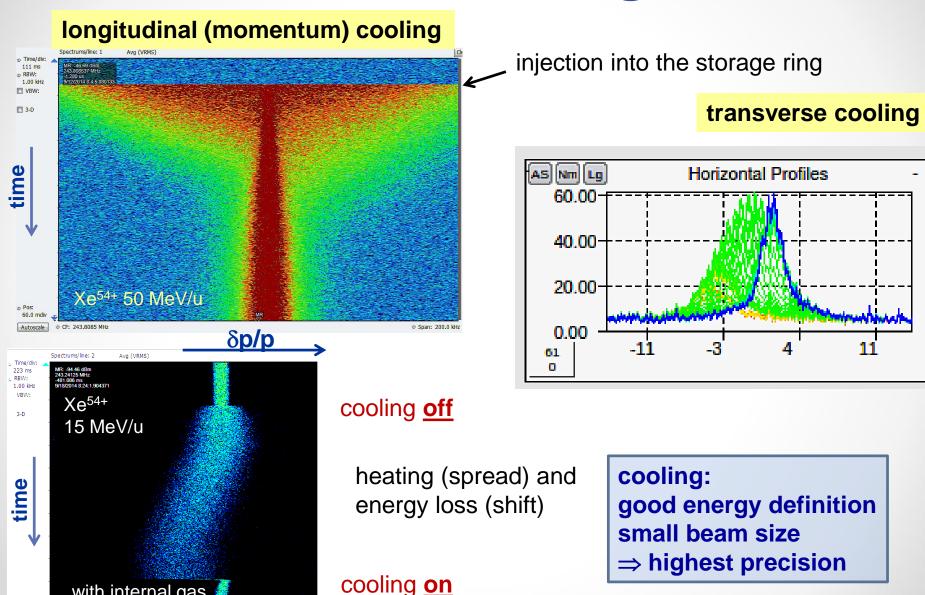
M. Steck, GSI, Darmstadt

CAS, Warsaw, 27 September – 9 October, 2015



with internal gas target operation

□ CF: 243.740 MHz

Introduction

- 1. Electron Cooling
- 2. Ionization Cooling
- 3. Laser Cooling
- 4. Stochastic Cooling

- Beam cooling is synonymous for a reduction of beam temperature.
- Temperature is equivalent to terms as phase space volume, emittance and momentum spread.
- Beam Cooling processes are not following Liouville's Theorem:
- `in a system where the particle motion is controlled by external conservative forces the phase space density is conserved' (This neglects interactions between beam particles.)
- Beam cooling techniques are non-Liouvillean processes which violate the assumption of a conservative force.
- e.g. interaction of the beam particles with other particles (electrons, photons, matter)

Cooling Force

Generic (simplest case of a) cooling force:

$$F_{x,y,s} = -\alpha_{x,y,s} v_{x,y,s}$$

 $v_{x,v,s}$ velocity in the rest frame of the beam

non conservative, cannot be described by a Hamiltonian

For a 2D subspace distribution function f(z, z', t)

$$F_z = -\alpha_z v_z \quad z = x, y, s \quad v_z = v_0 \cdot z'$$

$$\frac{df(z,z',t)}{dt} = -\lambda_z f(z,z',t) \qquad \lambda_z \text{ cooling (damping) rate}$$

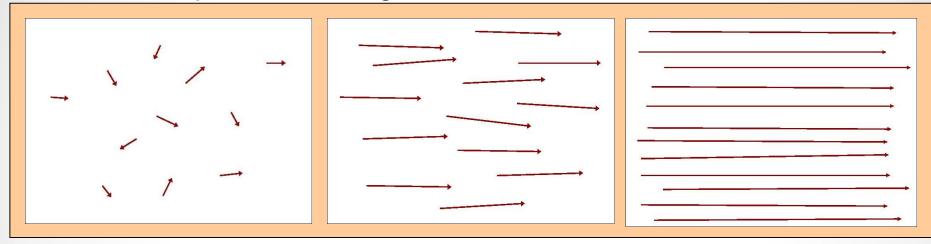
in a circular accelerator:

Transverse (emittance) cooling
$$\epsilon_{x,y}(t_0+t)=\epsilon_{x,y}(t_0)\ e^{-\lambda_{x,y}t}$$
 Longitudinal (momentum spread) cooling
$$\frac{\delta p_{\parallel}}{p_0}(t_0+t)=\frac{\delta p_{\parallel}}{p_0}(t_0)\ e^{-\lambda_{\parallel}t}$$

Beam Temperature

Where does the beam temperature originate from?

The beam particles are generated in a 'hot' source



at rest (source)

at low energy

at high energy

In a standard accelerator the beam temperature is not reduced (thermal motion is superimposed the average motion after acceleration)

but: many processes can heat up the beam

e.g. heating by mismatch, space charge, intrabeam scattering, internal targets, residual gas, external noise

Beam Temperature Definition

Longitudinal beam temperature

$$\frac{1}{2}k_B T_{\parallel} = \frac{1}{2}mv_{\parallel}^2 = \frac{1}{2}mc^2\beta^2(\frac{\delta p_{\parallel}}{p})^2$$

Transverse beam temperature

$$\frac{1}{2}k_BT_{\perp} = \frac{1}{2}mv_{\perp}^2 = \frac{1}{2}mc^2\beta^2\gamma^2\theta_{\perp}^2 \qquad \theta_{\perp} = \frac{v_{\perp}}{\beta c}, \quad \theta_{\perp}(s) = \sqrt{\frac{\epsilon}{\beta_{\perp}(s)}}$$

$$\theta_{\perp} = \frac{v_{\perp}}{\beta c}, \quad \theta_{\perp}(s) = \sqrt{\frac{\epsilon}{\beta_{\perp}(s)}}$$

Distribution function

$$f(v_{\perp}, v_{\parallel}) \propto \exp(-rac{mv_{\perp}^2}{2k_BT_{\perp}} - rac{mv_{\parallel}^2}{2k_BT_{\parallel}})$$

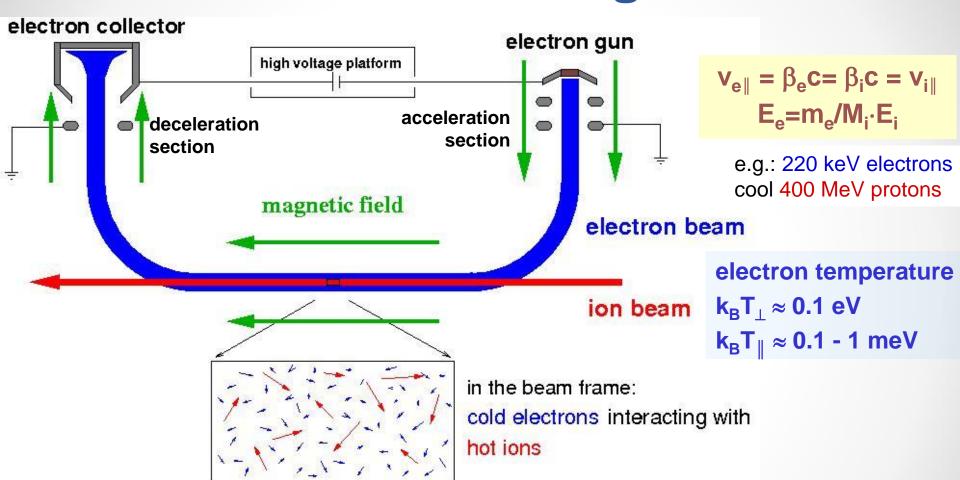
Particle beams can be anisotropic: $k_B T_{||} \neq k_B T_{\perp}$ e.g. due to laser cooling or the distribution of the electron beam

Don't confuse: beam energy ↔ beam temperature (e.g. a beam of energy 100 GeV can have a temperature of 1 eV)

Benefits of Beam Cooling

- Improved beam quality
 - Precision experiments
 - Luminosity increase
- Compensation of heating
 - Experiments with internal target
 - Colliding beams
- Intensity increase by accumulation
 - Weak beams from the source can be enhanced
 - Secondary beams (antiprotons, rare isotopes)

1. Electron Cooling

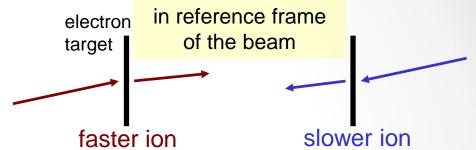


superposition of a cold intense electron beam with the same velocity

momentum transfer by Coulomb collisions cooling force results from energy loss in the co-moving gas of free electrons

Simple Derivation of the Electron Cooling Force

Analogy: energy loss in matter (electrons in the shell)



Rutherford scattering:
$$2 \ tan(\frac{\theta}{2}) = \frac{2Z_1Z_2e^2}{4\pi\epsilon_0\Delta pvb}$$
 $Z_1 = Q \ (ion), \ Z_2 = -1 \ (electron)$

Energy transfer:
$$\Delta E(b) = \frac{(\Delta p)^2}{2m_e} \simeq \frac{2Q^2e^4}{(4\pi\epsilon_0)^2m_ev^2} \frac{1}{b^2} \quad (for \quad b \gg b_{min})$$

Minimum impact parameter:
$$b_{min} = \frac{Qe^2}{(4\pi\epsilon_0)^2 m_e v^2}$$

from:
$$\Delta E(b_{min}) = \Delta E_{max} \simeq 2m_e v^2$$

Energy loss:

$$-\frac{dE}{dx} = 2\pi \int_{b_{min}}^{b_{max}} b n_e \Delta E \, db = \frac{4\pi Q^2 e^4}{(4\pi\epsilon_0)^2 m_e v^2} n_e \ln \frac{b_{max}}{b_{min}}$$

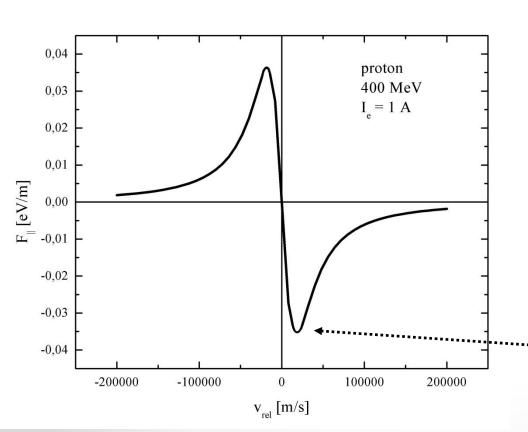
 $\begin{array}{c|c} & & & \\ & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\$

Coulomb logarithm $L_C=ln (b_{max}/b_{min}) \approx 10$ (typical value)

Characteristics of the Electron Cooling Force

$$\overrightarrow{F}(\overrightarrow{v_i}) = -\frac{4\pi Q^2 e^4 n_e}{(4\pi\epsilon_0)^2 m_e} \int L_C(\overrightarrow{v}_{rel}) f(\overrightarrow{v_e}) \frac{\overrightarrow{v}_{rel}}{v_{rel}^3} d^3 \overrightarrow{v_e}$$

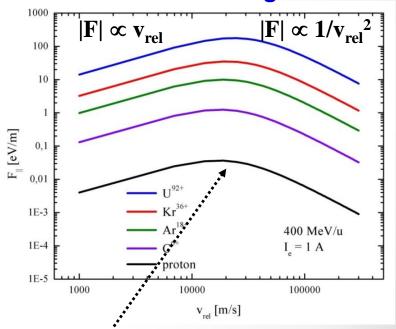
$$\overrightarrow{v}_{rel} = \overrightarrow{v_i} - \overrightarrow{v_e}$$



cooling force F

for small relative velocity: ∞v_{rel} for large relative velocity: ∞v_{rel}^{-2}

increases with charge: ∞ Q²



maximum of cooling force at effective electron temperature

Electron Cooling Time

first estimate: (Budker 1967)
$$\tau = \frac{3}{8\sqrt{2\pi}n_eQ^2r_er_icL_C}(\frac{k_BT_e}{m_ec^2} + \frac{k_BT_i}{m_ic^2})^{3/2}$$

for large relative velocities

cooling rate (τ^{-1}) :

- slow for hot beams $\propto \theta^{-3}$
- decreases with energy $\propto \gamma^{-2}$ ($\beta \cdot \gamma \cdot \theta$ is conserved)
- linear dependence on electron beam intensity n_e and cooler length $\eta = L_{ec}/C$
- favorable for highly charged ions Q²/A
- independent of hadron beam intensity

for small relative velocities

cooling rate is constant and maximum at small relative velocity

$$F \propto V_{rel} \Rightarrow \tau = \Delta t = p_{rel}/F = constant$$

Models of the Electron Cooling Force

binary collision model

description of the cooling process by successive collisions of two particles and integration over all interactions analytic expressions become very involved, various regimes (multitude of Coulomb logarithms)

dielectric model

interaction of the ion with a continuous electron plasma (scattering off of plasma waves) fails for small relative velocities and high ion charge

an empiric formula (Parkhomchuk) derived from experiments:

$$\overrightarrow{F} = -4 \frac{n_e}{m_e} \frac{(Qe^2)^2}{(4\pi\epsilon_0)^2} \ln\left(\frac{b_{max} + b_{min} + r_c}{b_{min} + r_c}\right) \frac{\overrightarrow{v}_{ion}}{(v_{ion}^2 + v_{eff}^2)^{3/2}}$$

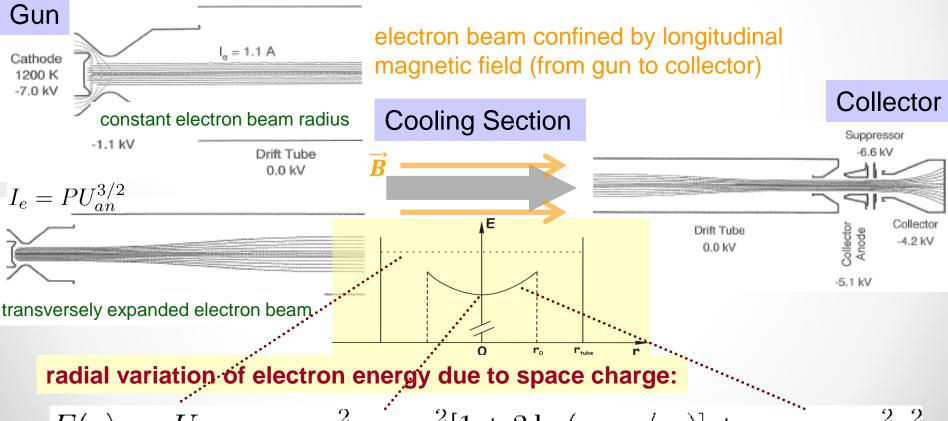
$$b_{min} = \frac{Qe^2/4\pi\epsilon_0}{m_e v_{ion}^2}; \quad b_{max} = \frac{v_{ion}}{min(\omega_{pe}, 1/T_{cool})}, \quad v_{eff}^2 = v_{e,\parallel}^2 + v_{e,\perp}^2$$

Electron Beam Properties

electron beam temperature

transverse $k_BT_{\perp}=k_BT_{cat}$, with transverse expansion ($\propto B_c/B_{gun}$) longitudinal $k_BT_{\parallel}=(k_BT_{cat})^2/4E_0<< k_BT_{\perp}$ lower limit : $k_BT_{\parallel}\geq 2e\frac{n_e^{1/3}}{4\pi\epsilon_0}$

longitudinal $k_B T_{\parallel} = (k_B T_{cat})^2/4E_0 << k_B T_{\perp}$ lower limit : $k_B T_{\parallel} \geq 2e_{4\pi}$ typical values: $k_B T_{\perp} \approx 0.1$ eV (1100 K), $k_B T_{\parallel} \approx 0.1$ - 1 meV



 $E(r) = eU_{cat} - \underline{n_e}\pi r_0^2 r_e m_e c^2 [1 + 2\ln(r_{tube}/r_0)] + \underline{n_e}\pi r_e m_e c^2 r^2$

Electron Motion in Longitudinal Magnetic Field

single particle cyclotron motion cyclotron frequency $\omega_c = eB/\gamma m_e$ cyclotron radius $r_c = v_\perp/\omega_c = (k_B T_\perp m_e)^{1/2} \gamma/eB$ electrons follow the magnetic field line adiabatically

important consequence: for interaction times long compared to the cyclotron period the ion does not sense the transverse electron temperature \Rightarrow magnetized cooling ($T_{eff} \approx T_{\parallel} << T_{\perp}$)

electron beam space charge:

transverse electric field + B-field \Rightarrow azimuthal drift $v_{azi} = r\omega_{azi} = r$

⇒ electron and ion beam should be well centered

Favorable for optimum cooling (small transverse relative velocity):

- high parallelism of magnetic field lines ΔB₁/B₀
- large beta function (small divergence) in cooling section

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 $2\pi r_e n_e c^2$

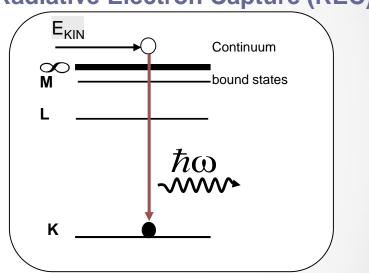
Imperfections and Limiting Effects in Electron Cooling

technical issues:

ripple of accelerating voltage
magnetic field imperfections
beam misalignment
space charge of electron beam
and compensation

physical limitation:

Radiative Electron Capture (REC)



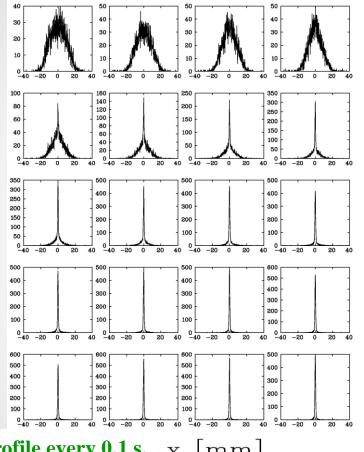
losses by recombination (REC)

loss rate
$$\tau^{-1} = \gamma^{-2} \alpha_{REC} n_e \eta$$

$$\alpha_{REC} = \frac{1.92 \times 10^{-13} Q^2}{\sqrt{k_B T}} \left(\ln \frac{5.66 Q}{\sqrt{k_B T}} + 0.196 (\frac{k_B T}{Q^2})^{1/3} \right) [cm^3 s^{-1}]$$

Examples of Electron Cooling

fast transverse cooling at TSR, Heidelberg



profile every 0.1 s. x [mm]

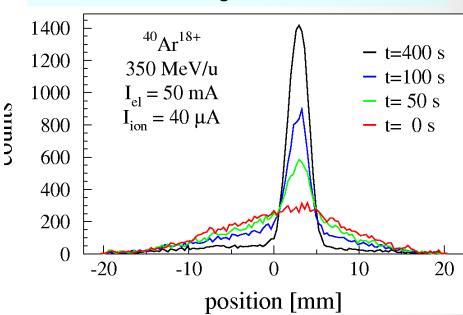
cooling of 6.1 MeV/u C⁶⁺ ions

0.24 A, 3.4 keV electron beam

 $n_{e} = 1.56 \times 10^{7} \text{ cm}^{-3}$

measured with residual gas ionization beam profile monitor

transverse cooling at ESR, Darmstadt

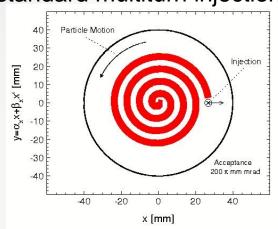


cooling of 350 MeV/u Ar¹⁸⁺ ions 0.05 A, 192 keV electron beam $n_e = 0.8 \times 10^6 \text{ cm}^{-3}$

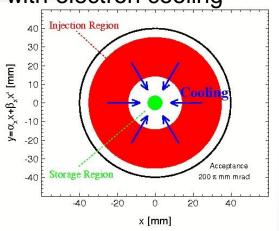
note! time scale, the cooling time varies strongly with beam parameters

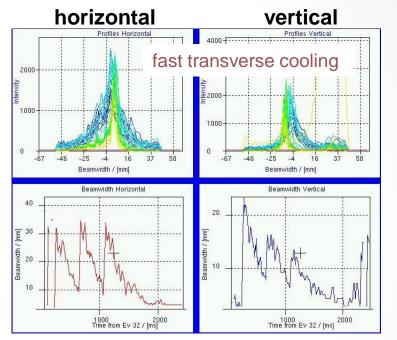
Accumulation of Heavy Ions by Electron Cooling

standard multiturn injection



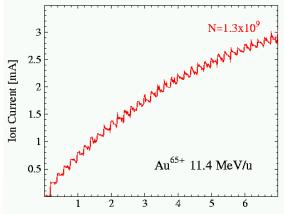
fast accumulation by repeated multiturn injection with electron cooling





profile

beam size



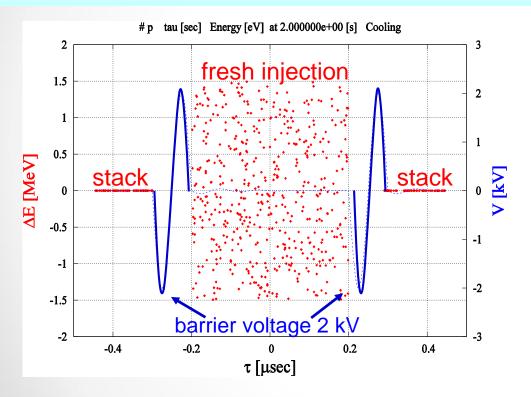
Time [s]

intensity increase in 5 s by a factor of ≈ 10

limitations: space charge tune shift, recombination (REC)

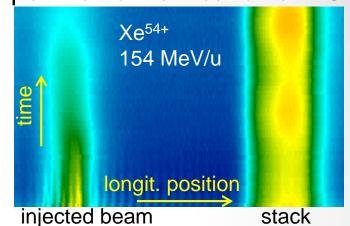
Accumulation of Secondary Particles

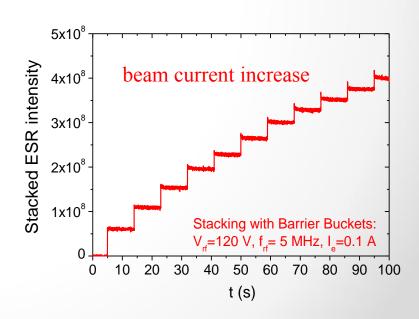
basic idea: confine stored beam to a fraction of the circumference, inject into gap and apply cooling to merge the two beam components ⇒ fast increase of intensity (for secondary beams)



simulation of longitudinal stacking with barrier buckets and electron cooling



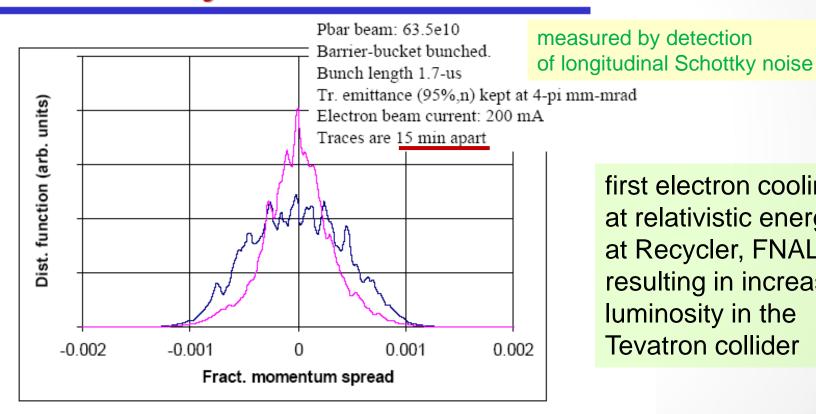




Examples of Electron Cooling

high energy electron cooling of 8 GeV antiprotons longitudinal cooling with 0.2 A, 4.4 MeV electron beam

First e-cooling demonstration - 07/15/05



first electron cooling at relativistic energy at Recycler, FNAL resulting in increased luminosity in the Tevatron collider

cooling time of some ten minutes has to be compared with the accumulation time of many hours

Electron Cooling Systems

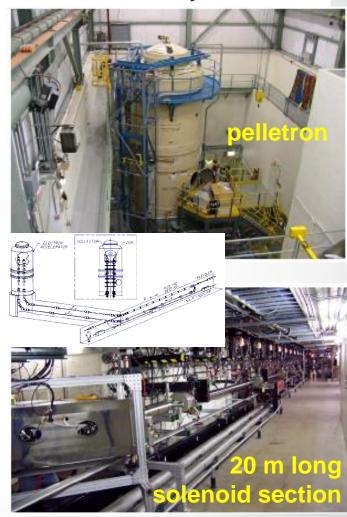
Low Energy: 35 keV SIS/GSI



Medium Energy: 300 keV ESR/GSI



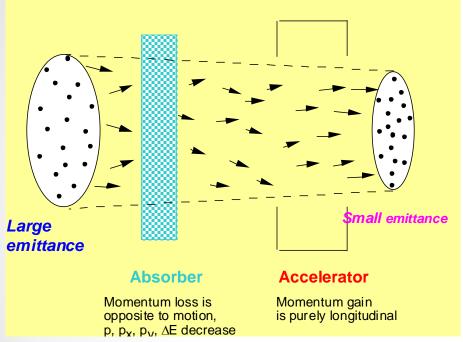
High Energy: 4.3 MeV Recycler/FNAL



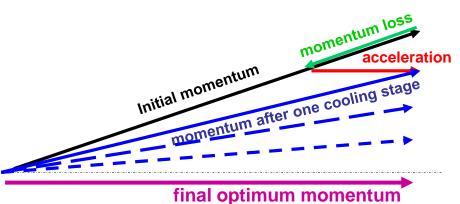
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2. Ionization Cooling

energy loss in solid matter



proposed for muon cooling



not useful for heavy particles due to strong interaction with matter

transverse cooling

$$\frac{d\epsilon_N}{ds} = -\frac{1}{\beta^2 E} \frac{dE}{ds} \epsilon_N + \frac{\beta \gamma \beta_\perp}{2} \frac{\langle \theta_{rms}^2 \rangle}{ds}$$
$$= -\frac{1}{\beta^2 E} \frac{dE}{ds} \epsilon_N + \frac{\beta_\perp E_s^2}{2\beta^3 m_\mu c^2 L_R E}$$

 \Rightarrow small β_{\perp} at absorber in order to minimize multiple scattering

large L_R , (dE/ds) \Rightarrow light absorbers (H₂)

Ionization Cooling

increased longitudinal cooling by longitudinal-transverse emittance exchange

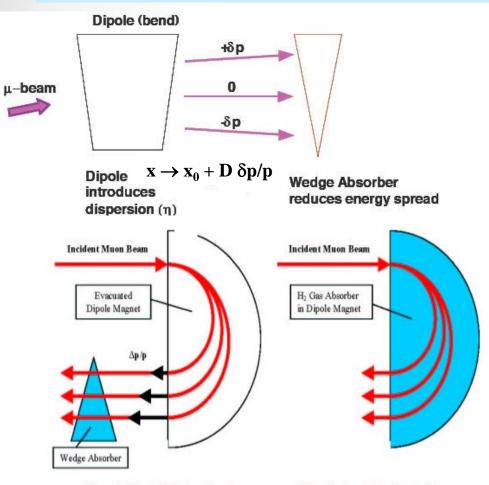


Figure 1. Use of a Wedge Absorber for Emittance Exchange

Figure 2. Use of Continuous Gaseous Absorber for Emittance Exchange

$$\frac{d\sigma_E^2}{ds} = -2\frac{\partial (dE/ds)}{\partial E}\sigma_E^2 + \frac{d\langle \Delta E_{rms}^2\rangle}{ds}$$
 cooling term heating term

cooling, if
$$\frac{\partial (dE/ds)}{\partial E} > 0$$

emittance exchange

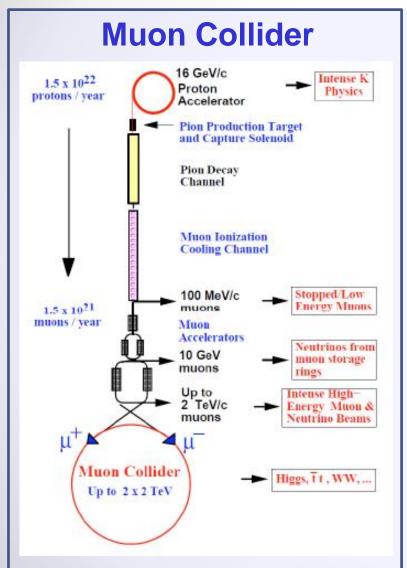
increased longitudinal cooling

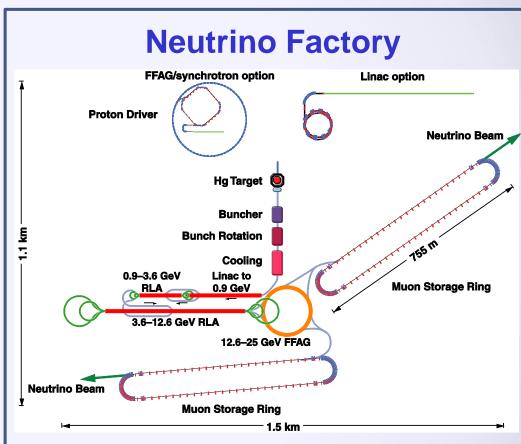
$$\frac{\partial \frac{dE}{ds}}{\partial E} \Rightarrow \frac{\partial \frac{dE}{ds}}{\partial E}|_{0} + \frac{dE}{ds} \frac{D\rho'}{\beta c p \rho_{0}}$$

reduced transverse cooling

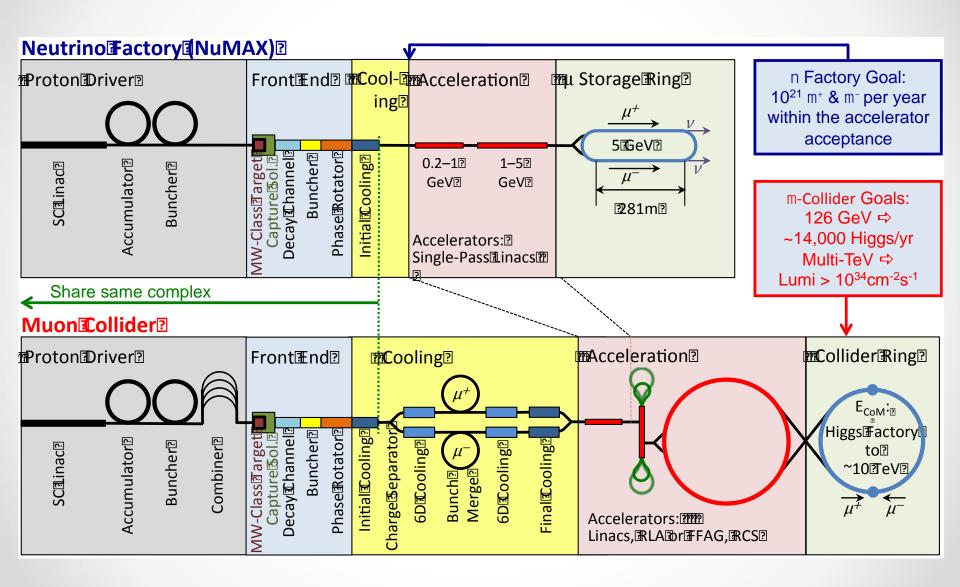
$$\frac{d\epsilon_N}{ds} = -\frac{1}{\beta^2 E} \frac{dE}{ds} (1 - \frac{D\rho'}{\rho_0}) \epsilon_N$$

Scenarios with Ionization Cooling



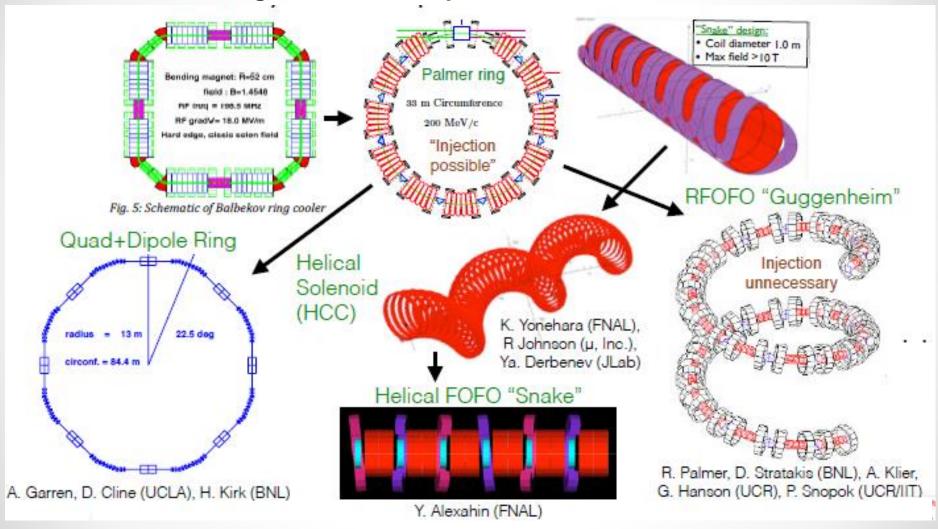


Scenarios with Ionization Cooling

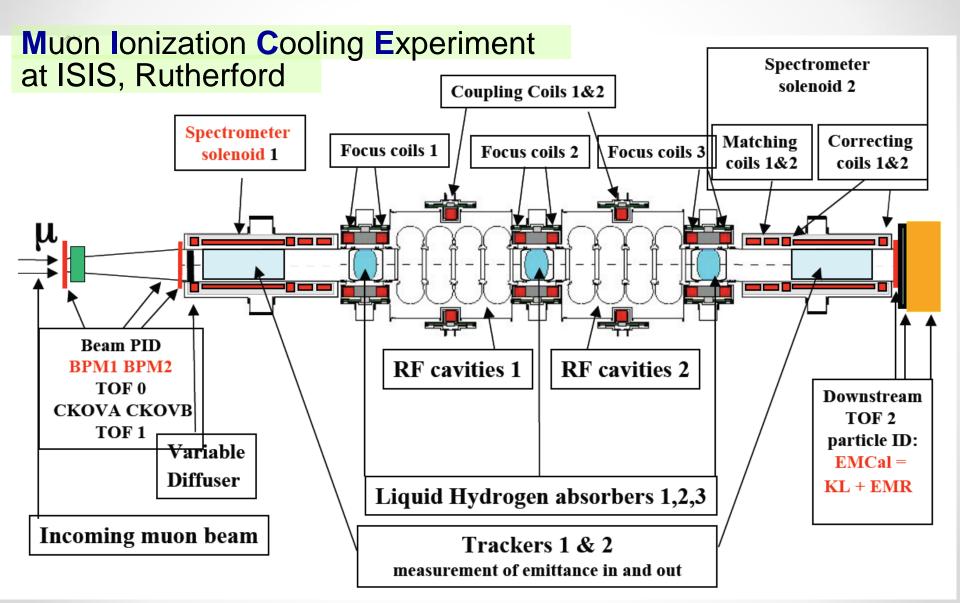


The Muon Cooling Section

studies for the arrangements of ion optical structure, absorber and rf section

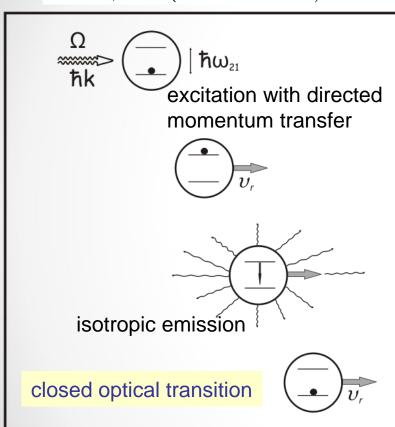


MICE

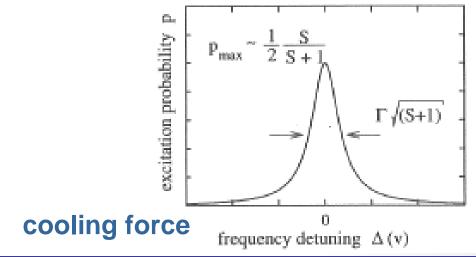


3. Laser Cooling

$$\Omega = \gamma \omega_{21} (1 - \beta \cos \theta)$$



the directed excitation and isotropic emission result in a transfer of velocity v_r



$$\overrightarrow{F}(\overrightarrow{v}, \overrightarrow{k}) = \frac{\hbar \overrightarrow{k}}{2} S\Gamma \frac{(\Gamma/2)^2}{(\omega - \omega_{21} - \overrightarrow{v} \overrightarrow{k}) + (\Gamma/2)^2 (1+S)}$$

Lorentzian with width $\Gamma/k \sim 10 \text{ m/s}$

minimum temperature
$$\,T_D=\frac{\hbar\Gamma}{2k_B}\,$$
 (Doppler limit) typical 10-5 – 10-4 K

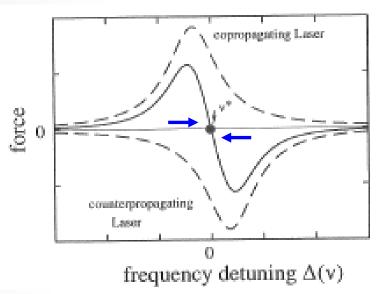
typical cooling time $\sim 10 \mu s$

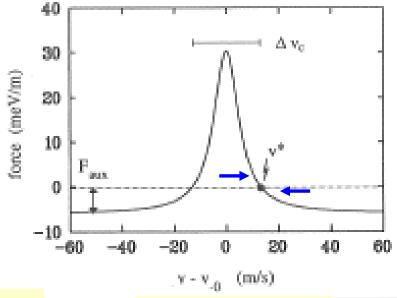
drawback: only longitudinal cooling

Laser Cooling

a single laser does not provide cooling (only acceleration or deceleration)

schemes for cooling





two counter-propagating lasers (matched to beam velocity, but slightly detuned)

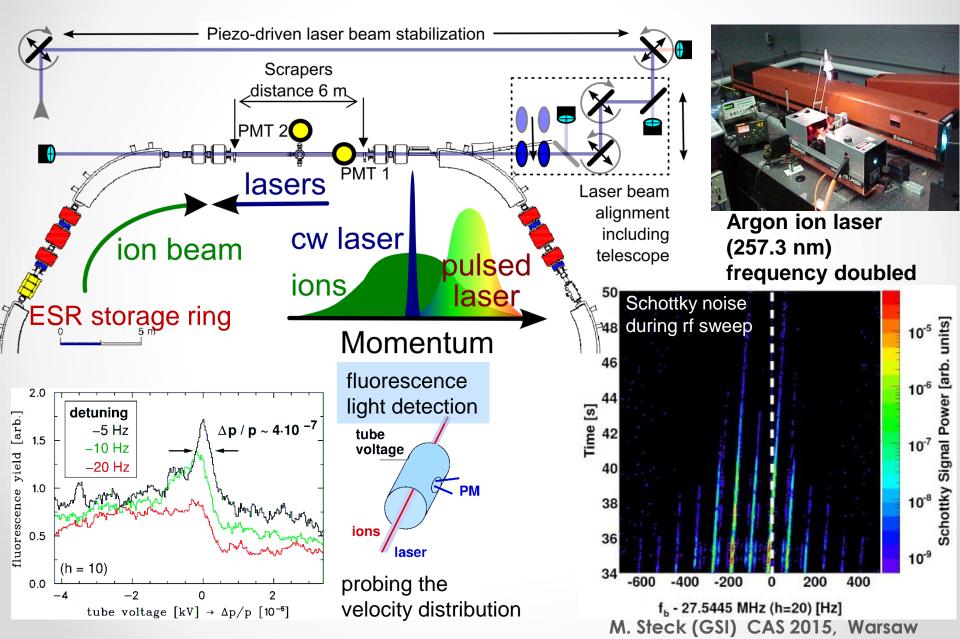
auxiliary force (betatron core, rf)

capture range of laser is limited ⇒ frequency sweep (snowplow)

ions studied so far: ⁷Li¹⁺, ⁹Be¹⁺, ²⁴Mg¹⁺, ¹²C³⁺

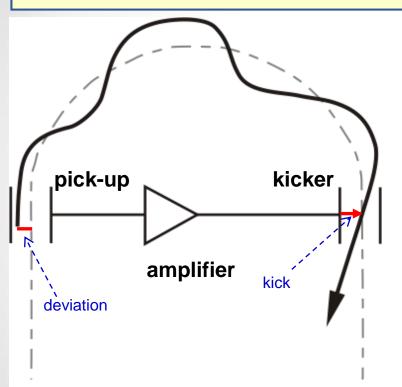
in future: Li-like heavy ions at relativistic energies large relativistic energy \Rightarrow large excitation energy in PRF Cooling rate increases with γ

Laser Cooling of C³⁺



4. Stochastic Cooling

First cooling method which was successfully used for beam preparation



S. van der Meer, D. Möhl, L. Thorndahl et al. (1925 – 2011) (1936-2012)

Conditions:

Betatron motion phase advance (pick-up to kicker): $(n + \frac{1}{2}) \pi$

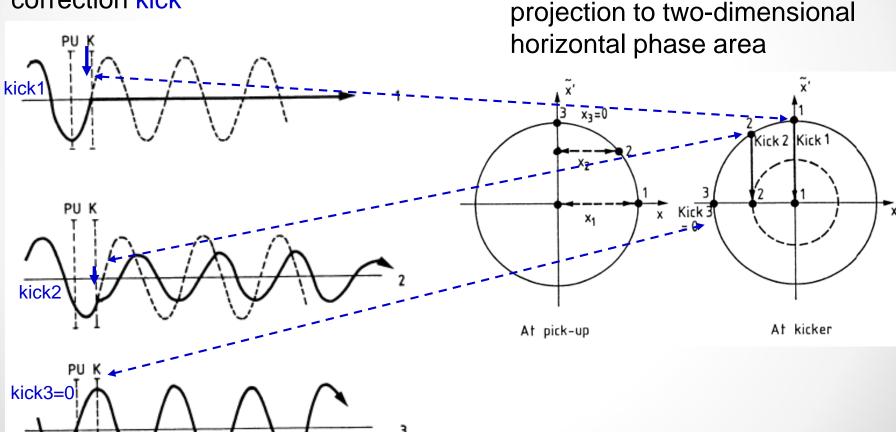
Signal travel time = time of flight of particle (between pick-up and kicker)

Sampling of sub-ensemble of total beam

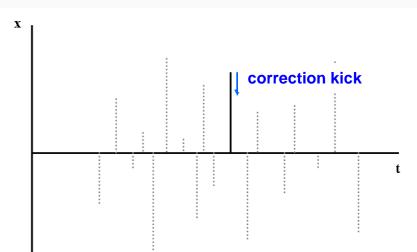
Principle of transverse cooling: measurement of deviation from ideal orbit is used for correction kick (feedback)

Stochastic Cooling

single particle betatron motion along storage ring without (dashed) and with (full) correction kick



Stochastic Cooling

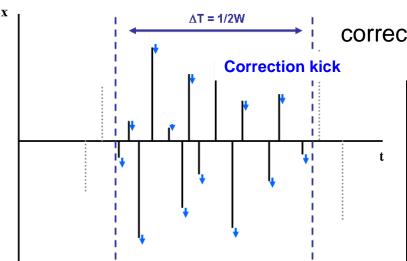


in time domain

correction kick (unlimited resolution)

$$\Delta x = g \times x$$

Nyquist theorem: a system with a band-width $\Delta f = W$ in frequency domain can resolve a minimum time duration $\Delta T = 1/(2W)$



correction kick
$$\Delta x = \frac{g}{N_s} \times \sum_{i=1..N_s} x_i$$
 , $N_s = N \frac{\Delta T}{T_0} = \frac{N}{2WT_0}$

For exponential damping $(x(t)=x(t_0)\cdot exp(-(t-t_0)/\tau))$:

$$\tau^{-1} = T_0^{-1} \times \frac{\Delta x}{x} = \frac{g2W}{N}, \ if \ \sum_{i=1..N_s} x_i = x$$

cooling rate

$$| au^{-1} \leq \frac{2W}{N} | if g$$

Stochastic Cooling

some refinements of cooling rate formula

noise: thermal or electronic noise adds to the beam signal

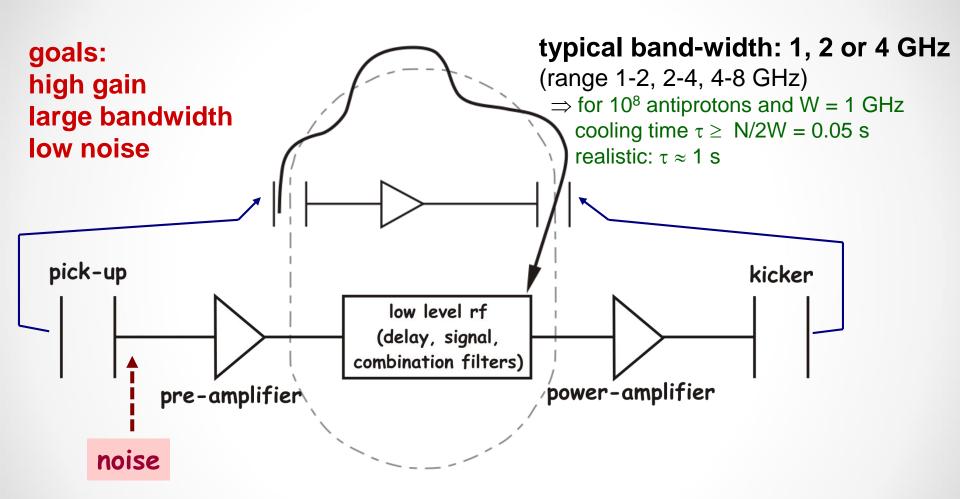
mixing: change of relative longitudinal position of particles due to momentum spread

$$\frac{d\lambda}{dq} = 0 \Rightarrow g = \frac{1}{M+U}$$

further refinement (wanted \leftrightarrow unwanted mixing):

with wanted mixing
$$M$$
 (kicker to pick-up)
$$\lambda = \tau^{-1} = \frac{2W}{N}(2g(1-\tilde{M}^2) - g^2(M+U))$$
 and unwanted mixing \tilde{M} (pick-up to kicker)

Stochastic Cooling Circuit



Transfer Function:

$$Z_{pick-up} \cdot G_{pick-up}(E) \cdot H(t_{delay}) \cdot F(E) \cdot G \cdot G_{kicker}(E) \cdot Z_{kicker}$$

Longitudinal Stochastic Cooling

1) Palmer cooling

pick-up in dispersive section detects horizontal position

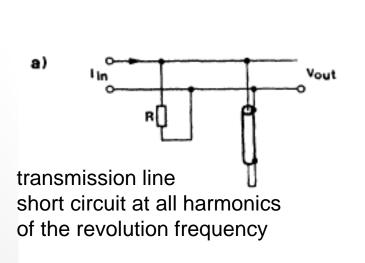
⇒ acceleration/deceleration kick corrects momentum deviation

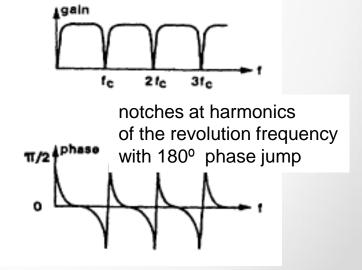
2) Notch filter cooling

filter creates notches at the harmonics of the nominal revolution frequency

⇒ particles are forced to circulate at the nominal frequency

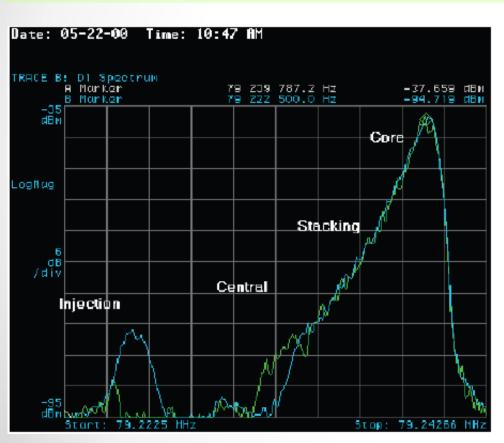
b)





Antiproton Accumulation by Stochastic Cooling

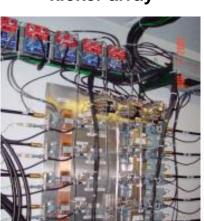
accumulation of 8 GeV antiprotons at accumulator ring, FNAL, shut down 09/2011 a similar facility AC/AA at CERN was shut down 11/1996



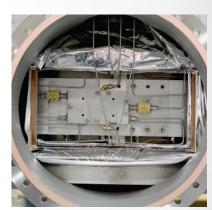
momentum distribution of accumulated antiproton beam



kicker array



microwave electronics



cryogenic microwave amplifier



power amplifiers (TWTs)

Stochastic Cooling of Rare Isotopes at GSI

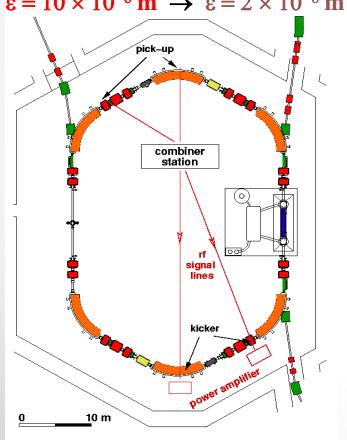
fast pre-cooling of hot fragment beams

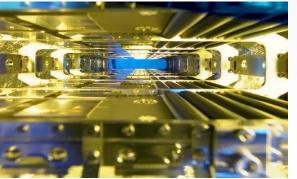
energy 400 (-550) MeV/u

bandwidth 0.8 GHz (range 0.9-1.7 GHz)

$$\delta p/p = \pm 0.35 \% \rightarrow \delta p/p = \pm 0.01 \%$$

 $\epsilon = 10 \times 10^{-6} \text{ m} \rightarrow \epsilon = 2 \times 10^{-6} \text{ m}$





electrodes installed inside magnets



combination of signals from electrodes



power amplifiers for generation of correction kicks

M. Steck (GSI) CAS 2015, Warsaw

Comparison of Cooling Methods

Stochastic Cooling Electron Cooling

Useful for: low intensity beams low energy

all intensities

hot (secondary) beams warm beams (pre-cooled)

high charge high charge

full 3D control bunched beams

Limitations: high intensity beams space charge effects

/problems beam quality limited recombination losses

bunched beams high energy

laser cooling (of incompletely ionized ions) and ionization cooling (of muons) are quite particular and not general cooling methods

Trends in Beam Cooling

Stochastic cooling was mainly developed for the production of high intensity antiproton beams for colliders (CERN, FNAL, 1972 – 2011). It is still in operation at AD (CERN), COSY (FZJ) and ESR (GSI). It will also be used in the FAIR project (Germany) for cooling of antiprotons and rare isotope beams.

Demonstration of bunched beam stochastic cooling (2008) with heavy ions (BNL) and the achievement of increased luminosity made it very attractive for ion colliders.

Now it is proposed for the collider of the Russian NICA project.

Electron cooling was and still is used in low energy storage rings for protons, ions, secondary beams (antiprotons, rare isotopes).

Electron cooling is interesting for low energy storage rings, but also application at higher energies (MeV electron energies) is envisaged after the successful demonstration of the 4 MeV electron cooler at FNAL. Bunched electron beam cooling and coherent electron cooling are in preparation for RHIC (BNL).

Muon (ionization) cooling is still far from implementation in a full scale machine.

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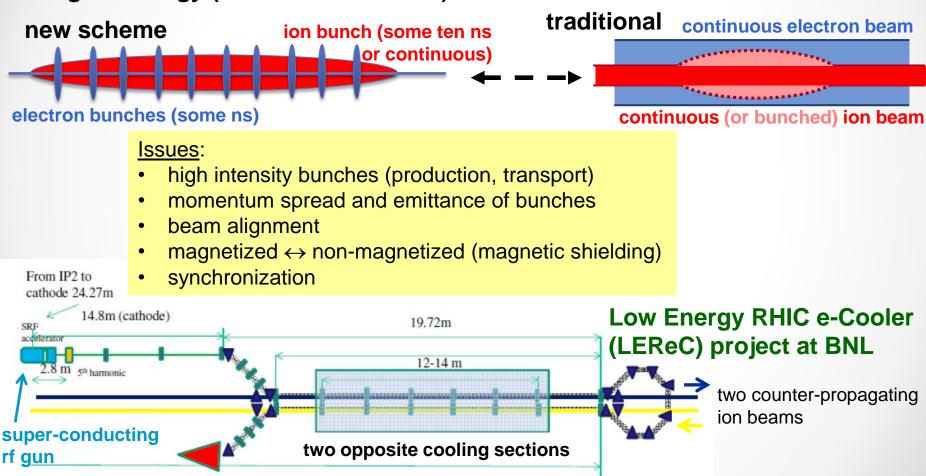
Ionization Cooling:

D. Neuffer, Introduction to Muon Cooling, Nucl. Instr. Meth. A 532 (2004) 26-31

Biannual Workshops on Beam Cooling: e. g. COOL'15, Jefferson Lab, USA

Bunched Beam Electron Cooling

Electron cooling with electrostatic acceleration is limited in energy (5-10 MeV). A bunched electron beam offers the extension of the electron cooling method to higher energy (linear rf accelerator).

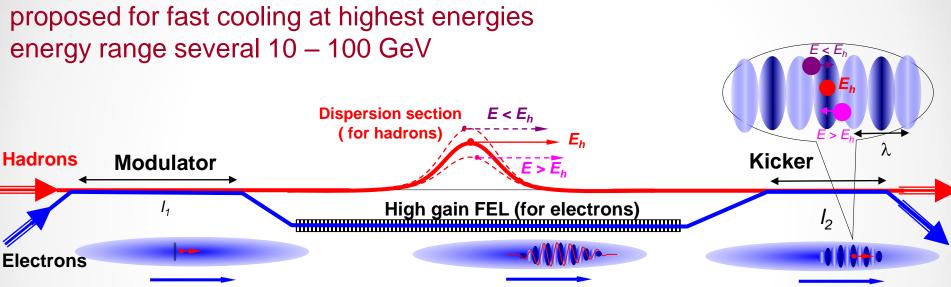


58.804 m from IP2

5 MeV, 250 kW beam dump

Coherent Electron Cooling

A combination of electron and stochastic cooling concepts



The Coherent Electron Cooling system has three major subsystems

modulator: the ions imprint a "density bump" on the electron distribution

• amplifier: FEL interaction amplifies a density bump by orders of magnitude

kicker: the amplified & phase-shifted electron charge distribution is used to correct the velocity offset of the ions