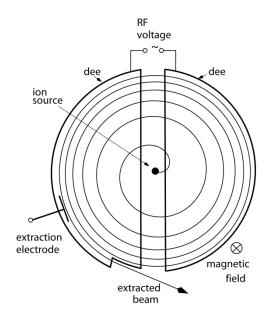


Cyclotrons - Outline

- the classical cyclotron
 history of the cyclotron, basic concepts and scalings,
 classification of cyclotron-like accelerators
- separated sector cyclotrons
 focusing in Thomas-cyclotrons, spiral angle, classical extraction:
 pattern/stepwidth, transv./long. space charge
- cyclotron subsystems
 extraction schemes, RF resonators, magnets, vacuum issues,
 instrumentation
- applications and examples of existing cyclotrons TRIUMF, RIKEN SRC, PSI Ring, PSI medical cyclotron
- discussion
 - Classification of circular accelerators Pro's and Con's of cyclotrons for different applications



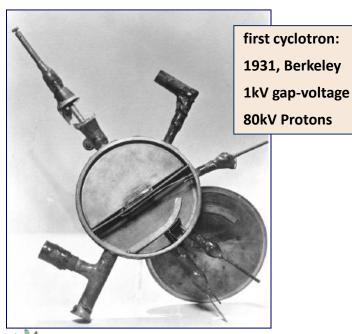
The Classical Cyclotron

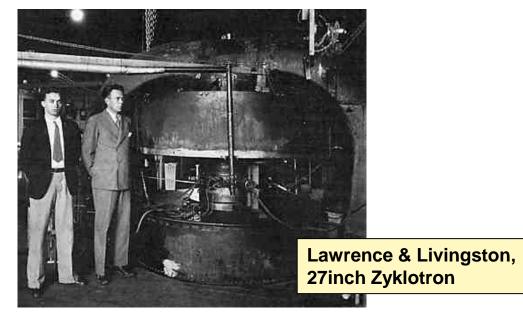


two capacitive electrodes "Dees", two gaps per turn internal ion source homogenous B field constant revolution time (for low energy, $\gamma \sim 1$)

powerful concept:

- → simplicity, compactness
- continuous injection/extraction
- multiple usage of accelerating voltage







cyclotron frequency and K value

• cyclotron frequency (homogeneous) B-field:

$$\omega_c = \frac{eB}{\gamma m_0}$$

- cyclotron K-value:
- ightarrow K is the **kinetic energy reach** for protons **from bending strength** in non-relativistic approximation: $K = \frac{e^2}{2m_0}(B\rho)^2$
- \rightarrow K can be used to rescale the energy reach of protons to other charge-to-mass ratios:

$$\frac{E_k}{A} = K \left(\frac{Z}{A}\right)^2$$

 \rightarrow K in [MeV] is often used for naming cyclotrons

examples: K-130 cyclotron / Jyväskylä

cyclone C230 / IBA



classical cyclotron - isochronicity and scalings

continuous acceleration \rightarrow revolution time must stay constant, though E_k , R vary

magnetic rigidity:

$$BR = \frac{p}{e} = \beta \gamma \frac{m_0 c}{e}$$

orbit radius from isochronicity:

$$R = \frac{c}{\omega_c} \beta = R_{\infty} \beta$$
$$= \frac{c}{\omega_c} \sqrt{1 - \gamma^{-2}}$$

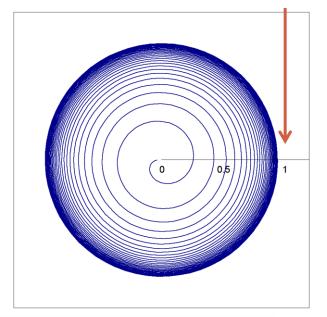
deduced scaling of B:

$$R \propto \beta; BR \propto \beta \gamma \longrightarrow B(R) \propto \gamma(R)$$

thus, to keep the isochronous condition, B must be raised in proportion to $\gamma(R)$; this contradicts the focusing requirements (discussed later)

radius increment per turn
decreases with increasing energy
→ extraction becomes more and
more difficult at higher energies

$$R_{\infty} = R/\beta$$





field index

the field index describes the (normalized) radial slope of the bending field:

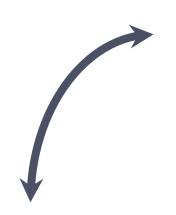
$$k = \frac{R}{B} \frac{dB}{dR}$$
 from isochronous condition:
$$B \propto \gamma, \ R \propto \beta$$

$$= \frac{\beta}{\gamma} \frac{d\gamma}{d\beta}$$

$$= \gamma^2 - 1$$



relativistic quantities in the context of cyclotrons

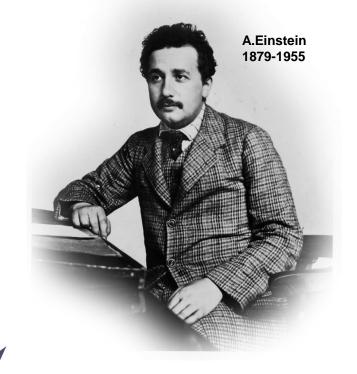


energy

$$E = \gamma E_0$$

kinetic energy:

$$E_k = (\gamma - 1)E_0$$



velocity

$$v = \beta c$$



revolution time:

$$\tau = \frac{2\pi R}{\beta c}$$

momentum

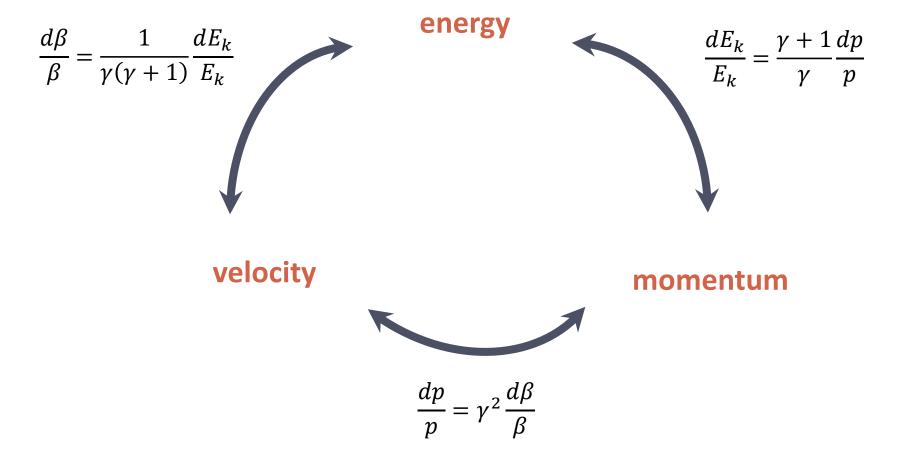
$$p = \beta \gamma m_0 c$$

bending strength:

$$BR = \beta \gamma \frac{m_0 c}{e}$$

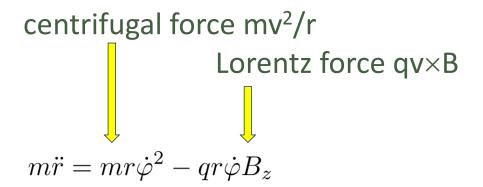


useful for calculations – differential relations





equation of motion in a classical cyclotron



focusing: consider small deviations x from beam orbit R (r = R+x):

$$\ddot{x} + \frac{q}{m}vB_z(R+x) - \frac{v^2}{R+x} = 0,$$

$$\ddot{x} + \frac{q}{m}v\left(B_z(R) + \frac{\mathrm{d}B_z}{\mathrm{d}R}x\right) - \frac{v^2}{R}\left(1 - \frac{x}{R}\right) = 0,$$

$$\ddot{x} + \omega_c^2(1+k)x = 0.$$

using:
$$\omega_{\rm c} = qB_z/m \approx v/R$$
, $r\dot{\varphi} \approx v$, $k = \frac{R}{B} \frac{dB}{dR}$



betatron tunes in cyclotrons

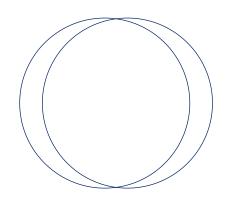
thus in radial plane:

$$\omega_r = \omega_c \sqrt{1+k} = \omega_c \nu_r$$

$$\nu_r = \sqrt{1+k}$$

$$\approx \gamma$$

note: simple case for k = 0: $v_r = 1$ (one circular orbit oscillates w.r.t the other)



using Maxwell to relate B_z and B_R :

$$rot \vec{B} = \frac{dB_R}{dz} - \frac{dB_z}{dR} = 0$$

in vertical plane:

$$\nu_z = \sqrt{-k}$$

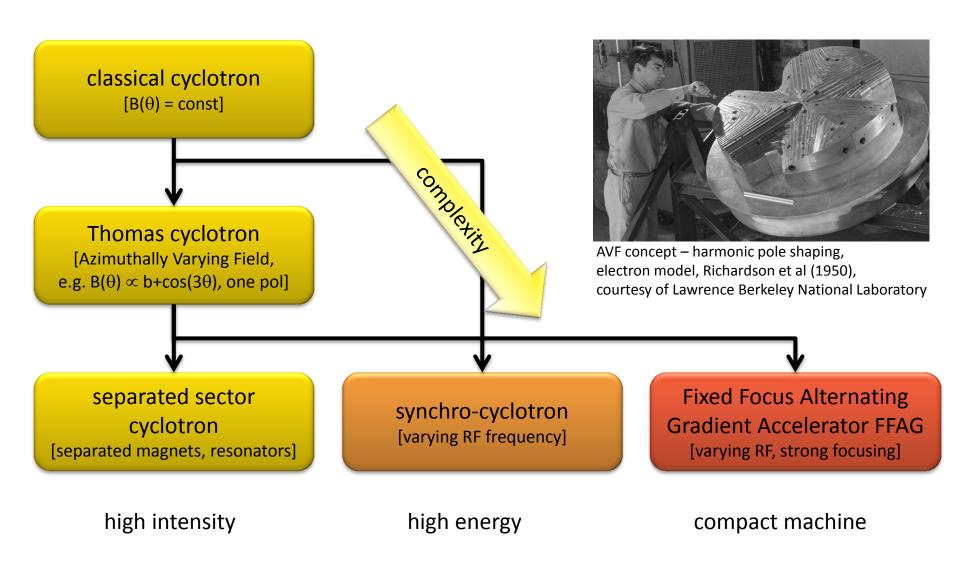


k<0 to obtain vertical focus.

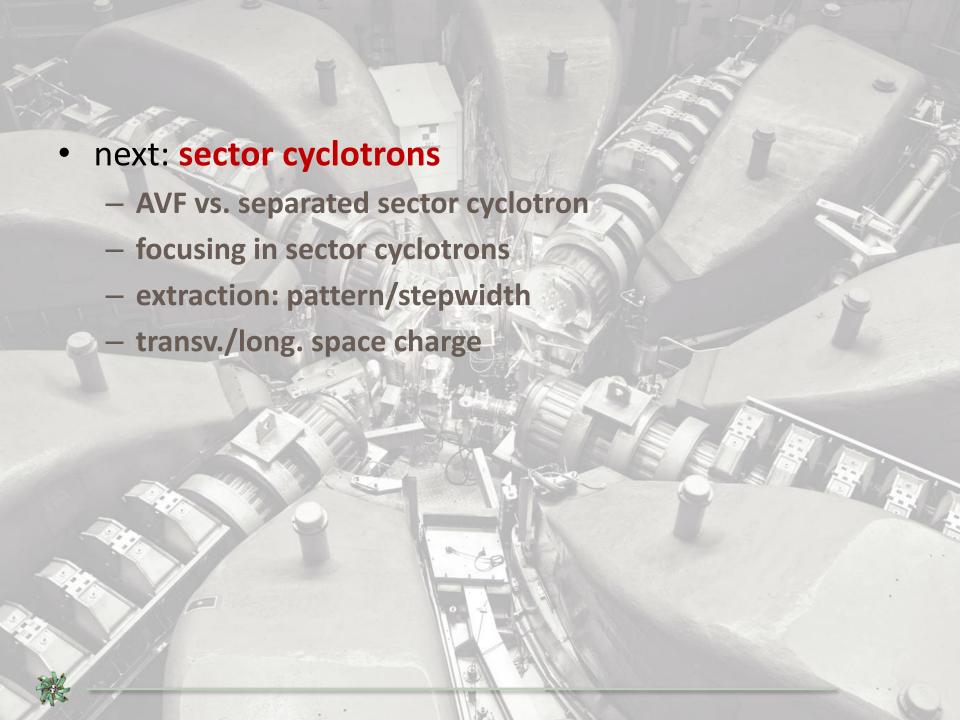
thus: in classical cyclotron k < 0 required; however this violates isochronous condition $k = \gamma^2 - 1 > 0$



classification of cyclotron like accelerators







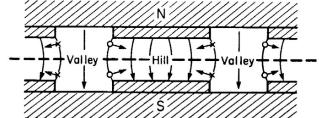
focusing in sector cyclotrons

hill / valley variation of magnetic field (Thomas focusing) makes it possible to design cyclotrons for higher energies

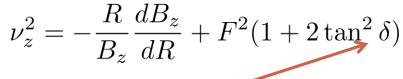
Flutter factor:

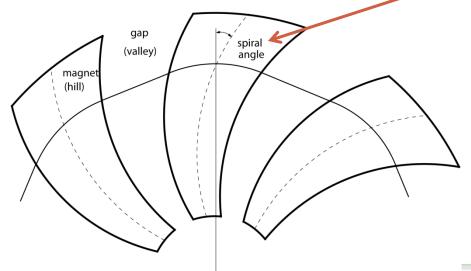
$$F^2 = \frac{\overline{B_z^2} - \overline{B_z}^2}{\overline{B_z}^2}$$

with flutter and additional spiral angle of bending field:



[illustration of focusing at edges]





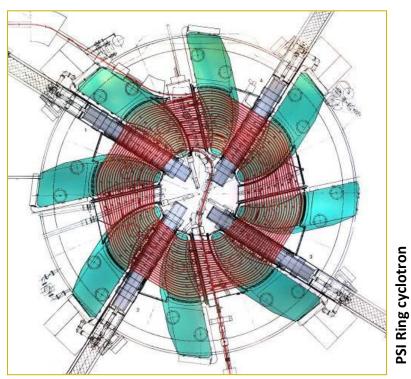


Azimuthally Varying Field vs. Separated Sector Cyclotrons



PSI/Varian comet: 250MeV sc. medical cyclotron

- AVF = single pole with shaping
- often spiral poles used
- internal source possible
- D-type RF electrodes, rel. low energy gain
- compact, cost effective
- depicted Varian cyclotron: 80% extraction efficiency; not suited for high power



- modular layout, larger cyclotrons possible, sector magnets, box resonators, stronger focusing, injection/extraction in straight sections
- external injection required, i.e. preaccelerator
- **box-resonators** (high voltage gain)
- high **extraction efficiency** possible:

e.g. PSI: $99.98\% = (1 - 2 \cdot 10^{-4})$



derivation of turn separation in a cyclotron

starting point: bending strength

- → compute total log.differential
- \rightarrow use field index $k = R/B \cdot dB/dR$

$$BR = \sqrt{\gamma^2 - 1} \frac{m_0 c}{e}$$

$$\frac{dB}{B} + \frac{dR}{R} = \frac{\gamma d\gamma}{\gamma^2 - 1}$$

$$\frac{dR}{d\gamma} = \frac{\gamma R}{\gamma^2 - 1} \frac{1}{1 + k}$$

radius change per turn

$$rac{dn_t}{dn_t} = rac{d\gamma}{d\gamma} rac{dn_t}{dn_t}$$
 $= rac{U_t}{m_0 c^2} rac{\gamma R}{(\gamma^2 - 1)(1 + k)}$ isochronicity not conserved (last turns) U_t R

 $[U_t = \text{energy gain per turn}]$

 $= \frac{U_t}{m_0 c^2} \frac{R}{(\gamma^2 - 1)\gamma}$ isochronicity conserved (general scaling)



turn separation - discussion

for clean extraction a large stepwidth (turn separation) is of utmost importance; in the PSI Ring most efforts were directed towards maximizing the turn separation

general scaling at extraction:

$$\Delta R(R_{\rm extr}) = \frac{U_t}{m_0 c^2} \frac{R_{\rm extr}}{(\gamma^2 - 1) \gamma}$$
 • limited energy (< 1GeV) • large radius $R_{\rm extr}$ • high energy gain U_t

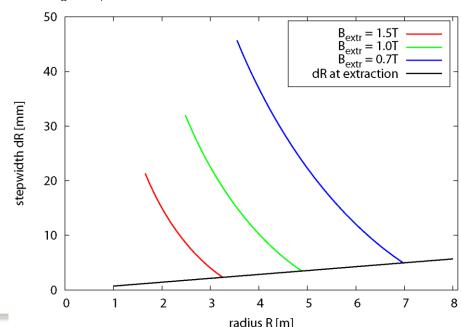
desirable:

- high energy gain U_t

scaling during acceleration:

$$\frac{dR}{dn_t} \approx \frac{U_t}{m_0 c^2} \frac{R}{\beta^2} \to \Delta R(R) \propto \frac{1}{R}$$

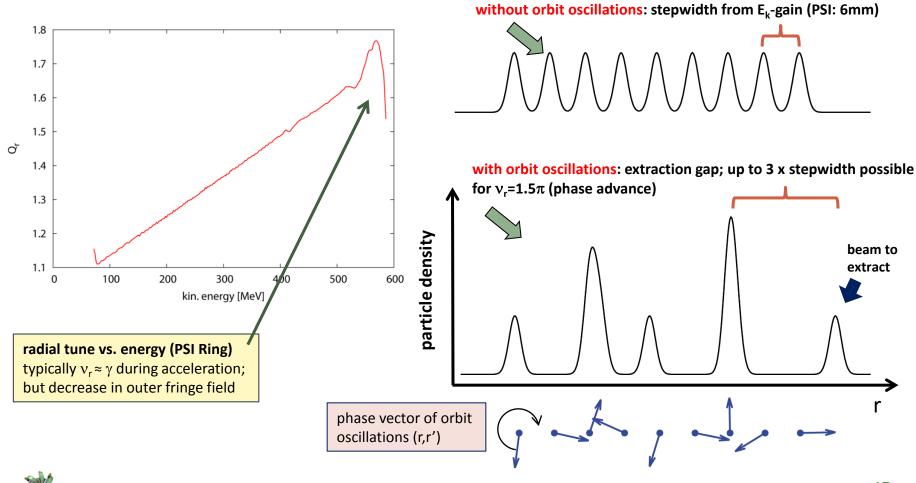
illustration: stepwidth vs. radius in cyclotrons of different sizes; 100MeV inj \rightarrow 800MeV extr





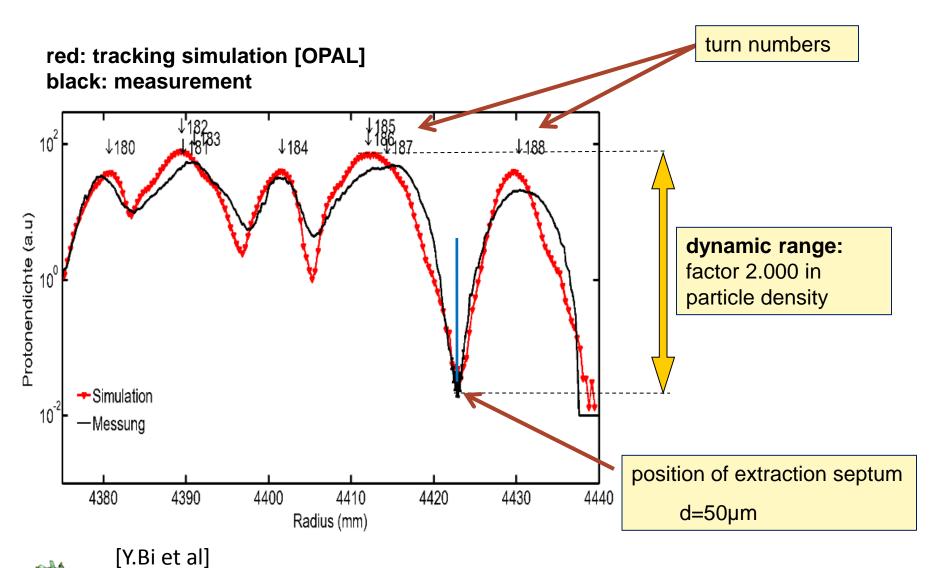
extraction with off-center orbits

betatron oscillations around the "closed orbit" can be used to increase the radial stepwidth by a factor 3!





extraction profile measured at PSI Ring Cyclotron

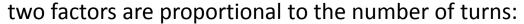




longitudinal space charge

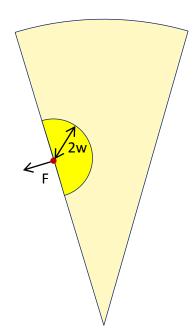
sector model (W.Joho, 1981):

- → accumulated energy spread transforms into transverse tails
- consider rotating uniform sectors of charge (overlapping turns)
- test particle "sees" only fraction of sector due to shielding of vacuum chamber with gap height 2w



- 1) the charge density in the sector
- 2) the time span the force acts

$$\Delta U_{sc} = \frac{8}{3} e I_p Z_0 \ln \left(4 \frac{w}{a} \right) \cdot \frac{n_{\text{max}}^2}{\beta_{\text{max}}} \approx 2.800\Omega \cdot e I_p \cdot \frac{n_{\text{max}}^2}{\beta_{\text{max}}}$$



derivation see: High Intensity Aspects of Cyclotrons, ECPM-2012, PSI

in addition:

- 3) the inverse of turn separation at extraction: $\frac{1}{\Delta R_{
 m extr}} \propto n_{
 m max}$
 - ightharpoonup thus the attainable current at constant losses scales as $n_{\rm max}^{-3}$



longitudinal space charge; evidence for third power law

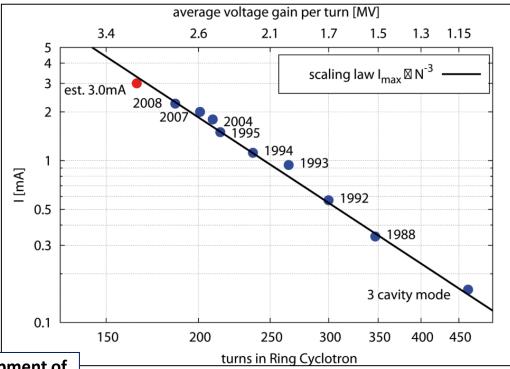
 at PSI the maximum attainable current indeed scales with the third power of the turn number

maximum energy gain per turn is of utmost importance in this type of high

intensity cyclotron

→ with constant losses at the extraction electrode the maximum attainable current indeed scales as:

$$I_{\rm max} \propto n_t^{-3}$$



historical development of current and turn numbers in PSI Ring Cyclotron



transverse space charge

with overlapping turns use current sheet model!

vertical force from space charge:
$$F_y = \frac{n_v e^2}{\epsilon_0 \gamma^2} \cdot y, \ n_v = \frac{N}{(2\pi)^{\frac{3}{2}} \sigma_y D_f R \Delta R}$$
 [constant charge density, $D_{\rm f} = I_{\rm avg}/I_{\rm peak}$]

focusing force:

$$F_y = -\gamma m_0 \omega_c^2 \nu_{y0}^2 \cdot y$$

thus, eqn. of motion:

$$\ddot{y} + \left(\omega_c^2 \nu_{y0}^2 - \frac{n_v e^2}{\epsilon_0 m_0 \gamma^3}\right) y = 0$$

→ equating space charge and focusing force delivers an intensity limit for loss of focusing!

$$\Delta \nu_y \approx -n_v \frac{2\pi r_p R^2}{\beta^2 \gamma^3 \nu_{y0}}$$

$$\approx -\sqrt{2\pi} \frac{r_p R}{e\beta c \nu_{y0} \sigma_z} \frac{m_0 c^2}{U_t} I_{\text{avg}}$$



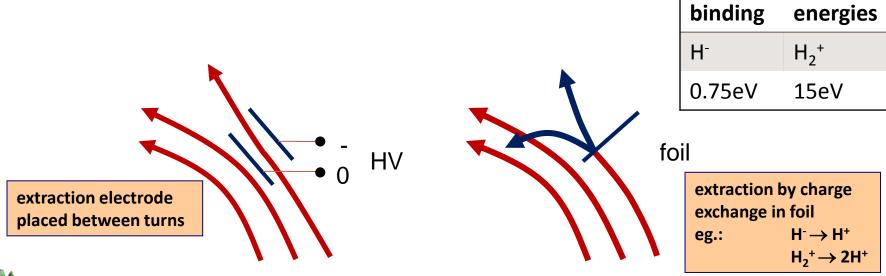
next: cyclotron subsystems

- extraction schemes
- RF systems/power efficiency
- cyclotron magnets
- comments on vacuum
- specific instrumentation



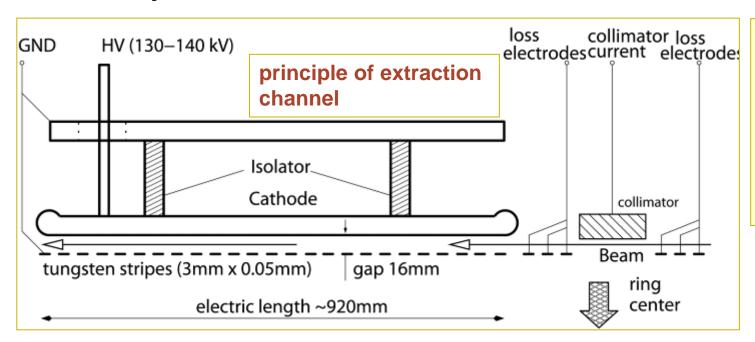
injection/extraction schemes

- deflecting element should affect just one turn, not neighboured turn → critical, cause of losses
- often used: electrostatic deflectors with thin electrodes
- alternative: charge exchange, stripping foil; accelerate H⁻ or H₂⁺ to extract protons (problem: significant probability for unwanted loss of electron; Lorentz dissociation: B-field low, scattering: vacuum 10⁻⁸mbar)





injection/extraction with electrostatic elements



parameters extraction chan.:

 $E_k = 590 MeV$

E = 8.8 MV/m

 θ = 8.2 mrad

 ρ = 115 m

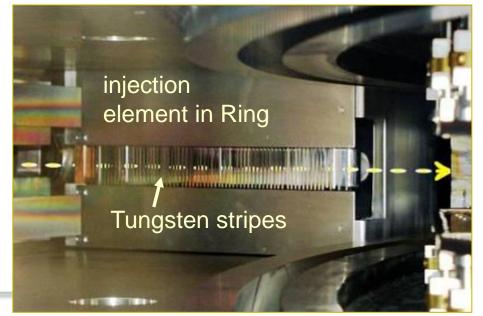
U = 144 kV

major loss mechanism is scattering in 50μm electrode!

electrostatic rigidity:

$$E\rho = \frac{\gamma + 1}{\gamma} \frac{E_k}{q}$$

$$\theta = \frac{qlE}{E_k} \frac{\gamma}{\gamma + 1}$$

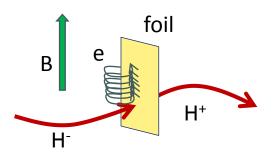




extraction foil

- thin foil, for example carbon, removes the electron(s) with high probability
- new charge state of ion brings it on a new trajectory → separation from circulating beam
- lifetime of foil is critical due to heating, fatigue effects, radiation damage
- conversion efficiencies, e.g. generation of neutrals, must be considered carefully

electrons removed from the ions spiral in the magnetic field and may deposit energy in the foil



How much power is carried by the electrons?

 \rightarrow velocity and thus γ are equal for p and e

$$E_{k} = (\gamma - 1)E_{0}$$

$$\to E_{k}^{e} = \frac{E_{0}^{e}}{E_{0}^{p}}E_{k}^{p} = 5.4 \cdot 10^{-4}E_{k}^{p}$$

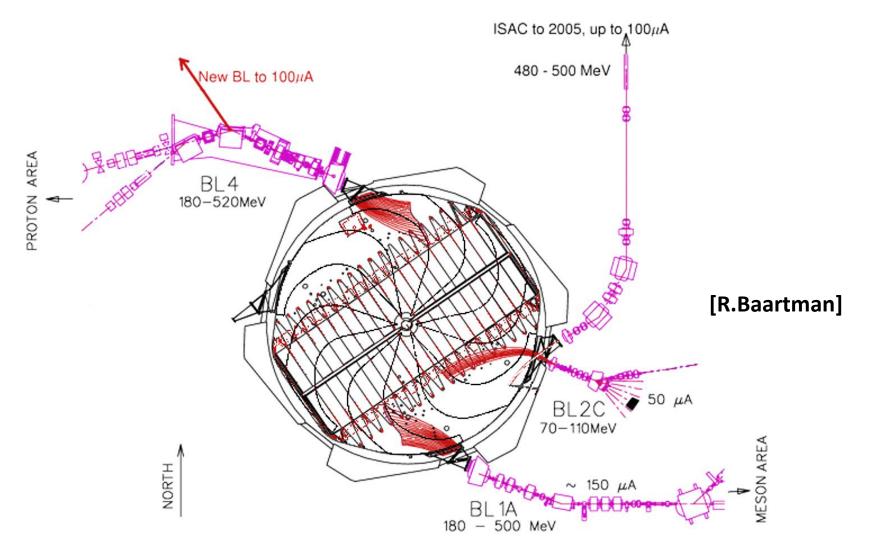
Bending radius of electrons?

$$\rho^e = \frac{E_0^e}{E_0^p} \rho^p$$

 \rightarrow typically mm

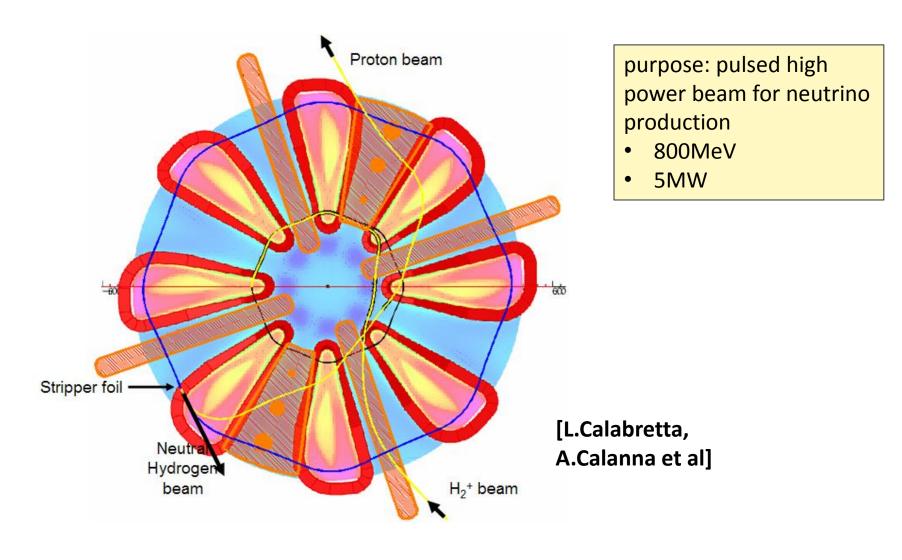


example: multiple H⁻ stripping extraction at TRIUMF





example: H₂⁺ stripping extraction in planned Daedalus cyclotron [neutrino source]



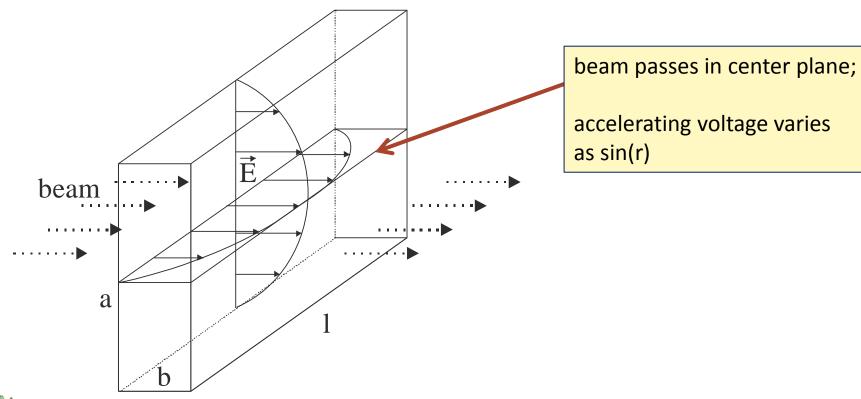


components: cyclotron resonators

cyclotron resonators are basically box resonators

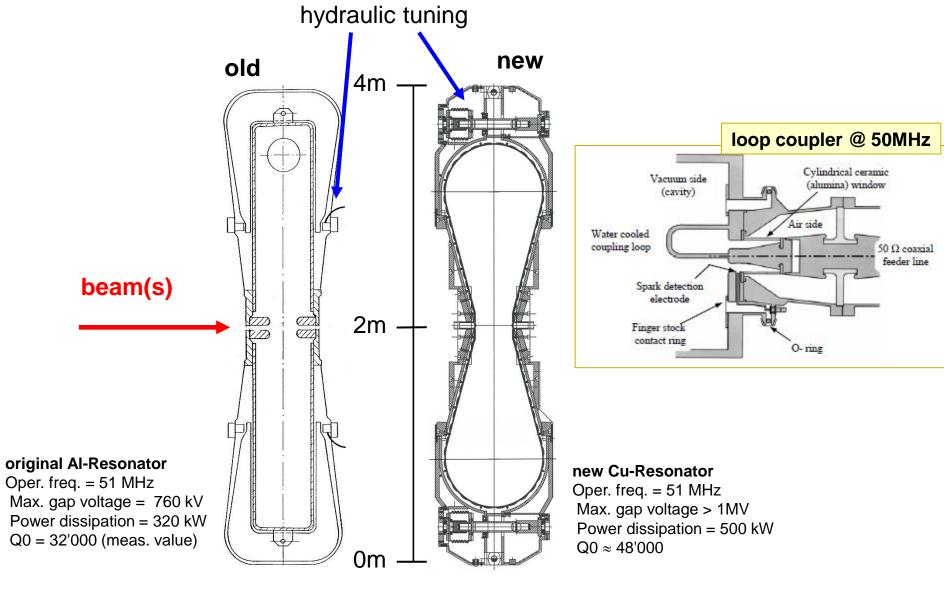
resonant frequency:

$$f_r = \frac{c}{2}\sqrt{\frac{1}{a^2} + \frac{1}{l^2}}$$





cross sections of PSI resonators





copper resonator in operation at PSI's Ring cyclotron

- f = 50.6MHz; $Q_0 = 4.8 \cdot 10^4$; $U_{max} = 1.2MV$ (presently 0.85MV)
- transfer of up to 400kW power to the beam per cavity
- Wall Plug to Beam Efficiency (RF Systems): **32**%



resonator hydraulic tuning inside devices (5x)





components: sector magnets

 cyclotron magnets typically cover a wide radial range → magnets are heavy and bulky, thus costly

PSI sector magnet

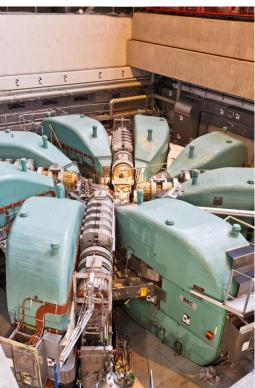
iron weight: 250 tons

coil weight: 28 tons

orbit radius: 2.1...4.5 m

spiral angle: 35 deg

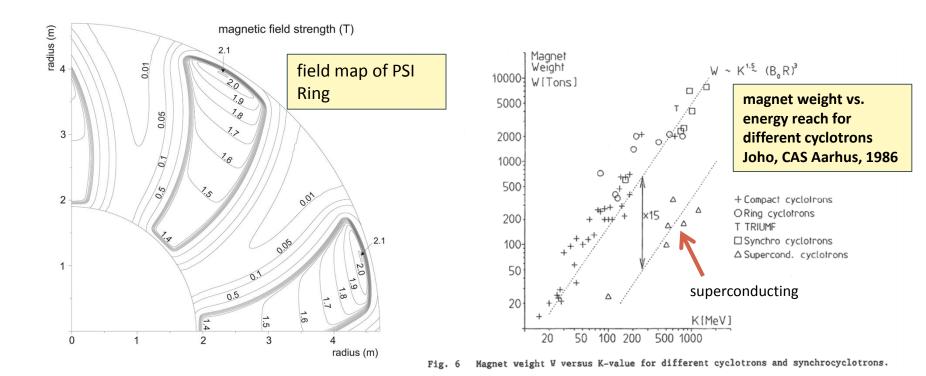






components: sector magnets

- focusing and isochronicity need to be precisely controlled →
 sophisticated pole shaping including spiral bounds, many trim coil circuits
- modern cyclotrons use superconducting magnets; but for high intensity compactness is generally disadvantageous



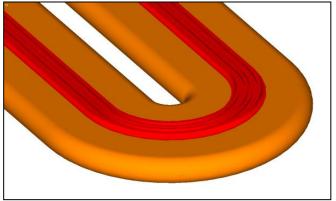


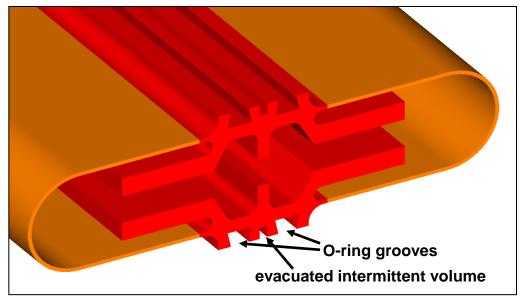
cyclotron vacuum system

- vacuum chamber with large radial width → difficult to achieve precisely matching sealing surfaces → noticeable leak rates must be accepted
- use cryo pumps with high pumping speed and capacity
- $\approx 10^{-6}$ mbar for p, $\approx 10^{-8}$ mbar for ions (instability! e.g. AGOR at KVI)
- design criterion is easy access and fast mountability (activation)

example: inflatable seals installed between resonators; length: 3.5m



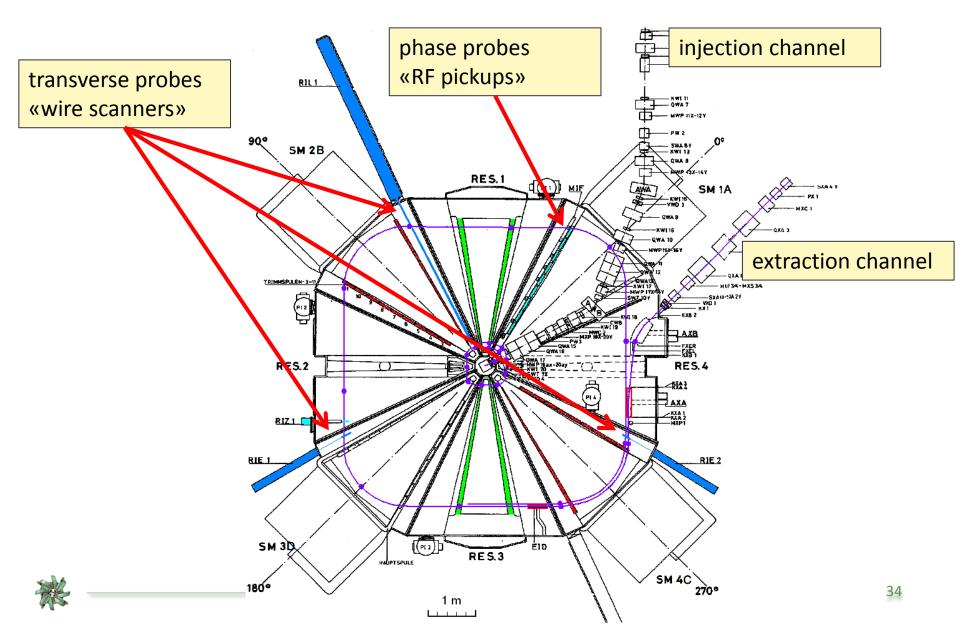






cyclotron instrumentation

example: PSI 72MeV injector cyclotron



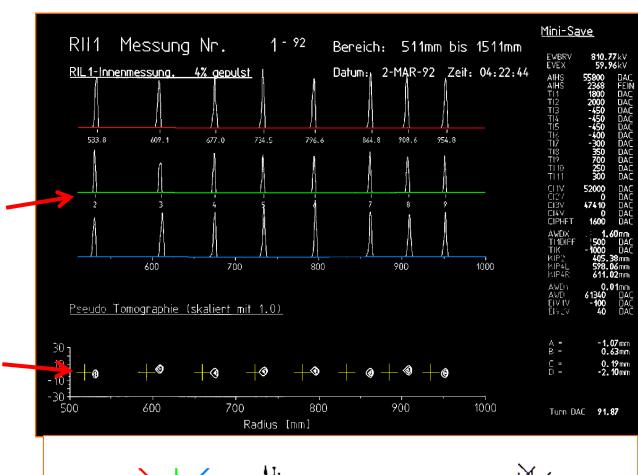
instrumentation: radial probe for turn counting / orbit analysis

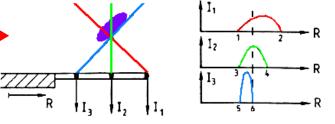
wire scanner with three tilted wires delivers radial beam profile and some vertical information

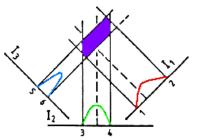
radial: positions of individual turns

vertical/radial orbit positions and stored reference orbit (crosses)

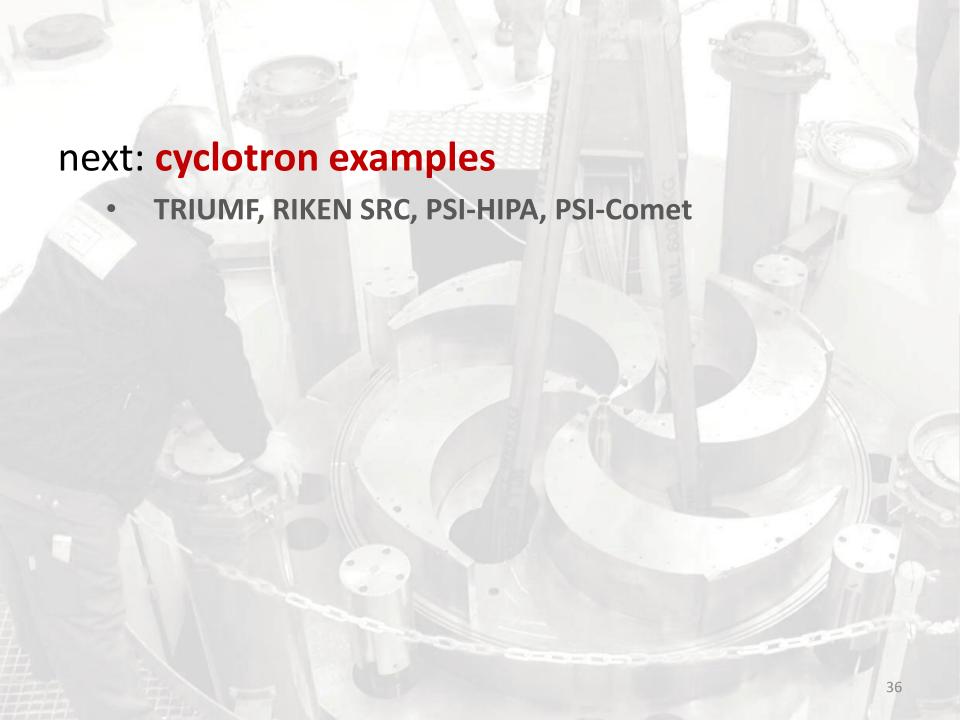
«pseudo tomography» with tilted wires











comparison of cyclotrons

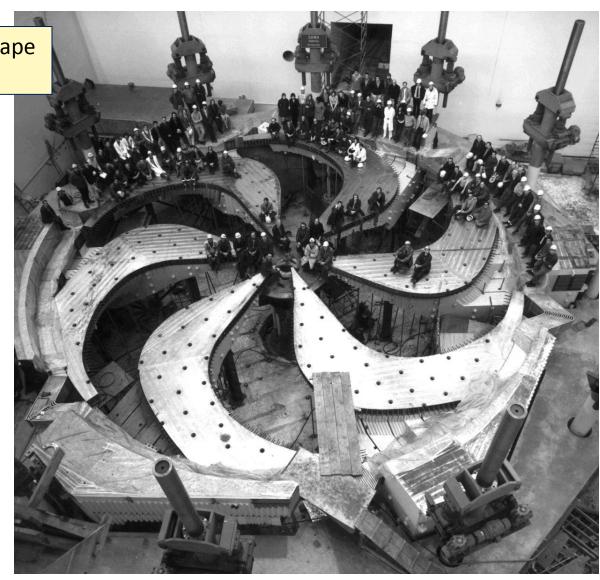
	TRIUMF	RIKEN SRC (supercond.)	PSI Ring	PSI medical (supercond.)
particles	$H- \rightarrow p$	ions	р	р
K [MeV]	520	2600	592	250
magnets (poles)	(6)	6	8	(4)
peak field strength [T]	0.6	3.8	2.1	3.8
R_{inj}/R_{extr} [m]	0.25/3.87.9	3.6/5.4	2.4/4.5	-/0.8
P _{max} [kW]	110	1 (86Kr)	1300	0.25
extraction efficiency (tot. transmission)	0.9995 (0.70)	(0.63)	0.9998	0.80
extraction method	stripping foil	electrostatic deflector	electrostatic deflector	electrostatic deflector
comment	variable energy	ions, flexible	high intensity	compact



cyclotron examples: TRIUMF / Vancouver

photo: iron poles with spiral shape $(\delta_{max}=70deg)$

- p, 520MeV, up to 110kW beam power
- diameter: 18m (largest n.c. cyclotron worldwide)
- extraction by stripping H⁻
 → variable energy;
 multiple extraction points
 possible





RIKEN SRC in the vault





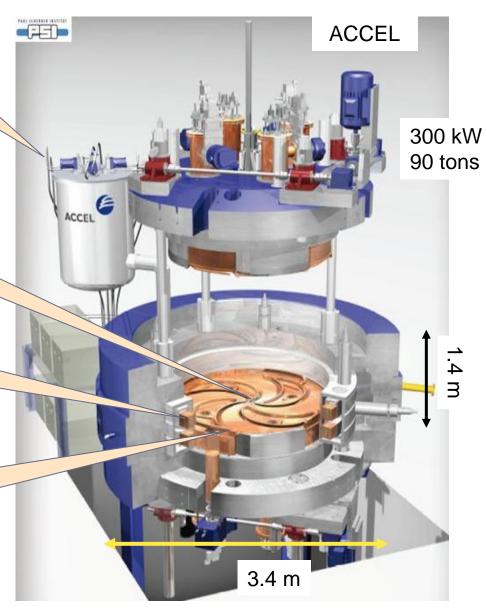
250 MeV proton cyclotron (ACCEL/Varian)

Closed He system 4 x 1.5 W @4K

Proton source

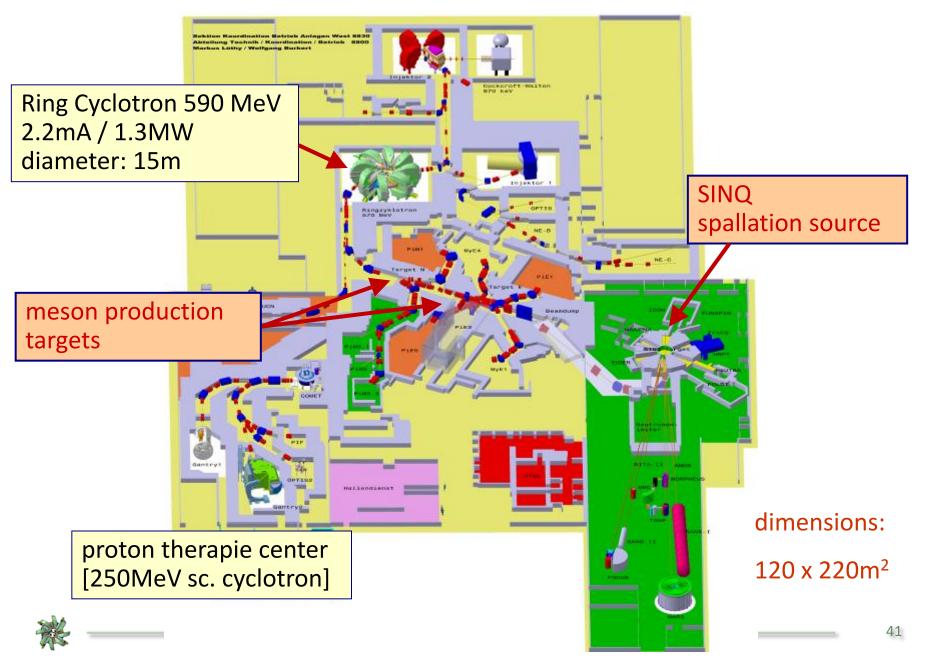
superconducting coils => 2.4 - 3.8 T

4 RF-cavities ≈100 kV on 4 Dees





examples: PSI High Intensity Proton Accelerator





classification of circular accelerators

	bending radius	bending field vs. time	bending field vs. radius	RF frequency vs. time	operation mode (pulsed/CW)	
betatron	→	~	7		ш	induction
microtron	~	→	→	→		varying <i>h</i>
classical cyclotron	<i>→</i>	→		→		simple, but limited E _k
isochronous cyclotron	~	→	<i>></i>	→		suited for high power!
synchro- cyclotron	<i>→</i>	→	→	7	4	higher E _k , but low P
FFAG	>	→	<i>→</i>	<i>→</i>	ш	strong focusing!
a.g. synchrotron	→	<i>→</i>			ш	high E _k , strong focus



pro and contra cyclotron

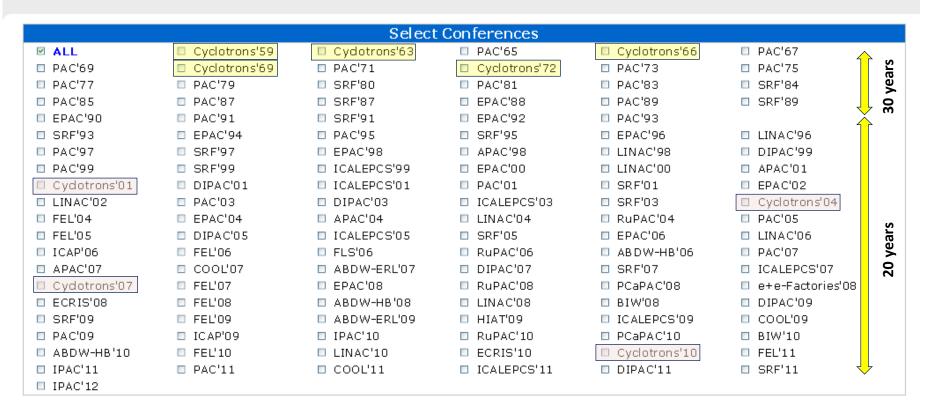
limitations of cyclotrons	typical utilization of cyclotrons
 energy limitation ≈1GeV due to relativistic effects relatively weak focusing is critical for space charge effects (10mA?) tuning is difficult; field shape; many turns; limited diagnostics wide vacuum vessel (radius variation) 	 medical applications ≤250MeV; intensity range well covered isotope production → several 10MeV acceleration of heavy ions (e.g. RIKEN) very high intensity proton beams (PSI:1.4MW, TRIUMF: 100kW)



cyclotron conferences – a valuable source of knowledge

- old cyclotron conferences are being digitized for JACOW (next 1975; effort of M.Craddock!)
- intl. cyclotron conference every 3 years; next in 2013 Vancouver; in-between European Cyclotron Progress Meeting (ECPM)

Joint Accelerator Conferences Website





some literature w.r.t. cyclotrons

comprehensive overview on cyclotrons	L.M.Onishchenko, Cyclotrons: A Survey, Physics of Particles and Nuclei 39, 950 (2008) http://www.springerlink.com/content/k61mg262vng17411/fulltext.pdf
scaling of PSI concept to 10MW	Th.Stammbach et al, The feasibility of high power cyclotrons, Nuclear Instruments and Methods in Physics Research B 113 (1996) 1-7
space charge effects and scalings	W.Joho, High Intensity Problems in Cyclotrons, Proc. 5th intl. Conf. on Cyclotrons and their Applications, Caen, 337-347 (1981)
long. space charge; comparison to analytical result	E.Pozdeyev, A fast code for simulation of the longitudinal space charge effect in isochronous cyclotrons, cyclotrons (2001) http://accelconf.web.cern.ch/AccelConf/c01/cyc2001/paper/P4-11.pdf
H ₂ ⁺ concept for high power	L.Calabretta et al, A multi megawatt cyclotron complex to search for cp violation in the neutrino sector, cyclotrons (2010); upcoming NIM paper! http://accelconf.web.cern.ch/AccelConf/Cyclotrons2010/papers/tua1cio01.pdf
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