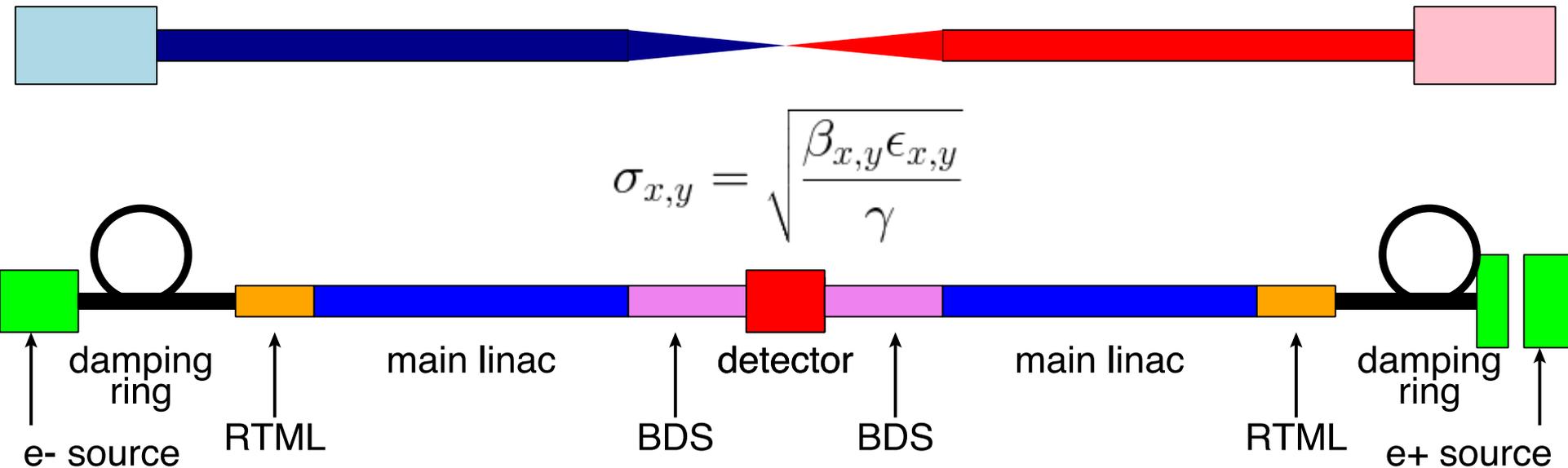


Beam-beam Effects in Linear Colliders

Daniel Schulte

Generic Linear Collider



Single pass poses luminosity challenge

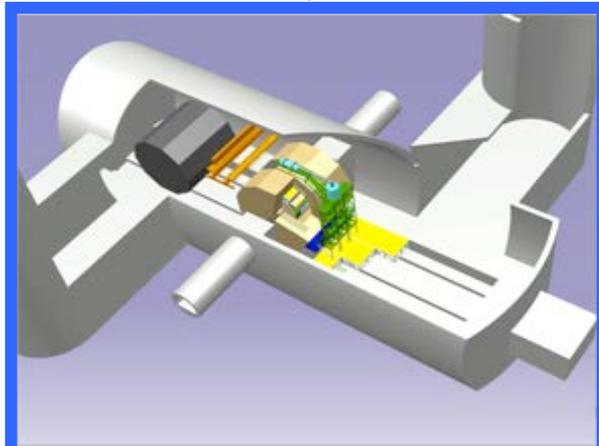
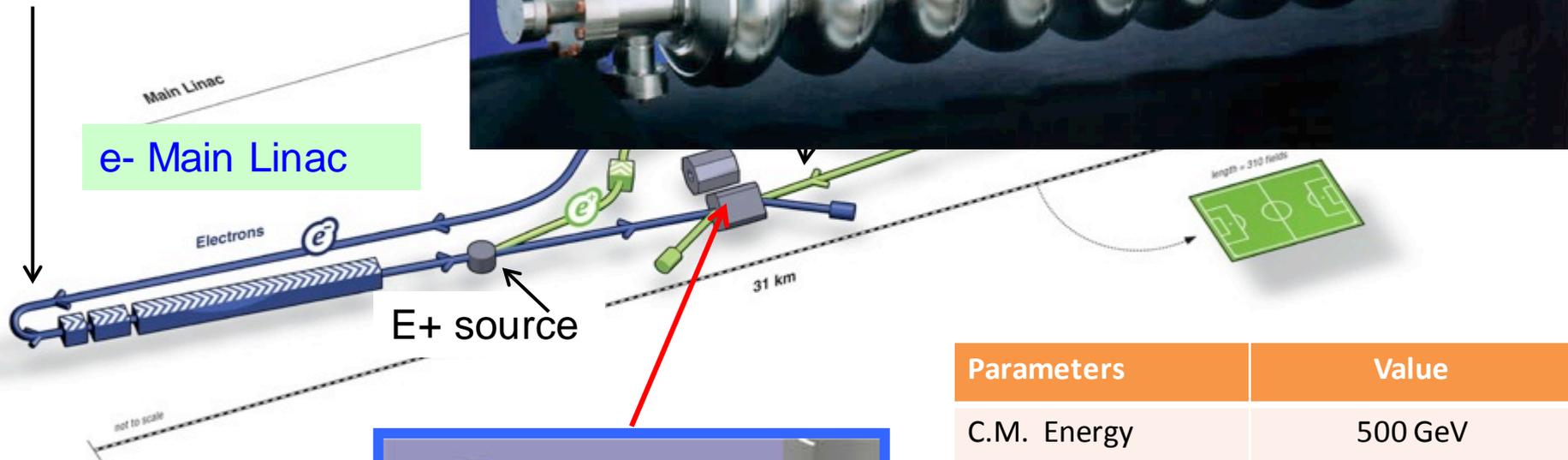
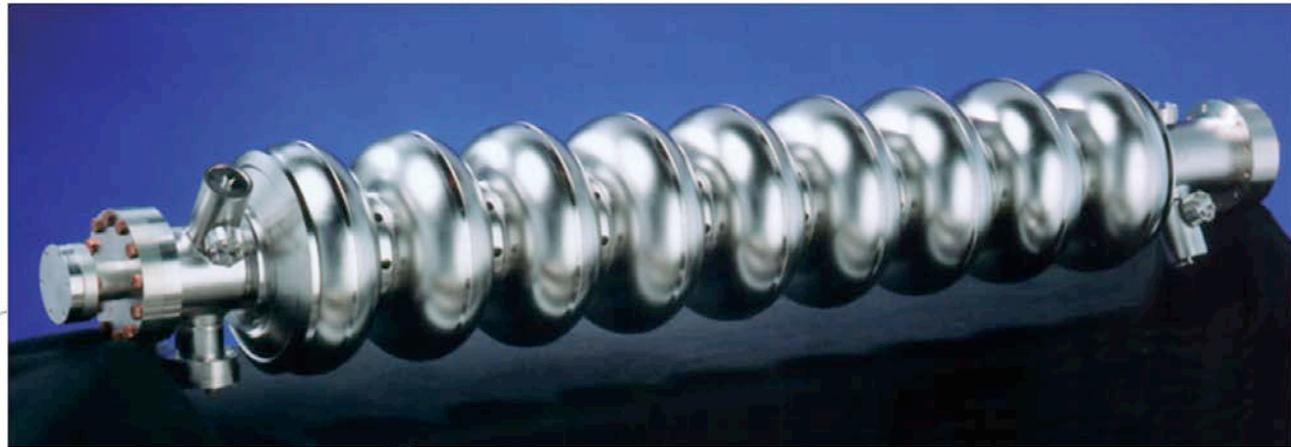
Low emittances are produced in the damping rings

They must be maintained with limited degradation

The beam delivery system (BDS) squeezes the beam as much as possible

ILC

Ring to Main Linac (RTML)
(w. bunch compressors)



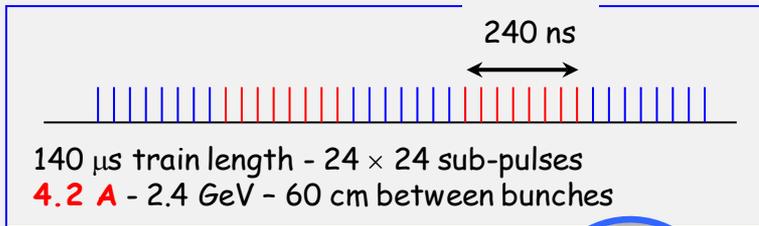
Parameters	Value
C.M. Energy	500 GeV
Peak luminosity	$1.8 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
Beam Rep. rate	5 Hz
Pulse duration	0.73 ms
Average current	5.8 mA (in pulse)
E gradient in SCRF acc. cavity	$31.5 \text{ MV/m} \pm 20\%$ $Q_0 = 1\text{E}10$

CLIC (at 3TeV)

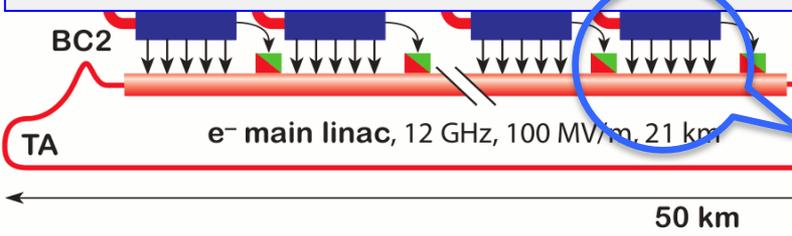
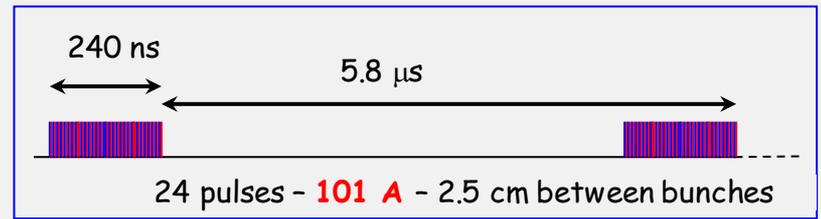
540 kVstrons

540 kVstrons

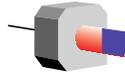
Drive beam time structure - initial



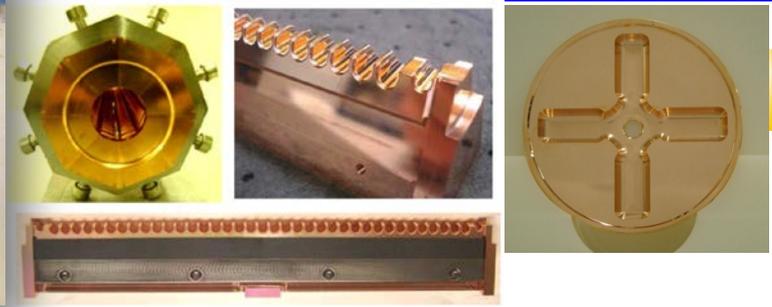
Drive beam time structure - final



CR combiner ring
 TA turnaround

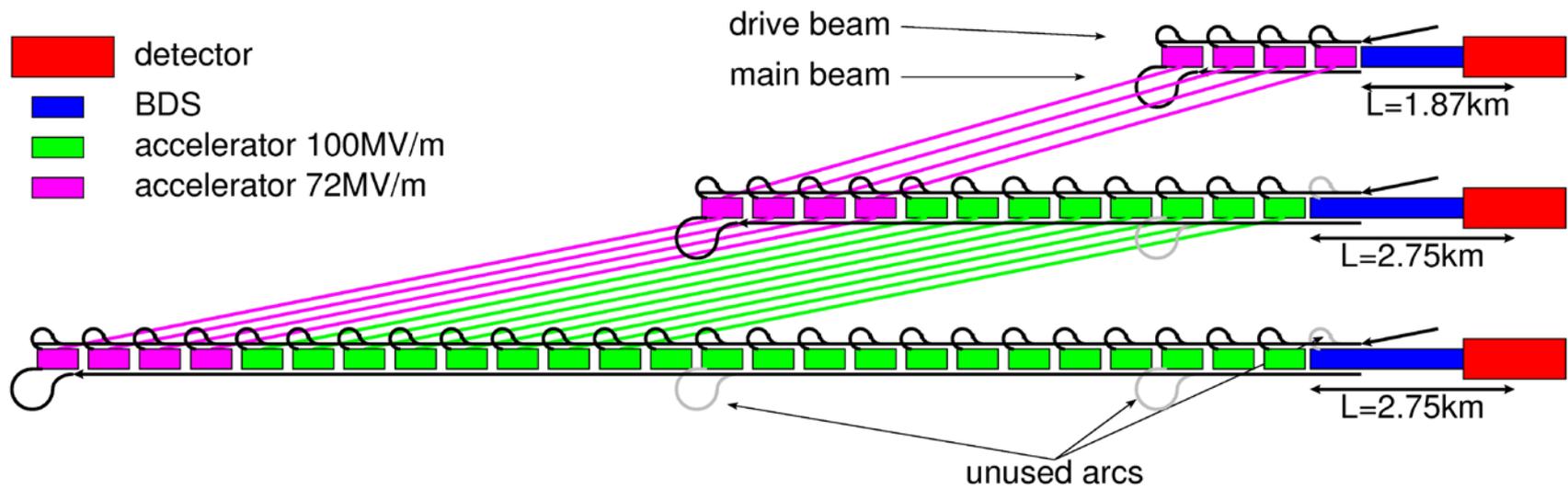


D. Schulte



Beam-beam effects in Linear Colliders

CLIC Staged Approach



- First stage: $E_{\text{cms}}=380\text{Gev}$, $L=1.5 \times 10^{34}\text{cm}^{-2}\text{s}^{-1}$, $L_{0.01}/L > 0.6$
- Second stage: $E_{\text{cms}}=O(1.5\text{TeV})$
- Final stage: $E_{\text{cms}}=3\text{TeV}$, $L_{0.01}=2 \times 10^{34}\text{cm}^{-2}\text{s}^{-1}$, $L_{0.01}/L > 0.3$

Linear Collider Experiment

10^9 readout cells

Field return and muon particle identification

Final steering of nm-size beams

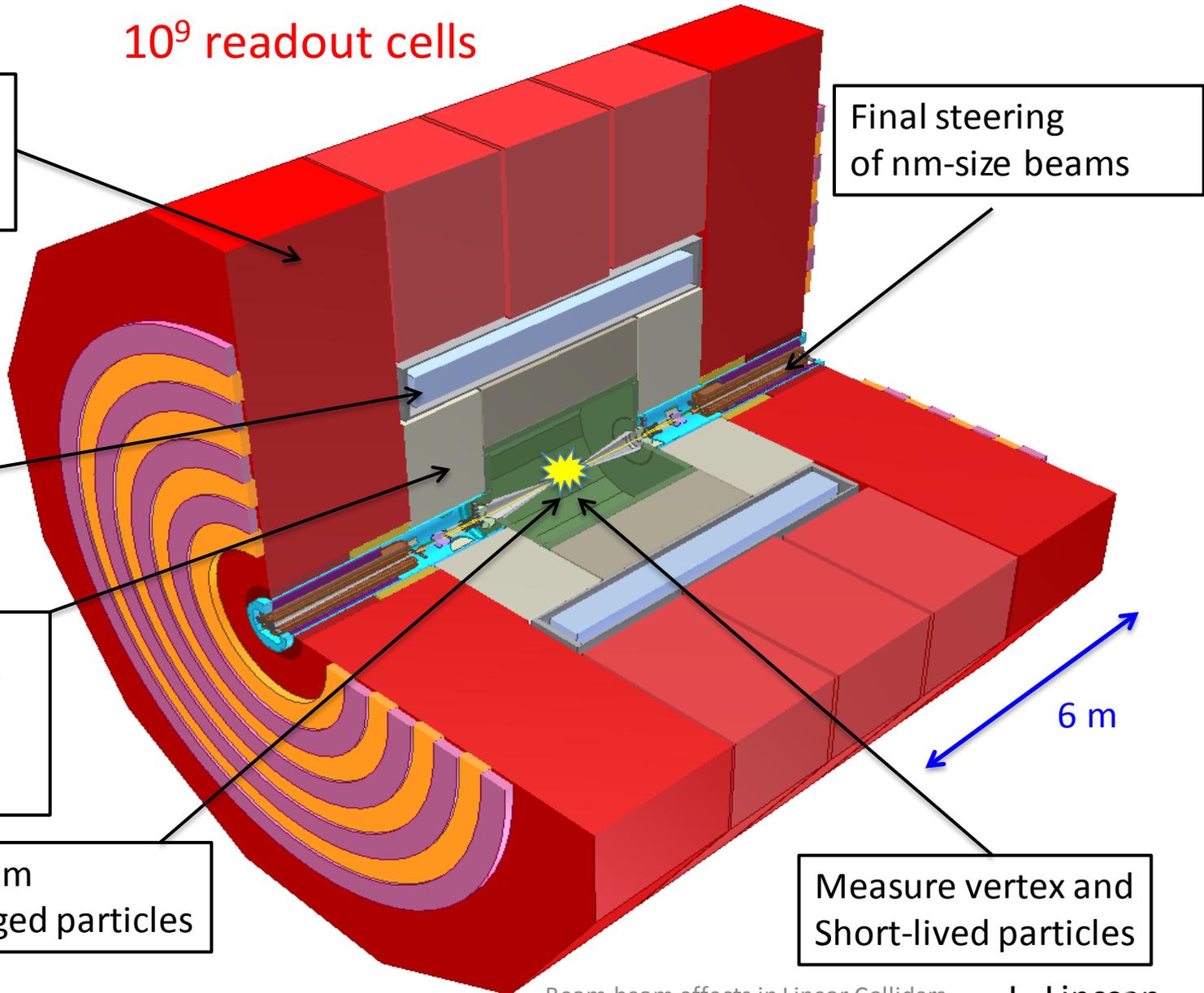
B-field for momentum and charge measurement

Energy measurement of (charged and) neutral particles

Measure momentum and charge of charged particles

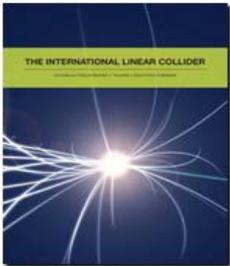
Measure vertex and Short-lived particles

6 m



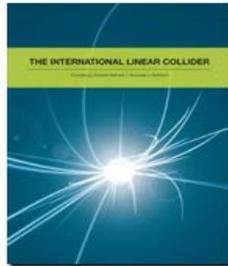
Note: ILC TDR

Volume 1 - Executive Summary



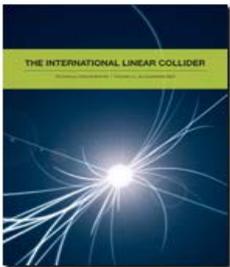
[Download the pdf](#) (9.5 MB)

Volume 2 - Physics



[Download the pdf](#) (9.5 MB)

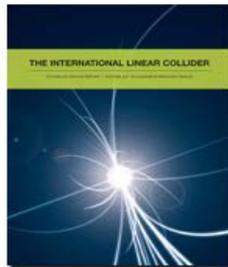
Volume 3 - Accelerator



Part I: R&D in the Technical Design Phase

[Download the pdf](#) (91 MB)

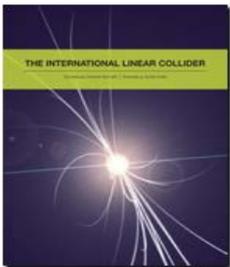
Volume 3 - Accelerator



Part II: Baseline Design

[Download the pdf](#) (72 MB)

Volume 4 - Detectors



[Download the pdf](#) (66 MB)

From Design to Reality



[Download the pdf](#) (5.5 MB)

[Visit the web site](#)

<http://www.linearcollider.org/ILC/Publications/Technical-Design-Report>

Note: CLIC CDR



Vol 1: The CLIC accelerator and site facilities

- CLIC concept with exploration over multi-TeV energy range up to 3 TeV
- Feasibility study of CLIC parameters optimized at 3 TeV (most demanding)
- Consider also 500 GeV, and intermediate energy range
- <https://edms.cern.ch/document/1234244/>



Vol 2: Physics and detectors at CLIC

- Physics at a multi-TeV CLIC machine can be measured with high precision, despite challenging background conditions
- External review procedure in October 2011
- <http://arxiv.org/pdf/1202.5940v1>



Vol 3: “CLIC study summary”

- Summary and available for the European Strategy process, including possible implementation stages for a CLIC machine as well as costing and cost-drives
- Proposing objectives and work plan of post CDR phase (2012-16)
- <http://arxiv.org/pdf/1209.2543v1>

In addition a shorter overview document was submitted as input to the European Strategy update, available at: <http://arxiv.org/pdf/1208.1402v1>

Input documents to Snowmass 2013 has also been submitted: <http://arxiv.org/abs/1305.5766> and <http://arxiv.org/abs/1307.5288>

ILC and CLIC Main Parameters

Parameter	Symbol [unit]	SLC	ILC	CLIC	CLIC
Centre of mass energy	E_{cm} [GeV]	92	500	380	3000
Geometric luminosity	L_{geom} [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	0.00015	0.75	0.8	4.3
Total luminosity	L [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	0.0003	1.8	1.5	6
Luminosity in peak	$L_{0.01}$ [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	0.0003	1	0.9	2
Gradient	G [MV/m]	20	31.5	72	100
Particles per bunch	N [10^9]	37	20	5.2	3.72
Bunch length	σ_z [μm]	1000	300	70	44
Collision beam size	$\sigma_{x,y}$ [nm/nm]	1700/600	474/5.9	149/2.9	40/1
Emittance	$\epsilon_{x,y}$ [$\mu\text{m}/\text{nm}$]	$\sim 3/3000$	10/35	0.95/30	0.66/20
Betafunction	$\beta_{x,y}$ [mm/mm]	$\sim 100/10$	11/0.48	8.2/0.1	6/0.07
Bunches per pulse	n_b	1	1312	352	312
Distance between bunches	Δz [ns]	-	554	0.5	0.5
Repetition rate	f_r [Hz]	120	5	50	50

There are more parameter sets for ILC and CLIC at different energies
 CLIC at 3TeV has higher order optics and radiation effects

Luminosity and Parameter Drivers

Can re-write normal
luminosity formula
(note: no crossing angle
assumed)

$$\mathcal{L} = H_D \frac{N^2}{4\pi\sigma_x\sigma_y} n_b f_r$$

$$\mathcal{L} \propto H_D \frac{N}{\sigma_x} N n_b f_r \frac{1}{\sigma_y}$$

Luminosity spectrum

Beam power

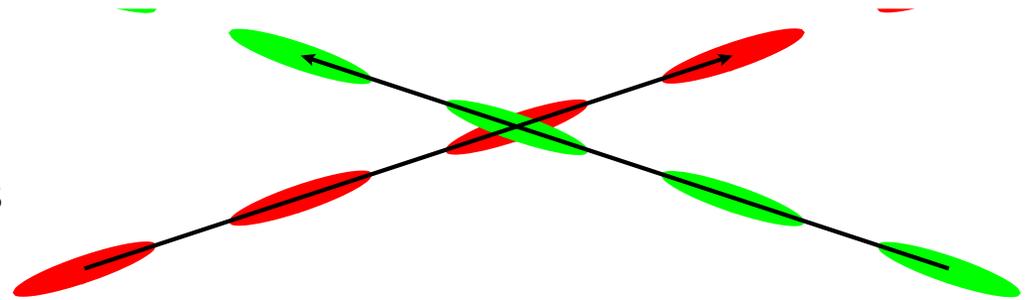
Beam Quality (+bunch length)

Somewhat simplified view

Note: Crossing Angle

Have crossing angles

- ILC: 14mradian
- CLIC: 20mradian
- to reduce effects of parasitic crossings
- to extract the spent beam cleanly

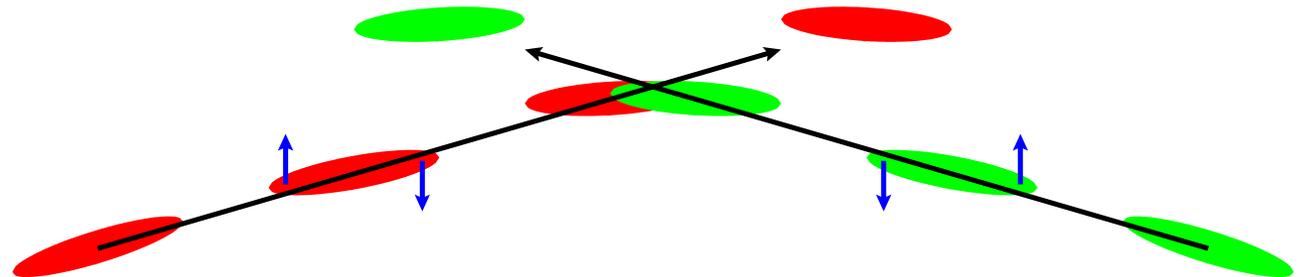


Luminosity with crossing angle

$$\mathcal{L} = H_D \frac{N^2 f_r n_b}{4\pi\sigma_x\sigma_y} \frac{1}{\sqrt{1 + \left(\frac{\sigma_z}{\sigma_x} \tan \frac{\theta_c}{2}\right)^2}}$$

0.1-0.2

Use crab cavities:



Can ignore crossing angle for beam-beam calculation
But not in detector design

Beam-beam Effect

Bunches are squeezed strongly to maximise luminosity



Electron magnetic fields are very strong



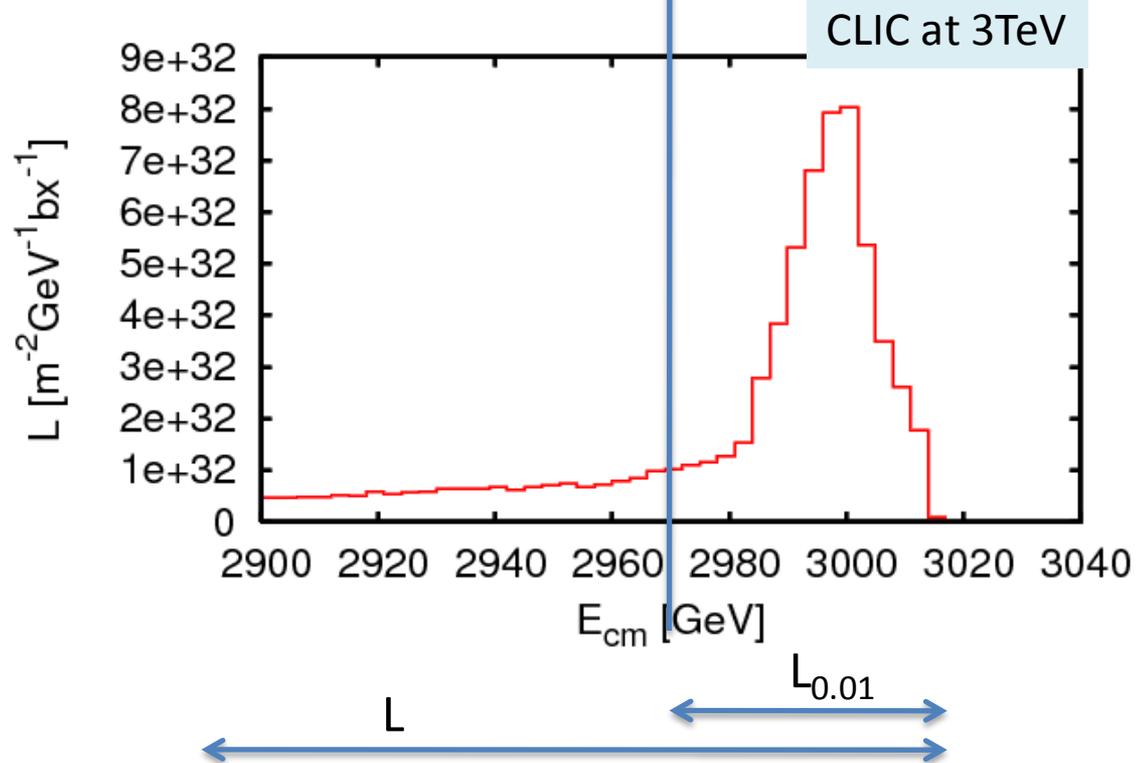
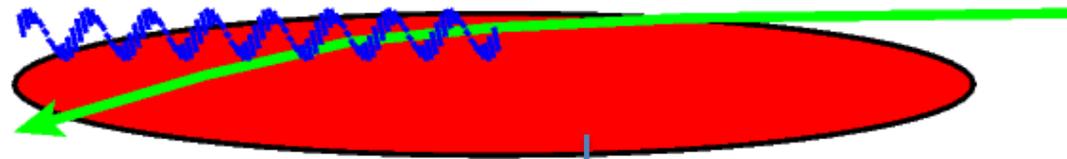
Beam particles travel on curved trajectories



They emit photons (O(1)) (beamstrahlung)



They collide with less than nominal energy



Request from physics
 $L_{0.01}/L > 0.6$ below 500GeV
 $L_{0.01}/L > 0.3$ at 3TeV

Beam Focusing

Note: The colliding beams are flat to reduce beamstrahlung, we will see later why

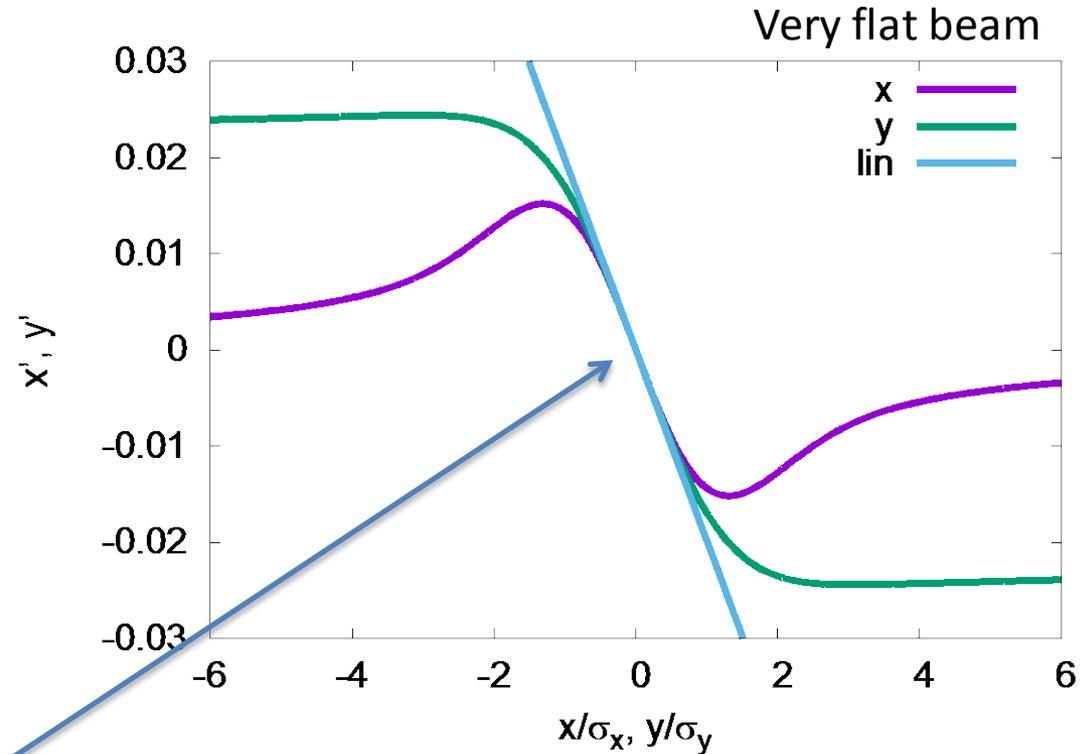
Deflection easy to calculate for

- small offset to the axis
- no initial angle
- negligible change of trajectory

In each plane core of beam is focused to one point

$$s = f_x \quad s = f_y$$

$$r_e \approx 2.8 \times 10^{-15} \text{ m}$$



Previous lecture showed

$$\left. \frac{dx}{dz} \right|_{final} = - \frac{2Nr_e x}{\gamma \sigma_x (\sigma_x + \sigma_y)}$$

$$\left. \frac{dy}{dz} \right|_{final} = - \frac{2Nr_e y}{\gamma \sigma_y (\sigma_x + \sigma_y)}$$

Disruption Parameter

We define the disruption parameters to compare the focal length of the bunch to its length

$$D_x = \frac{\sigma_z}{f_x} = \frac{2Nr_e\sigma_z}{\gamma(\sigma_x + \sigma_y)\sigma_x} \quad D_y = \frac{\sigma_z}{f_y} = \frac{2Nr_e\sigma_z}{\gamma(\sigma_x + \sigma_y)\sigma_y}$$



$$D \ll 1$$

- Particles do not move much in beam
- ⇒ Thin lens approximation is OK
- ⇒ Analytic calculation possible
- ⇒ Weak-strong simulation sufficient
- ⇒ Typical for x-plane

$$D \gg 1$$

- Particles do move in beam
- ⇒ thin lens assumption has been wrong
- ⇒ Analytic calculation tough
- ⇒ Strong-strong simulation required
- ⇒ Typical for y-plane

Typical Disruption

Parameter	Symbol [unit]	SLC	ILC	CLIC	CLIC
Centre of mass energy	E_{cm} [GeV]	92	500	380	3000
Particles per bunch	N [10^9]	37	20	5.2	3.72
Bunch length	σ_z [μm]	1000	300	70	44
Collision beam size	$\sigma_{x,y}$ [nm/nm]	1700/600	474/5.9	149/2.9	40/1
Vertical emittance	$\varepsilon_{x,y}$ [nm]	3000	35	40	20
Horizontal disruption	D_x	0.6	0.3	0.24	0.2
Vertical disruption	D_y	1.7	24.3	12.5	7.6

$$D_x \ll 1 \text{ and } D_y \gg 1$$



Need to resort to strong-strong simulation

Simulation Codes

Need strong-strong code

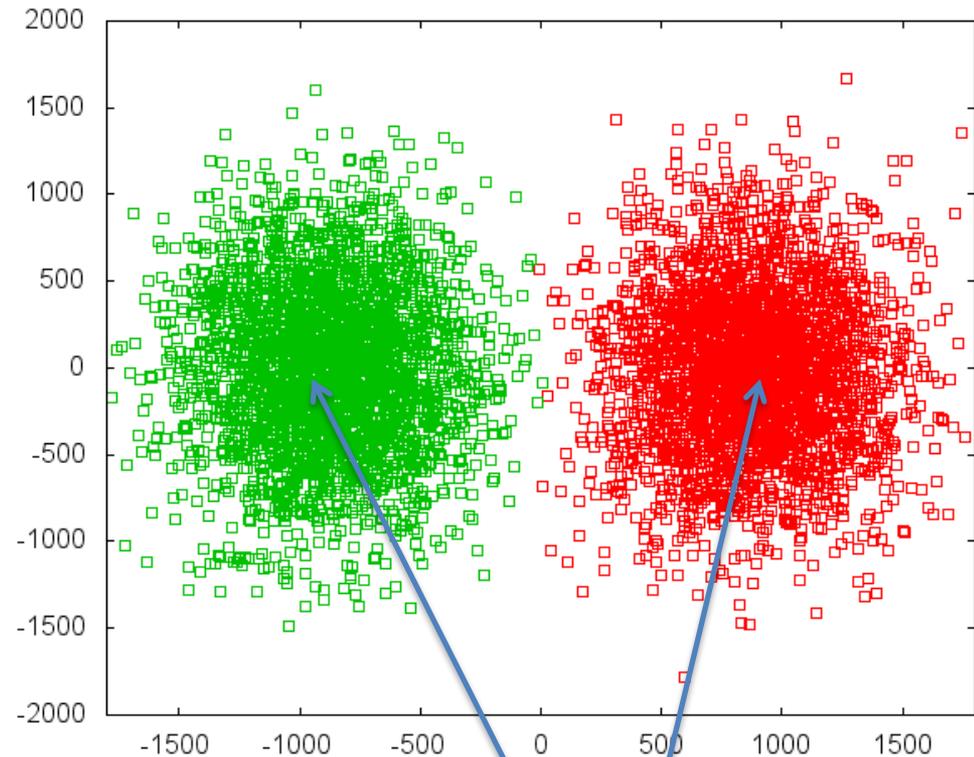
- CAIN (K. Yokoya et al.)
- GUINEA-PIG (D. Schulte et al.)

- Beams => macro particles
- Beams => slices
- Slices => cells
- The simulation is performed in a number of time steps in each of them
- The macro-particle charges are distributed over the cells
 - The forces at the cell locations are calculated
 - The forces are applied to the macro particles
 - The particles are advanced

All simulation performed with
GUINEA-PIG

X direction

ILC



Z direction

Predicted focal points
(for beam centre)

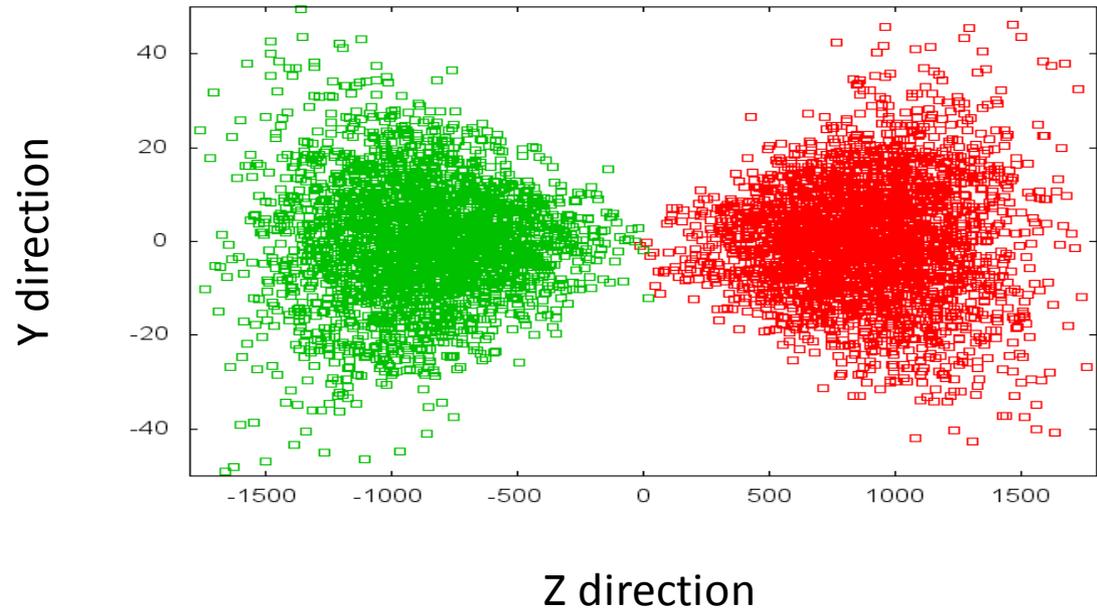
Simulation Codes

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 - The particles are advanced

Beam-beam force switched off

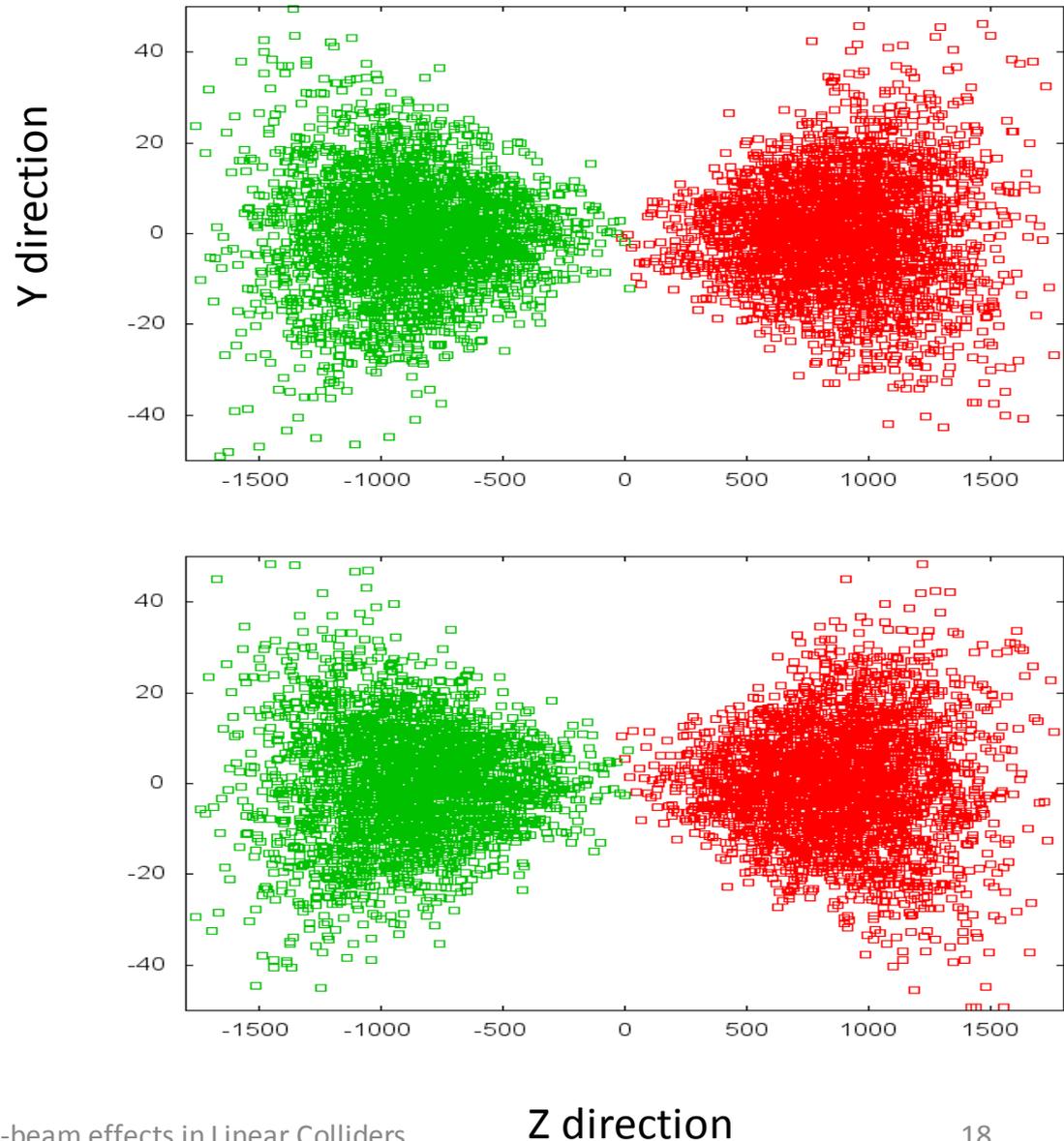


Simulation Codes

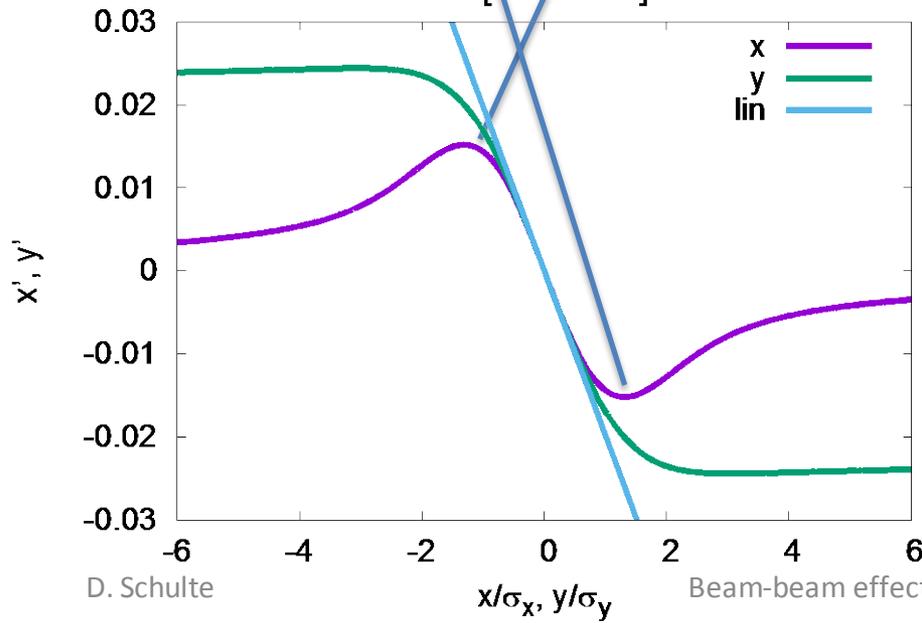
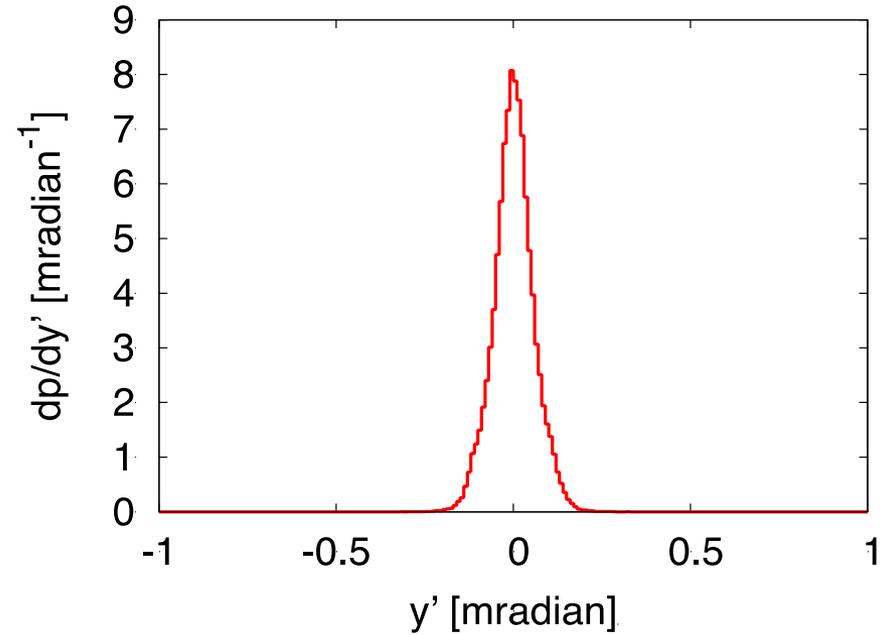
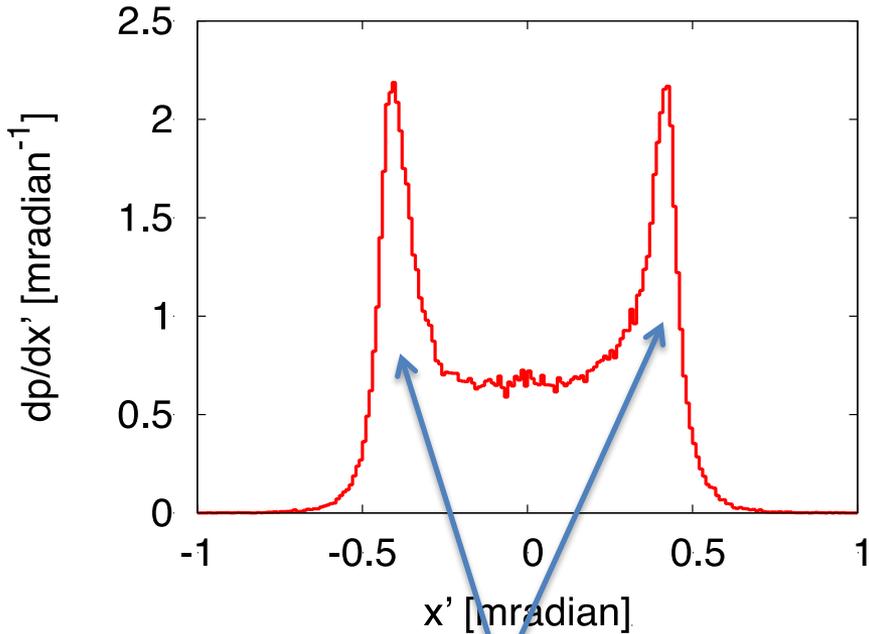
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Beam-beam force switched off



The Spent Beam

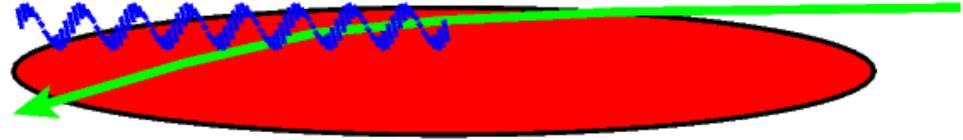


Particles move little in the horizontal plane

⇒ Can see the field profile

They start to oscillate in the vertical plane
 ⇒ Final angle depends also on the phase that they happen to have at the end of the collision

Beamstrahlung



Similar to synchrotron radiation

From local trajectory curvature calculate critical

$$\hbar\omega_c = \frac{3}{2} \frac{\gamma^3 \hbar c}{\rho}$$

Define beamstrahlung parameter Upsilon

$$\Upsilon = \frac{2}{3} \frac{\hbar\omega_c}{E_0}$$

Average Upsilon is approximately given by

$$\langle \Upsilon \rangle = \frac{5}{6} \frac{N r_e^2 \gamma}{\alpha (\sigma_x + \sigma_y) \sigma_z}$$

Beamstrahlung Power Spectrum

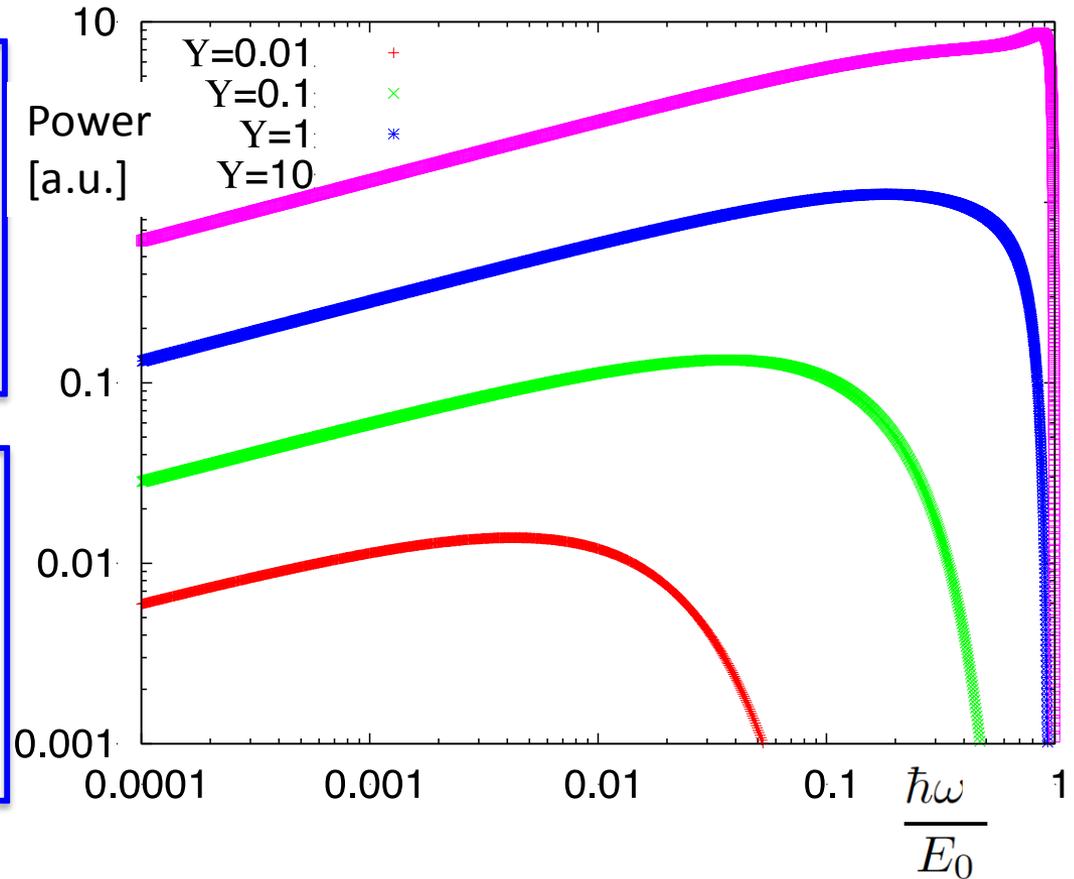
Classical regime $\Upsilon \ll 1$

ILC $Y=0.06$

CLIC at 380GeV $Y=0.17$

Quantum regime $\Upsilon \gg 1$

CLIC at 3TeV $Y=5$



The spectrum is given by
$$\frac{d\dot{w}}{d\omega} = \frac{\alpha}{\sqrt{3}\pi\gamma^2} \left[\int_x^\infty K_{\frac{5}{3}}(x') dx' + \frac{\hbar\omega}{E} \frac{\hbar\omega}{E - \hbar\omega} K_{\frac{2}{3}}(x) \right]$$

With modified Bessel functions $K_{\frac{5}{3}}$ and $K_{\frac{2}{3}}$ $x = \frac{\omega}{\omega_c} \frac{E}{E - \hbar\omega}$

Photons in the Classical Regime $\gamma \ll 1$

Number of photons
 Dominates $L/L_{0.01}$

Energy of photons
 Defines shape of tail

$$n_\gamma \propto \frac{N}{\sigma_x + \sigma_y}$$

$$\frac{E_\gamma}{E_0} \propto \frac{N}{\sigma_x + \sigma_y} \frac{\gamma}{\sigma_z}$$

$$\mathcal{L} \propto \frac{N}{\sigma_x \sigma_y}$$

$$\sigma_x \gg \sigma_y$$

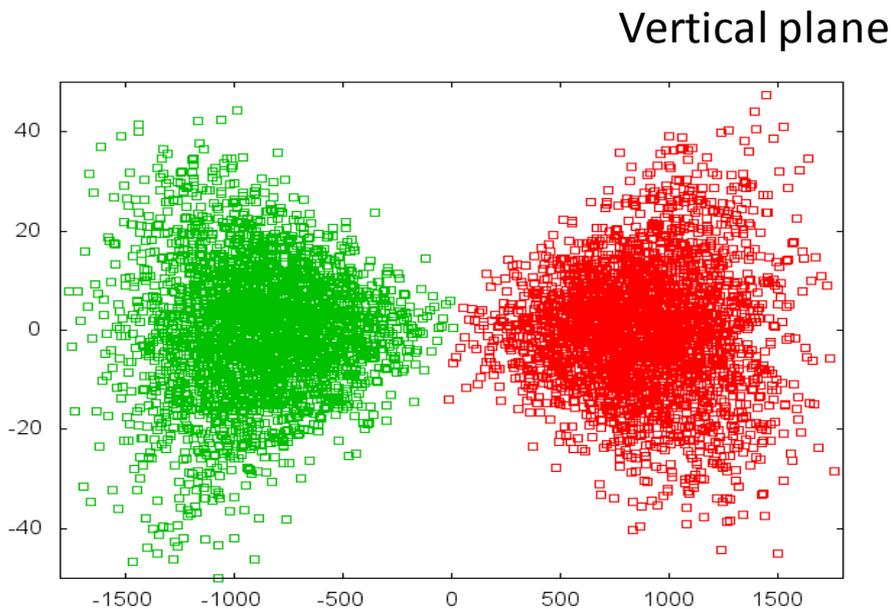
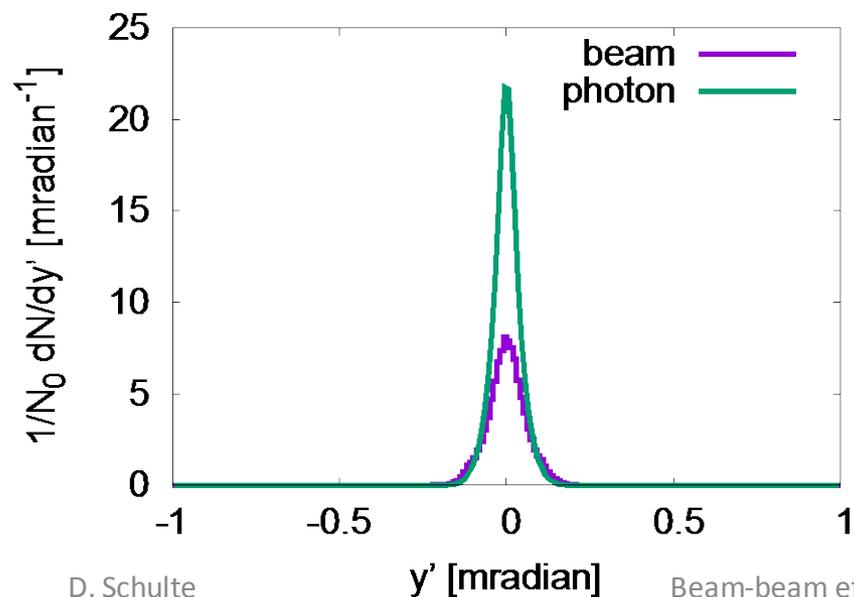
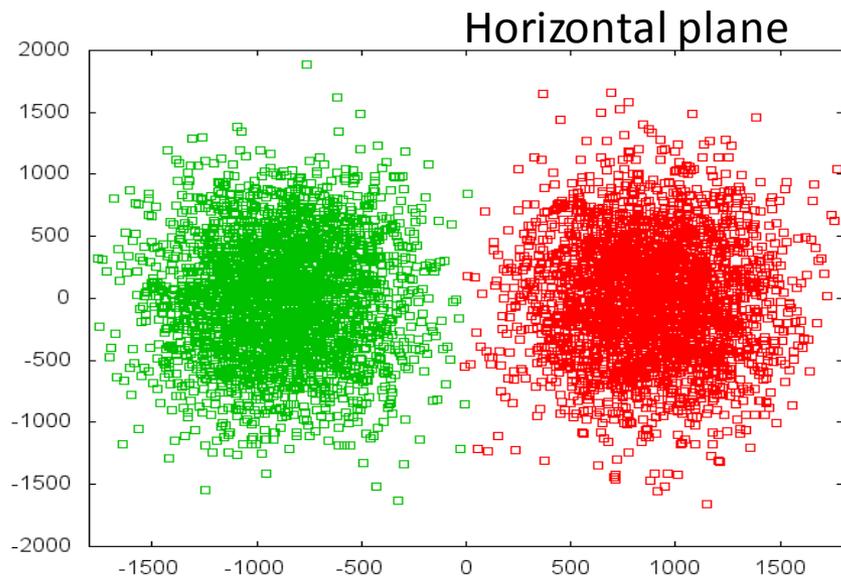
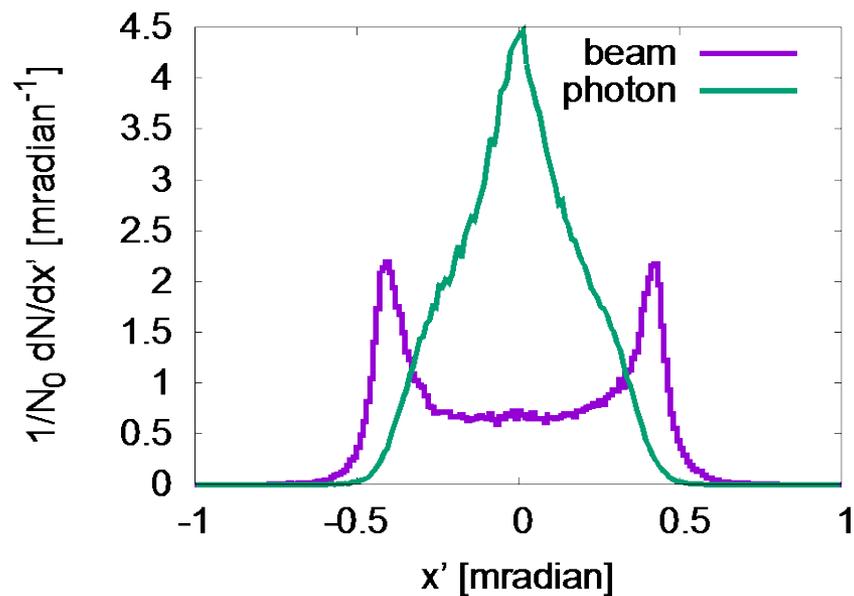
$$\sigma_x + \sigma_y \approx \sigma_x$$

$$\mathcal{L} \propto H_D \left(\frac{N}{\sigma_x} \right) N n_b f_r \frac{1}{\sigma_y}$$

$\propto n_\gamma$

Determined by beamstrahlung

Photon Production



ILC and CLIC Main Parameters

Parameter	Symbol [unit]	ILC	CLIC	CLIC
Centre of mass energy	E_{cm} [GeV]	500	380	3000
Total luminosity	L [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	1.8	1.5	6
Luminosity in peak	$L_{0.01}$ [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	1	0.9	2
Particles per bunch	N [10^9]	20	5.2	3.72
Bunch length	σ_z [μm]	300	70	44
Collision beam size	$\sigma_{x,y}$ [nm/nm]	474/5.9	149/2.9	40/1
Vertical emittance	$\epsilon_{x,y}$ [nm]	35	40	20
Photons per beam particle	n_γ	1.9	1.5	2.1
Average photon energy	$\langle E_\gamma/E_0 \rangle$ [%]	2.4	4.5	13

Photon numbers and $L_{0.01}/L$ are similar for ILC and CLIC at low energies

Average photon energy does not seem to matter too much for $L_{0.01}$

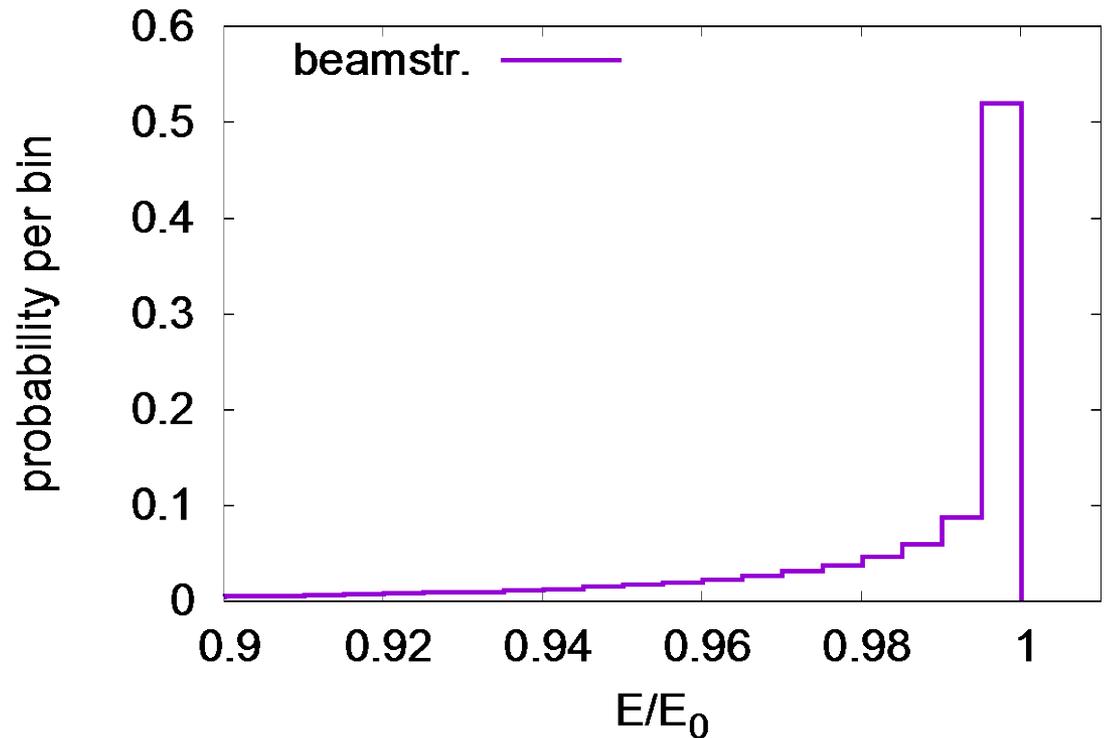
Luminosity Spectrum

Luminosity spectrum for ILC,
CLIC at 380GeV looks similar

(beam energy spread is ignored)

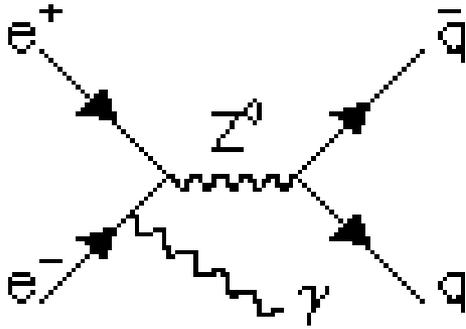
Luminosity $L_{0.01}$ above 99% of
nominal CMS energy is
 $L_{0.01}/L = 60\%$

For CLIC380, this has been the
design criterion



But why did the experiments
chose $L_{0.01}/L > 60\%$?

Note: Initial State Radiation

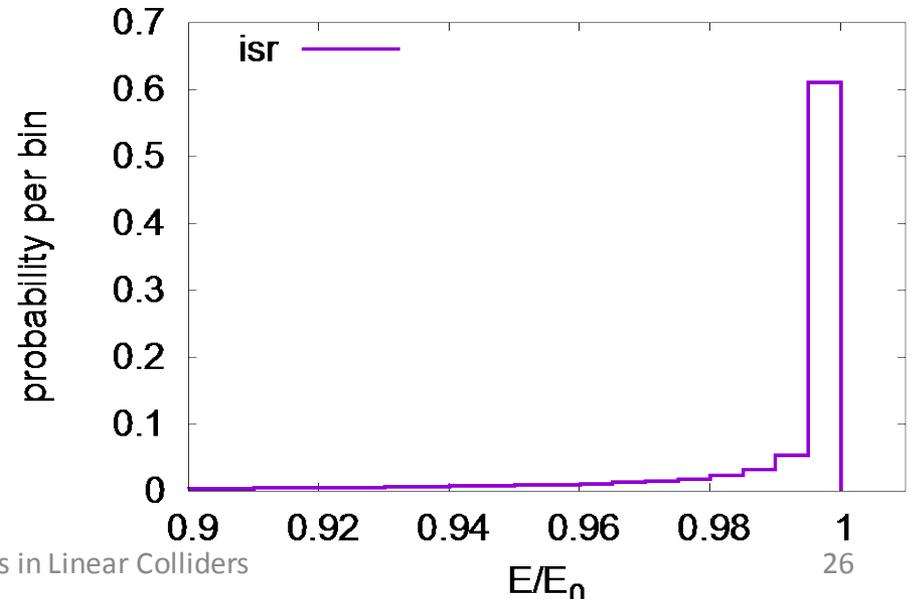
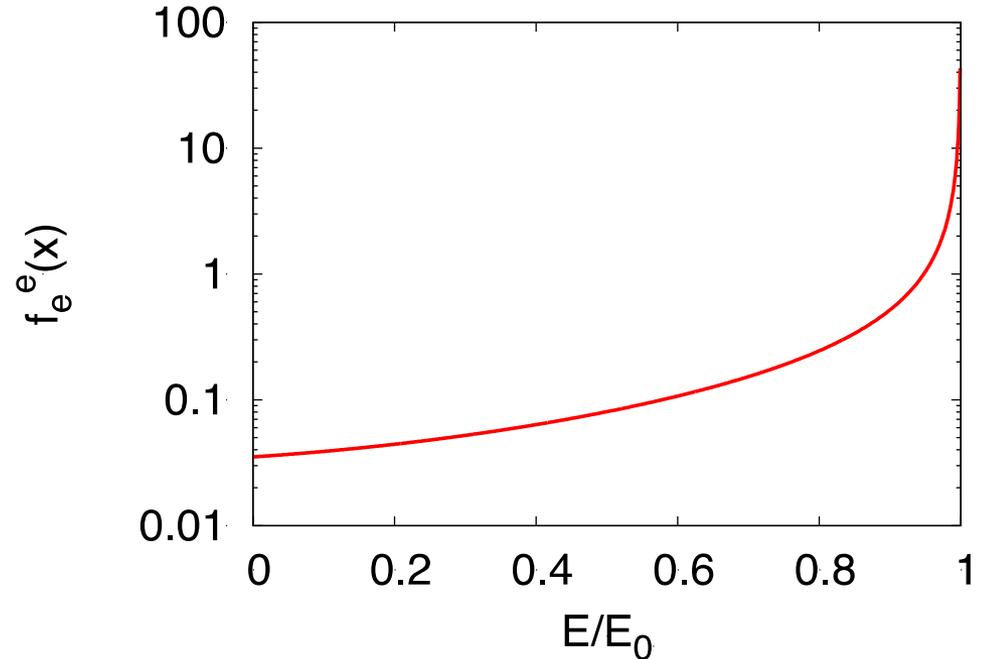


Electrons often emit a photon before the collision
⇒ Initial State Radiation

The electron can be replaced by a spectrum of electrons

This yields a luminosity spectrum

About 65% probability of collision with more than 99% of nominal energy



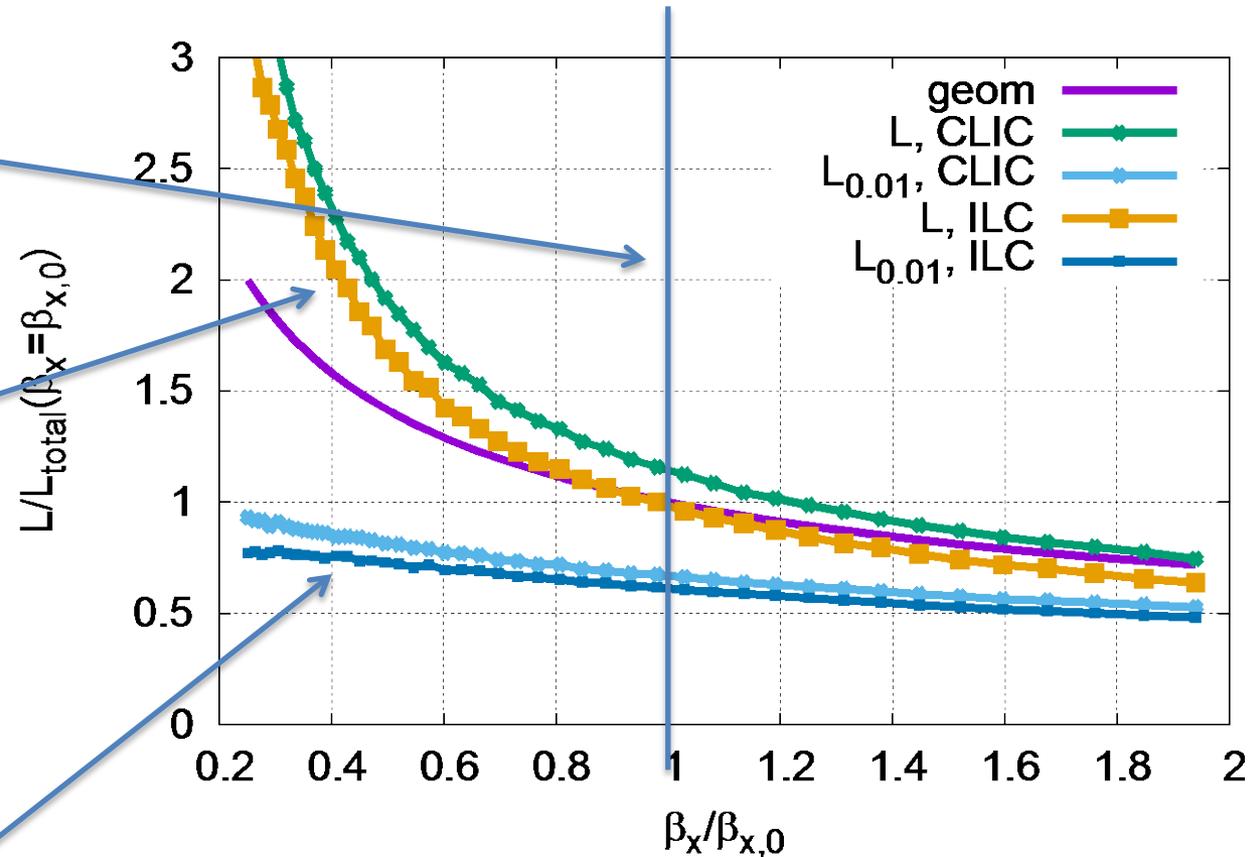
Luminosity Spectrum

Design value
 $L_{0.01}/L=60\%$

The total luminosity L varies strongly with beta-function

But $L_{0.01}$ does not change so much

Hard to push beta-functions That low



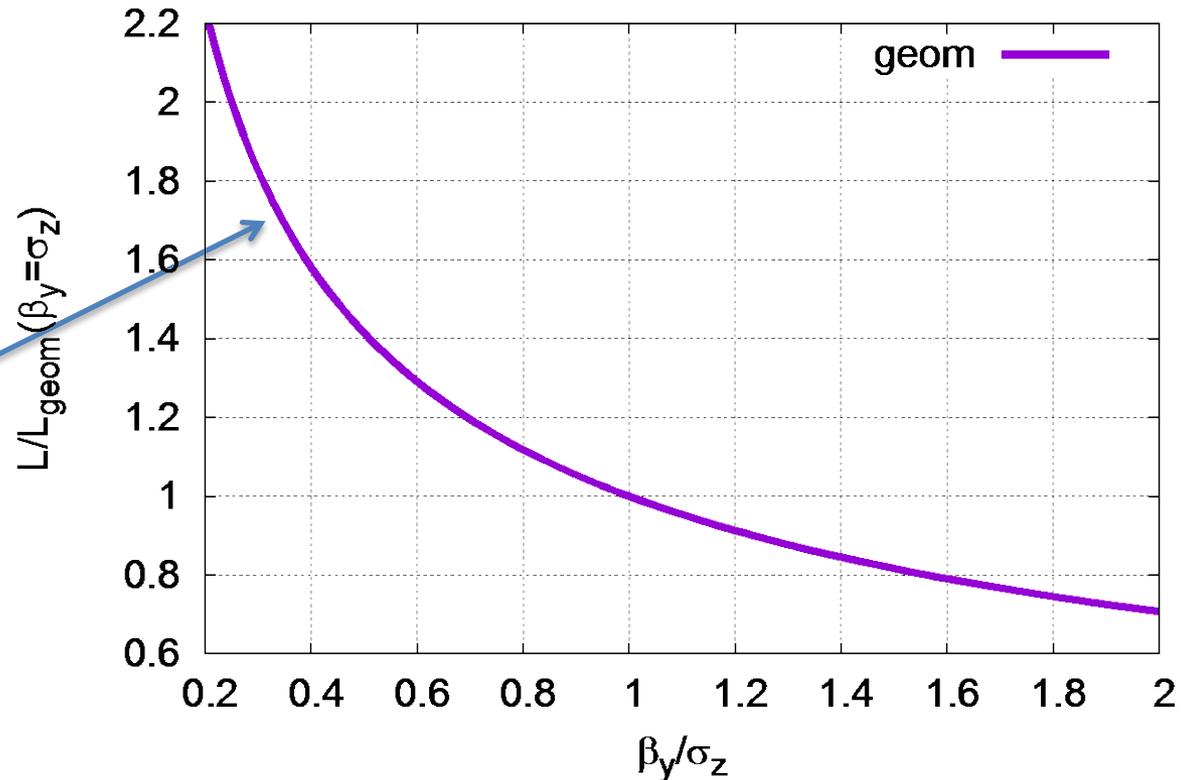
So tend to use $L_{0.01}/L=60\%$ as criterion

Reasonable compromise for most physics studies

Vertical Beamsize

Using the naïve luminosity calculation with beta-function at the IP we find that the luminosity can be increased by reducing β_y

$$\mathcal{L} = \frac{N^2}{4\pi\sigma_x\sigma_y} n_b f_r$$



There are two limits:

The lattice design tends to find a practical lower limit a bit below $\beta_y=100 \mu\text{m}$
CLIC at 3TeV has $\beta_y=70 \mu\text{m}$ but strong geometric aberrations

Luminosity actually increases not as predicted

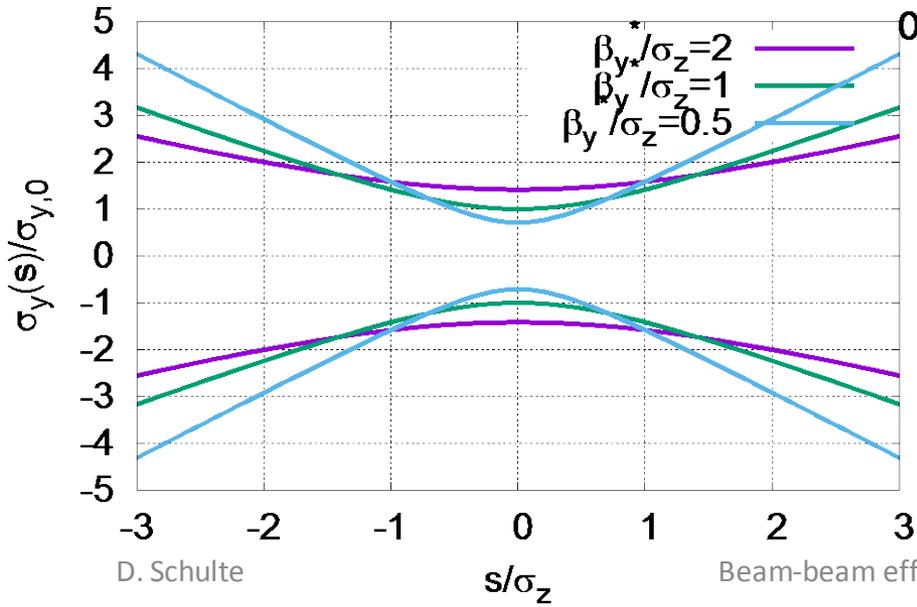
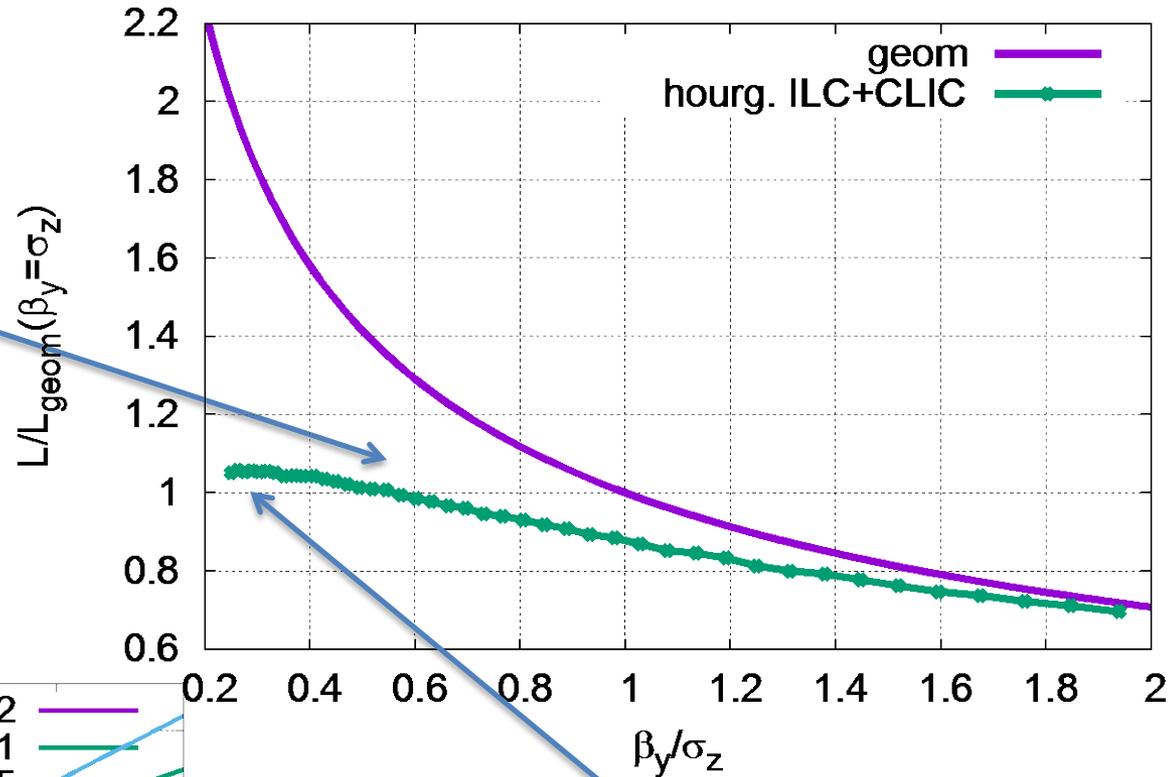
Not excluded that this can be improved but people worked on it for years

Hourglass Effect

Taking into account
hourglass effect

$$\beta(s) = \sqrt{\beta(0) + \frac{s^2}{\beta(0)}}$$

Luminosity does not improve
much below $\beta_y < \sigma_z$



For flat beams, the optimum is around $\beta_y = 0.25 \times \sigma_z$

Note: This is different for round beams

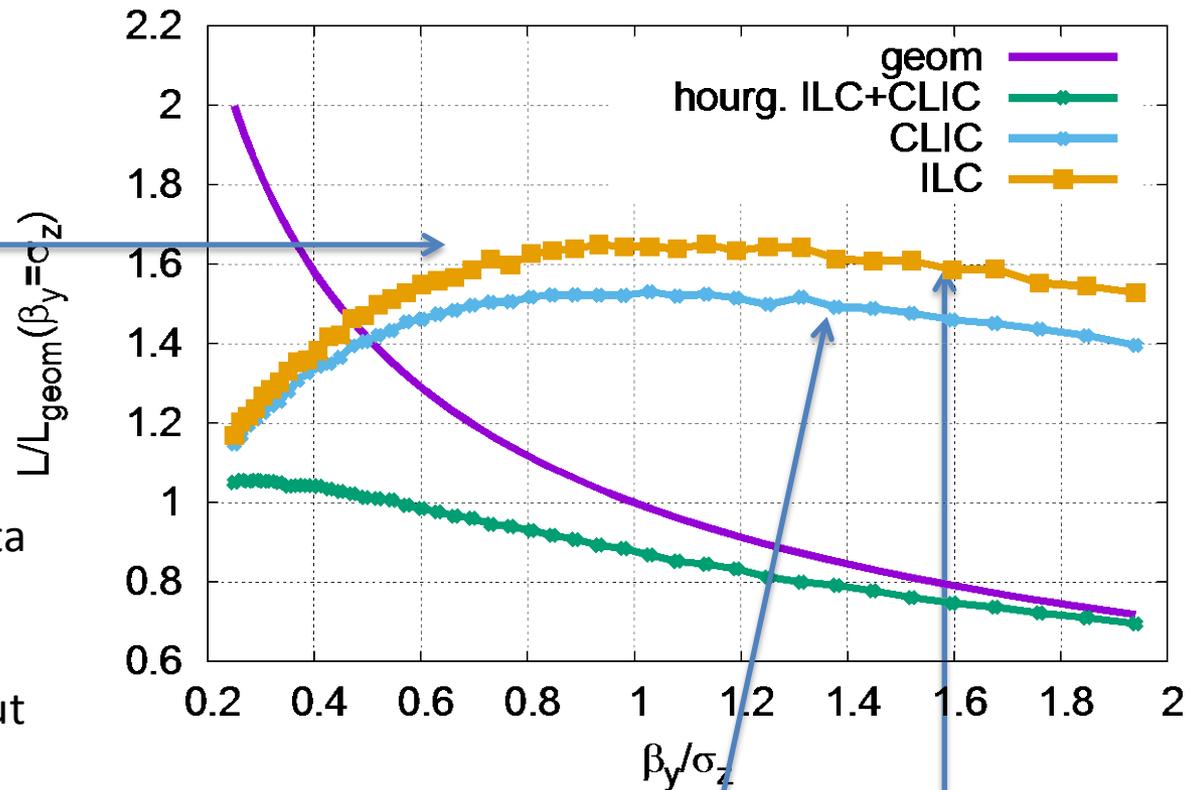
Beam-beam Effects

Including pinch effect

$$\mathcal{L} = H_D \frac{N^2}{4\pi\sigma_x\sigma_y} n_b f_r$$

There is an optimum value for beta

For smaller beta-function the geometric luminosity increases but the enhancement is reduced



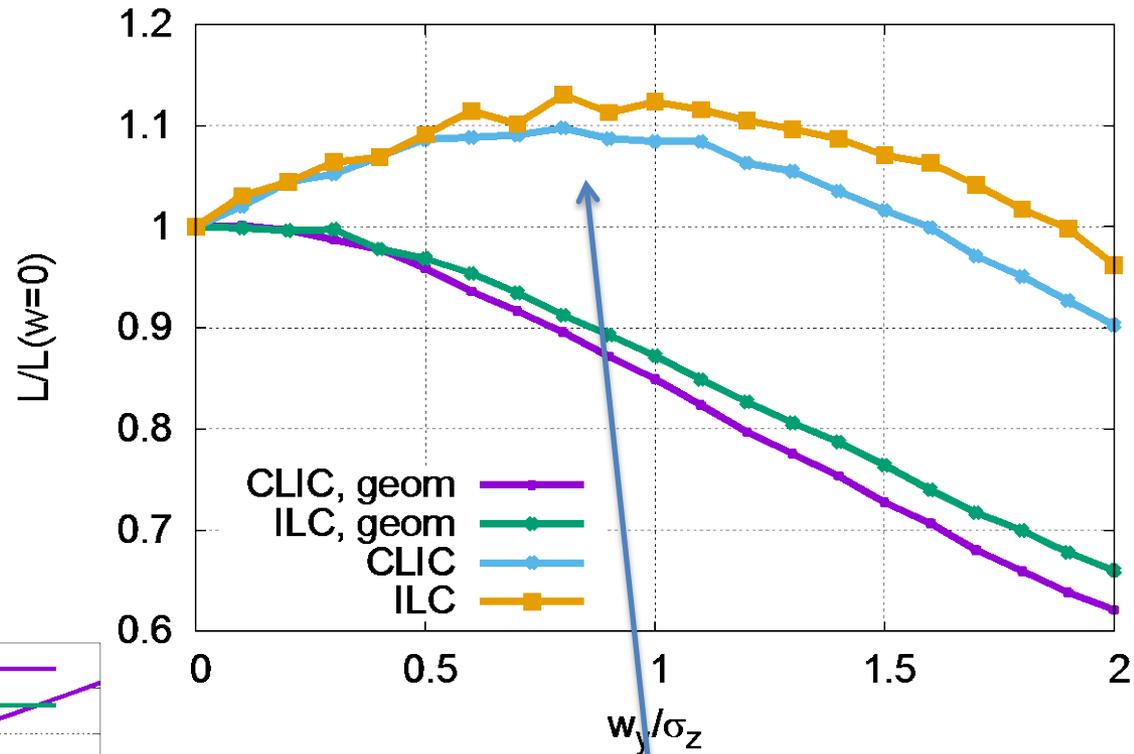
Small beta-functions lead to
 High chromaticity
 ⇒ Optics is difficult
 Large divergence
 ⇒ Quadrupole aperture is limited

CLIC choice

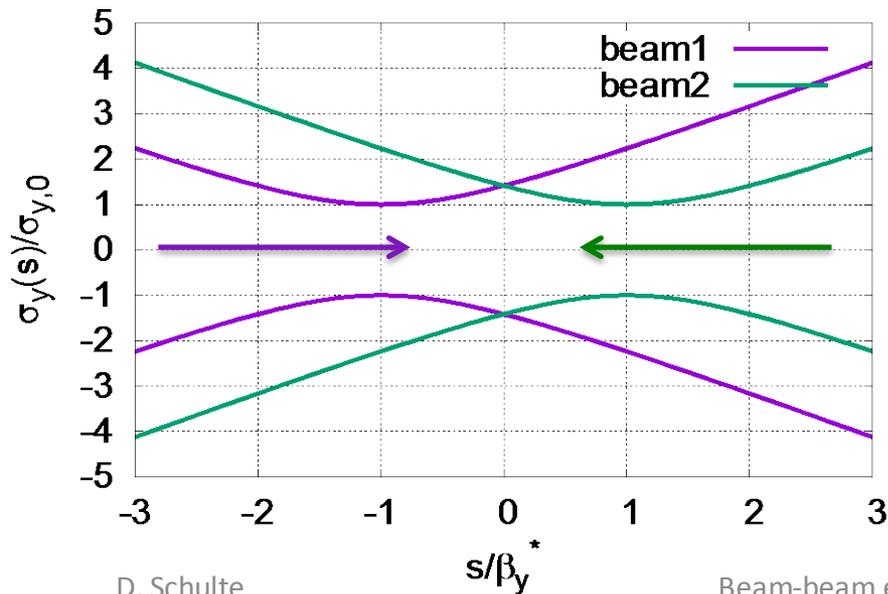
ILC choice

Waist Shift

Focusing before IP leads to more luminosity (D.S.)



For CLIC and ILC ~10% luminosity gain

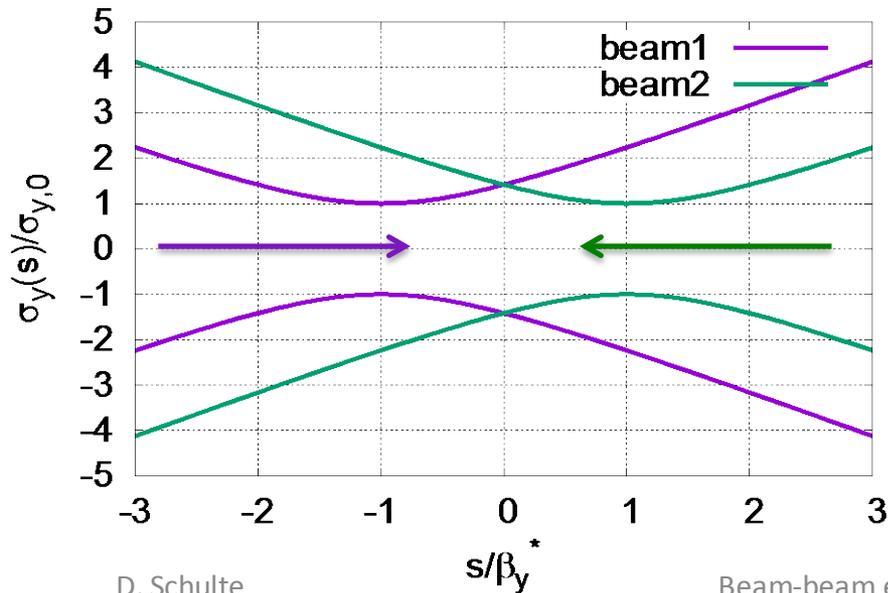
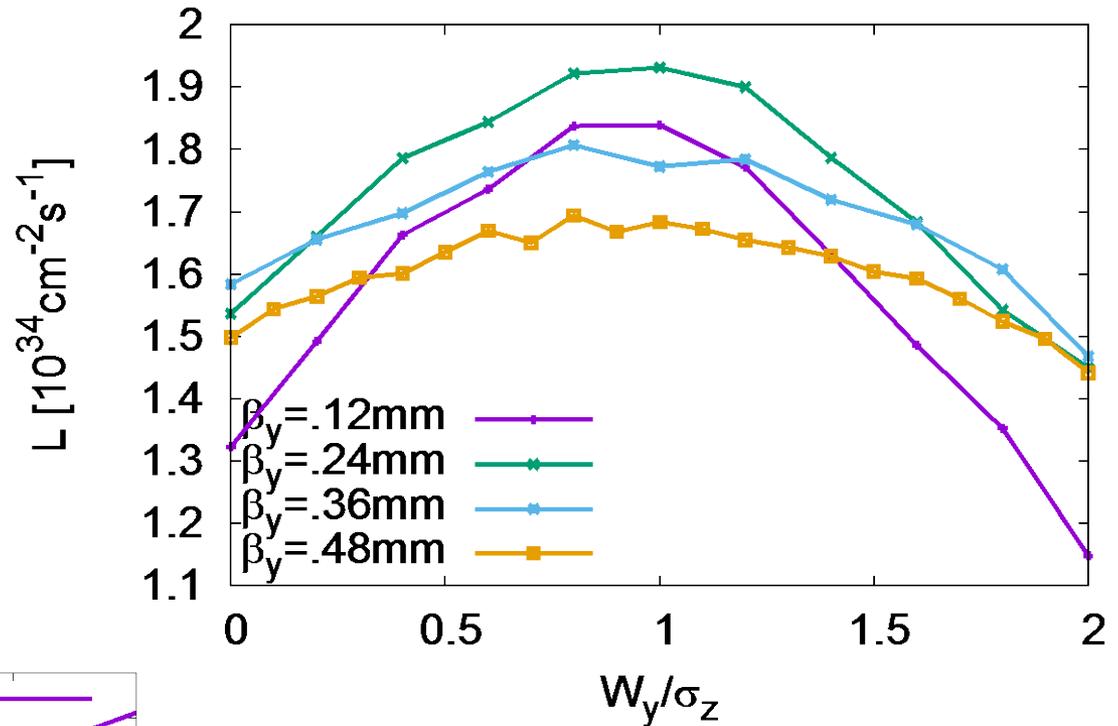


Note: ILC Full Optimisation

For ILC could consider smaller vertical beta-functions

Smaller beta-functions profit more from waist shift
 \Rightarrow 0.24mm seems best

Would gain 15% luminosity



But still more difficult to produce
 (larger divergence)
 And tolerances become tighter

Luminosity and Offset

Luminosity loss for rigid bunches with offset

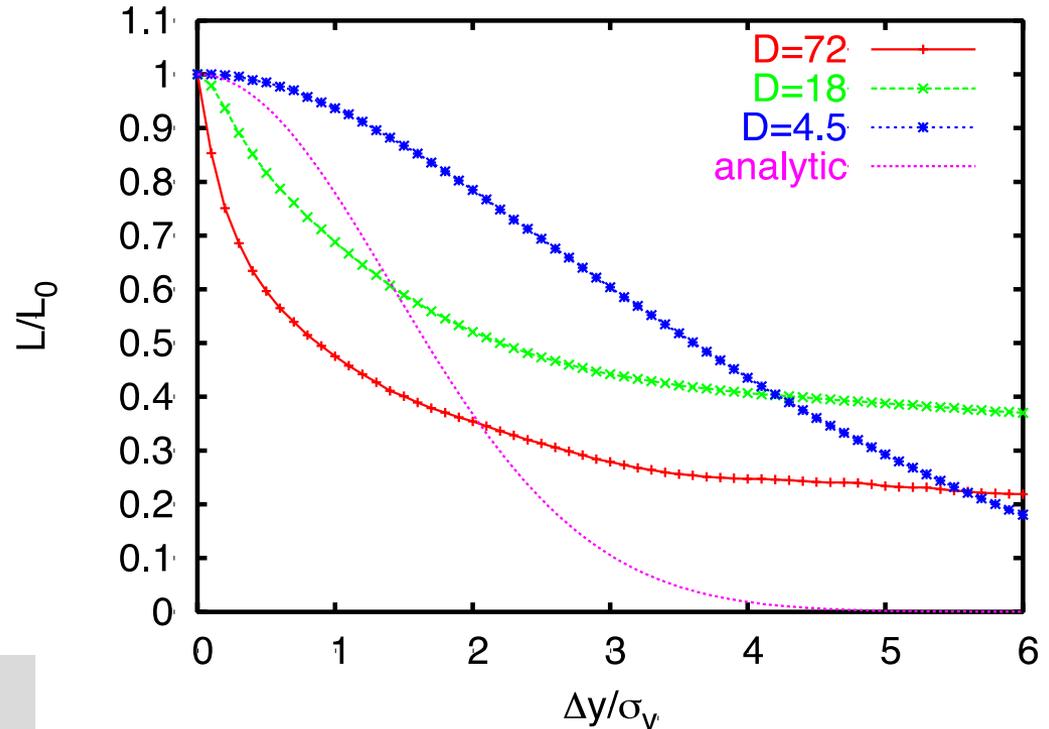
$$\frac{\mathcal{L}}{\mathcal{L}_0} = \exp\left(-\frac{\Delta y^2}{4\sigma_y^2}\right)$$

Actual loss depends strongly on disruption

Note: the simulations suffer from noise (use of macroparticles)

Need to enforce symmetric charge distribution to simulate high disruption

Can you trust the results in real life?



Luminosity and Offset

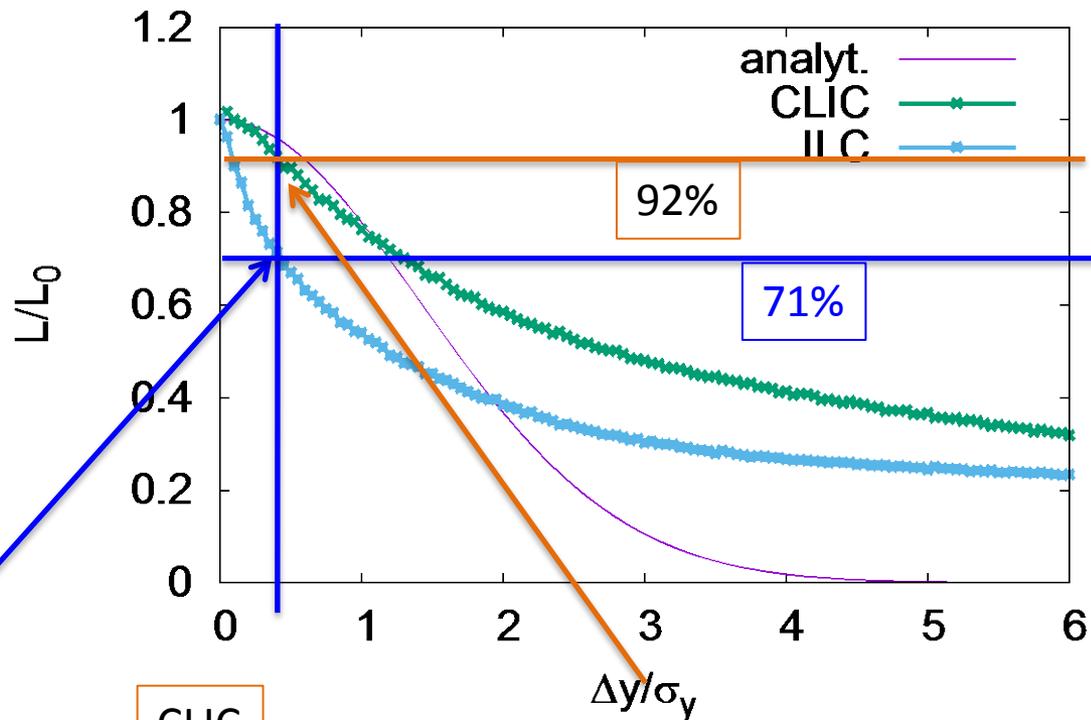
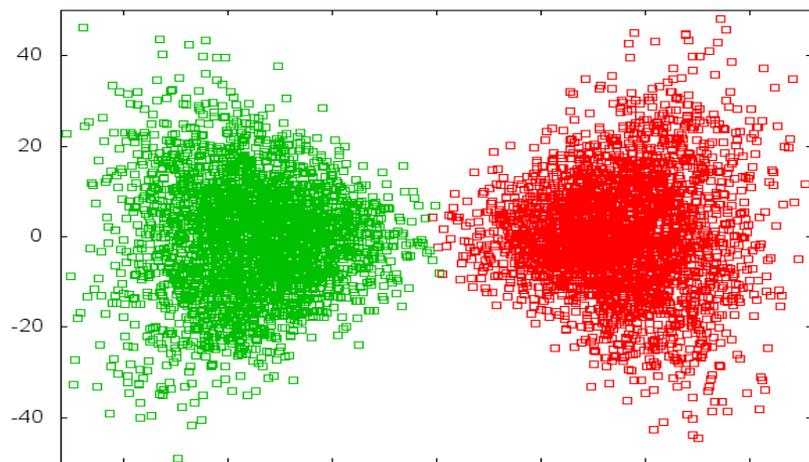
Luminosity loss for beam offsets depends strongly on disruption parameter

$$\Delta y = 0.4 \sigma_y$$

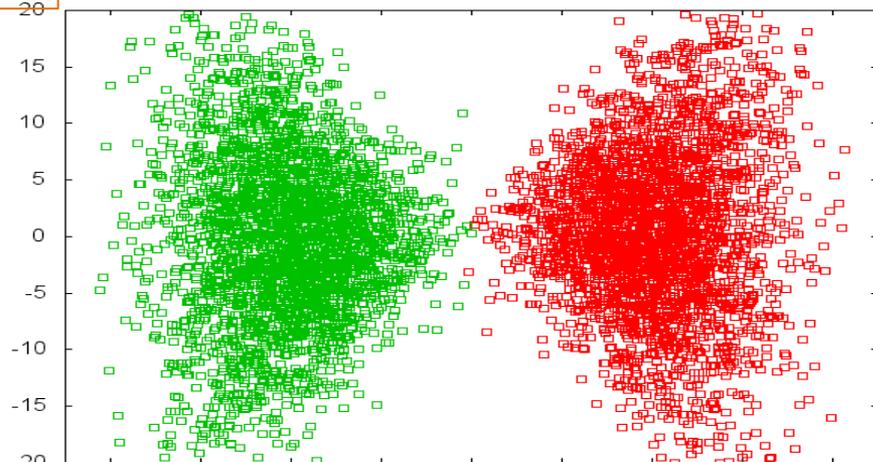
$$L = 0.71 L_0 \quad D_y \sim 24$$

$$L = 0.92 L_0 \quad D_y \sim 12$$

ILC



CLIC



Luminosity and Offset

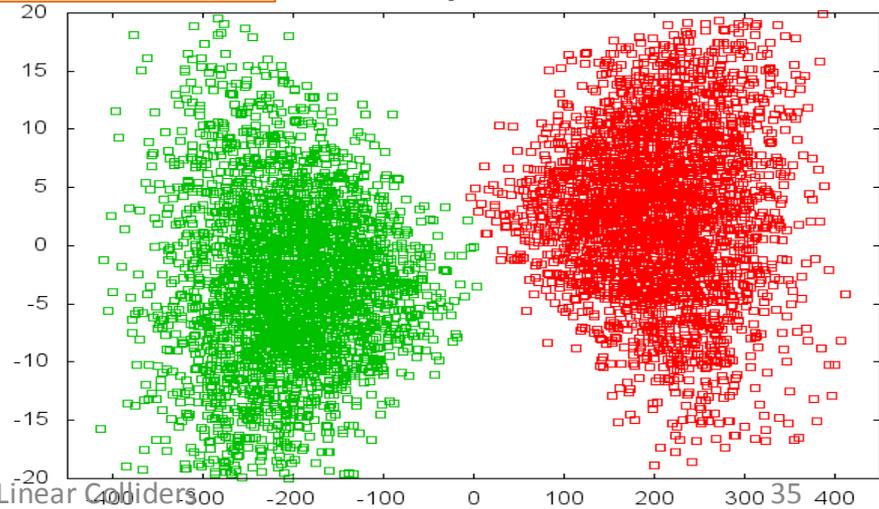
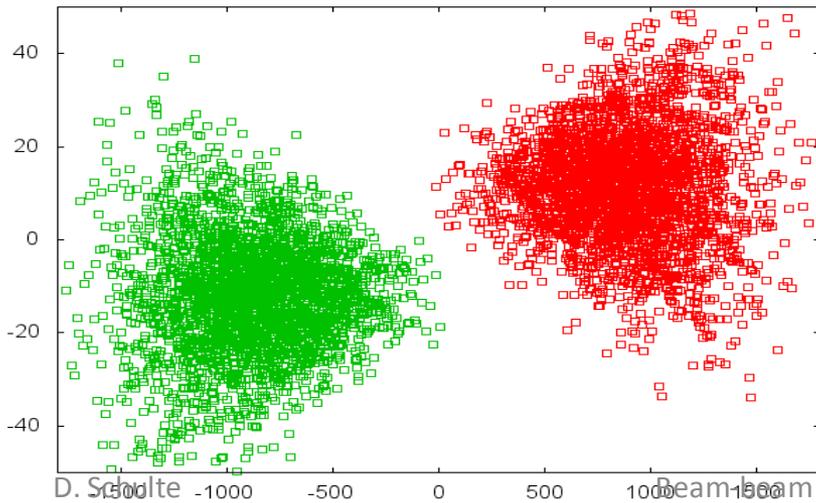
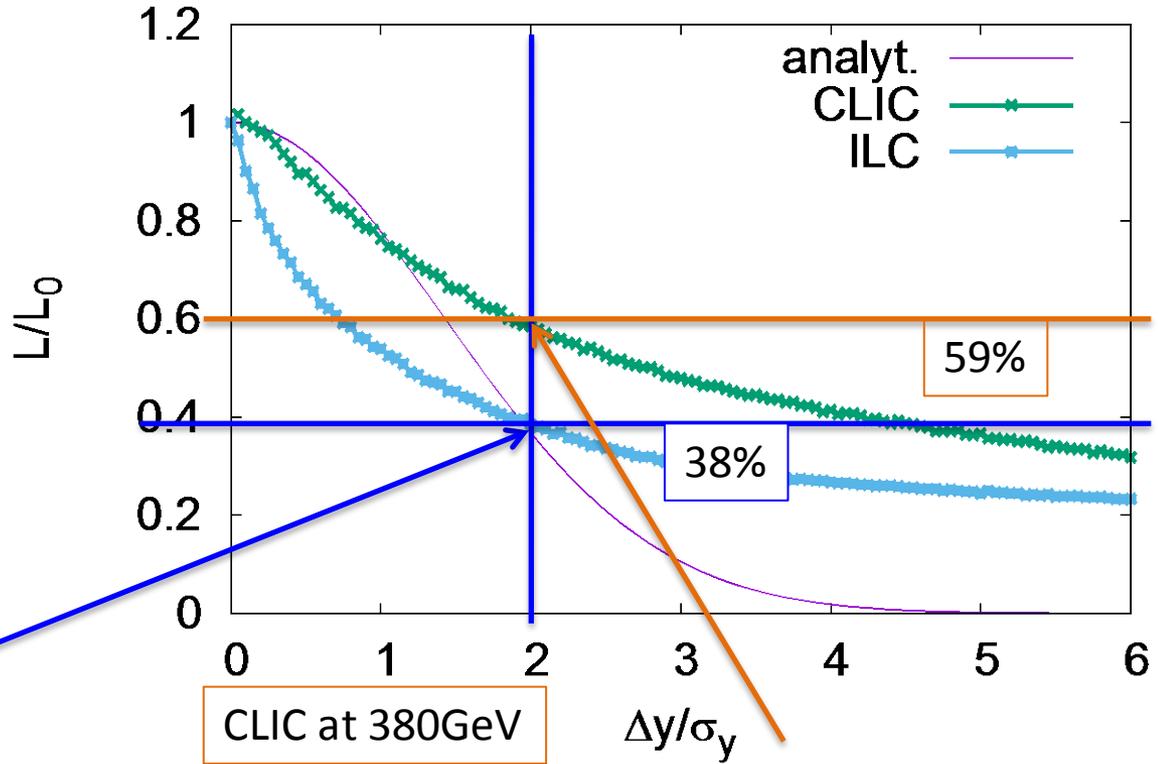
Luminosity loss for beam offsets depends strongly on disruption parameter

$$\Delta y = 2 \sigma_y$$

$$L = 0.38 L_0$$

$$L = 0.59 L_0$$

ILC

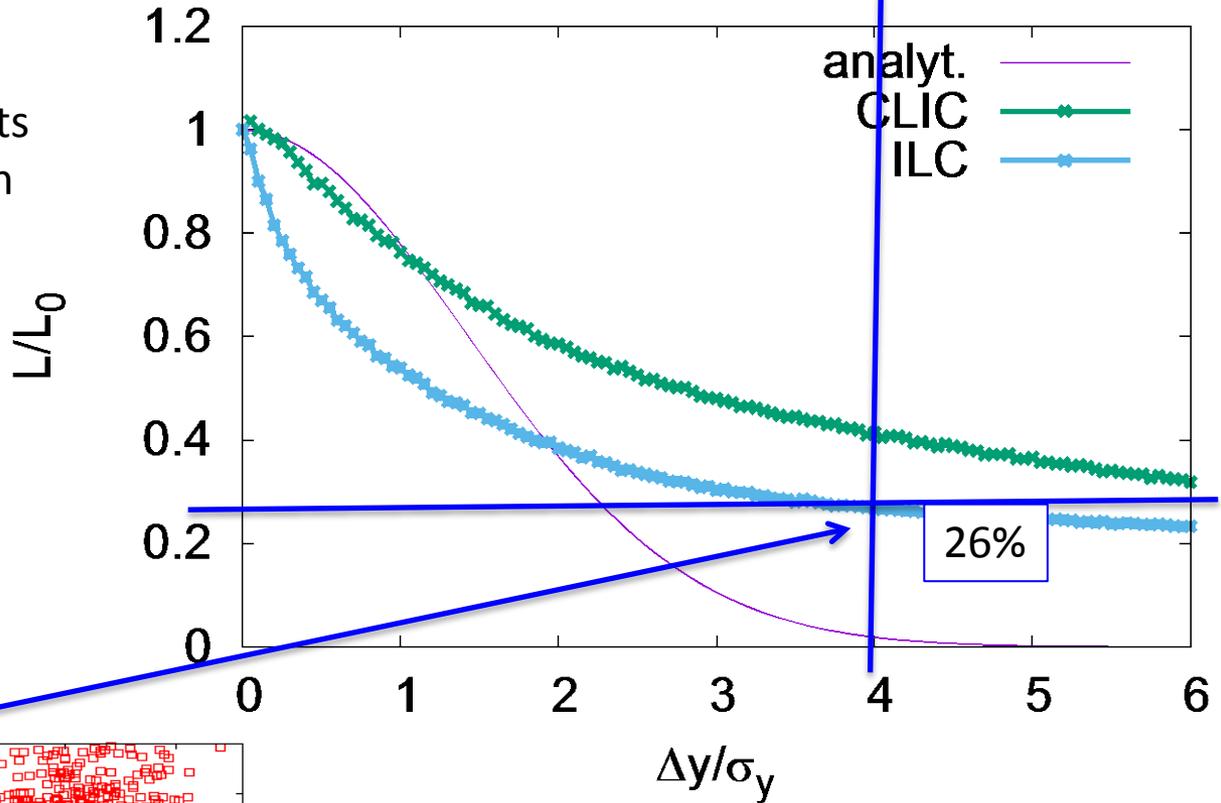


Luminosity and Offset

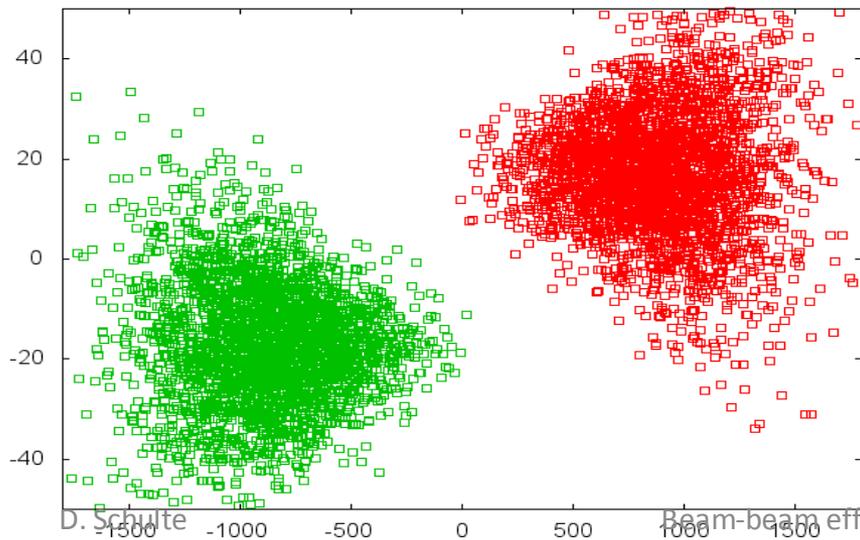
Luminosity loss for beam offsets depends strongly on disruption parameter

$$\Delta y = 4 \sigma_y$$

$$L = 0.26 L_0$$



ILC

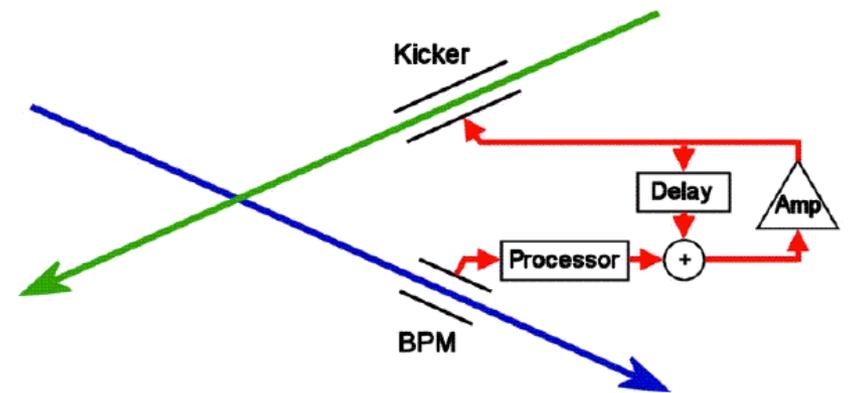
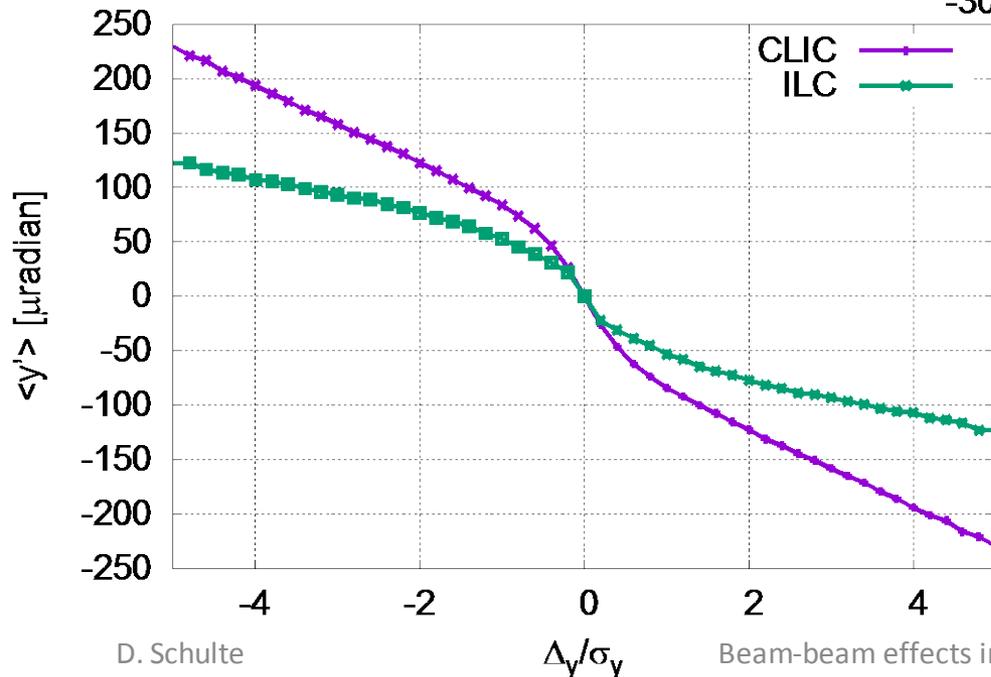
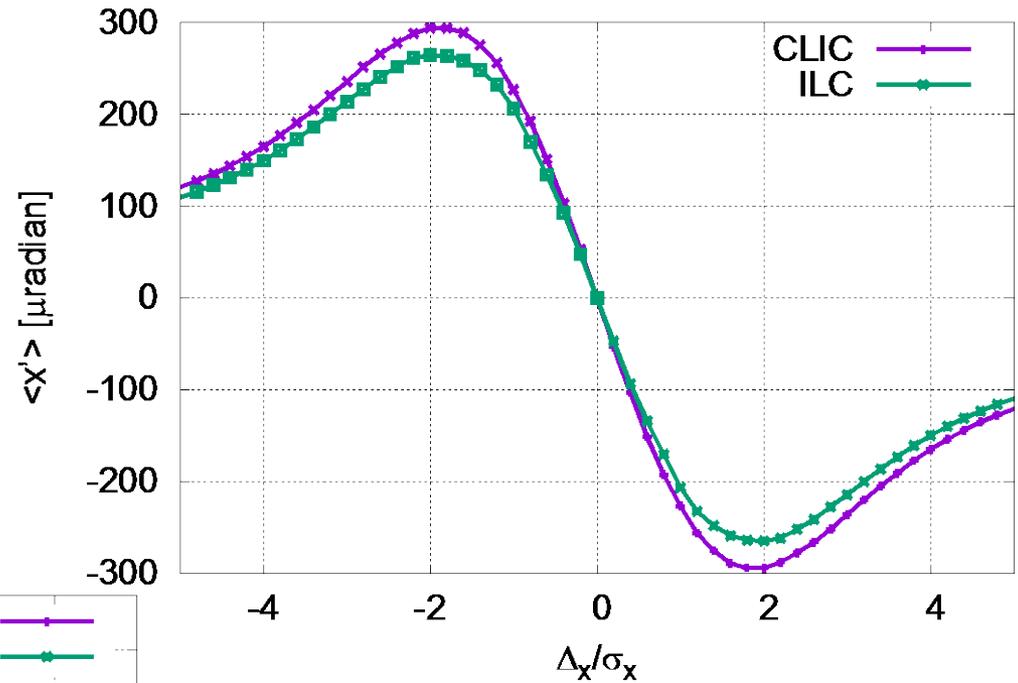


Beam-beam Deflection

Strong deflection allows to easily measure and correct offset

In CLIC an offset $\Delta_y = 0.1\sigma_y = 0.1\text{nm}$
 \Rightarrow 3m downstream of IP $40\mu\text{m}$ beam offset

Get great signals for the BPMs

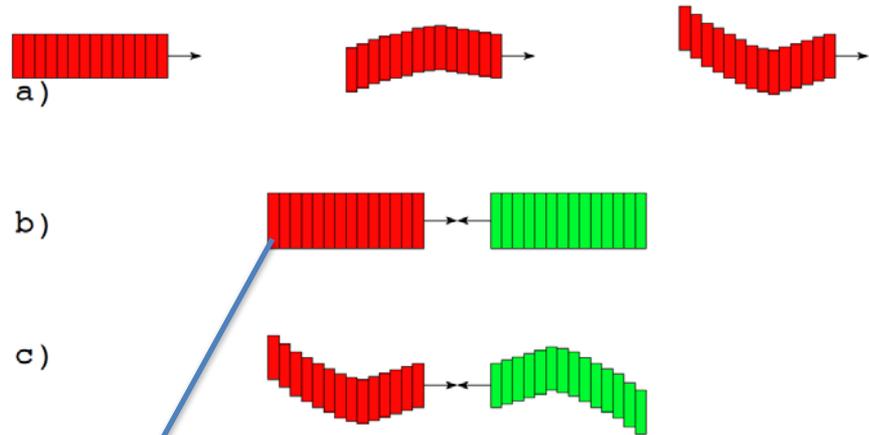


Note: The Banana Effect

a) Wakefields+dispersion can create banana-shaped bunch in main linac

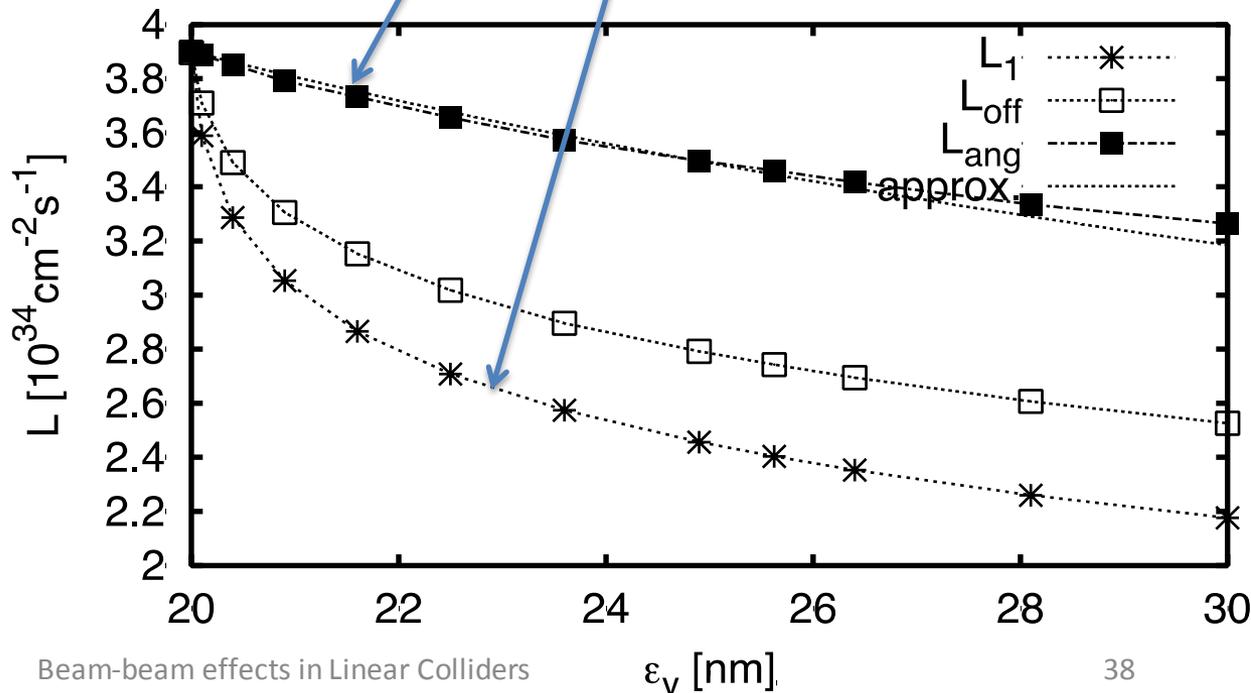
b) Do not model with projected emittance

c) The correct shape should be used



For large disruption (ILC) banana can reduce luminosity

Study done for TESLA
Similar disruption as ILC



CLIC 3TeV Beamstrahlung

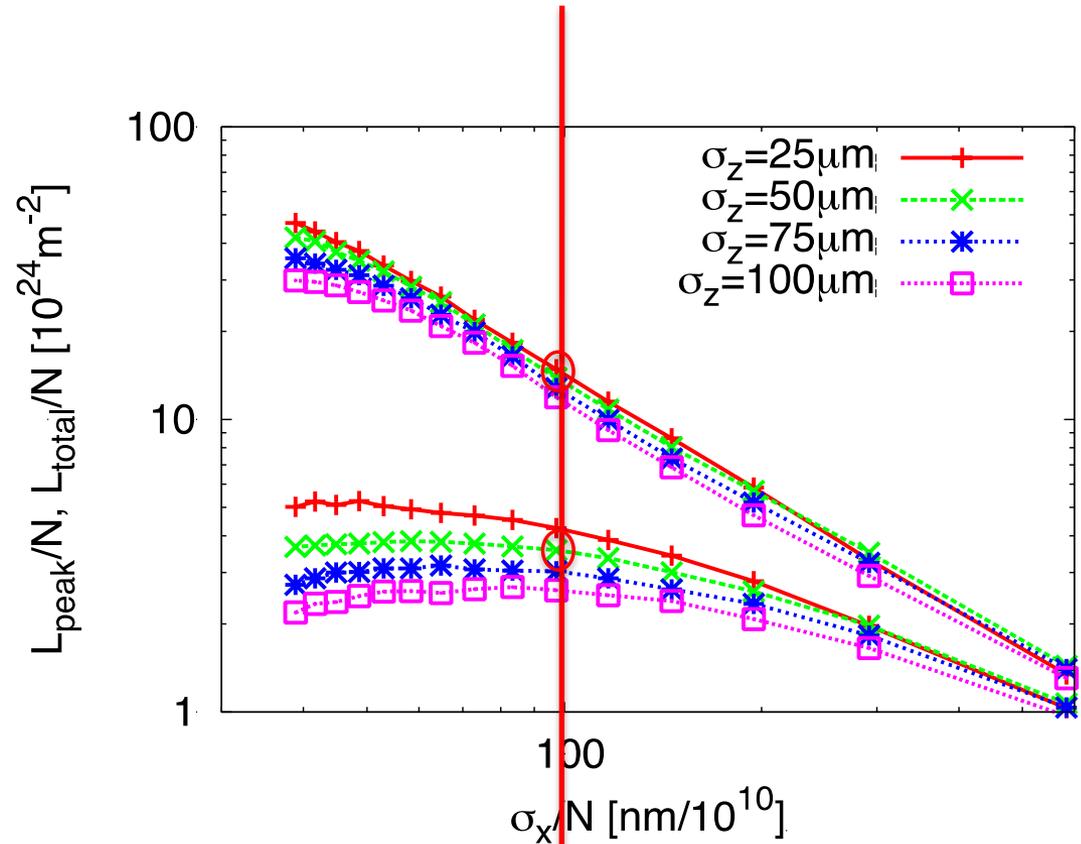
Goal is to maximise $L_{0.01}$

And $L_{0.01}/L > 0.3$

$$\Upsilon \gg 1$$

$$n_\gamma \propto \left(\frac{\sigma_z}{\gamma}\right)^{\frac{1}{3}} \left(\frac{N}{\sigma_x + \sigma_y}\right)^{\frac{2}{3}}$$

$$\mathcal{L} \propto \frac{n_\gamma^{3/2}}{\sqrt{\sigma_z}} \eta P_{wall} \frac{1}{\sigma_y} \cdot H_D$$



Coherent Pair Creation

Beam fields in the rest system of a photon can reach the **Schwinger Critical Field**
⇒ The quantum electrodynamics becomes non-linear

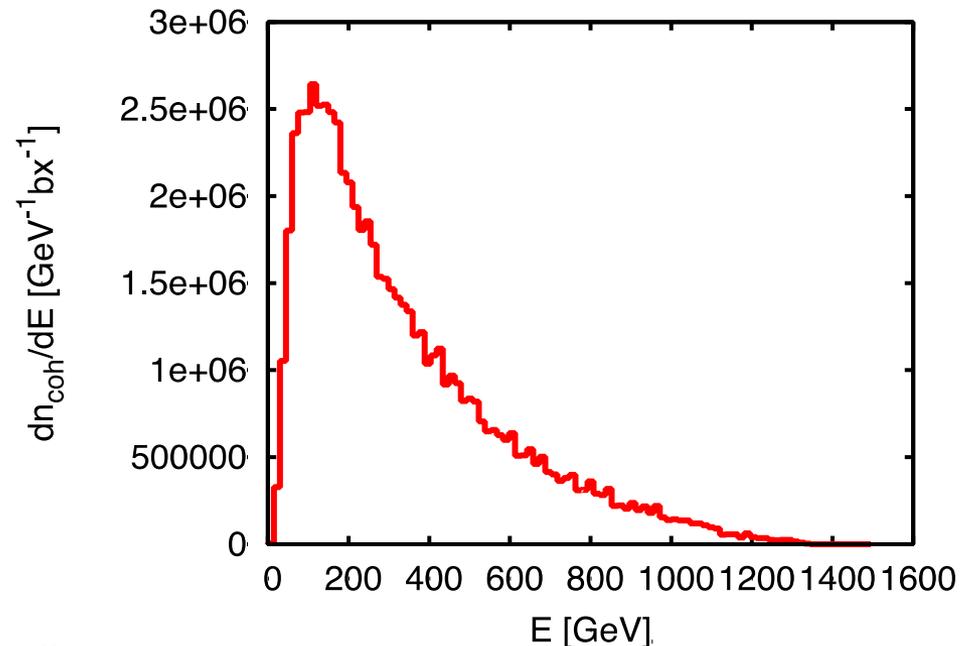
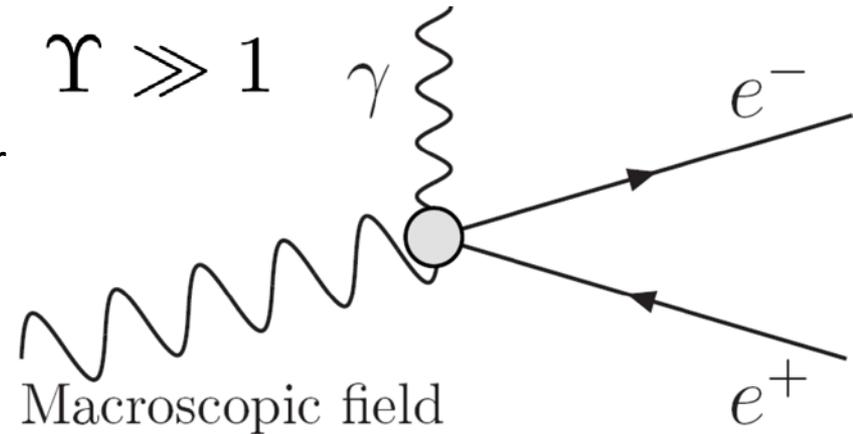
A photon in a very strong field can form an electron-positron pair
⇒ Coherent pair creation

$$\frac{\gamma B}{B_c} = \Upsilon$$

$$B_c \approx 4.4 \times 10^9 \text{ T}$$

Produce 6.8×10^8 pairs

Average particle energy 0.3 TeV



Spent Beam Divergence

Beam particles are focused by oncoming beam

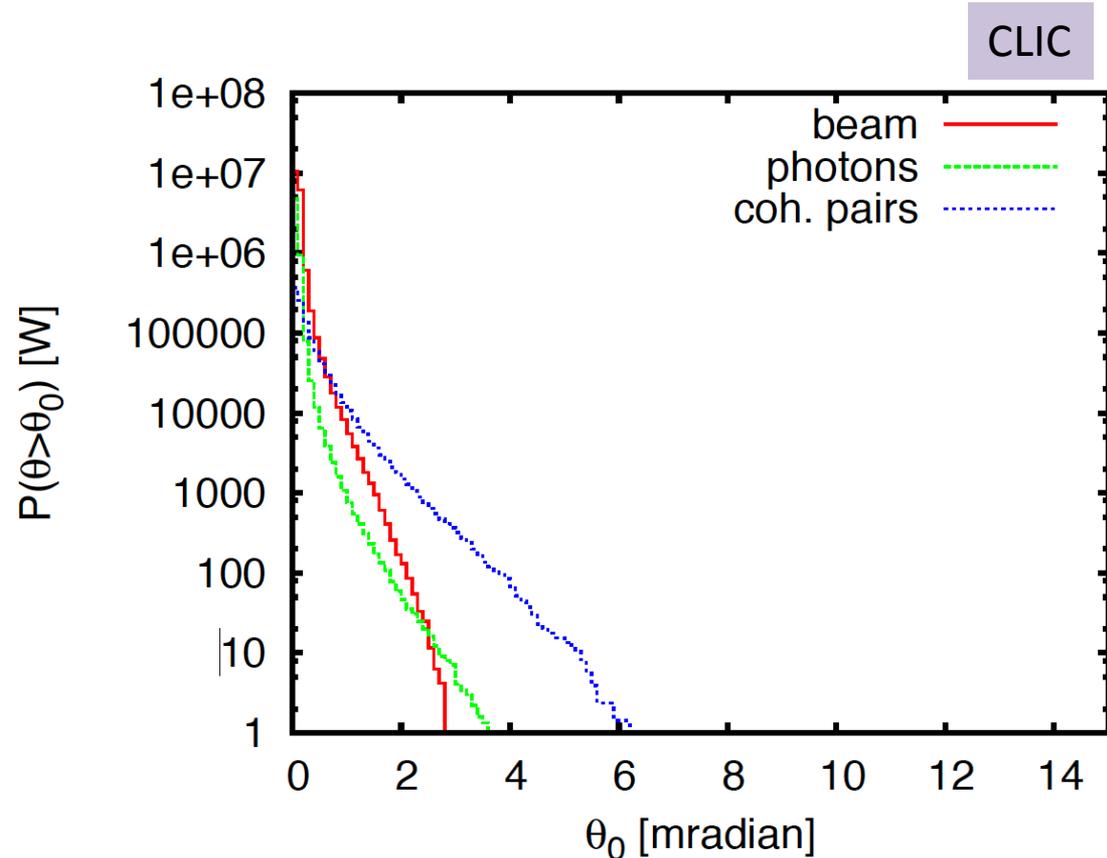
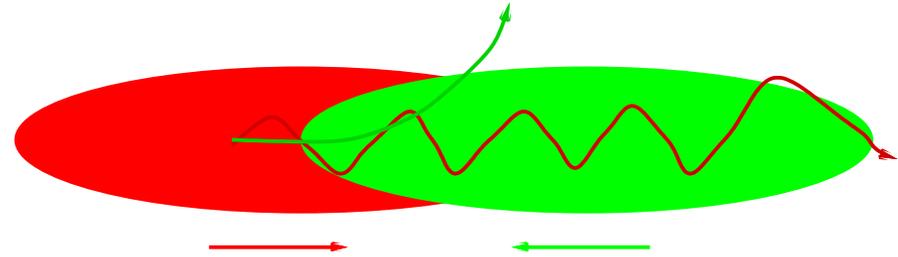
Photons are radiated into direction of beam particles

Coherent pair particles can be focused or defocused by the beams but deflection limited due to their high energy

-> Extraction hole angle should be significantly larger than 6mradian

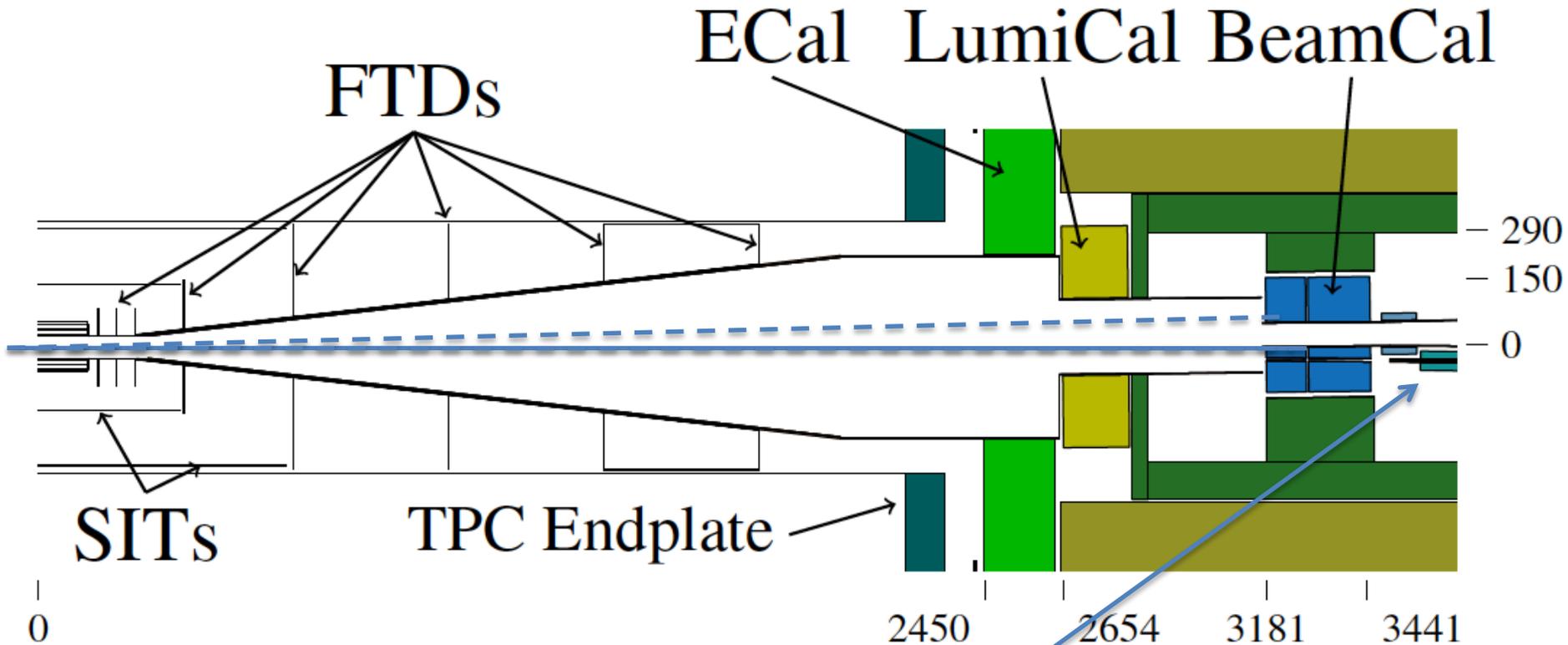
We chose 10mradian for CLIC
-> 20mradian crossing angle

ILC requires 14mradian crossing angle



1 W \approx 400 TeV/bx \approx
300 beamparticles/bx

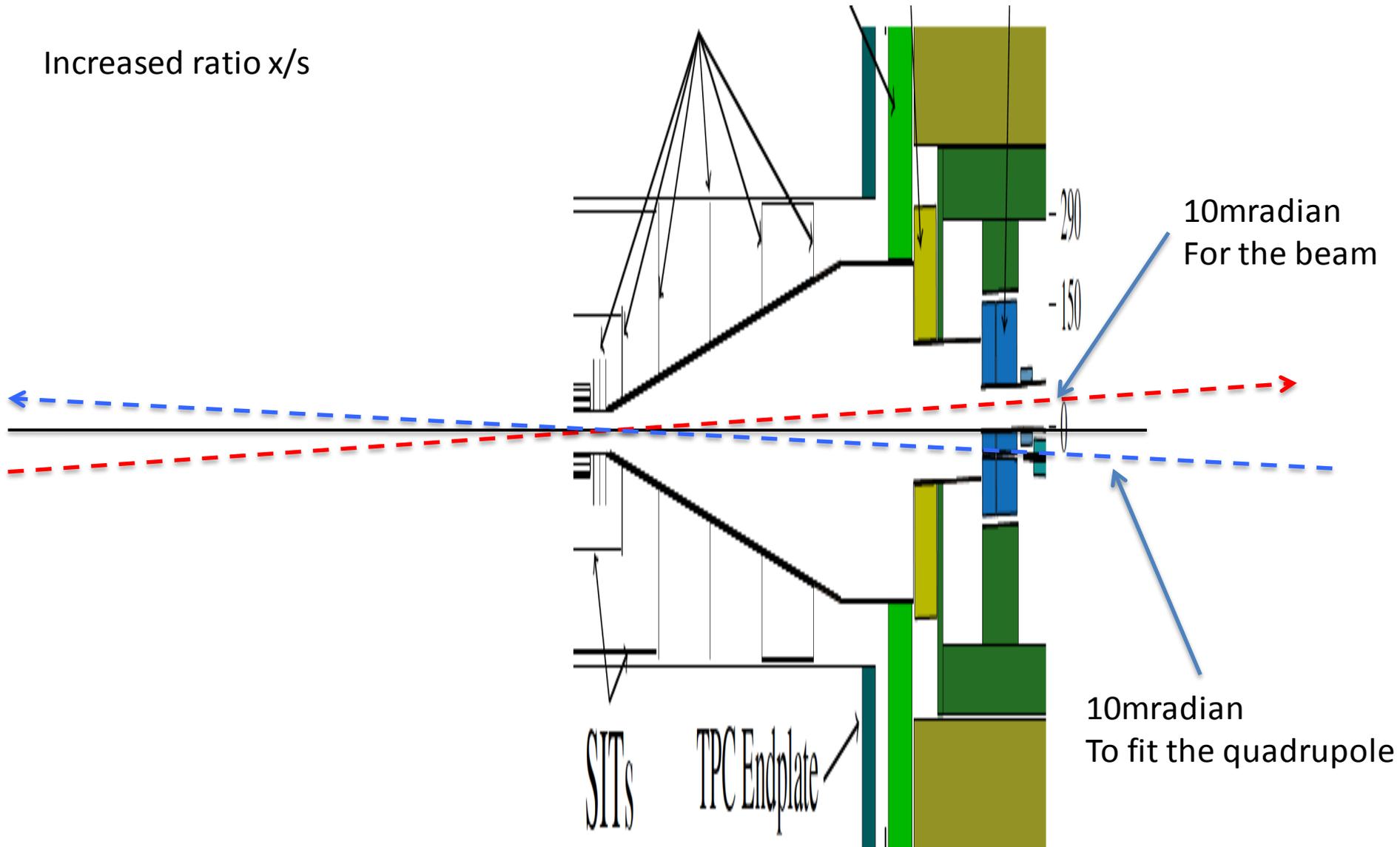
CLIC Inner Detector Layout



The last focusing magnet of the machine is inside of the detector

A. Seiler

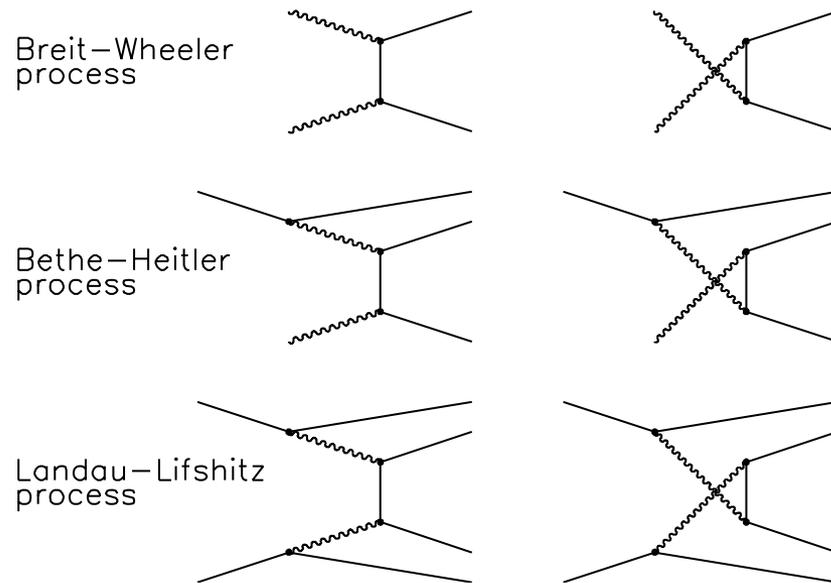
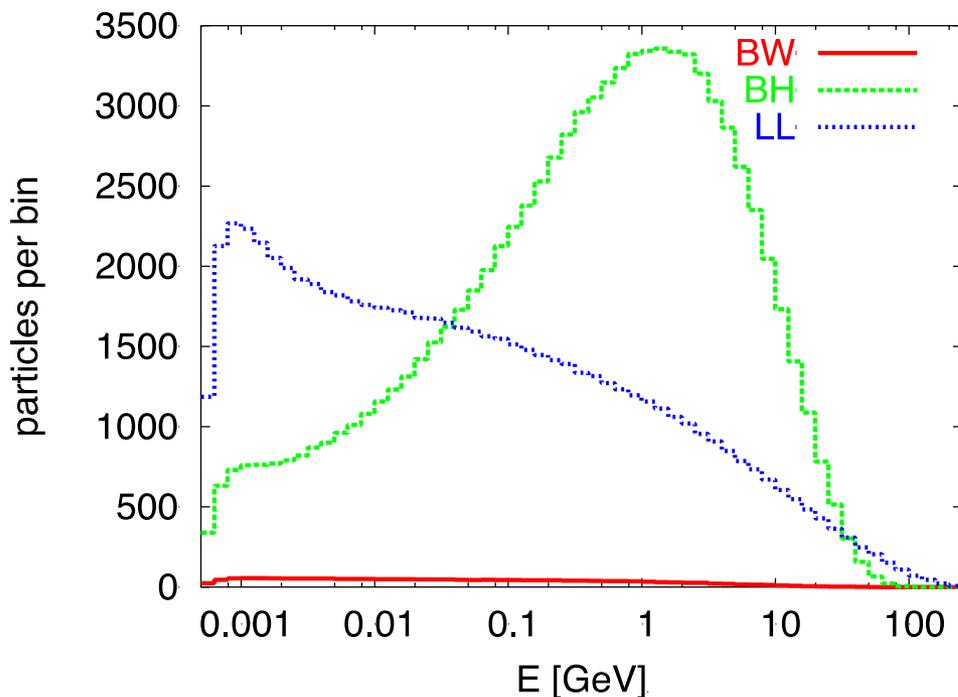
CLIC Inner Detector Layout



Electron-Positron Pair Production

Colliding photons can produce electron-positron pairs (incoherent pair production)

$O(10^5)$ per bunch crossing



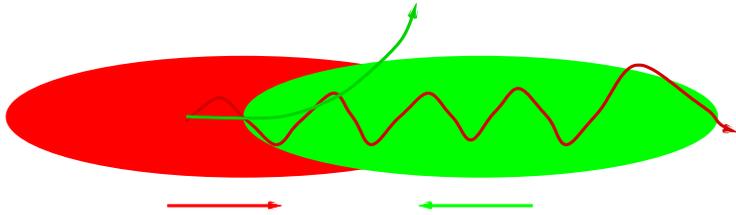
Note: beamsizes effect gives some reduction, ignored here

Also muons can be produced, but small rate

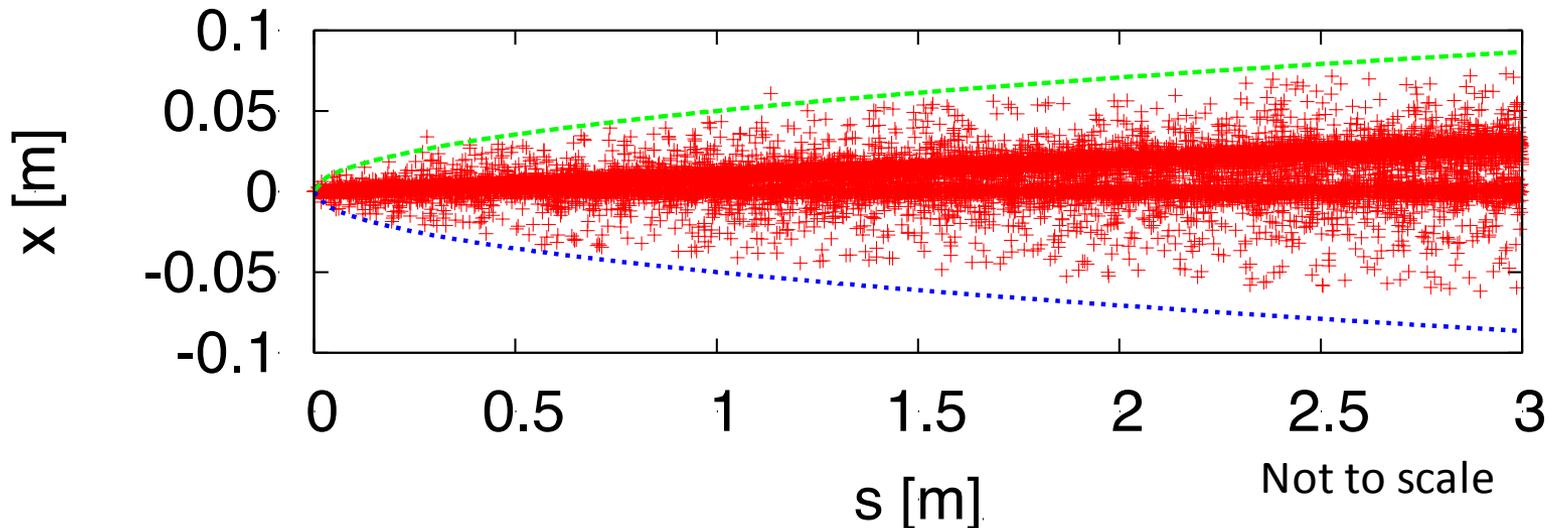
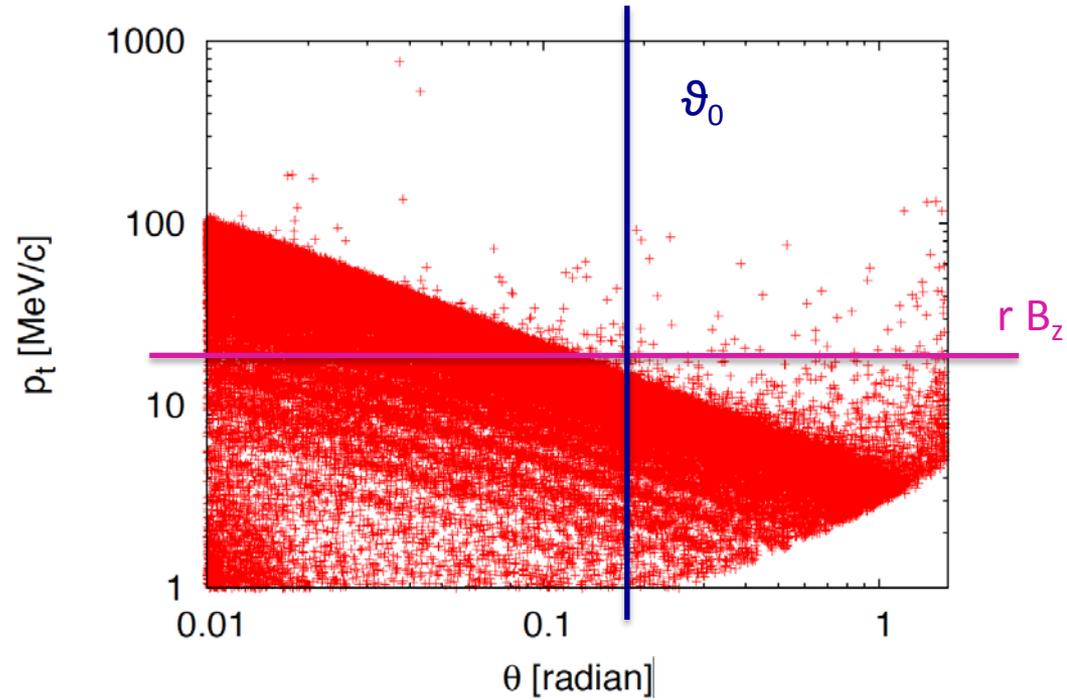
ILC and CLIC Main Parameters

Parameter	Symbol [unit]	ILC	CLIC	CLIC
Centre of mass energy	E_{cm} [GeV]	500	380	3000
Total luminosity	L [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	1.8	1.5	6
Luminosity in peak	$L_{0.01}$ [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	1	0.9	2
Particles per bunch	N [10^9]	20	5.2	3.72
Bunch length	σ_z [μm]	300	70	44
Collision beam size	$\sigma_{x,y}$ [nm/nm]	474/5.9	149/2.9	40/1
Vertical emittance	$\epsilon_{x,y}$ [nm]	35	40	20
Photons per beam particle	n_γ	1.9	1.5	2.1
Average photon energy	$\langle E_\gamma/E_0 \rangle$ [%]	2.4	4.5	13
Coherent pairs	N_{coh}	-	-	6.8×10^8
Their energy	E_{coh} [TeV]	-	-	2.1×10^8
Incoherent pairs	N_{incoh}	196×10^3	58×10^3	300×10^3
Their energy	E_{incoh} [TeV]	484	187	2.3×10^4

Incoherent Pairs

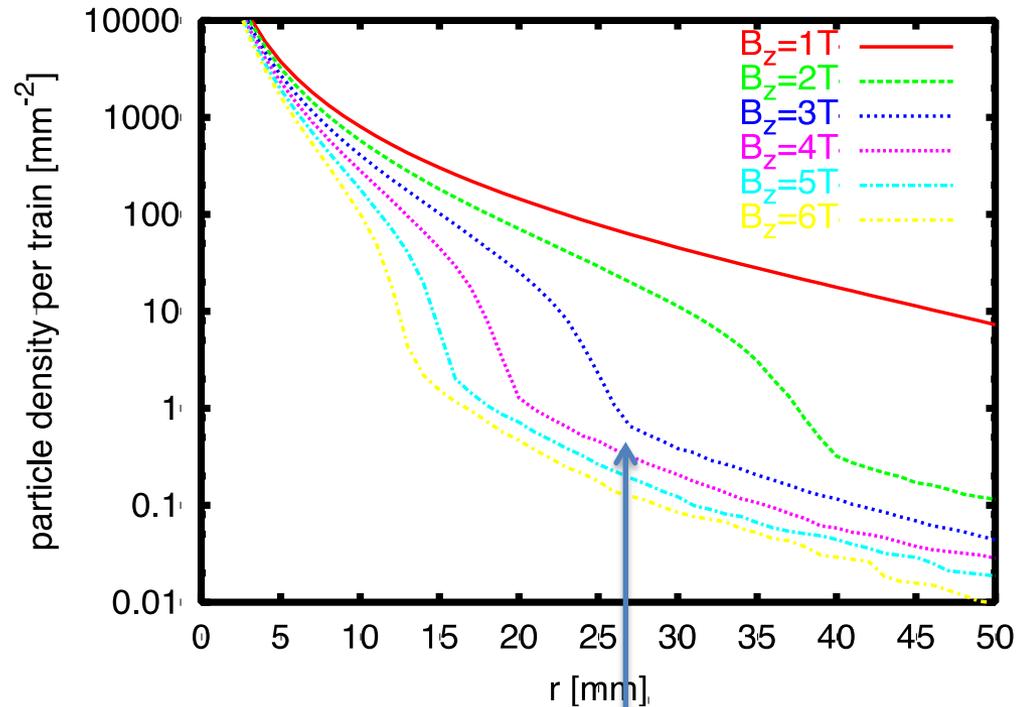
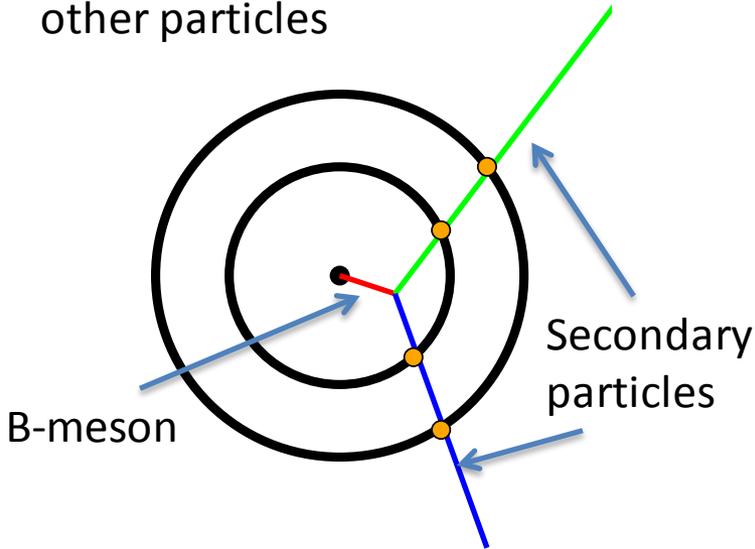


Incoherent pairs can be strongly deflected by the
Maximum deflection angle depends on their energy

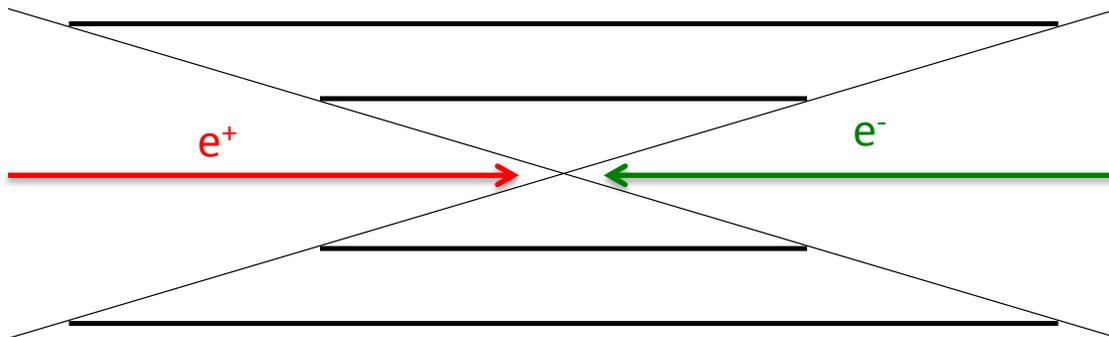


Impact on Vertex Detector

To vertex detector can identify particles originating from decays of other particles



Need a certain angular coverage



Hit density from pairs depends on radius and field
Edge is due to beam-beam deflection

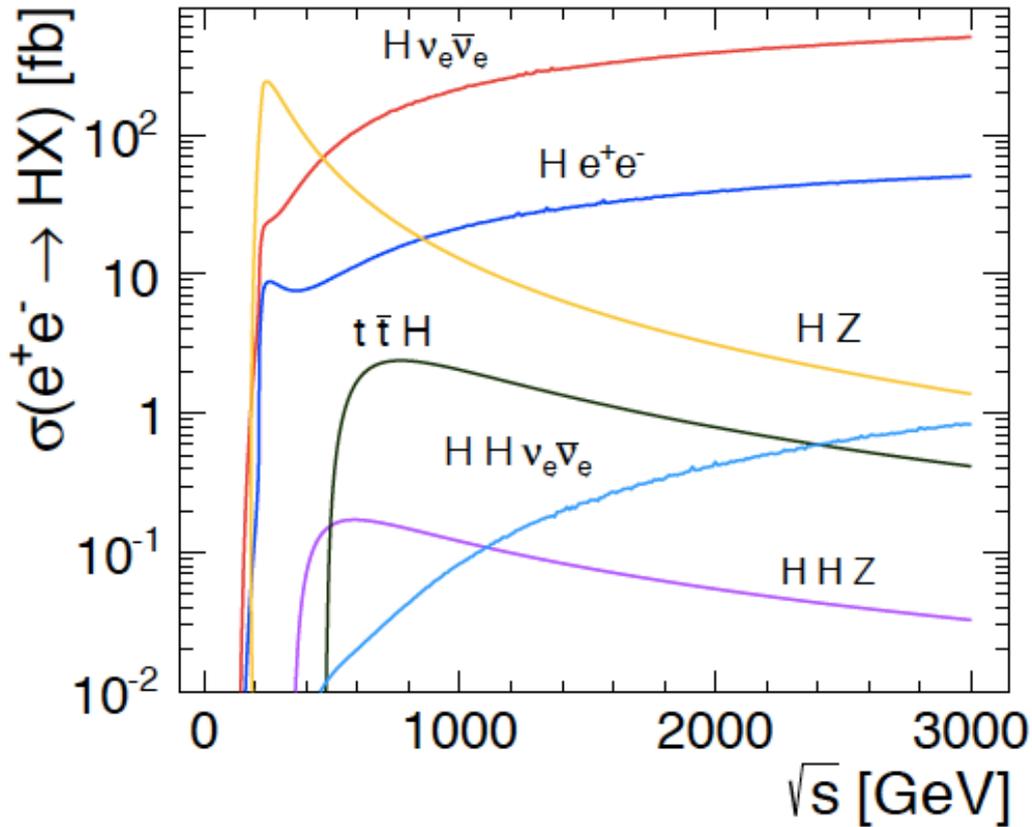
Limit $O(1\text{mm}^{-2})$

Conclusion

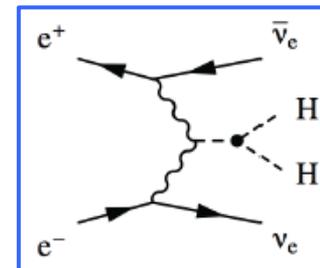
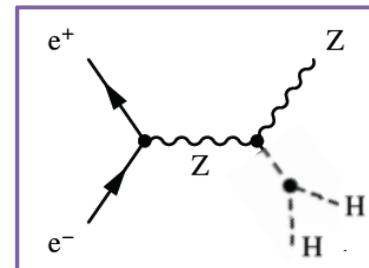
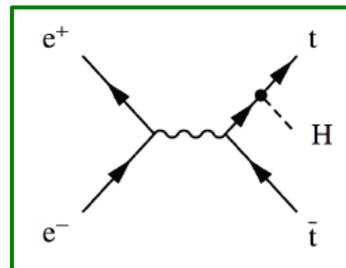
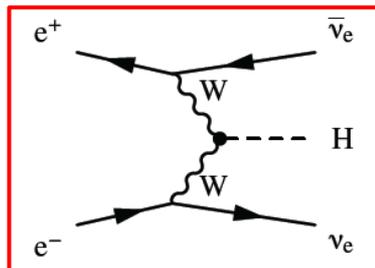
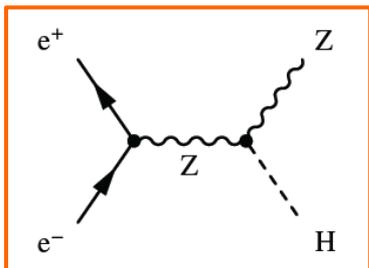
- Beam-beam effects have critical impact on luminosity in linear colliders
 - Strong pinching enhances luminosity
 - Simulations tool are important
 - Beamstrahlung requires flat beams and gives lower limit on horizontal size
 - Has impact on experiment performance
 - For high disruption collisions can be unstable
 - Very good beam-beam stability is required
 - Non-linear QED can appear at high energies
 - Beam charge can increase by $O(10\%)$
- Machine background poses important constraints on the experiment
 - Minimum vertex detector radius is given by beam parameters

Reserve

Higgs Physics in e+e- Collisions



- **Precision Higgs measurements**
- Model-independent
 - Higgs couplings
 - Higgs mass
- Large energy span of linear colliders allows to collect a maximum of information:
 - ILC: 500 GeV (1 TeV)
 - CLIC: ~350 GeV – 3 TeV

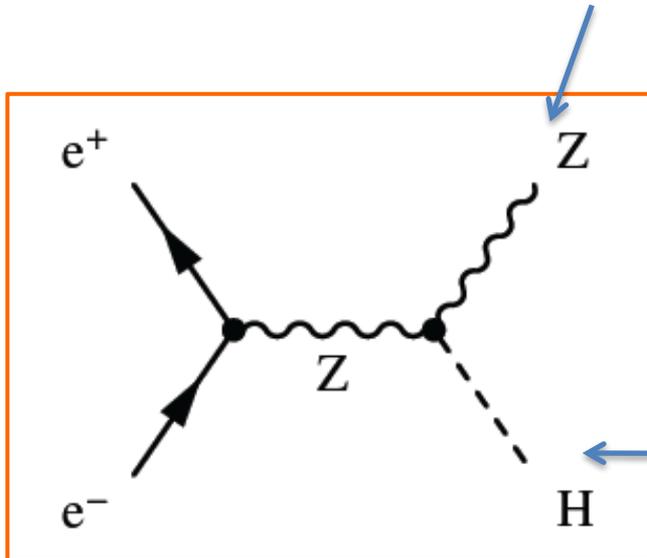


Invisible Higgs Decays

Can we check that the Higgs does not decay into something invisible, e.g. neutrinos?

Yes, missing mass (or recoil mass) analysis:

1) Measure the Z, e.g. from produced jets



2) Subtract Z momentum from initial state

$$(E_{\text{cm}}, 0, 0, 0) - (E_Z, P_{Z,x}, P_{Z,y}, P_{Z,z}) = (E_H, P_{H,x}, P_{H,y}, P_{H,z})$$

3) Result is mass and momentum of other particle
Even if we do not see it

So we know the missing particle

Automatic Parameter Determination

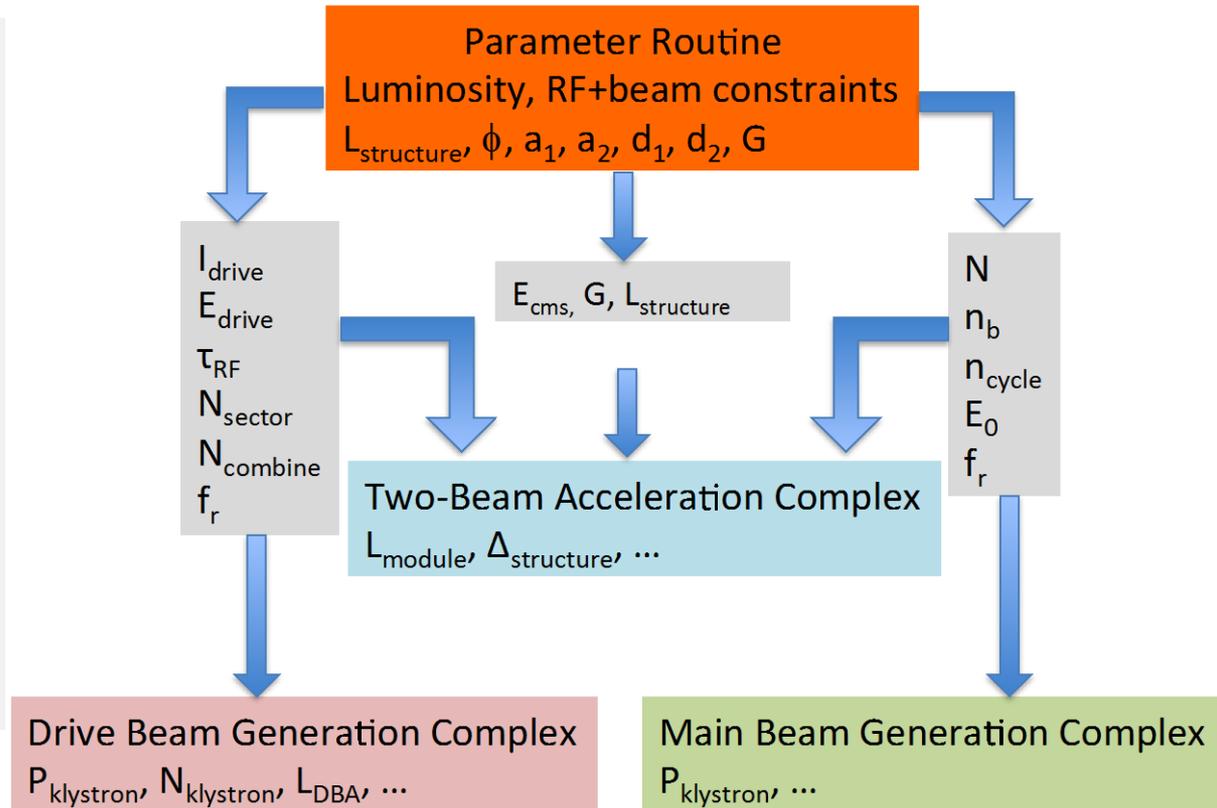
Structure design fixed by few parameters

$$a_1, a_2, d_1, d_2, N_c, \phi, G$$

Beam parameters derived automatically to reach specific energy and luminosity

Consistency of structure with RF constraints is checked

Repeat for 1.7 billion cases



Design choices and specific studies

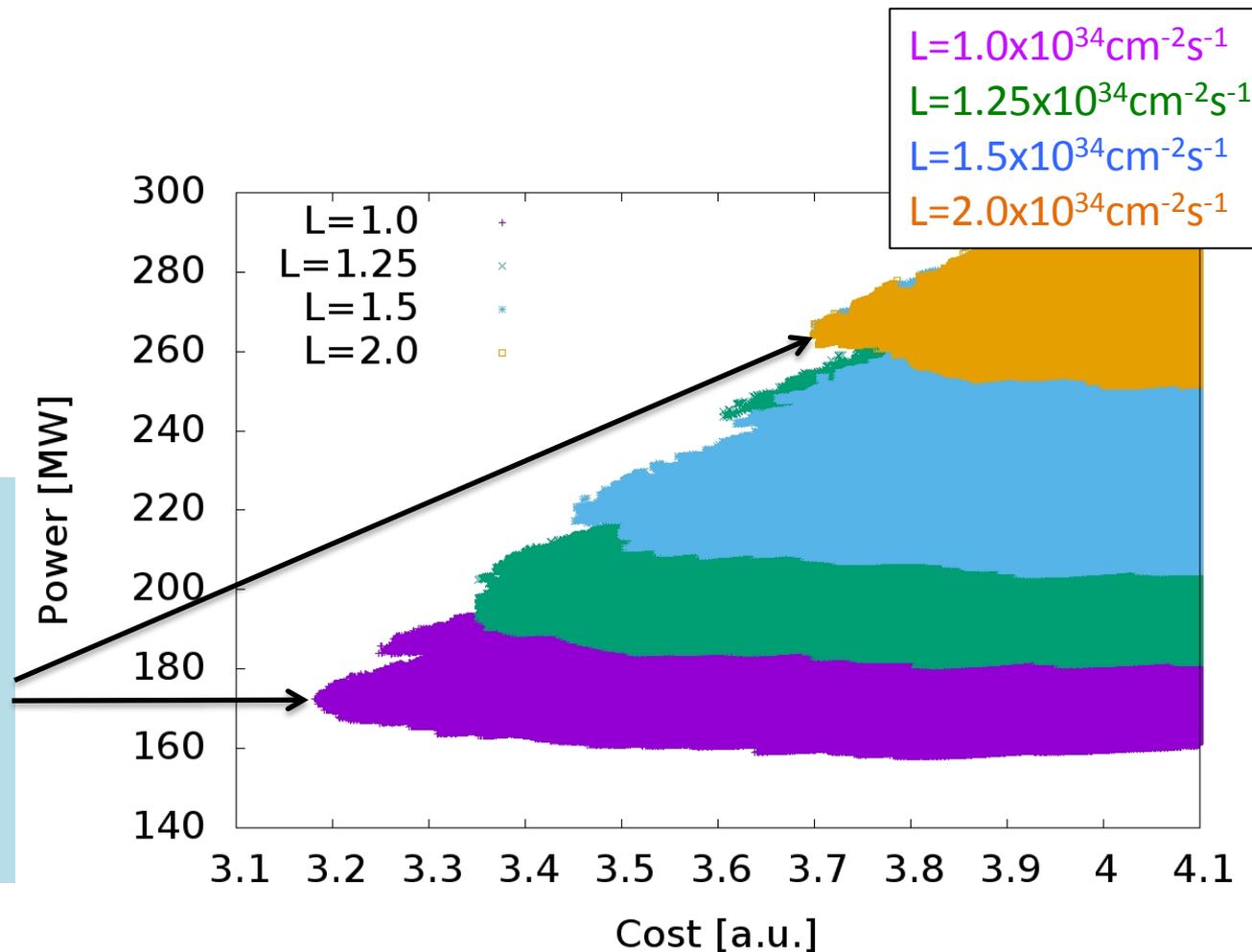
- Use 50Hz operation for beam stability
- Scale horizontal emittance with charge to keep the same risk in damping ring
- Scale for constant local stability in main linac, i.e. tolerances vary but stay above CDR values
- BDS design similar to CDR, use improved β_x -reach as reserve

Optimisation at 380GeV

Many thanks to the rebaselining team that provided the models that are integrated in the code

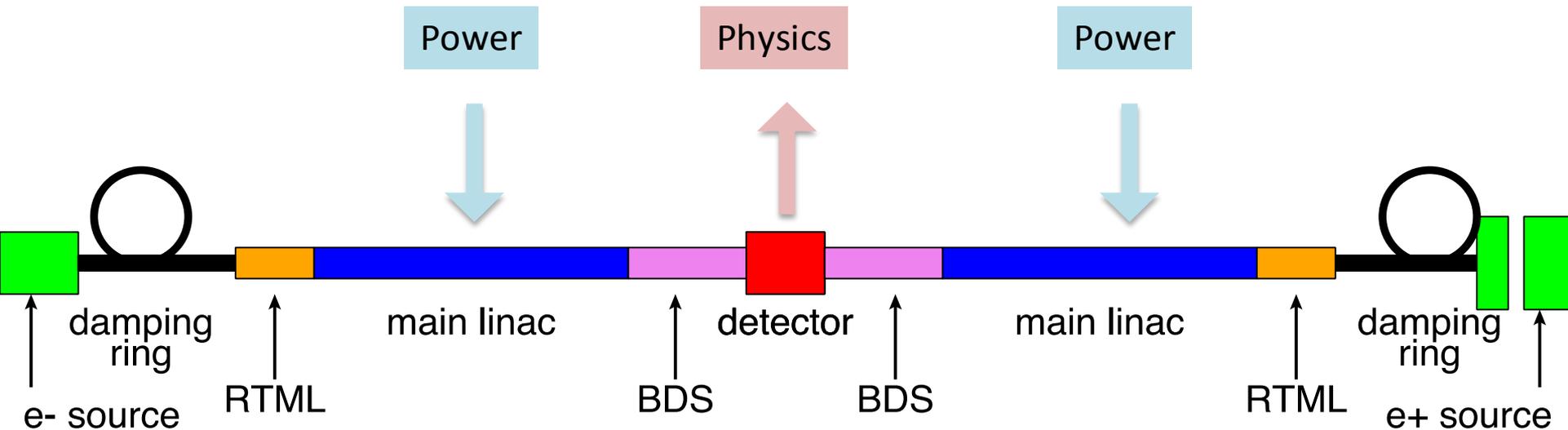
Luminosity goal significantly impact minimum cost
For $L=1 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$ to $L=2 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$:

Costs 0.5 a.u.
And O(100MW)



Cheapest machine is close to lowest power consumption => small potential for trade-off

Generic Linear Collider



Can reach high electron-positron centre-of-mass energies

- almost no synchrotron radiation

Single pass, hence two main challenges

- gradient
- luminosity

Note: Luminosity Enhancement

Parameter	Symbol [unit]	ILC	CLIC	CLIC
Centre of mass energy	E_{cm} [GeV]	500	380	3000
Total luminosity	L [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	1.8	1.5	6
Luminosity in peak	$L_{0.01}$ [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	1	0.9	2
Particles per bunch	N [10^9]	20	5.2	3.72
Bunch length	σ_z [μm]	300	70	44
Collision beam size	$\sigma_{x,y}$ [nm/nm]	474/5.9	149/2.9	40/1
Vertical emittance	$\epsilon_{x,y}$ [nm]	35	40	20
Geometric luminosity	L_{geom} [$10^{34}\text{cm}^{-2}\text{s}^{-1}$]	0.75	0.8	4.3
Enhancement factor	H_D	2.4	1.9	1.5

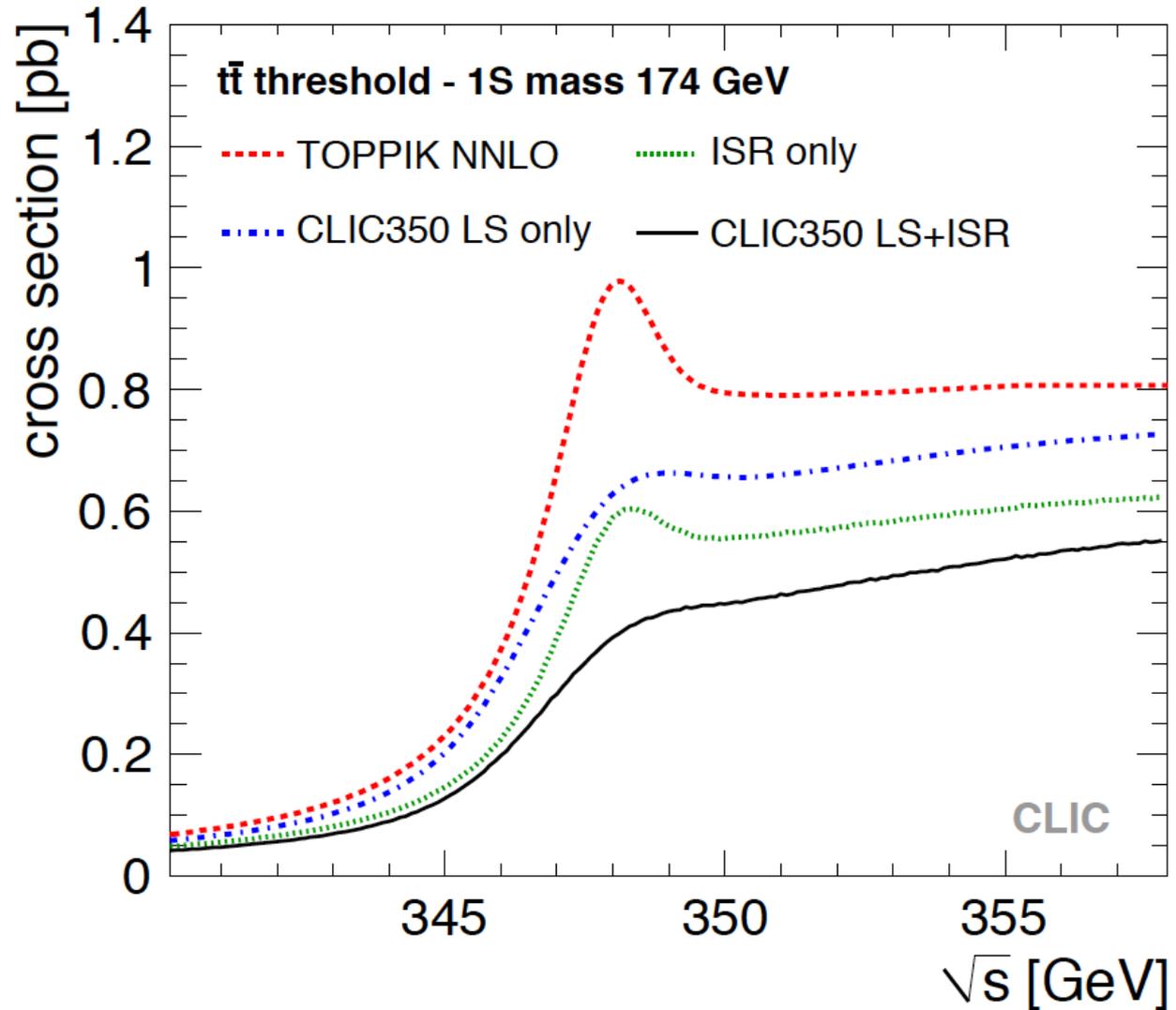
Top Production at Threshold

K. Seidel et al. arXiv:1303.3758

Top production at threshold is strongly affected by beam energy spread and beamstrahlung

For $L_{0.01} > 0.6 L$ impact of beamstrahlung is comparable to ISR

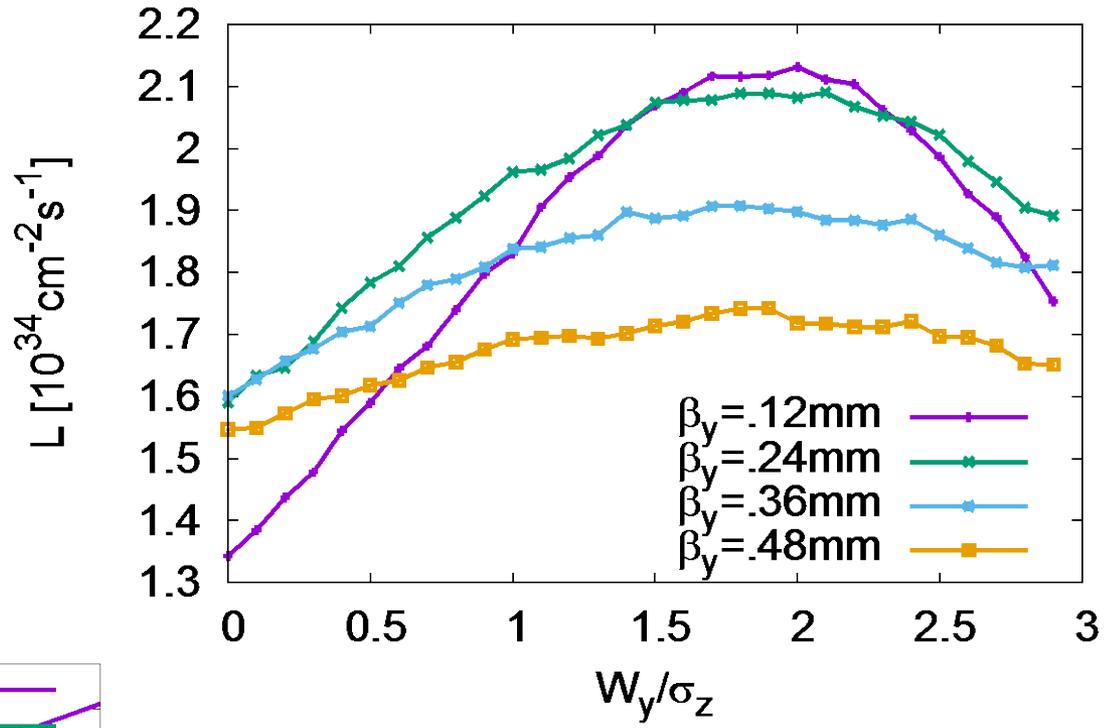
But depends on physics



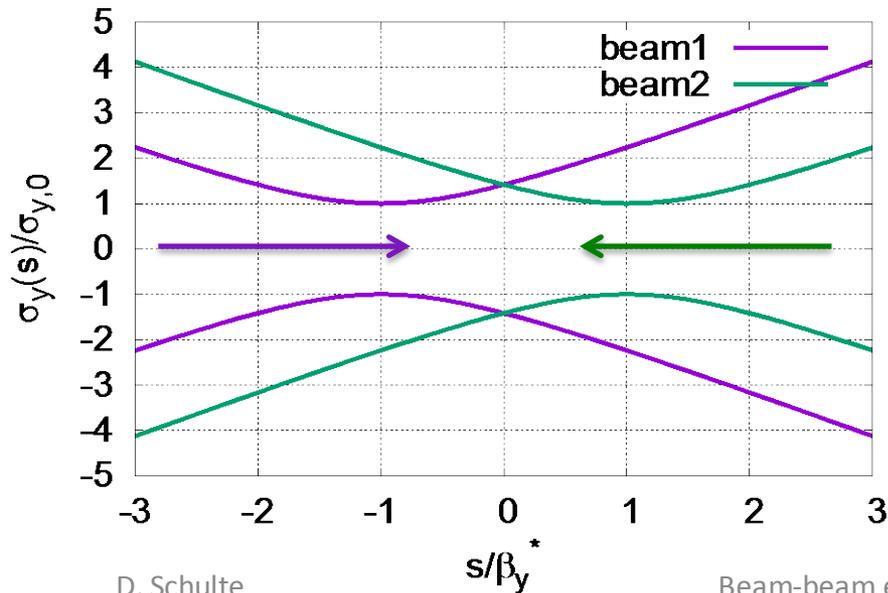
Note: Travelling Focus

Travelling focus (Balakin):
 We focus each slice of the beam
 on one point of the oncoming
 beam, e.g. $2\sigma_z$ before the
 centre

The beam-beam forces keep
 the beam small

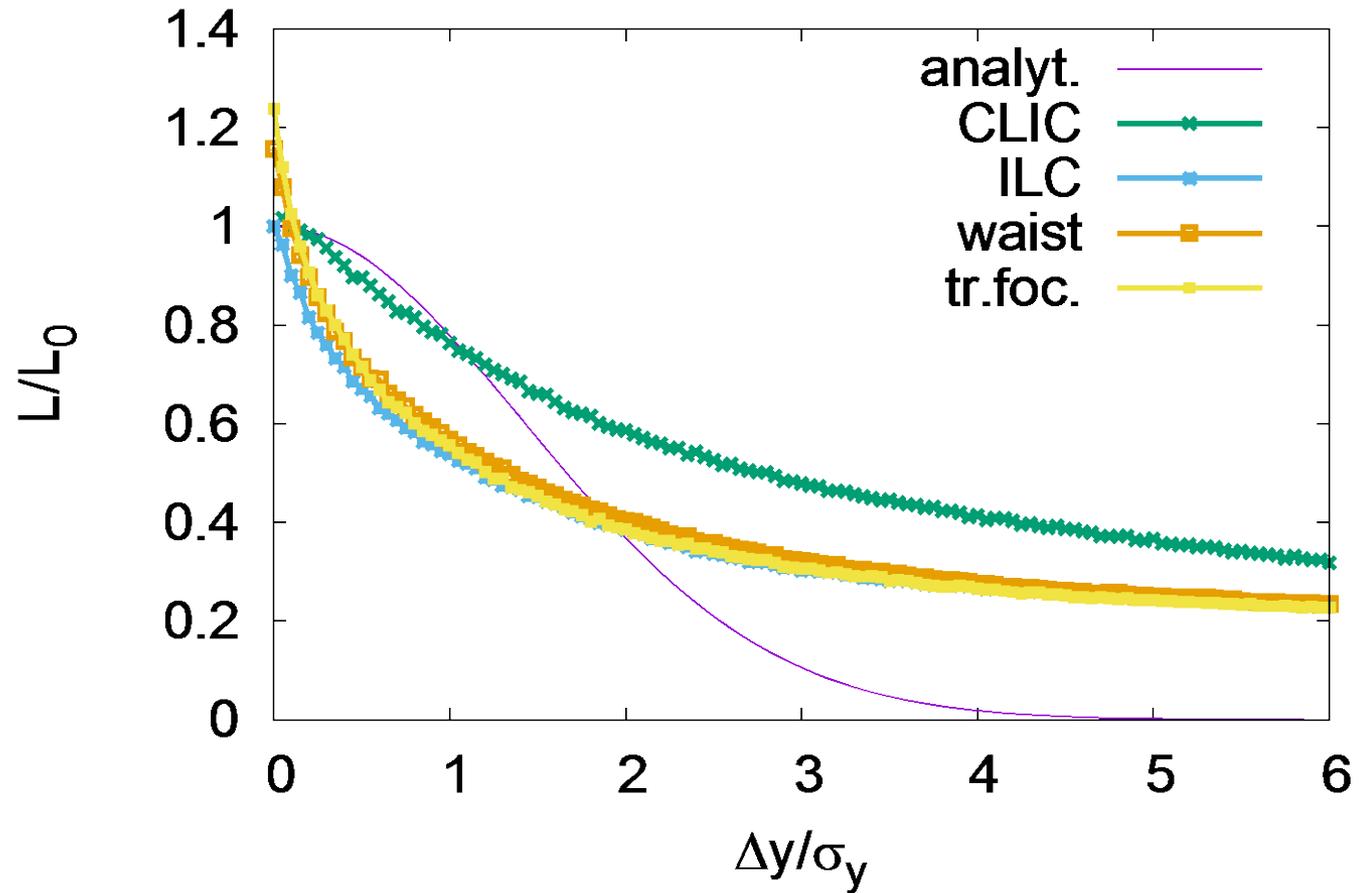


Additional gain of 10% in
 luminosity



Note: ILC with $\beta_y=0.24\text{mm}$

Even stronger offset
dependence for smaller
beta-function



So in practice less gain
than expected