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# Lecture I&II Outline



A. Gallo, Timing and Synchronization I, 2-15 June 2018, Tuusula, Finland

## MOTIVATIONS

Lecture I

- ✓ Why accelerators need synchronization, and at what precision level
- DEFINITIONS AND BASICS
  - ✓ Glossary: Synchronization, Master Oscillator, Drift vs. Jitter
  - ✓ Fourier and Laplace Transforms, Random processes, Phase noise in Oscillators
  - ✓ Phase detectors, Phase Locked Loops, Precision phase noise measurements
  - ✓ Electro-optical and fully optical phase detection

ecture II.

### SYNCRONIZATION ARCHITECTURE AND PERFORMANCES

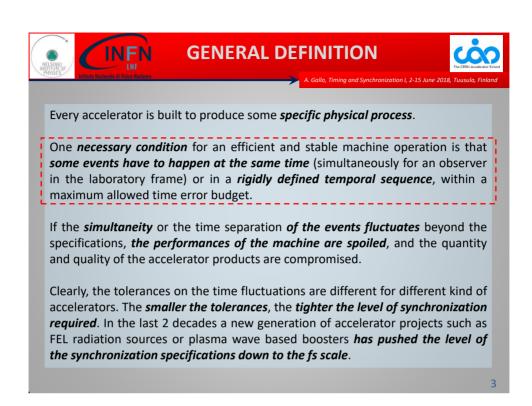
- ✓ Phase lock of synchronization clients (RF systems, Lasers, Diagnostics, ...)
- ✓ Residual absolute and relative phase jitter
- ✓ Reference distribution actively stabilized links

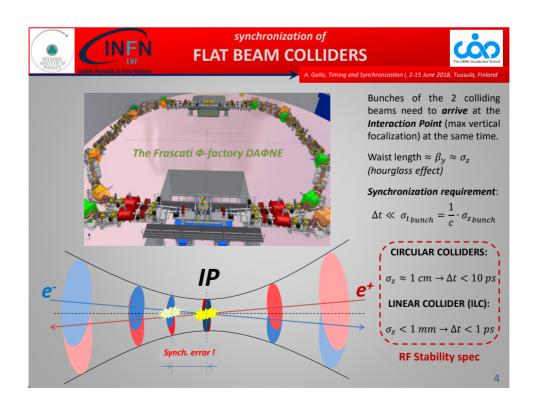
## BEAM ARRIVAL TIME FLUCTUATIONS

- ✓ Bunch arrival time measurement techniques
- Expected bunch arrival time downstream magnetic compressors (an example)
- ✓ Beam synchronization general case

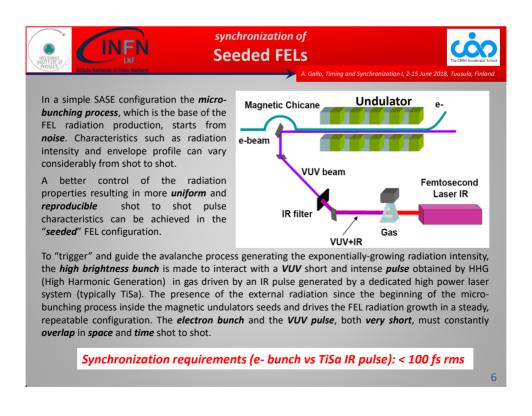
## **CONCLUSIONS AND REFERENCES**

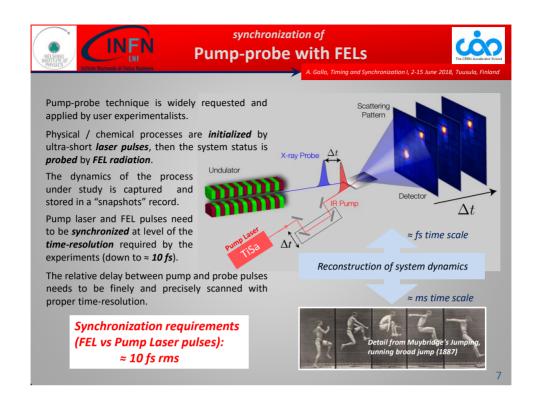
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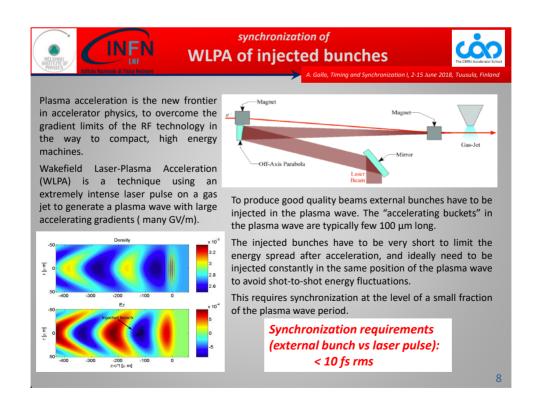


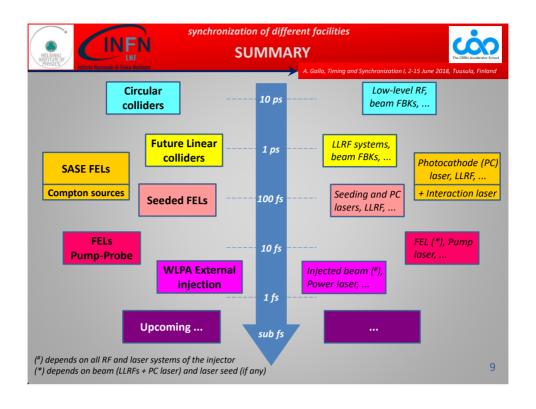




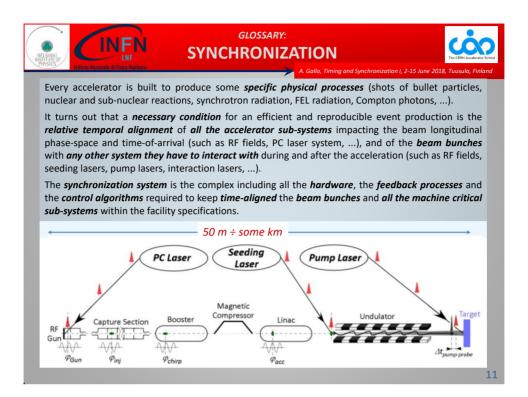


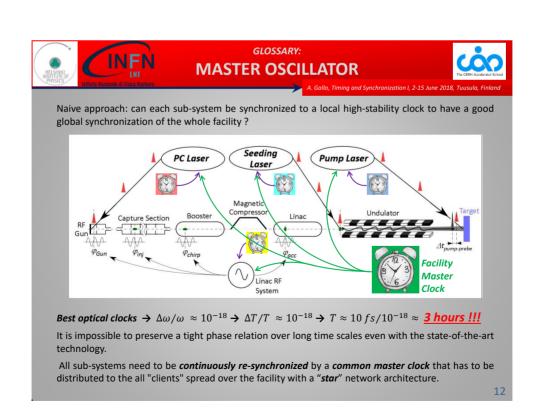


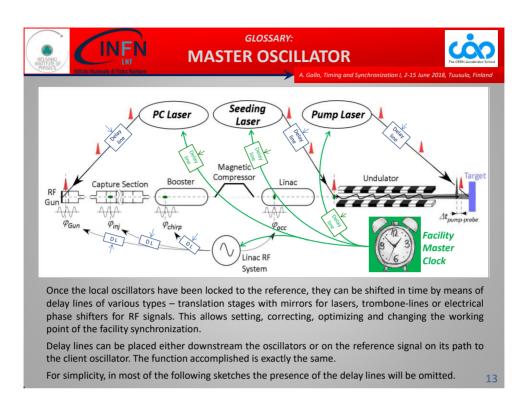




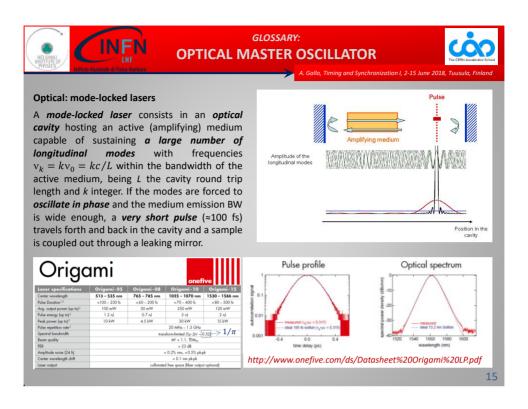


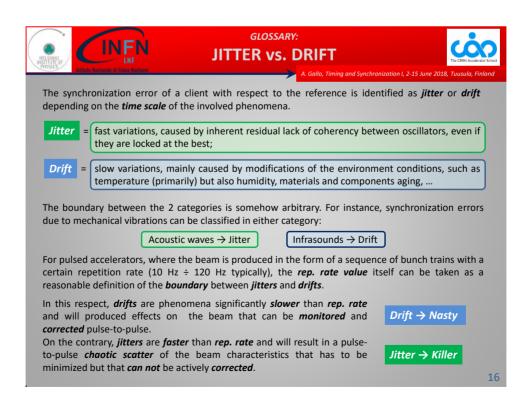


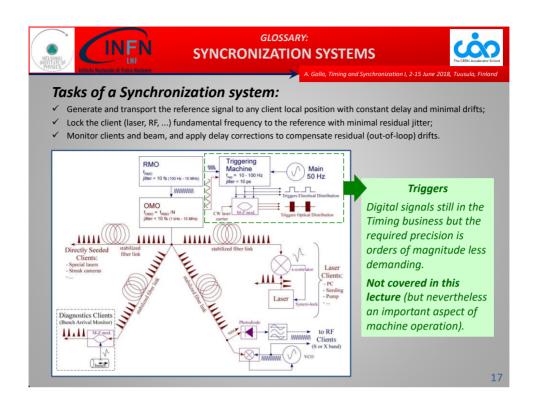


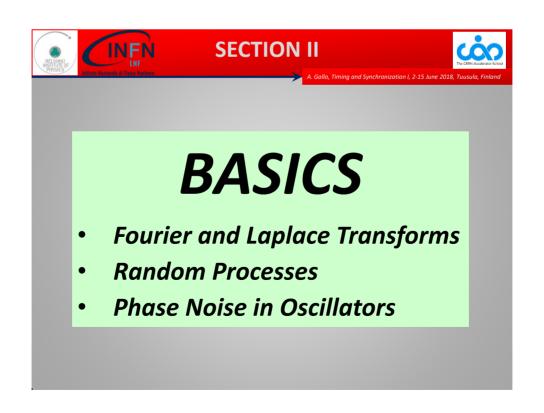


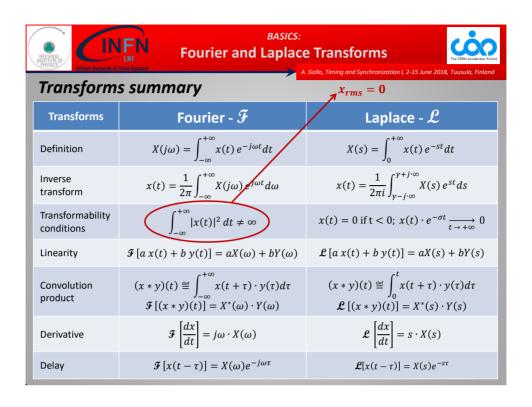


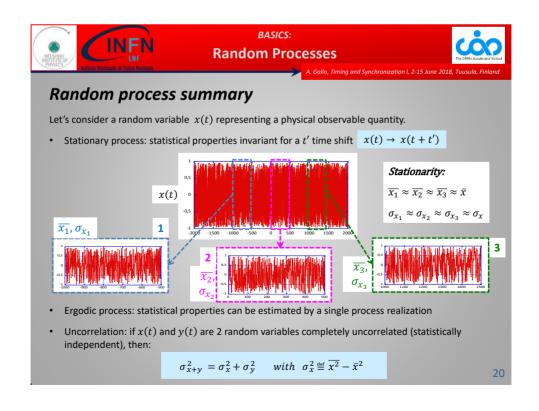


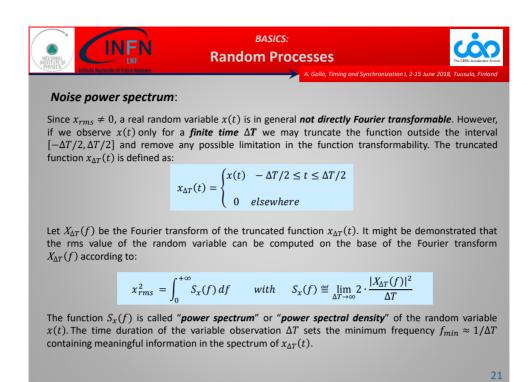


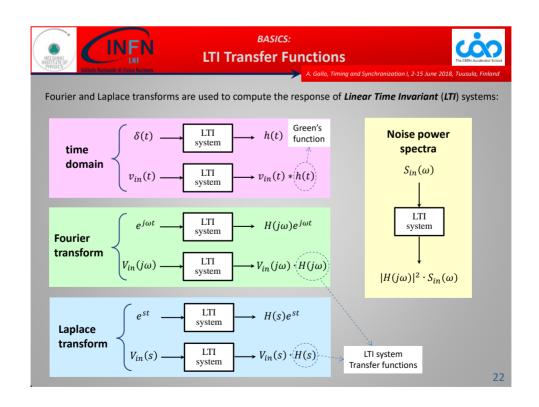


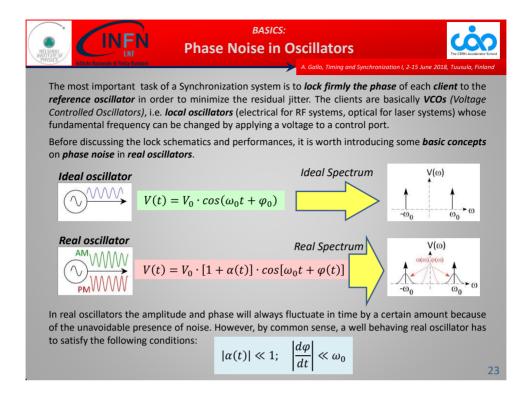


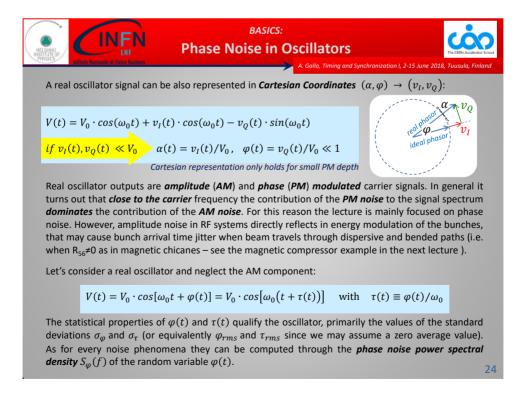








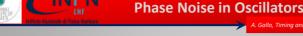






#### BASICS:





Again, for practical reasons, we are only interested in observations of the random variable  $\varphi(t)$  for a finite time  $\Delta T$ . So we may truncate the function outside the interval  $[-\Delta T/2, \Delta T/2]$  to recover the function transformability.

$$arphi_{\Delta T}(t) = egin{cases} arphi(t) & -\Delta T/2 \leq t \leq \Delta T/2 \\ 0 & elsewhere \end{cases}$$

Let  $arPhi_{\Delta T}(f)$  be the Fourier transform of the truncated function  $arphi_{\Delta T}(t)$ . We have:

$$(\varphi_{rms}^2)_{\Delta T} = \int_{f_{min}}^{+\infty} S_{\varphi}(f) df \text{ with } S_{\varphi}(f) \stackrel{\text{def}}{=} 2 \frac{|\Phi_{\Delta T}(f)|^2}{\Delta T}$$

 $S_{\omega}(f)$  is the **phase noise power spectral density**, whose dimensions are  $rad^2/Hz$ .

Again, the time duration of the variable observation  $\Delta T$  sets the minimum frequency  $f_{min} \approx 1/\Delta T$ containing meaningful information on the spectrum  $\Phi_{\Delta T}(f)$  of the phase noise  $\varphi_{\Delta T}(t)$ .

IMPORTANT:

we might still write

$$\varphi_{rms}^2 = \lim_{\Delta T \to \infty} (\varphi_{rms}^2)_{\Delta T} = \int_0^{+\infty} \left( 2 \cdot \lim_{\Delta T \to \infty} \frac{|\varphi_{\Delta T}(f)|^2}{\Delta T} \right) df = \int_0^{+\infty} S_{\varphi}(f) df$$

but we must be aware that in this case  $\phi_{rms}$  is *likely to diverge*. This is physically possible since the power in the carrier does only depend on amplitude and not on phase. In these cases the rms value can better be specified for a given observation time  $\Delta T$  or equivalently for a given frequency range of integration  $[f_1, f_2]$ .



# BASICS:



**Phase Noise in Oscillators** 

We have:

$$\varphi_{rms}^{2} \Big|_{\Delta T} = 2 \cdot \int_{f_{min}}^{+\infty} \mathcal{L}(f) \, df \quad with \quad \mathcal{L}(f) = \begin{cases} \frac{|\Phi_{\Delta T}(f)|^{2}}{\Delta T} & f \ge 0 \\ 0 & f < 0 \end{cases}$$

The function  $\mathcal{L}(f)$  is defined as the "Single Sideband Power Spectral Density" and is called "script-L"

 $\mathcal{L}(f) = \frac{power \ in \ 1 \ Hz \ phase \ modulation \ single \ sideband}{total \ simple \ power} = \frac{1}{2} S_{\varphi}(f) \leftarrow IIIE \ standard \ 1139 - 1999$ total signal power

Linear scale  $\rightarrow \mathcal{L}(f)$  units  $\equiv Hz^{-1}$  or  $rad^2/Hz$ 

Log scale  $\rightarrow \mathbf{10} \cdot \text{Log}[\mathcal{L}(f)]$  units  $\equiv dBc/Hz$ 

## **CONCLUSIONS:**

- ✓ Phase (and time) jitters can be computed from the spectrum of  $\varphi(t)$  through the  $\mathcal{L}(f)$  - or  $S_{\varphi}(f)$  -
- ✓ Computed values depend on the integration range, i.e. on the duration  $\Delta T$  of the observation. Criteria are needed for a proper choice (we will see ...).

