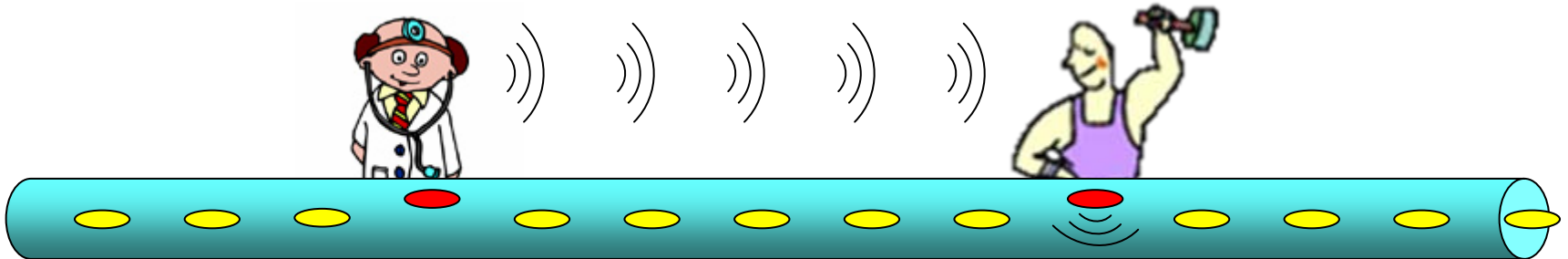


Multi-bunch Feedback Systems

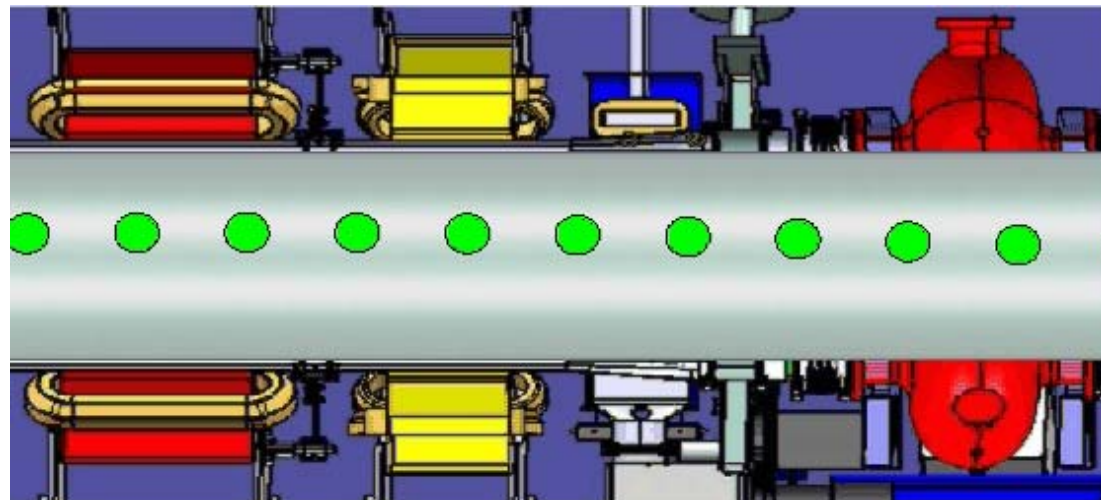
Marco Lonza
Sincrotrone Trieste - Elettra



- Coupled-bunch instabilities
- Basics of feedback systems
- Feedback system components
- Theory of feedback control
- Digital signal processing
- Diagnostics features
- Feedback system setup and optimization
- Effects of multi-bunch feedbacks

Coupled-bunch instabilities at a glance

- Bunched beam in a storage ring
- Transverse (betatron) and longitudinal (synchrotron) oscillations normally damped by natural damping
- Interaction of the electromagnetic field with metallic surroundings (wake fields)
- Wake fields act back on the beam and produces growth of oscillations
- If the growth rate is stronger than the natural damping the oscillation gets unstable



Example: interaction with an RF cavity can excite its Higher Order Modes (HOM)

Bunch

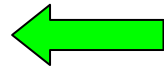
"Zoomed" beam pipe

Objective of storage ring based particle accelerators

High brightness in synchrotron light sources
 High luminosity in high energy physics experiments



High currents
 Many bunches



Storage of intense particle beams



The interaction of these beams with the surrounding metallic structures gives rise to collective effects called "coupled-bunch instabilities"



Large amplitude instabilities can cause beam loss

- Limitation of the stored current to low values

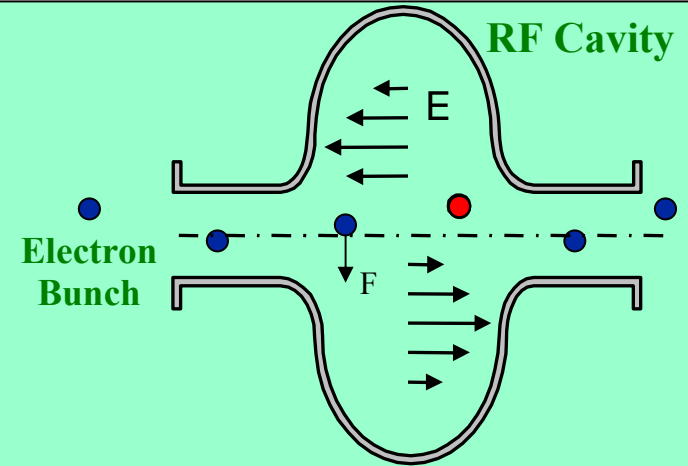
If the growth of instability saturates, the beam may stay in the ring

- Large instabilities degrade the beam quality: brightness or luminosity

Sources of instabilities

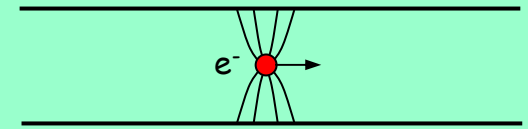
Cavity High Order Modes (HOM)

High Q spurious resonances excited by the beam act back on the beam itself
 Each bunch affects the following bunches through the wake fields excited in the cavity
 The cavity HOM can couple with a beam oscillation mode at the same frequency and give rise to an instability



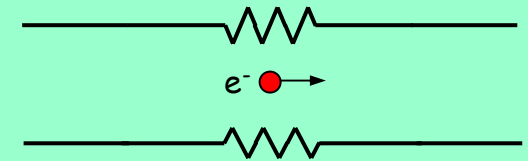
Resistive wall impedance

Interaction of the beam with the vacuum chamber (skin effect)
 Particularly strong in low-gap chambers and in-vacuum insertion devices (undulators and wigglers)



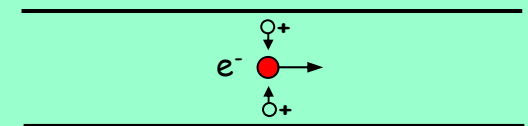
Interaction of the beam with other objects

Discontinuities in the vacuum chamber, small cavity-like structures, ...
 Ex. BPMs, vacuum pumps, bellows, ...



Ion instabilities

Gas molecules ionized by electron beam
 Positive ions remains trapped in the negative electric potential
 Produce electron-ion coherent oscillations



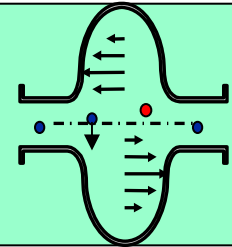
Passive cures

Cavity High Order Modes (HOM)

Thorough design of the RF cavity

Mode dampers with antennas and resistive loads

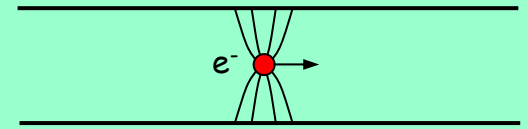
Tuning of HOMs frequencies through plungers or changing the cavity temperature



Resistive wall impedance

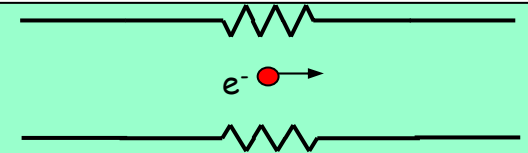
Usage of low resistivity materials for the vacuum pipe

Optimization of vacuum chamber geometry



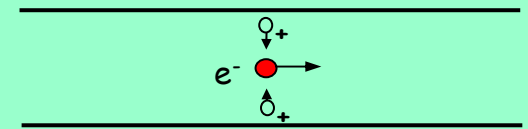
Interaction of the beam with other objects

Proper design of the vacuum chamber and of the various installed objects



Ion instabilities

Ion cleaning with a gap in the bunch train



Landau damping by increasing the tune spread

Higher harmonic RF cavity (bunch lengthening)

Modulation of the RF

Octupole magnets (transverse)

Active Feedbacks

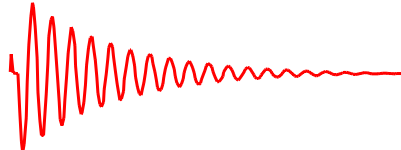
"X" is the oscillation coordinate (longitudinal or transverse displacement)

Natural damping

Betatron/Synchrotron frequency:
tune \times revolution frequency ω_0

$$\ddot{x}(t) + 2D \dot{x}(t) + \omega^2 x(t) = 0$$

If $\omega \gg D$, an approximated solution of the differential equation is a damped sinusoidal oscillation:

$$x(t) = e^{-\frac{t}{\tau_D}} \sin(\omega t + \varphi)$$


where $\tau_D = 1/D$ is the "damping time constant" (D is called "damping rate")

Externally excited uncorrelated oscillations (ex. quantum excitation) are damped by natural damping (synchrotron radiation damping or Landau damping). The **oscillation** of the individual particles is **uncorrelated** and shows up as an emittance growth

Coherent Bunch Oscillation

Coupling with other bunches through the interaction with surrounding metallic structures add a "driving force" term $F(t)$. The oscillation of individual particles becomes correlated and the centroid of the bunch oscillates giving rise to **coherent bunch oscillations** (coupled bunch)

Equation of motion of one bunch: $\ddot{x}(t) + 2D \dot{x}(t) + \omega^2 x(t) = F(t)$

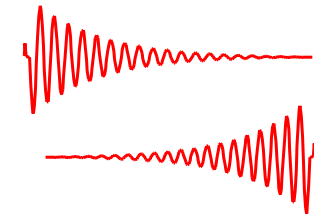
If the driving force is sinusoidal with frequency ω and the amplitude is proportional to the bunch oscillation amplitude, the equation becomes:

$$\ddot{x}(t) + 2(D - G)\dot{x}(t) + \omega^2 x(t) = 0$$

where $\tau_G = 1/G$ is the "growth time constant" (G is called "growth rate")

If $D > G$ the oscillation amplitude decays exponentially

If $D < G$ the oscillation amplitude grows exponentially



as: $x(t) = e^{-\frac{t}{\tau}} \sin(\omega t + \varphi)$ where $\frac{1}{\tau} = \frac{1}{\tau_D} - \frac{1}{\tau_G}$

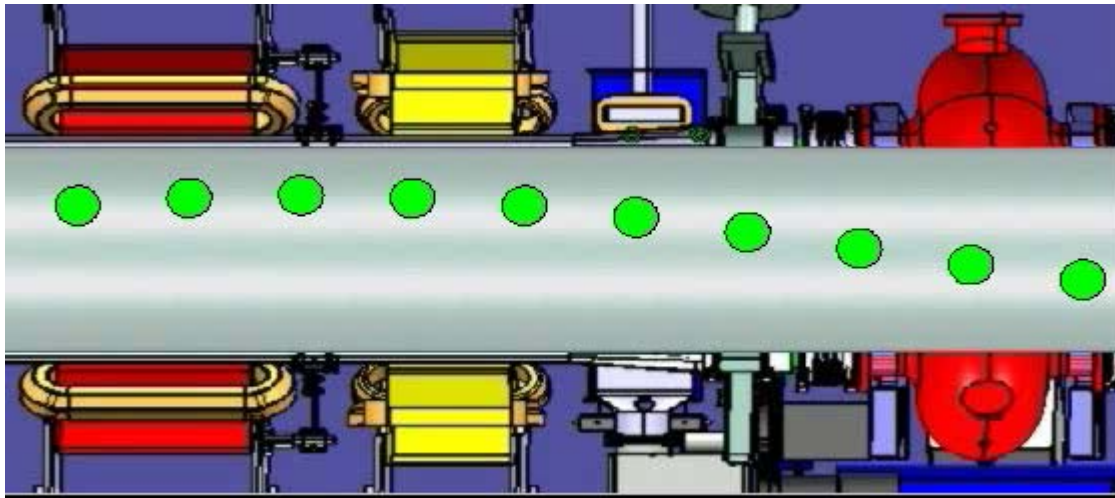
Since G is proportional to the beam current I_b , if I_b is lower than a given threshold I_{th} the coupled bunch oscillation does not show up, if higher a coupled bunch oscillation arises

Feedback Action

Feedback systems act on the beam by adding a damping term D_{fb} to the equation of motion

$$\ddot{x}(t) + 2(D - G + D_{fb}) \dot{x}(t) + \omega^2 x(t) = 0 \quad \text{Such that } D - G + D_{fb} > 0$$

The feedback is made of a sensor called **detector** and an actuator called **kicker**

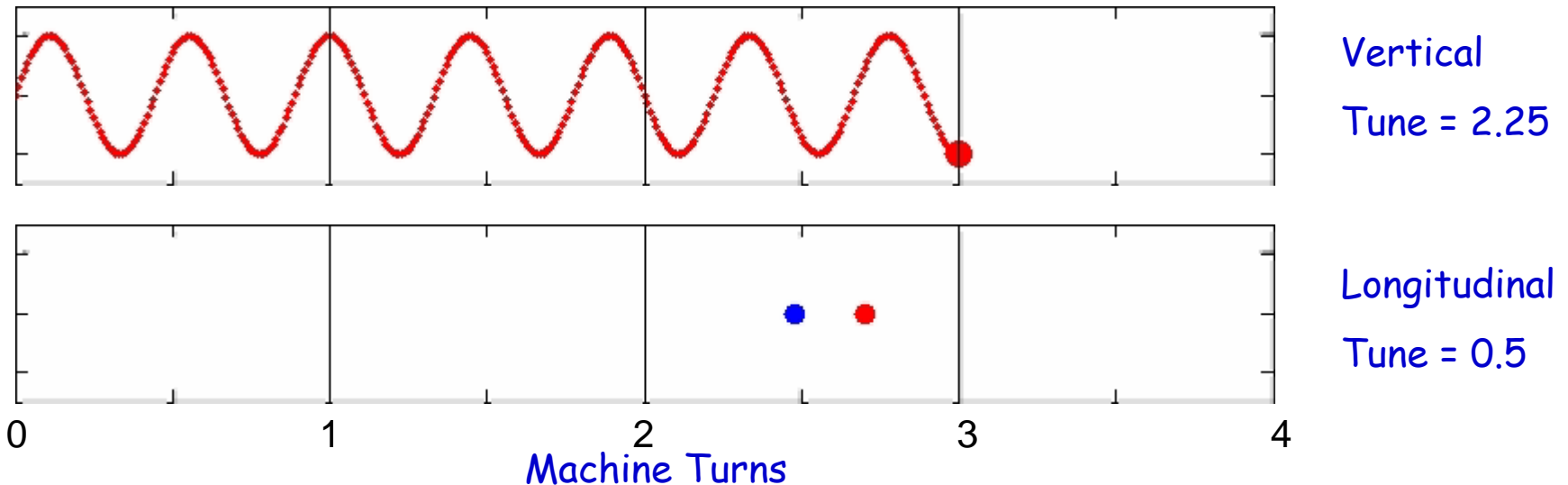


In order to add damping, the feedback must provide a kick proportional to the derivative of the bunch oscillation

Since the oscillation is sinusoidal, the kick signal for each bunch is generated by shifting by $\pi/2$ the oscillation signal of the same bunch when it passes through the kicker

Multi-bunch modes

Typically, transverse oscillation frequencies (horizontal and vertical) are higher than the revolution frequency, while the longitudinal frequency is lower than the revolution frequency



Although each bunch oscillates at the tune frequency, there can be different modes of oscillation, called **multi-bunch modes** depending on how each bunch oscillates with respect to the others

Multi-bunch modes

M bunches equally spaced around the ring

Each multi-bunch mode is characterized by a bunch-to-bunch phase difference of:

$$\Delta\Phi = m \frac{2\pi}{M} \quad m = \text{multi-bunch mode number } (0, 1, \dots, M-1)$$

Each multi-bunch mode is associated to a characteristic set of frequencies:

$$\omega = pM\omega_0 \pm (m+\nu)\omega_0$$

Where:

p is an integer number $-\infty < p < \infty$

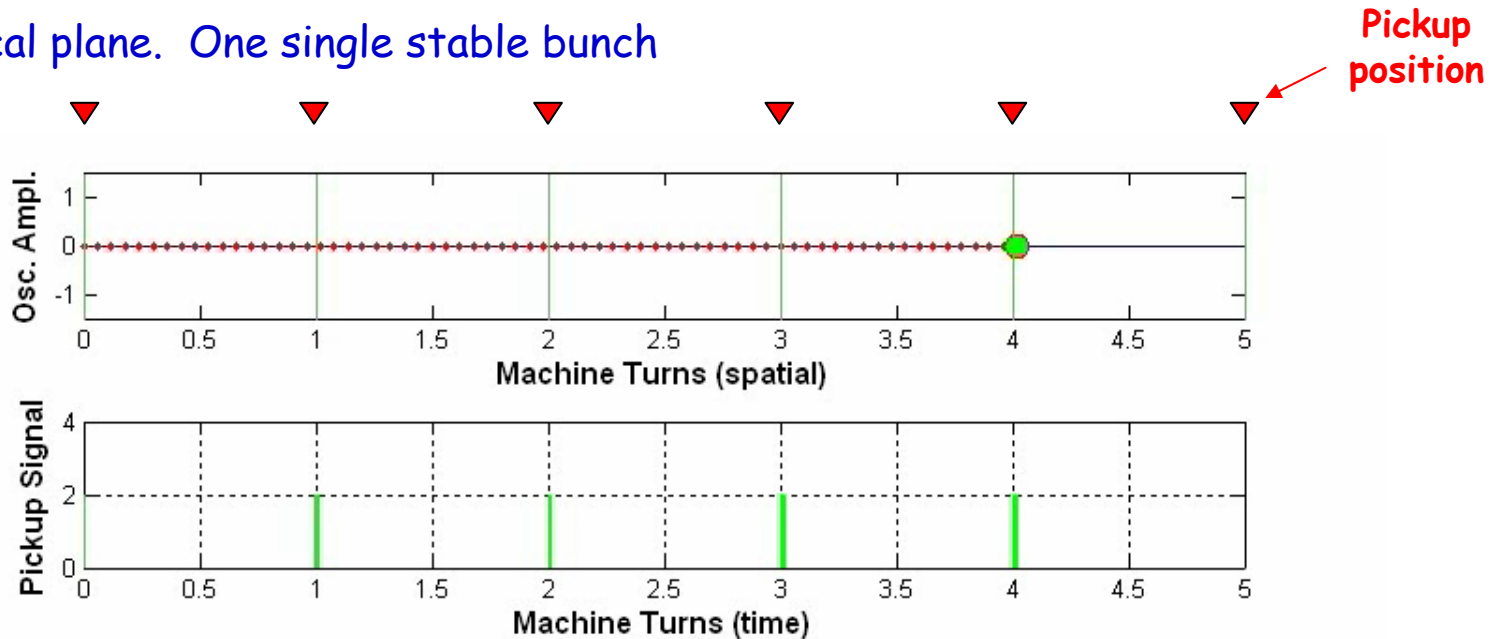
ω_0 is the **revolution frequency**: $M\omega_0$ is the RF frequency (bunch repetition freq.)

ν is the **tune**

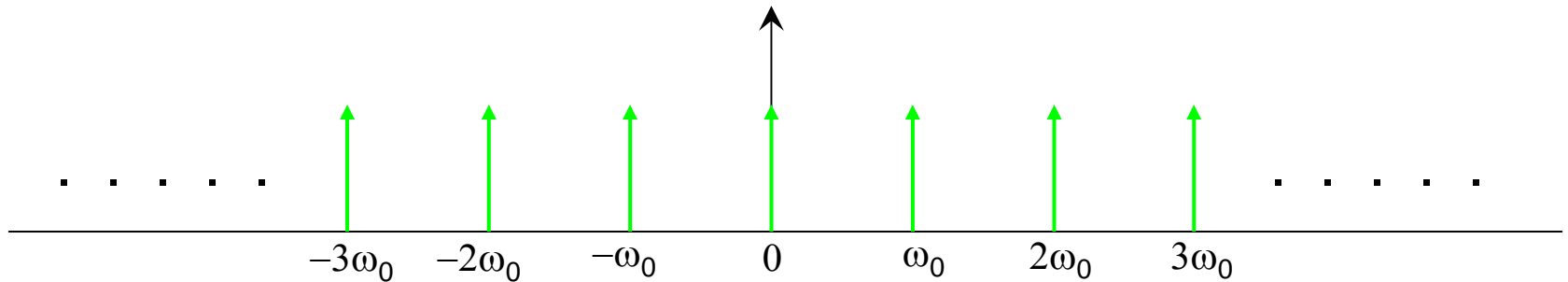
Two sidebands at $\pm(m+\nu)\omega_0$ for each multiple of the RF frequency

Multi-bunch modes: example1

Vertical plane. One single stable bunch

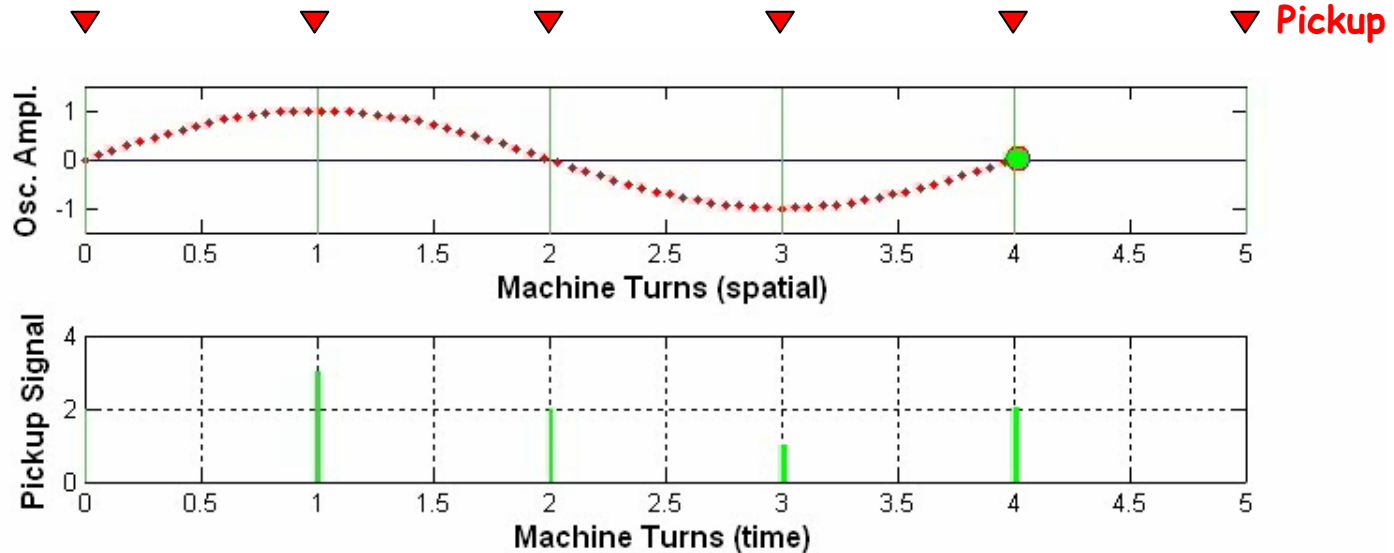


Every time the bunch passes through a pickup (∇) placed at coordinate 0 a pulse is generated. If we think it as a Dirac impulse, the spectrum is a repetition of frequency lines at multiple of the revolution frequency: $p\omega_0$ for $-\infty < p < \infty$

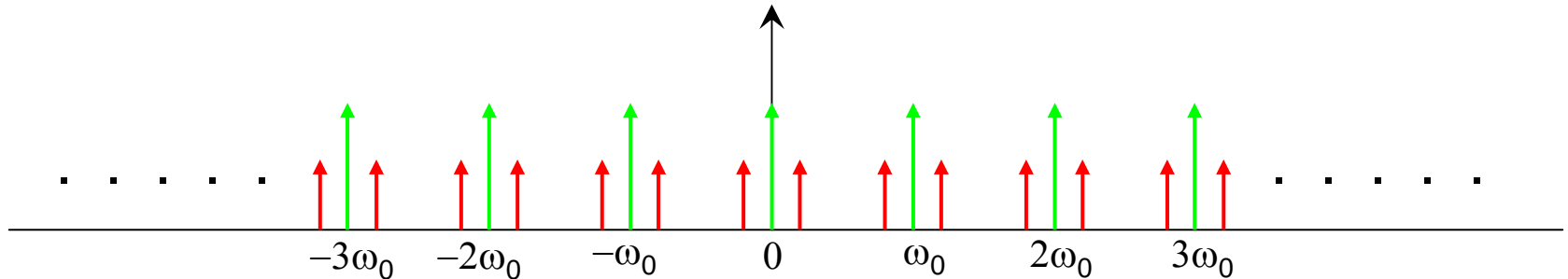


Multi-bunch modes: example2

One single bunch oscillating at the tune frequency $\nu\omega_0$: for simplicity we consider a vertical tune $\nu < 1$, ex. $\nu = 0.25$. $M = 1 \rightarrow$ only mode #0 exists

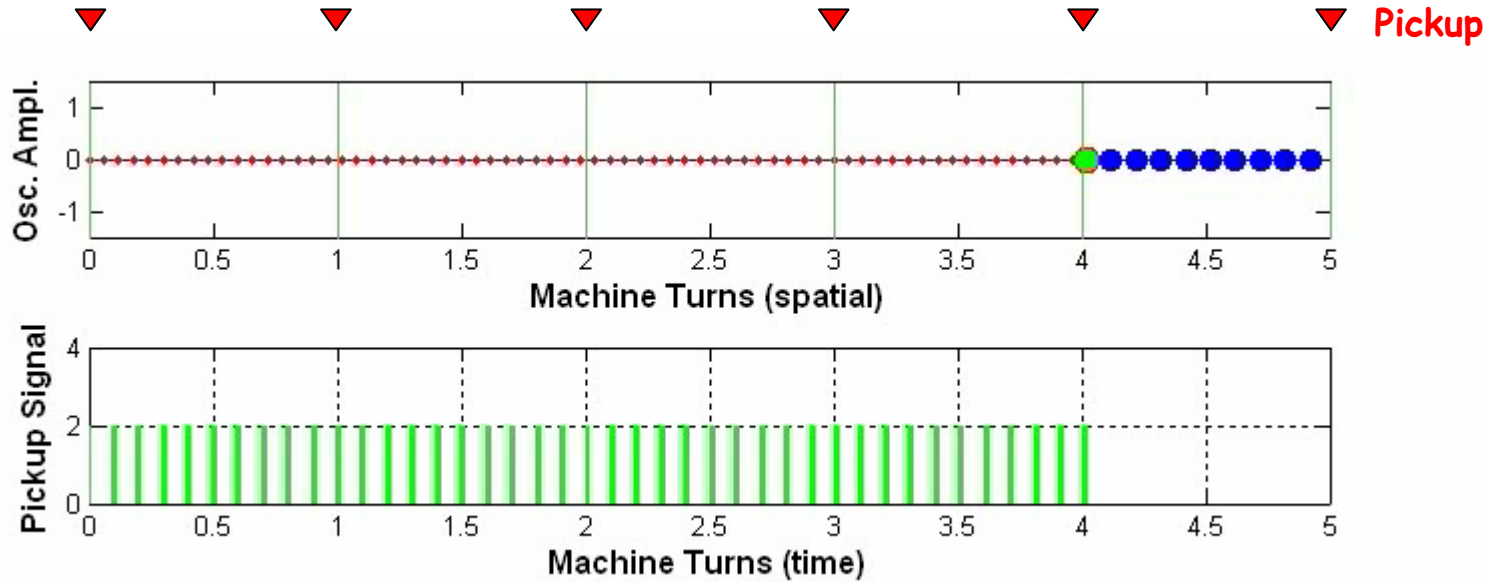


The Dirac impulse is modulated in amplitude with frequency $\nu\omega_0$
 Two sidebands at $\pm\nu\omega_0$ appear at each of the spectrum frequency lines

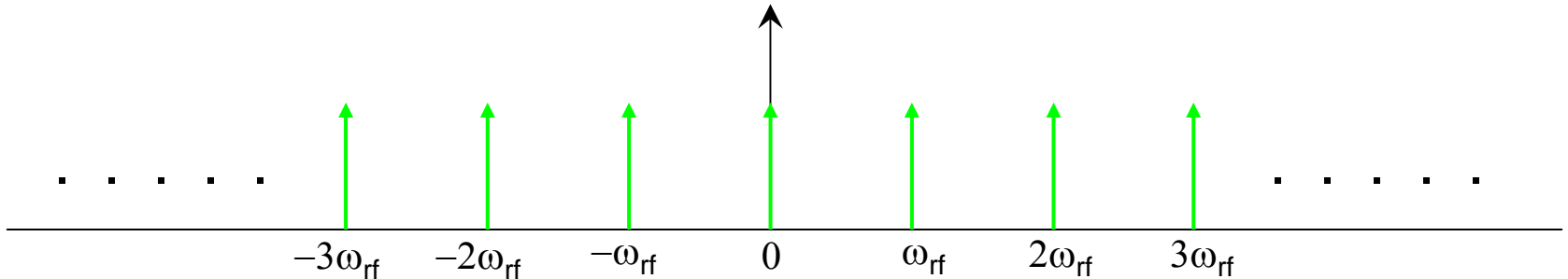


Multi-bunch modes: example3

Ten identical equally-spaced stable bunches filling all the ring buckets



The spectrum is a repetition of frequency lines at multiples of the bunch repetition frequency:
 $\omega_{rf} = 10 \omega_0$ (RF frequency)



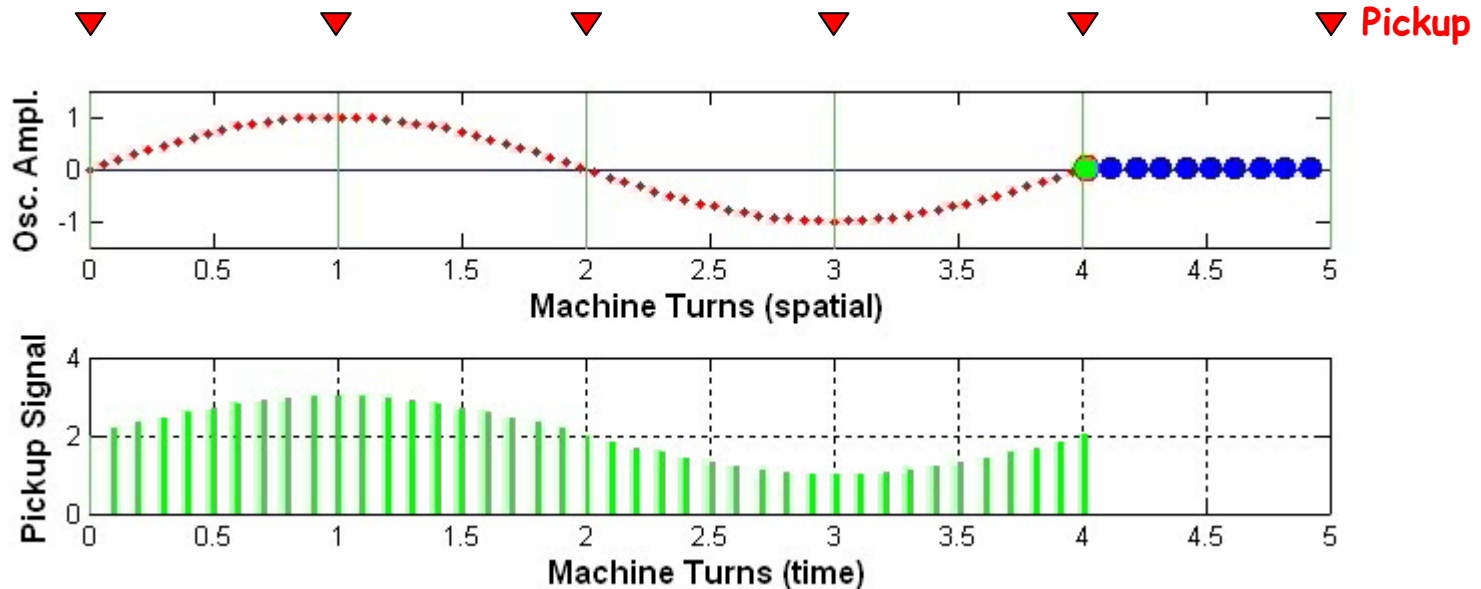
Multi-bunch modes: example4

10 identical equally-spaced bunches oscillating at the tune frequency $\omega\nu$ ($\nu = 0.25$)

$M = 10 \rightarrow$ there are 10 possible modes of oscillation

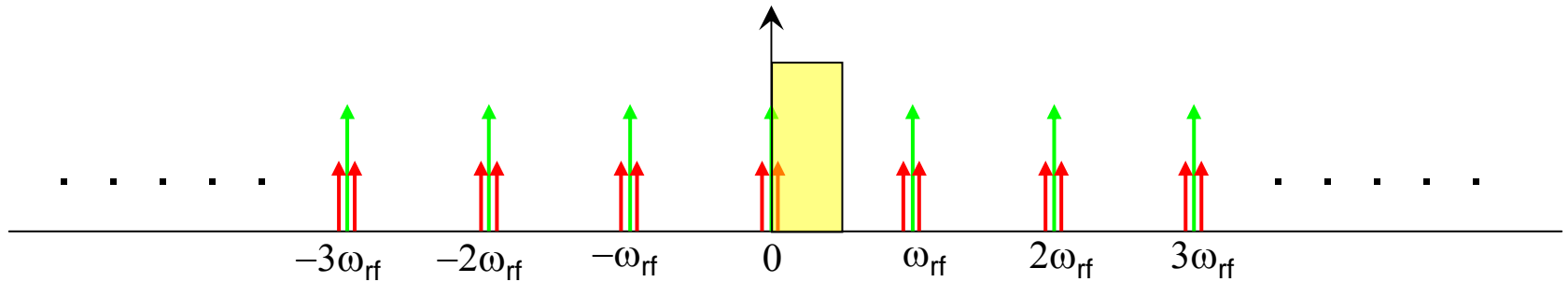
$$\Delta\Phi = m \frac{2\pi}{M}$$

Ex.: mode #0 ($m = 0$) $\Delta\Phi=0$ i.e. all bunches oscillate with the same phase

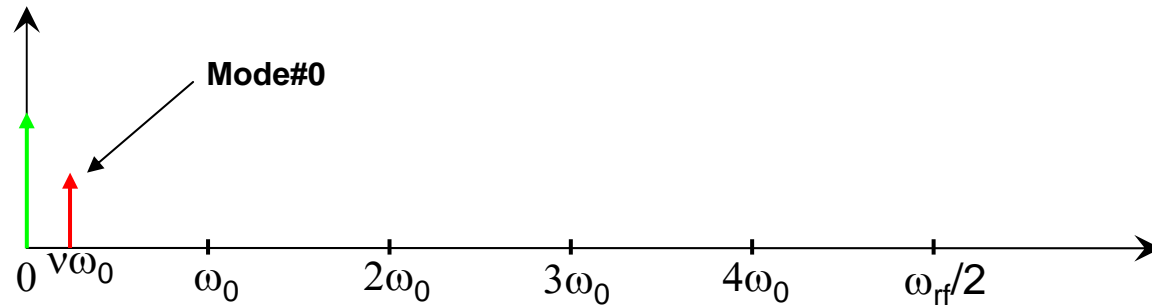


Multi-bunch modes: example4

The spectrum is a repetition of frequency lines at multiples of the bunch repetition frequency, modulated in amplitude with frequency $\nu\omega_0$. Sidebands at $\pm\nu\omega_0$ appear at each of the spectrum frequency lines:

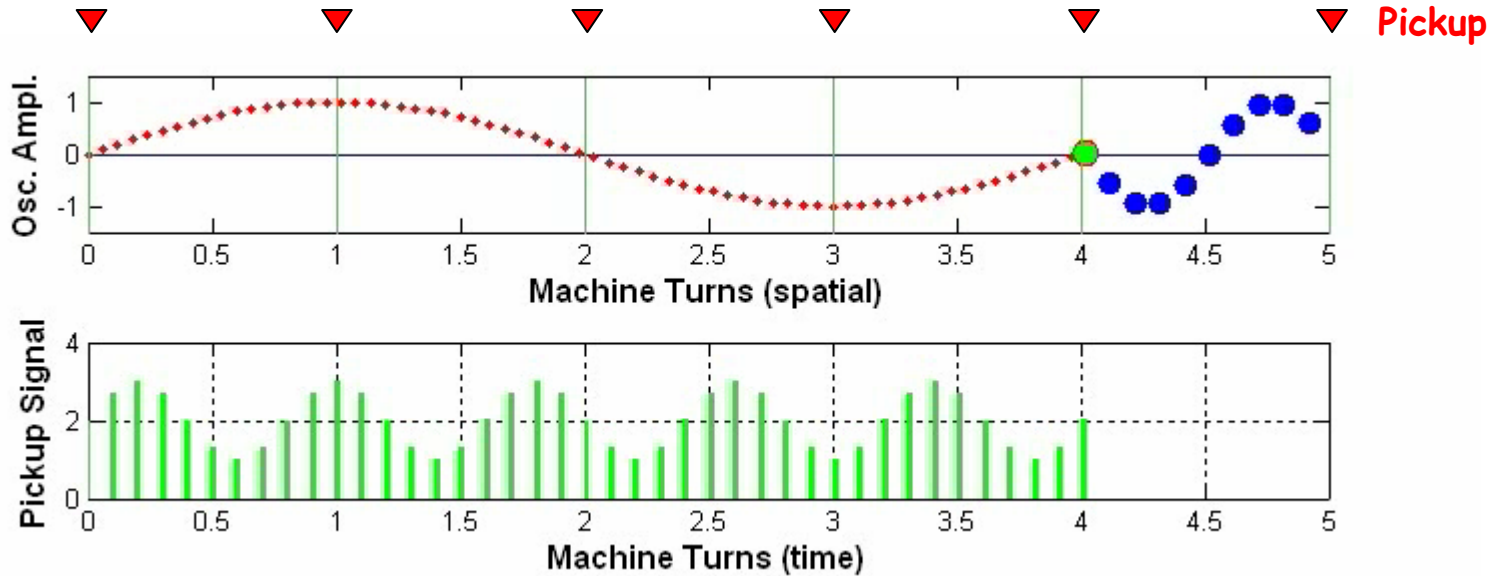
$$\omega = p\omega_{rf} \pm \nu\omega_0 \quad -\infty < p < \infty \quad (\nu = 0.25)$$


Since the spectrum is periodic and each mode appears twice (upper and lower side band) in a $M\omega_0$ frequency span, we can limit the spectrum analysis to a $M\omega_0/2$ frequency range

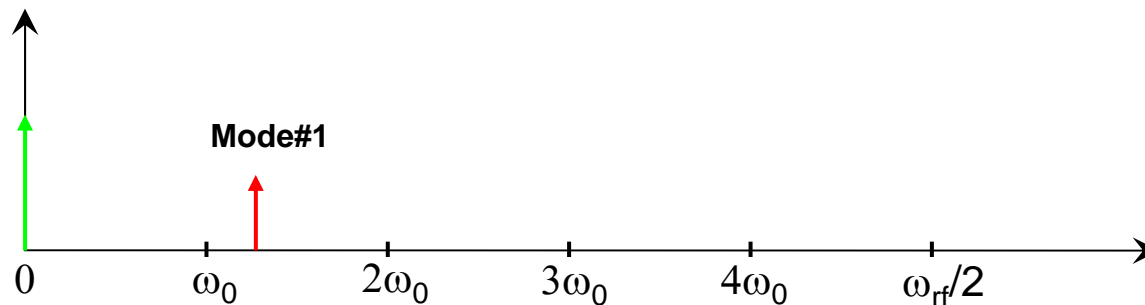


Multi-bunch modes: example5

Ex.: mode #1 ($m = 1$) $\Delta\Phi = 2\pi/10$ ($\nu = 0.25$)

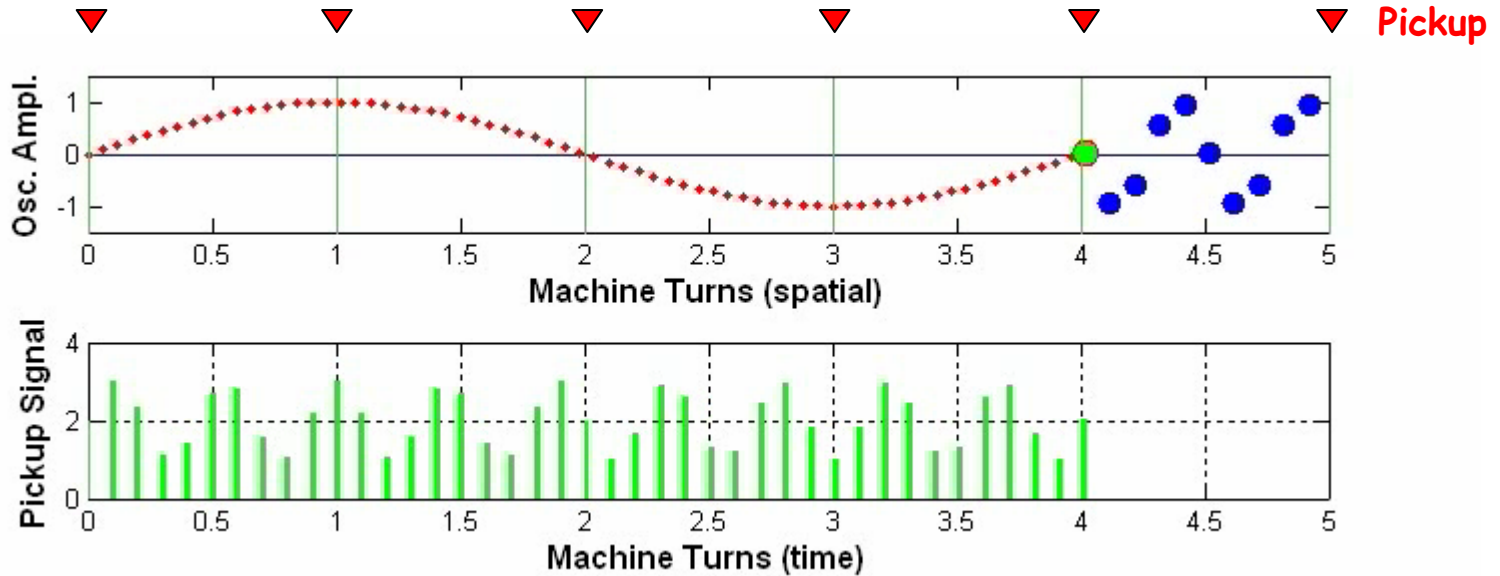


$$\omega = p\omega_{rf} \pm (\nu+1)\omega_0 \quad -\infty < p < \infty$$

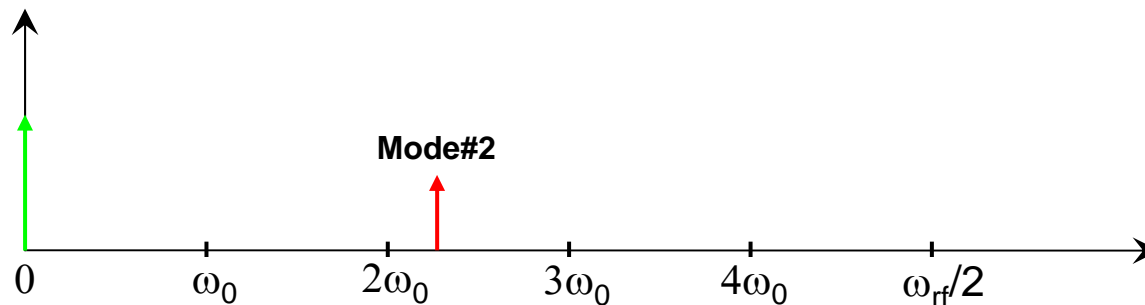


Multi-bunch modes: example 6

Ex.: mode #2 ($m = 2$) $\Delta\Phi = 4\pi/10$ ($\nu = 0.25$)

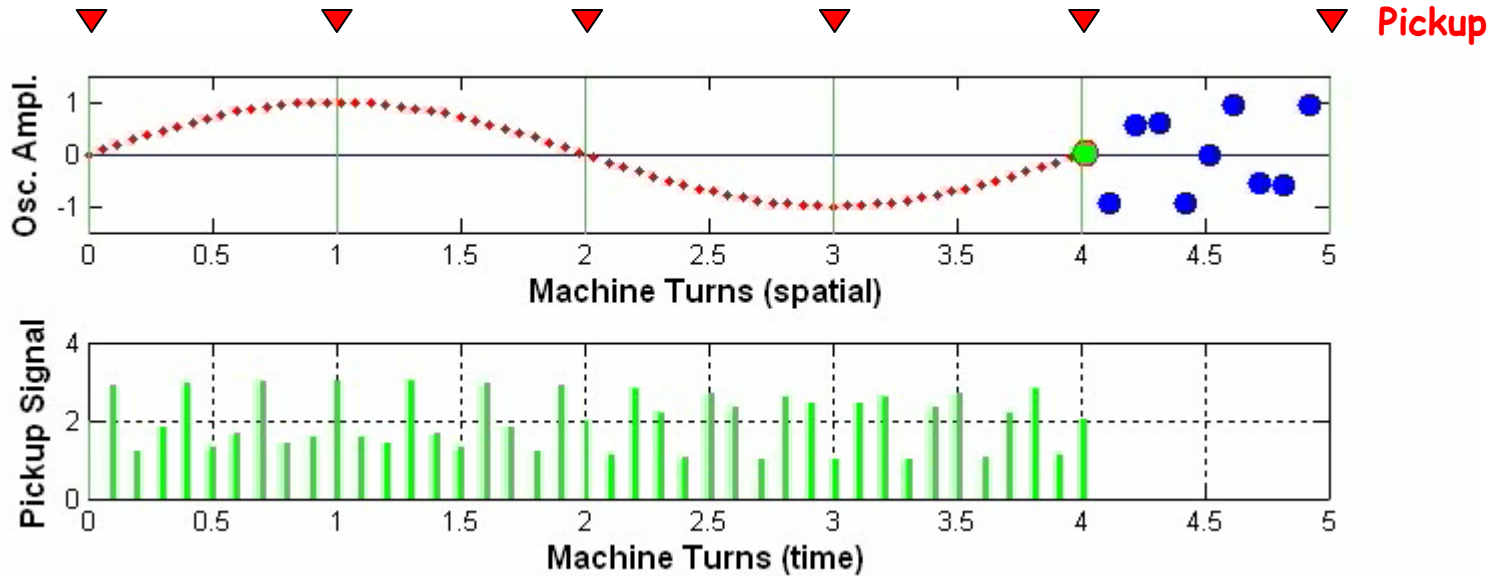


$$\omega = p\omega_{rf} \pm (\nu+2)\omega_0 \quad -\infty < p < \infty$$

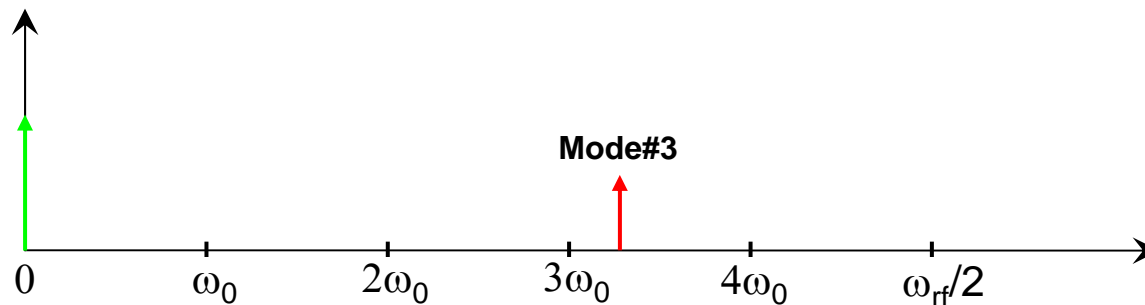


Multi-bunch modes: example7

Ex.: mode #3 ($m = 3$) $\Delta\Phi = 6\pi/10$ ($\nu = 0.25$)

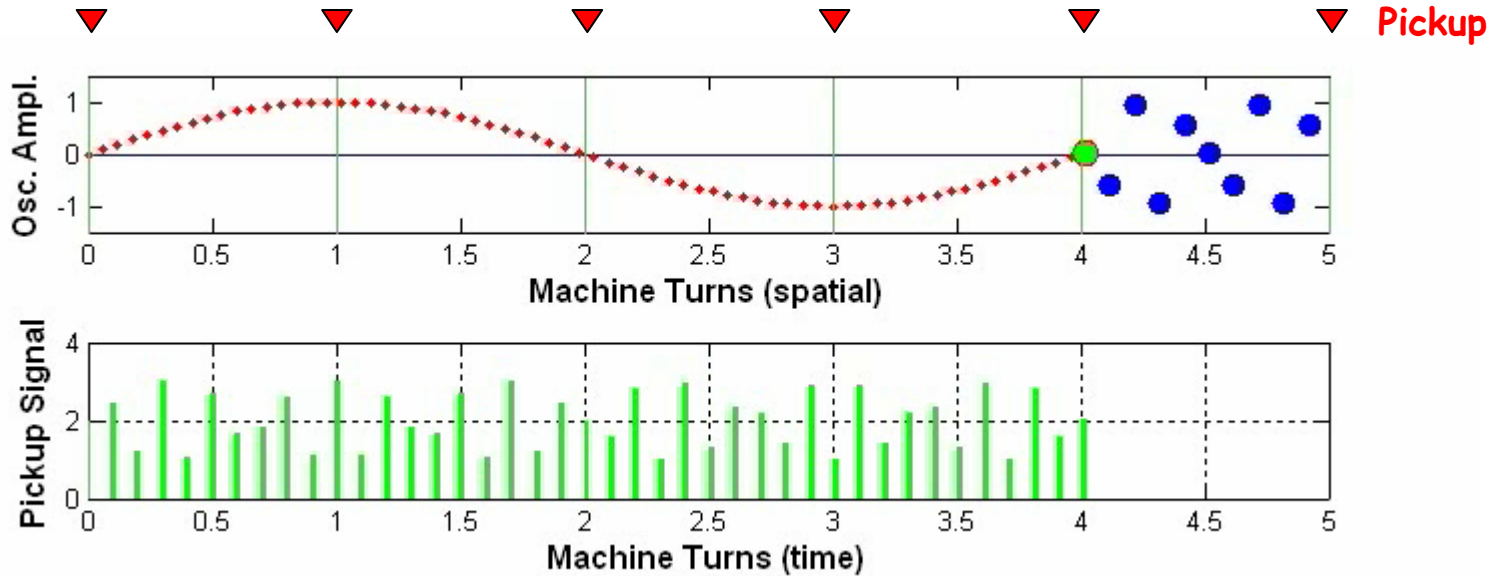


$$\omega = p\omega_{rf} \pm (\nu+3)\omega_0 \quad -\infty < p < \infty$$

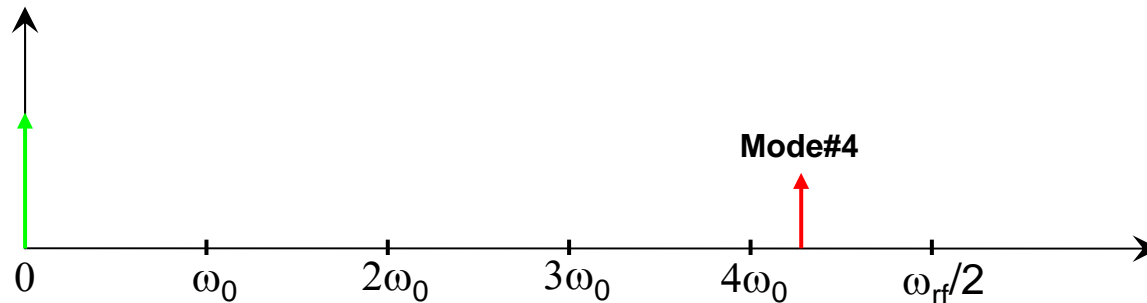


Multi-bunch modes: example8

Ex.: mode #4 ($m = 4$) $\Delta\Phi = 8\pi/10$ ($\nu = 0.25$)

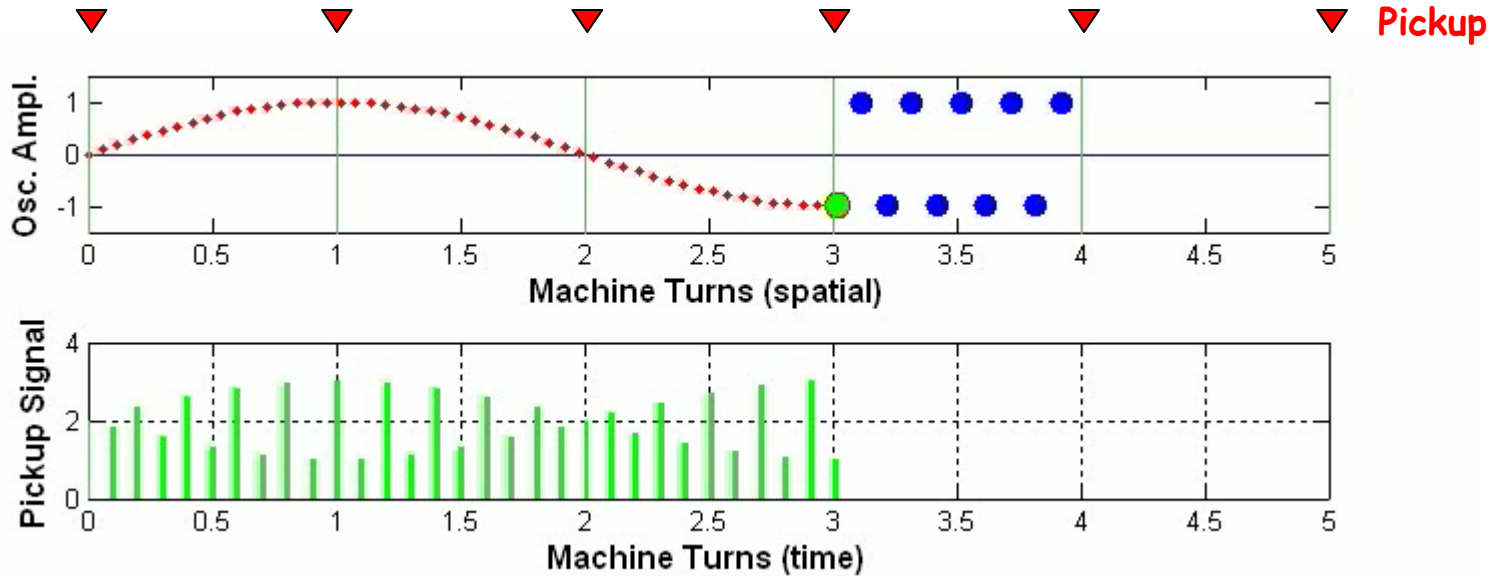


$$\omega = p\omega_{rf} \pm (\nu+4)\omega_0 \quad -\infty < p < \infty$$

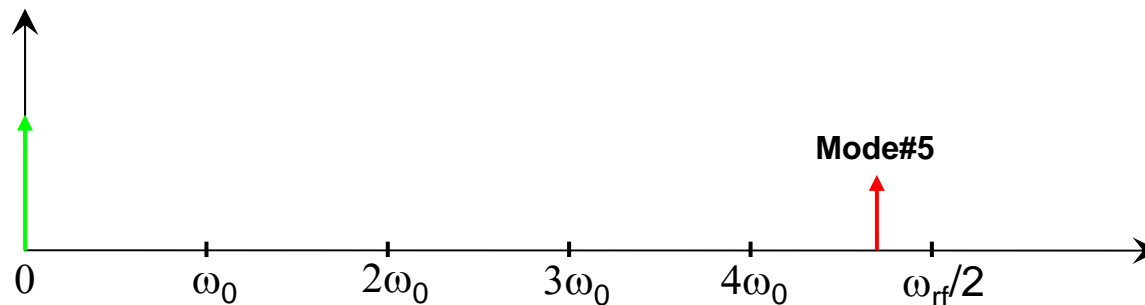


Multi-bunch modes: example9

Ex.: mode #5 ($m = 5$) $\Delta\Phi = \pi$ ($\nu = 0.25$)

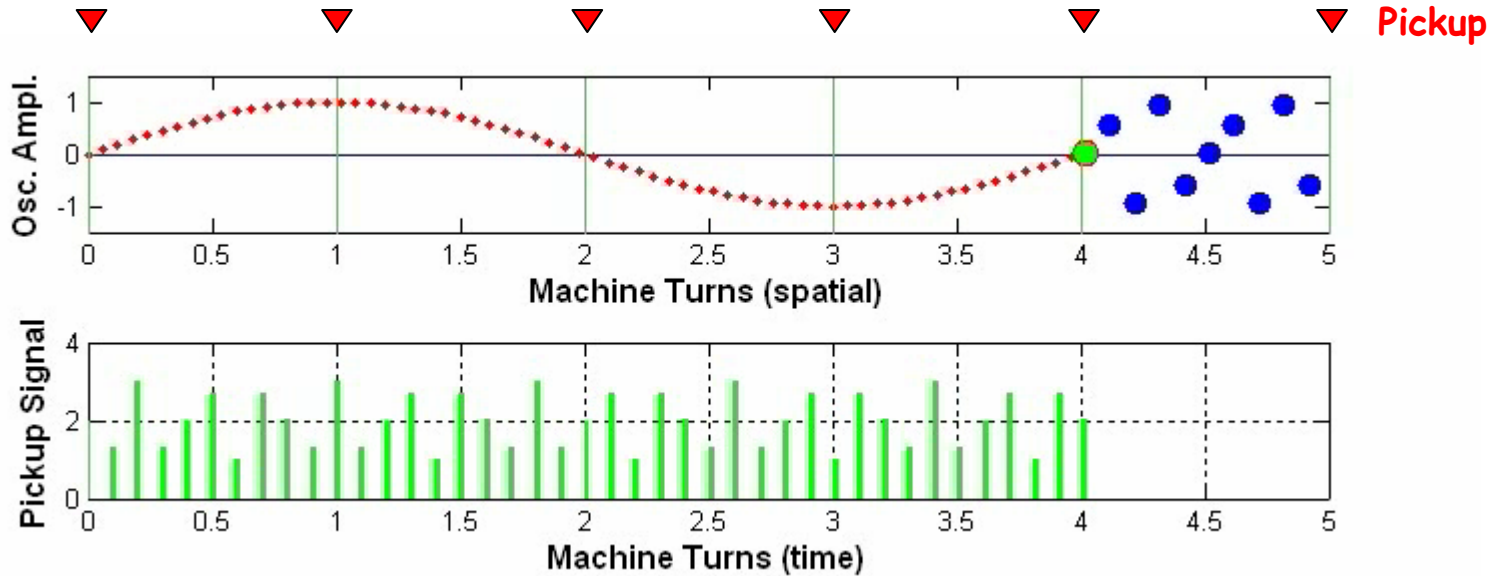


$$\omega = p\omega_{rf} \pm (\nu+5)\omega_0 \quad -\infty < p < \infty$$

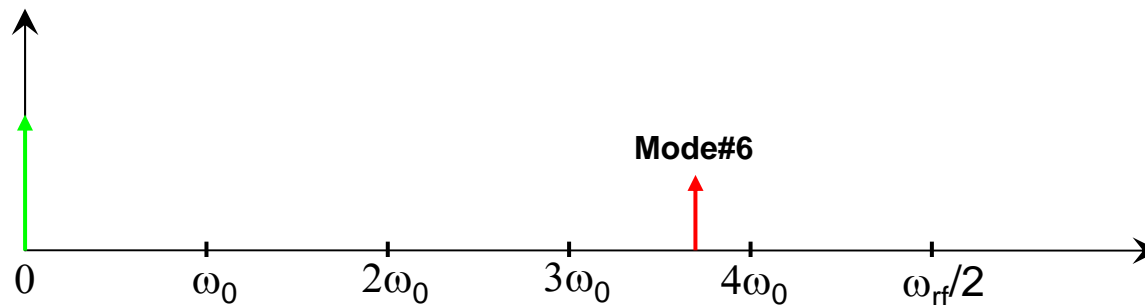


Multi-bunch modes: example10

Ex.: mode #6 ($m = 6$) $\Delta\Phi = 12\pi/10$ ($\nu = 0.25$)

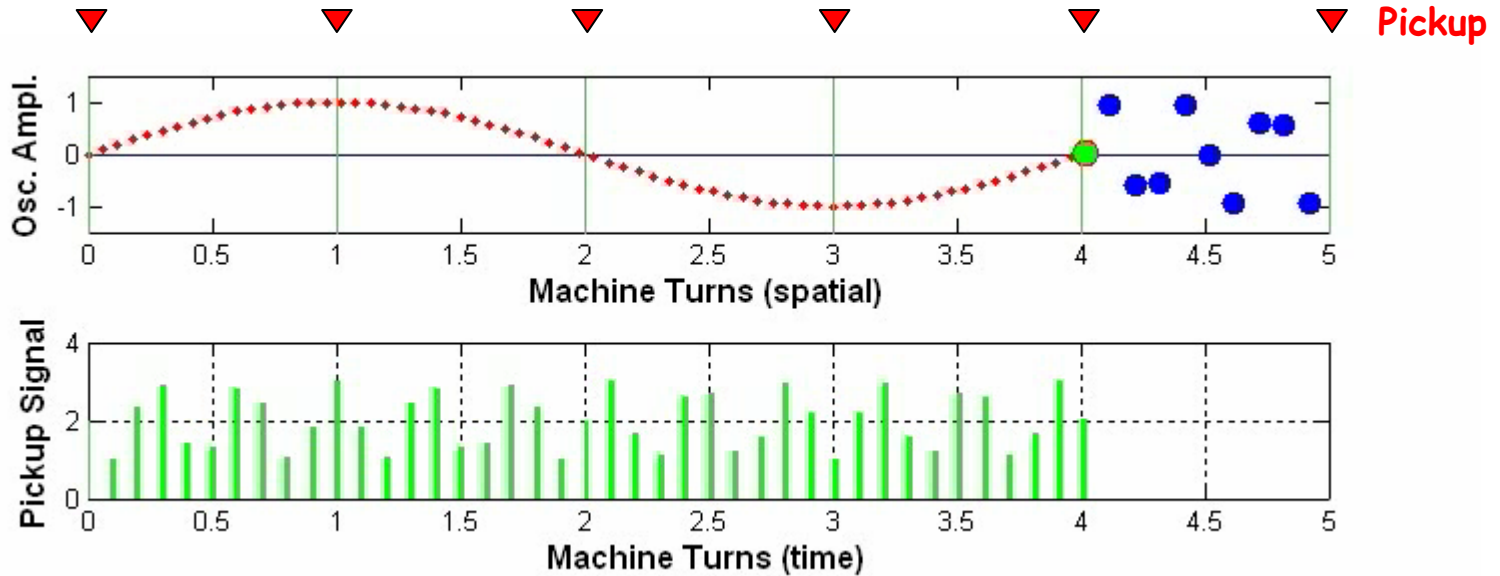


$$\omega = p\omega_{rf} \pm (\nu+6)\omega_0 \quad -\infty < p < \infty$$

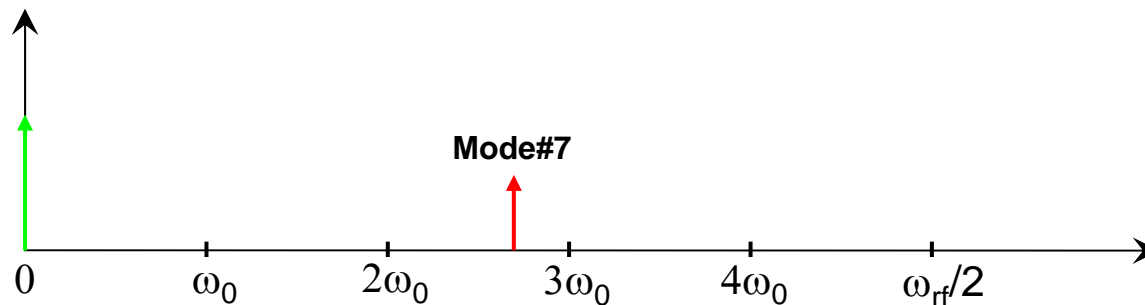


Multi-bunch modes: example11

Ex.: mode #7 ($m = 7$) $\Delta\Phi = 14\pi/10$ ($\nu = 0.25$)

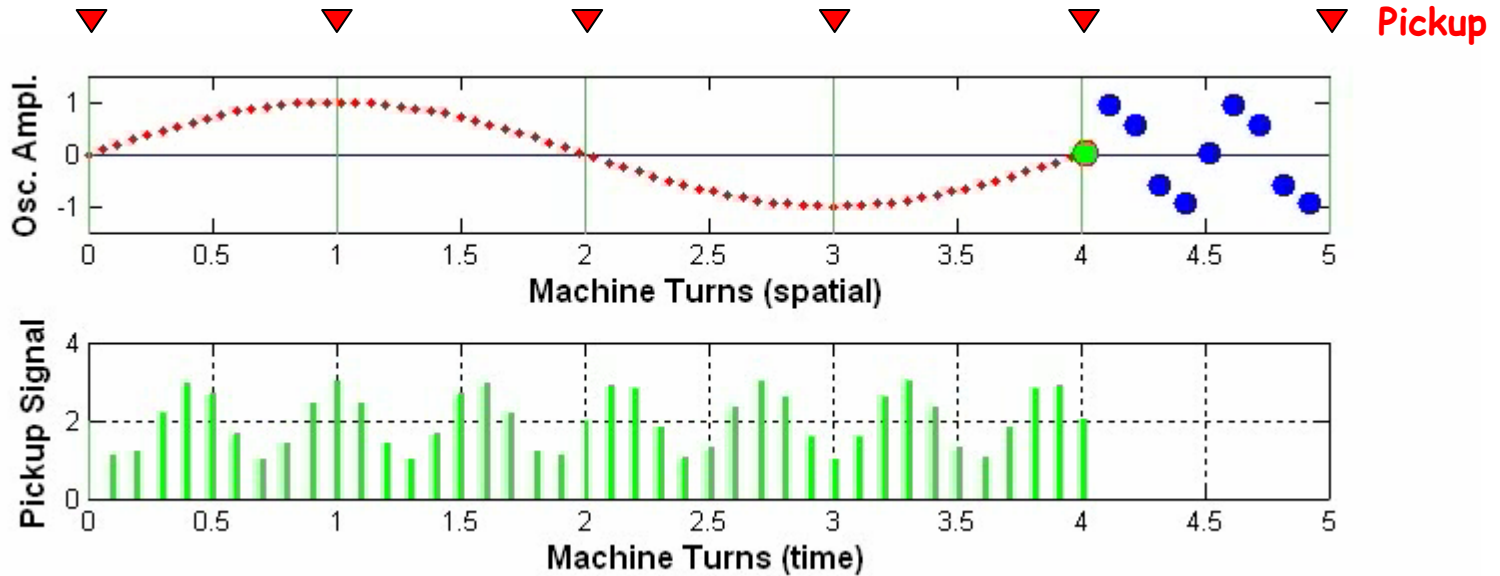


$$\omega = p\omega_{rf} \pm (\nu+7)\omega_0 \quad -\infty < p < \infty$$

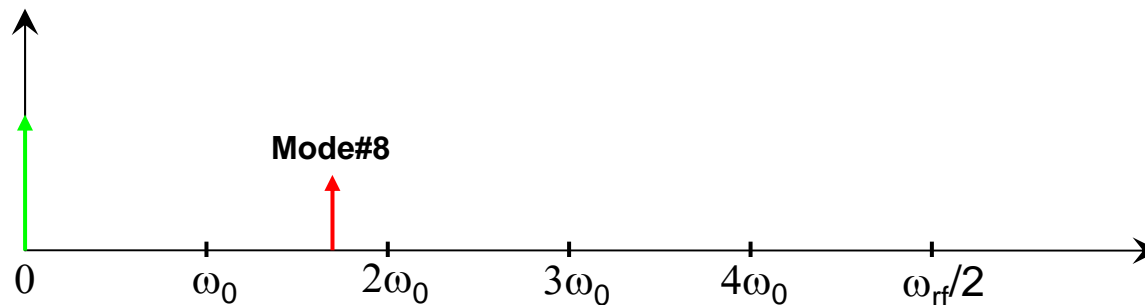


Multi-bunch modes: example12

Ex.: mode #8 ($m = 8$) $\Delta\Phi = 16\pi/10$ ($\nu = 0.25$)

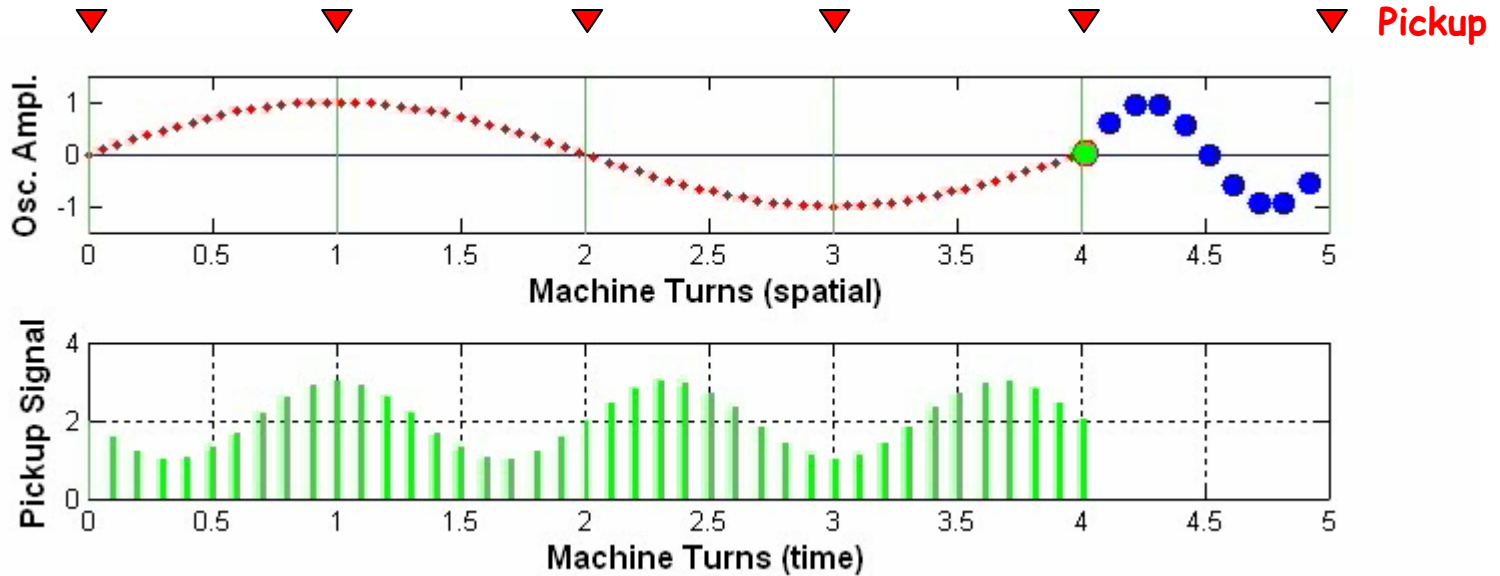


$$\omega = p\omega_{rf} \pm (\nu+8)\omega_0 \quad -\infty < p < \infty$$

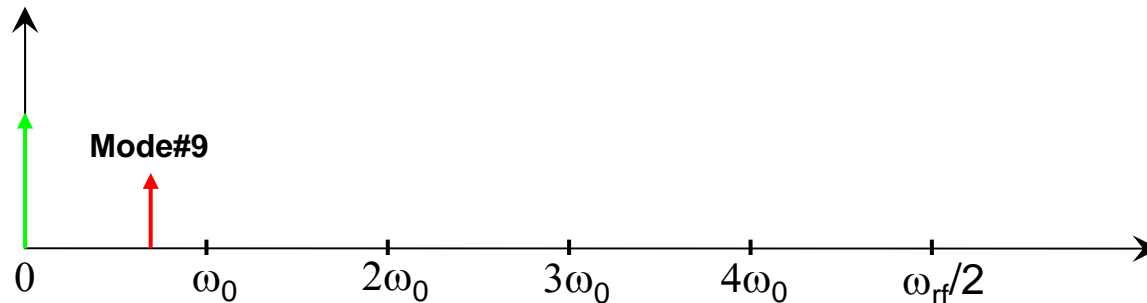


Multi-bunch modes: example13

Ex.: mode #9 ($m = 9$) $\Delta\Phi = 18\pi/10$ ($\nu = 0.25$)



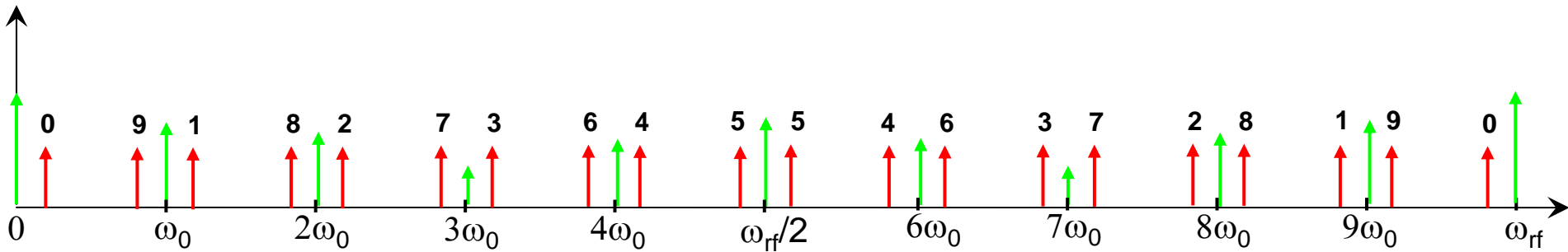
$$\omega = p\omega_{rf} \pm (\nu+9)\omega_0 \quad -\infty < p < \infty$$



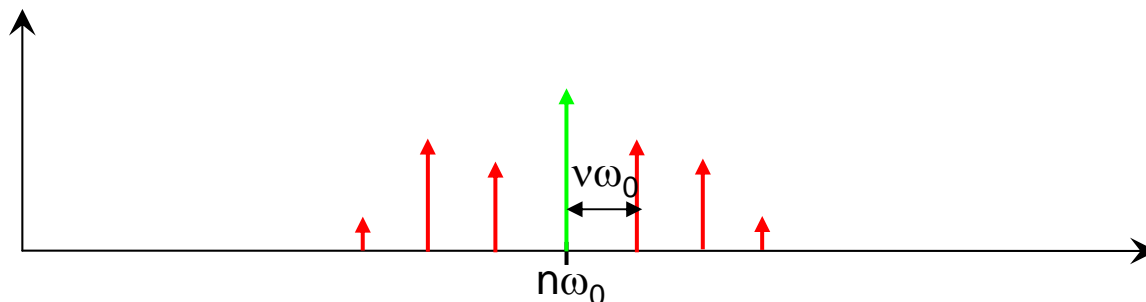
Multi-bunch modes: uneven filling and longitudinal modes

Any $\omega_{rf}/2$ portion of the beam spectrum contains the information of all potential modes and can be used to detect the presence of an instability and measure its amplitude

If the bunches have **not the same charge**, i.e. the buckets are not equally filled (uneven filling), the spectrum also has frequency **components at the revolution harmonics** (multiples of ω_0). The amplitude of each revolution harmonic depends on the filling pattern of one machine turn



In case of **longitudinal modes**, we have a **phase modulation** of the stable beam spectrum. Components at $\pm v\omega_0, \pm 2v\omega_0, \pm 3v\omega_0, \dots$ can appear aside the revolution harmonics. Their amplitude depends on the depth of the phase modulation (Bessel series)

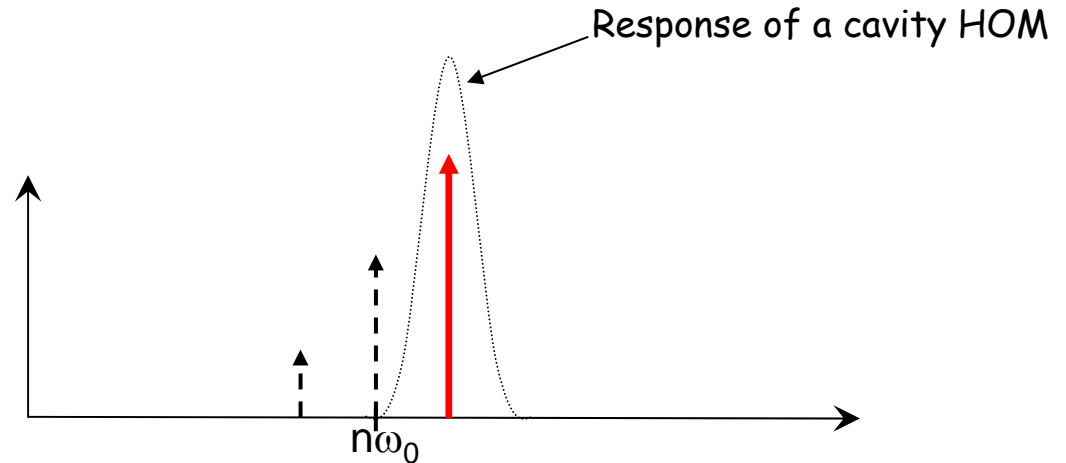


Multi-bunch modes: coupled-bunch instability

The resonance of a metallic structure surrounding the beam (ex. RF cavity) can couple with a multi-bunch mode and give rise to a **coupled-bunch instability** that increases the amplitude of the spectral line corresponding to that mode



Synchrotron Radiation Profile Monitor (SRPM) showing the transverse beam shape



Effects of coupled-bunch modes:

- ☹ increase of the beam dimensions
- ☹ increase of the effective emittance
- ☹ risk of beam loss
- ☺ increase of lifetime due to decreased Touschek scattering (more diluted bunches)

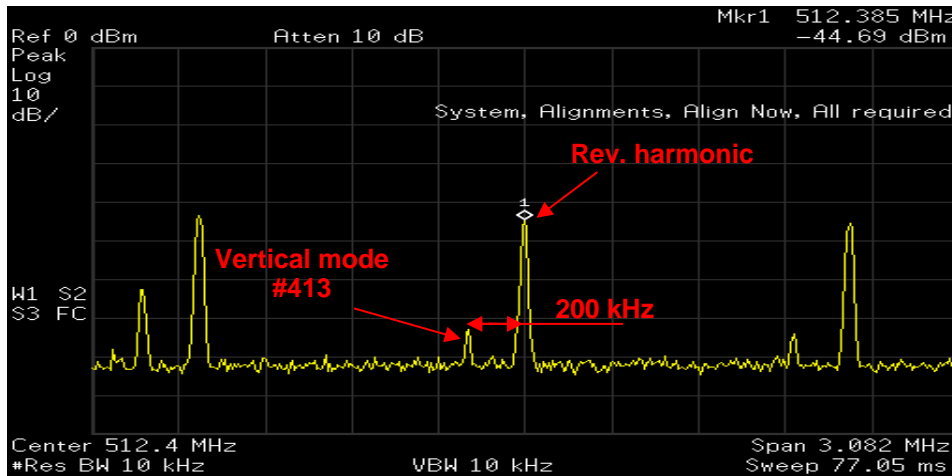
Real example: Elettra synchrotron light source

$f_{rf} = 499.654$ MHz, 432 bunches, bunch spacing ≈ 2 ns, $f_0 = 1.15$ MHz

$V_{hor} = 12.30$ (fractional tune frequency = 345 kHz), $V_{vert} = 8.17$ (fractional tune frequency = 200 kHz)

$V_{long} = 0.0076$ (8.8 kHz)

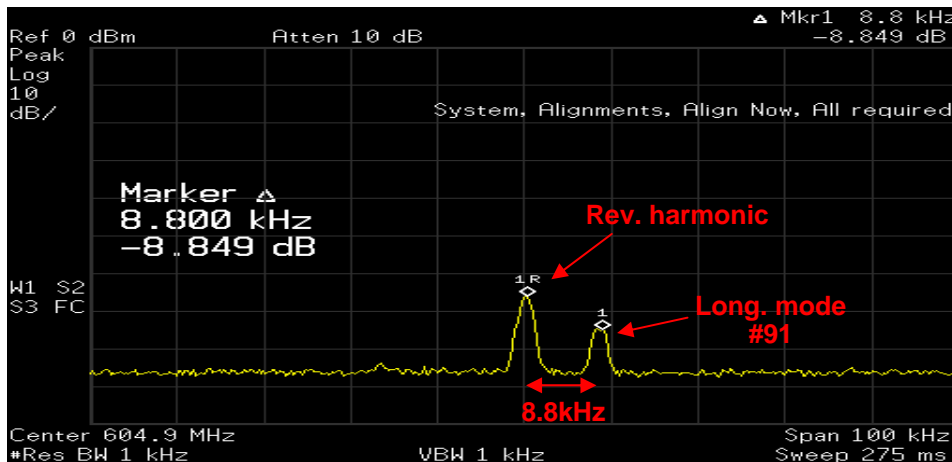
$$\omega = pM\omega_0 \pm (m+v)\omega_0$$



Spectral line at 512.185 MHz

Lower sideband 200 kHz apart from the revolution harmonics

→ vertical mode #413

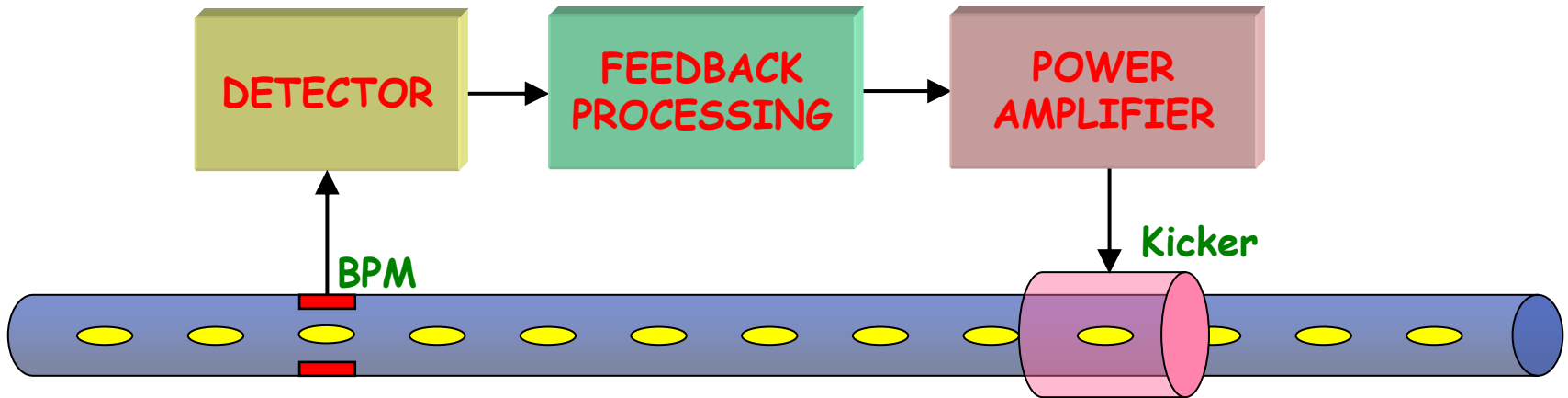


Spectral line at 604.9 MHz

Upper sideband 8.8 kHz apart from the 91st revolution harmonic

→ longitudinal mode #91

Multi-bunch feedback systems detect the instability using one or more Beam Position Monitors (BPM) and act back on the beam to damp the oscillation through an electromagnetic actuator called **kicker**



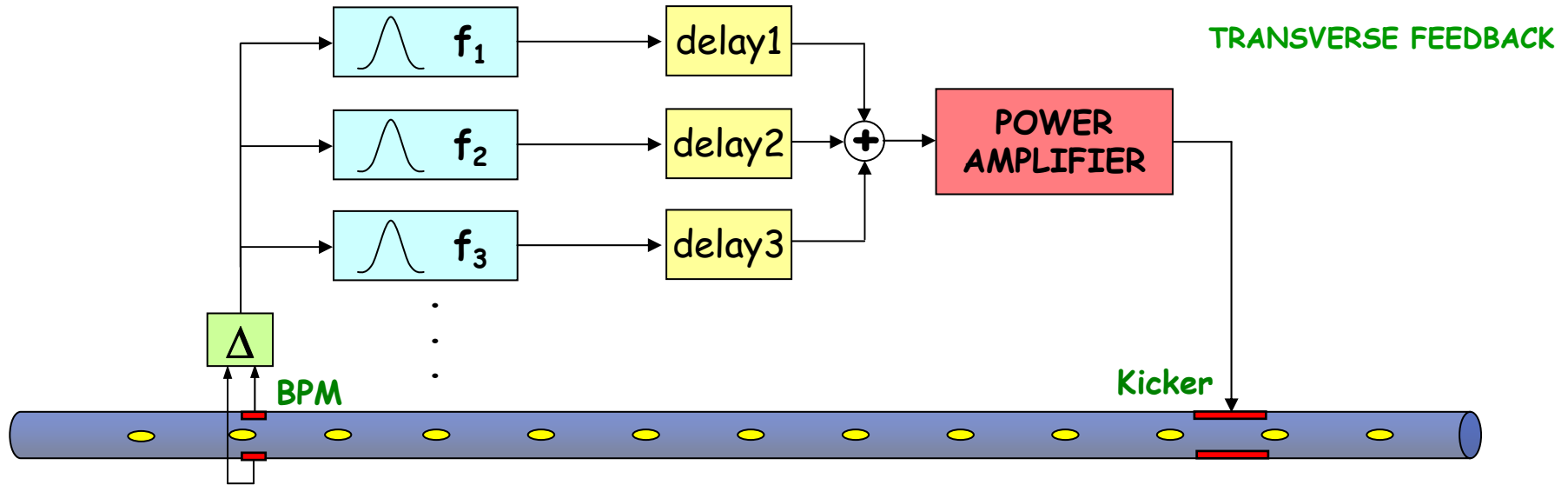
BPM and detector measure the beam oscillations

The feedback processing unit generate the correction signal

RF power amplifier and kicker act on the beam

Mode-by-mode feedback

A mode-by-mode (frequency domain) feedback acts separately on each unstable mode



An analog wideband electronics generates the position error signal from two BPM buttons

A narrow band-pass filter selects a given mode

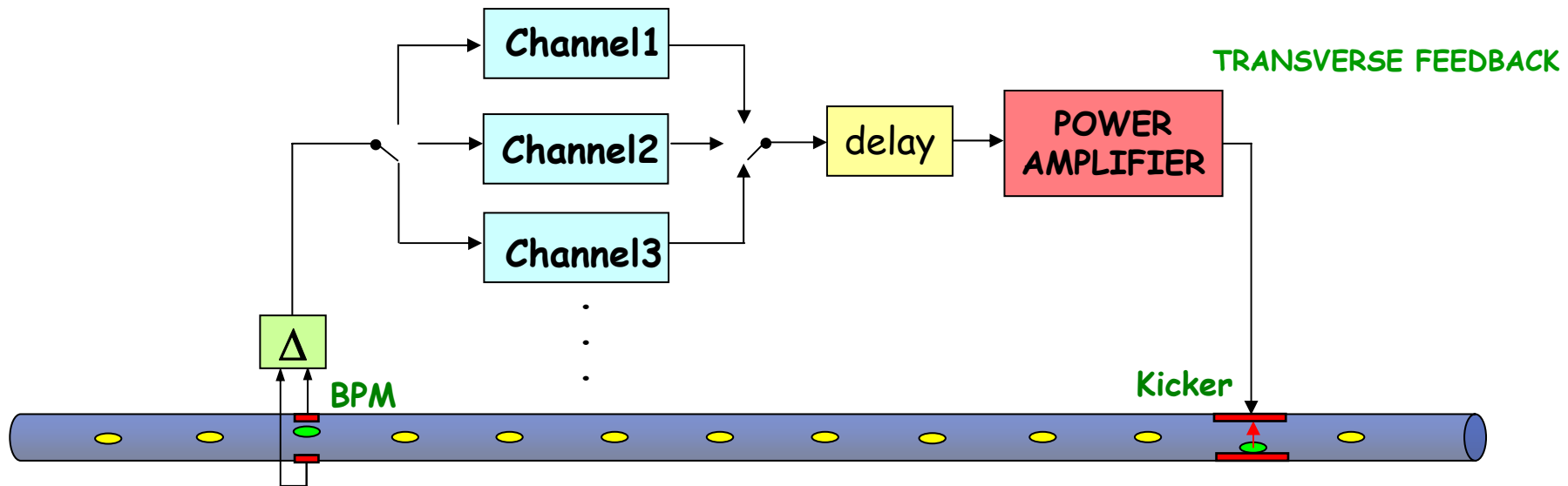
The filtered signal is phase shifted by an adjustable delay line to produce a negative feedback

One channel per unstable mode: all the channels work in parallel

For machines with many bunches and several potentially unstable modes, the mode-by-mode feedback is not the appropriate choice

Bunch-by-bunch feedback

A bunch-by-bunch (time domain) feedback acts individually on each bunch



The correction signal for a given bunch is computed based only on the motion of that bunch

There are as many processing channels as the number of bunches

Every bunch is measured and corrected at every machine turn but, due to the delay of the feedback chain, the correction kick corresponding to a given measurement is applied to the bunch one or more turns later

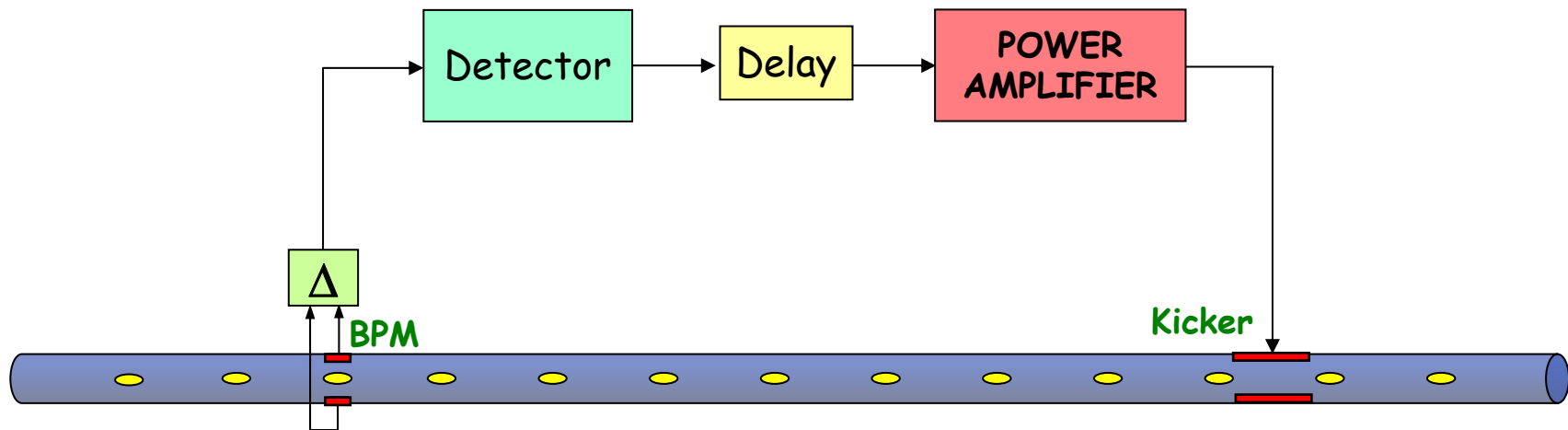
Damping the oscillation of each bunch is equivalent to damping all the multi-bunch modes

Bunch-by-bunch analog implementation: one-BPM feedback

Transverse feedback

The correction signal applied to a given bunch must be **proportional to the derivative of the bunch oscillation** at the kicker, thus a sampled sinusoid shifted $\pi/2$ with respect to the oscillation of the bunch when it passes through the kicker

The signal from a BPM with the **appropriate betatron phase advance** with respect to the kicker can be used to generate the correction signal

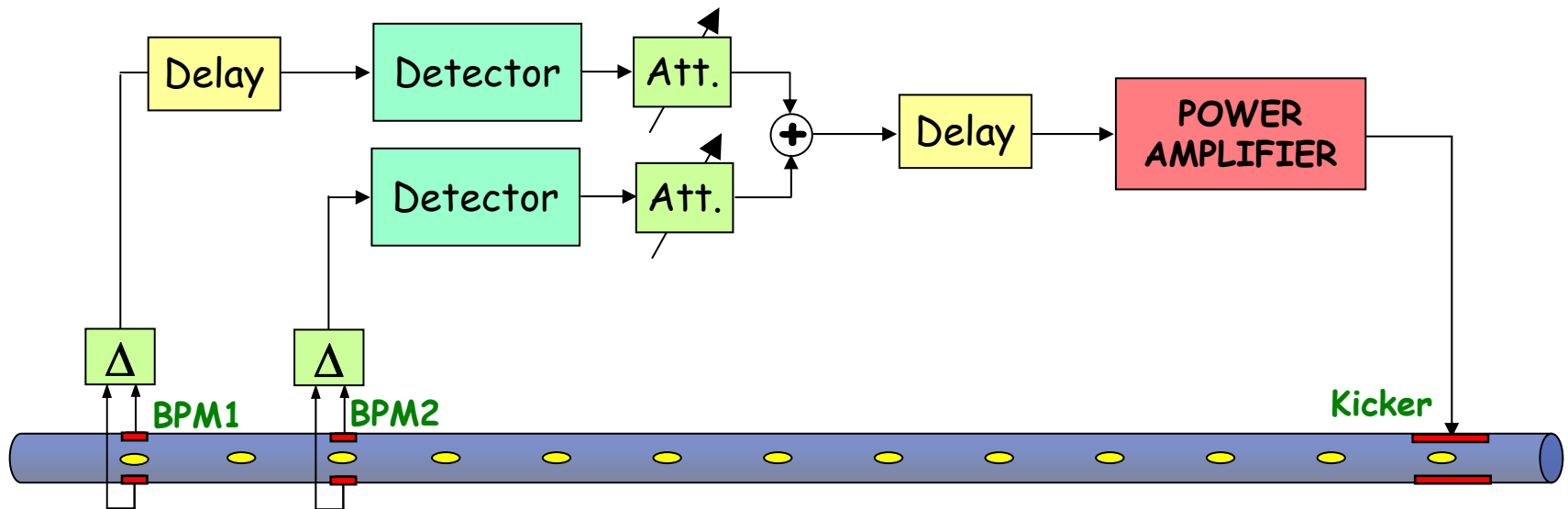


The **detector** down converts the high frequency (typically a multiple of the bunch frequency f_{rf}) BPM signal into base-band (range $0 - f_{rf}/2$)

The **delay line** assures that the signal of a given bunch passing through the feedback chain arrives at the kicker when, after one machine turn, the same bunch passes through it

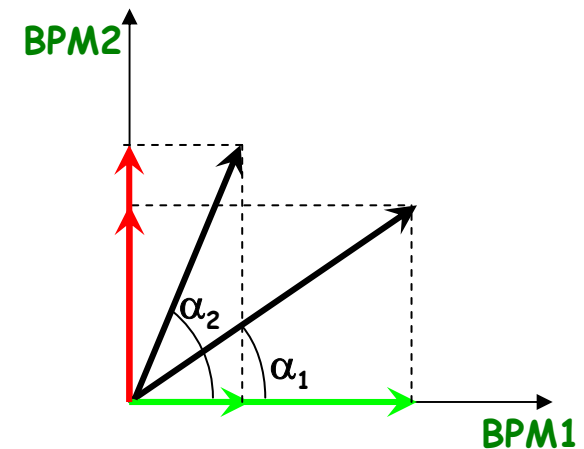
Analog implementation: two-BPM feedback

Transverse feedback case



The two BPMs can be in any ring position with respect to the kicker providing that they are separated by $\pi/2$ in betatron phase

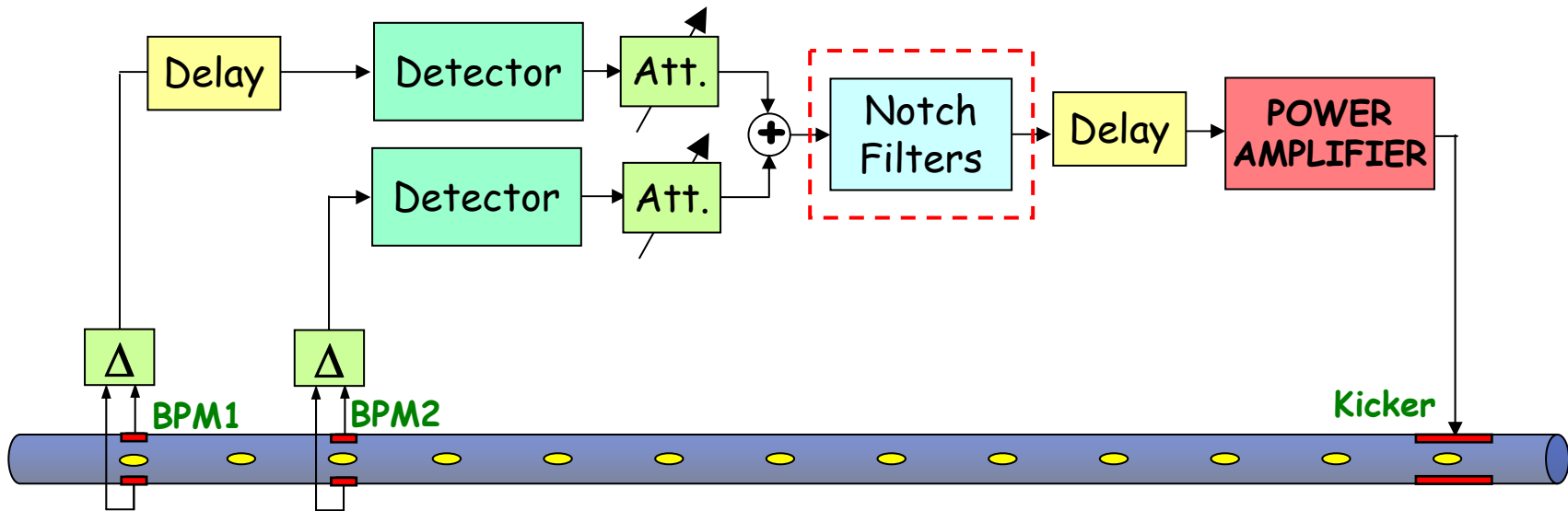
Their signals are combined with variable attenuators in order to provide any required phase of the resulting signal



Analog implementation: revolution harmonics suppression

Transverse feedback case

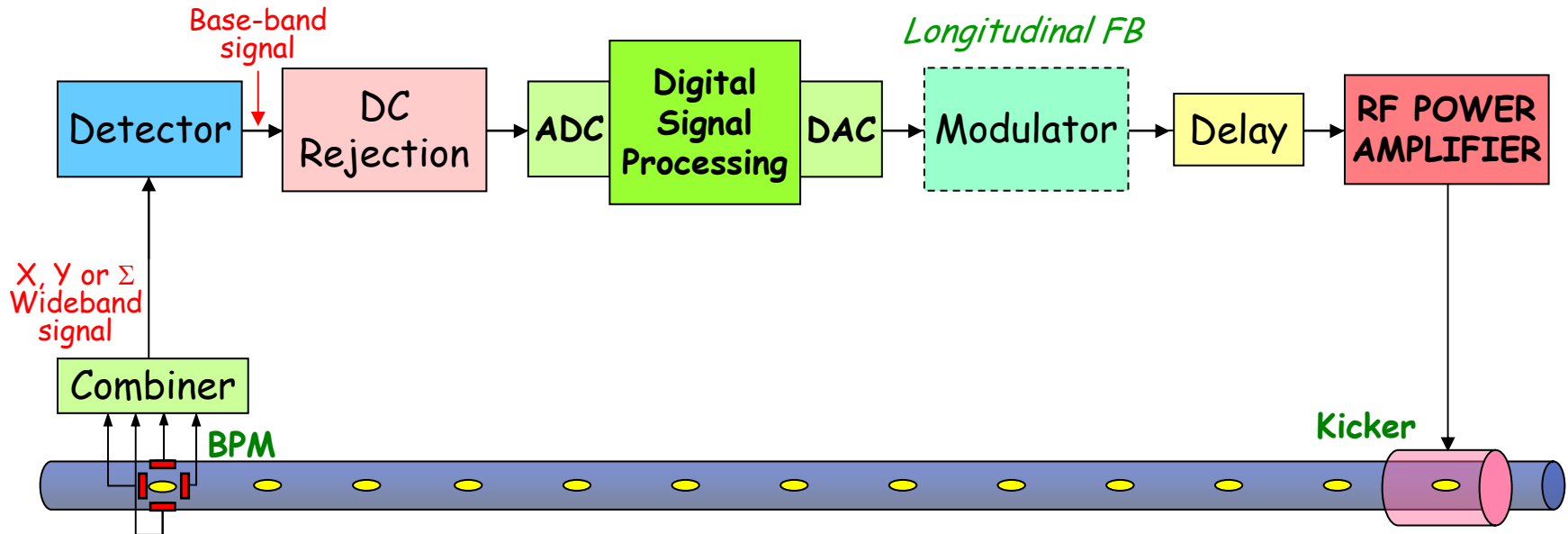
The revolution harmonics (frequency components at multiples of ω_0) are useless signal components that have to be eliminated in order not to saturate the RF amplifier



A similar feedback architecture has been used to build the ALS transverse multi-bunch feedback system, also used at PLS and BessyII light sources.

Digital bunch-by-bunch feedback

Transverse and longitudinal case



The **combiner** generates the X , Y or Σ signal from the BPM button signals

The **detector** demodulates the position signal

The "stable beam components" are suppressed by the **DC rejection unit**

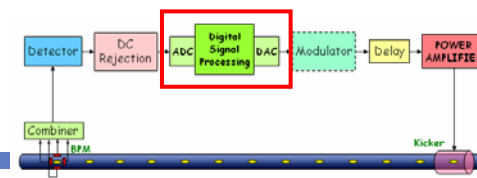
The resulting signal is digitized, processed and re-converted to analog by the **processing unit**

The **modulator** translates the correction signal to the frequency of the kicker (longitudinal)

The **delay line** adjusts the timing of the signal to match the bunch arrival time

The **RF power amplifier** supplies the power to the **kicker**

Digital vs. analog feedbacks



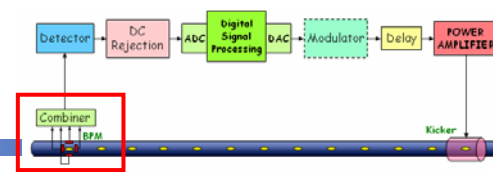
ADVANTAGES OF DIGITAL FEEDBACKS

- **Reproducibility**: not subject to temperature or environment changes, aging, ...
- **Flexibility**: modification made by software/firmware (ex. control algorithms, transverse/longitudinal FB, ...)
- **Higher performance of feedback controllers** and implementation of sophisticated control algorithms
- **Efficient control**: combination of basic control algorithms and additional control features (ex. saturation control, down sampling, etc.)
- **Effective integration with control system**: feedback setup and optimization, data acquisition, easy and automated operations, ...
- **Availability of diagnostic features** for both feedback commissioning and optimization, and for machine physics studies

DISADVANTAGE OF DIGITAL FEEDBACKS

- **High group delay** due to ADC, digital processing and DAC

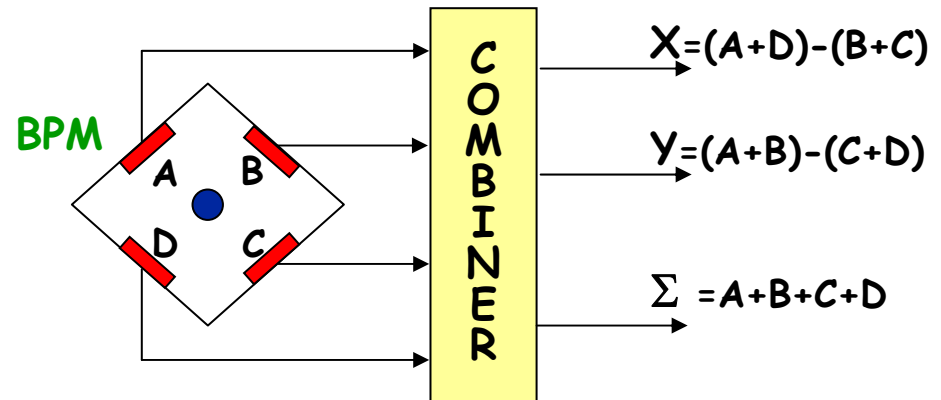
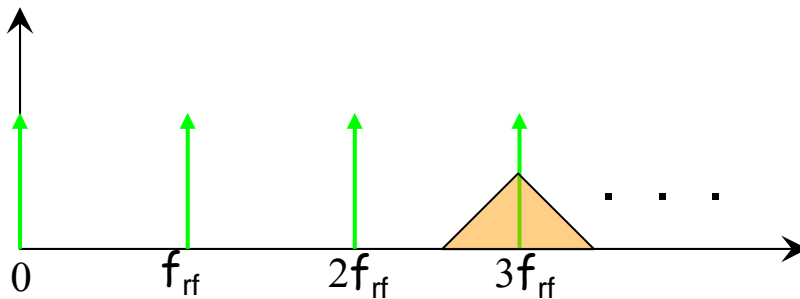
BPM and Combiner



The four signals from a standard four-button BPM can be opportunely combined to obtain the wide-band X, Y and Σ signals used respectively by the transverse horizontal, vertical and by the longitudinal feedback systems

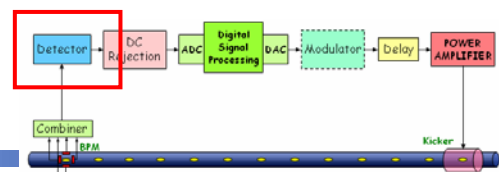
Usually BPM and combiner work around a multiple of f_{rf} , where the overall BPM-cables transfer function has maximum amplitude

Moreover, a higher f_{rf} harmonic is preferred for the longitudinal feedback because of the higher sensitivity of the phase detection system



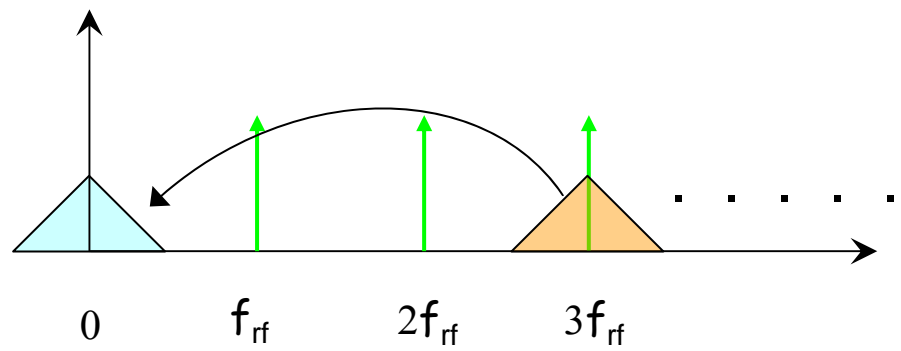
The SUM (Σ) signal only contains bunch arrival time information since the sum of the buttons has almost constant amplitude

Detector: transverse feedback

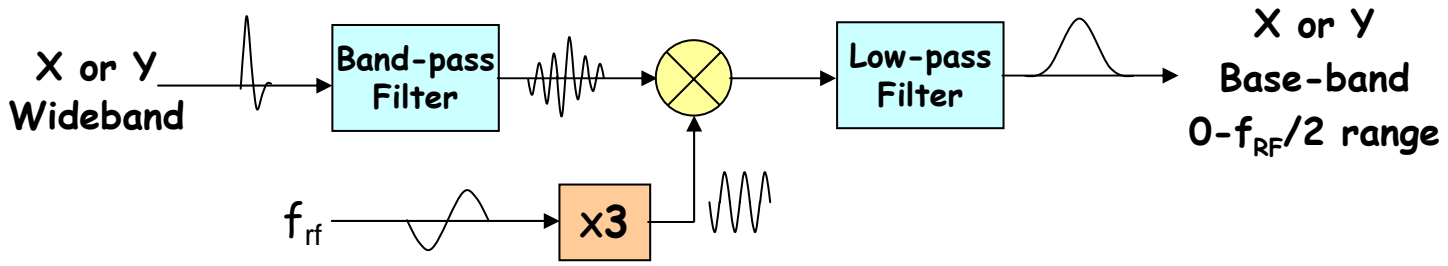


Any $f_{rf}/2$ portion of the beam spectrum contains the information of all potential multi-bunch modes and can be used to detect an instability and measure its amplitude

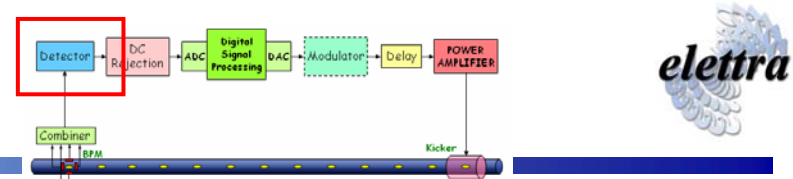
The detector (or RF front-end) translates the wide-band signal into base-band ($0-f_{rf}/2$ range): the operation is an **amplitude demodulation**



Heterodyne technique: the "local oscillator" signal is derived from the RF by multiplying its frequency by an integer number corresponding to the chosen harmonic of f_{rf}

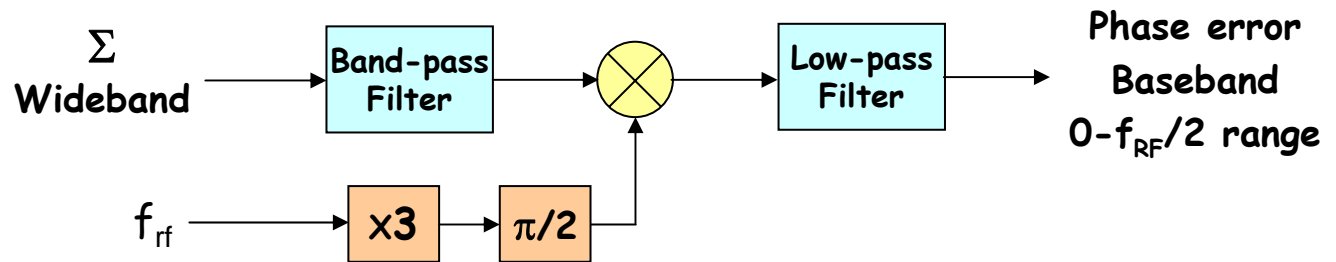


Detector: longitudinal feedback



The detector generates the base-band longitudinal position (phase error) signal ($0-f_{rf}/2$ range) by processing the wide-band signal: the operation is a **phase demodulation**

The phase demodulation can be obtained with the same heterodyne technique but using a "local oscillator" signal shifted by $\pi/2$ with respect to the bunches



Amplitude demodulation:

$$A(t) \sin(3\omega_{rf} t) \cdot \sin(3\omega_{rf} t) \propto A(t) (\cos(0) - \cos(6\omega_{rf} t)) \approx A(t)$$

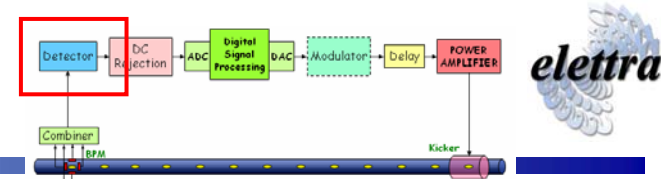
~~Low-pass filter~~

Phase demodulation:

$$\sin(3\omega_{rf} t + \varphi(t)) \cdot \cos(3\omega_{rf} t) \propto \sin(6\omega_{rf} t + \varphi(t)) + \sin(\varphi(t)) \approx \varphi(t)$$

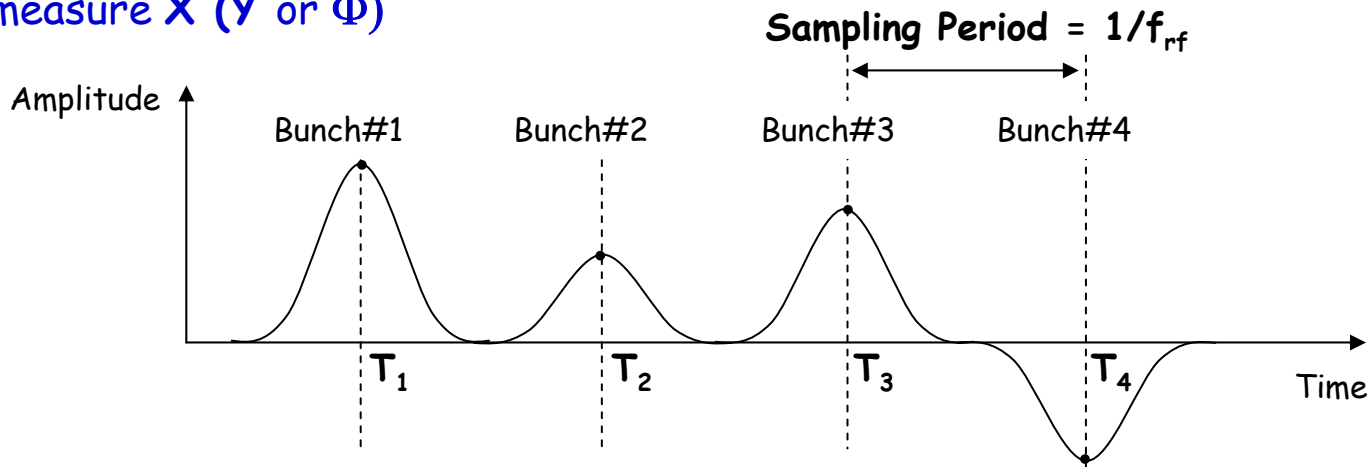
~~Low-pass filter~~ For small signals

Detector: time domain considerations



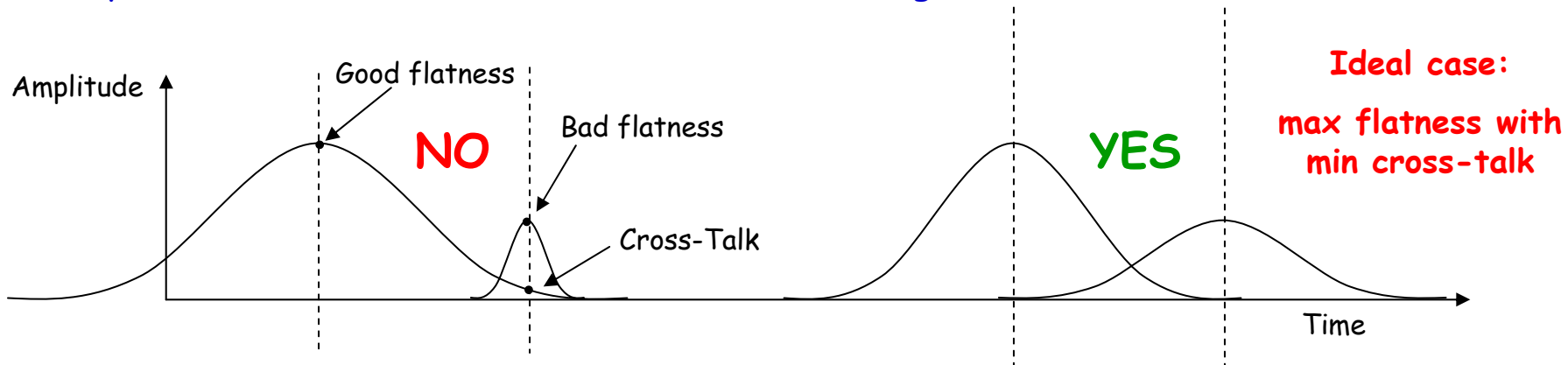
The base-band signal can be seen as a sequence of "pulses" each with amplitude proportional to the position error X (Y or Φ) and to the charge of the individual bunches

By sampling this signal with an A/D converter synchronous to the bunch frequency, one can measure X (Y or Φ)

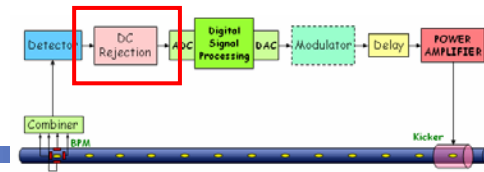


The multi-bunch-mode number $M/2$ is the one with higher frequency ($\approx f_{rf}/2$): the pulses have the same amplitude but alternating signs

The band-pass and low-pass filters design is a compromise between **maximum flatness** of the top of the pulses and **cross-talk** between bunches due long rise/fall times



Rejection of stable beam signal

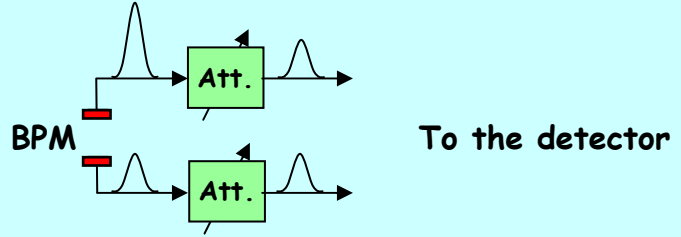


The base-band signal of each bunch can have a constant offset (DC component) due to:

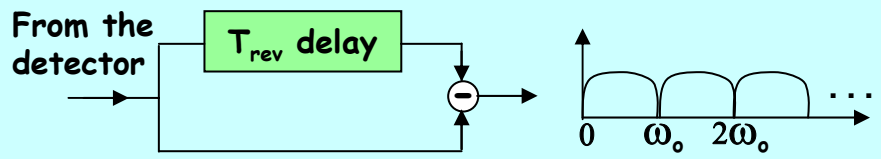
- transverse case: closed orbit or unbalanced BPM electrodes or cables
- longitudinal case: beam loading, i.e. different stable beam phases for each bunch

In the frequency domain, the stable beam signal shows up as non-zero revolution harmonics. These components have to be suppressed because they are useless for the feedback, reduce the dynamic range of the A/D converter and can saturate the D/A converter and the amplifier.

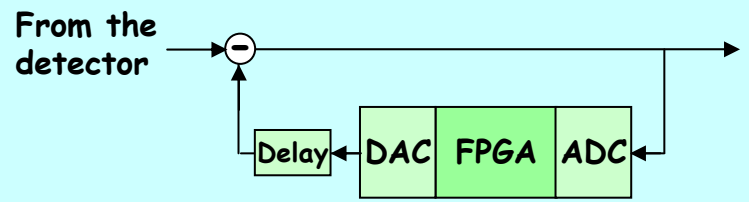
Variable attenuators on the BPM electrodes to make the signals identical in amplitude



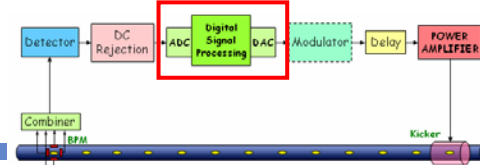
Correlation filter: $1-z^{-1}$ ($T=T_{rev}=1/f_0$) analog FIR filter made of delay lines and combiners to suppress all the revolution harmonics (DC included)



DC rejection module: the signal is sampled at f_{rf} , the mean value is calculated for each bunch, integrated, converted to analog and subtracted to the bunch signal



Digital processor

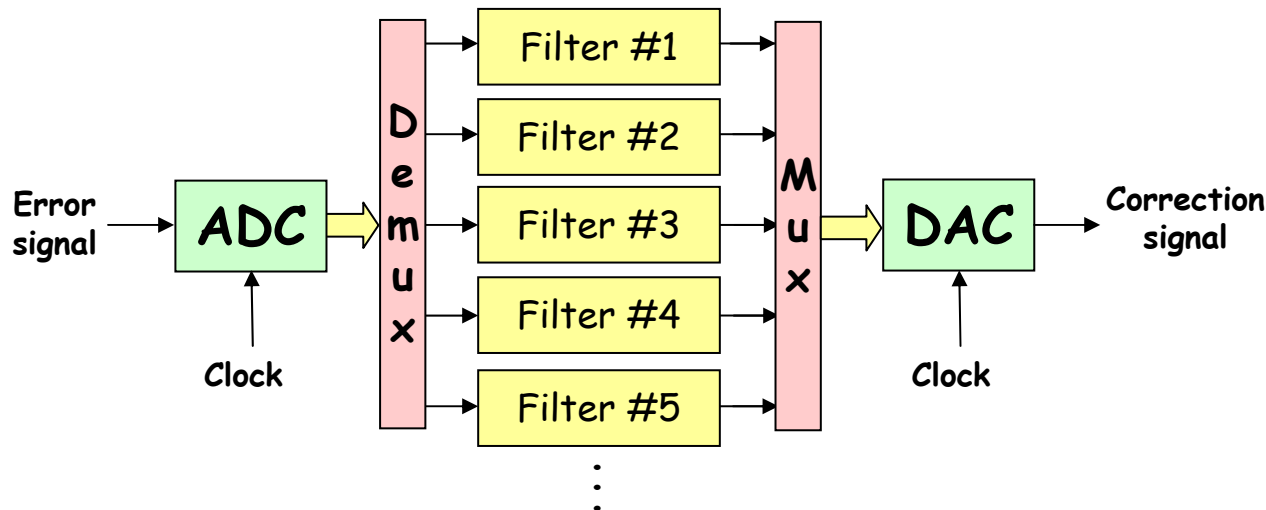


The **A/D converter** samples and digitizes the signal at the bunch repetition frequency: each sample corresponds to the position (X , Y or Φ) of a given bunch. Precise synchronization of the sampling clock with the bunch signal must be provided

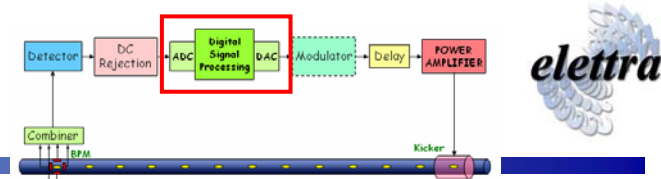
The **digital samples** are then **de-multiplexed** into M channels (M is the number of bunches): in each channel the turn-by-turn samples of a given bunch are processed by a dedicated **digital filter** to calculate the correction samples

The processing consists in **DC component suppression** and **phase shift** at the betatron/synchrotron frequency

After processing, the correction sample streams are **recombined** and eventually converted to analog by the **D/A converter**



Digital processor: the implementation



ADC: existing multi-bunch feedback systems usually employ 8-bit ADCs at up to 500 Msample/s; some implementations use a number of ADCs with higher resolution (14 bits) and lower rate working in parallel and sampling the same signal with shifted sampling clocks

ADCs with more resolution have some advantages:

- lower quantization noise (crucial for low-emittance machines)
- higher dynamic range (in some cases rejection of stable beam signal is not necessary)

DAC: usually employed DACs convert samples at up to 500 Msample/s and 14-bit resolution

Digital Processing: the feedback processing can be executed by DSPs or FPGAs

Pros

Cons

DSP

- Easy programming
- Flexible

- Difficult HW integration
- Latency
- Sequential program execution
- A number of DSPs are necessary

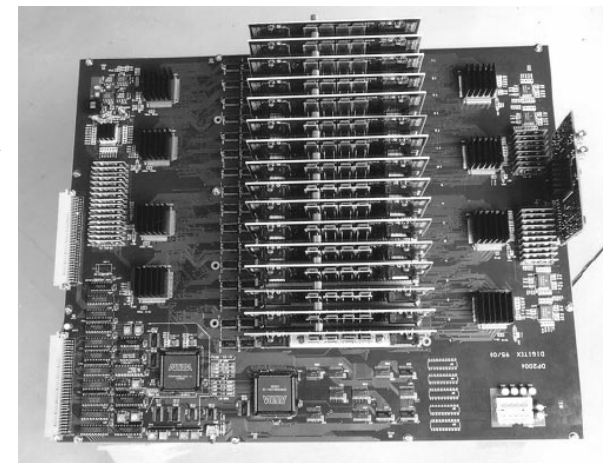
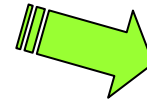
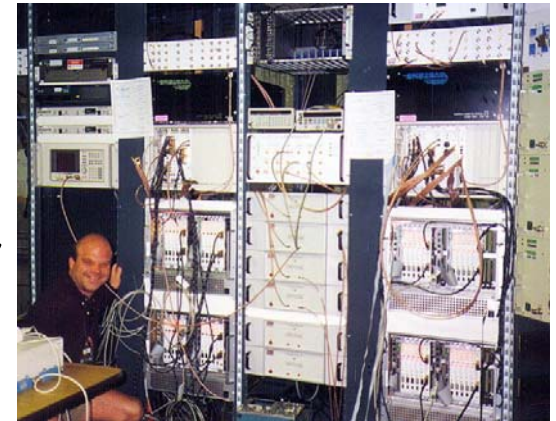
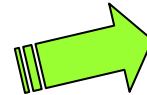
FPGA

- Fast (only one FPGA is necessary)
- Parallel processing
- Low latency

- Difficult programming
- Less flexible

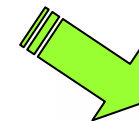
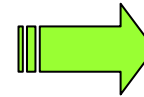
Implementations and examples

- ▶ ALS (PLS, BessyII): completely analogic transverse FB
- ▶ ALS, PEP-II, DaΦne (SPEAR, PLS, BessyII): digital longitudinal FB, a number of VME crates with DSP boards
- ▶ PEP-II: transverse digital FB, delay line with ADC-FPGA-DAC
- ▶ KEKB digital transverse and longitudinal FB: two-tap FIR filter performing DC rejection, filtering and delay
- ▶ SPring-8 (TLS, KEK Photon Factory, Soleil): digital transverse FB, smart analog de-multiplexer + a number of ADC-FPGA channels and one DAC

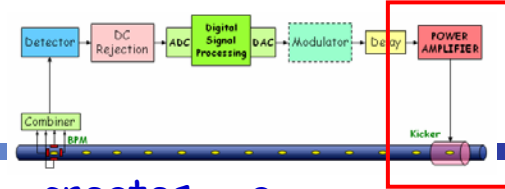


Implementations and examples

- Elettra, SLS: digital transverse and longitudinal FB with VME ADC/DAC and commercial DSP boards
- CESR: digital longitudinal FB with one DSP, transverse digital FB with S/Hs and a number of ADC-FIFO channels and one DAC
- HERA-p: longitudinal digital FB with ADC-FPGA-DAC
- ESRF and Diamond: digital transverse and longitudinal FB using Libera (Instrumentation Technologies) with four ADCs one FPGA and one DAC
- DaΦne, KEK Photon Factory: digital transverse feedback using iGp (Dimtel) with ADC-FPGA-DAC



Kicker and Amplifier



The **kicker** is the **feedback actuator**. It creates a transverse/longitudinal electromagnetic field that kicks the bunches as they pass through the kicker at every turn. The overall effect is the damping of the betatron/synchrotron oscillations

The **amplifier** must provide the necessary RF power to the kicker by amplifying the signal from the DAC (or from the modulator in the case of longitudinal feedbacks)

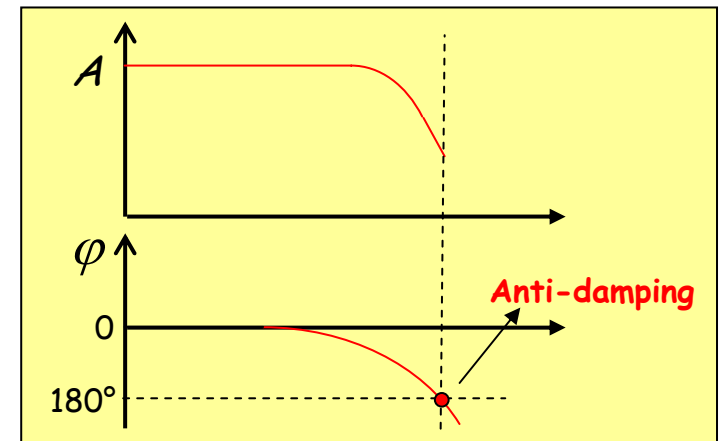
A **bandwidth** of at least $f_{rf}/2$ is necessary: from DC (all kicks of the same sign) to $f_{rf}/2$ (kicks of alternating signs)

The bandwidth of amplifier-kicker must be sufficient to correct each bunch with the appropriate kick without affecting the neighbour bunches. The amplifier-kicker design has to maximize the kick strength while minimizing the cross-talk between corrections given to different bunches

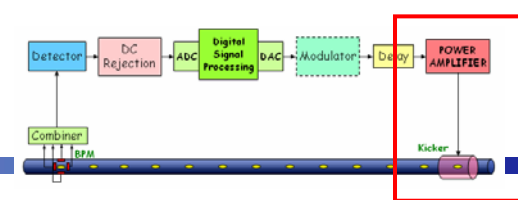
Shunt impedance, ratio between the squared voltage seen by the bunch and twice the power at the kicker input:

$$R = \frac{V^2}{2P_{IN}}$$

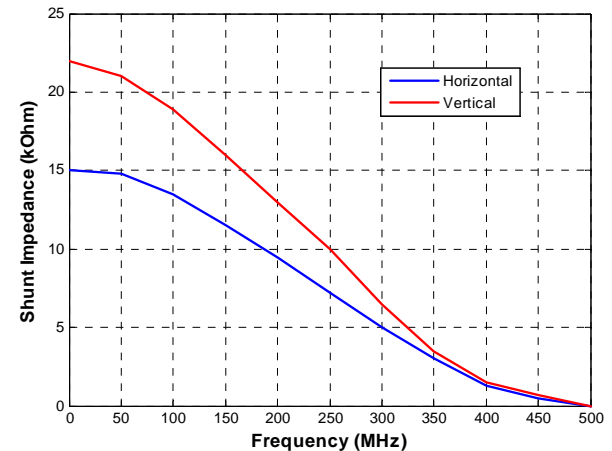
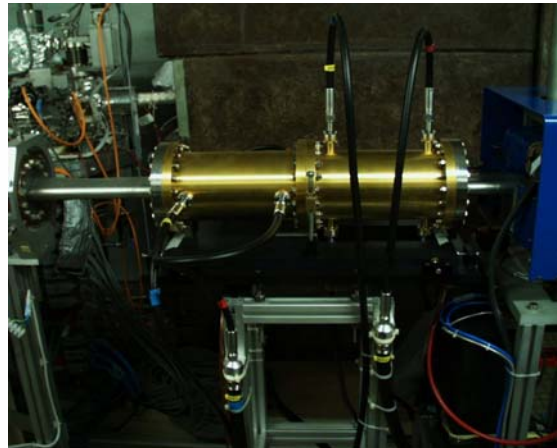
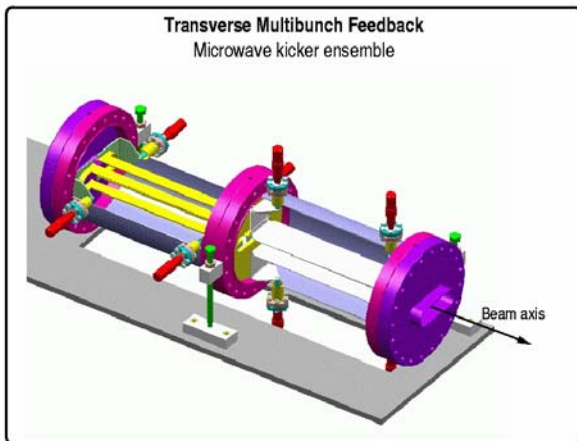
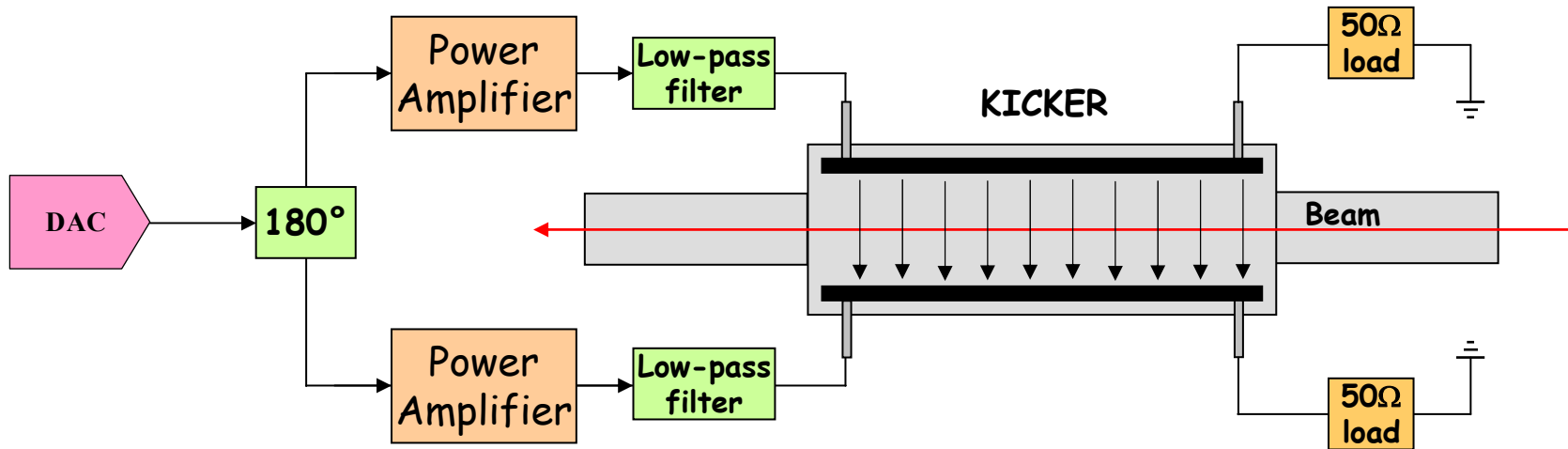
Important issue: the group delay of the amplifier must be as constant as possible, e.g. the phase response must be linear, otherwise the feedback efficiency is reduced for some modes or can even excite some high frequency modes



Kicker and Amplifier: transverse FB



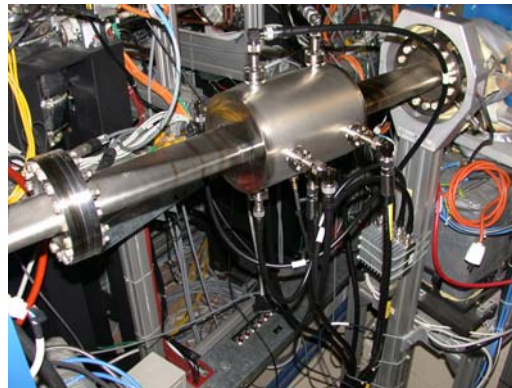
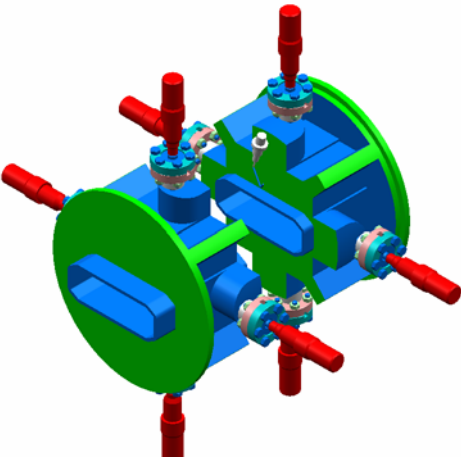
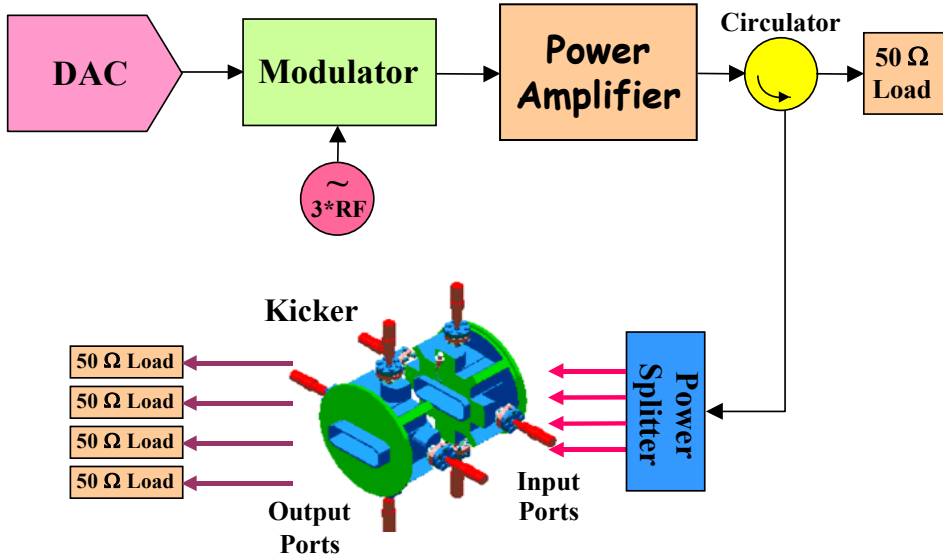
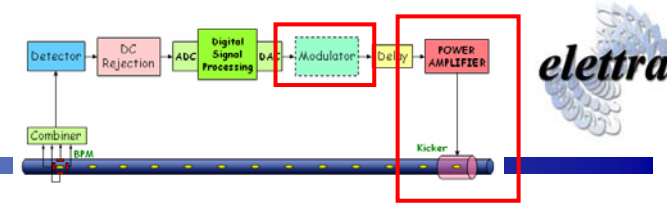
For the transverse kicker a **stripline** geometry is usually employed
 Amplifier and kicker work in the $\sim DC - f_{rf}/2$ frequency range



The ELETTRA/SLS transverse kicker (design by Micha Dehler-PSI)

Shunt impedance of the ELETTRA/SLS transverse kickers

Kicker and Amplifier: longitudinal FB



The ELETTRA/SLS longitudinal kicker (design by Micha Dehler-PSI)

A "cavity like" kicker is usually preferred
Higher shunt impedance and smaller size

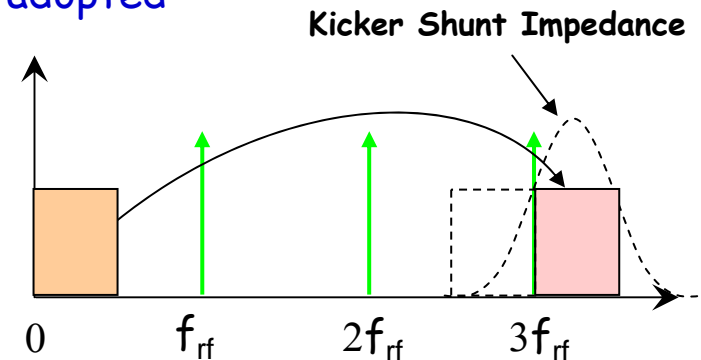
The operating frequency range is typically $f_{rf}/2$ wide and placed on one side of a multiple of f_{rf} :

$$\text{ex. from } 3f_{rf} \text{ to } 3f_{rf} + f_{rf}/2$$

A "pass-band" instead of "base-band" device

The base-band signal from the DAC must be modulated, e.g. translated in frequency

A SSB (Single Side Band) amplitude modulation or similar techniques (ex. QPSK) can be adopted



Theory of feedback control: transverse feedback

The motion of a particle can be described as a pseudo-harmonic oscillator with amplitude proportional to the square root of the β -function

$$x(s) = a \sqrt{\beta(s)} \cos \varphi(s), \quad \text{where} \quad \varphi(s) = \int_0^s \frac{d\bar{s}}{\beta(\bar{s})}$$

The derivative of the position, i.e. the angle of the trajectory is:

$$x' = -\frac{a}{\sqrt{\beta}} \sin \varphi + \frac{a\beta'}{2\sqrt{\beta}} \cos \varphi, \quad \text{with} \quad \varphi' = \frac{1}{\beta}$$

By introducing $\alpha = -\frac{\beta'}{2}$ we can write: $x' = \frac{a}{\sqrt{\beta}} \sqrt{1 + \alpha^2} \sin(\varphi + \arctan \alpha)$

At the coordinate s_k , the electromagnetic field of the kicker deflects the particle bunch which varies its angle by k : as a consequence the bunch starts another oscillation

$$x_1 = a_1 \sqrt{\beta} \cos \varphi_1$$

which must satisfy the following constraints:

$$\begin{cases} x(s_k) = x_1(s_k) \\ x'(s_k) = x_1'(s_k) + k \end{cases}$$

By introducing $A = a\sqrt{\beta}$, $A_1 = a_1\sqrt{\beta}$ the two-equation two-unknown-variables system becomes:

$$\begin{cases} A \cos \varphi = A_1 \cos \varphi_1 \\ A \frac{\sqrt{1 + \alpha^2}}{\beta} \sin(\varphi + \arctg(\alpha)) = A_1 \frac{\sqrt{1 + \alpha^2}}{\beta} \sin(\varphi_1 + \arctg(\alpha)) + k \end{cases}$$

The solution of the system gives amplitude and phase of the new oscillation:

$$\begin{cases} A_1 = \sqrt{(A \sin \varphi - k\beta)^2 + A^2 \cos^2 \varphi} \\ \varphi_1 = \arccos\left(\frac{A}{A_1} \cos \varphi\right) \end{cases}$$

Theory of feedback control: transverse feedback

From $A_1 = \sqrt{(A \sin \varphi - k\beta)^2 + A^2 \cos^2 \varphi}$ when the kick is small ($k \ll \frac{A}{\beta}$) then $\frac{\Delta A}{A} = \frac{A - A_1}{A} \cong \frac{\beta}{A} k \sin \varphi$

In the linear feedback case, e.g. when the turn-by-turn kick signal is a sinusoid proportional to the bunch oscillation amplitude, in order to maximize the damping rate the kick signal must be in-phase with $\sin \varphi$:

$$k = g \frac{A}{\beta} \sin \varphi \quad \text{with } 0 < g < 1$$

The gain g is determined by the max allowed kicker value which is generated when the oscillation amplitude at the kicker A is max:

$$g = \frac{k_{\max}}{A_{\max}} \beta \quad \text{therefore} \quad k = \frac{k_{\max}}{A_{\max}} A \sin \varphi$$

For small kicks $\frac{\Delta A}{A} \cong \frac{k_{\max}}{A_{\max}} \beta \sin^2 \varphi$ the relative amplitude decrease is monotonic and its average is: $\left\langle \frac{\Delta A}{A} \right\rangle \cong \frac{\beta k_{\max}}{2 A_{\max}}$

Therefore, the average relative decrease is constant, which means that, in average, the amplitude decrease is exponential with time constant τ (damping time) given by:

$$\frac{1}{\tau} = \left\langle \frac{\Delta A}{A} \right\rangle \frac{1}{T_0} = \frac{\beta k_{\max}}{2 A_{\max} T_0} \quad \text{where } T_0 \text{ is the revolution period.}$$

By referring to the oscillation at the BPM location,

$$\frac{1}{\tau} = \frac{k_{\max}}{2 T_0 A_{B\max}} \sqrt{\beta_k \beta_B}$$

$A_{B\max}$ is the max oscillation amplitude at the BPM

Theory of feedback control: transverse feedback

The change in the transverse momentum p of the bunch passing through the kicker can be expressed by:

$$\Delta p = \frac{e}{c} V_{\perp} \quad \text{where} \quad V_{\perp} = \int_0^L (\bar{E} + c \times \bar{B})_{\perp} dz \quad \text{is the kick voltage and} \quad p = \frac{E_B}{c}$$

e = electron charge, c = light speed, \bar{E}, \bar{B} = fields in the kicker, L = length of the kicker, E_B = beam energy

$$V_{\perp} \text{ can be derived from the definition of kicker shunt impedance: } R_k = \frac{V_{\perp}^2}{2P_k}$$

The max deflection angle in the kicker is given by:

$$k_{\max} = \frac{\Delta p}{p} = e \frac{V_{\perp}}{E_B} = \left(\frac{e}{E_B} \right) \sqrt{2P_k R_k}$$

From the previous equations we can obtain the power required to damp the bunch oscillation with damping rate τ :

$$P_k = \frac{2}{R_k \beta_k} \left(\frac{E_B}{e} \right)^2 \left(\frac{T_0}{\tau} \right)^2 \left(\frac{A_{B\max}}{\sqrt{\beta_B}} \right)^2$$

Kicker power: transverse feedback

$$P_K = \frac{2}{R_K \beta_K} \left(\frac{E_B}{e} \right)^2 \left(\frac{T_0}{\tau} \right)^2 \left(\frac{A_{B \max}}{\sqrt{\beta_B}} \right)^2$$

Max oscillation amplitude at the BPM

Required damping time

Ex.: (Elettra):

$R_K = 15 \text{ k}\Omega$ (mean value)

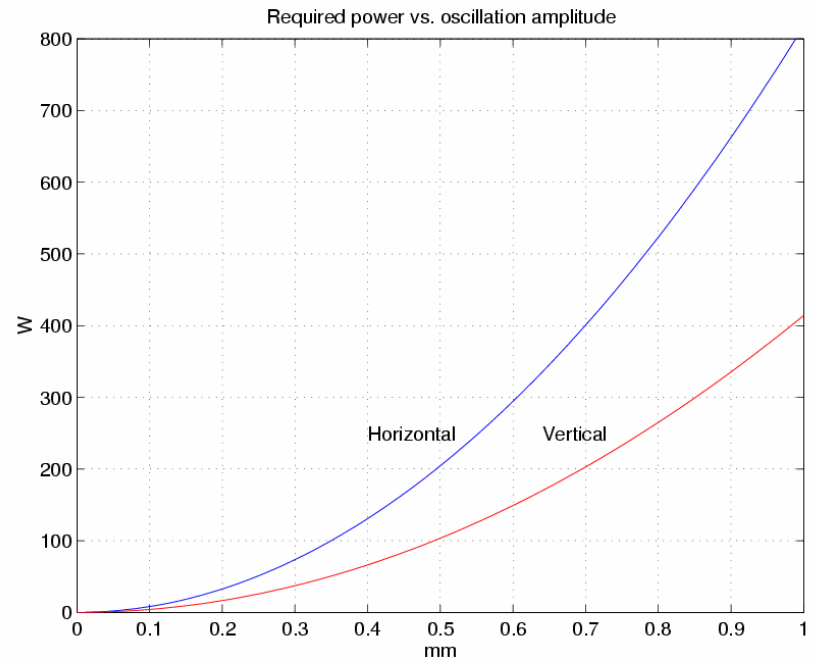
$E_B/e = 2 \text{ GeV}$

$T_0 = 864 \text{ ns}$

$\tau = 120 \text{ }\mu\text{s}$

$\beta_{B \text{ H,V}} = 5.2, 8.9 \text{ m}$

$\beta_{K \text{ H,V}} = 6.5, 7.5 \text{ m}$



Kicker power: longitudinal feedback

$$P_k = \frac{2}{R_k} \left(\frac{\omega_S E_B \varphi_{\max}}{\omega_0 \alpha f_{RF} \tau} \right)^2$$

τ = feedback damping time

ω_0 = revolution frequency

ω_S = synchrotron frequency

α = momentum compaction factor

f_{RF} = RF frequency

R_k = kicker shunt impedance

E_B = beam energy

φ_{\max} = maximum oscillation amplitude

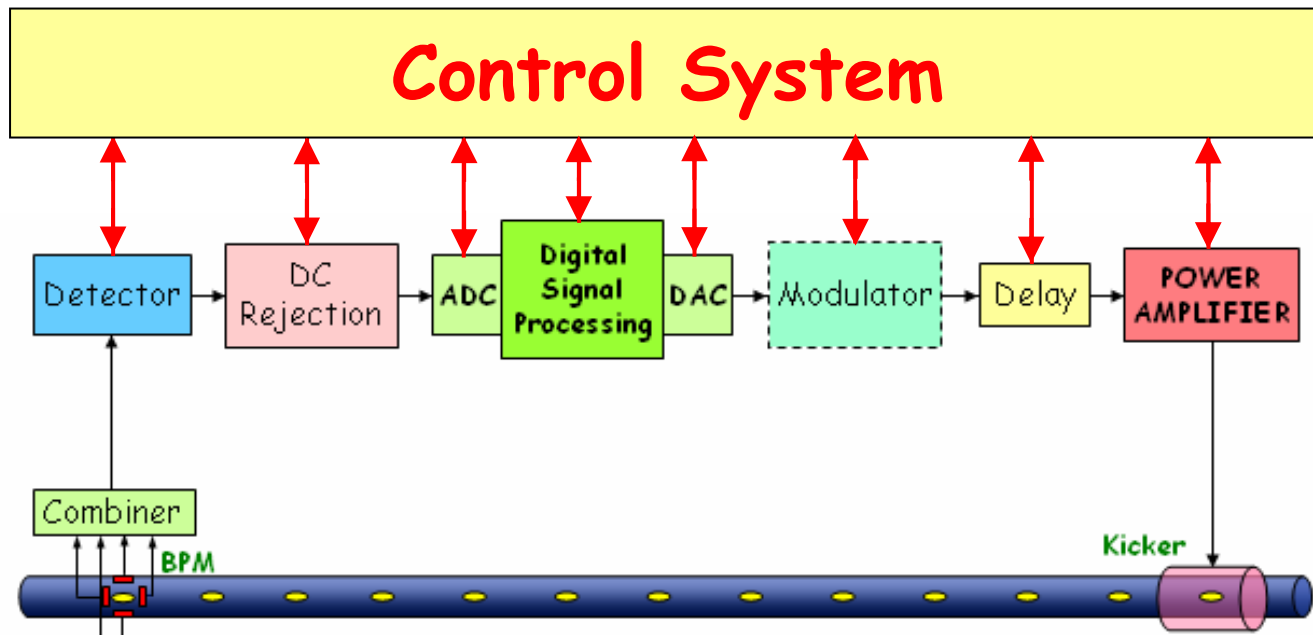
The power is proportional to the square of the maximum phase oscillation

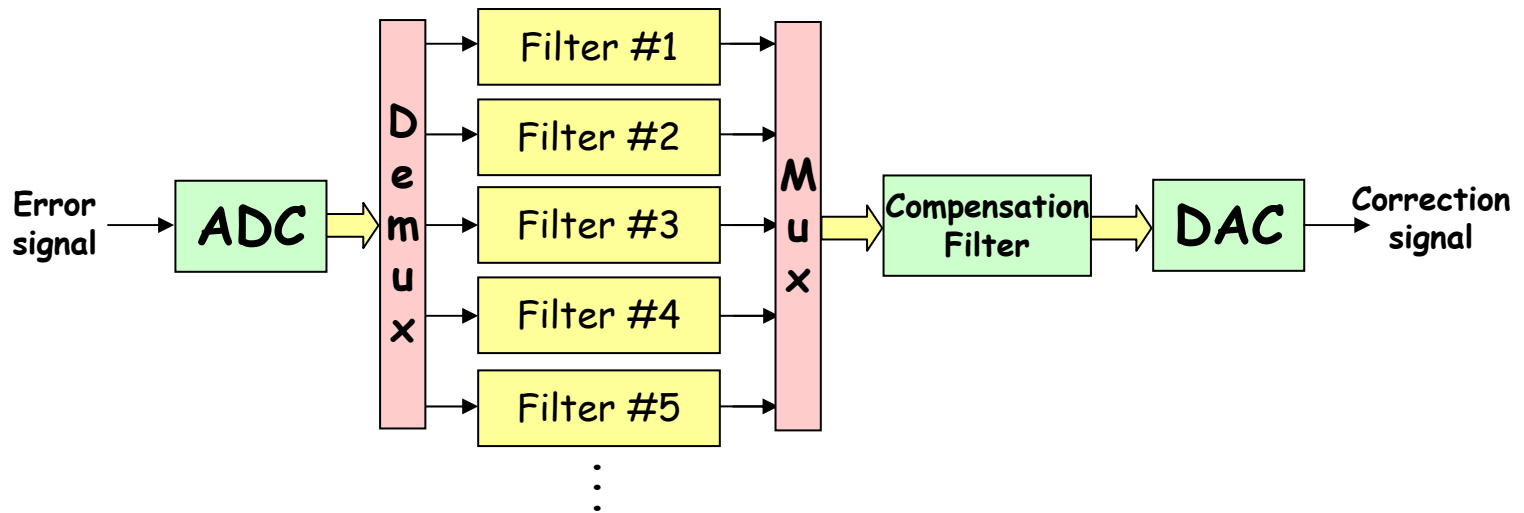
If we switch on the feedback when the oscillation is small, the required power is lower

The feedback gain must be kept high (a small oscillation corresponds to the entire dynamic range of DAC/amplifier)

Control system integration

- It is desirable that each component of the feedback system that needs to be configured and adjusted has a **control system interface**
- Any **operation** must be possible from **remote** to facilitate the system commissioning and the optimization of its performance
- An effective data acquisition channel has to provide **fast data transfer** of large amounts of data for analysis of feedback performance and beam dynamics studies
- It is preferable to have a direct connection to a mathematical tool (ex. **Matlab**) to develop measurement procedures using a script language and acquire data for post processing and data visualization





M (number of bunches) filters each dedicated to one bunch

To damp the bunch oscillations the kick must be the derivative of the bunch position at the kicker: for a given oscillation frequency, a $\pi/2$ phase shifted signal must be generated

In the computation of the required filter phase response, the relative position of BPM and kicker must be taken into account (transverse feedback) as well as any additional delay due to the feedback latency (multiple of one machine revolution period)

The digital processing must also reject any residual constant offset (DC component) from the bunch signal to avoid DAC saturation

Digital filters can be implemented with FIR (Finite Impulse Response) or IIR (Infinite Impulse Response) architectures

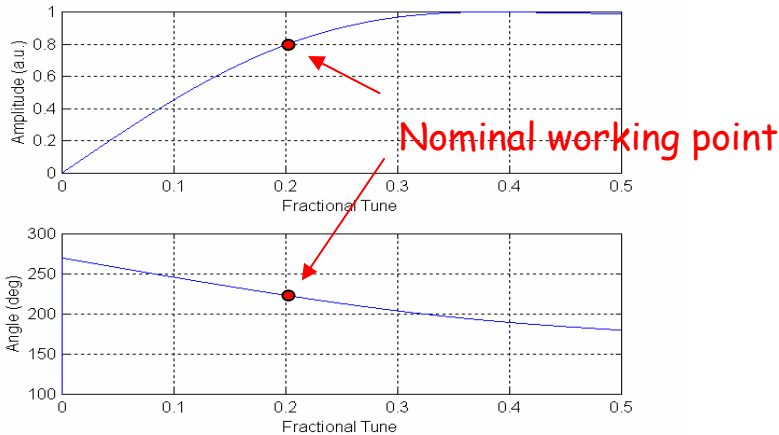
A filter on the full-rate data stream can compensate for amplifier/kicker unwanted behaviour

Digital filter design: 3-tap FIR filter

The minimum requirements are:

1. DC rejection (coefficients sum = 0)
2. Amplitude response at the tune frequency
3. Phase response at the tune frequency

A 3-tap FIR filter fulfils these requirements: the filter coefficients can be calculated analytically



Example:

- Fractional tune = 0.2
- Amplitude response at tune = 0.8
- Phase response at tune = 225°

$$H(z) = -6.5 + 5.4 z^{-1} + 1.1 z^{-2}$$

Z transform of the FIR filter response

In order to have zero amplitude at "0" frequency, we must put a "zero" in $z=1$. Then another zero in $z=c$ is added to fulfill the phase requirements.

"c" can be calculated analytically:

$$H(z) = k(1 - z^{-1})(1 - cz^{-1})$$

$$H(z) = k(1 - (1+c)z^{-1} + cz^{-2}) \quad z = e^{j\omega}$$

$$H(\omega) = k(1 - (1+c)e^{-j\omega} + ce^{-2j\omega})$$

$$e^{-j\omega_0} = \sin \omega_0 - j \cos \omega_0, \quad \alpha = \text{ang}(H(\omega_0))$$

$$\text{tg}(\alpha) = \frac{c(\sin(\omega_0) - \sin(2\omega_0)) + \sin(\omega_0)}{c(\cos(2\omega_0) - \cos(\omega_0)) + 1 - \cos(\omega_0)}$$

$$c = \frac{\text{tg}(\alpha)(1 - \cos(\omega_0)) - \sin(\omega_0)}{(\sin(\omega_0) - \sin(2\omega_0)) - \text{tg}(\alpha)(\cos(2\omega_0) - \cos(\omega_0))}$$

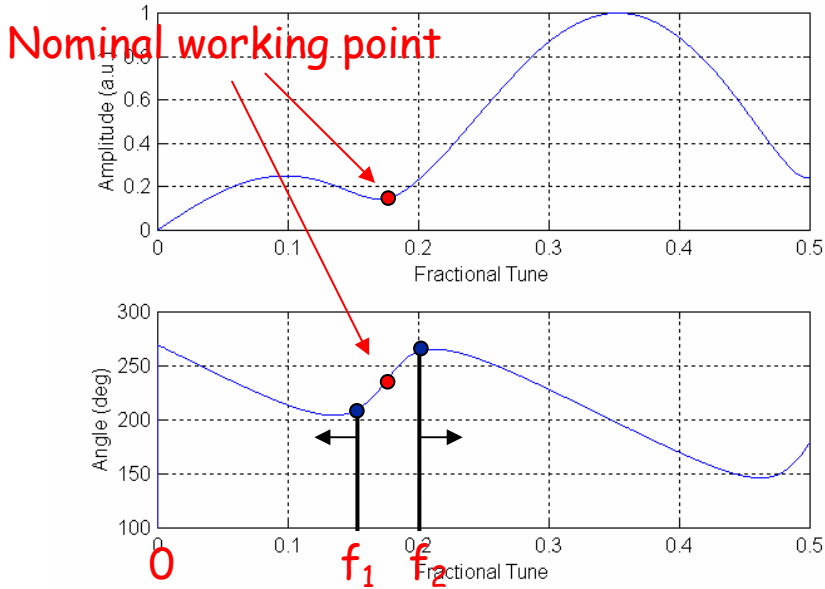
K is determined by the required amplitude of the transfer function at $\omega = \omega_0$

Digital filter design: 5-tap FIR filter

With more degrees of freedom additional features can be obtained

Ex.: *transverse feedback*. The **tune frequency** of the accelerator can significantly **change** during machine operations. The filter response (amplitude and angle) must guarantee the same feedback efficiency in a frequency range by performing an **automatic compensation**

In this example, given the feedback processing delay, the kick is applied to the bunch after 4 machine turns. When the tune frequency increases, the phase of the filter must also increase, e.g. the **phase response** must have a **positive slope** around the working point.



In this case the filter design can be made using the Matlab function *invfreqz()*

This function calculates the filter coefficients that best fit the required frequency response using the **least squares method**

The desired response is provided to *invfreqz()* by defining amplitude and phase at three different frequencies:

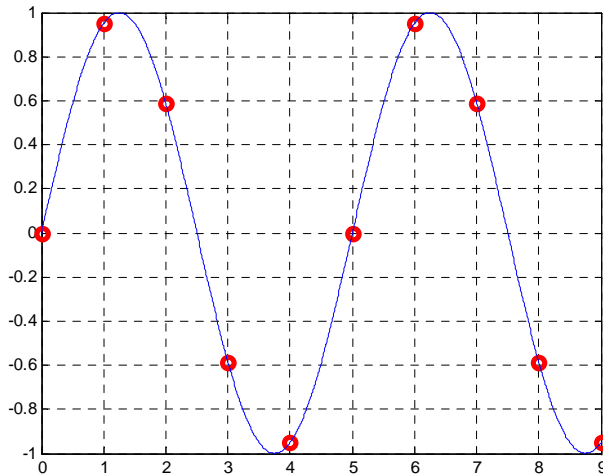
0, f_1 and f_2

Digital filter design: selective FIR filter

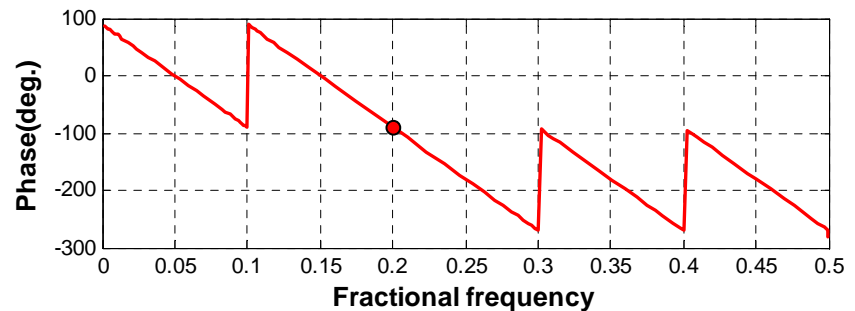
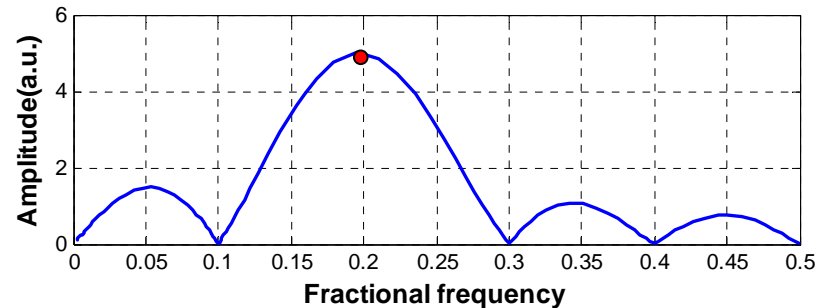
A FIR digital filter often used in longitudinal feedback systems is a "correlator" filter, which impulse response (the filter coefficients) is a **sampled sinusoid** with frequency equal to the bunch oscillation frequency (synchrotron tune)

This filter has a maximum of amplitude at the tune frequency and linear phase

The more filter coefficients we use the more selectivity we obtain, thus rejection of the unwanted spectrum components



Samples of the filter impulse response
(= filter coefficients)



Amplitude and phase response of the filter

Digital filter design: IIR filters

Using **IIR digital filters** opens the door to a number of design techniques allowing for additional interesting features of the controller that can be implemented

The disadvantage is a more difficult filter design and an increased complexity in the filter implementation

Examples of additional features:

- increase of the amplitude response selectivity for better noise rejection
- possibility to simultaneously stabilize different frequencies (ex. dipole/quadrupole, horizontal/vertical, ...)
- increase of the working frequency range with reduced performance degradation
- reduction of the amplitude response at frequencies that must not be fed back
-

Various techniques are used: i.e. **frequency domain design** and **model based design**

More sophisticated techniques can improve **performance** and **robustness** of the feedback under parametric changes of the accelerator and feedback components (i.e. optimal control, robust control, etc.)

Longitudinal feedback: down sampling

The synchrotron frequency is usually much lower than the betatron frequency: one complete synchrotron oscillation is accomplished in many machine turns (ex. 100)

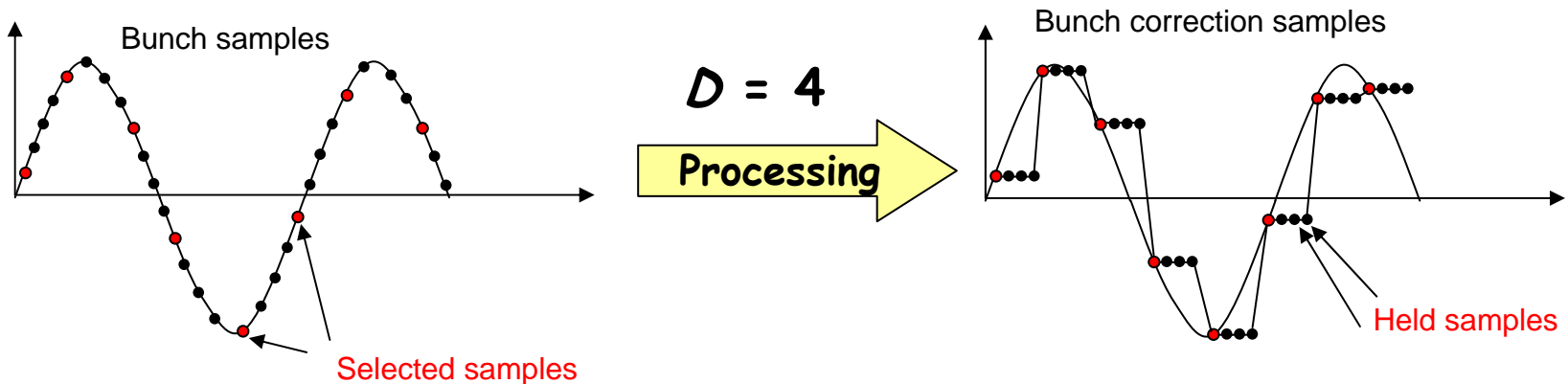
In order to be able to properly filter the bunch signal, **down sampling** is necessary

One out of D samples are taken: D is the **down sampling factor**

The processing is performed on the down sampled digital signal and the filter design is done in the down sampled frequency domain (enlarged by the down sampling factor D)

The **reduced data rate** also allows for more time available to perform filter calculations and more complex filters can therefore be implemented

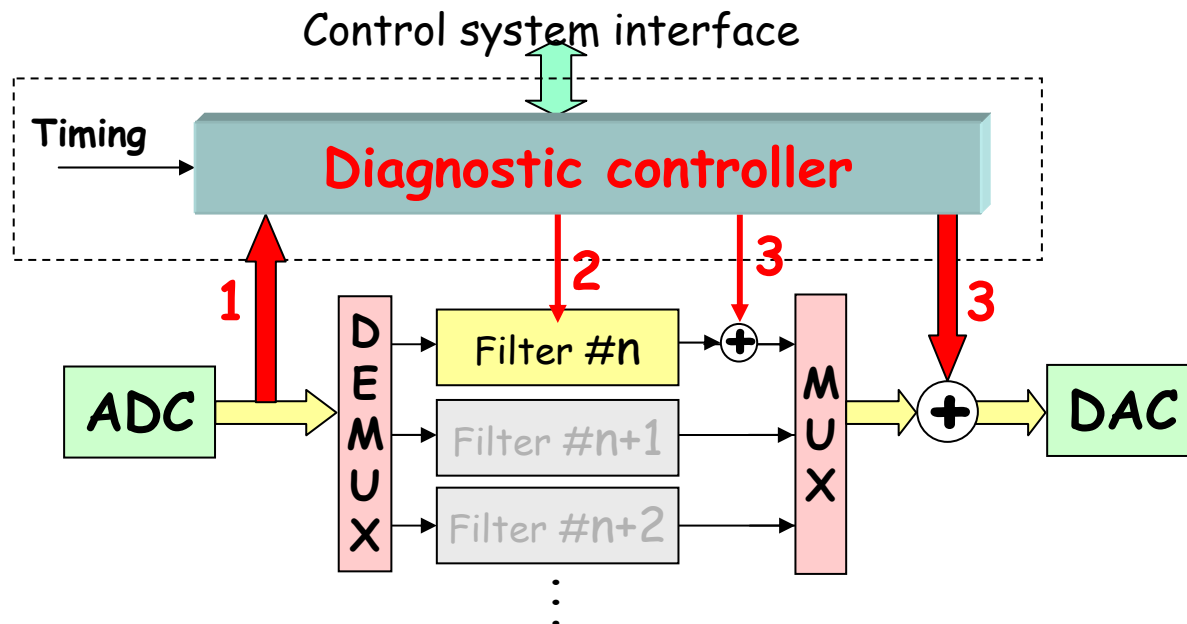
The correction signal at full rate is reconstructed by a **hold buffer** that keeps the same correction value for D turns



Diagnostic features

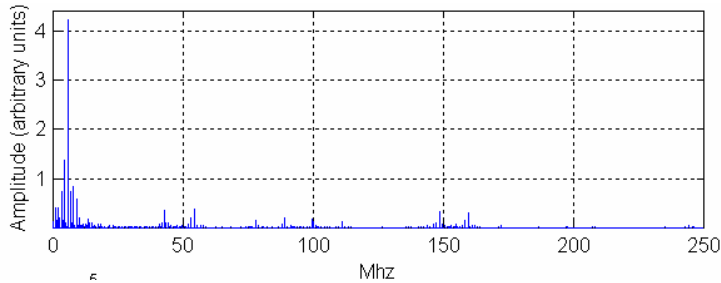
The feedback system can implement a number of diagnostic capabilities useful for both commissioning and optimization of the feedback system and for machine physics studies:

1. **Input data recording** for data analysis: acquisition of large number of samples in parallel with the feedback processing
2. **Changing filter parameters on the fly** with required timing and individually for each bunch: switching ON/OFF the feedback, generation of grow/damp transients, optimization of feedback performance
3. **Generation of output arbitrary waveforms**: multi-bunch and individually for each bunch

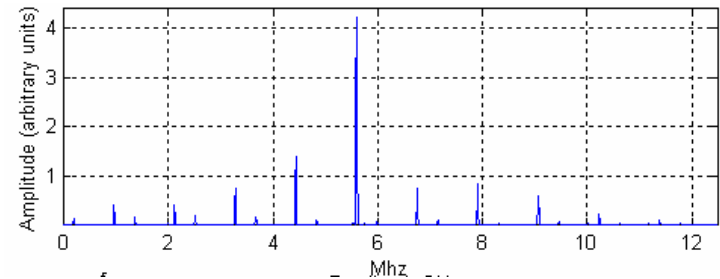


Diagnostic features: data recording

Ex. 1: acquisition of ADC data (500 MSamples/s) and spectrum made by FFT with Matlab

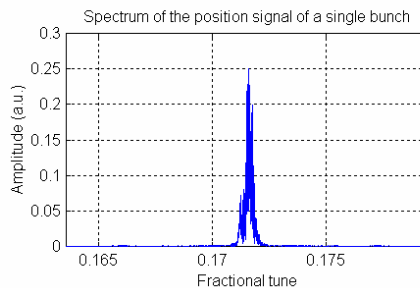
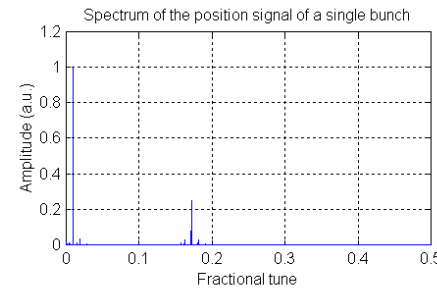
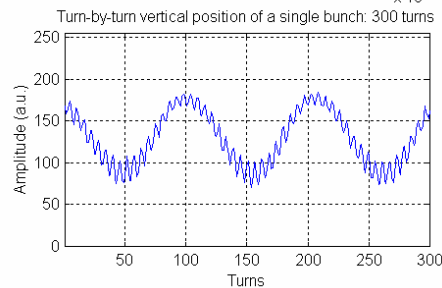
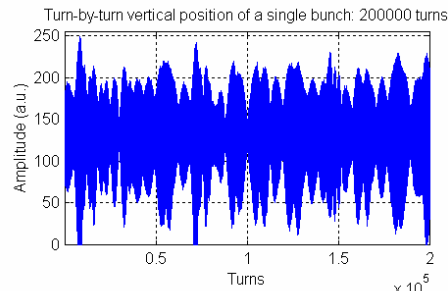


Spectrum of multi-bunch data from an unstable beam



Zoomed spectrum: side-bands of the revolution harmonics corresponding to the excited modes

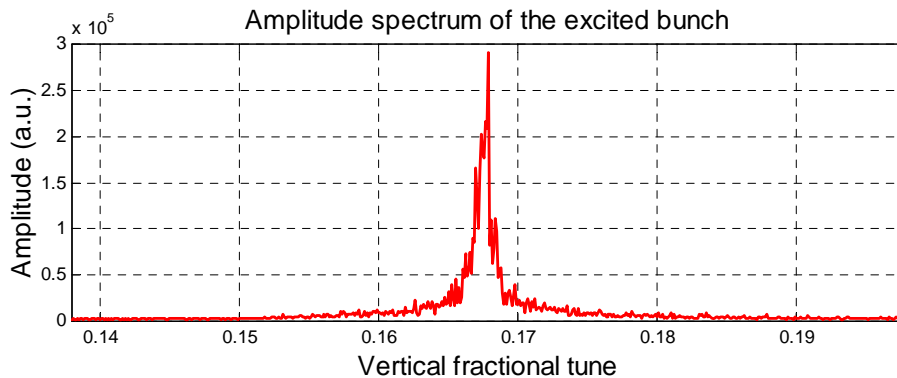
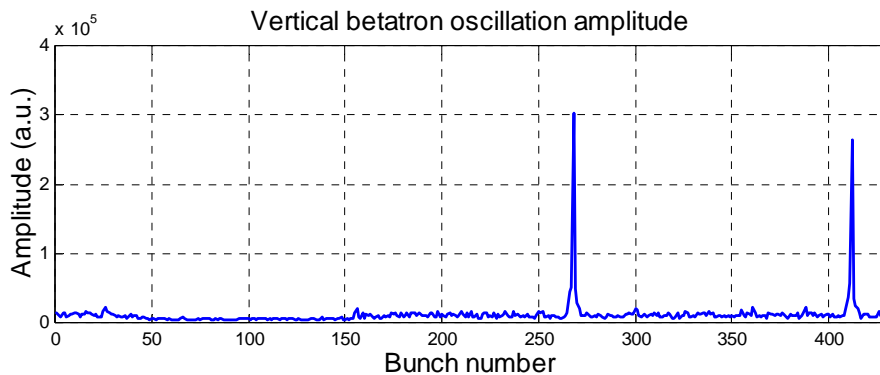
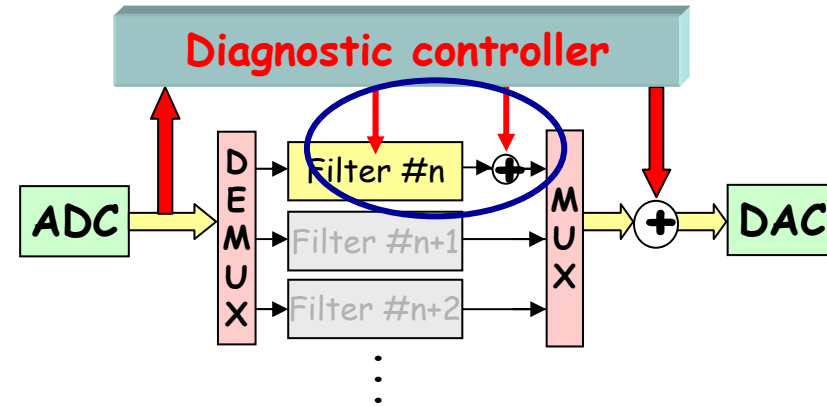
Ex. 2: acquisition of turn-by-turn samples of a given bunch and FFT with Matlab



Diagnostic features: excitation of individual bunches

The feedback loop is switched off on single bunches and the excitation signal is injected in place of the correction. Excitation signals can be:

- white (or pink) noise
- sinusoids

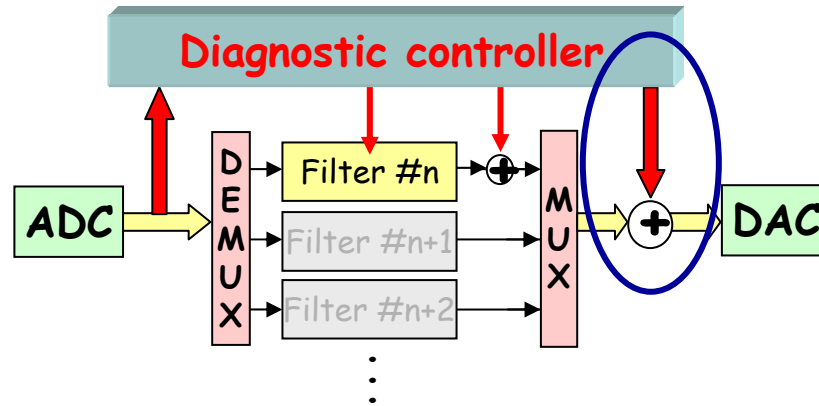


In this example two bunches are vertically **excited** with **pink noise** in a range of frequencies centered around the tune, while the feedback is applied on the other bunches. The spectrum of the excited bunch reveals a **peak at the tune frequency**

This technique is used to **measure the betatron tune** with almost no disturbance for machine operations

Diagnostic features: multi-bunch excitation

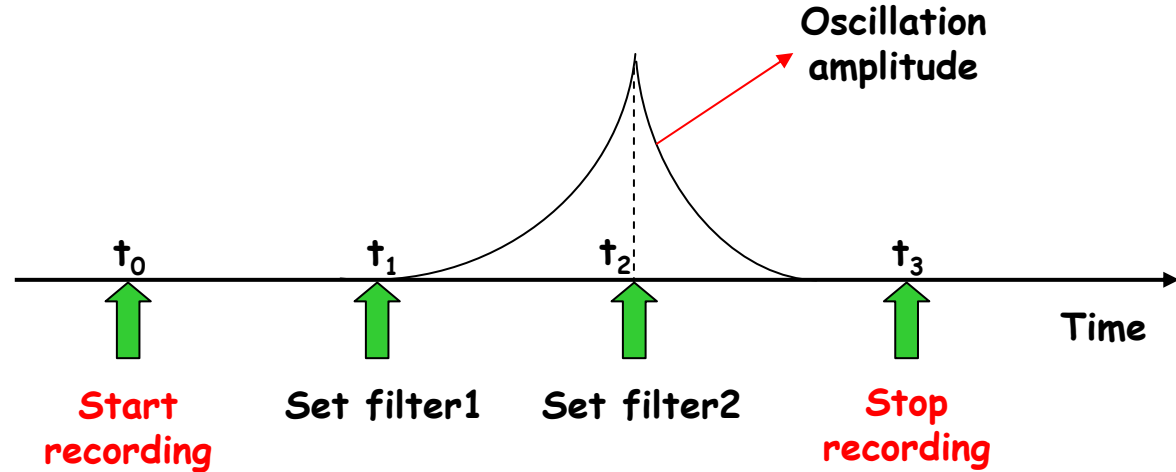
Interesting measurements can be performed by adding pre-defined signals to the output of the feedback



1. By adding a **sinusoid** at a given frequency, the corresponding beam **multi-bunch mode can be excited** to test the performance of the feedback
2. By adding an appropriate output signal and recording the feedback input data with filter coefficients set to zero, the **open loop transfer function** can be calculated
3. By adding an appropriate output signal and recording the feedback input data with filter coefficients set to the nominal values, the **closed loop transfer function** can be calculated

Diagnostic features: transient generation

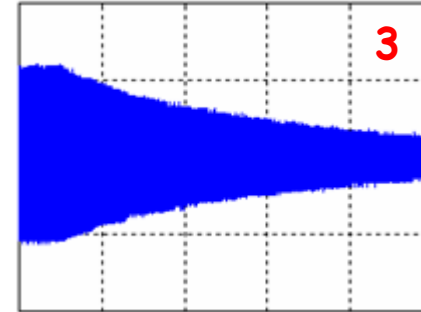
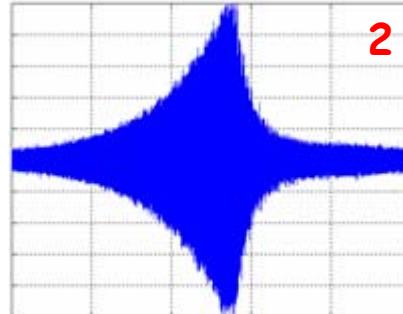
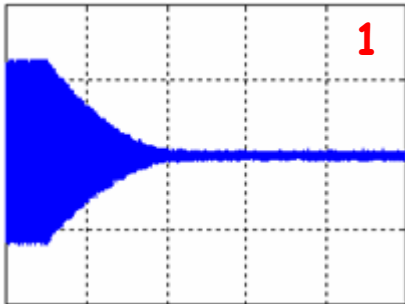
A powerful diagnostic application is the **generation of transients**. Transients can be generated by **changing the filter coefficients** accordingly to a predefined timing and by concurrently recording the oscillations of the bunches



Different types of transients can be generated, **damping times and growth rates** can be determined by exponential fitting of the transients:

1. free oscillations → FB on
2. FB on → FB off → FB on
3. Stable beam → positive FB on, anti-damping → FB off, natural damping

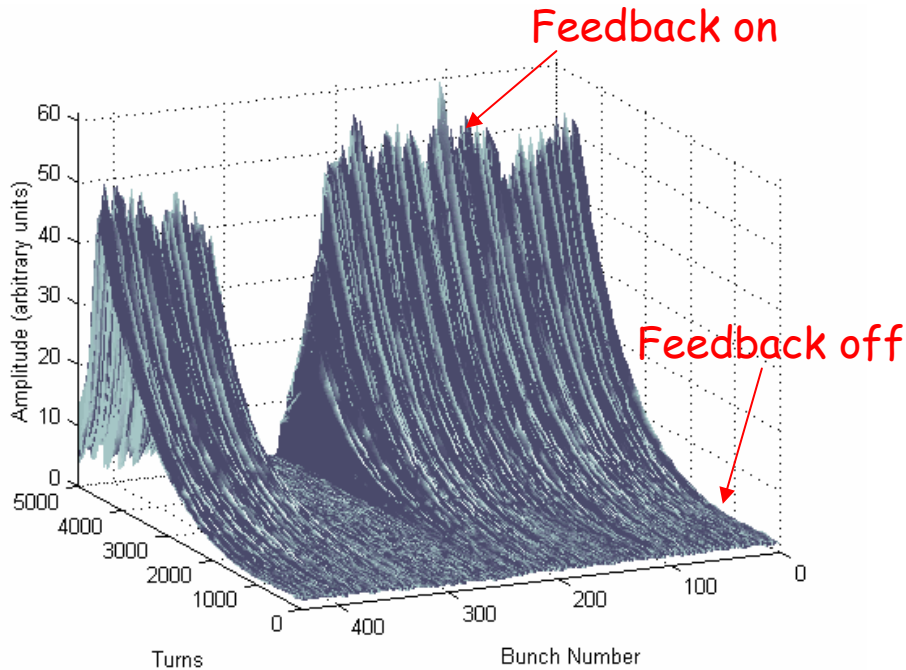
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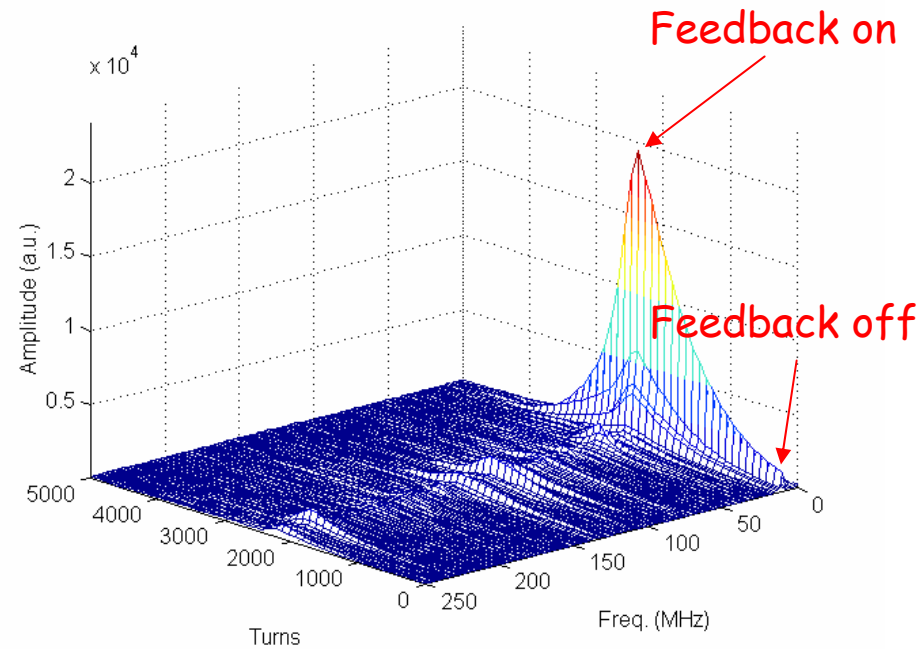
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Grow-damp transients : 3-D graphs

Grow-damp transients can be analyzed by recording the oscillation samples, processing the data, i.e. with Matlab, and displaying the results with 3-D graphs



Evolution of the bunches oscillation during a grow-damp transient



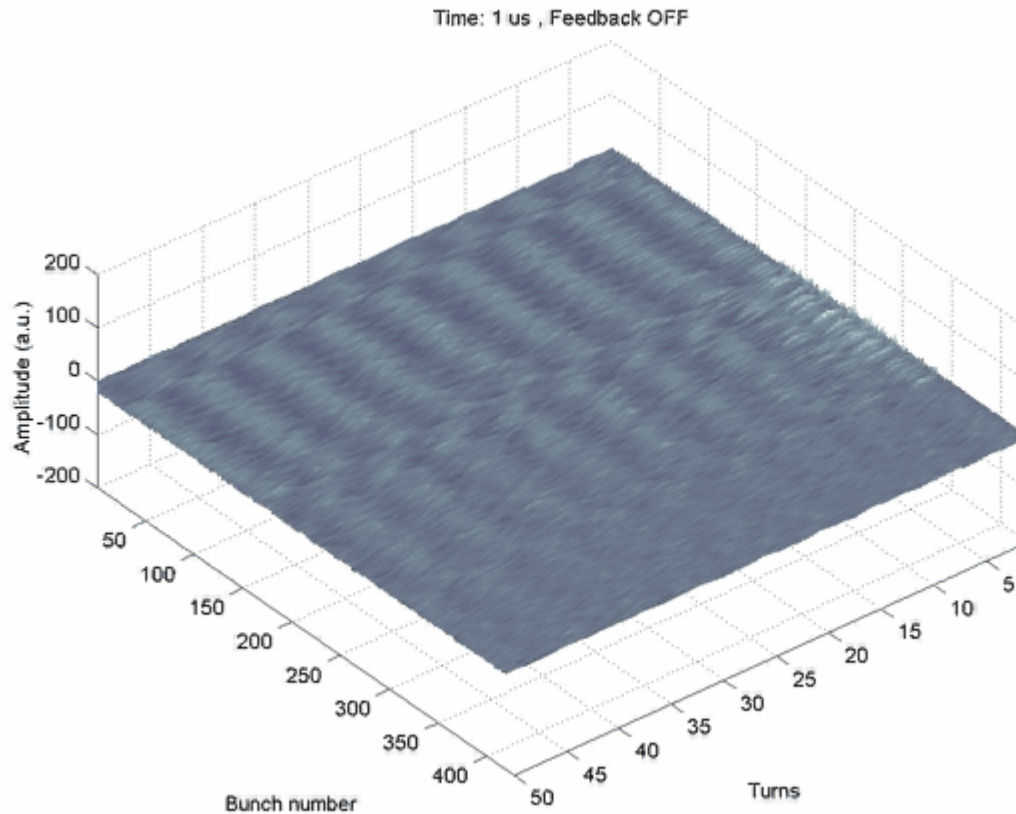
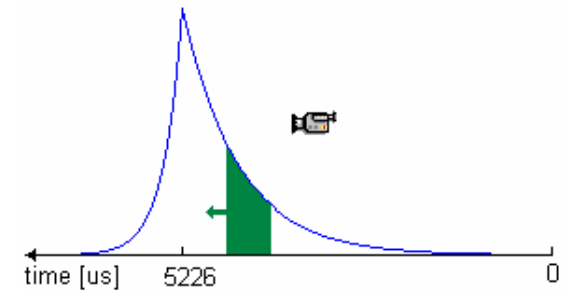
Evolution of the coupled-bunch unstable modes during a grow-damp transient

Grow-damp transients: real movies

'Movie' sequence:

1. Feedback OFF
2. Feedback ON after 5.2 ms

'Camera' view slice is 50 turns (about $43 \mu\text{s}$)

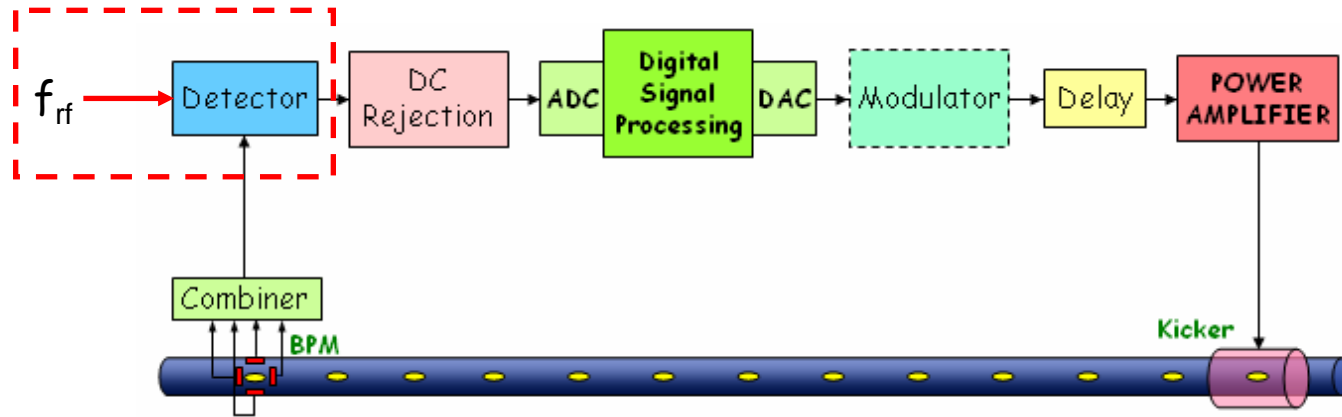


Transients generation is a useful tool to characterize and optimize the feedback system and also to study coupled-bunch modes and beam dynamics:

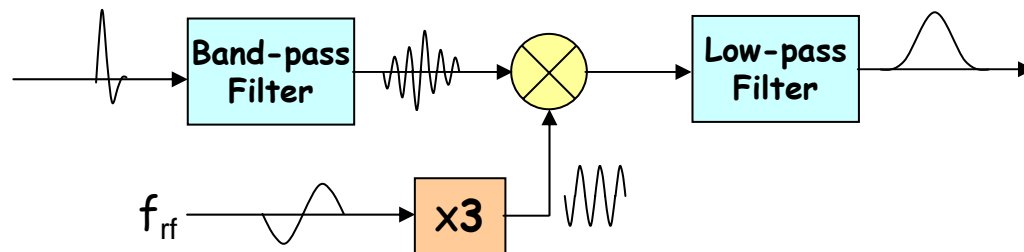
- **Feedback damping times**: can be used to characterize and optimize the feedback performance
- **Resistive and reactive response**: feedback not perfectly tuned has a reactive behavior (tune shift)
- **Modal analysis**: coupled-bunch mode complex eigenvalues, analysis of growth rates and tune shifts of the oscillation with exponential fit
- **Storage-ring impedance**: evaluation of the transverse/longitudinal machine impedance
- **Stable modes** : modes below the instability threshold can be studied
- **Bunch train studies**: different behavior of bunches in the train to study the origins of the coupled-bunch modes
- **Phase space analysis**: analysis of the phase evolution of unstable coupled-bunch modes

Feedback optimization: detector phase

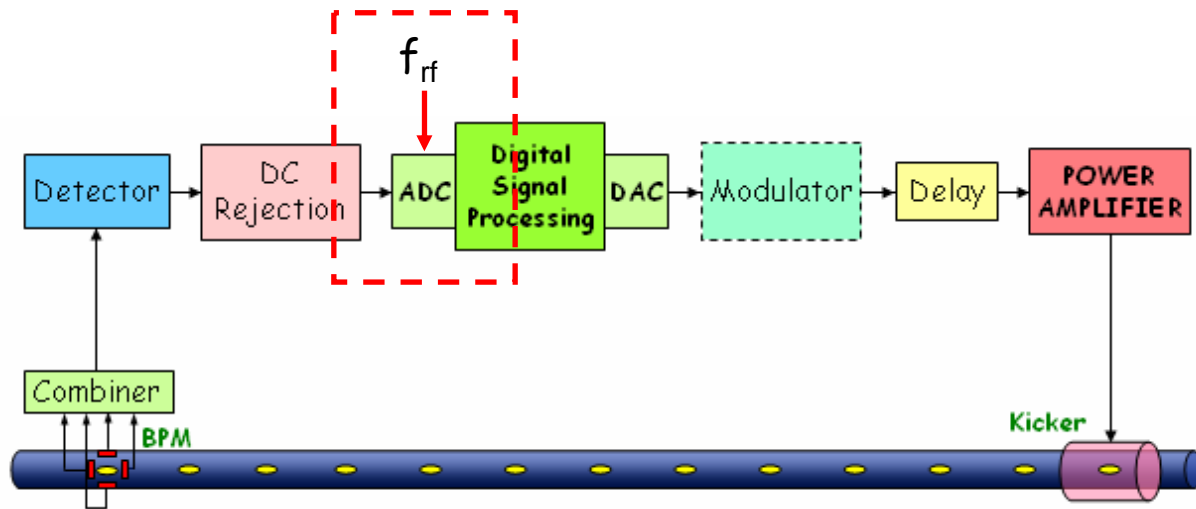
A number of adjustments have to be carried out after the feedback is set up to make the system work with optimized performance



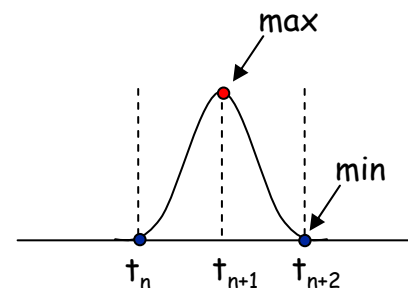
Detector demodulation phase: the "local oscillator" signal derived from the bunch frequency must be adjusted in order to be in-phase (amplitude demodulation) or in quadrature (phase demodulation) with the bunch signal. The optimal phase can be found for example with the analysis of the data acquired by the ADC from an unstable beam and by maximizing the detected bunch oscillation amplitude



Feedback optimization: sampling clock



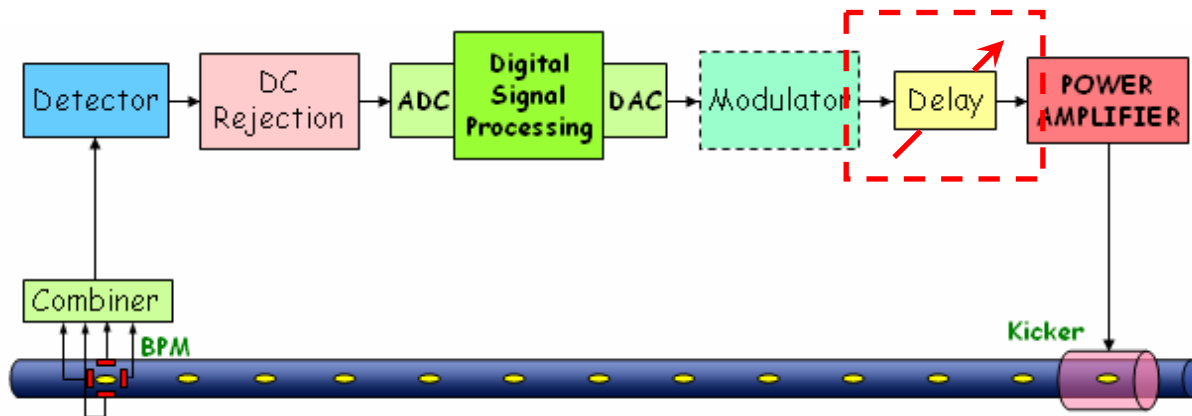
ADC sampling clock: the phase of the clock must be adjusted to sample the "pulse" of every bunch on the top. This task is usually carried out with the machine filled with a single bunch: the optimum clock phase maximizes the amplitude of the samples of the filled bucket and minimizes the amplitude of the samples of the adjacent empty buckets



Feedback optimization: delay line

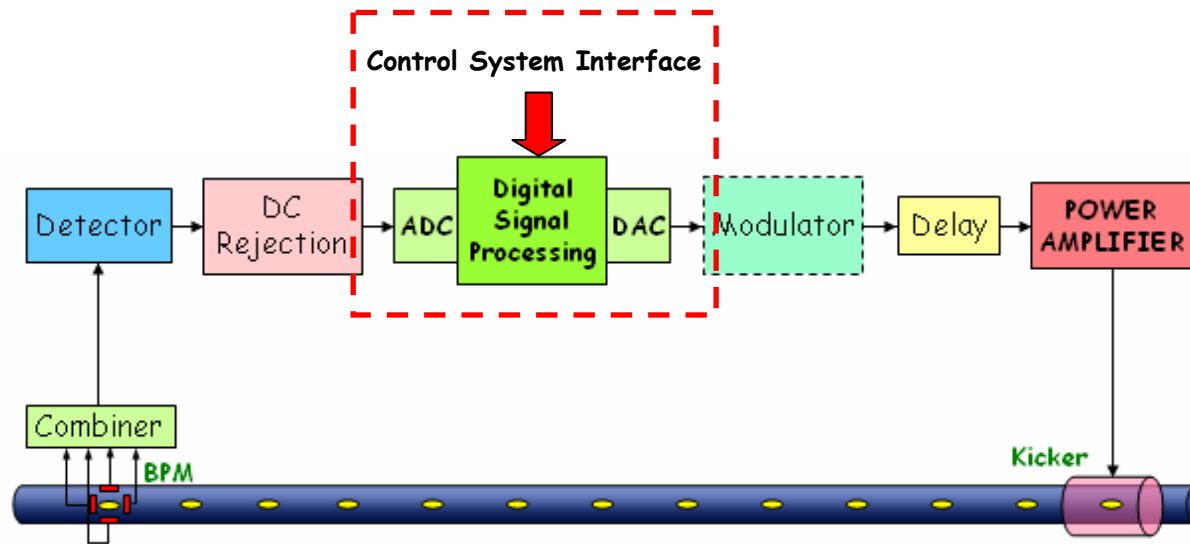
Delay line: must be properly set in order to kick each bunch with the correction signal calculated for that bunch. The adjustment can be done in two phases using the feedback system:

1. **Coarse adjustment** (resolution $< T_{rf}$): excite a single stable bunch (ex. with white noise or with a sinusoid at the tune frequency) and adjust the delay until the bunch we wanted to excite is really seen excited by analyzing the acquired data
2. **Fine adjustment** (resolution $< T_{rf}/100$): optimizing the feedback performance. Maximum reduction of coupled-bunch modes (natural or artificially excited by the use of the feedback system), minimum damping time in grow/damp transients, ...

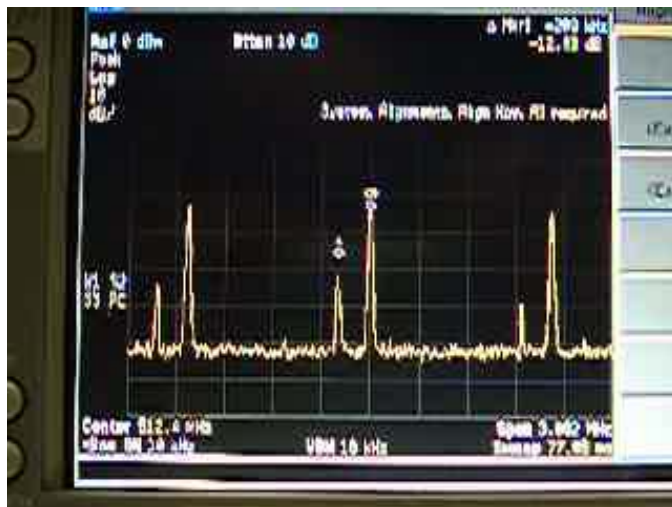
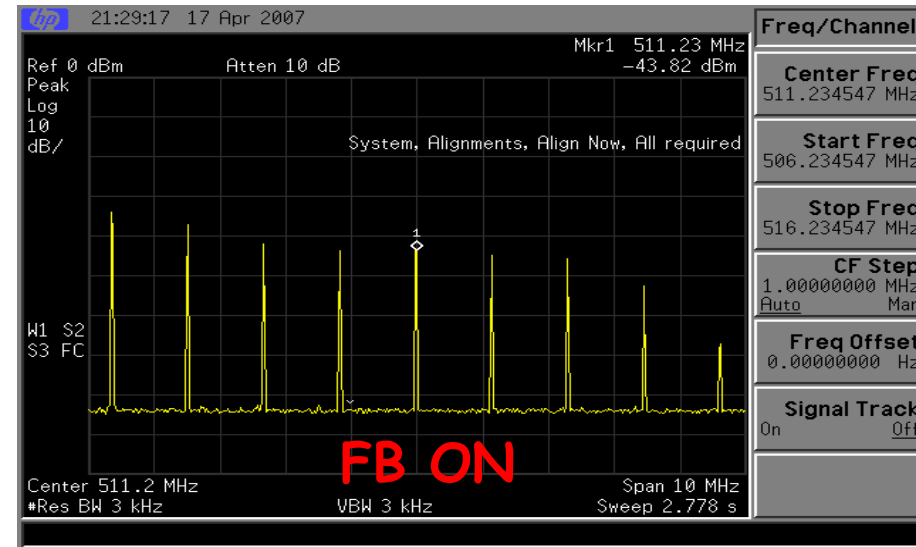
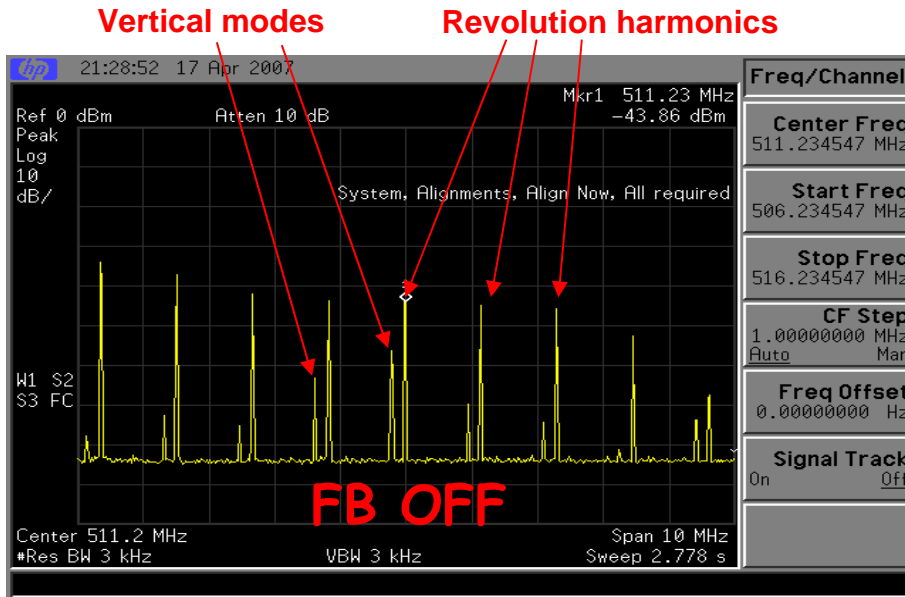


Feedback optimization: digital filter

Digital filter: the digital filter is designed based on given requirements (phase and amplitude response). A **fine optimization** can be done with the **real machine** by adjusting the basic parameters (phase at the tune and gain) and trying to maximize the feedback performance (maximum reduction of coupled-bunch modes). A careful analysis of grow/damp transients gives useful information on the feedback behavior with the objective to find optimal working conditions: evaluation of damping time and reactive component of the feedback, phase space analysis, ...

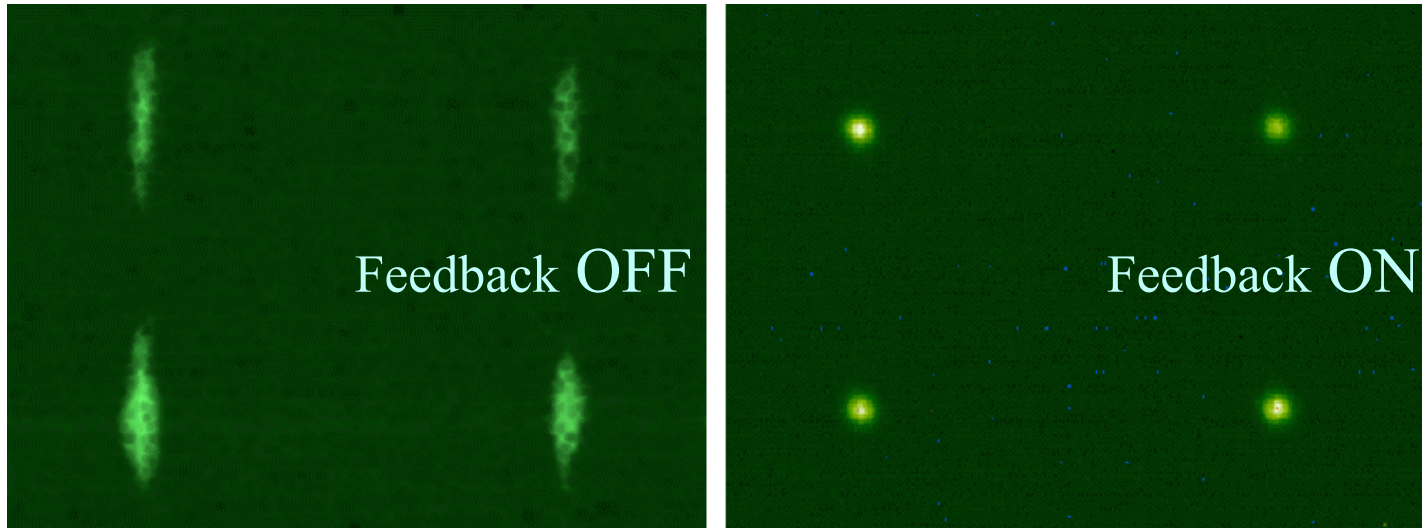


Effects of the feedback: beam spectrum



Spectrum analyzer connected to a stripline pickup: observation of vertical instabilities. The sidebands corresponding to vertical coupled-bunch modes disappear as soon as the transverse feedback is activated

Effects of the feedback: beam transverse profile



Pin-hole camera images (courtesy of Micha Dehler SLS/PSI)

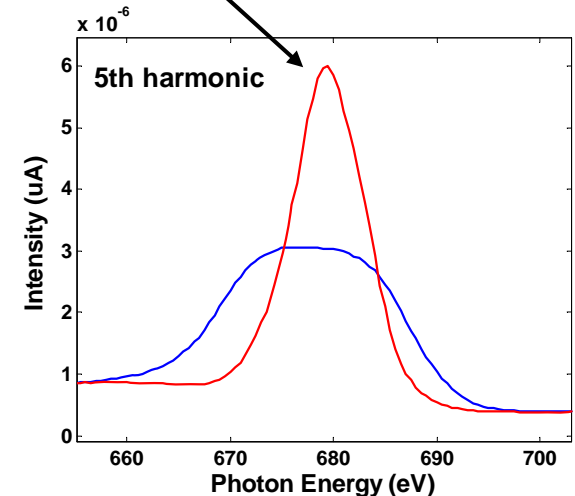
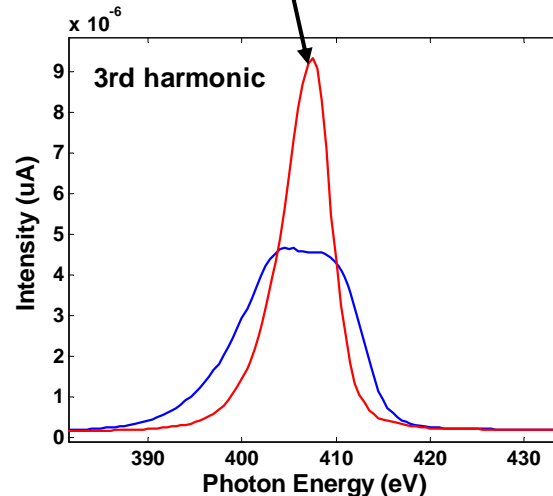
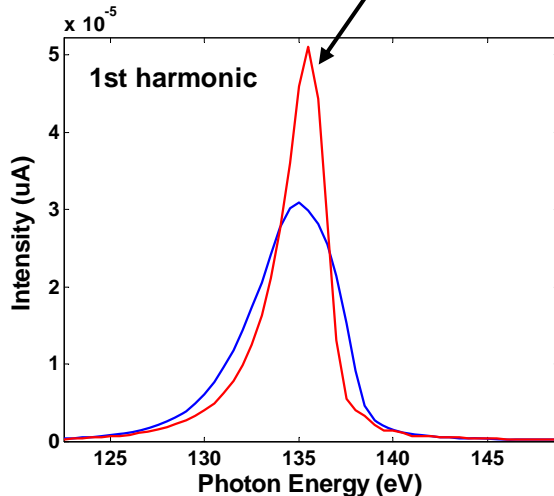
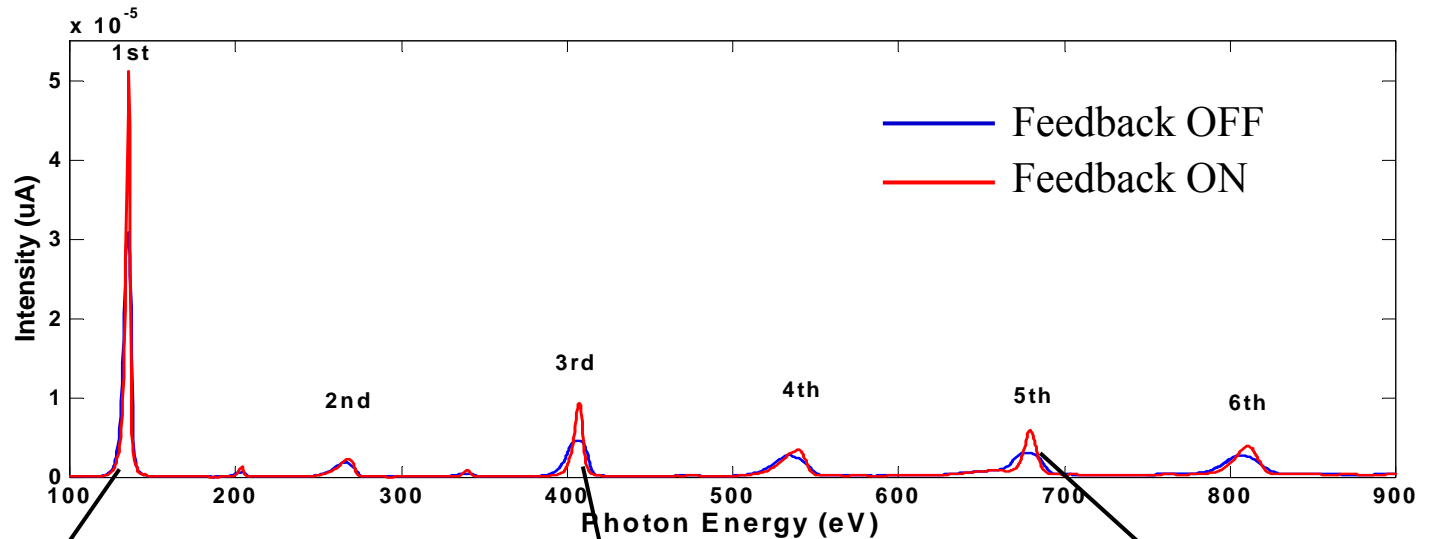
Synchrotron Radiation Profile Monitor (SRPM) showing the reduction of the vertical beam dimension when the transverse feedback is switched on (Elettra)



Effects of the feedback: photon beam spectra

Effects on the synchrotron light: spectrum of photons produced by an undulator
 The spectrum is noticeably improved when vertical instabilities are damped by the feedback

SuperESCA
 beamline at
 Elettra



- ↘ Feedback systems are indispensable tools to cure multi-bunch instabilities in storage rings
- ↘ Technology advances in digital electronics allow implementing digital systems
- ↘ Digital signal processing theory widely used to design and implement filters as well as to analyze data acquired by the feedback
- ↘ Feedback systems not only for closed loop control but also as powerful diagnostic tools
- ↘ Full potentialities of digital feedback systems still to be exploited:
 - ↘ improvement of feedback performance
 - ↘ studies of beam dynamics



- Herman Winick, "Synchrotron Radiation Sources", World Scientific
- Many papers about coupled-bunch instabilities and multi-bunch feedback systems (KEK, SPring-8, DaΦne, ALS, PEP-II, ESRF, Elettra, SLS, CESR, DESY, PLS, Bessy, SRRC, ...)
- Special mention for the articles of the SLAC team (J.Fox, D.Teytelman, S.Prabhakar, etc.) about development of feedback systems and studies of coupled-bunch instabilities