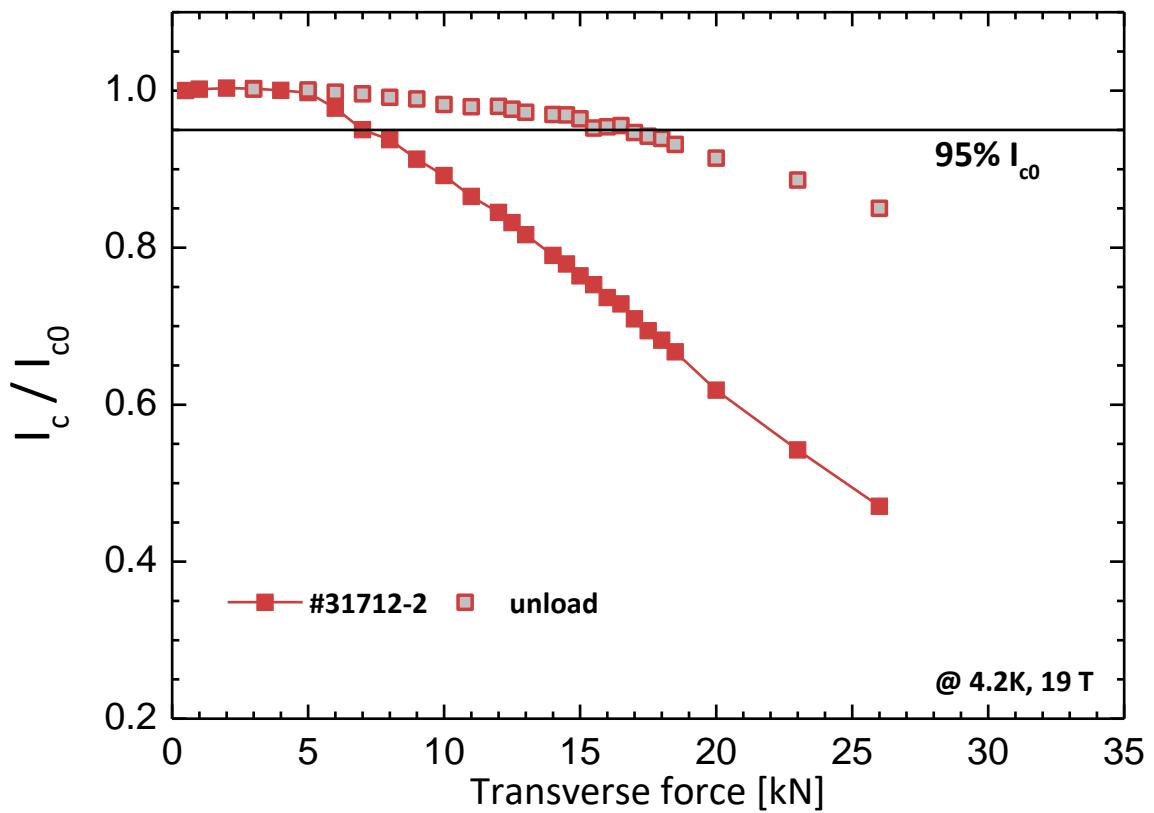
*Wire impregnated with epoxy
applied stress uniformly
distributed*

How the measurement works



Wire ID	Diameter [mm]	# of filaments	Filament size/shape	Cu/nonCu	Non-Cu $J_c(12T,4.2K)$ [A/mm ²]
#31712 #14310 Fresca2	1.0	192	~50 μm round	1.22	2450

How the measurement works



The irreversible limit is defined at the force level leading to a 95% recovery of the initial I_c after unload

Here

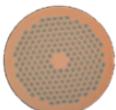
$$F_{irr} = 16 \text{ kN}$$

The corresponding irreversible stress limit is

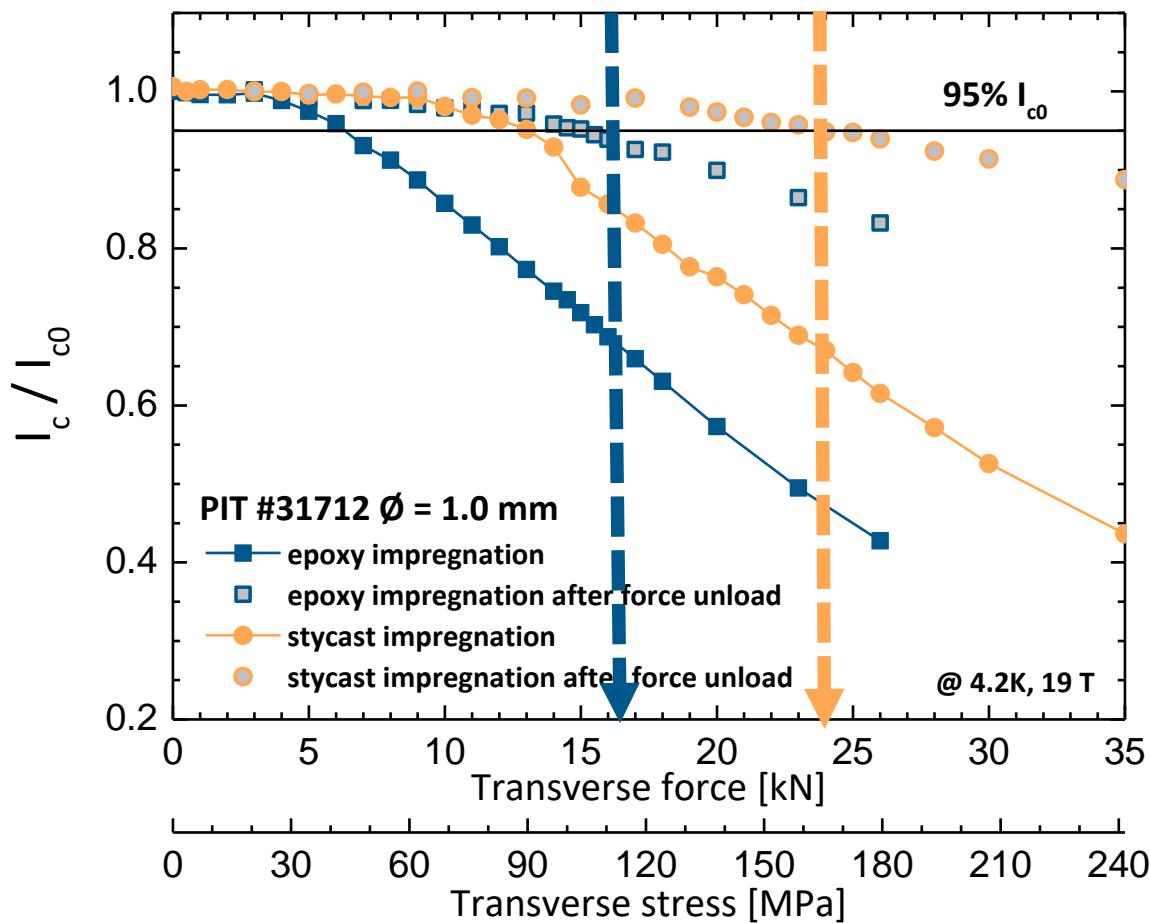
$$\sigma_{irr} = 110 \text{ MPa}$$

where

$$\text{Stress} = \frac{\text{Force}}{\text{groove length} \times \text{groove width}}$$

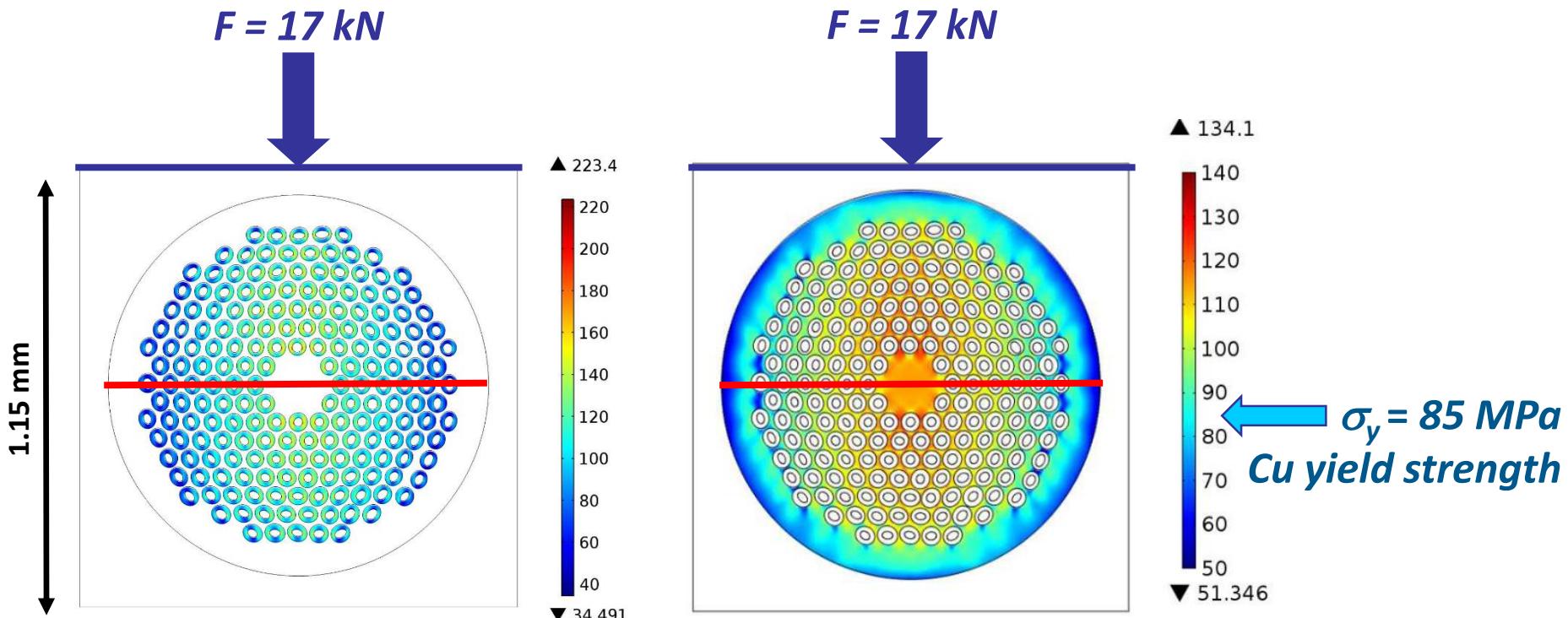
Wire ID	Diameter [mm]	# of filaments	Filament size/shape	Cu/nonCu	Non-Cu $J_c(12T,4.2K)$ [A/mm ²]
#31712 #14310 Fresca2	1.0	192	~50 μm round	1.22	2450
					

I_c vs. transverse stress: epoxy vs. stycast



*The change of resin, from epoxy to stycast, leads to an increase of σ_{irr} by > 50 MPa
The result is comparable to the value found with epoxy + glass fiber sleeve*

FEM: stress redistribution in the wire

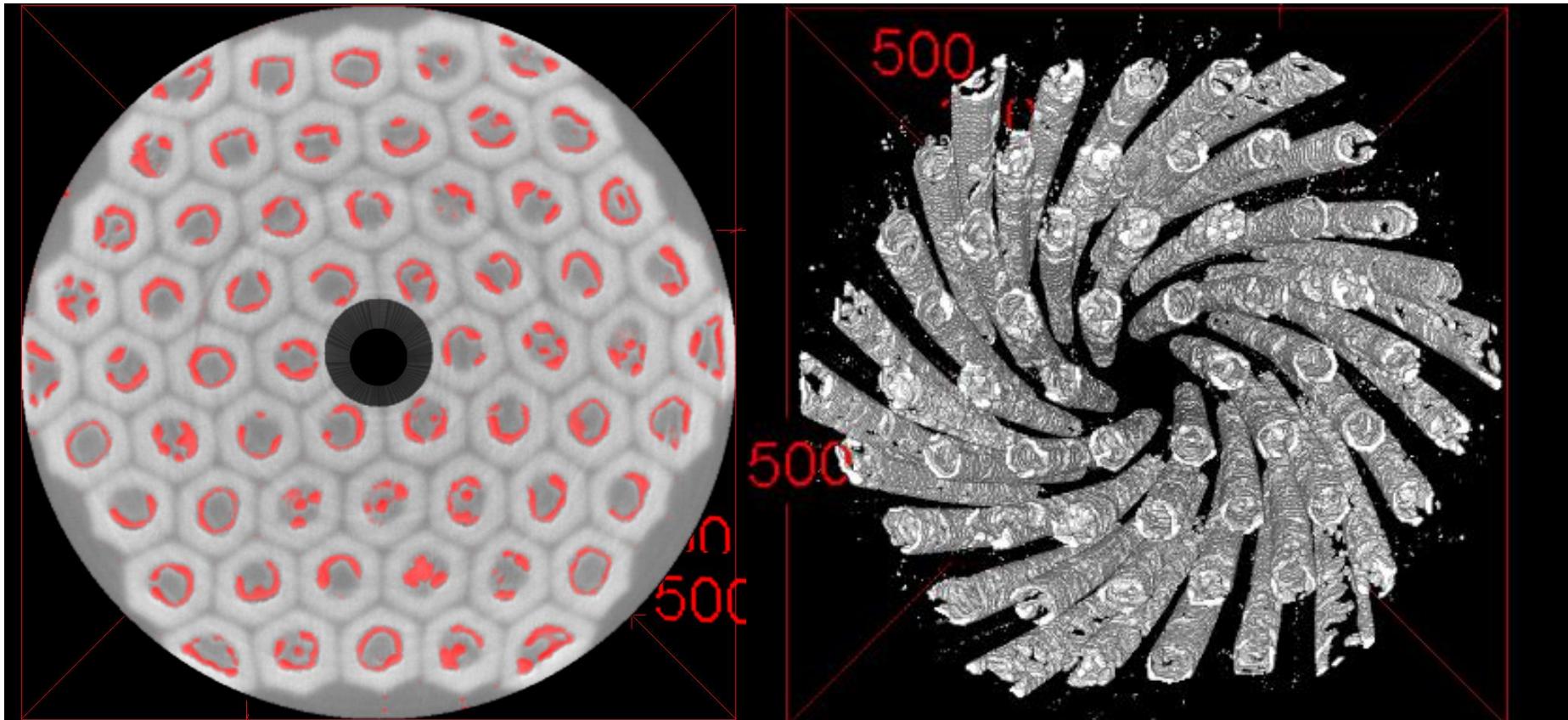


Irreversible degradation is determined by filament cracks and residual strain on Nb₃Sn imposed by plastically deformed Cu

FEM suggests that smaller filaments and higher Cu/nonCu ratio lead to higher stress tolerance

XRD Microtomography

Void morphology in RRP wires

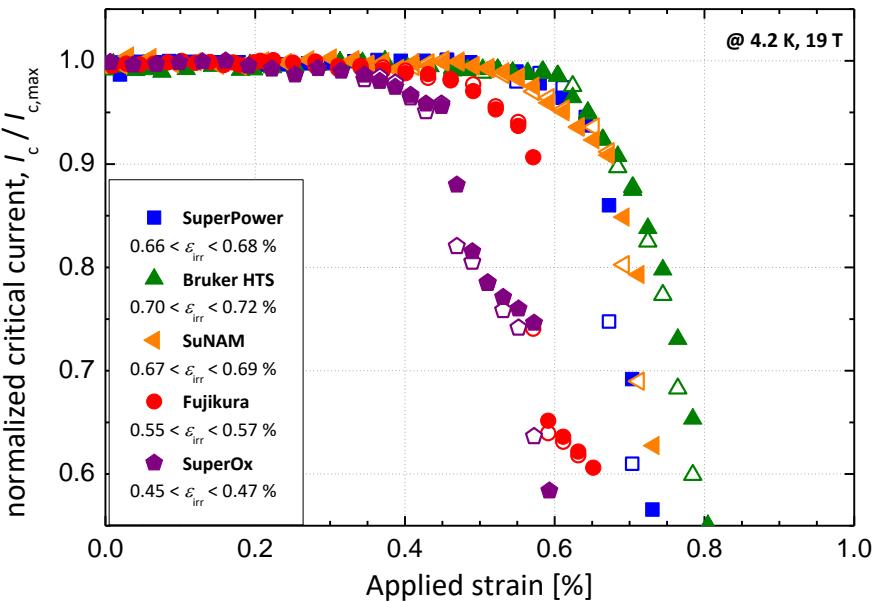


And what about REBCO tapes ?

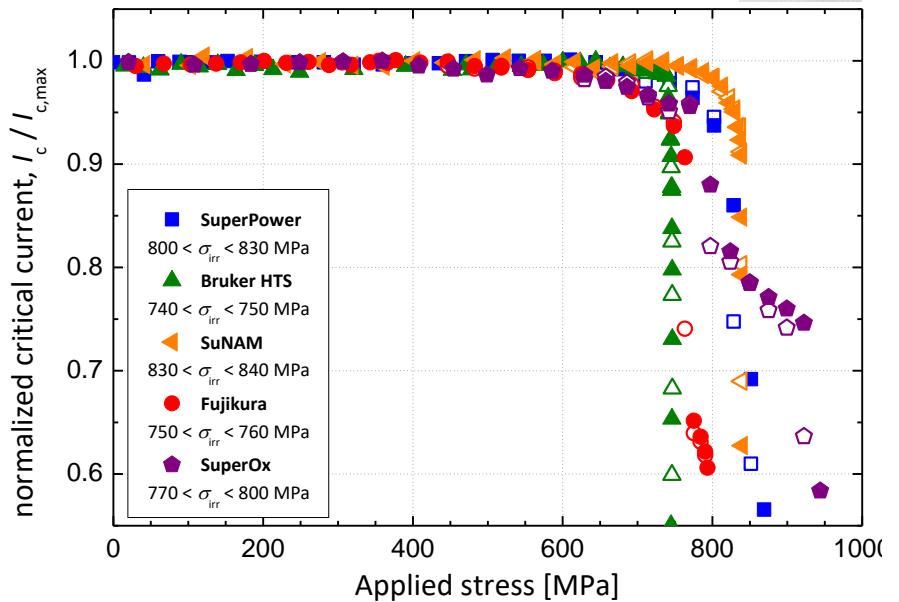


REBCO CCs: Dependence of I_c on axial loads

I_c vs. axial strain



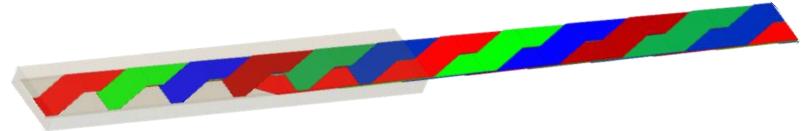
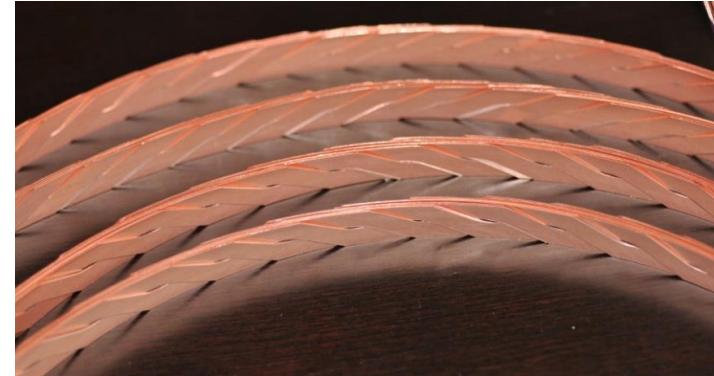
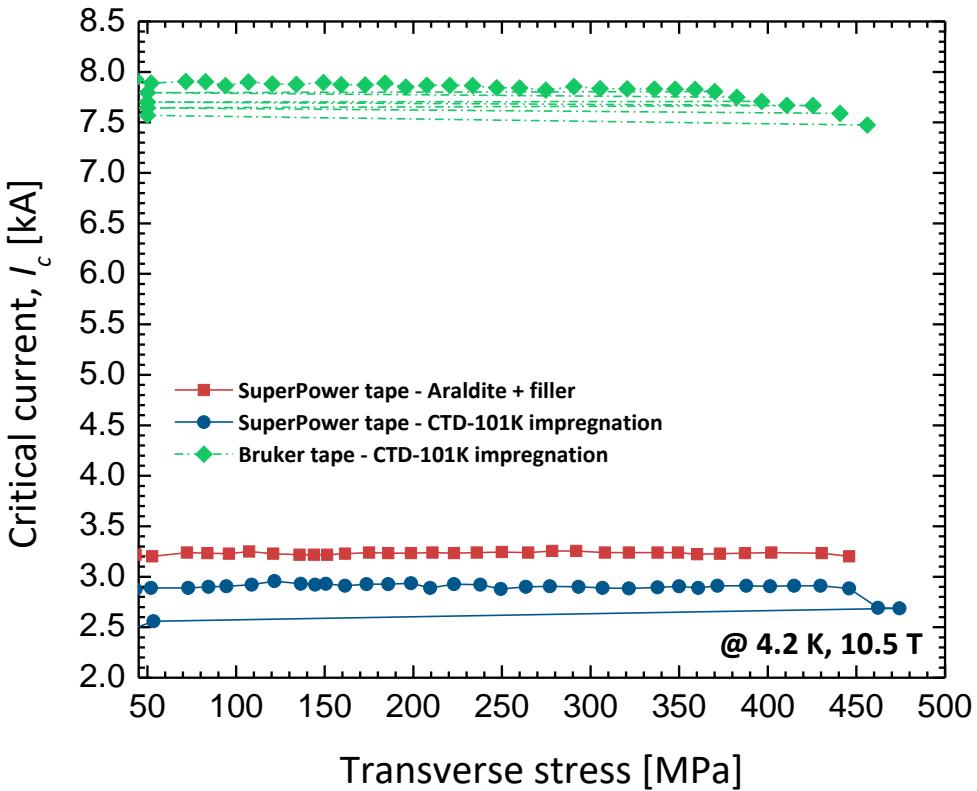
I_c vs. axial stress



- REBCO CCs are inherently strong, ~50% is a high strength alloy
- Very low stress effect → curves are flat in rev. region
- Irreversible stress limits above 500 MPa
- The only weakness is delamination...



REBCO Roebel cables under transverse compression



- *2 REBCO tape manufacturers*
- *2 different impregnation resins*
- *Irreversible stress limit > 400 MPa*