Beam Position Monitor: Detector Principle, Hardware and Electronics Peter Forck, Piotr Kowina and Dmitry Liakin Gesellschaft für Schwerionenforschung, Darmstadt

Outline:

- ➤ Signal generation → transfer impedance
- Consideration for capacitive shoe box BPM
- Consideration for capacitive button BPM
- ➤ Other BPM principles: stripline → traveling wave, inductive → wall current, cavity → resonator for dipole mode
- Electronics for position evaluation
- Some examples for position evaluation and other applications
- > Summary

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General Idea: Detection of Wall Charges

The image current at the vacuum wall is monitored on a high frequency basis i.e. the ac-part given by the bunched beam.



For relativistic velocities, the electric field is mainly transversal: $E_{\perp,lab}(t) = \gamma \cdot E_{\perp,rest}(t)$



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- It has a low cut-off frequency i.e. dc-beam behavior can not be monitored (exception: Schottky spectra, here the physics is due to finite number of particles)
- \Rightarrow Usage with bunched beams!
- It delivers information about:
- 1. The center of the beam
- Closed orbit
 - i.e. central orbit averaged over a period much longer than a betatron oscillation
- → Bunch position on a large time scale: bunch-by-bunch → turn-by-turn → averaged position
- Single bunch position \rightarrow determination of parameters like tune, chromaticity, β -function
- > Time evolution of a single bunch can be compared to 'macro-particle tracking' calculations
- ➢ Feedback: fast bunch-by-bunch damping → precise (and slow) closed orbit correction

2. Longitudinal bunch shapes

- Bunch behavior during storage and acceleration
- ➢ For proton LINACs: the beam velocity can be determined by two BPMs
- ≻ Low current *relative* measurement down to 10 nA.

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Model for Signal Treatment of capacitive BPMs

The wall current is monitored by a plate or ring inserted in the beam pipe:



The image current I_{im} at the plate is given by the beam current and geometry: $I_{im}(t) \equiv dQ_{im}/dt = A/\pi a \cdot dQ_{beam}(t)/dt = A/\pi a \cdot l/\beta c \cdot dI_{beam}/dt = A/\pi a \cdot l/\beta c \cdot i\omega I_{beam}(\omega)$ Using a relation for Fourier transformation: $I_{beam} = I_0 e^{i\omega t} \Rightarrow dI_{beam}/dt = i\omega I_{beam}$.

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At a resistor R the voltage U_{im} from the image current is measured. The transfer impedance Z_t is the ratio between voltage U_{im} and beam current I_{beam} in *frequency domain*: $U_{im}(\omega) = R \cdot I_{im}(\omega) = Z_t(\omega, \beta) \cdot I_{beam}(\omega)$.

Capacitive BPM:

- •The pick-up capacitance *C*:
 - plate \leftrightarrow vacuum-pipe and cable.
- •The amplifier with input resistor *R*.
- •The beam is a high-impedance current source:

$$U_{im} = \frac{R}{1 + i\omega RC} \cdot I_{im}$$

= $\frac{A}{\pi a} \frac{1}{\beta c} \cdot \frac{1}{C} \cdot \frac{i\omega RC}{1 + i\omega RC} \cdot I_{beam}$
= $Z_t(\omega, \beta) \cdot I_{beam}$



equivalent circuit

This is a high-pass characteristic with $\omega_{cut} = 1/RC$: It is: $|Z_t(\omega)| = \frac{A}{\pi a} \frac{1}{\beta cC} \cdot \frac{\omega/\omega_{cut}}{\sqrt{1+\omega^2/\omega_{cut}^2}}$ and phase $\varphi(\omega) = \arctan(\omega_{cut}/\omega)$

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Example of Transfer Impedance for Proton Synchrotron

The high-pass characteristic for typical synchrotron BPM.



Signal Shape for capacitive BPMs: differentiated \leftrightarrow proportional



Depending on the frequency range *and* termination the signal looks different: \rightarrow *High frequency range* $\omega \gg \omega_{cut}$:

$$Z_t \propto \frac{i\omega/\omega_{cut}}{1+i\omega/\omega_{cut}} \to 1 \Longrightarrow U_{im}(t) = \frac{1}{C} \cdot \frac{1}{\beta c} \cdot \frac{A}{\pi a} \cdot I_{beam}(t)$$

 \Rightarrow direct image of the bunch. Signal strength $Z_t \alpha A/C$ i.e. nearly independent on length

b Low frequency range $\omega \ll \omega_{cut}$:

$$Z_{t} \propto \frac{i\omega/\omega_{cut}}{1+i\omega/\omega_{cut}} \to i\frac{\omega}{\omega_{cut}} \implies U_{im}(t) = R \cdot \frac{A}{\beta c \cdot \pi a} \cdot i\omega I_{beam}(t) = R \cdot \frac{A}{\beta c \cdot \pi a} \cdot \frac{dI_{beam}}{dt}$$

 \Rightarrow derivative of bunch, single strength $Z_t \alpha$ A, i.e. (nearly) independent on C

Example from synchrotron BPM with 50 Ω termination (reality at p-sychrotron : $\sigma >>1$ ns): derivative intermediate proportional



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Examples for differentiated & proportional Shape

Proton LINAC, e⁻-LINAC&synchtrotron: 100 MHz $< f_{rf} <$ 1 GHz typically *R*=50 Ω processing to reach bandwidth $C\approx$ 5 pF $\Rightarrow f_{cut} = 1/(2\pi RC) \approx$ 700 MHz *Example:* 36 MHz GSI ion LINAC



Proton synchtrotron:

1 MHz $< f_{rf} < 30$ MHz typically $R=1 \text{ M}\Omega$ for large signal i.e. large Z_t $C \approx 100 \text{ pF} \Rightarrow f_{cut} = 1/(2\pi RC) \approx 10 \text{ kHz}$ **Example:** non-relativistic GSI synchrotron $f_{rf}: 0.8 \text{ MHz} \rightarrow 5 \text{ MHz}$ time $[\mu s]$ 3 begin acceleration .: 11 MeV 50 100 200 150 synchrotron circumference [m] time [µs] 0.20.3 0.40.50.60.70.8 end acceleration: 1000 MeV 50 100 200 150 synchrotron circumference [m]

Remark: During acceleration the bunching-factor is increased: 'adiabatic damping'.

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Example Shoe-box BPMs

Shoe-box BPMs used at low β proton & ion synchrotron for $1 \text{MHz} < f_{rf} < 10 \text{MHz}$. *Example:* HIT cancer therapy synchrotron 0.8 MHz $< f_{rf} < 5 \text{ MHz}$ Aperture 180x70 mm² horizontal



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Transfer Impedance Measurement

With a network analyzer and an antenna the BPM properties can be determined.



Calculation of Signal Shape: Single Bunch

The transfer impedance is used in frequency domain! The following is performed:



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Calculation of Signal Shape: Bunch Train



➢ Baseline shift due to ac-coupling

Remark: 1 MHz $< f_{rf} <$ 10MHz \Rightarrow Bandwidth \approx 100MHz=10 $\cdot f_{rf}$ for broadband observation

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Calculation of Signal Shape: Bunch Train

Train of bunches with $R=50 \Omega$ termination: 6 ounch current I_{beem} [mA] 0.8 5 ngle bunch power spectrum bunch train 0.6 4 З 0.42 0.2 1 0 0.0 4 6 time [µs] 2 8 10 0 2 10 120 6 6 frequency [MHz] 2 $[M_{\rm m}]$ **Parameter:** signal voltage U_m $R=50 \Omega \Rightarrow f_{cut}=32 \text{ MHz}$ 0 all buckets filled, no amp *C*=100pF, *l*=10cm, β =50%, σ_t =100 ns -22 4 6 time [μs] 10 \blacktriangleright Low frequency cut-off due to $f_{cut}=32$ MHz Differentiated bunches, 15 fold lower amplitude

> Modified Fourier spectrum with low amplitude value, maximum shift to higher frequencies

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Calculation of Signal Shape: Bunch Train with empty Buckets

Synchrotron during filling: Empty buckets, R=10 k Ω termination:



> Fourier spectrum is more complex, harmonics are broader

> Varying baseline with $\tau = 1/3 f_{cut} = 3 \mu s$

► Baseline shift calls for dedicated restoring algorithm for time domain processing.

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Calculation of Signal Shape: Bunch Train with Cable Damping

Effect of cable or other electronics:



Bunch signal is damped; 8 fold lower amplitude, higher frequencies are damped stronger
 Bunch signal gets asymmetric, baseline did not reach zero

 $\succ \Rightarrow$ 'Good cables' are a precaution for broadband signal transmission

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Calculation of Signal Shape: Filtering of Harmonics

Effect of filters, here bandpass: nth order Butterworth Filter: (Math. simple, but **not** well suited) 1.4 bunch current I_{beem} [mA] single bunch 1.2 $|Z_{low}| = \frac{1}{\sqrt{1 + (\omega / \omega_{cut})^{2n}}}$ bunch train 1.0 0.8 0.6 $|Z_{high}| = \frac{(\omega / \omega_{cut})^n}{\sqrt{1 + (\omega / \omega_{cut})^{2n}}}$. 0.4 0.20 0.0 2 4 6 time [µs] 10 8 0 0 10 2 8 frequency [MHz] 0.8 $Z_{filter} = Z_{high} \cdot Z_{low}$ □ 0.6 ំ0.4 ផ្ទ Ringing due to sharp cutoff **Parameter:** 0.2 $R=10 \text{ k}\Omega, 4^{\text{th}} \text{ order}$ \triangleright Other filter types more appropriate -0.0Butterworth filter at *f_{cut}*=2 MHz -0.2, -0.4 $C=100 \text{pF}, l=10 \text{cm}, \beta=50\%, \sigma=100 \text{ ns}$ -0.62 4 6 frequency [MHz] n Generally: $Z_{tot}(\omega) = Z_{cable}(\omega) \cdot Z_{filter}(\omega) \cdot Z_{amp}(\omega) \cdot \dots \cdot Z_{t}(\omega)$ Calculation via FFT: $I_{beam}(t) \xrightarrow{FFT} I_{beam}(\omega) \rightarrow U_{im}(\omega) = Z_{tot}(\omega) \cdot I_{beam}(\omega) \xrightarrow{invFFT} U_{im}(t)$ Remark: For electronics calculation, time domain filters (FIR and IIR) are more appropriated

Principle of Position Determination with BPM

The difference between plates gives the beam's center-of-mass \rightarrow most frequent application

'Proximity' effect leads to different voltages at the plates:



It can be assumed: $Z_{\perp}(\omega, x) = k(\omega, x) \cdot Z_t(\omega)$

with $k(\omega, x)$ or $S(\omega, x) = 1/k(\omega, x)$ called displacement sensitivity

They are geometry dependent, non-linear function, which have to be optimized.

Units: *k*=[mm] and *S*=[%/mm] or *S*=[dB/mm]

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Outline:

- ➤ Signal generation → transfer impedance
- > Consideration for capacitive 'shoe box' = 'linear cut' BPM

position sensitivity calculation, crosstalk, realization

- **Consideration for capacitive button BPM**
- ➤ Other BPM principles: stripline → traveling wave, inductive → wall current, cavity → resonator for dipole mode
- > Electronics for position evaluation
- Some examples for position evaluation and other applications
 Summary

Shoe-box BPM for Proton or Ion Synchrotron

Frequency range: 1 MHz $\leq f_{rf} \leq 10$ MHz \Rightarrow bunch-length >> BPM length.



Boundary Contribution \Rightarrow FEM Calculation required

Boundary condition by the environment can significantly influence BPM properties

- \Rightarrow real properties have to be calculated numerically by Finite Element Method: Examples are: CST-Studio (MAFIA), Comsol, HFFS General idea of FEM calculations:
- \blacktriangleright Volume is divided in 3-dim meshes with typically 10⁶ to 10⁷ nodes
- Fixed boundary conditions at the mechanical parts and eventually source terms
- ≻Goal: Field distribution within the meshes
- The Maxwell equations are solved by iterative matrix inversion
- Time domain: Propagation of source terms (here: Gaussian shaped pulse corresponding to 200 MHz bandwidth)
- ≻Frequency domain: e.g. eigenmodes

>Output: time dependent signal, frequency dependences, S-parameters, field distribution etc.



Simulation: Gaussian pulse travels on wire on different positions

- \rightarrow induced voltage calculated on matched output ports
- \rightarrow calculation of $\Delta U/\Sigma U$

Criteria of optimization: linearity, sensitivity, offset reduction, x-y plane independence



Nearly perfect behavior: k_x =104mm, δ_x =-0.4mm (ideal value k_x =90mm, δ =0) k_y =38mm, δ_y =-0.04mm (ideal value k_y =35mm, δ =0) at 1 MHz

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Frequency Dependence of Position Sensitivity



Plate—to-Plate Cross-Talk reduces Sensitivity

- •Capacitive coubling determines position sensitivity
- •Plate-to-plate cross talk caused by ceramic permittivity ϵ =9.6 resulting in high coupling capacitance between adjacent plates
- ⇒Insertion of the guard-ring between plates reduces cross talks by more than 10dB



-18

-161 -384 -913

Technical Realization of Shoe-Box BPM

Technical realization at HIT synchrotron of 46 m length for 7 MeV/u \rightarrow 440 MeV/u BPM clearance: 180x70 mm², standard beam pipe diameter: 200 mm.





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Other Types of diagonal cut BPM

Round type: cut cylinder Same properties as shoe-box:



Other realization: Full metal plates

- \rightarrow No guard rings required
- \rightarrow but mechanical alignment more difficult

Wounded strips:

Same distance from beam and capacitance for all plates But horizontal-vertical coupling.



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- Consideration for capacitive button BPM simple electro-static model, low β effect, modification for synch. light source Comparison shoe box button BPM

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- ➤ Other BPM principles: stripline → traveling wave, inductive → wall current, cavity → resonator for dipole mode
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LINACs, e⁻-synchrotrons: 100 MHz $\leq f_{rf} \leq 3$ GHz \rightarrow bunch length \approx BPM length

Button BPM with 50 $\Omega \Rightarrow U_{im}(t) = R \cdot \frac{A}{\beta c \cdot \pi a} \cdot \frac{dI_{bea}}{dt}$ Example: LHC type incide on BeCu CENTER SMA TYPE -CONDUCTOR //OLYBDENU// ENTER PIN Example: LHC-type inside cryostat: ALUMINA Ø24 mm, half aperture a=25 mm, C=8 pF \Rightarrow f_{cut}=400 MHz, Z_∞ = 1.3 Ω : CuN HOUSING 51.5 CM BUTTON From C. Boccard (CERN) G 5 1 P. Forck, P. Kowina, D. Liakin, GSI, CAS, May 30th, 2008 28 Beam Position Monitors: Principle and Realization

 \rightarrow 50 Ω signal path to prevent reflections

2-dim Model for Button BPM

'Proximity effect': larger signal for closer plate <u>Ideal 2-dim case:</u> Cylindrical pipe \rightarrow image current density via 'image charge method' for 'pensile' beam:

$$j_{im}(\phi) = \frac{I_{beam}}{2\pi a} \cdot \left(\frac{a^2 - r^2}{a^2 + r^2 - 2ar \cdot \cos(\phi - \theta)}\right)$$

Image current: Integration of finite BPM size:

plate
current density
$$I_{im} = \int_{-\alpha/2}^{\alpha/2} j_{im}(\phi) d\phi$$



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Ideal 2-dim model:

Due to the non-linearity, the beam size enters in the position reading.



Remark: For most LINACs: Linearity is less important, because beam has to be centered

 \rightarrow correction as feed-forward for next macro-pulse.

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FEM Calculation for Button BPM simple Test Case

For realistic beam, 3-dim FEM calculations are required. *Example:* Button BPM at r=3 cm beam-pipe, flat, round \emptyset 4cm frequency f_{rf} =150 MHz, effect for higher harmonics calculated



Low Velocity Effect: General Consideration

Simple Lorentz transformation of single point-like charge: Lorentz boost and transformation of time: $E_{\perp}(t) = \gamma E'(t')$ and $t \rightarrow t'$

E-field of a point-like charge:

$$E_{\perp}(t) = \frac{e}{4\pi\varepsilon_0} \cdot \frac{\gamma R}{\left[R^2 + \left(\gamma\beta ct\right)^2\right]^{3/2}}$$



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FEM Calculation of low B Effect for p-LINAC



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Position Measurement for Button BPM

Example <u>L</u>HC type: Measurement with movable 50 Ω matched antenna:

Non-linearity and horizontal-vertical coupling

 \Rightarrow Polynomial fit with x and y dependence

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Realization of Button BPM at LHC

Example LHC: \emptyset 24 mm, half aperture a=25 mm, installed inside cryostat Critically: 50 Ω matching of button to standard feed-through.



From C. Boccard, C. Palau-Montava et al.(CERN).

The button BPM can be rotated by 45° to avoid exposure by synchrotron light:

Frequently used at boosters for light sources



horizontal:
$$x = \frac{1}{S} \cdot \frac{(U_1 + U_4) - (U_2 + U_3)}{U_1 + U_2 + U_3 + U_4}$$

vertical: $y = \frac{1}{S} \cdot \frac{(U_1 + U_2) - (U_3 + U_4)}{U_1 + U_2 + U_3 + U_4}$

Example: Booster of ALS, Berkeley



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Due to synchrotron radiation, the button insulation might be destroyed \Rightarrow buttons only in vertical plane possible \Rightarrow increased non-linearity Optimization: horizontal distance and size of buttons 08







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Beam position swept with 2 mm steps
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From S. Varnasseri, SESAME, DIPAC 2005 -Beam Position Monitors: Principle and Realization

Comparison Shoe-Box and Button BPM



	Shoe-Box BPM	Button BPM
Precaution	Bunches longer than BPM	Bunch length comparable to BPM
Shape	Rectangular, cut cylinder	Orthogonal or in-plane orientation
BPM length (typical)	10 to 20 cm length per plane	Ø1 to 3 cm per button
Bandwidth (typical)	0.1 to 100 MHz	100 MHz to 5 GHz
Coupling	1 M Ω or $\approx 1 \text{ k}\Omega$ (transformer)	50 Ω
Cutoff frequency (typical)	0.01 10 MHz (<i>C</i> =30100pF)	0.3 1 GHz (<i>C</i> =210pF)
Linearity	Very good, no x-y coupling	Non-linear, x-y coupling
Sensitivity	Good, care: plate cross talk	Good, care signal matching
Usage	At (low energy) proton synchrotrons	All electron acc., proton Linacs, high energy synchrotrons
	vertical	
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