

# TRANSFER LINES - TOOLS

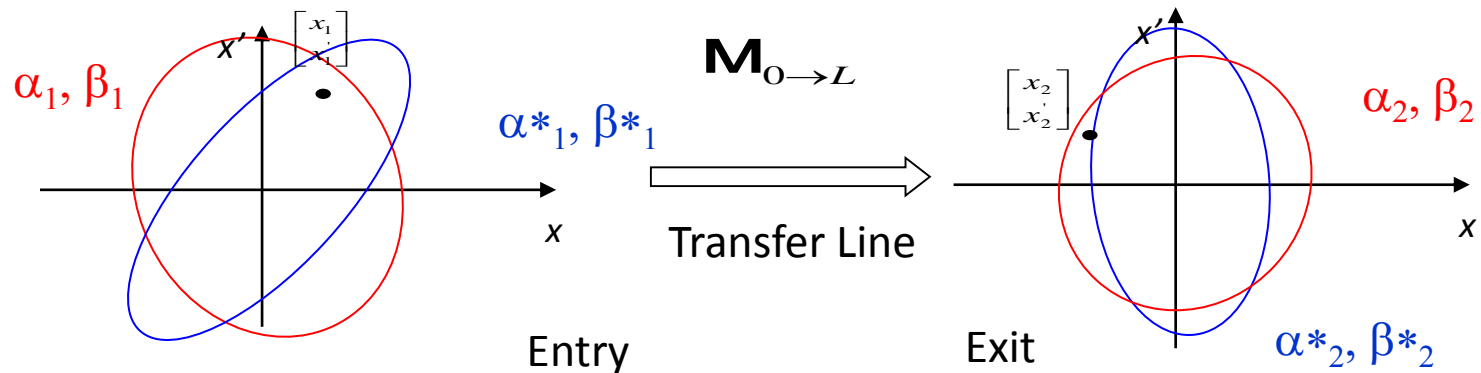
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Wolfgang Bartmann

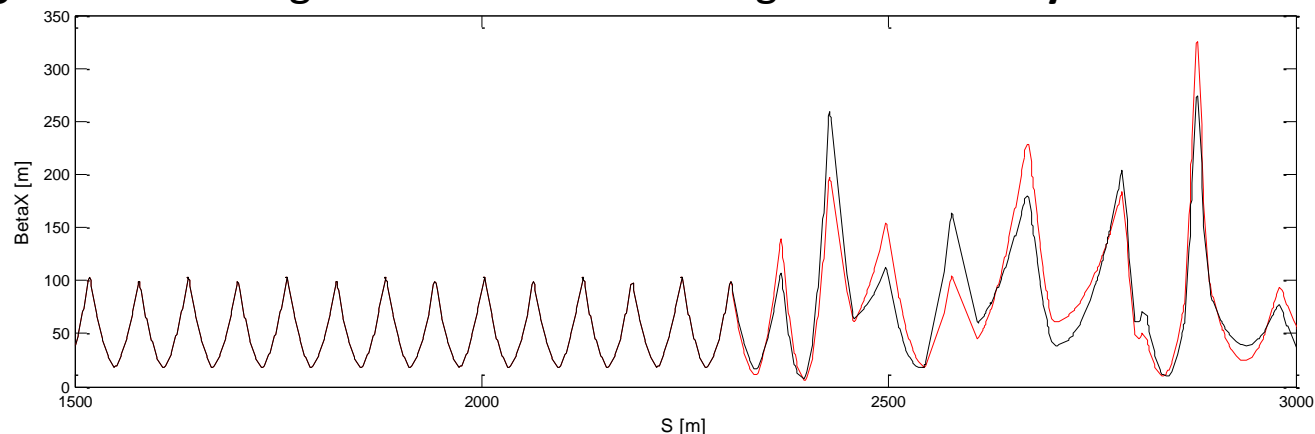
CAS, Erice, March 2017

# Wrap up

- Optics in a ring is defined by ring elements and **periodicity** – optics in a transfer line is dependent line elements and **initial conditions**



- Changes** of the strength of a transfer line magnet **affect only downstream optics**



## Wrap up

- Geometry calculations require a set of coordinates in a common reference frame
- **Bending fields** are defined by geometry and the **magnetic or electric rigidity**:

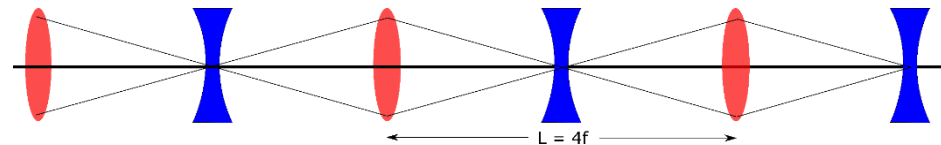
$$B\rho [Tm] = 3.3356 \frac{A}{n} p [GeV/c] \quad E\rho [kV] = \frac{\gamma+1}{\gamma} \frac{A}{n} T [keV]$$

$$\theta = \frac{Bdl}{B\rho} \text{ or } \frac{Edl}{E\rho}$$

- The choice between magnetic and electric depends mainly on the beam energy
- If you are in the grey zone, consider: field design and measurement, power consumption, vacuum, interlocking
- For the estimates of bending radii in lines remember to take into account the filling factor (~70%) and Lorentz-Stripping in case of H<sup>-</sup> ions

# Wrap up

- **Quadrupole gradients and apertures** can be estimated in case of simple focussing structure like FODO cells

$$\frac{L}{f} = 4 \sin \frac{\mu}{2} \quad \leftarrow \quad \text{Stability} \quad f > \frac{L}{4} \quad \rightarrow$$


The diagram illustrates a FODO cell, a common structure in particle accelerators. It consists of a sequence of optical elements: a red focusing lens, a blue defocusing lens, a red focusing lens, a blue defocusing lens, and a red focusing lens. The distance between the two central blue defocusing lenses is labeled as  $L = 4f$ , where  $f$  is the focal length of the lenses.

$$\beta = \left( L + \frac{L^2}{4f} \right) / \sin \mu \quad \rightarrow \quad \text{Defines beam size and quadrupole pole tip field}$$

- **Aperture specifications** require safety factors for the optics and constant contributions for trajectory variations and alignment errors

$$\bullet A_{x,y} = \pm n_{sig} \cdot \sqrt{k_{\beta} \cdot \beta_{x,y} \cdot \frac{\epsilon_{x,y}}{\beta_{\gamma}}} \pm D_{x,y} \cdot k_{\beta} \cdot \frac{\Delta p}{p} \pm CO \cdot \sqrt{\frac{\beta_{x,y}}{\beta_{xmax,ymax}}} \pm \text{alignment}$$

# Wrap up

- **Estimating tolerances** from emittance growth:

- Dipole field and alignment:  
$$\epsilon_2 = \epsilon_1 + \frac{1}{2} \left( (\Delta y)^2 \frac{1+\alpha^2}{\beta} + (\Delta y')^2 \beta \right)$$

The diagram illustrates the components of the emittance growth equation. A box labeled "Magnet misalignment" has an arrow pointing to the  $(\Delta y)^2$  term in the equation. Another box labeled "Dipole field error" has an arrow pointing to the  $(\Delta y')^2$  term. Below the "Dipole field error" box is a smaller box containing the equation  $\Delta y' = \frac{\Delta B l}{B \rho}$ .

- Gradient errors:


$$\epsilon_2 = \frac{1}{2} (k^2 \beta^2 + 2) \epsilon_1 \quad k = -\frac{\Delta G l}{B \rho}$$

# Outline

- Introduction
  - What is a transfer line?
- Paper studies
  - Geometry – estimate of bend angles
  - Optics – estimate of quadrupole gradients and apertures
  - Error estimates and tolerances on fields
- Examples of using MADX for
  - Optics and survey matching
  - Final focus matching
  - Achromats
  - Error and correction studies
- Special cases in transfer lines
  - Particle tracking
  - Plane exchange
  - Tilt on a slope
  - Dilution
  - Stray fields



1<sup>st</sup> hour



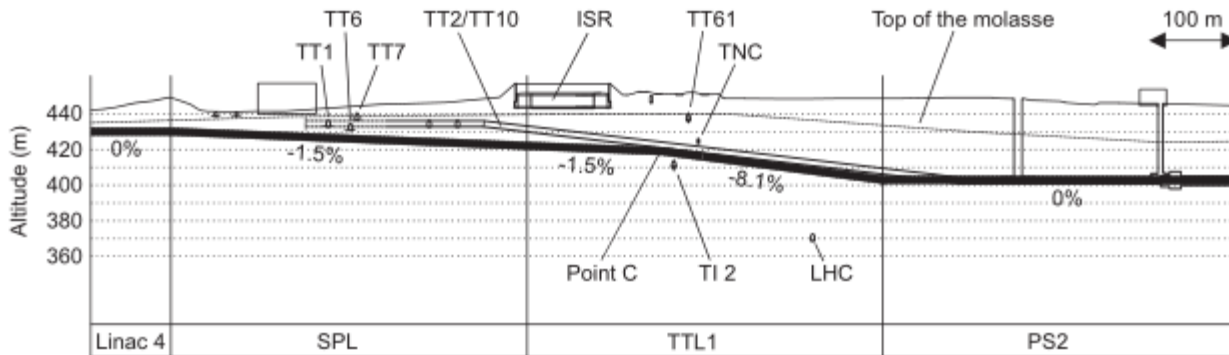
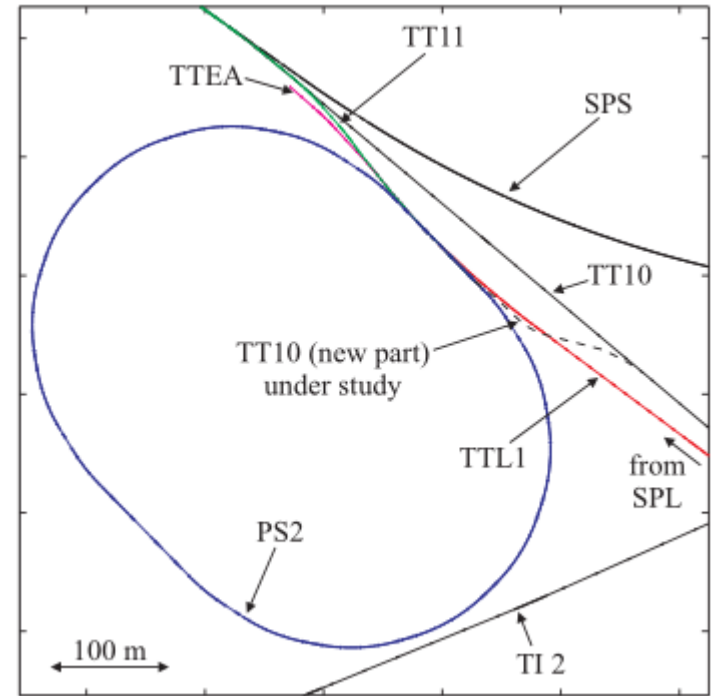
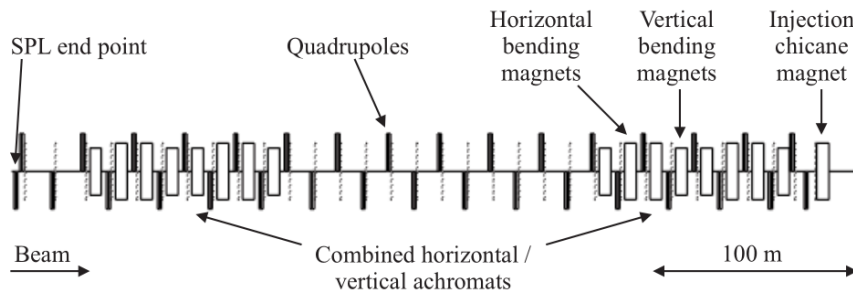
2<sup>nd</sup> hour



3<sup>rd</sup> hour

# MADX example – Optics and survey matching

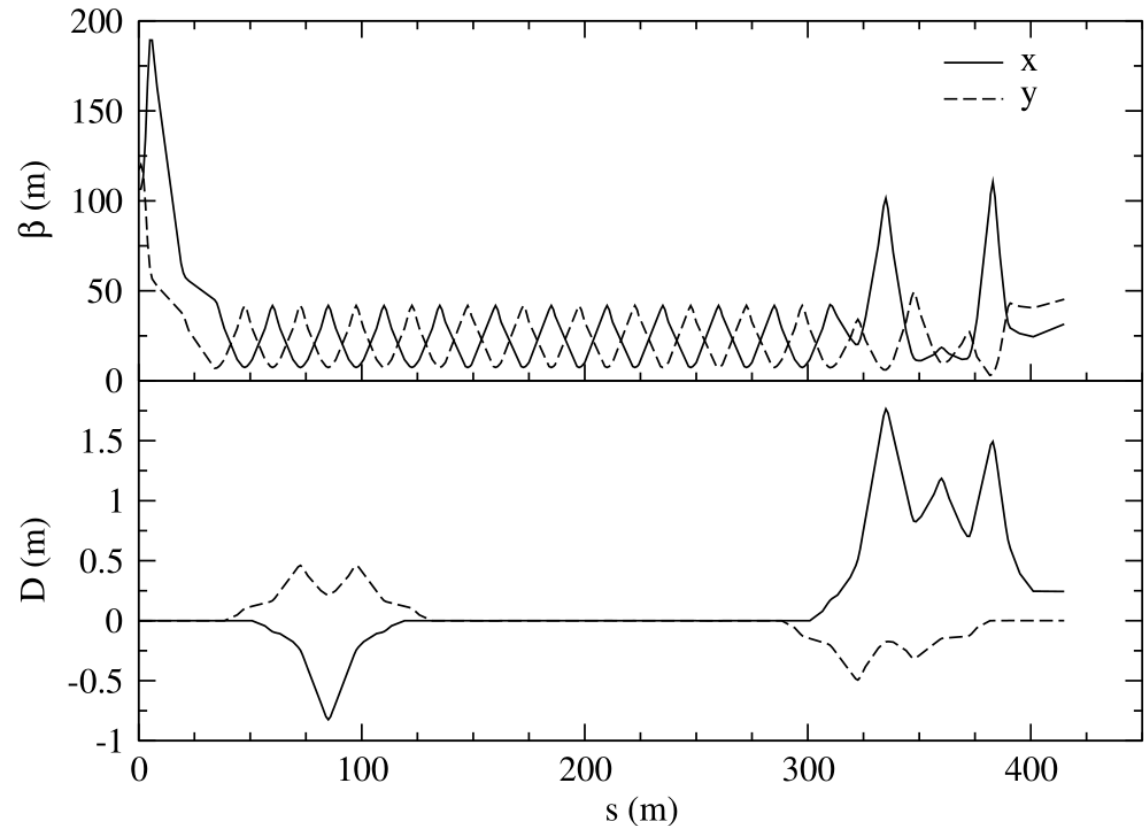
# SPL to PS2 transfer line





# SPL to PS2 optics

- Periodic FODO structure in the main part of the line
- Matching section from SPL to FODO and from FODO to PS2 injection
- Horizontal and vertical achromats in the 90 deg FODO – where they come for free
- Why do we provide dispersion at injection?



```

TITLE, 'TTL1';
// read in sequence file
OPTION, -ECHO, WARN, -INFO;
CALL, FILE = "ttl1-v1.0.0.seq";
// read in beam properties
call, file = "beam.madx";

//----- Survey matching to PS2 -----
USE, SEQUENCE = TTL1;
// read in survey coordinates at the injection point (stripping foil)
// in the PS2 (real beam direction)
call, file = 'out.ps2foil-v8.0.4.survey.ini.mad';
value, ps2.omk.foil.x0,
      ps2.omk.foil.y0,
      ps2.omk.foil.z0,
      ps2.omk.foil.theta0,
      ps2.omk.foil.phi0,
      ps2.omk.foil.psi0;

// define macro for position matching routine:
m1: MACRO={USE, SEQUENCE = TTL1;
          SURVEY, x0 = -1510.09247,
                 y0 = 2423.58630,
                 z0 = 2278.25946,
                 theta0 = 0.8715909,
                 phi0 = -0.0150853,
                 psi0 = 0.0;};

// match position and angles at injection point (stripping foil):
MATCH, USE_MACRO;

//VARY, name = MB.v1.angle, STEP = 0.001, LOWER = 0.01, UPPER = 0.03;
VARY, name = MB.h1.angle, STEP = 0.001, LOWER = -0.06, UPPER = -0.01;
VARY, name = MB.h2.angle, STEP = 0.001, LOWER = 0.01, UPPER = 0.06;
//VARY, name = MB.v2.angle, STEP = 0.001, LOWER = -0.033, UPPER = -0.01;
VARY, name = ps2.omk.foil.at, STEP = 0.001, LOWER = 400, UPPER = 425;

USE_MACRO, name= m1;

CONSTRAINT, expr= table(survey,ps2.omk.foil,x) = ps2.omk.foil.x0;
//CONSTRAINT, expr= table(survey,ps2.omk.foil,y)=ps2.omk.foil.y0;
CONSTRAINT, expr= table(survey,ps2.omk.foil,z)=ps2.omk.foil.z0;
CONSTRAINT, expr= table(survey,ps2.omk.foil,theta)=ps2.omk.foil.theta0;
//CONSTRAINT, expr= table(survey,ps2.omk.foil,phi)=ps2.omk.foil.phi0;
//CONSTRAINT, expr= table(survey,ps2.omk.foil,psi)=ps2.omk.foil.psi0;

LMDIF, CALLS:=5000, TOLERANCE:=1.E-10;
//JACOBIAN, CALLS= 500, TOLERANCE= 1.0E-21;
ENDMATCH;

```

## Survey

- Call sequence and define BEAM command
- Get the survey coordinates x,y,z, theta, phi, psi of the stripping foil
- Define macro for matching routine

When matching the geometry of the line, the path length is changing → the position of the foil in the sequence has to be matched simultaneously

# FODO

```
// FODO cell properties
l.fodo      = 25;
phadv      = pi/2.0;// 90deg phase advance per cell
k1.theo    = 4.0 / (l.mq * l.fodo) * sin(phadv/2.0);
value, l.fodo, phadv, k1.theo;

kqif.cell = k1.theo;// 5.98643e-02
kqid.cell = -k1.theo;// -5.98462e-02

//----- Prototype Cell -----

FCELL: SEQUENCE,      L = l.fodo;

MQF.b:MQH,  AT := l.MQ/4,           K1 := kqif.cell;
MQD.a:MQH,  AT := l.fodo*0.5-l.MQ/4, K1 := kqid.cell;
MQD.b:MQH,  AT := l.fodo*0.5+l.MQ/4, K1 := kqid.cell;
MQF.a:MQH,  AT := l.fodo-l.MQ/4,    K1 := kqif.cell;

ENDSEQUENCE;

USE,      SEQUENCE = FCELL;
MATCH,   SEQUENCE = FCELL;
  VARY,   NAME = kqif.cell, STEP = 0.001,  LOWER = 0.0, UPPER = mq.k1.max;
  VARY,   NAME = kqid.cell, STEP = 0.001,  LOWER = -mq.k1.max, UPPER = 0.0;
  CONSTRAINT, RANGE = #E, MUX = phadv/(2*pi), MUY = phadv/(2*pi);
IMDIF, CALLS:=50, TOLERANCE:=1.E-10;
ENDMATCH;

SELECT, FLAG=TWISS, COLUMN=NAME,S,BETX,BETY,ALFX,ALFY,DX,DPX,DY,DPY;
TWISS, FILE = "fodo.twiss";
```

$$\frac{L}{f} = 4 \sin \frac{\mu}{2}$$

# Matching sections

```
//----- Match TTL1 to SPL -----
USE, SEQUENCE = TTL1;
MATCH, SEQUENCE = TTL1, VLENGTH = TRUE,
      BETX = BETX0, ALFX = ALFX0,
      DX = DX0, DPX = DPX0,
      BETY = BETY0, ALFY = ALFY0,
      DY = DY0, DPY = DPY0;
VARY, NAME = kqid.0, STEP = 0.001, LOWER = -0.1, UPPER = 0.0;
VARY, NAME = kqif.1, STEP = 0.001, LOWER = 0.0, UPPER = 0.1;
VARY, NAME = kqid.1, STEP = 0.001, LOWER = -0.1, UPPER = 0.0;
VARY, NAME = kqif.2, STEP = 0.001, LOWER = 0.0, UPPER = 0.1;
CONSTRAINT, RANGE = MQF.4, BETX = MQF.betx, BETY = MQF.bety;
CONSTRAINT, RANGE = MQF.4, ALFX = MQF.alfx, ALFY = MQF.alfy;
LMDIF, CALLS:=5000, TOLERANCE:=1.E-10;
ENDMATCH;
```

SPL to FODO  
matching

```
//----- Match TTL1 to PS2 -----
USE, SEQUENCE = TTL1;
MATCH, SEQUENCE = TTL1, VLENGTH = TRUE,
      BETX = BETX0, ALFX = ALFX0,
      DX = DX0, DPX = DPX0,
      BETY = BETY0, ALFY = ALFY0,
      DY = DY0, DPY = DPY0;
VARY, NAME = kqif.13, STEP = 0.001, LOWER = 0.04, UPPER = 0.1;
VARY, NAME = kqid.13, STEP = 0.001, LOWER = -0.1, UPPER = 0.0;
VARY, NAME = kqif.14, STEP = 0.001, LOWER = 0.04, UPPER = 0.071;
VARY, NAME = kqid.14, STEP = 0.001, LOWER = -0.1, UPPER = 0.0;
VARY, NAME = kqif.15, STEP = 0.001, LOWER = 0.04, UPPER = 0.07;
VARY, NAME = kqid.15, STEP = 0.001, LOWER = -0.1, UPPER = 0.0;
VARY, NAME = kqif.16, STEP = 0.001, LOWER = 0.0, UPPER = 0.1;
VARY, NAME = kqid.16, STEP = 0.001, LOWER = -0.1, UPPER = 0.0;
CONSTRAINT, RANGE = ps2.omk.foil, BETX=BETX1, BETY=BETY1;
CONSTRAINT, RANGE = ps2.omk.foil, ALFX=ALFX1, ALFY=ALFY1;
CONSTRAINT, RANGE = ps2.omk.foil, DX=DX1, DPX=DPX1;
CONSTRAINT, RANGE = ps2.omk.foil, DY=DY1, DPY=DPY1;
LMDIF, CALLS:=5000, TOLERANCE:=1.E-10;
ENDMATCH;
```

FODO to PS2  
matching

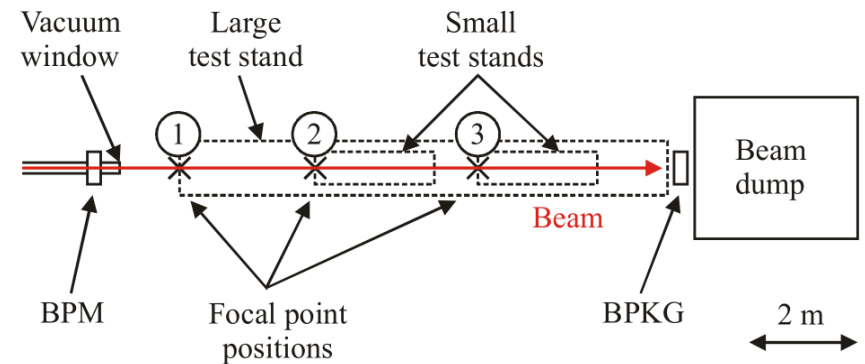
- Matching itself rather straightforward as long as you have enough knobs - independently powered quadrupoles
- Start generous to find optimum solution for optics
- Then minimize number of independent quadrupoles for economy – maybe even at the expense of non-perfect optics
- Tunability!

- Not so straightforward to get the optics constraints right
- Make a clear handover point – better something mechanical than magnetic
- Calculation of optics at handover point
  - Take into account kicker – will alter dispersion
  - Switch on injection bump

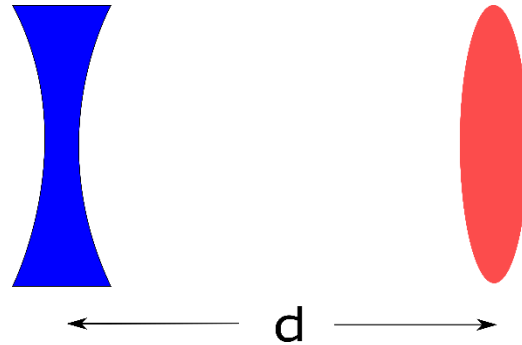
Example – Final focus matching

# HiRadMat

- Material test facility at the SPS
- 440 GeV
- $5 \times 10^{13}$  protons per shot
- Adjustable focal point
- Beam size 0.1 – 2 mm



# Doublet



$$\begin{pmatrix} 1 & 0 \\ -1/f_2 & 1 \end{pmatrix} \begin{pmatrix} 1 & d \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 \\ 1/f_1 & 1 \end{pmatrix} = \begin{pmatrix} 1 + d/f_1 & d \\ 1/f_1 - 1/f_2 - d/f_1 f_2 & 1 - d/f_2 \end{pmatrix}$$

For equal quadrupole strength:

$$R = \begin{pmatrix} 1 + d/f & d \\ -d/f^2 & 1 - d/f \end{pmatrix}$$

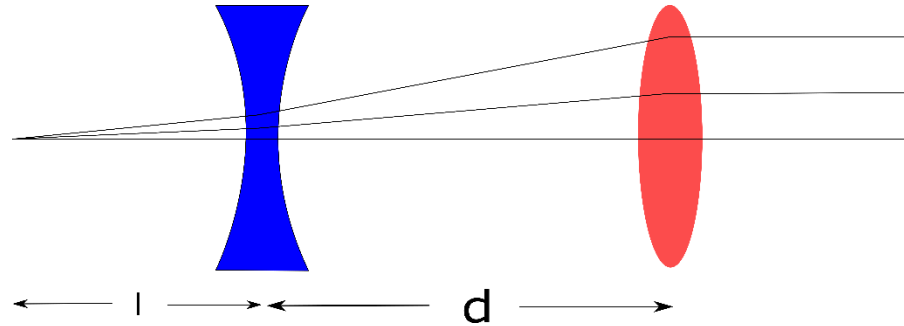


$$f^* = \frac{f^2}{d}$$

Effective focal length

# Point to parallel focusing

- Drift of length  $l$  preceding the doublet



- $R_{22}$  and  $R_{44}$  need to be zero which gives

$$f_1 f_2 = ld \quad \frac{f_1}{f_2} = \frac{l}{l+d}$$

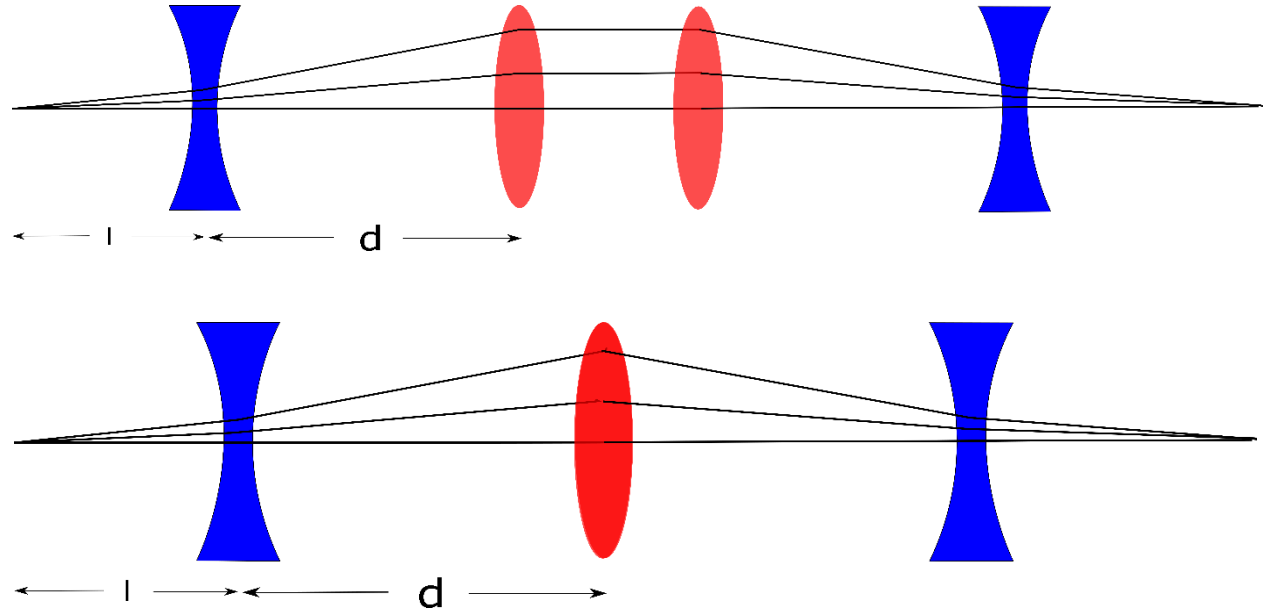
- And for the magnetic fields:

$$f_1 = l \sqrt{\frac{d}{l+d}} \quad f_2 = \sqrt{d(l+d)}$$



# Symmetric point to point focusing - Triplet

- Use two doublets to focus point to point
- Also works with one doublet, but asymmetric in x/y
- Triplet – symmetric in x/y  
→ can create round beam spots at target

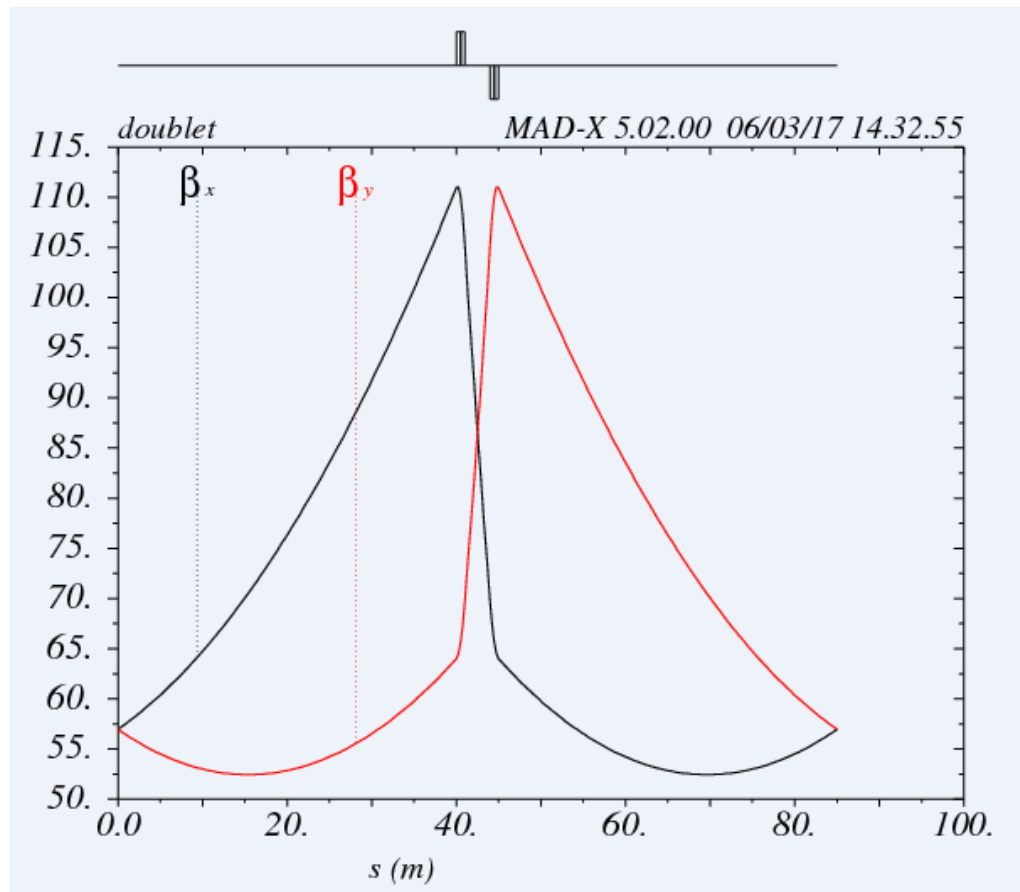


$$R = \begin{pmatrix} 1 - 2\frac{d^2}{f^2} & 2d \left(1 - \frac{d}{f}\right) \\ -2\frac{d}{f^2} \left(1 + \frac{d}{f}\right) & 1 - 2\frac{d^2}{f^2} \end{pmatrix} \quad f^* = \frac{f^2}{2d} \left(1 + \frac{d}{f}\right)$$

Transfer matrix and effective focal length of triplet structure

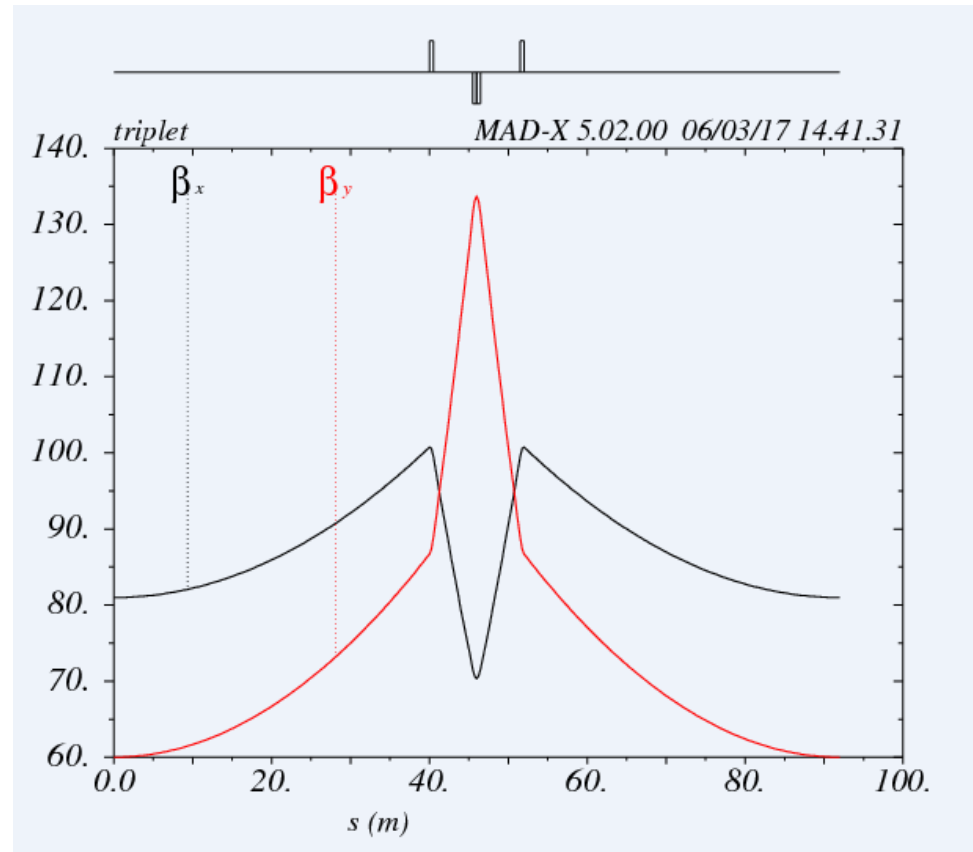
# Doublet optics

- Compared to FODO, the doublet provides longer drift spaces for special equipment
- Steep asymmetric slopes in betatron functions

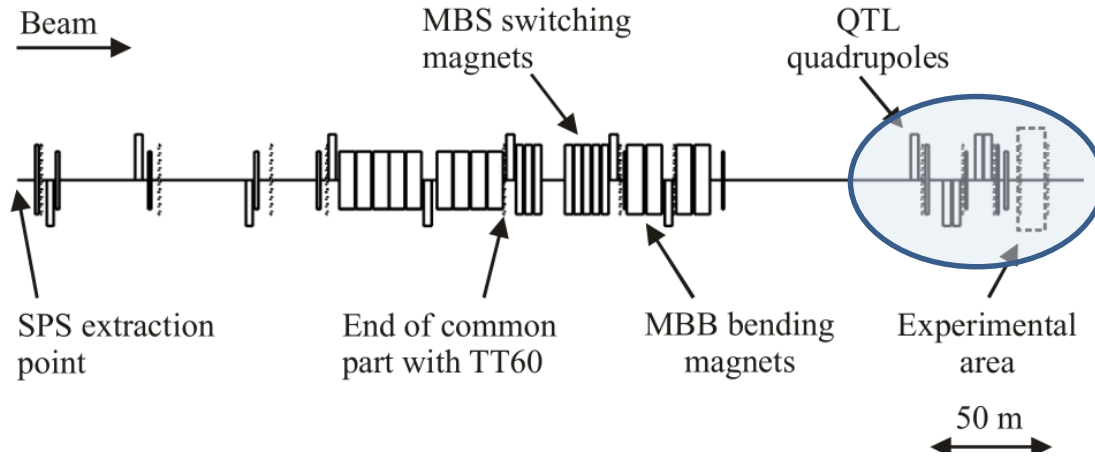


# Triplet optics

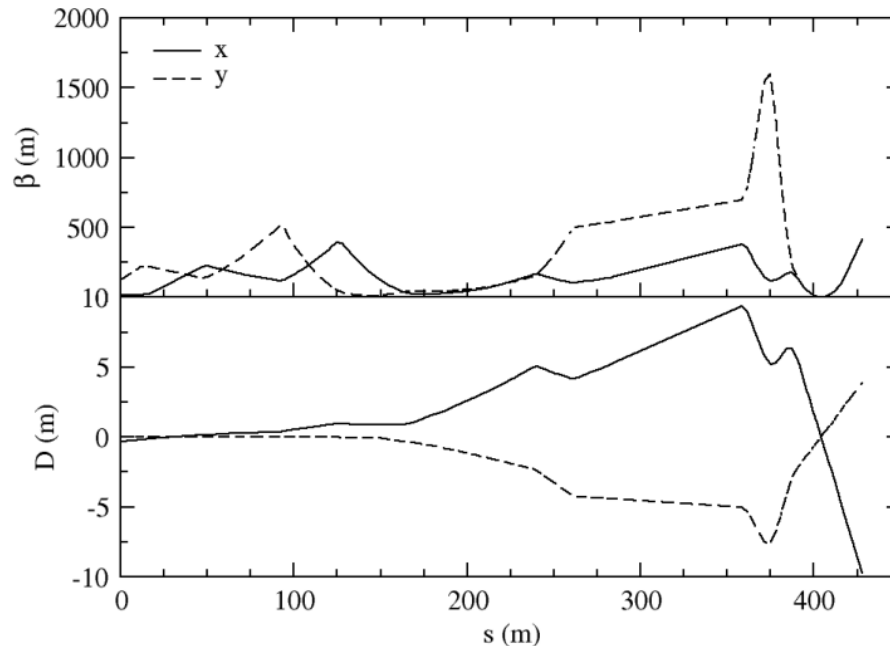
- Triplets have distinct locations of high betatron functions but then allow to focus them down over long distances
- $\mu = \int \frac{ds}{\beta}$  – large phase advance for closing dispersion bumps
- Low betas for economic dipole production



# HiRadMat



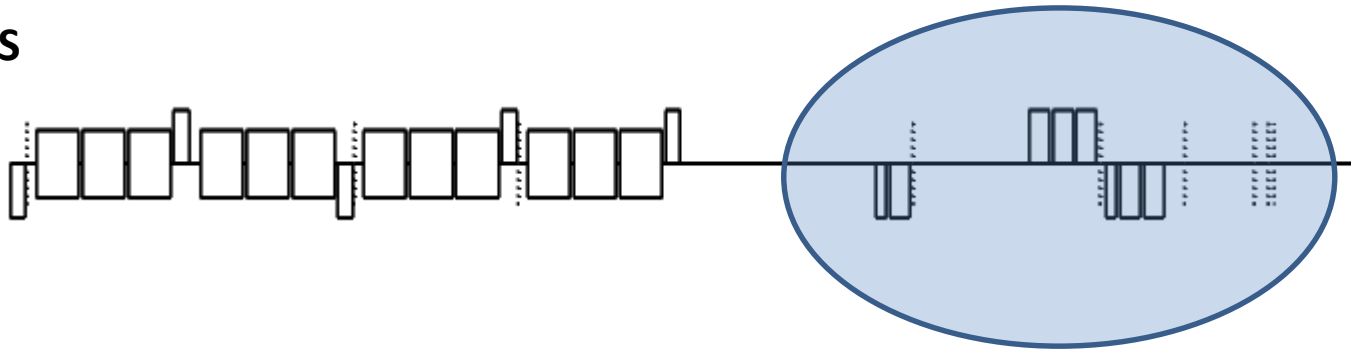
Triplet structure as final focus of HiRadMat to control both planes and different focal length



In this case focus down to minimum beam size in both planes – large peak of betatron function upstream

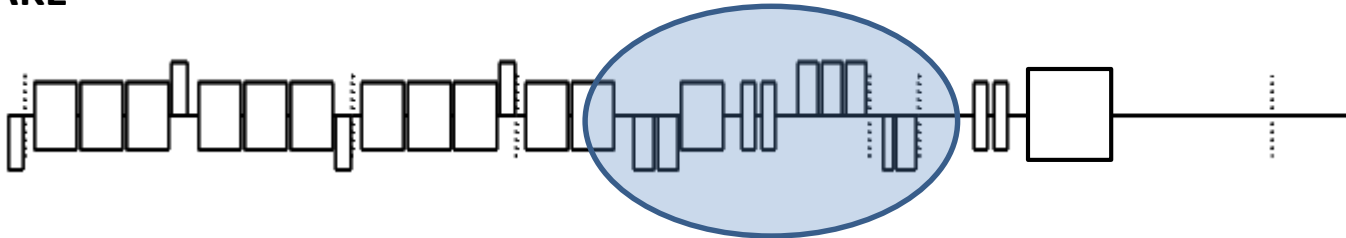
# CNGS and AWAKE

**CNGS**

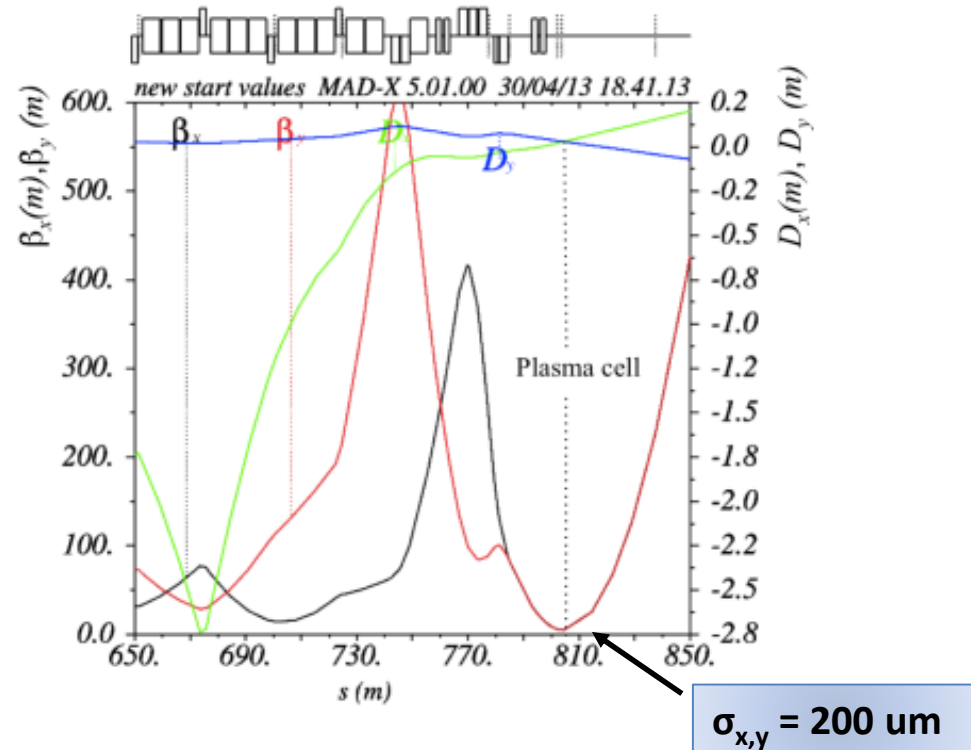
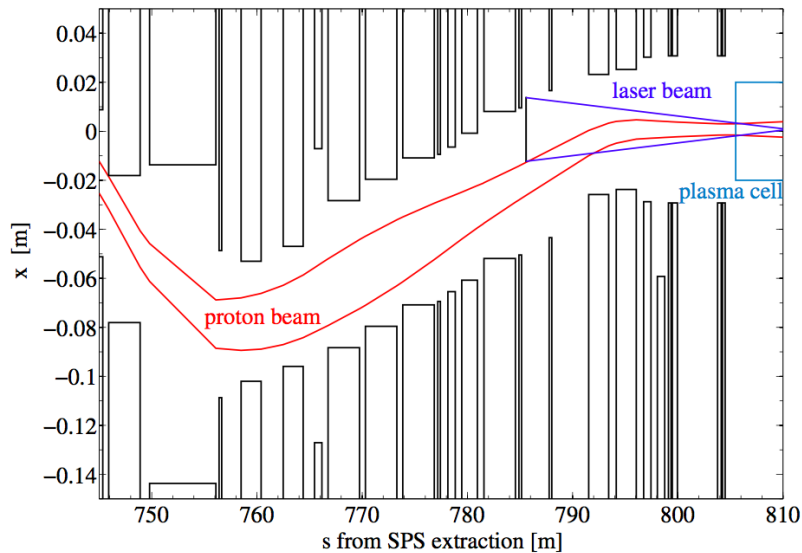


Final focus structure

**AWAKE**

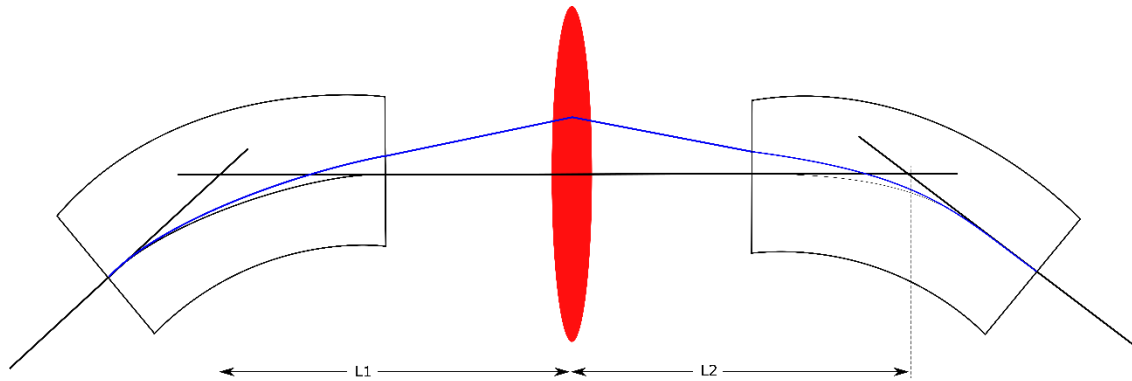


# AWAKE final focus



- Displace existing magnets of final focusing to fulfill optics requirements at the entrance of the plasma cell
- Move existing dipole + 4 additional dipoles to create a chicane for laser mirror integration

# Achromat



$$R_{bend} = \begin{pmatrix} 1 & 0 & 0 \\ -hs & 1 & s \\ 0 & 0 & 1 \end{pmatrix}$$

$$h = \frac{B}{B\rho}$$

$$s = \sin \alpha$$

$$M = \begin{pmatrix} 1 & 0 & 0 \\ -hs_2 & 1 & s_2 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & L_2 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ -1/f & 1 & s_2 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & L_1 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ -hs_1 & 1 & s_1 \\ 0 & 0 & 1 \end{pmatrix}$$

# Achromat

- Multiply the matrix and determine the expressions for Dispersion and its derivative:

$$D_x = L_2 s_1 \left( 1 - \frac{L_1}{f} \right) + L_1 s_1$$

$$D'_x = L_1 s_1 \left( -h s_2 - \frac{1}{f} + \frac{h s_2 L_2}{f} \right) + s_1 (1 - h s_2 L_2) + s_2$$

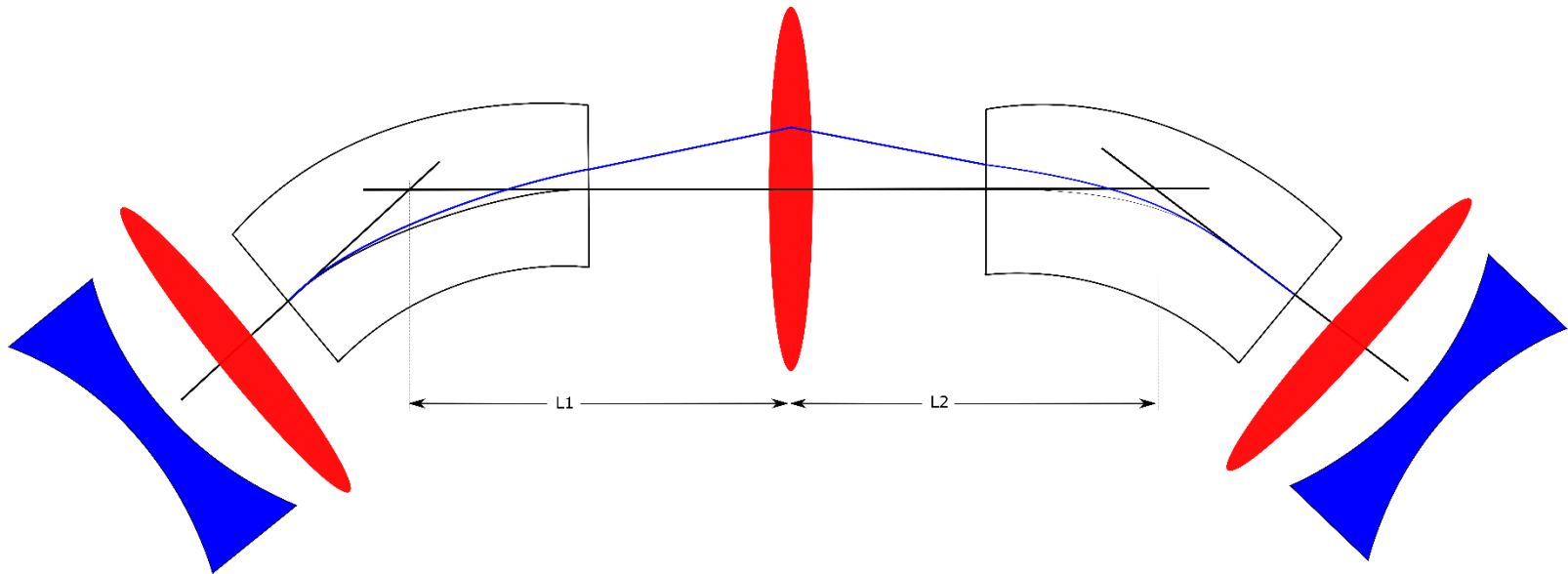
- For an achromat, both must vanish which defines the strengths and lengths parameters in our system:

$$\frac{1}{f} = \frac{1}{L_1} + \frac{1}{L_2}$$

$$L_1 s_1 = L_2 s_2$$

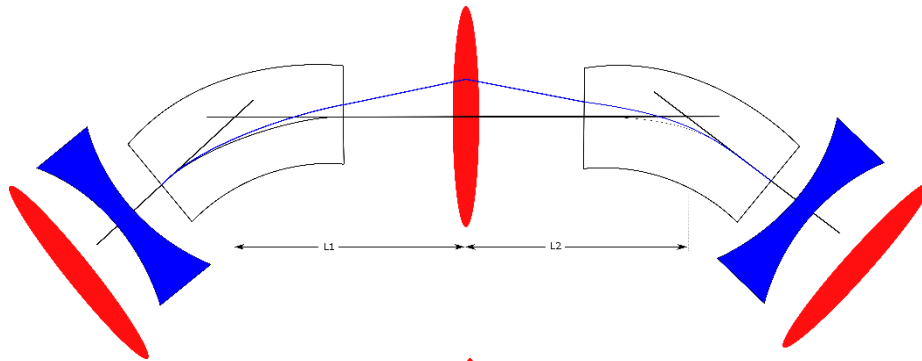


# Achromat with point to point focusing

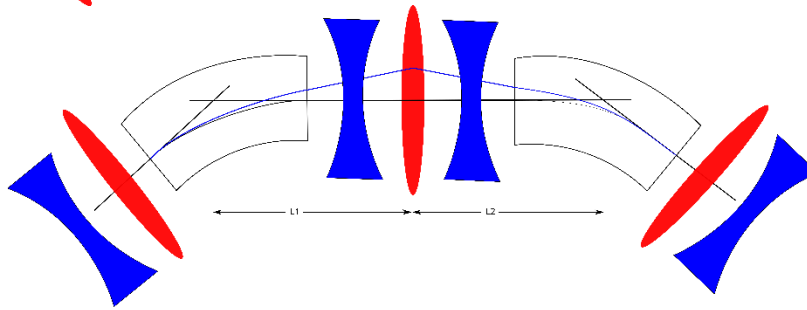


- Central quadrupole is focusing the dispersion down to zero at the outer ends of the bends and contributes little to the overall focusing
- Quadrupoles outside the achromat do not affect the dispersion behaviour; they solely provide focusing in both planes
- Target at the centre can be used as spectrometer

# Achromat examples from high brightness machines

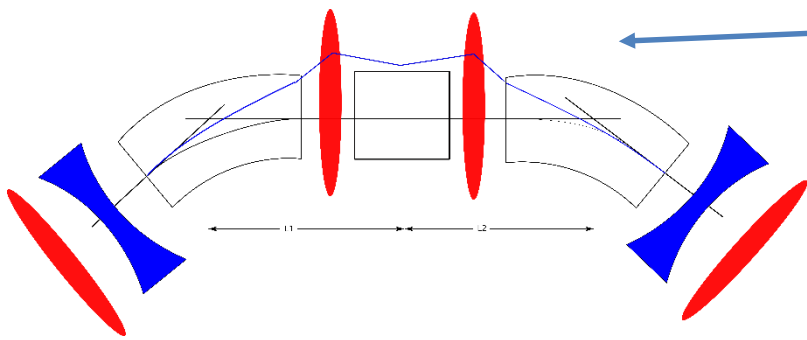


Double bend achromat –  
Chasman-Green



Expanded DBA version

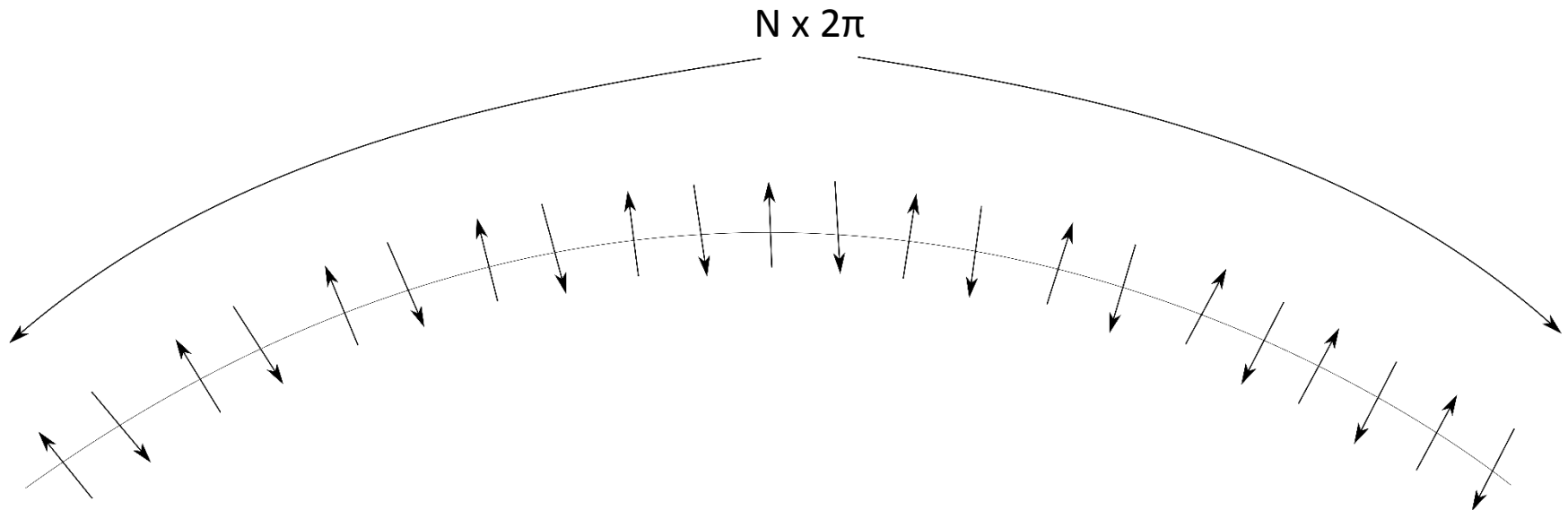
Strong focussing in  
dispersive area – consider  
installing sextupoles for  
chromaticity correction



Triple bend achromat

# Resonant dispersion condition in arcs

- More relevant for rings
- Resonant condition for dispersion cancellation in an arc



[8] Senichev Yuriy. A "resonant" lattice for a synchrotron with a low or negative momentum compaction factor. 1997.

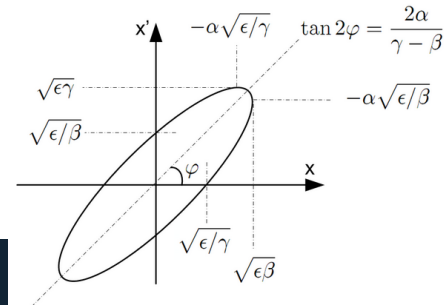
# MADX example – Error and correction studies

# Error studies

- Define acceptable error levels of your line
  - Loss level – W/m, % beam, activation level...
  - Trajectory offset in position and angle at point of delivery
  - Shot-to-shot variation of trajectory
  - Long term variation of trajectory
  - Optics mismatch at point of delivery
  - Rotation, energy mismatch
- Assume reasonable errors for the hardware and study their impact
- Iterate input until error level is acceptable and specify hardware accordingly

# MADX example - Error studies

- Input error from preceding machine
- According to optics at handover



```
corrmacro(nx): macro={
//use, sequence=btbtp4;
use, sequence=bt1btp;
sigma:=2;
vert:=TGAUSS(2);

EOPTION, SEED=nx, ADD=false;

eps_x=2e-6/2.9676;
//delta_p=1.07e-3;
delta_p=0;

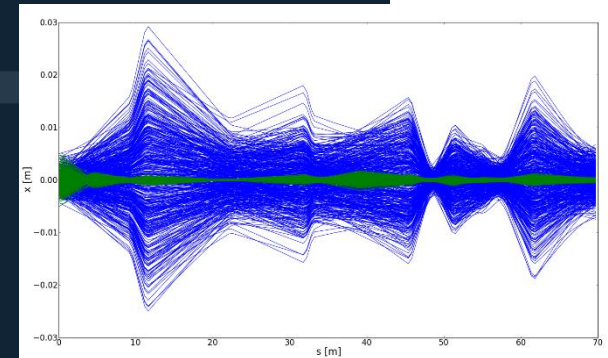
rand_x=gauss(nx);
sigma_x = sqrt(eps_x * betx0);
x0 = 0.015*rand_x * (sigma_x + (abs(dx0) * delta_p));

rand_px=gauss(nx);
px0 = 0.015*rand_px * ((sqrt(eps_x / betx0) - (alfx0 / betx0) * sigma_x) + (dpx0 * delta_p));

eps_y=2e-6/2.9676;
//delta_p=1.07e-3;

rand_y=gauss(nx);
sigma_y = sqrt(eps_y * bety0);
y0 = 0.01*rand_y * (sigma_y + (abs(dy0) * delta_p));

rand_py=gauss(nx);
py0 = 0.01*rand_py * ((sqrt(eps_y / bety0) - (alfy0 / bety0) * sigma_y) + (dpy0 * delta_p));
```



# Error assignment

```
EOPTION,ADD= FALSE, SEED:=nx;  
SELECT, flag= error, clear;  
  
SELECT, FLAG= ERROR, PATTERN= "BT.BHZ10";  
EFCOMP, ORDER:= 0, Radius:=0.01  
DKNR:={5e-4*TGAUSS(sigma),0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0},  
DKSR:={0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0,0};  
EALIGN, DS:= 0.3e-3*TGAUSS(sigma), DX:= 0.3e-3*TGAUSS(sigma), DY:= 0.3e-3*TGAUSS(sigma),  
DPHI:= 0.3e-3*TGAUSS(sigma), DTHETA:= 0.3e-3*TGAUSS(sigma), DPSI:= 0.3e-3*TGAUSS(sigma);
```

What do these numbers for field error and reference radius mean for a magnet?

# Multipole expansion of static magnetic field

The magnetic field in the aperture of the accelerator magnet is usually expanded as:

$$B_y + iB_x = B_{ref} \sum_{n=1} (b_n + ia_n) \left( \frac{x + iy}{R_{ref}} \right)^{n-1}$$

where  $b_n$ ,  $a_n$ , are normal and skew multipole coefficients.  $R_{ref}$  is the reference radius, and  $B_{ref}$  an appropriately chosen normalization.

For a long magnet, the vector potential  $A$  in the magnet aperture has only the longitudinal component  $A(0, 0, A_z)$ , with:

$$A_z = -B_{ref} \sum_{n=1} (b_n + ia_n) \frac{\text{Re}(x + iy)^n}{nR_{ref}^{n-1}}$$

The Hamiltonian then directly contains the multipole coefficients.

$$H(x, y, z, t) = q\phi + \sqrt{\left( \frac{p_z - q\mathbf{A}}{1 + k_x x} \right)^2 + p_x^2 + p_y^2 + m^2 c^4}$$



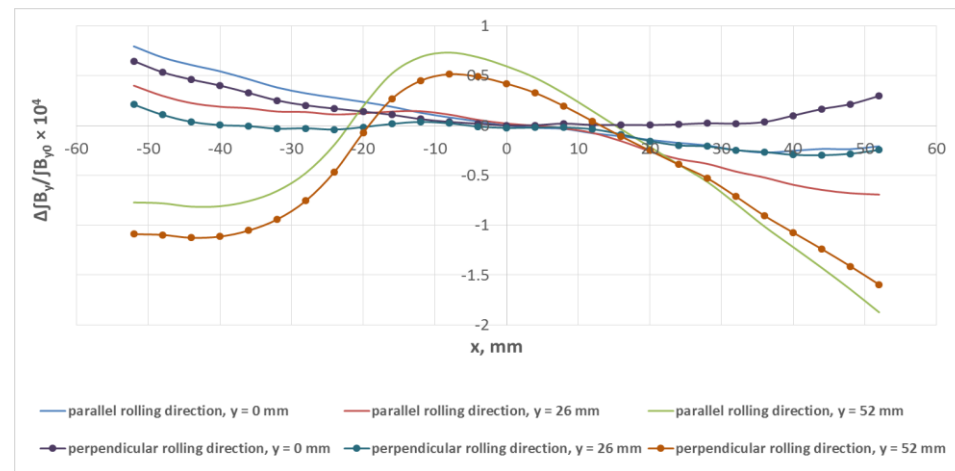
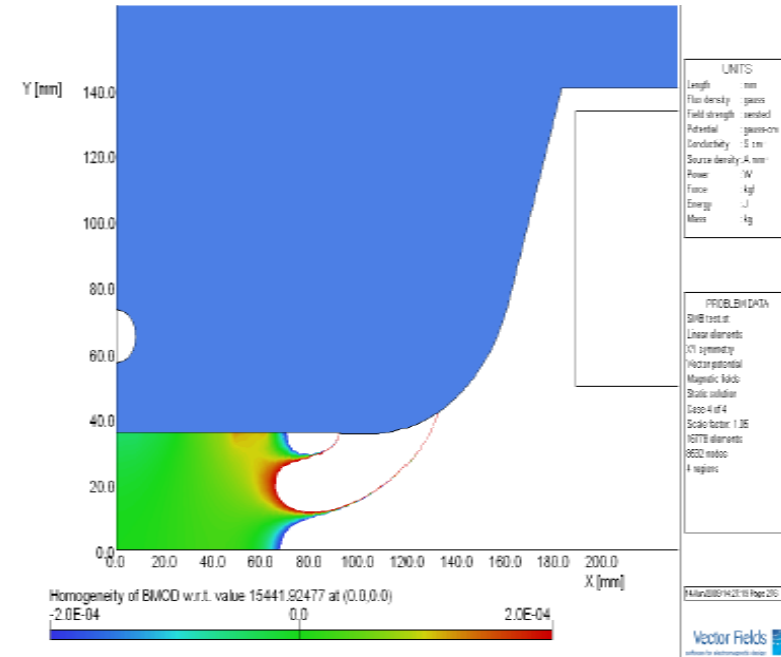
# Main properties of multipole expansion

Multipole expansion:

- is analytical and satisfies automatically the **equations for the static field** in 2D.
- is based on a **complete and orthogonal** set of basis functions:
  - the value of the low order multipoles does not depend on the number of terms included in the expansion (important for precision of dipole, quadrupole and sextupole fields – stability of optical functions – which do not change if the series contains 8 or 10 terms, for example)
- guarantees convergence for all  $r < R_{\text{ref}}$ .
- on a circle is well matched to the rotating coil technique (low measurement and low data treatment errors)
- Most (if not all) optics codes use multipole expansion.
- If the aperture is very asymmetric (classical dipoles), multipole expansion can be performed on an elliptical boundary. Circular and elliptical multipoles are related by a linear transformation.

# “Good Field Region”

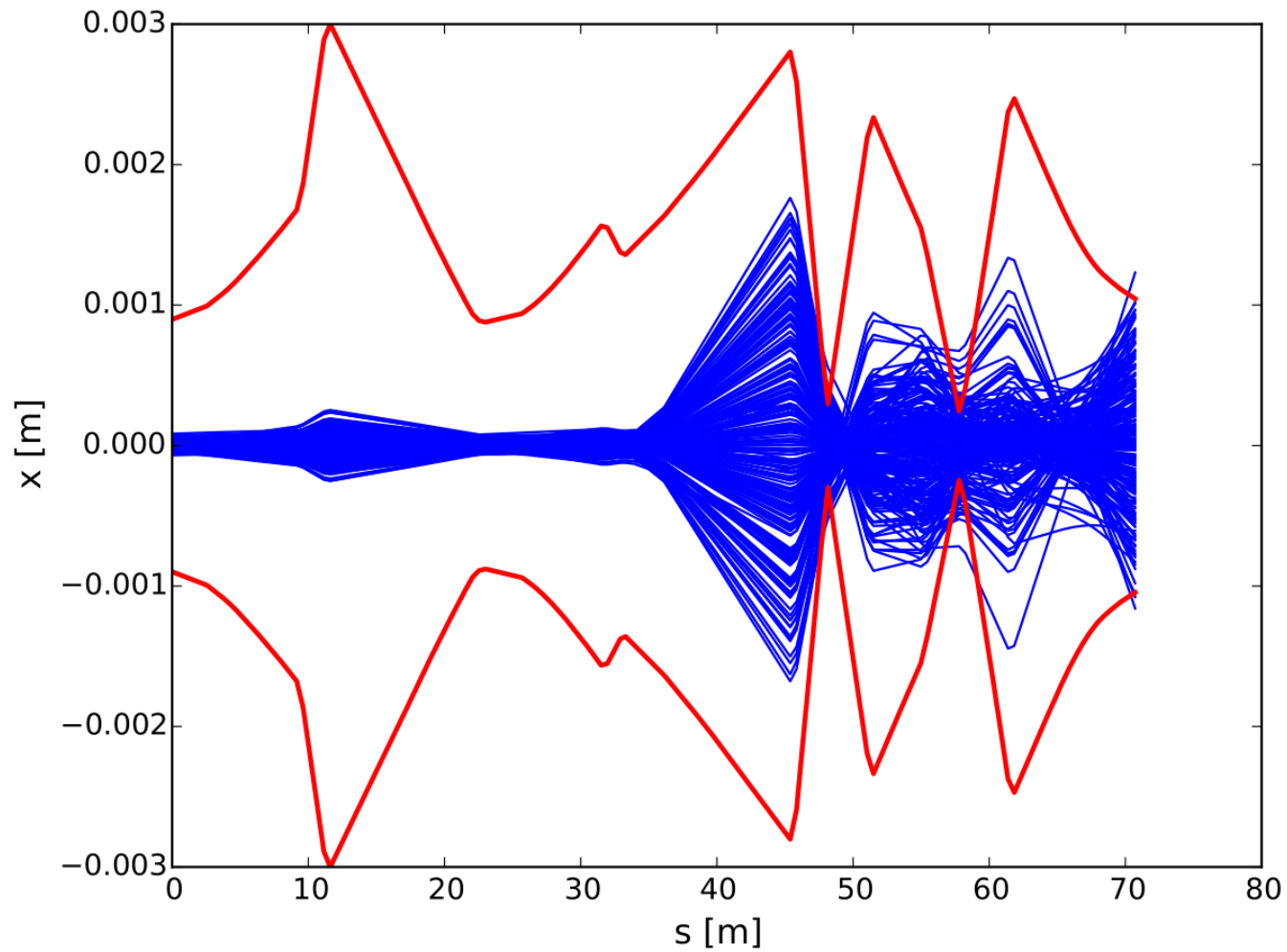
- Concept related to iron-dominated dipole magnets, with an implicit assumption that the field deviations are largest at the borders of the region (near the pole).
- How to use the field plots?
- A field given in layers of  $y=\text{const}$  invites a fit with a polynomial in  $x$ . But:
  - Polynomials are not orthogonal
  - Do not necessarily satisfy the field equations.



# Magnet errors in transfer lines

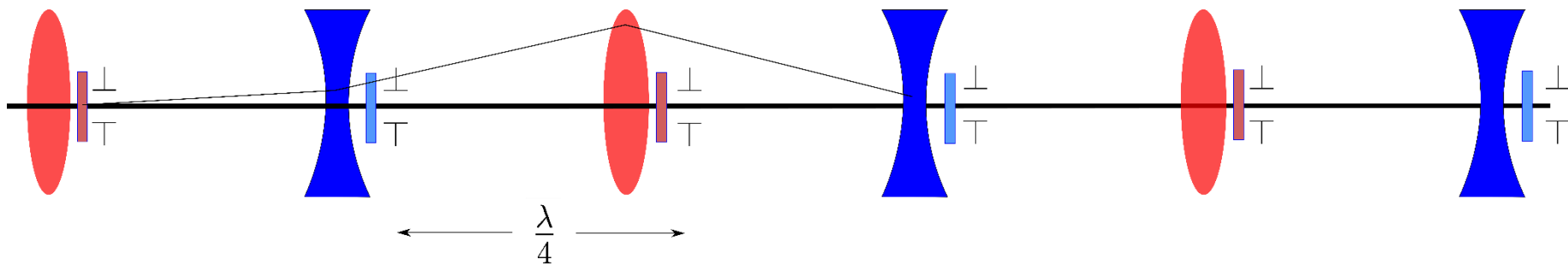
- The errors of the magnetic elements to be considered in the transfer lines are:
  - Linear terms: dipole and quadrupole strengths, including PC errors, transverse misalignments and rotations
  - First non-linear term: normal sextupole
    - These errors affect the emittance growth, rms orbit errors, and chromatic properties of the transfer lines.
- The relevant factors are the strengths of magnetic field multipoles up to  $n=3$  (sextupole).
- The field in the aperture, measured or calculated, should be obtained on the largest possible  $R_{ref}$ .
- The specification of the field should be given in terms of multipoles on a circle (or ellipse, in special cases).

# Apply error distributions onto the beam



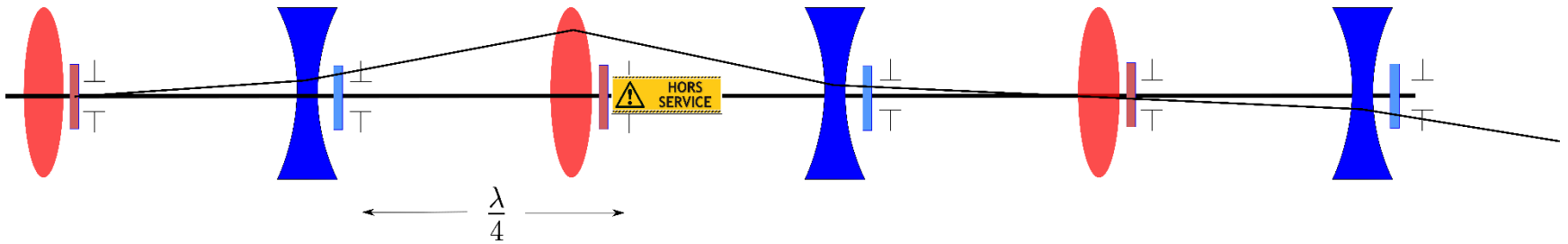
# Trajectory correction

- Use small independently powered dipole magnets (correctors) to steer the beam
- Measure the response using monitors (pick-ups) downstream of the corrector ( $\pi/2$ ,  $3\pi/2$ , ...)



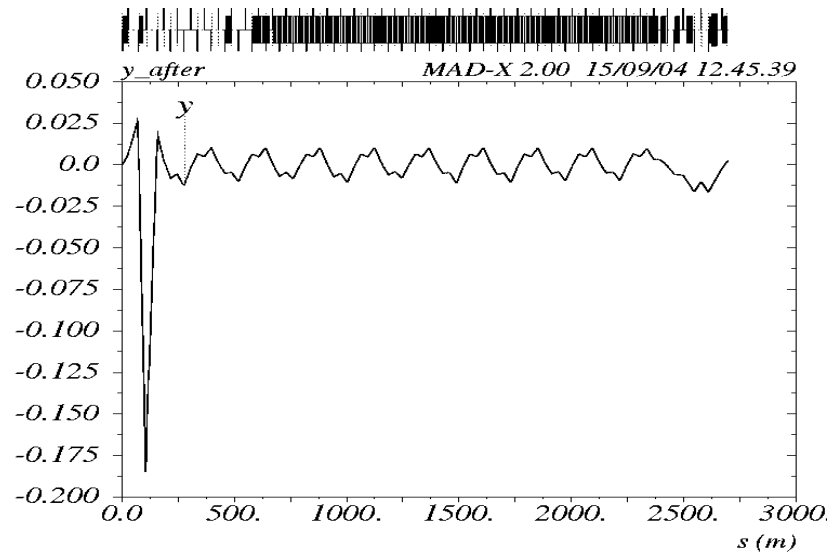
- Horizontal and vertical elements are separated
- H-correctors and pick-ups located at F-quadrupoles (large  $\beta_{tx}$ )
- V-correctors and pick-ups located at D-quadrupoles (large  $\beta_{ty}$ )

# $\pi$ - bumps



Correction with some monitors disabled

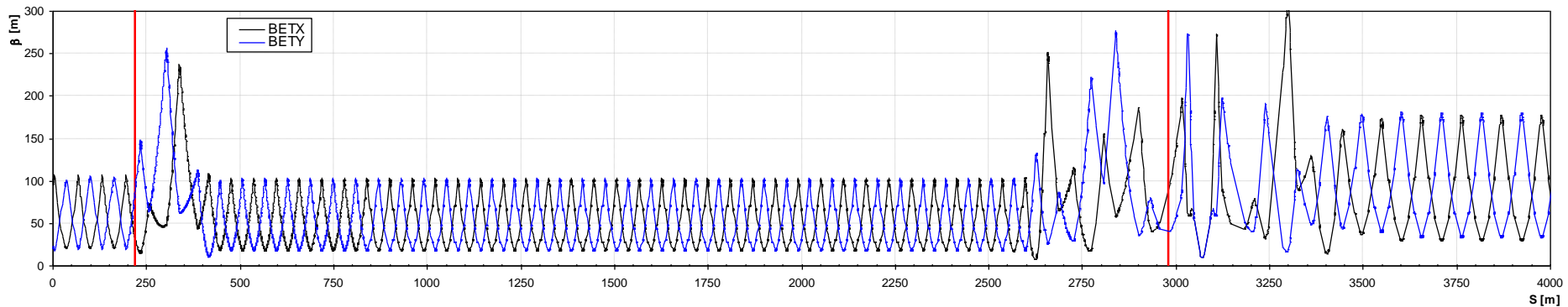
With poor BPM phase sampling the correction algorithm produces a trajectory with 185mm  $y_{\max}$



Sufficient instrumentation is essential for trajectory correction

# Trajectory correction

- Global correction can be used which attempts to minimise the RMS offsets at the BPMs, using all or some of the available corrector magnets.
- Steering in matching sections, extraction and injection region requires particular care
  - D and beta functions can be large  $\rightarrow$  bigger beam size
  - Often very limited in aperture
  - Injection offsets can be detrimental for performance
  - Losses at collimators



# Correction

```
SELECT, FLAG=ERROR, FULL;
ESAVE, FILE='errors.tfs';

select, flag=twiss, clear;
select, flag= twiss, column= s,x,y,betx,bety,px,py;
TWISS, file="outcorr/test/twissnocorr.nx.tfs", deltap= 0.0, sequence= bt1btp, BETA0=INITBETA0;

option, echo;
COPTION, PRINT=10;

CORRECT, flag = line, PLANE= x, MODE=svd, COND=0, MONON=1, MONERROR=1, MONSCALE=0, RESOUT=0,
        ERROR=1.E-6, CORRLIM=1.0, CLIST="/orbit_correction/xcorr.nx.out";
CORRECT, flag = line, PLANE= y, MODE=svd, COND=0, MONON=1, MONERROR=1, MONSCALE=0, RESOUT=0,
        ERROR=1.E-6, CORRLIM=1.0, CLIST="/orbit_correction/ycorr.nx.out";

select, flag= corr, column= PX.OLD, PY.OLD, PX.CORRECTION, PY.CORRECTION;

select, flag=twiss, clear;
select, flag= twiss, column= s,x,y,betx,bety,px,py;
TWISS, file="outcorr/test/twisscorr.nx.tfs", deltap= 0.0, sequence= bt1btp, BETA0=INITBETA0;
};

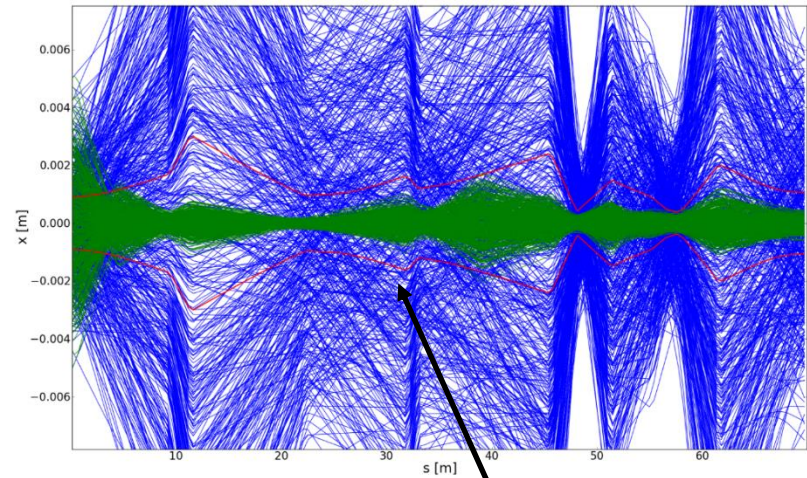
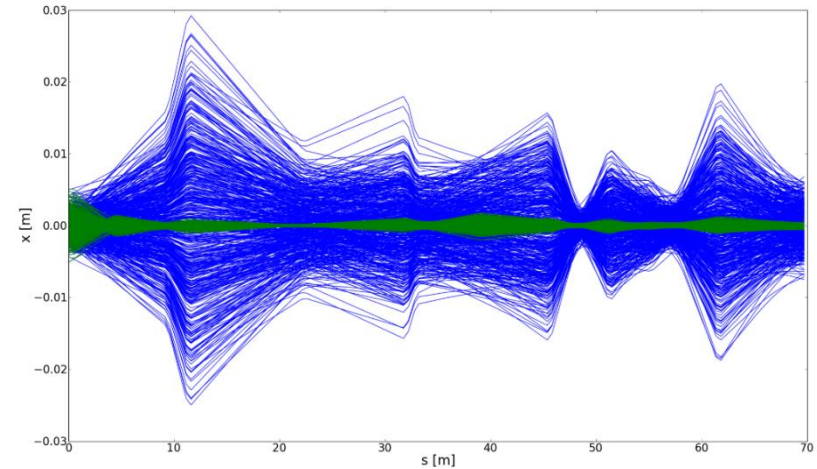
n=0;
while (n < 200) {
    exec, corrmacro($n);
    n= n+1;
}
```

Check that corrector kicks are not adding up  
→ set them to 0 each time



# Output

- Display uncorrected/corrected trajectories
- Compare to what is included in aperture definition (losses)

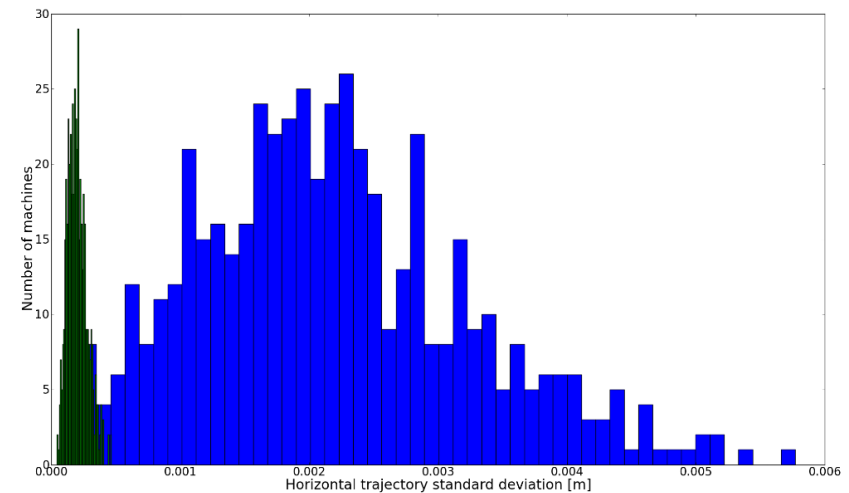
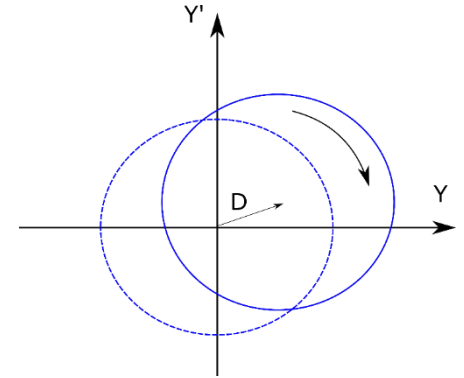


$$A_{x,y} = \pm n_{sig} \cdot \sqrt{k_{\beta} \cdot \beta_{x,y} \cdot \frac{\epsilon_{x,y}}{\beta_{\gamma}}} \pm D_{x,y} \cdot k_{\beta} \cdot \frac{\Delta p}{p} \pm CO \cdot \sqrt{\frac{\beta_{x,y}}{\beta_{xmax,ymax}}} \pm \text{align}$$

# Output

- Display uncorrected/corrected trajectories
- Compare to what is included in aperture definition (losses)
- Statistics on error at handover to ring – filamentation will occur
- Useful to express error in  $x$ ,  $p_x$ ,  $y$ ,  $p_y$  in displacement vector form in normalized phase space – can directly estimate the expected emittance growth

$$\epsilon_2 = \epsilon_1 + \frac{1}{2}D^2$$



# Output

- Display uncorrected/corrected trajectories
- Compare to what is included in aperture definition (losses)
- Statistics on error at handover to ring – filamentation will occur
- Useful to express error in x, px, y, py in displacement vector form in normalized phase space – can directly estimate the expected emittance growth
- Sensitivity analysis – which error is the most important one
  - Instrumentation sensitivity – reading/scaling error and full failure – pi bumps!

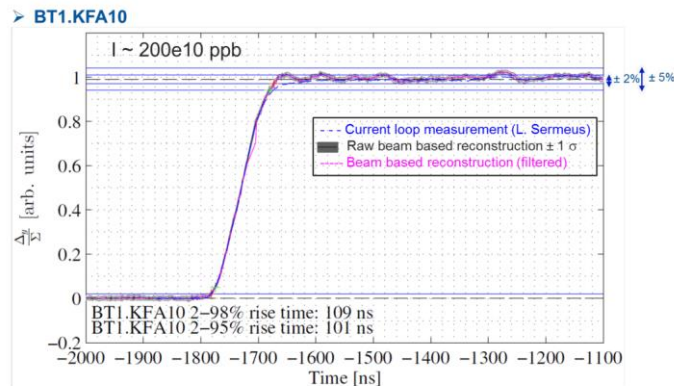
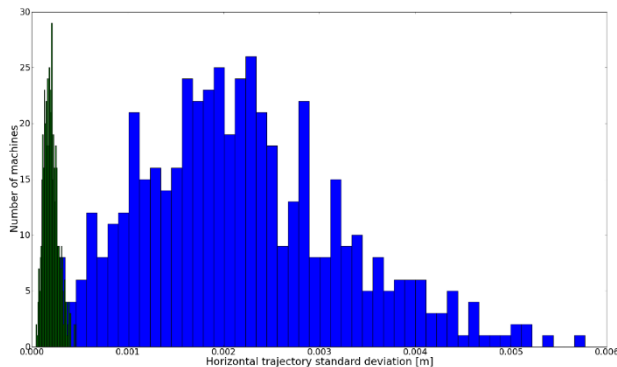
	Tolerance $\Delta I/I$	x rms mm	$p_x$ rms $\mu\text{rad}$	$R_x^2/\epsilon_0$ $1 \times 10^{-3}$	y rms mm	$p_y$ rms $\mu\text{rad}$	$R_y^2/\epsilon_0$ $1 \times 10^{-3}$
<i>Random effects</i>							
PSB orbit $\pm 0.15/0.10$ mm (h/v)		0.04	4	<b>0.4</b>	0.04	2	<b>0.2</b>
BVT10	$1 \times 10^{-4}$				0.08	1	<b>0.3</b>
SMV10	$1 \times 10^{-4}$				0.13	1	<b>1</b>
QNO10	$5 \times 10^{-4}$				0.11	1	<b>1</b>
QNO20	$5 \times 10^{-4}$				0.03	1	<b>0.06</b>
KFA10	$3 \times 10^{-4}$				0.02	1	<b>0.06</b>
SMV20	$1 \times 10^{-4}$				0.01	4	<b>1</b>
KFA20	$3 \times 10^{-4}$				0.01	0	<b>0.02</b>
BVT20	$1 \times 10^{-4}$				0.05	3	<b>1</b>
BT.BHZ10	$1 \times 10^{-4}$	0.07	0.02	<b>4</b>			
<b>All random effects</b>		<b>0.08</b>	<b>17</b>	<b>5.1</b>	<b>0.21</b>	<b>6</b>	<b>4.0</b>
<i>Systematic effects</i>							
KFA10	$5 \times 10^{-3}$				0.39	15	<b>17</b>
KFA20	$5 \times 10^{-3}$				0.22	8	<b>5</b>

# Specify transverse feedback

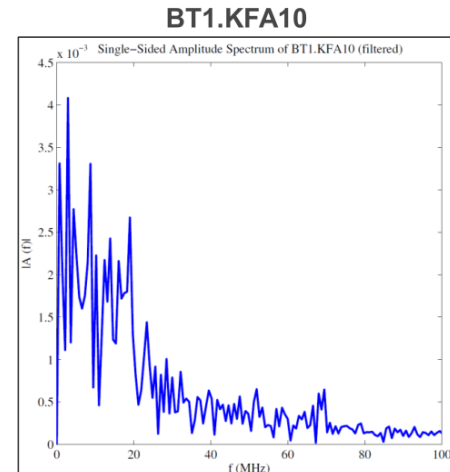
$$\epsilon_2 = \epsilon_1 + \frac{1}{2} \left( (\Delta y)^2 \frac{1+\alpha^2}{\beta} + (\Delta y')^2 \beta \right) \left( \frac{1}{1+\tau_D C/\tau_d} \right)^2$$

Damping effect of  
transverse feedback

Need to specify the peak oscillation amplitude and bandwidth of the system



Vincenzo Forte



# Typical specifications from correction studies

- Number of monitors and required resolution
  - Every  $\frac{1}{4}$  betatron wavelength
  - Grid resolution:  $\sim 3$  wires/sigma
- Number of correctors and strength
  - Every  $\frac{1}{2}$  betatron wavelength H - same for V
  - Displace beam by few betatron sigma per cell
- Dipole and quadrupole field errors
  - Integral main field known to better than  $1-10 \text{ E-}4$
  - Higher order field errors  $< 1-10 \text{ E-}4$  of the main field
- Dynamic errors from power converter stability
  - $1-10\text{e-}5$
- Alignment tolerances
  - $0.1-0.5 \text{ mm}$
  - $0.1-0.5 \text{ mrad}$



Take typical values as good guess starting point and refine them according to your simulations



Error source	tolerance $\Delta I/I_{nom}$	$\Delta\sigma_x$	$\Delta\sigma_y$
<i>Random effects</i>			
SPS Orbit $\pm 0.10\text{mm}$		0.113	0.113
Line stability $\pm 0.20\text{mm}$		0.226	0.226
MSE	$\pm 1.3\text{E-}04$	0.104	0.000
BH1	$\pm 5.0\text{E-}05$	0.083	0.000
MSI	$\pm 5.0\text{E-}05$	0.096	0.000
MBI	$\pm 2.5\text{E-}05$	0.171	0.000
BV1	$\pm 2.5\text{E-}05$	0.000	0.112
rms sum ( $1 \sigma$ )		0.342	0.279
<i>Systematic effects</i>			
MKE (systematic)	$\pm 5.0\text{E-}03$	0.224	0.000
MKI (systematic)	$\pm 5.0\text{E-}03$	0.000	0.354

# Summary

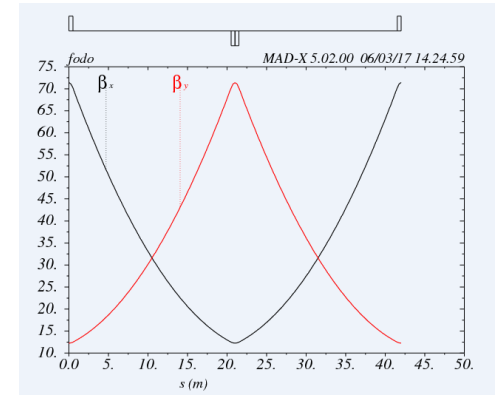
- Before switching on a computer we can define for a transfer line
  - Number of dipoles and quadrupoles, correctors and monitors
  - Dipole field and quadrupole pole tip field
  - Aperture of magnets and beam instrumentation
  - Rough estimate of required field quality and alignment accuracy
- With computer codes
  - We can calculate the optics for matching sections and final focus for fixed target beams
    - Give a precise value for the field in each dipole and quadrupole
  - We can run error and correction studies
    - Define misalignment tolerances
    - Define field homogeneity and ripple
    - Define sensitivity of instrumentation
    - Define specifications for transverse feedback systems

# Wrap up - optics

- FODO

- Classical choice for high flux transport
- Analytically straightforward – can create achromat ‘by eye’
- Good aperture and correction behaviour

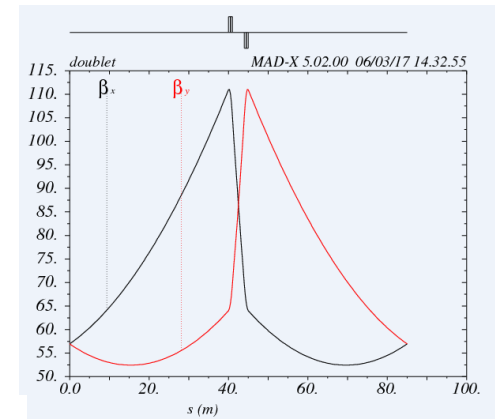
$$\frac{L}{f} = 4 \sin \frac{\mu}{2}$$



- Doublet

- Provides space for equipment
- Steep, asymmetric in beta functions
- Can focus from point source to parallel beams and point-to-point (secondary beam lines)

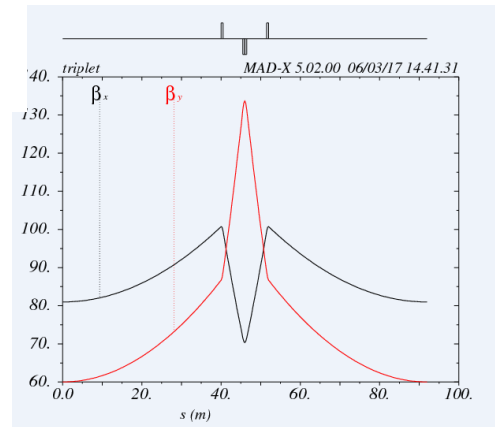
$$f^* = \frac{f^2}{d}$$



- Triplet

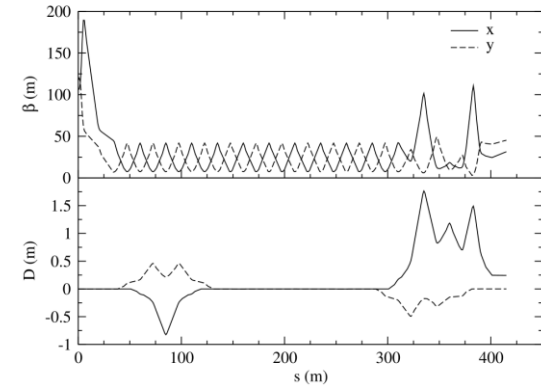
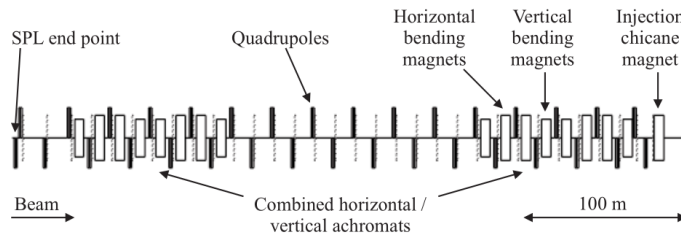
- Locally very high beta functions
- Can focus beta to low values over long distance – good for dipole aperture
- Can provide large phase advance over short distance – good to close a dispersion bump, achromat
- Versatile for final focus matching and secondary beam lines (point to parallel – parallel to point)

$$f^* = \frac{f^2}{2d} \left( 1 + \frac{d}{f} \right)$$



# Wrap up - achromat

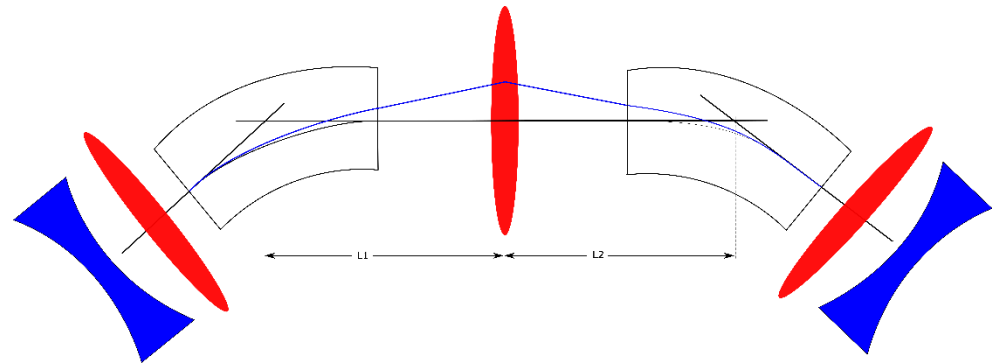
- Straight forward dipole locations in a FODO lattice



- Spectrometer functionality if

$$\frac{1}{f} = \frac{1}{L_1} + \frac{1}{L_2}$$

$$L_1 s_1 = L_2 s_2$$





## Wrap up – error/correction studies

- Make sure magnet and optics designer speak about the same errors
- Multipole expansion is a useful language
- For a transfer line errors up to order  $n=3$  (sextupole) are relevant
- Trajectory correction in a line is straight forward
  - Specify sensitivity of instrumentation – be aware of pi-bumps in case of failure
- Apply errors systematically (distributed error function, sensitivity check) and evaluate effect on beam quality (losses, emittance)

# Thank you for your attention

And many thanks to my colleagues for helpful input:

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- [1] B. Goddard. Transfer lines. *CAS*, 2004.
- [2] N. Ibarrola and M. Jones. Analysis and Evaluation of the CERN Reference Systems. *International Workshop of Accelerator Alignment*, 2016.
- [3] M Fraser et al. Beam Dynamics Studies of the ELENA Electrostatic Transfer Lines. (CERN-ACC-2015-340):MOPJE044. 4 p, 2015.
- [4] D. Johnson. Challenges Associated with 8 GeV H- Transport and Injection for FERMILAB PROJECT-X \*. (Proceedings of Hadron Beam 2008), 2008.
- [5] P. Bryant. Beam Transfer Lines. (CAS), 1992.
- [6] D. Carey. The Optics of Charged Particle Beams. 1987.
- [7] J. Rossbach and P. Schmueser. Basic Course on Accelerator Optics. (CAS), 1992.
- [8] Senichev Yuriy. A "resonant" lattice for a synchrotron with a low or negative momentum compaction factor. 1997.
- [9] Werner Herr. Mathematical and Numerical Methods for Non Linear Beam Dynamics in Rings. CAS 2013.