



Magnets

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CAS - Basics of Accelerator Physics and
Technology

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Contents

- Introduction
 - magnetic field and magnet principles for resistive and superconducting magnets
 - Field description and magnet types
- Resistive magnets
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- Literature on Magnets



The 2 Maxwell equations relevant for magnets

Integral form

$$\oint \vec{H} d\vec{s} = \int_A \left(\vec{J} + \frac{\partial \vec{D}}{\partial t} \right) d\vec{A}$$

Ampere's law:

“A magnetic field is produced by an electrical current or a time varying electrical field”

Differential form

$$\text{rot} \vec{H} = \vec{J} + \frac{\partial \vec{D}}{\partial t}$$

$$\int_A \vec{B} d\vec{A} = 0$$

Gauss's law for magnetism:

The magnetic field is divergence free: the flux lines are closed

$$\text{div} \vec{B} = 0$$

With: $\vec{B} = \mu \vec{H} = \mu_0 \mu_r \vec{H}$



Magnetic field quality: multipole description

$$B_y(z) + iB_x(z) = 10^{-4} B_1 \sum_{n=1}^{\infty} (b_n + ia_n) \left(\frac{x + iy}{R_{ref}} \right)^{n-1}$$

with:

$$z = x + iy,$$

B_x and B_y the flux density components in the x and y direction,

R_{ref} the radius of the reference circle,

B_1 the dipole field component at the reference circle,

b_n the normal n th multipole component,

a_n the skew n th multipole component.

In a ring shaped accelerator, where the beam does multiple passes, one typically demands :

$$a_n, b_n \leq 1 \text{ unit } 10^{-4}$$

From Ampere's law with no time dependencies, We can derive the law of **Biot and Savart**

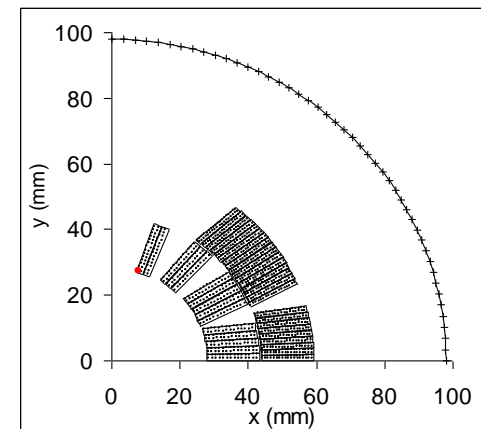
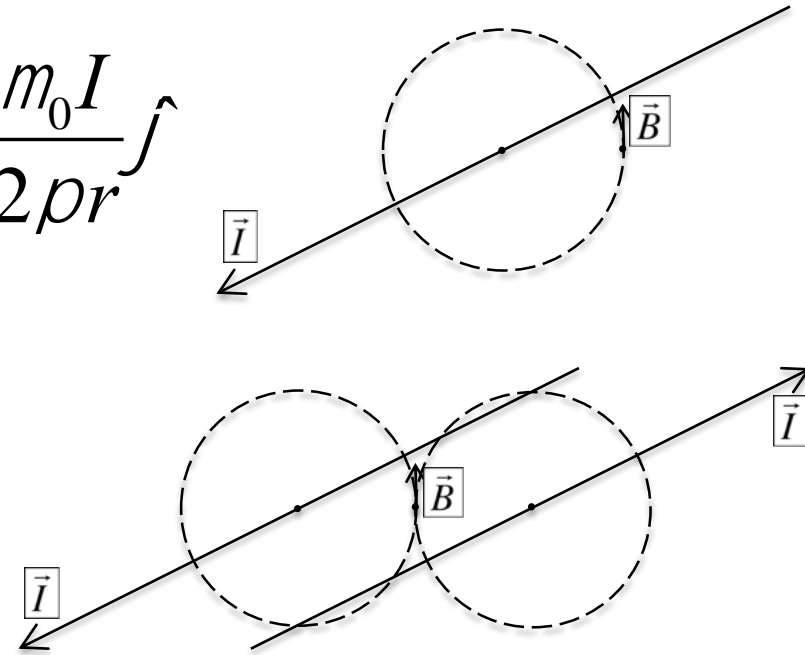
$$\vec{B} = \frac{\mu_0 I}{2\pi r} \hat{j}$$

If you wanted to make a $B = 1.5$ T magnet with just two infinitely thin wires placed at 100 mm distance in air one needs : $I = 187500$ A

- To get reasonable fields ($B > 1$ T) one needs large currents
- Moreover, the field homogeneity will be poor

And If you wanted to make a $B = 8$ T one needs : $I = 5 \cdot 10^5$ A
(LHC dipole coil 80 turns of 11850 A at 8.3 T = $9.48 \cdot 10^5$ A)

For LHC dipole @ 8.3 T ~ 1 MA in 3300 mm² : ~ 300 A/mm²
(overall current density in the coil area)

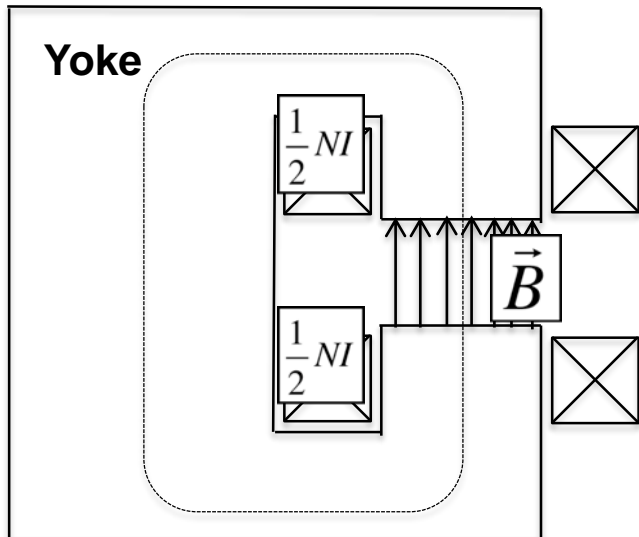


Courtesy E. Todesco

Iron dominated magnets (aka: Classical, Resistive)

With the help of an iron yoke we can get fields with less current

Example: C shaped dipole for accelerators



coil

$B = 1.5 \text{ T}$

Gap = 50 mm

$N \cdot l = 59683 \text{ A}$

2 x 30 turn coil

$l = 994 \text{ A}$

@5 A/mm², 200 mm²

14 x 14 mm Cu

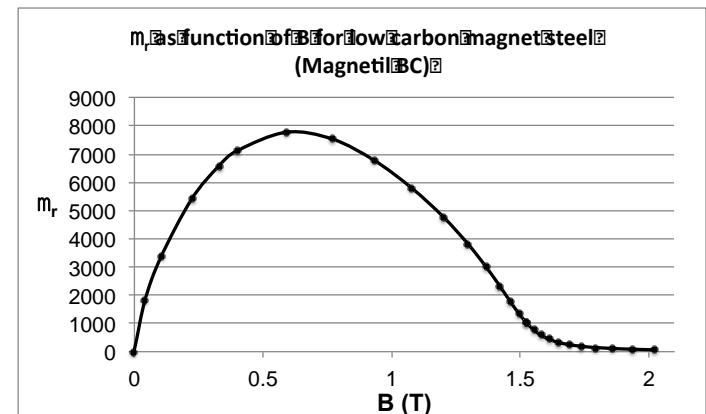
$$\oint_C \vec{H} \times d\vec{l} = N \times I$$

$$N \times I = H_{iron} \times l_{iron} + H_{airgap} \times l_{airgap} \quad \text{D}$$

$$N \times I = \frac{B}{\cancel{\mu_0} \mu_r} \times l_{iron} + \frac{B}{\mu_0} \times l_{airgap} \quad \text{D}$$

$$N \times I = \frac{l_{airgap} \times B}{\mu_0}$$

This is valid as $\mu_r \gg \mu_0$ in the iron : limited to $B < 2 \text{ T}$





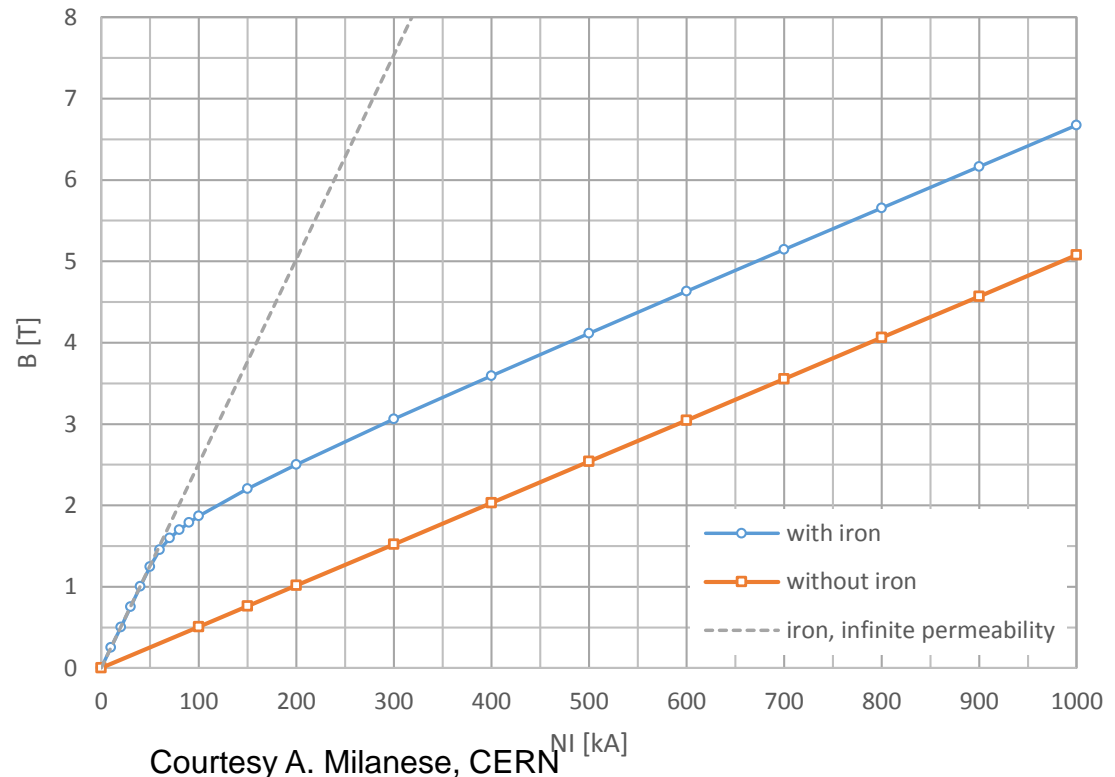
Comparison : iron magnet and air coil

Imagine a magnet with a 50 mm vertical gap (horizontal width ~100 mm)

Iron magnet wrt to an air coil:

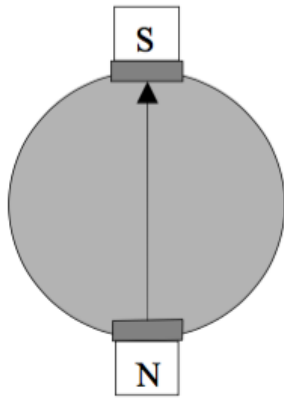
- Up to 1.5 T we get ~6 times the field
- Between 1.5 T and 2 T the gain flattens of : the iron saturates
- Above 2 T the slope is like for an air-coil: currents become too large to use resistive coils

These two curves are the transfer functions – B field vs. current – for the two cases

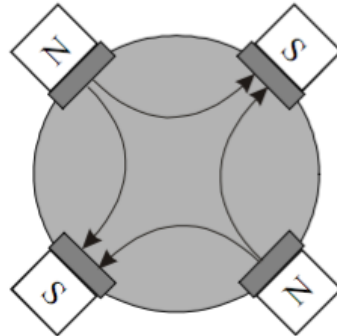


Types of magnet fields for accelerators

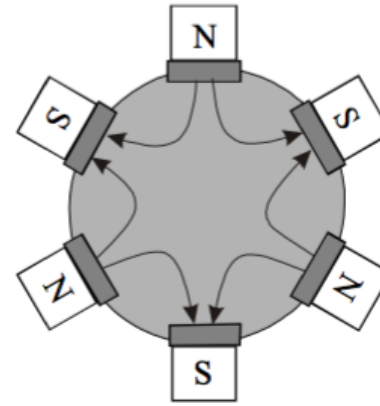
NORMAL : vertical field on mid-plane



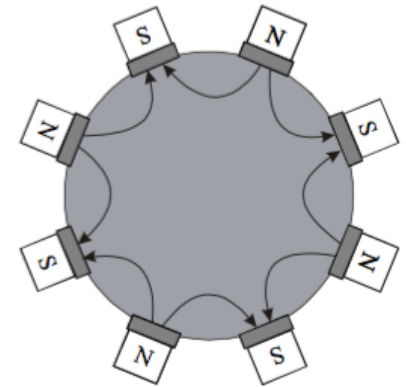
Dipole
 $|B|=const$



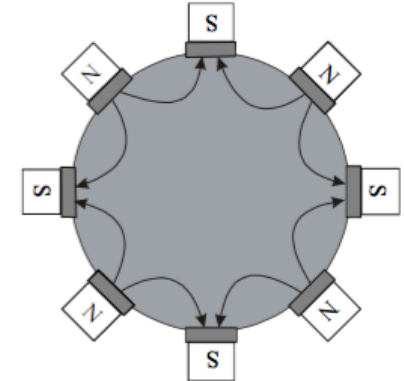
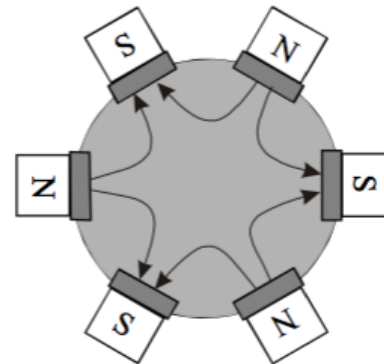
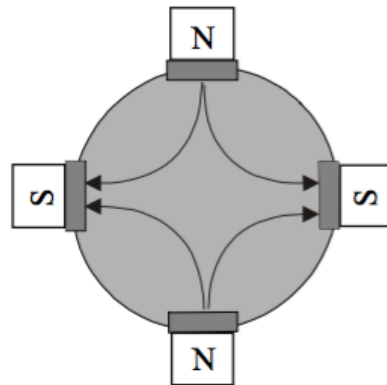
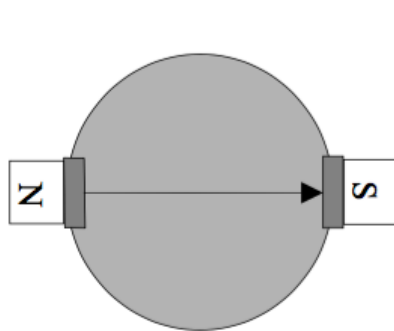
Quadrupole
 $|B|=G \cdot r$



Sextupole
 $|B|=1/2 \cdot B'' \cdot r^2$

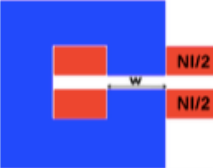
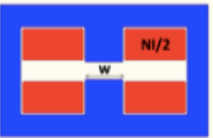
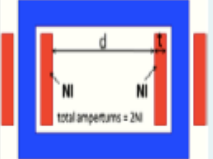
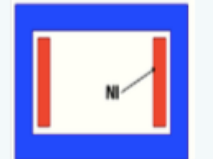
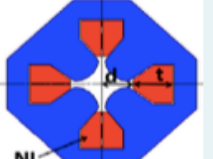
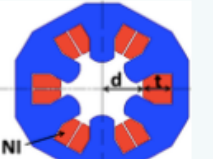


Octupole
 $|B|=1/6 \cdot B''' \cdot r^3$



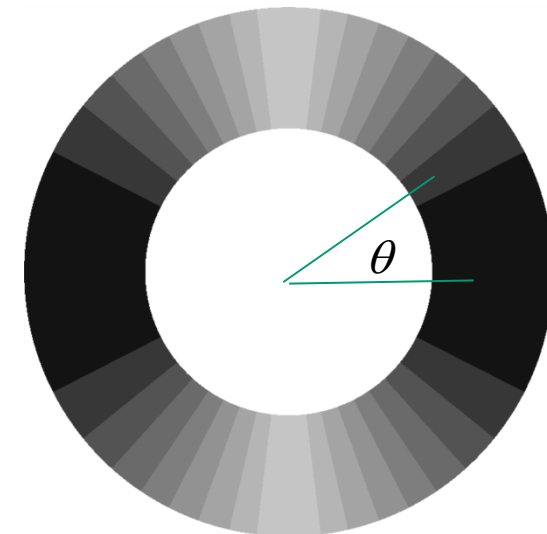
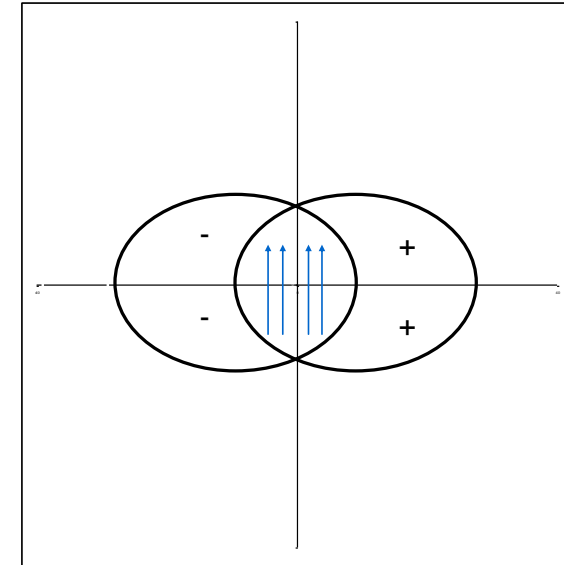
SKREW : horizontal field on mid-plane

Basic resistive magnet types

Magnet	Pole shape	Transfer function
 <p> w : pole width g : vertical gap </p>	parallel	$B = \mu_0 NI / g$
 <p> w : pole width g : vertical gap </p>	parallel	$B = \mu_0 NI / g$
 <p> w : pole width g : pole gap t : coil width total ampere-turns = $2NI$ </p>	parallel	$B = \mu_0 NI / g$
 <p> w : pole width g : pole gap t : coil width </p>	parallel	$B = \mu_0 NI / g$
 <p> R : aperture radius d : coil distance t : coil width </p>	$2xy = R^2$	$B(r) = G \cdot r$ $G = 2\mu_0 NI / R^2$
 <p> R : aperture radius d : coil distance t : coil width </p>	$3x^2y - y^3 = R^3$	$B(r) = S \cdot r^2 = \frac{1}{2} B'' \cdot r^2$ $S = 3\mu_0 NI / R^3$

“Free” Coils for generating the Perfect Dipole Field

- Used for magnets where the field is fully determined by the coil only (not by the poles), mostly the case for superconducting magnets
- Conductors 2 solid Intersecting ellipses (or circles)
 - A uniform, opposite polarity, current density in the area of two intersecting ellipses produces a pure dipolar field, but:
 - The aperture is not circular
 - Not easy to simulate with a flat cable
- Thick conductor shell with a $\cos\theta$ current distribution
 - Pure dipolar field
 - Easier to reproduce with a flat rectangular cable



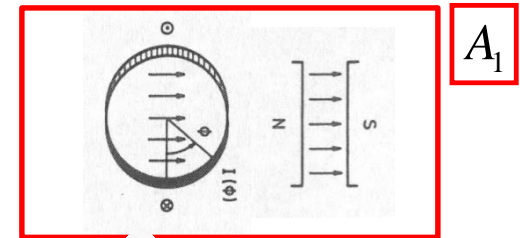
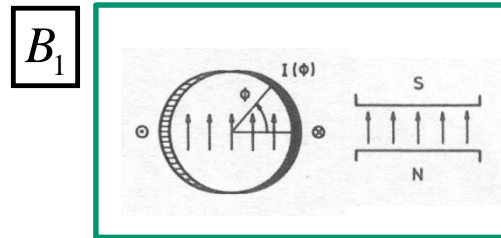
Magnet types and higher orders

a “pure” multipolar field can be generated by a specific coil geometry

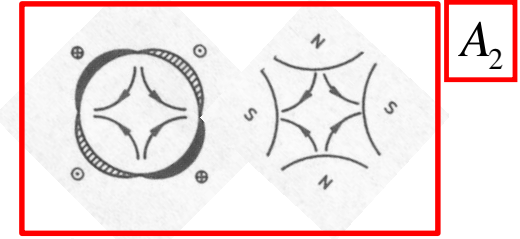
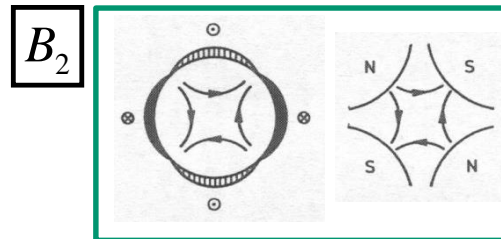
normal

skew

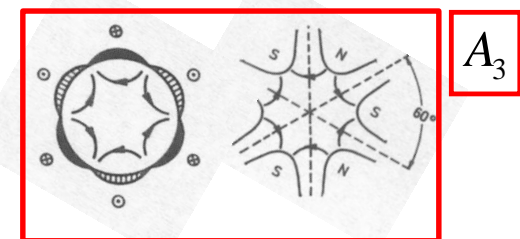
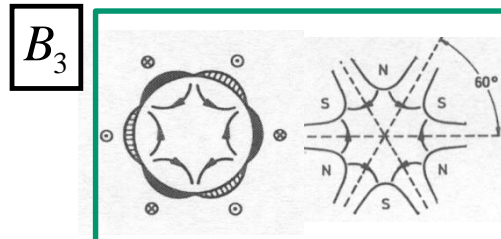
dipole $n=1$



quadrupole $n=2$

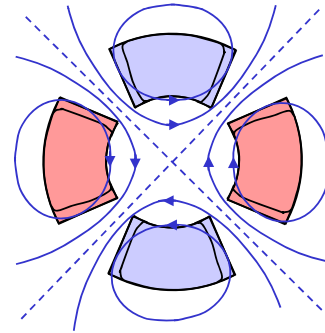
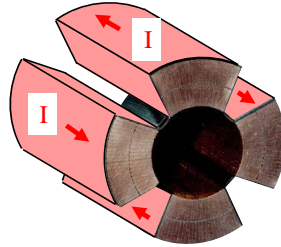
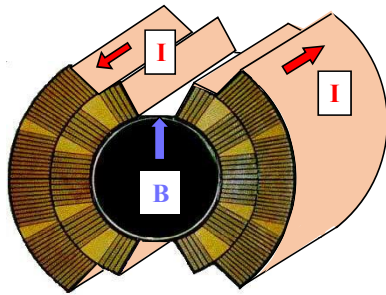


sextupole $n=3$

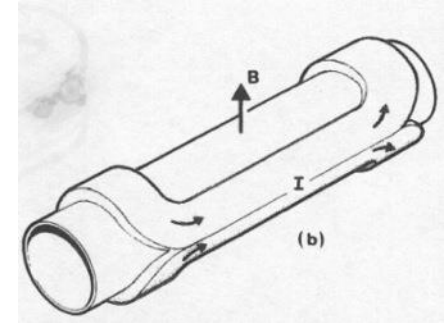


What is specific about sc accelerator magnets ?

- Cylindrical volume with perpendicular field
- Dipoles, quadrupoles, etc

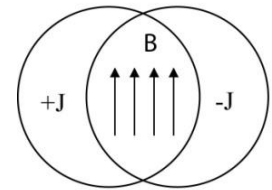


CosΘ coil : $J = J_0 \cos\Theta$



Artist view of a dipole, from M. N. Wilson « Superconducting Magnets »

- Field quality: $\frac{DB_z}{|B|} \leq \text{few} \cdot 10^{-4}$



- Field quality formulated and measured in a multipole expansion,

$$B_y + iB_x = 10^{-4} B_1 \sum_{n=1}^{\infty} (b_n + ia_n) \left(\frac{x + iy}{R_{ref}} \right)^{n-1} \quad b_n, a_n \in \text{few} \times \text{units}$$

- Long magnets: dipoles from 6 m (Tevatron) to 15 m (LHC)
- Often magnets are bend (9.14 mm sagitta for the LHC dipoles)



Resistive magnets

Also called: Classical magnets, Iron dominated magnets



Practical resistive magnet design & manufacturing

Steps in the process:

1. Specification
2. Conceptual design
3. Raw materials choice
4. Detailed design
 1. Coil cross-section geometry: cooling
 2. Yoke shape, pole shape: FE model optimization
 3. Yoke ends, coil ends design
5. Yoke manufacturing, tolerances, alignment, structure
6. Coil manufacturing, insulation, impregnation type
7. Magnetic field measurements



Specification

Before you start designing you need to get from the accelerator designers:

- B(T) or G (T/m) (higher orders: G_3 (T/m²), etc)
- Magnet type: C-type, H-type, DC (slow ramp) or AC (fast ramp)
- Aperture:
 - Dipole : “good field region“ → airgap height and width
 - quads and higher order: “good field region“ → aperture inscribed circle
- Magnetic length and estimated real length
- Current range of the power convertor (and the voltage range: watch out for the cables)
- Field quality:
$$\text{dipole: } \frac{\Delta B}{B} \text{ (ref volume),} \quad \text{quadrupole: } \frac{\Delta G}{G} \text{ (reference circle)}$$

$$\text{or } b_n, a_n \text{ for } n = 1, 2, 3, 4, 5, \dots$$
- Cooling type: air, water (P_{\max} , Δp_{\max} and Q_{\max} (l/min))
- Jacks and Alignment features
- Vacuum chamber to be used → fixations, bake-out specifics

These need careful negotiation and often iteration after conceptual (and detailed) design

Conceptual design

- From B and l you get NI (A)

$$NI = \frac{l_{airgap} B}{\mu_0}$$

- From NI (A) and the power convertor I_{max} you get N

- Then you decide on a coil X-section using:

$$j_{coil} = 5 \text{ A/mm}^2 \text{ for water cooled}$$

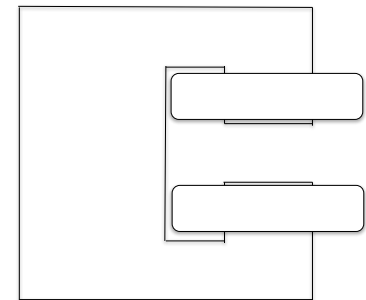
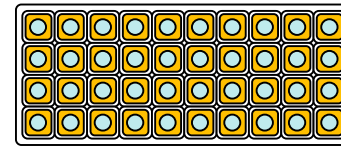
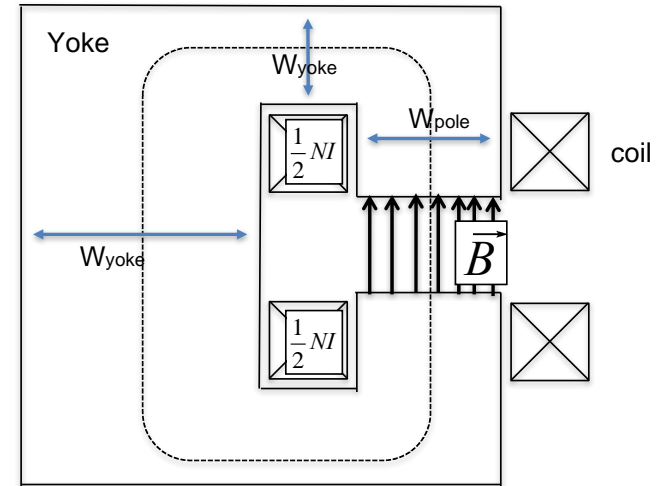
$$\text{or } j_{coil} = 1 \text{ A/mm}^2 \text{ for air cooled}$$

- This defines the coil cavity in the yoke (you add 0.5 mm insulation around each conductor and 1 mm ground insulation around the coil) and select the best fitting rectangular

- You can the draw the draft X-section using:

$$W_{yoke} = W_{pole} \frac{B}{B_{sat}} \text{ with } 1.5 T < B_{sat} < 2 T$$

- Decide on the coil ends: racetrack, bedstead
- You now have the rough magnet cross section and envelope





Power and cooling

Power generated by coil

- DC: from the length of the conductor $N \cdot L_{turn}$, the cross section σ and the specific resistivity ρ of the material one gets the spent Power in the coil

$$P/l[W/m] = \frac{\rho}{S} I^2 \quad \text{with:} \quad \begin{aligned} \rho_{Cu} &= 1.72(1 + 0.0039(T - 20))10^{-8}\Omega m \\ \rho_{Al} &= 2.65(1 + 0.0039(T - 20))10^{-8}\Omega m \end{aligned}$$

- For pulsed magnets: take the average I^2 for the duty cycle

Coil Cooling

- ΔT (entrance-exit of the coil) is usually chosen as 20°C or 30°C depending on the $T_{cooling\ water}$
- The cooling water needs to be in moderately turbulent regime (with laminar flow the flow speed is zero on the wall !) (*Reynolds* > 2000)
- In general a few bars (eg. 4 bar) pressure drop is chosen



Theoretical pole shapes

The ideal poles for dipole, quadrupole, sextupole, etc. are lines of constant scalar potential

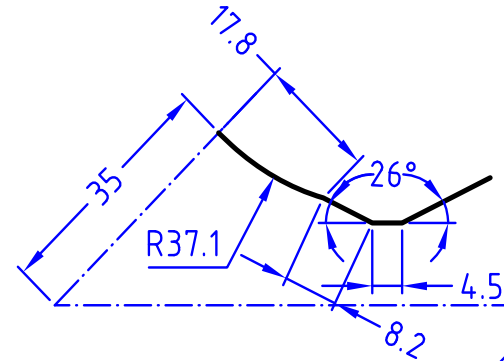
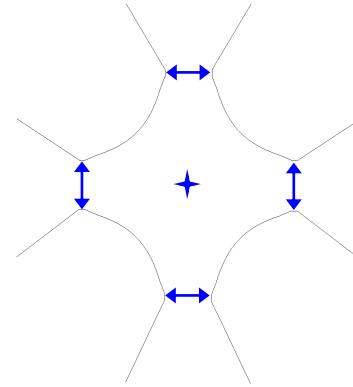
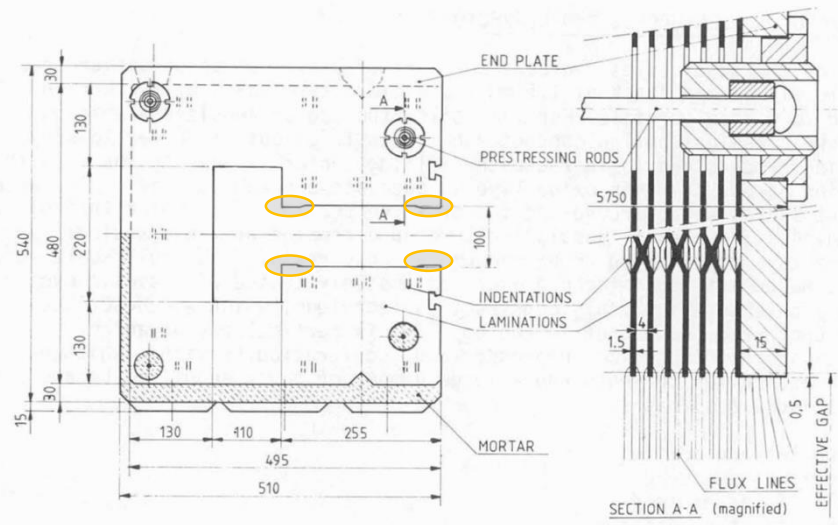
Dipole $y = \pm h/2$ straight line

quadrupole $2xy = \pm r^2$ hyperbola

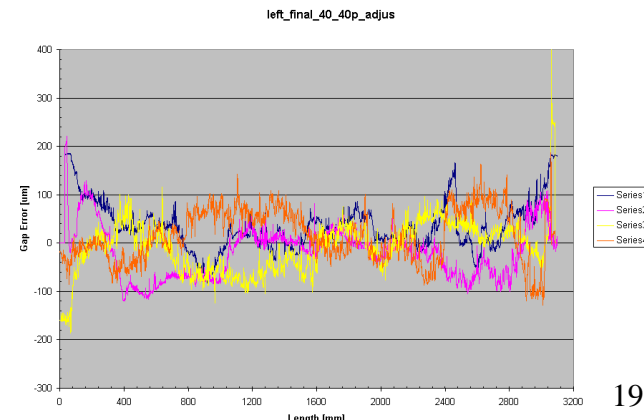
sextupole $3x^2y - y^3 = \pm r^3$

Practical pole shapes: shims and alignment features

- Dipole example: below a lamination of the LEP main bending magnets, with the pole shims well visible



- Quadrupoles: at the edge of the pole one can put a combination a shim and alignment feature (examples: LHC-MQW, SESAME quads, etc)
- This then also allows to measure the pole distances : special instrumentation can be made for this





Finite Element electromagnetic models

- Aim of the electromagnetic FE models:
 - The exact shape of the yoke needs to be designed
 - Optimize field quality: adjust pole shape, minimize high saturation zones
 - Minimize the total steel amount (magnet weight, raw material cost)
 - Calculate the field: needed for the optics and dynamic aperture modelling
 - transfer function $B_{xsection}(l)$, $\int B dl$, magnetic length
 - multipoles (in the centre of the magnet and integrated) b_n and a_n
- Some Electromagnetic FE software packages that are often used:
 - **Opera** from Cobham: 2D and 3D commercial software see: <http://operafea.com/>
 - “Good old” **Poisson**, 2D: now distributed by LANL-LAACG see: http://laacg.lanl.gov/laacg/services/download_sf.phtml
 - **ROXIE** (CERN) 2D and 3D, specialized for accelerator magnets; single fee license for labs & universities see: <https://espace.cern.ch/roxie/default.aspx>
 - **ANSYS Maxwell**: 2D and 3D commercial software see: <http://www.ansys.com/Products/Electronics/ANSYS-Maxwell>



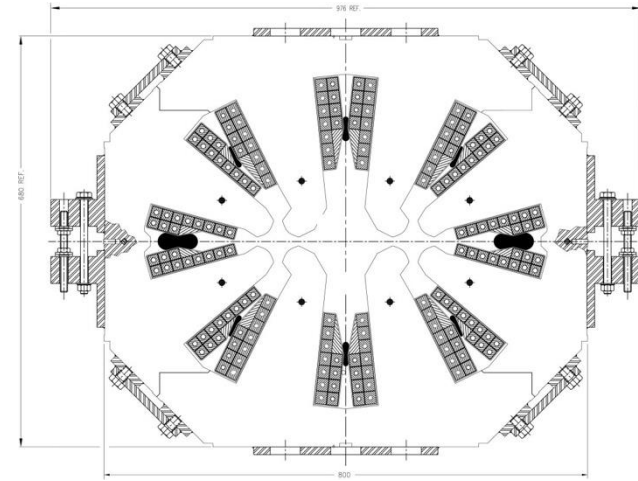
Yoke shape, pole shape: FE model optimization

Use symmetry and the thus appropriate boundary conditions to model only $\frac{1}{4}$ th (dipoles, quadrupoles) or even $\frac{1}{6}$ th sextupoles.

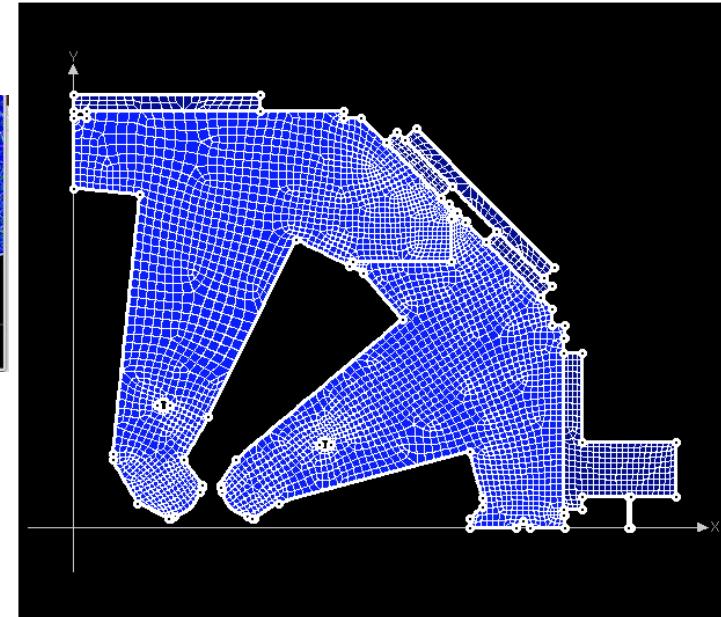
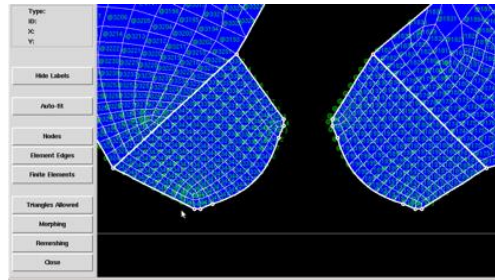
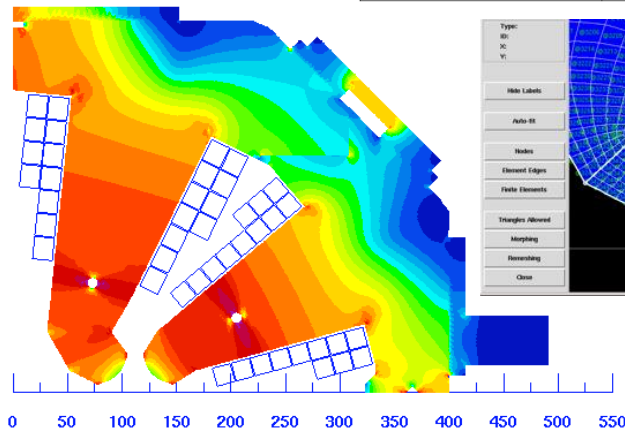
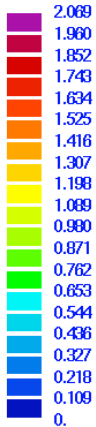
Meshing needs attention in the detailed areas like poles, slits, etc

Table 8.6: Main parameters of the MQW normal conducting quadrupole magnet

Magnet type	MQWA	MQWB
Magnetic length		3.1 m
Beam separation		224 mm
Aperture diameter		46 mm
Operating temperature		< 65° C
Nominal gradient	35 T/m	30 T/m
Nominal current	710 A	600 A
Inductance		28 mH
Resistance		37 mΩ
Conductor X-section	20.5 x 18.0 mm ² inner poles 17.0 x 17.0 mm ² outer poles	
Cooling hole diameter	7 mm inner poles, 8 mm outer poles	
Number of turns per magnet	8 x 11	
Minimum water flow	28 l/min	
Dissipated power at I _{nom}	19 kW	14 kW
Mass	11700 kg	



|Btot| (T)





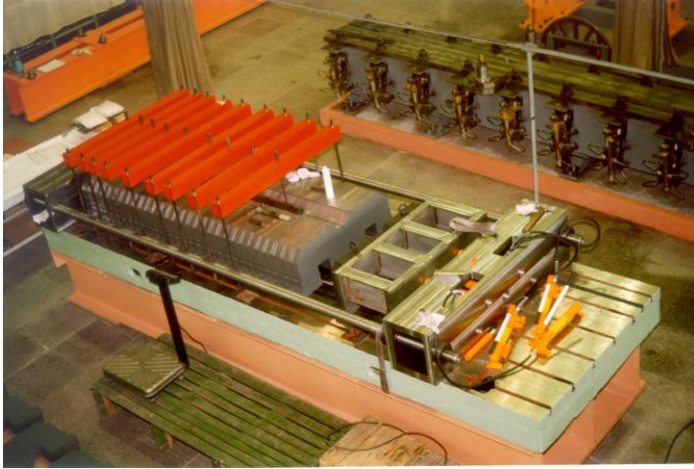
Yoke manufacturing

- Yokes are nearly always laminated to reduce eddy currents during ramping
- Laminations can be coated with an inorganic (oxidation, phosphating, Carlite) or organic (epoxy) layer to increase the resistance
- Magnetic properties: depend on chemical composition + temperature and mechanical history
- Important parameters: coercive field H_c and the saturation induction.
 - H_c has an impact on the remnant field at low current
 - $H_c < 80$ A/m typical or $H_c < 20$ A/m for magnets at low field ($B < 0.05$ T)
- low carbon steel (C content $< 0.006\%$) is best for higher fields $B > 1$ T
- Yokes are either :
 - Glued , using epoxy coated laminations
 - Welded, full length plates are welded on the outside
 - Compressed by tie rods in holesor a combination of all these
- To be able to keep the yoke (or yoke stack) stable you probably need end plates (can range from ± 1 cm to 5 cm depending on the size)
- The end plates have pole chamfers and often carry end shims



Yoke manufacturing

Stacking an MBW dipole yoke stack



Double aperture LHC quad. MQW
Stacking on a precision table



Welding the structural plates



Half magnet handling



Glued yoke (MCIA LHC TL)



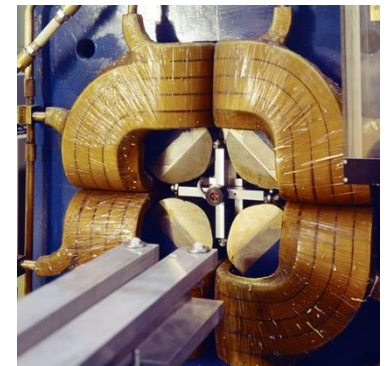
Coil manufacturing, insulation, impregnation type

- Winding Cu conductors is an well established technique
- When the Cu conductor is thick it is best to use “dead soft” Cu (T treatment)
- Insulation of the coil
 - Glass fibre – epoxy impregnated
 - Individual conductor 0.5 mm glass fibre, 0.25 mm tape wound half lapped
 - Impregnated with radiation resistant epoxy, total glass volume ratio >50%
 - For thin conductors: Cu enamel coated, possibly epoxy impregnated afterwards

For dipoles some main types are racetrack or bedstead



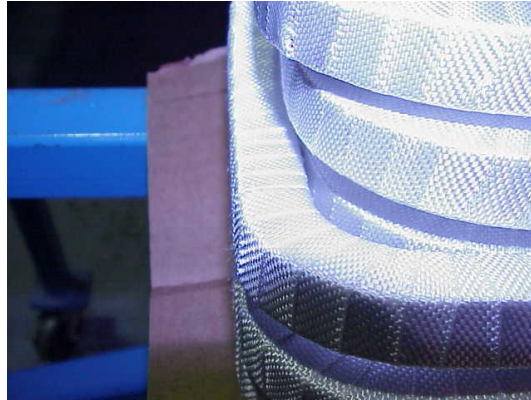
Quadrupoles





Coil manufacturing

MQW Glass fibre tape wrapping.



Winding the hollow Cu conductor



coil electrical test (under water !)



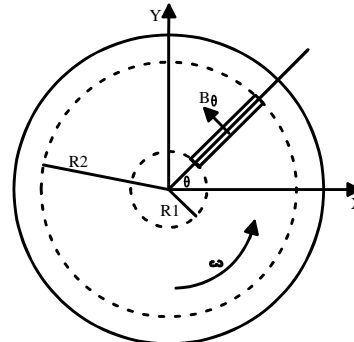
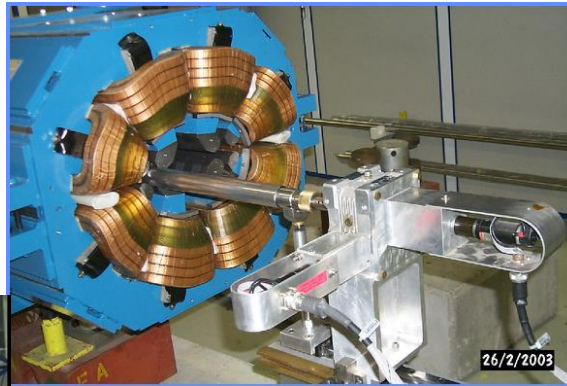
Finished MBXW coil



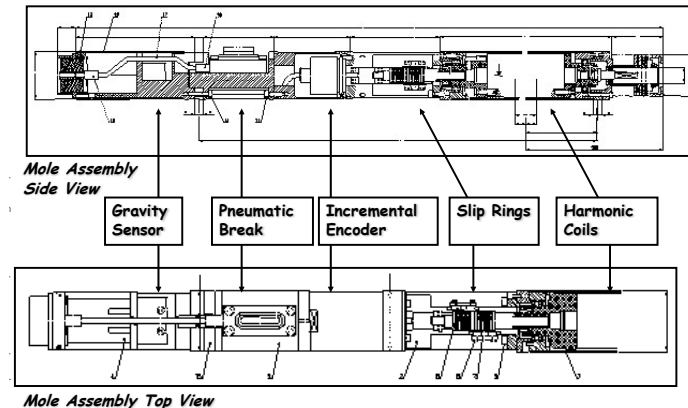
Magnetic field measurements

Several Magnetic Measurements techniques can be applied, e.g.:

- Rotating coils: multipoles and integrated field or gradient in all magnets
- Stretched wire: magnetic centre and integrated gradient for $n > 1$ magnets
- Hall probes: field map
- Pickup coils: field on a current ramp
- Example below : MQW : double aperture quadrupole for the LHC.



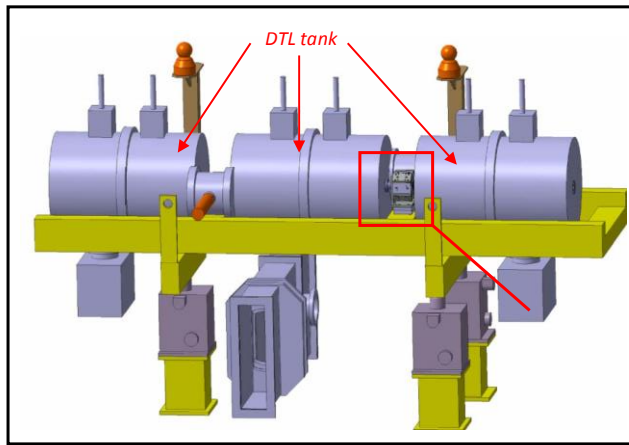
Rotating radial coil



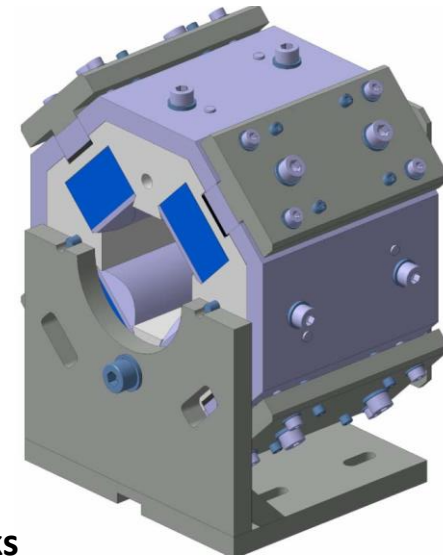
Mole Assembly Top View

Permanent magnets

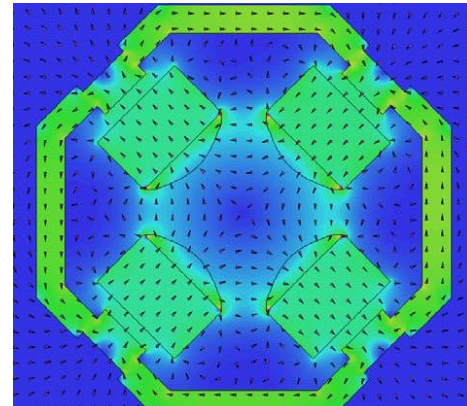
Linac4 @ CERN permanent magnets , quadrupoles



Pictured : Cell-Coupled Drift Tube Linac module.



- Permanent magnet because of space between DTL tanks
- $\text{Sm}_2\text{Co}_{17}$ permanent magnets
- Integrated gradient of 1.3 to 1.6 Tesla
- 15 magnets
- Magnet length 0.100 m
- Field quality/amplitude tuning blocks



Courtesy D. Tommasini, CERN

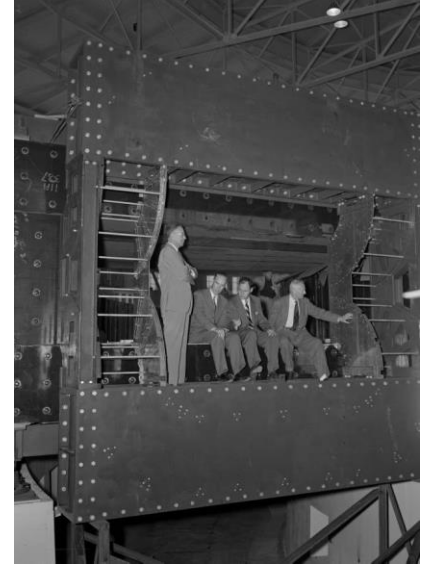
Examples of resistive magnets;

Some history, some modern regular magnets and some special cases

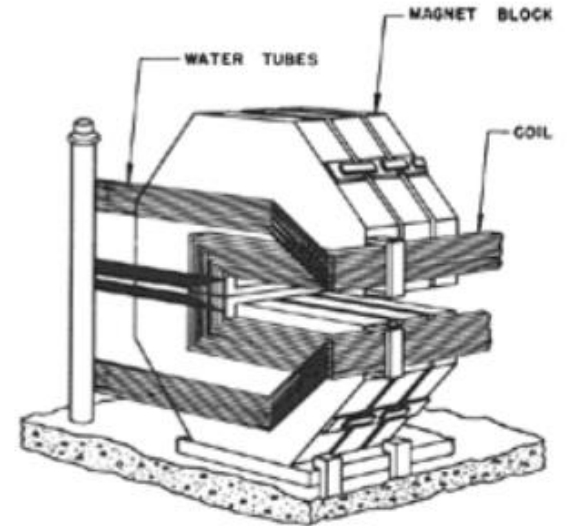
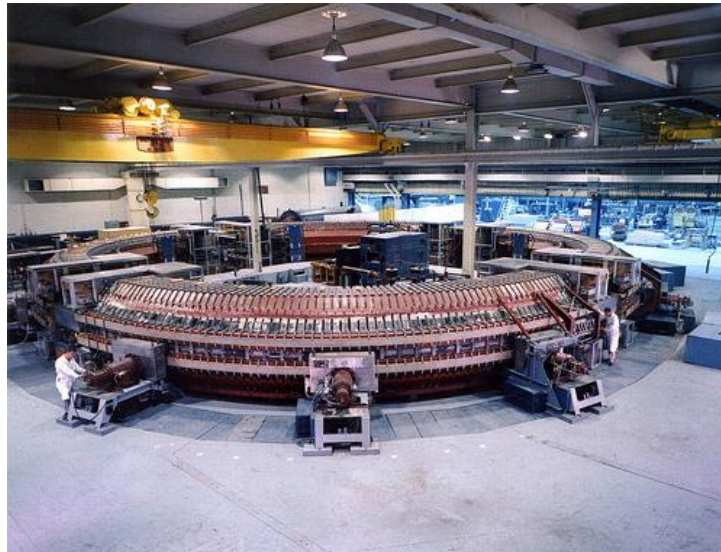


Some early magnets (early 1950-ies)

Bevatron
(Berkeley)
1954, 6.2 GeV



Cosmotron
(Brookhaven)
1953, 3.3 GeV
Aperture:
20 cm x 60 cm



CAS Basics, Chavannee-de-Bogis, 7-Febr-2017, Magnets, GdR

Magnetic field:

at injection

147 G

for 24.3 GeV

1.2 T

maximum

1.4 T

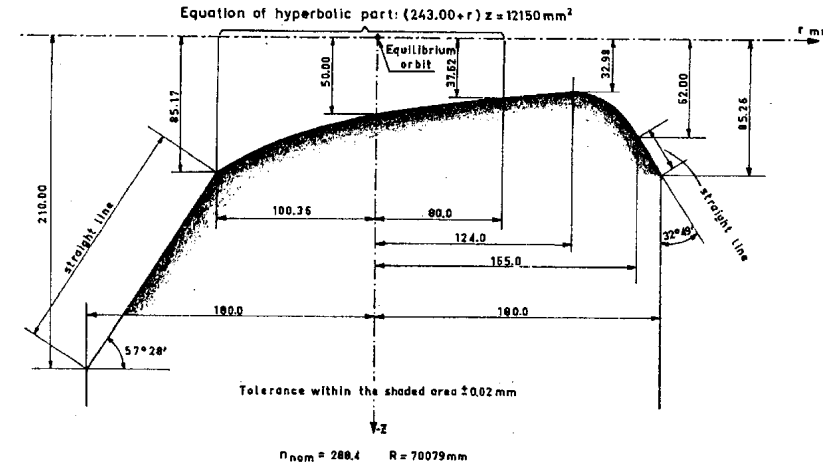
Weight of one magnet unit

38 t

Gradient @ 1.2 T : 5 T/m

Equipped with pole-face windings for higher order corrections

Water cooled Al race-track coils



FINAL POLE PROFILE.

Fig. 9: Final pole profile.

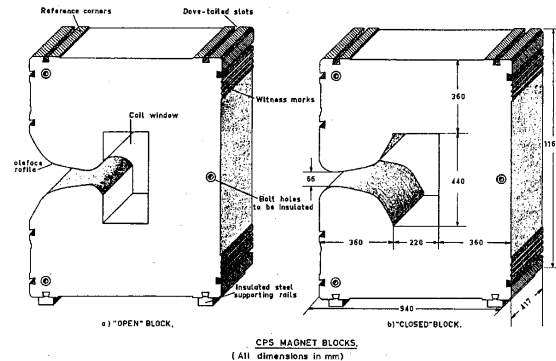
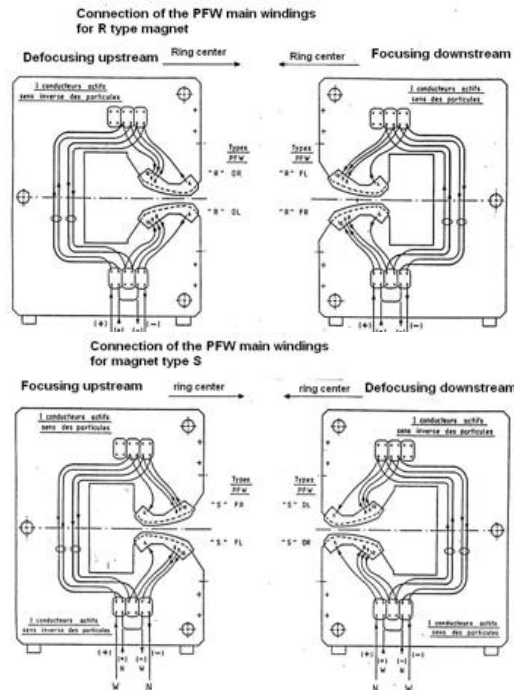


Fig. 12: Final design of the magnet blocks.



dipole magnet : SPS dipole

H magnet type MBB

$B = 2.05 \text{ T}$

Coil : 16 turns

$I_{max} = 4900 \text{ A}$

Aperture = $52 \times 92 \text{ mm}^2$

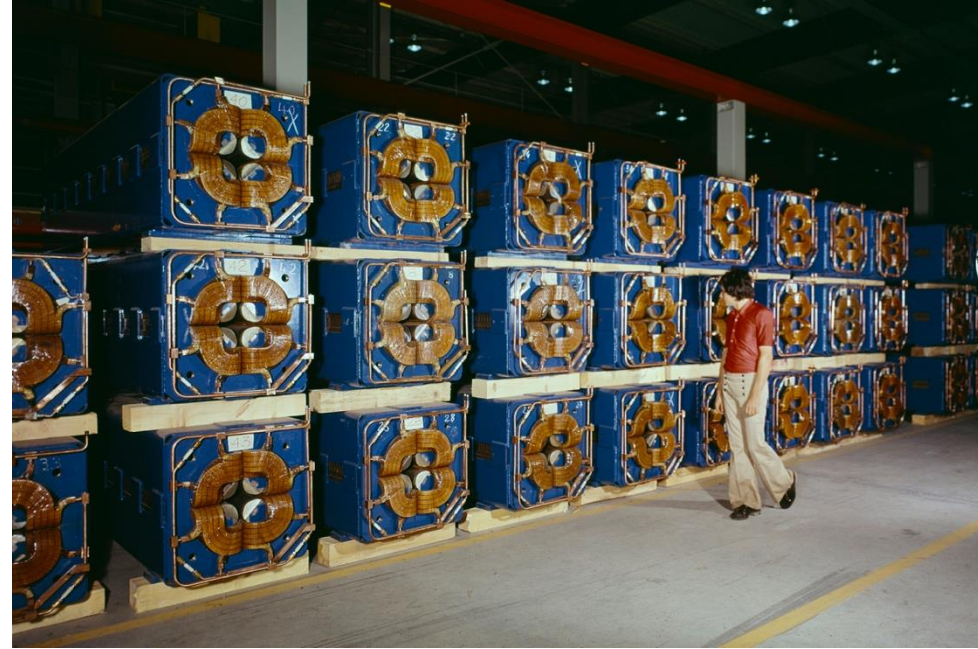
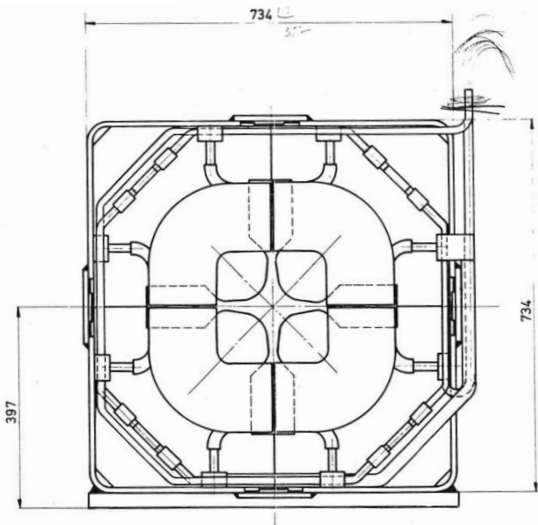
$L = 6.26 \text{ m}$

Weight = 17 t





Quadrupole magnet : SPS quadrupole



type MQ

$G = 20.7 \text{ T/m}$

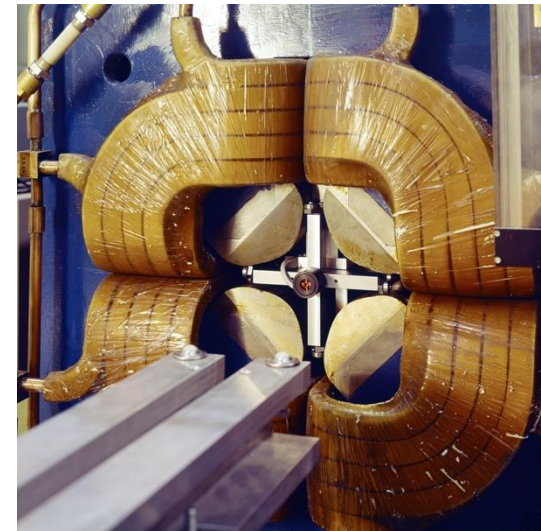
Coil : 16 turns

$I_{max} = 1938 \text{ A}$

Aperture inscribed radius = 44 mm

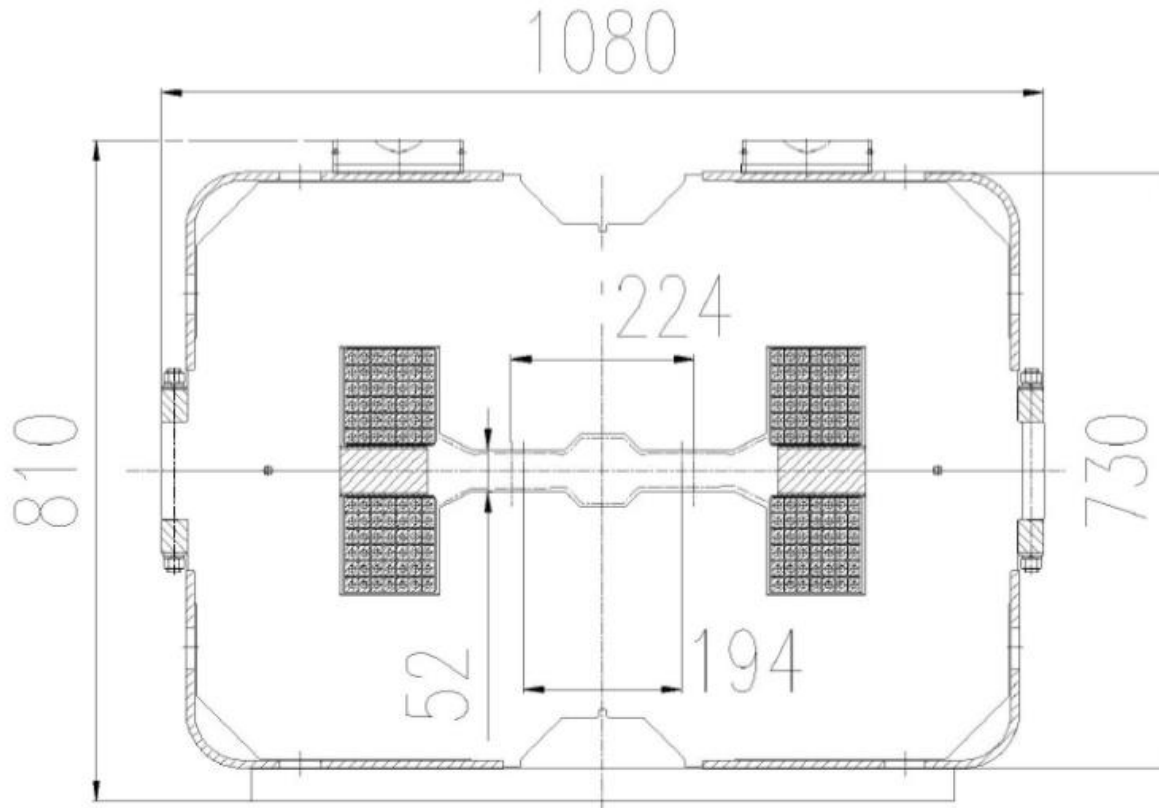
$L_{coil} = 3.2 \text{ m}$

Weight = 8.4 t

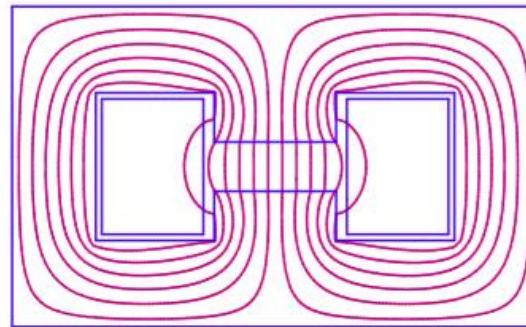
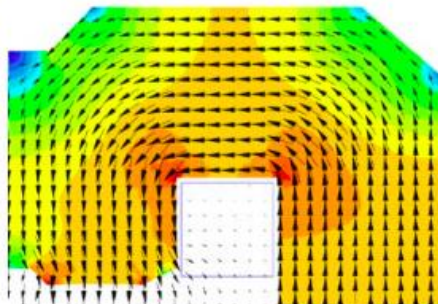
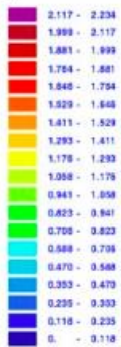




MBW LHC warm separation dipole (1)

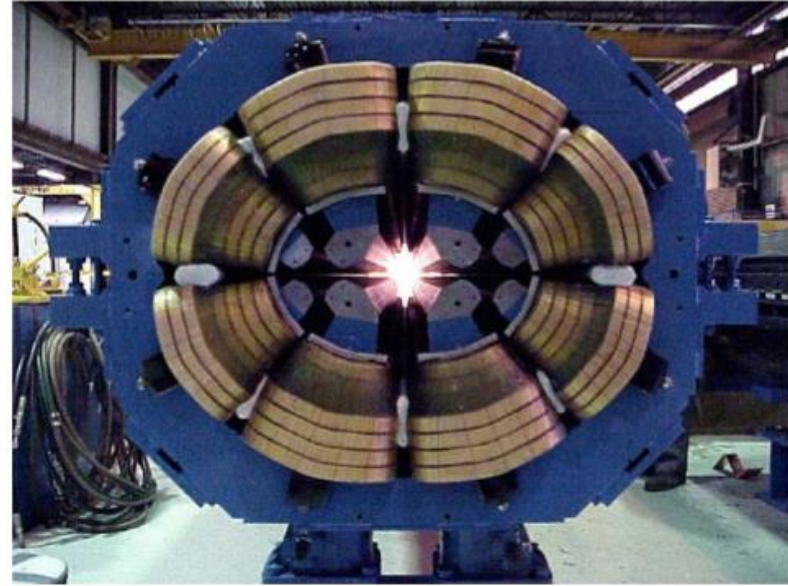
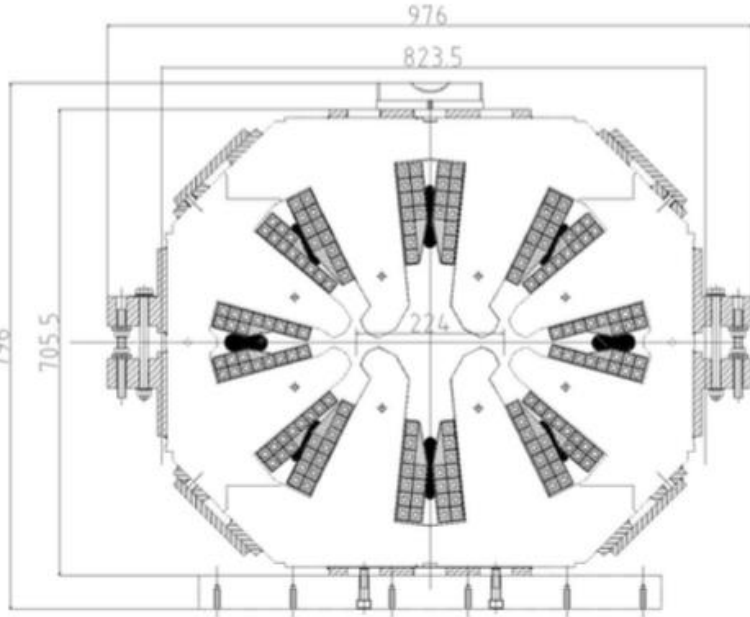


Parameter	Value
Aperture	52 mm
Nominal field	1.42 T
Magnetic length	3.4 m
Weight	18 t
Water flow	19 l/min
Power	29 kW





MQW: LHC warm double aperture quadrupole



CAS Basics, Chavannee-de-Bogis, 7-Febr-2017, Magnets, GdR

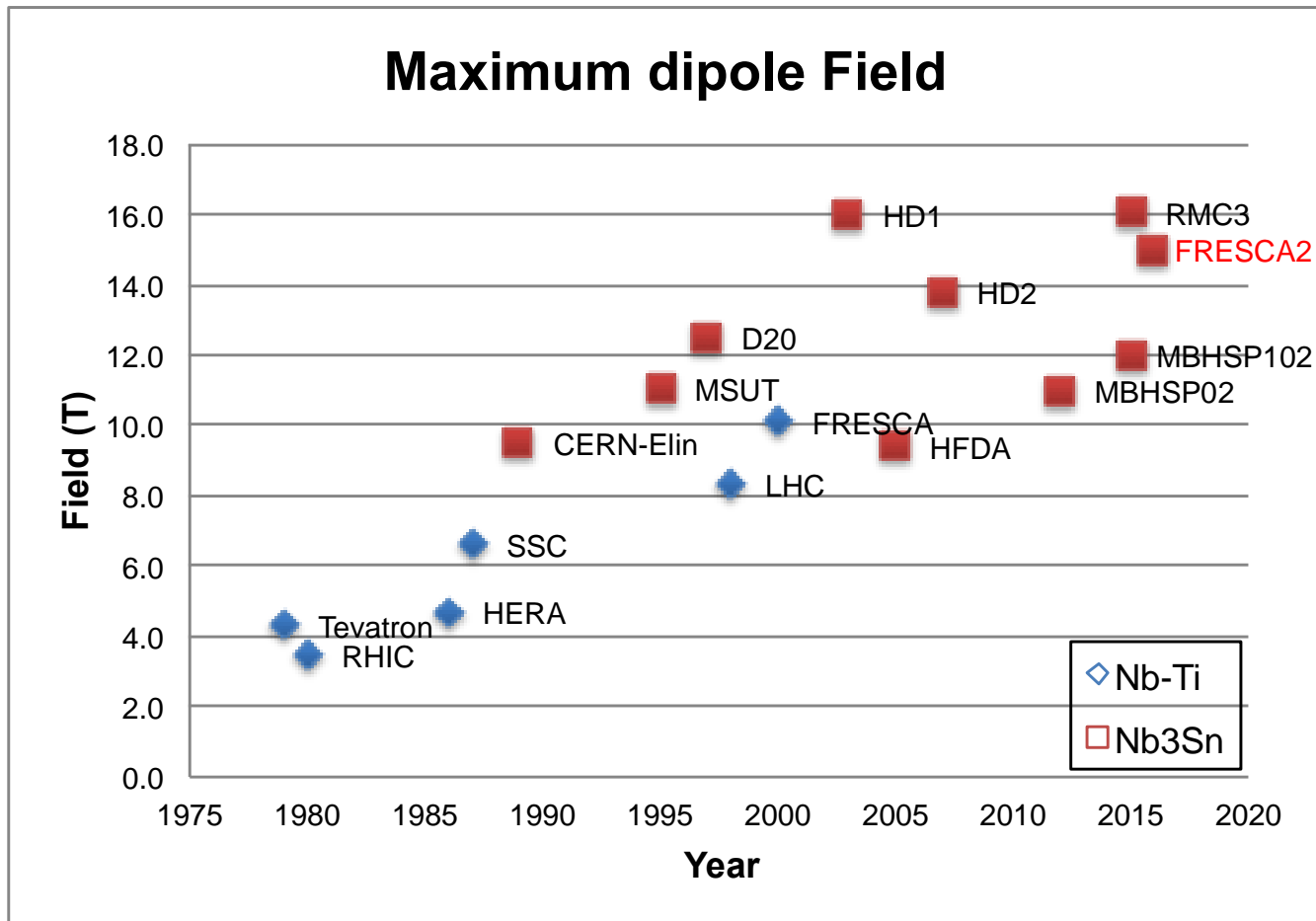


Superconducting magnets



Superconducting accelerators magnets; the state of the art

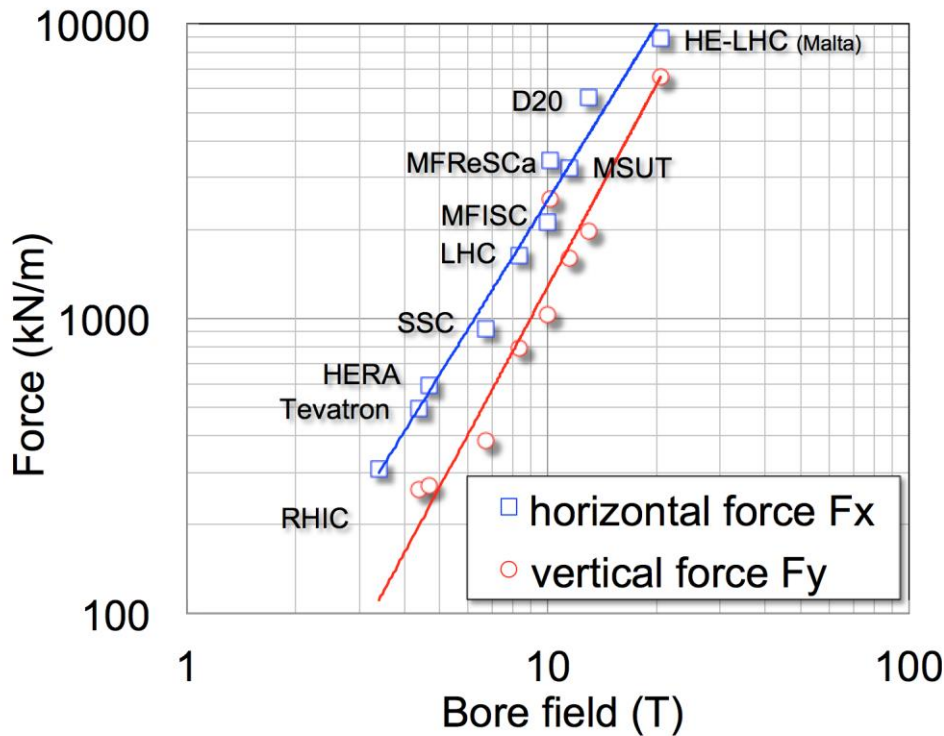
- Maximum attainable field slowly approaches 16 T
 - 20% margin needed (80% on the load line):
for a 16 T nominal field we need to design for 20 T



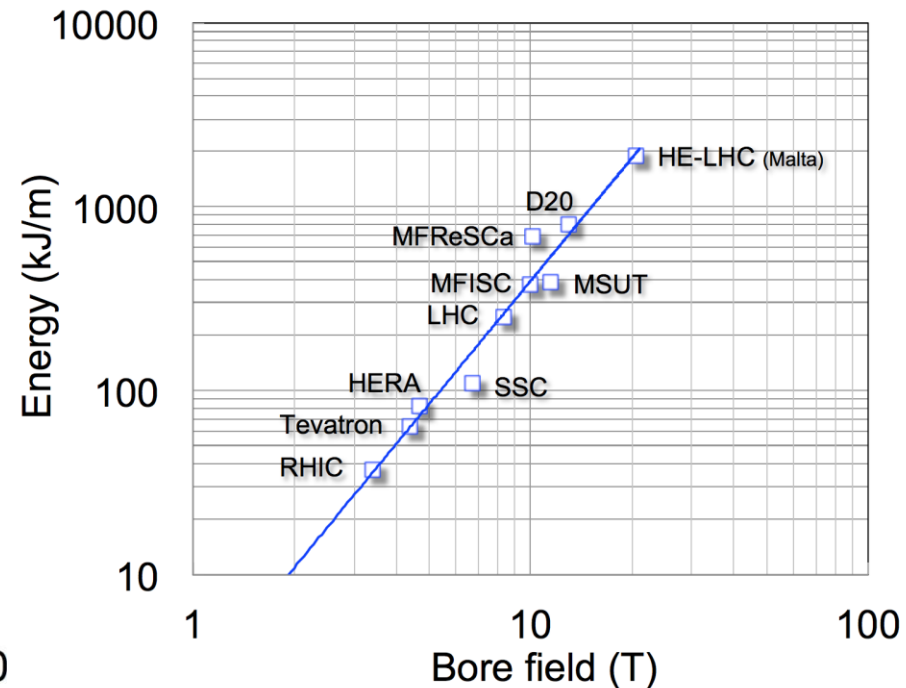


Forces and Stored Energy

Scaling of **forces** on coil quadrant vs. Field, for recent production and R&D dipoles



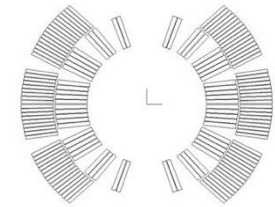
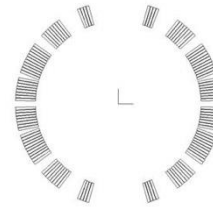
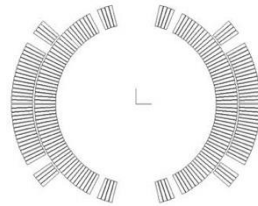
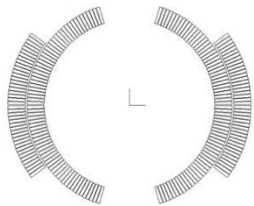
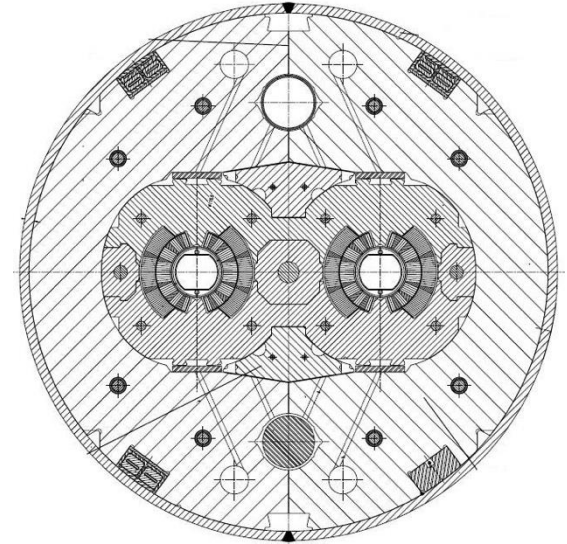
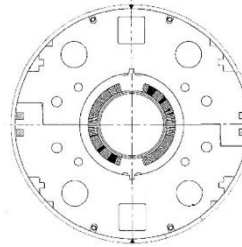
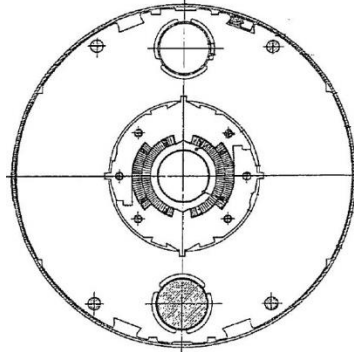
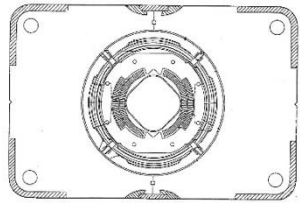
Scaling of the **stored energy** per unit length of magnet vs. Field, for recent production and R&D dipoles



The electromagnetic loads in a 20 T dipole would be a factor 5 to 8 larger than in the LHC dipoles



Existing Superconducting Accelerator dipole magnets (1)



Tevatron

HERA

RHIC

LHC

76 mm bore

$B = 4.4 \text{ T}$

$T = 4.2 \text{ K}$

first beam 1983

75 mm bore

$B = 5.0 \text{ T}$

$T = 4.5 \text{ K}$

first beam 1991

80 mm bore

$B = 3.5 \text{ T}$

$T = 4.3\text{-}4.6 \text{ K}$

first beam 2000

56 mm bore

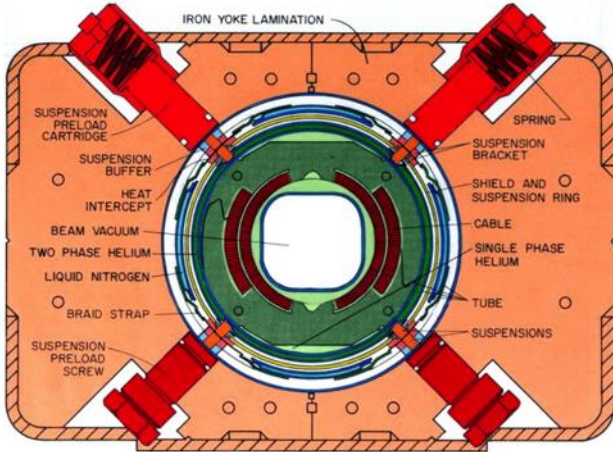
$B = 8.34 \text{ T}$

$T = 1.9 \text{ K}$

first beam 2008

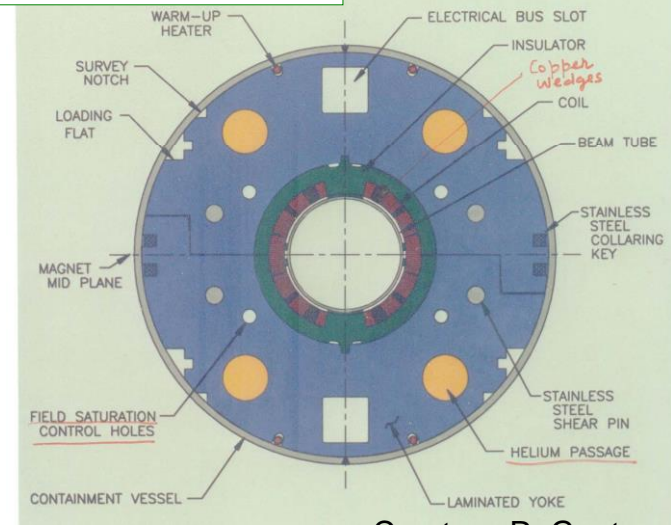


Existing Superconducting Accelerator dipole magnets (2)



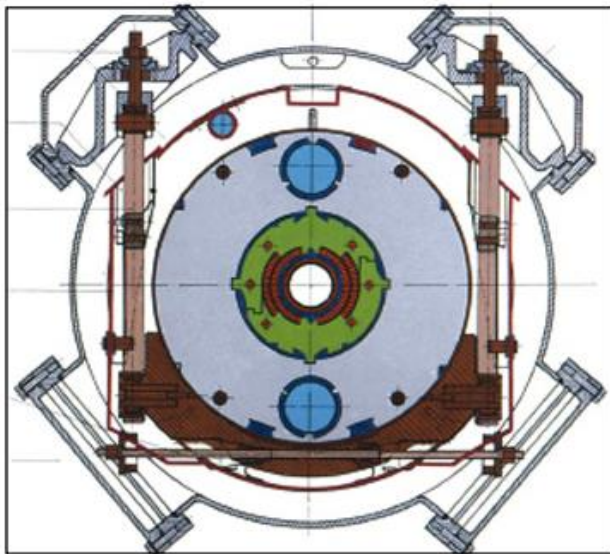
Tevatron: 4.4 T
1983

RHIC: Relativistic Heavy Ion Collider



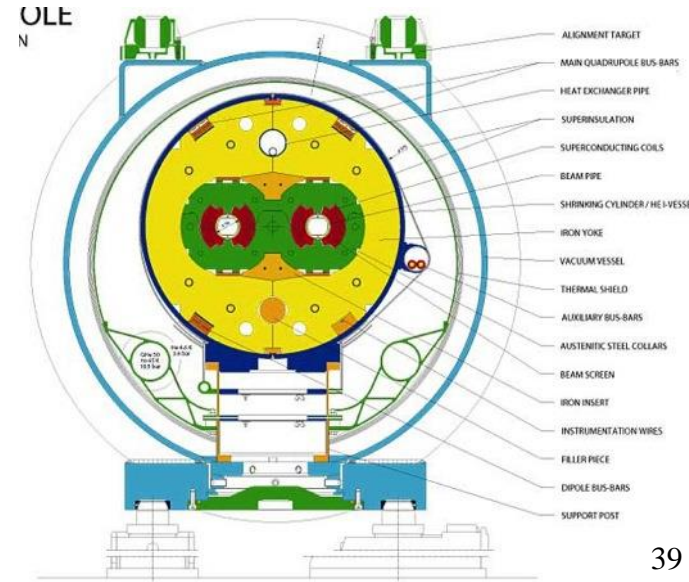
Courtesy R. Gupta

RHIC: 3.5 T
2000



HERA: 5 T
1992

LHC: 8.34 T
2008



CAS Basics, Chavannee-de-Bogis, 7-Febr-2017, Magnets, GdR

Type II Superconductors

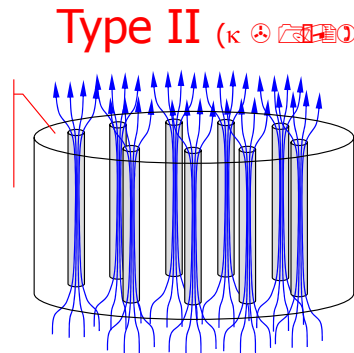
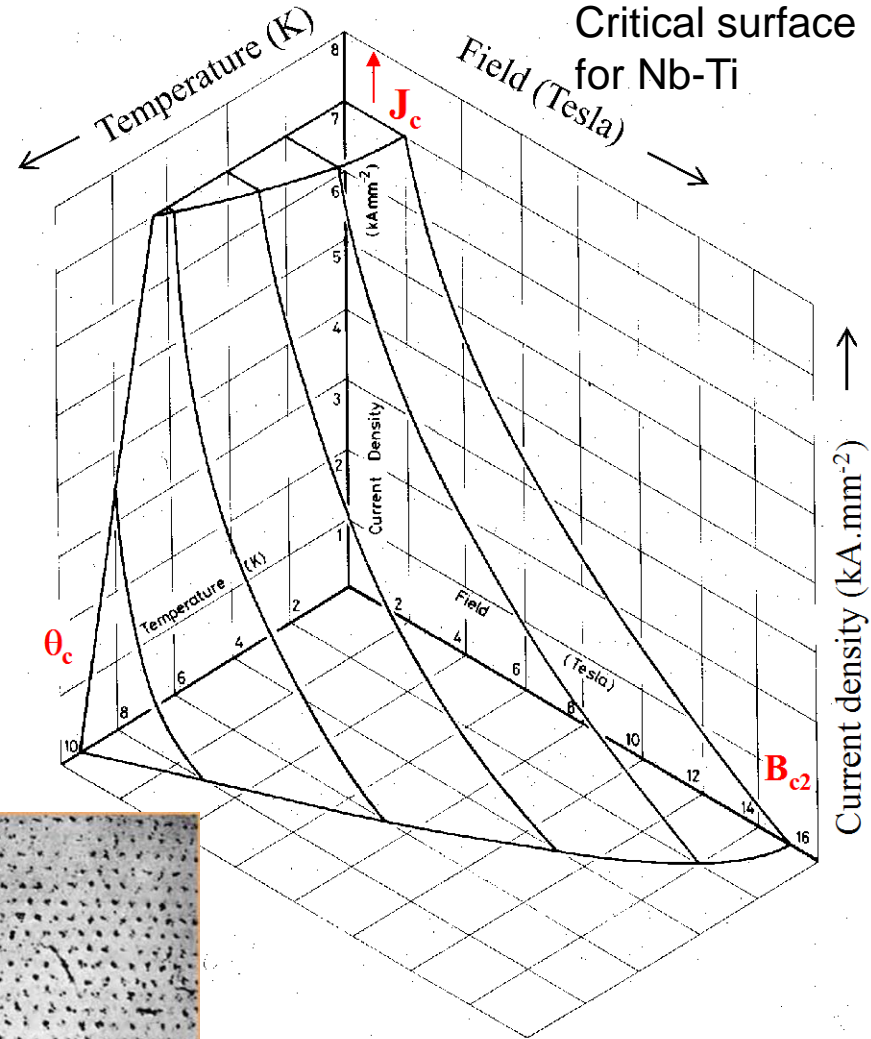
Below a the critical surface the material is “superconducting”. Above the surface it is “normal conducting”

- θ_c Critical Temperature (at zero field and current density)
- B_{c2} Critical Field (at zero temperature and current density)
- J_c Critical Current Density (at zero temperature and field)

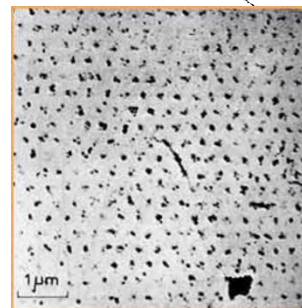
The Critical surface depends on the material type Nb-Ti, Nb₃Sn, etc) and the processing

Superconducting means: $R = 0$

J_c : few $\times 10^3$ A/mm² inside the superconductor



Courtesy L. Bottura



Quantized fluxoids in a superconductor

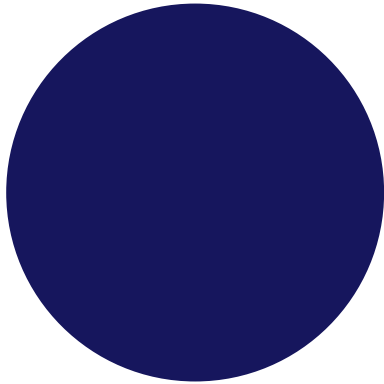
Courtesy M. Wilson



Superconductivity

Typical operational conditions (0.85 mm diameter strand)

Cu

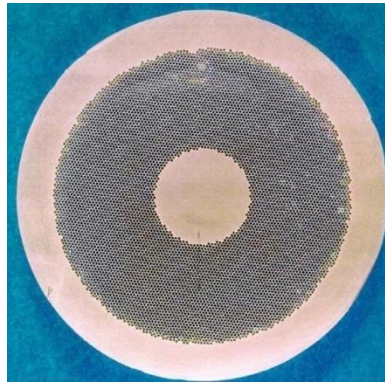


$J \sim 5 \text{ A/mm}^2$

$I \sim 3 \text{ A}$

$B = 2 \text{ T}$

Nb-Ti

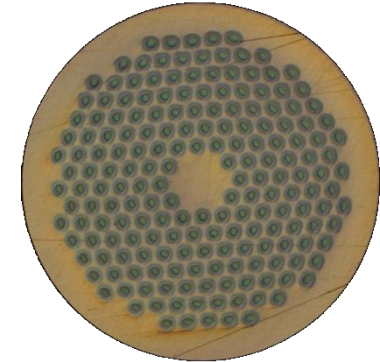


$J \sim 1500\text{-}2000 \text{ A/mm}^2$

$I \sim 400 \text{ A}$

$B = 8\text{-}9 \text{ T}$

Nb₃Sn



$J \sim 1500\text{-}2000 \text{ A/mm}^2$

$I \sim 400 \text{ A}$

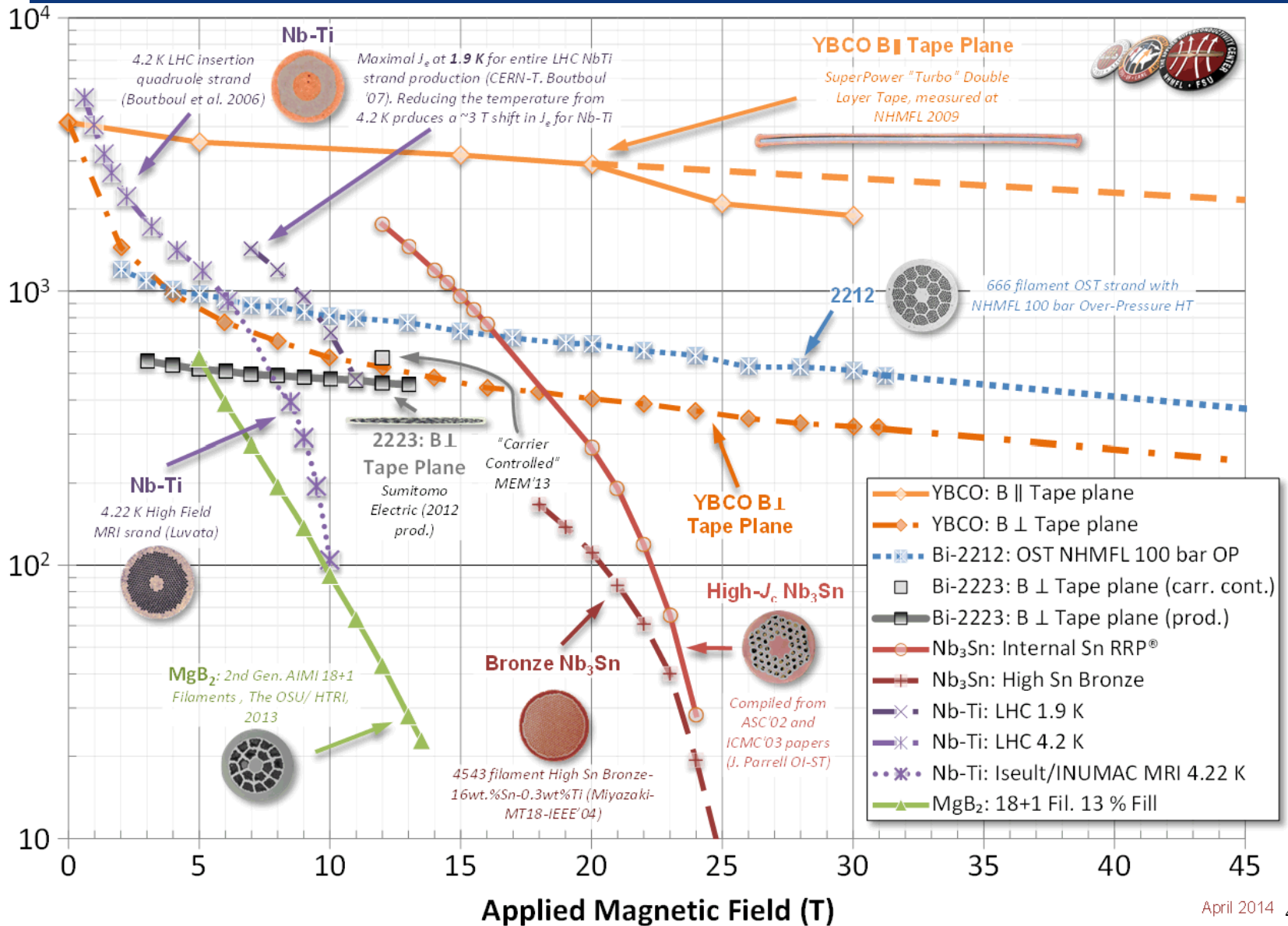
$B = 12\text{-}13\text{-}16 \text{ T}$

- Nb-Ti: ductile alloy: easy to process by extrusion and drawing
- $T < 9 \text{ K}$ it becomes a type II superconductor.
- $T_C \sim 9.2 \text{ K @ } 0 \text{ T}$; $B_{C2} \sim 14.5 \text{ T @ } 0 \text{ K}$
- Cost: appr. 100-150 US\$/kg of wire

- Nb₃Sn: Brittle and strain sensitive
- $T < 18 \text{ K}$ it becomes a type II superconductor.
- $T_C \sim 18 \text{ K @ } 0 \text{ T}$; $B_{C2} \sim 28 \text{ T @ } 0 \text{ K}$
- Cost: appr. 700-1500 US\$/kg of wire

Available Superconductors

Whole Wire Critical Current Density (A/mm^2 , 4.2 K)

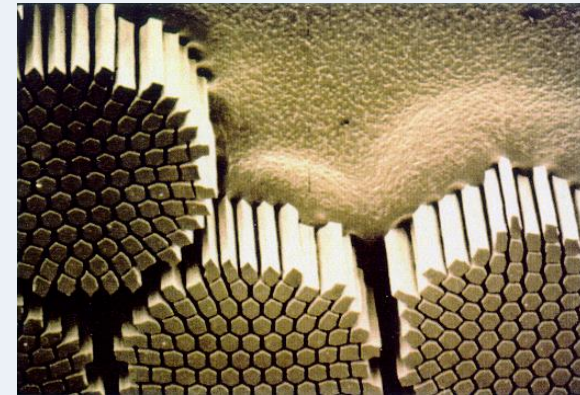
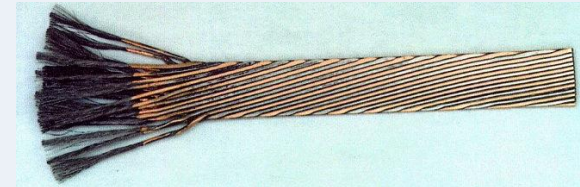


- Nb-Ti is the workhorse for present accelerators, medical magnets, cyclotrons, etc

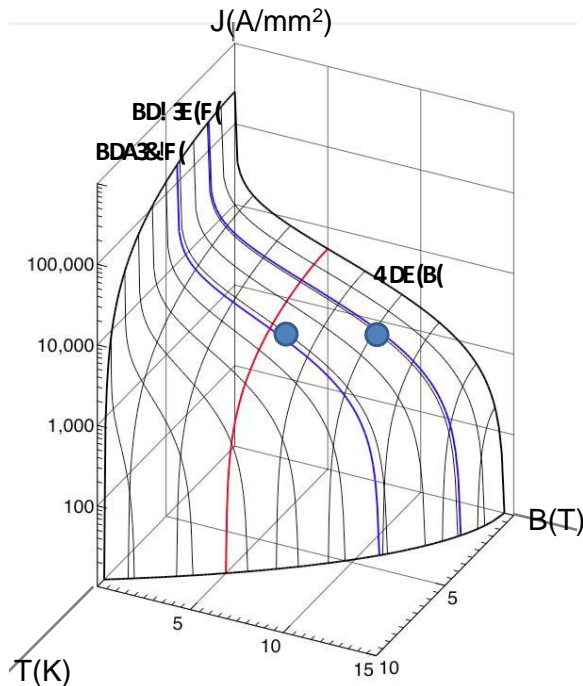
Strands and Cables for LHC Dipole Magnets

Performance specification

STRAND	Type 01	Type 02
Diameter (mm)	1.065	0.825
Cu/NbTi ratio	1.6-1.7 ± 0.03	1.9-2.0 ± 0.03
Filament diameter (µm)	7	6
Number of filaments	8800	6425
Jc (A/mm ²) @1.9 K	1530 @ 10 T	2100 @ 7 T
µ ₀ M (mT) @1.9 K, 0.5 T	30 ± 4.5	23 ± 4.5
CABLE	Type 01	Type 02
Number of strands	28	36
Width (mm)	15.1	15.1
Mid-thickness (mm)	1.900 ± 0.006	1.480 ± 0.006
Keystone angle (degrees)	1.25 ± 0.05	0.90 ± 0.05
Cable Ic (A) @ 1.9 K	13750 @ 10T	12960 @ 7T
Interstrand resistance (µΩ)	10-50	20-80



Cable compaction ~ 91 %

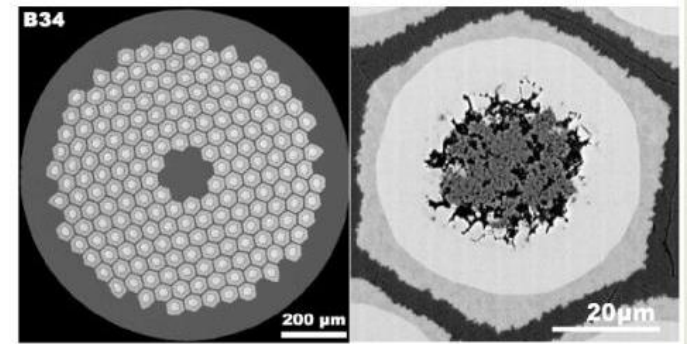
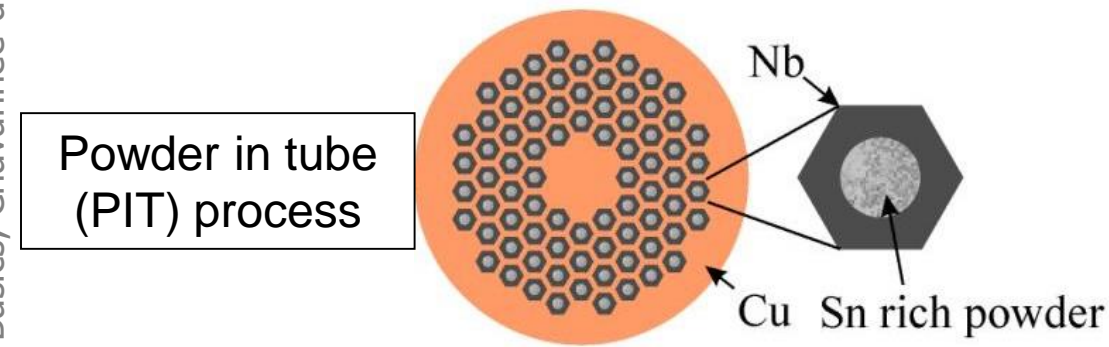
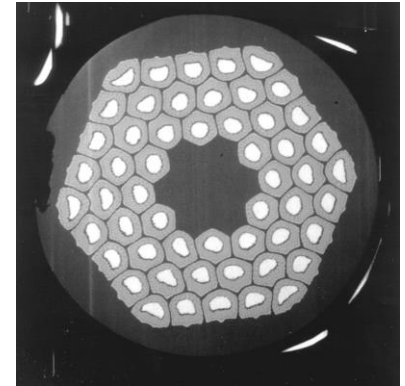




Multifilament wires

Fabrication of Nb₃Sn multifilament wires

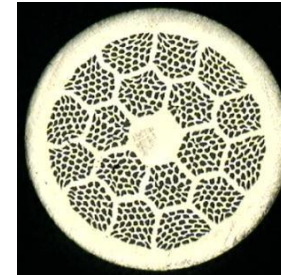
- Since Nb₃Sn is brittle, it cannot be extruded and drawn like Nb-Ti.
- The process requires several steps:
 - Assembly multifilament billets from Nb₃Sn precursor: Nb and Sn
 - Fabrication of the wire through extrusion-drawing
 - Fabrication of the cable
 - Fabrication of the coil
 - “reaction”: the Cu, Sn and Nb are heated to 600-700 C and the Sn diffuses in Nb and reacts to form Nb₃Sn



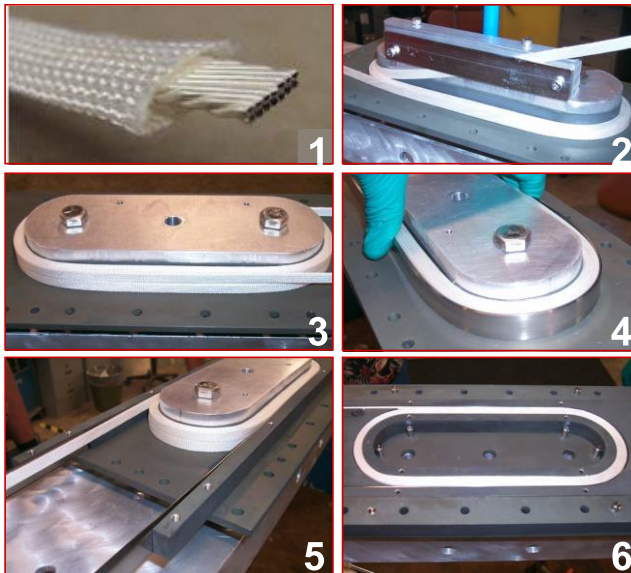
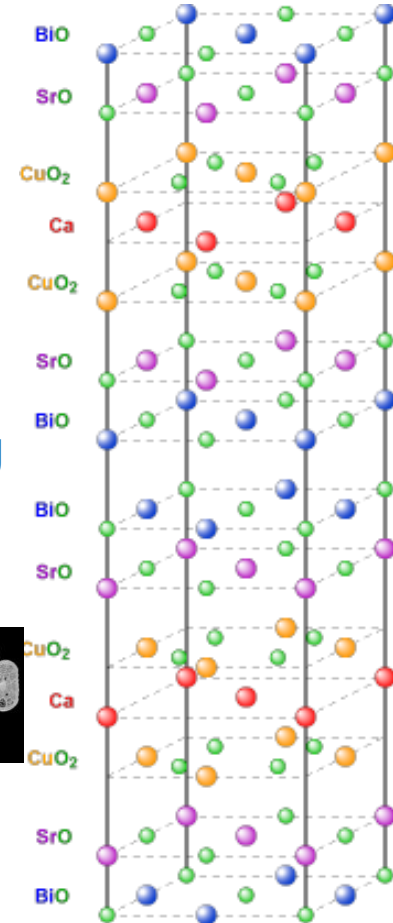
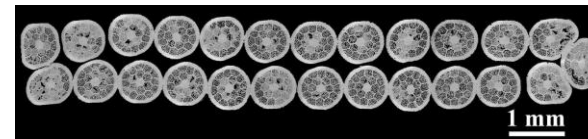
Superconducting strands and tapes: BSCCO

BSCCO: Bismuth strontium calcium copper oxide

- Available in strands (OST)
- Can reach 400 A/mm² (overall)
- Is fragile under stress and strain
- Powder in a silver tube
- Has to be reacted at 850° C with a temperature precision of 1° C in an oxygen atmosphere
- Can be cabled in high current Rutherford cables



OST wire
0.8 mm using
Nexans
precursor

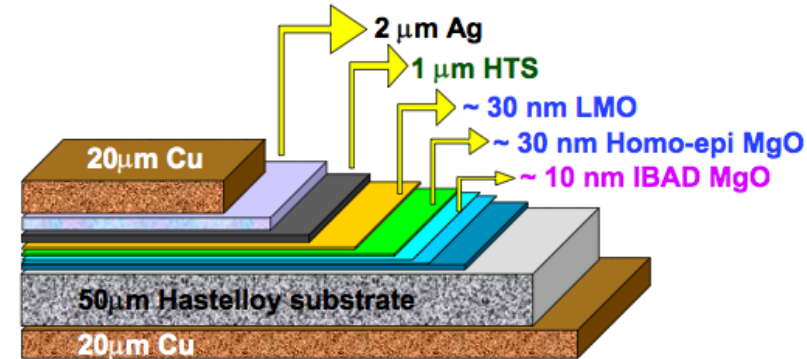
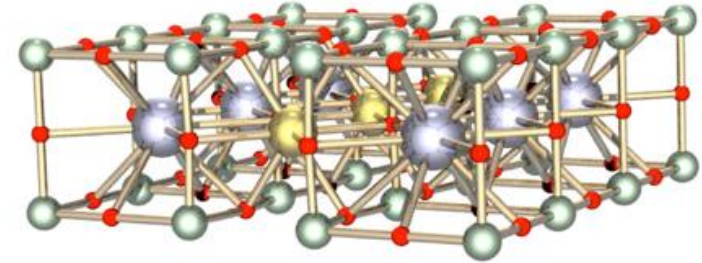


Difficult technology but could be promising for high field magnets in >20 T region

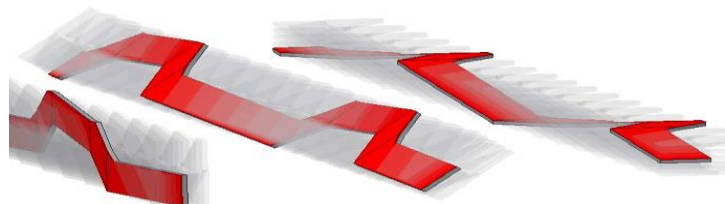
Superconducting tapes: YBCO

YBCO: Yttrium barium copper oxide

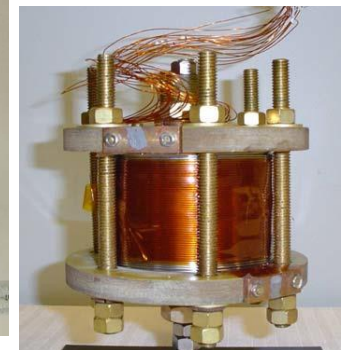
- Available in tapes : YBCO deposited on a substrate to impose the texture (1-2 μm)
- Can reach $> 600 \text{ A/mm}^2$ (overall)
- Is strong under axial stress and strain
- Limited cabling possibilities:



- Difficult technology but could be promising for high field magnets in $>20 \text{ T}$ region.



Potted racetrack coils



YBCO
SUPERPOWER
Record field (25 T),
adding 3 T
NHMFL - Florida



Superconducting cables for magnets

We need multi-strand cables

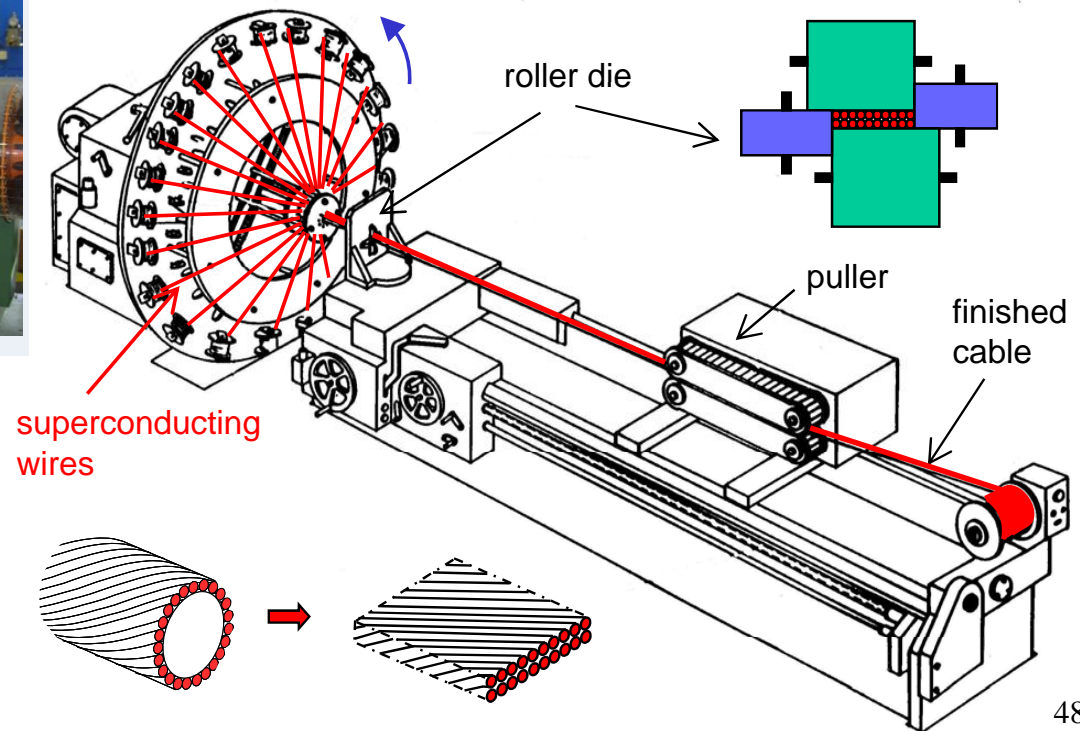
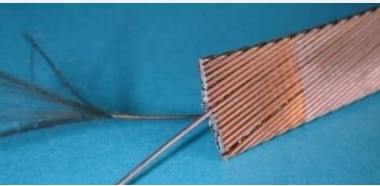
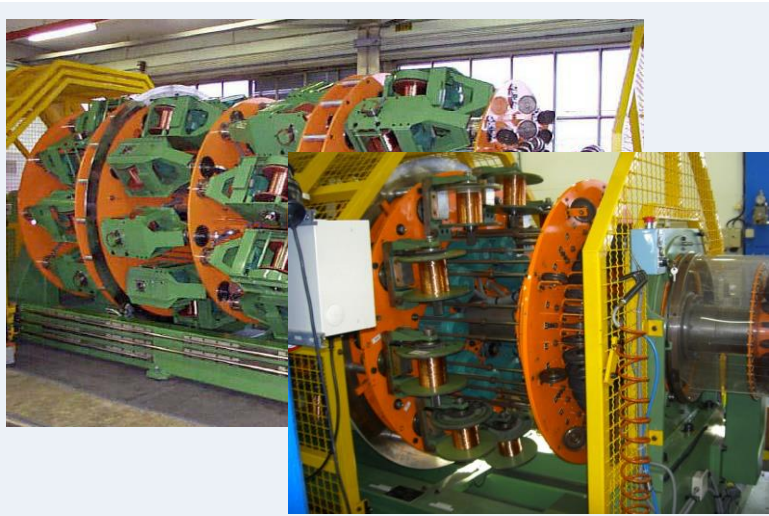
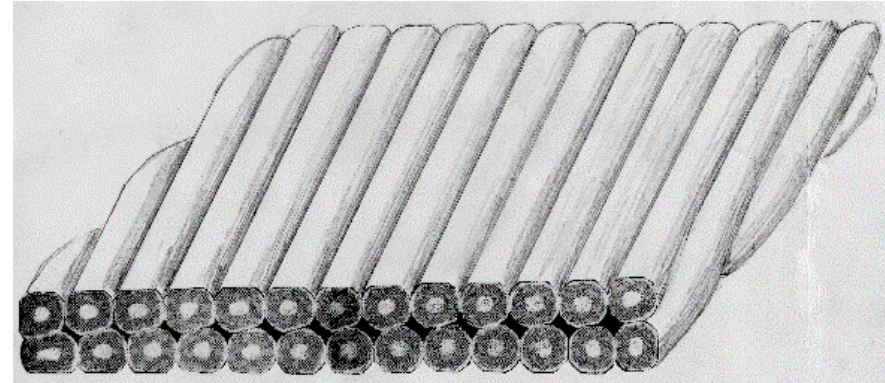
- Superconducting accelerators are ramped up in time spans 100 s to 1000 s
- Coils are designed for voltages to ground of around 1000 V
- With the number of turns and the current the inductance is to be limited to keep the voltage below 1000 V
- Dipoles and Current:
 - Tevatron $B = 4.4 \text{ T} ; I \sim 4000 \text{ A}$
 - Hera $B = 5 \text{ T} ; I \sim 6000 \text{ A}$
 - LHC $B = 8.3 \text{ T} ; I \sim 12000 \text{ A}$
- For magnets $10 \text{ T} < B < 15 \text{ T}$ the current has to be $10 \text{ kA} < I < 15 \text{ kA}$
- For stability reasons strands are $0.6 \text{ mm} < \text{strand diameter} < 1 \text{ mm}$
- With a Cu-nonCu ratio (stability) around 1 and a $J_c \sim 1000 \text{ A/mm}^2$
 - ➔ a 1 mm diameter strand can carry $\sim 400 \text{ A}$
 - ➔ so we need a 30 strand cable to get up to 12 kA

$$V = -L \frac{dI}{dt}$$

$$L \gg N^2$$

Rutherford cables

- Compact cables giving high overall current density
- Easy rectangular geometry for convenient winding





How to get high fields in accelerator dipole and quadrupole magnets ?

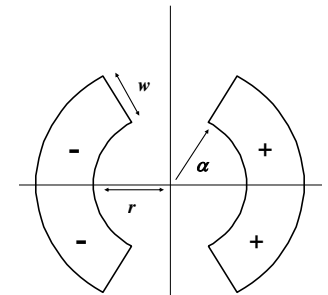
From Ampere's law one can derive the field resulting from the current in a line conductor and integrate this over the surface of a coil

- **Dipole 60° sector coil** [see ref 10, 14]

- The field is *proportional to the current density j*
- The field is *proportional to coil width*
- The field is *independent of aperture*

$$B_1 = -4 \frac{j m_0}{2 \rho} \int_0^{\rho/3} \int_0^{\rho/3} \frac{\cos q}{r} r dr dq = -\frac{\sqrt{3} m_0}{\rho} j w$$

with: r : inner radius coil
w : coil width
ρ : radial coordinate
J : current density

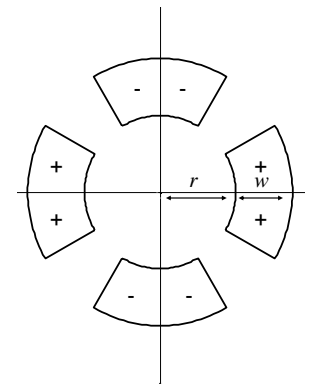


Cross-section of a dipole based on 60° sector coils

- **Quadrupole 30° sector coil** [see ref 11, 14]

- The gradient is *proportional to the current density j*
- The gradient depends on *w/r*

$$G = -8 \frac{j m_0}{2 \rho} \int_0^{\rho/6} \int_0^{\rho/6} \frac{\cos q}{r} r dr dq = -\frac{\sqrt{3} m_0}{\rho} j \ln \frac{1}{e} + \frac{w}{r}$$



Cross-section of a quadrupole based on 30° sector coils

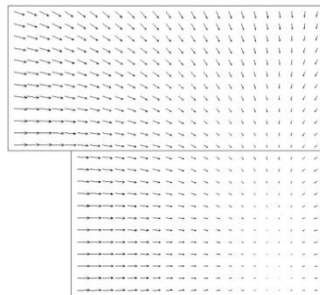
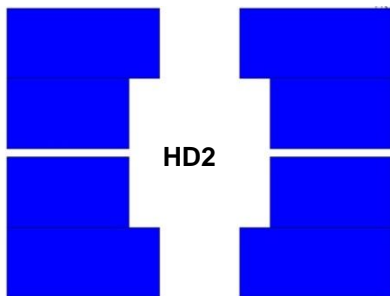
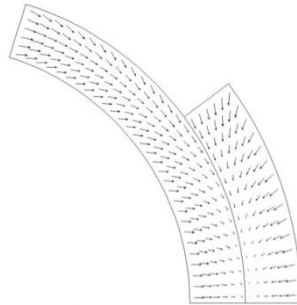
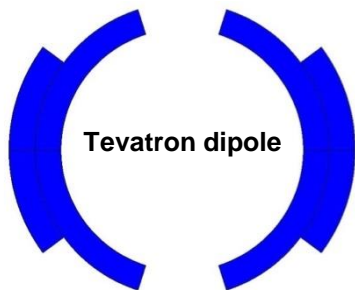
➔ **by having very high current density close to the beam pipe**

See: E. Todesco et al. ref[10] and indirectly : N. Wilson ref[1], K-H Mess et al. ref[2]

For a in depth study of magnetic field calculations: S. Russenschuck ref[4]

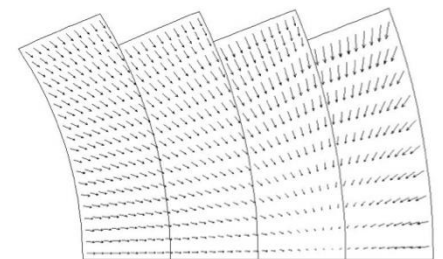
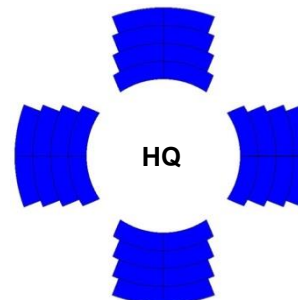
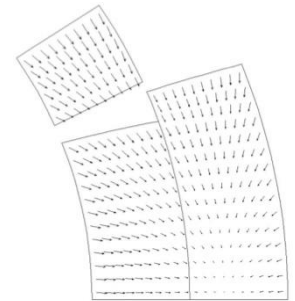
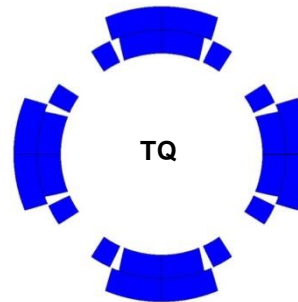
The e.m. forces in a dipole magnet tend to push the coil

- Towards the mid plane in the vertical-azimuthal direction ($F_y, F_\theta < 0$)
- Outwards in the radial-horizontal direction ($F_x, F_r > 0$)



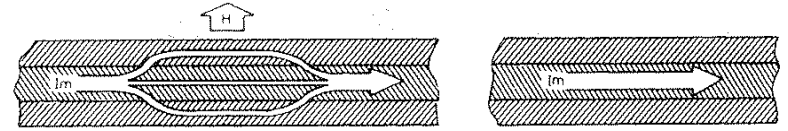
The e.m. forces in a quadrupole magnet tend to push the coil

- Towards the mid plane in the vertical-azimuthal direction ($F_y, F_\theta < 0$)
- Outwards in the radial-horizontal direction ($F_x, F_r > 0$)

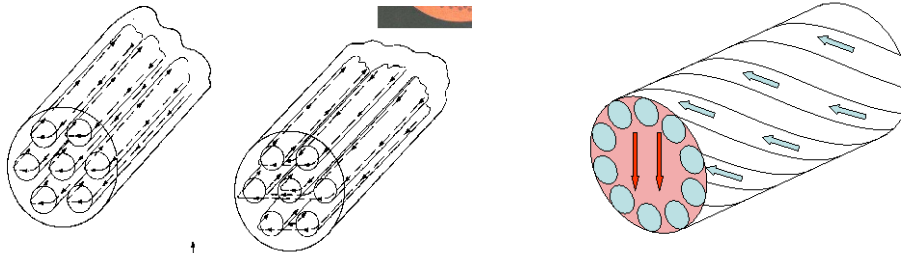
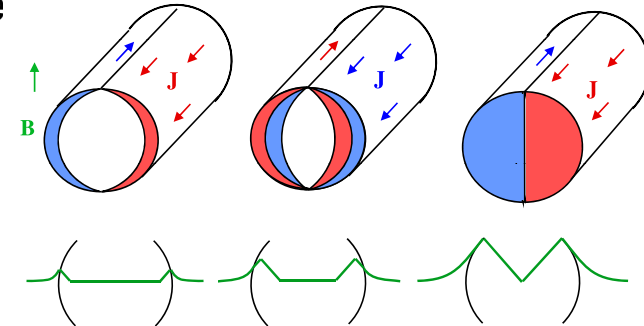
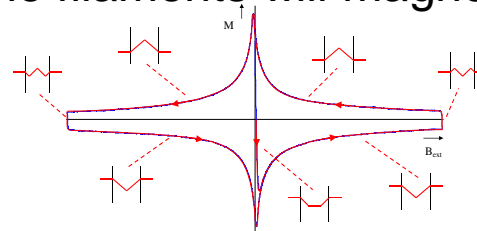


Conductor stability and AC behaviour

- Pure massive superconductor is not stable as they (Nb-Ti, Nb₃Sn) are poor normal conductors
- To 'cryogenically stabilize' the conductor one surrounds it in Cu:
 - good electrical conductivity
 - good heat transfer to the He
- During current ramping the filaments will magnetize
 → make them thinner

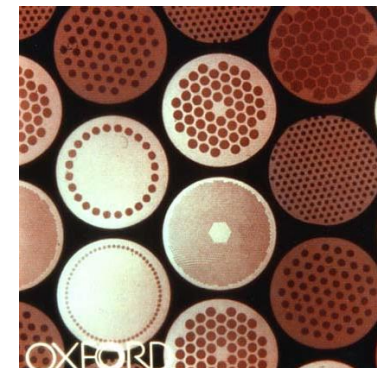


- Filaments will have magnetic coupling
 → twist the strand



Courtesy M. Wilson

- Practical low temperature superconductors are made as thin (5 μm – 100 μm) superconducting filaments in a Cu matrix, which is twisted



Quench: a thermal runaway effect

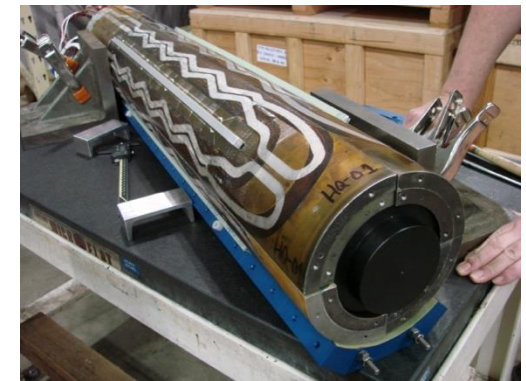
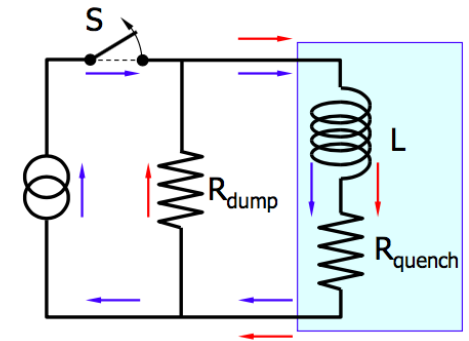
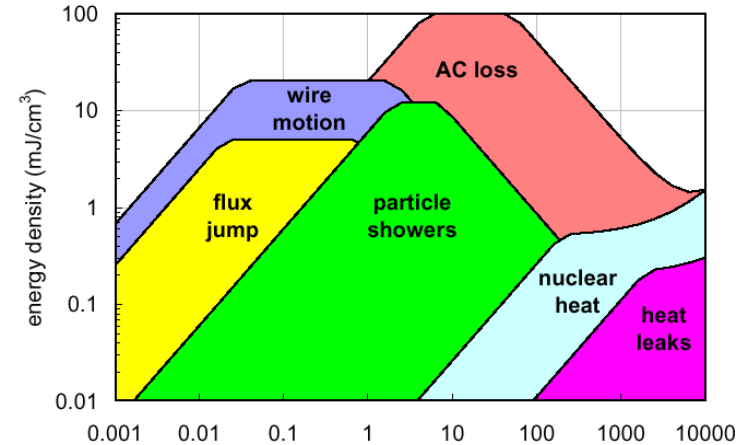
Due to perturbations locally the conductor can get $T > T_c (J_l, B_l)$

A thermal runaway can then occur, called a **Quench**

With stored energies $> \text{MJ}$ the coils can overheat if nothing is done ($T = 3000\text{K}$ is possible !)

What to do ?

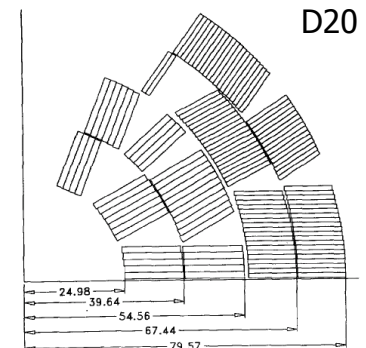
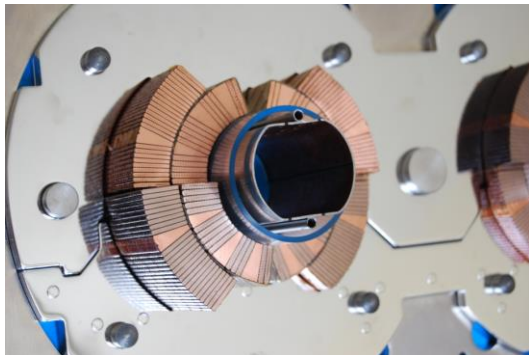
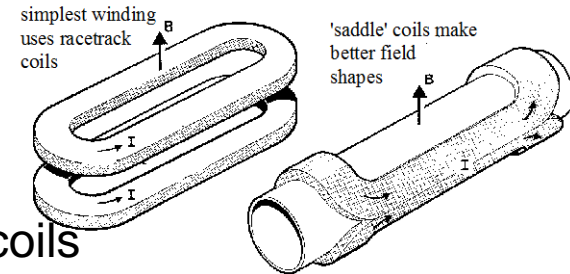
- Detect the quench : SC: $R=0 \rightarrow V=0$, quench $V>0$ (typically 100mV threshold)
- Switch power convertor off
- Heat up the whole coil with quench heaters
- Dump energy of the circuit into a dump resistor



Two types of coils are in use for high field magnets:

Cos(θ) coil and *Block coil*

- *Cos(θ) coil* (the traditional solution)
 - Allows a very good field quality ($b_n < 1 \cdot 10^{-4}$) in thin coils
 - all (but one) existing accelerators use this type of coil
 - Is very efficient wrt the quantity of superconductor used
 - The EM forces cause a stress buildup at the midplane where also high fields are located
 - Wedges are needed in the straight part ('Keystoned' cable)
 - The ends are short, special geometry for which there is a large experience but not it is easy

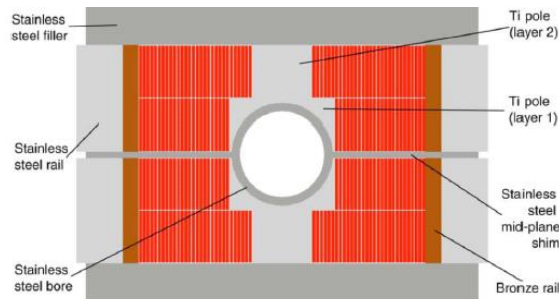


Courtesy M. Wilson

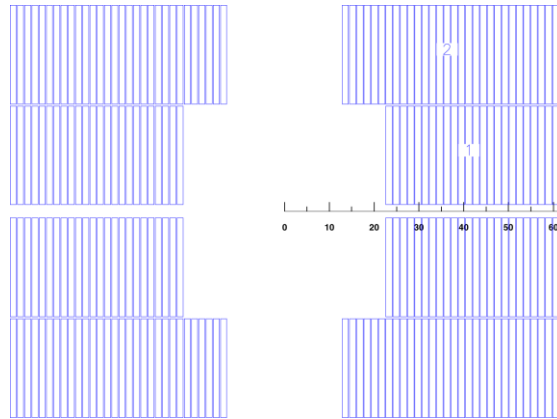
Courtesy LBNL

Practical accelerator magnet design: Dipoles

- Block coil (used on development magnets)
 - Used with thick coils the field quality is good
 - Not yet used in accelerators
 - Is less efficient ($\sim 10\%$) wrt to $\cos(\Theta)$ for quantity of superconductor used
 - The EM forces cause a stress buildup at the outside edge of the coil where the fields are lower
 - The straight part is very easy : rectangular cable and wedges (field quality)
 - ‘flared ends’ look easy but there is little experience exists to make them



HD2



Courtesy LBNL





Pre-stress

- Why pre-stress ?
 - Field quality is determined by the cable positioning (be precise to ~ 0.02 mm)
 - Under the MN forces the coils will move
 - ➔ Apply pre-stress to fix the positioning
 - Very small amounts of heat can quench the coil: limit the movement (avoid stick-slip effects on ~ 10 μm movements)
 - ➔ Apply pre-stress to fix the positioning
- How to put pre-stress ?

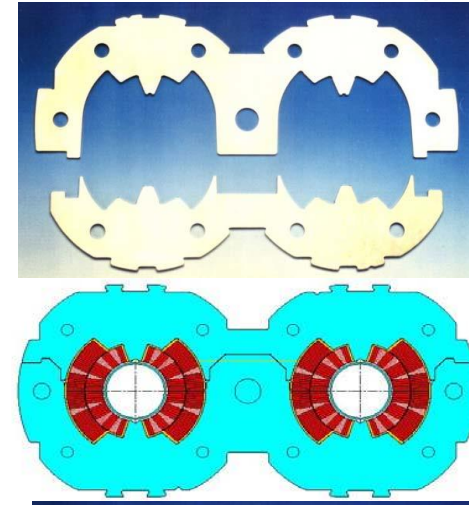
Three methods:

 1. Compress at room temperature: collar system
 2. Use room temperature pre-stress plus differential shrinkage at cool-down: Al or stainless steel shrinking cylinder and/or a (shrinking) key
 3. Compress a bit at room temperature and use differential shrinkage at cool-down: Al shrinking cylinder + bladder and key system
- Order of magnitudes: LHC @ 8.34 T: 70 MPa warm, 30 MPa cold
Fresca2 @ 13 T: 60 MPa warm, 130 MPa cold

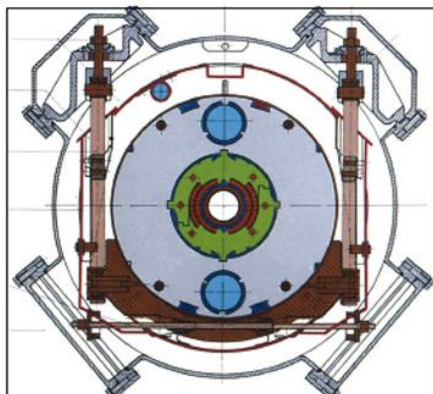
Prestress: collars

“The classical solution”

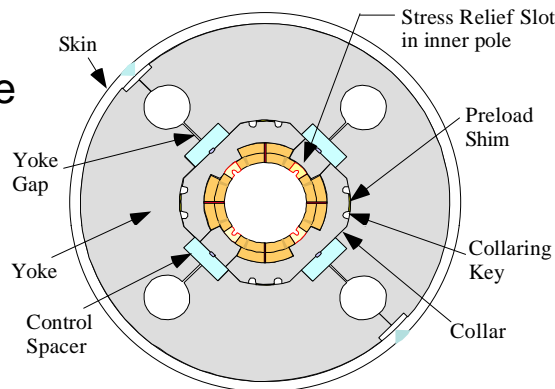
- Thin collars put around the coil
- The coil is well contained in a fixed cavity
- Pressed together and locked with pins or keys
- At 300K apply a prestress 2-3 times of what is needed as part of the stress is lost during cooldown: for very high field tends to be too high (LHC:70 MPa at 300 K and 40 MPa at cold)
- Field quality is in good part determined by collar shape
- If the coils size is not so well controlled, the stress can be too high or too low
- Nb_3Sn is stress sensitive and this could be a problem



LHC dipole
CERN



Hera dipole
DESY



TQC quadrupole
LARP-FNAL





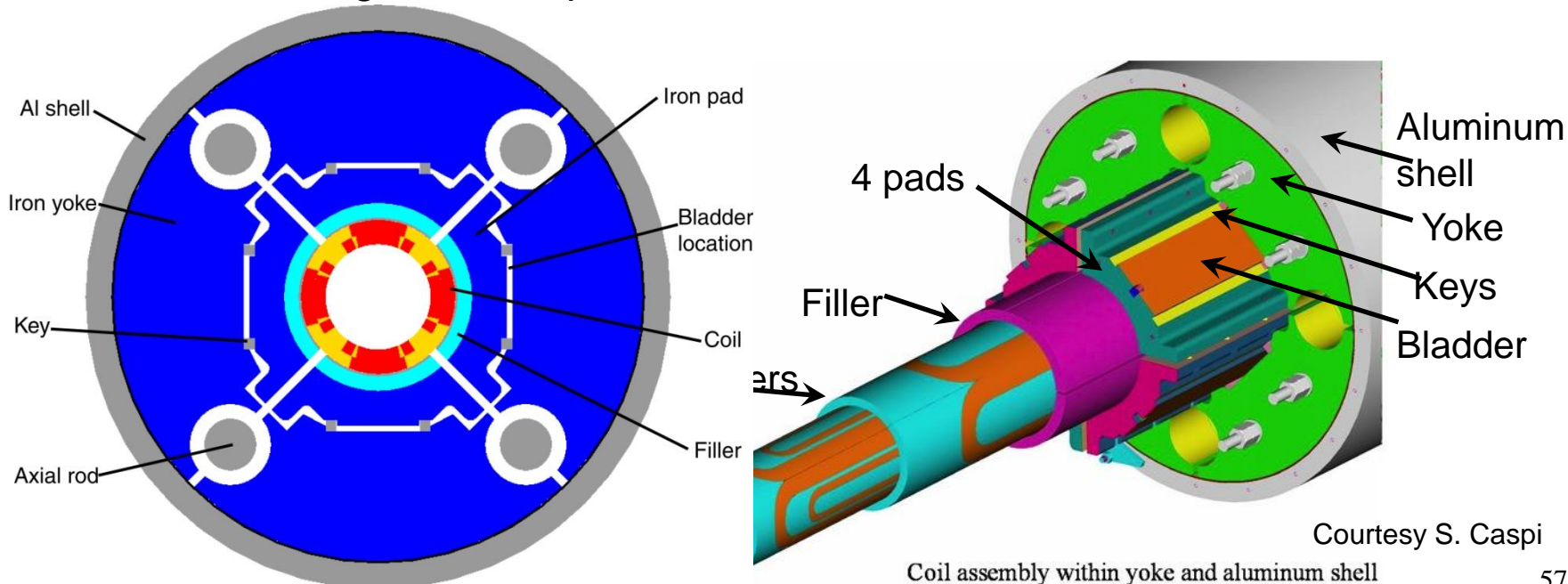
Prestress: Al shrinking cylinder + bladder and keys

Developed at LBNL, example: TQS a LARP model quadrupole

300 K: Bladders pressurized with water (<600 bar) , then insert keys → load between 10 MPa and 80 MPa

Cooldown: differential shrinkage between AL shell and Fe yoke load another ~100 MPa

Needs careful mechanical FE modeling before and strain measurements during bladder operations and cooldown



Courtesy S. Caspi

Coil assembly within yoke and aluminum shell

CAS Basics, Chavannee-de-Bogis, 7-Febr-2017, Magnets, GdR



Looking in the kitchen of future SC magnet development

What is happening after the 8T magnets for LHC ?

At CERN

- 1) Upgrade the LHC luminosity: HL-LHC (HILUMI)
 - use large aperture Nb₃Sn triplet quadrupoles (12T class)
 - improve collimation: use a few 11T dipoles to make space
2. Go to higher energies
 - 16 T Nb₃Sn dipoles in the LHC ring for $E_{com}=26$ TeV : HE-LHC
 - 16 T Nb₃Sn dipoles in a 100 km new ring for $E_{com}=100$ TeV : FCC (Future Circular Collider)

But even !

- 20 T HTS hybrid dipoles in the LHC ring: for $E_{com}=33$ TeV : HE-LHC
- 20 T HTS hybrid dipoles in a 80 km new ring for $E_{com}=100$ TeV : FCC

In China

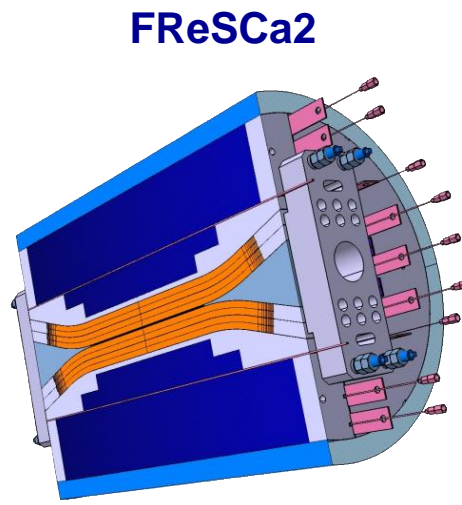
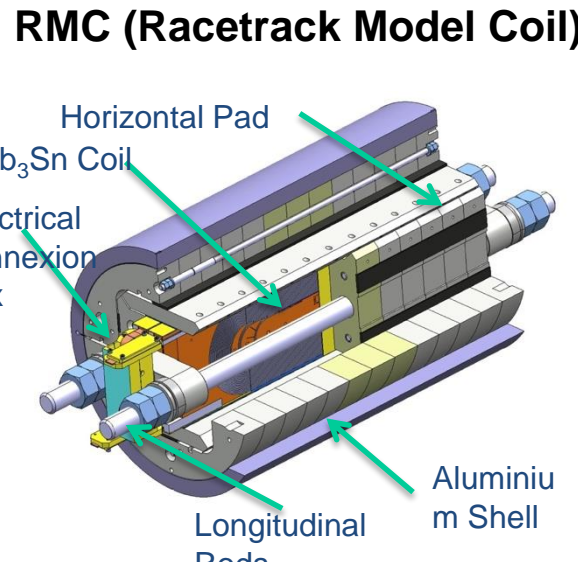
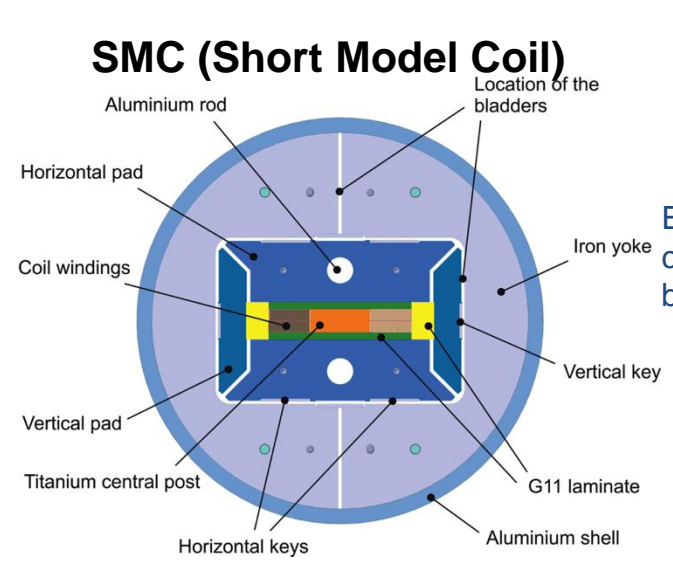
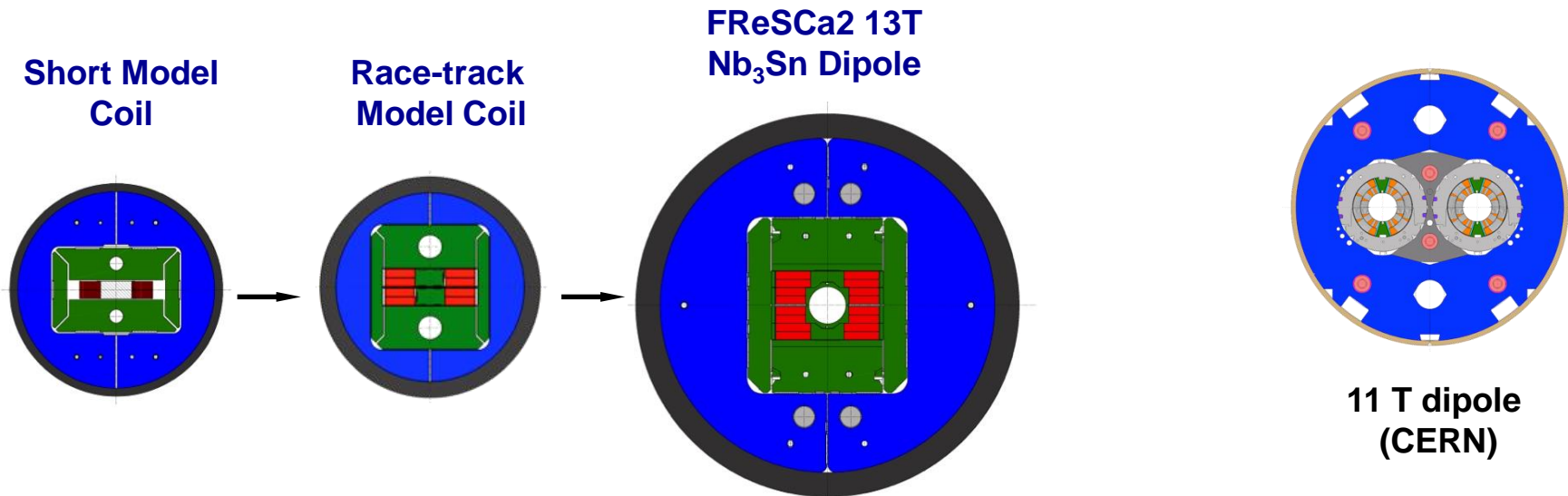
A similar completely new project is being studied in China: SPPC (C=54 km, B=20 T, $E_{com}=71$ TeV)

For these, basic High Field Magnet development programs are since many years running in the US and Europe and recently in China



CERN-European development evolution

CAS Basics, Chavannee-de-Bogis, 7-Febr-2017, Magnets, GdR



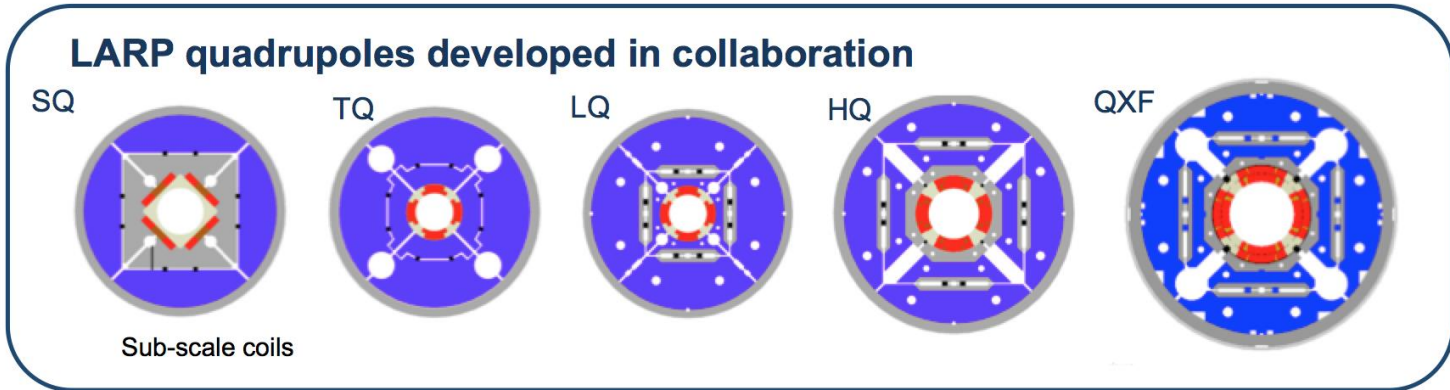
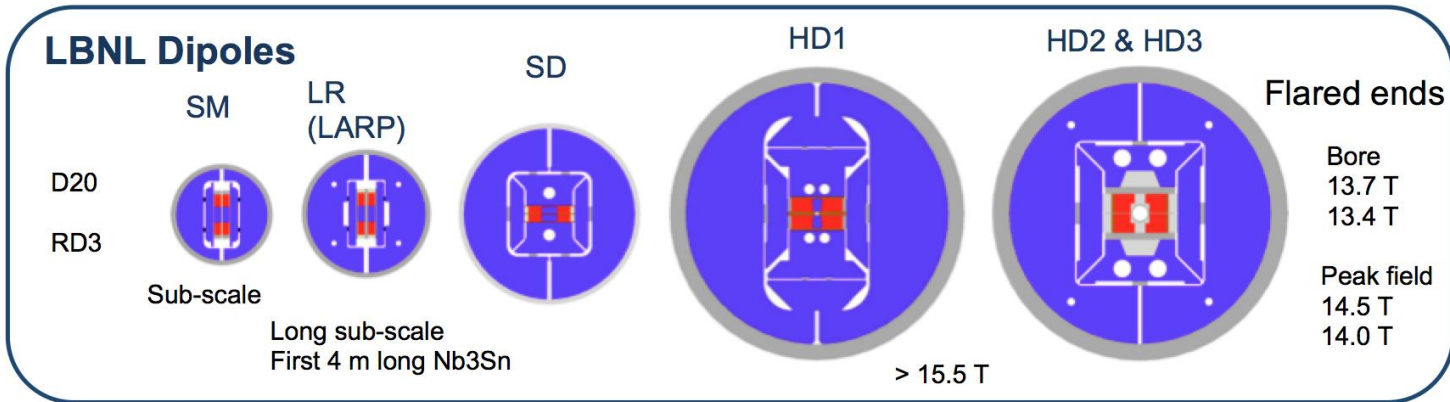


Basic magnet technology development for HL-LHC and beyond (2004-2013) ; US development evolution



History of LBNL and LARP Magnet Develop

Used bladder and key technology developed at LBNL



By courtesy of D. Dietderich, LBNL



U.S. DEPARTMENT OF ENERGY

Office of Science

ACCELERATOR TECHNOLOGY & APPLIED PHYSICS DIVISION



CAS Basics, Chavannee-de-Bogis, 7-Febr-2017, Magnets, GdR



Basic HFM development : Some achievements at LBNL (1995-2004)

Since 20 years LBNL is running a high field dipole development program

Some achievements:

- D20, 50 mm aperture, cosQ 4 layer dipole, reached 13.5 T@1.9K
- HD1, flat block coil, 8 mm aperture, reached 16 T
- HD2, flared end block coil, 36 mm aperture, reached 13.8 T

These pose a clear breakthrough above 10 T with a new coil layout (block coil) and a mechanical structure aimed (shell-bladder and keys) at high fields

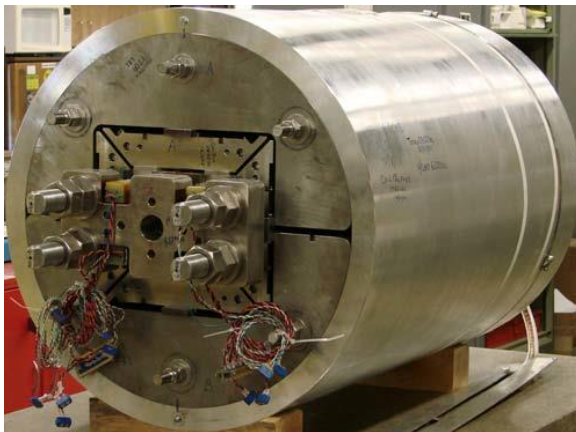


Fig. 1. HD2 assembled and pre-loaded.

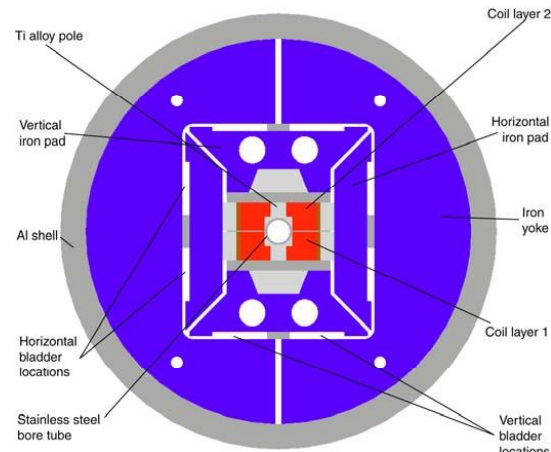
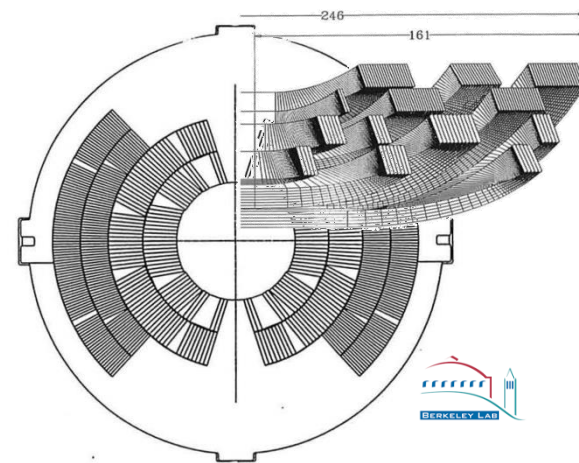


Fig. 2. HD2 cross-section.

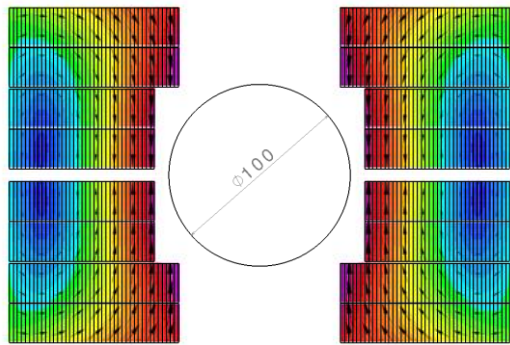


A.D. McInturff, et al., Proc. of PAC 1997, 3212



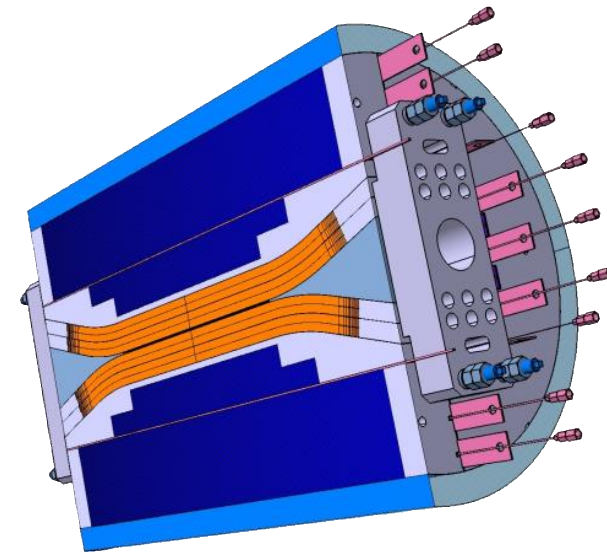
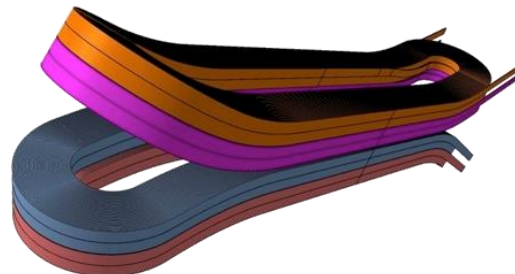
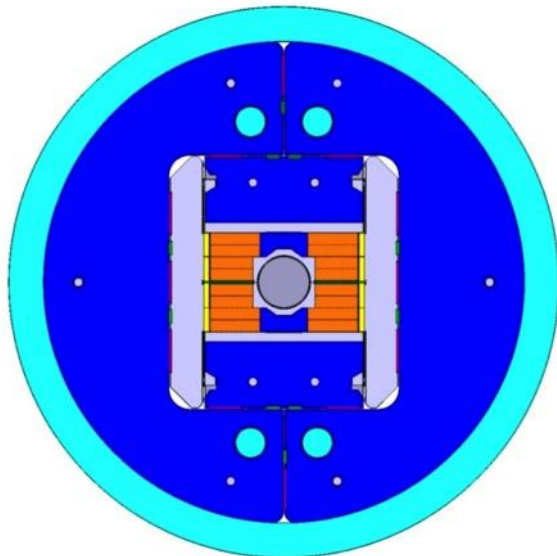
Basic HFM development : EuCARD high field dipole (Fresca2):

- Fresca2 : CERN, CEA construction phase
- First tests 2014



- 156 turns per pole
- Iron post
- $B_{\text{center}} = 13.0 \text{ T}$
- $I_{13\text{T}} = 10.7 \text{ kA}$
- $B_{\text{peak}} = 13.2 \text{ T}$
- $E_{\text{mag}} = 3.6 \text{ MJ/m}$
- $L = 47\text{mH/m}$

- Diameter Aperture = 100 mm
- L coils = 1.5 m
- L straight section = 700 mm
- L yoke = 1.6 m
- Diameter magnet = 1.03 m



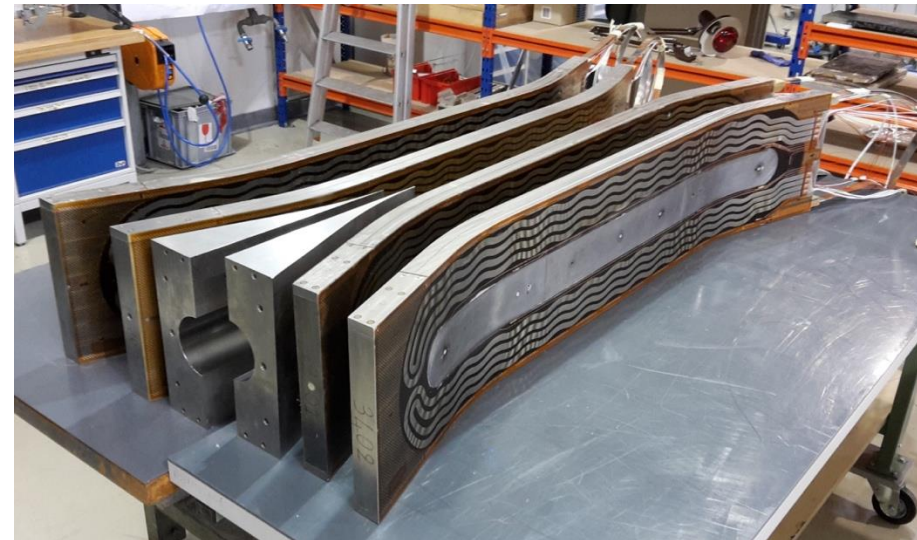
Courtesy Attilio Milanese,
Pierre Manil

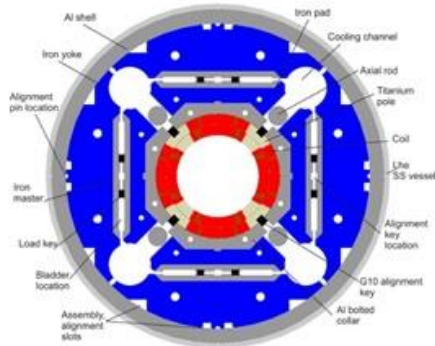


Fabrication of Fresca2 coils

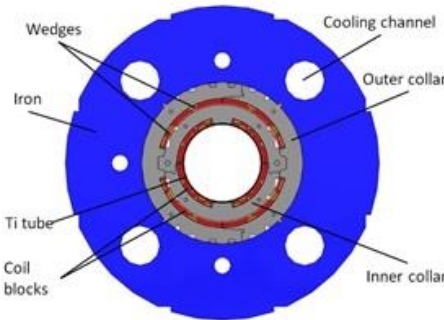
Straightforward technology to wind block coils with flared ends:

This is a lesson for FCC magnets !

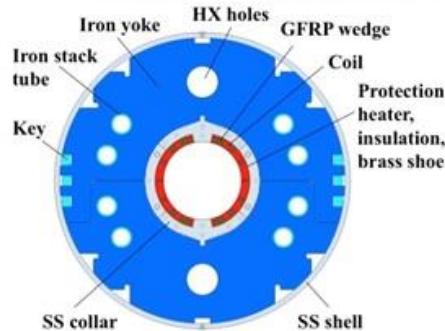




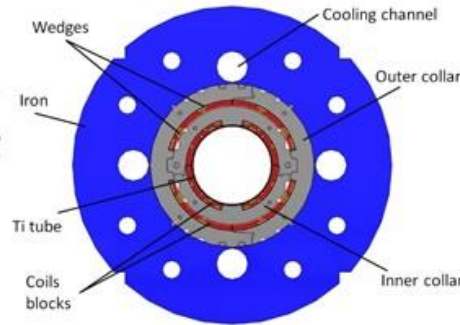
Triplet [G. Ambrosio, P. Ferracin et al.]



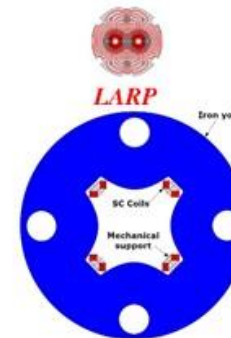
MCBXFB [F. Toral, et al.]



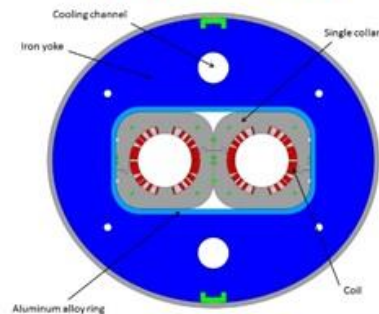
D1 [T. Nakamoto et al.]



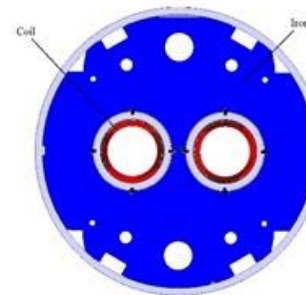
MCBXFA [F. Toral, et al.]



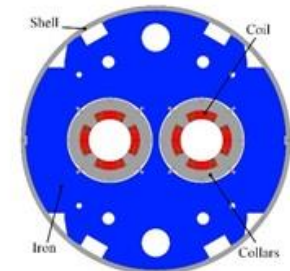
Skew quad [G. Volpini, et al.]



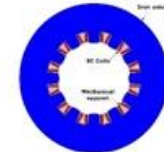
D2 [P. Fabbriatore, S. Farinon]



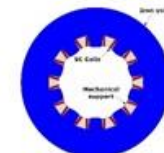
D2 Q4 correctors [G. Kirby]



Q4 [J. M. Rifflet, M. Segreti, et al.]



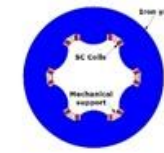
Dodecapole



Decapole



Octupole



Spring 2016 the first model achieved the nominal and ultimate field at FNAL !

A CERN LARP collaboration.

Nominal Gradient 132.6 T/m

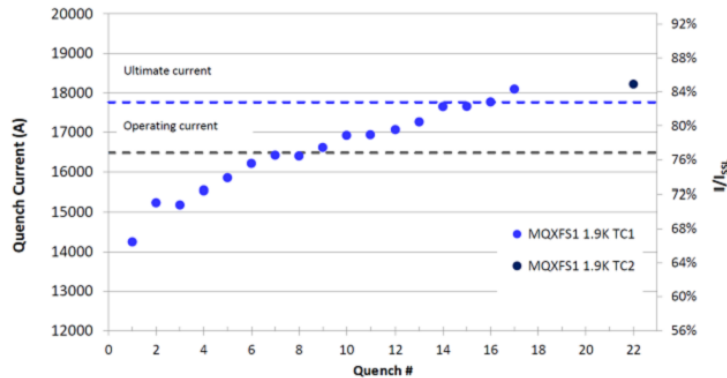
Aperture diameter 150 mm

Peak Field 12.1 T

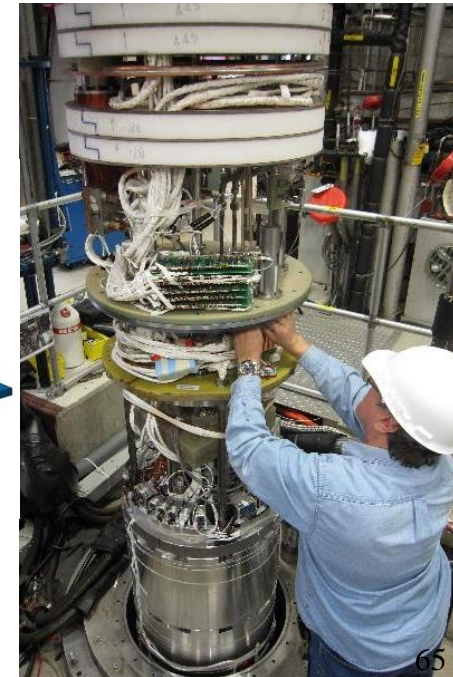
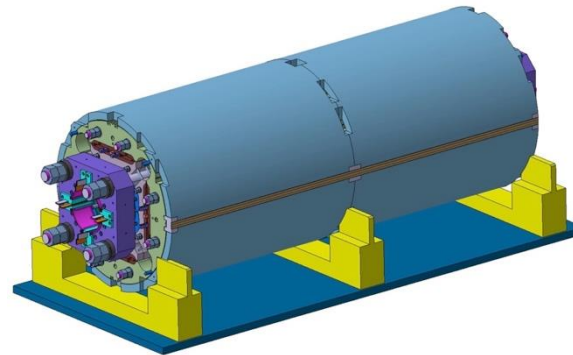
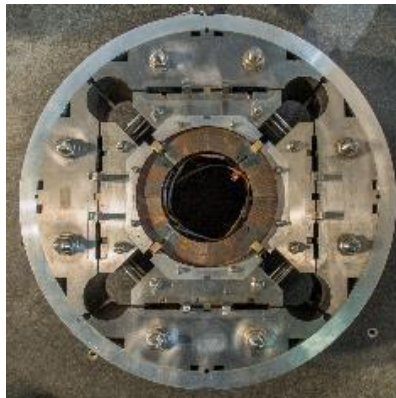
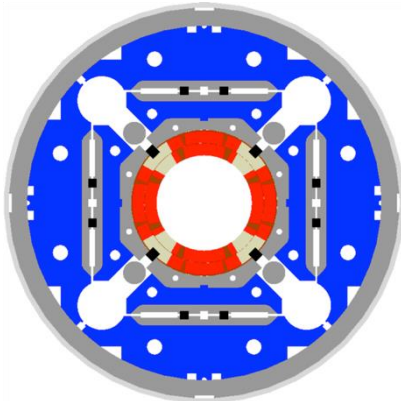
Current 17.5 A

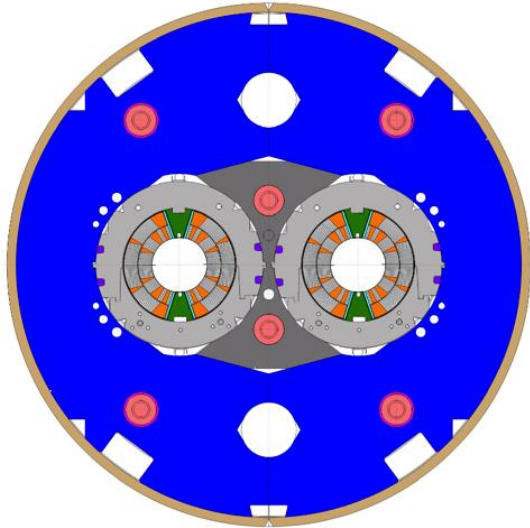
Loadline Margin 20% @ 1.9 K

Stored Energy 1.32 MJ/m



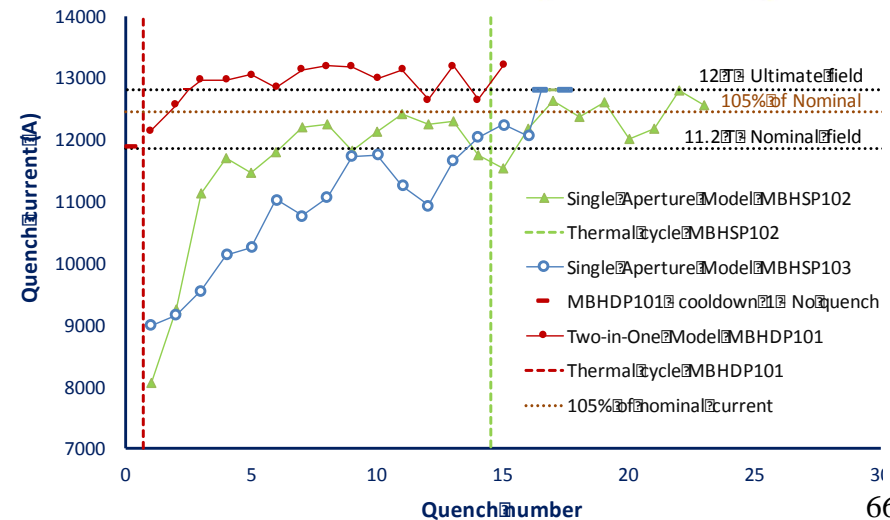
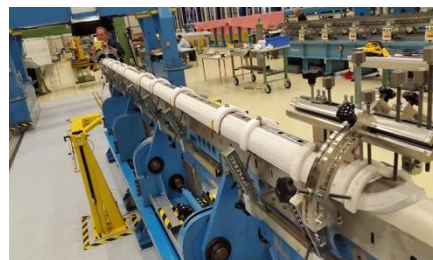
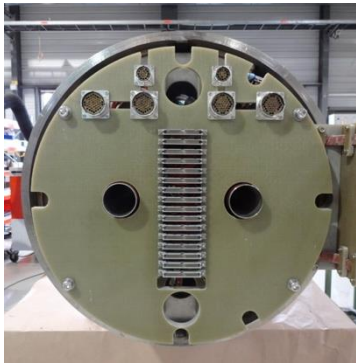
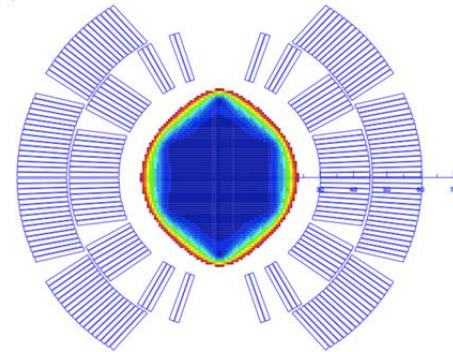
By courtesy of G. Ambrosio (FNAL), P. Ferracin (CERN et al)





- First Nb3Sn magnet to go into an accelerator (2019) !
- Present model program (CERN and FNAL)
 - demonstrated the required performance (11.25 T at 11850 A) and Achieved accelerator field quality

Nominal Field 11 T
 Aperture diameter 60 mm
 Peak Field 11.35 T
 Current 11.85 kA
 Loadline Margin 19.7% @ 1.9 K
 Stored Energy 0.96 MJ/m





FCC development (2014 - ...)

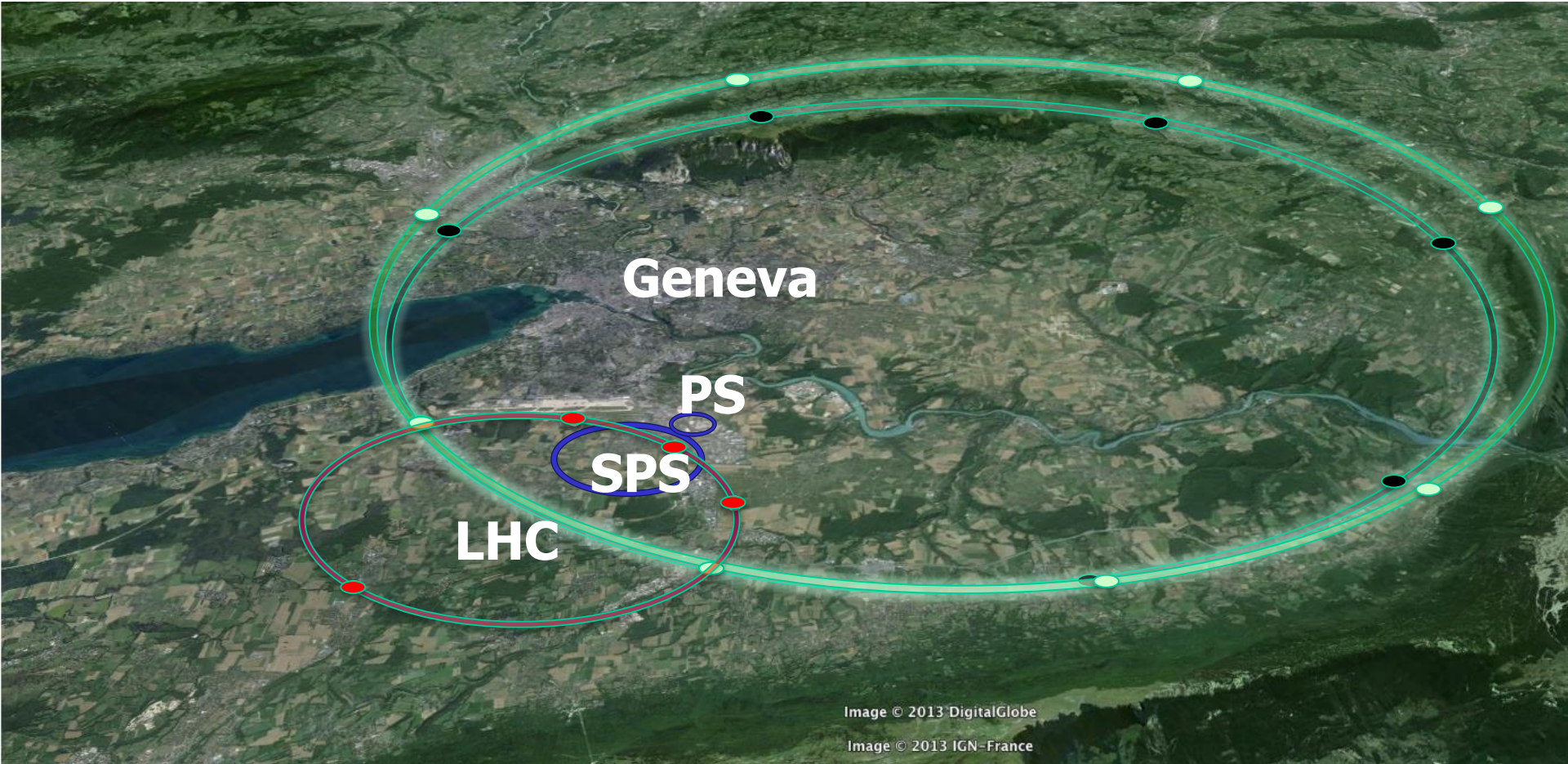


Image © 2013 DigitalGlobe

Image © 2013 IGN-France

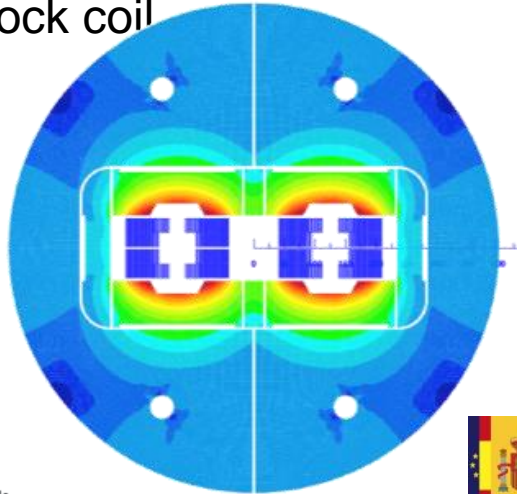
LHC
27 km, 8.33 T
14 TeV (c.o.m.)

HE-LHC
27 km, 20 T
33 TeV (c.o.m.)

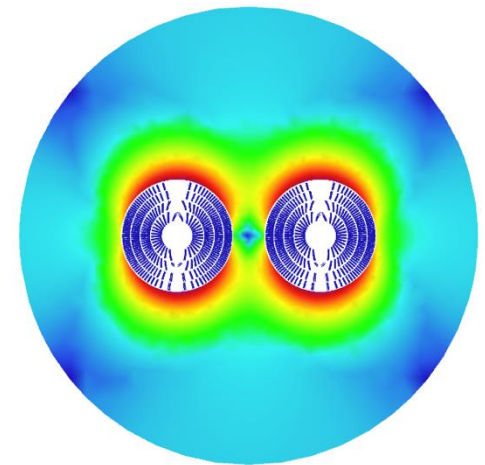
FCC-hh
80 km, 20 T
100 TeV (c.o.m.)

FCC-ee
100 km, 16 T
100 TeV (c.o.m.)

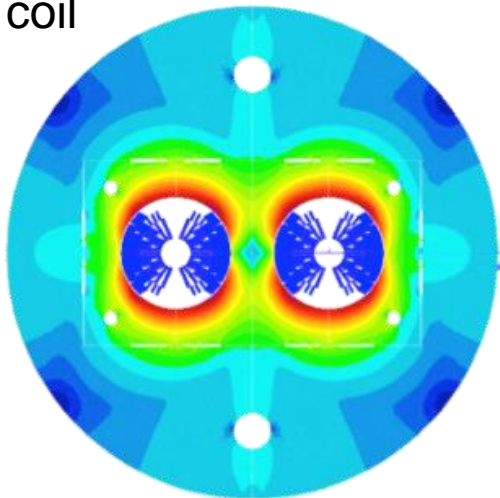
Block coil



Canted Cos-theta



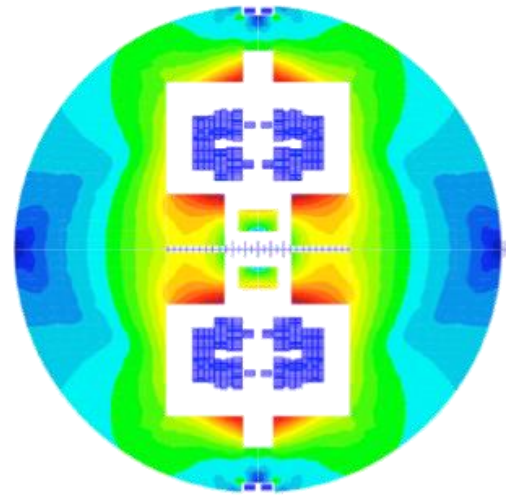
Cos-theta coil



C. Lorin, M. Durante (CEA)



Common coils

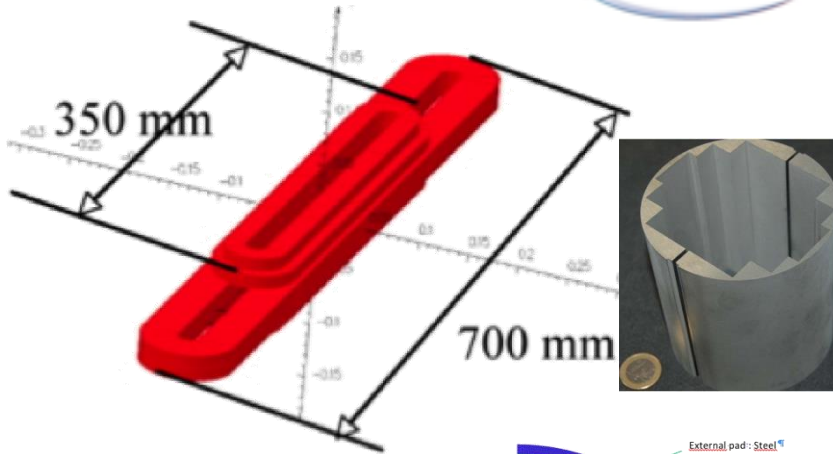


B. Auchmann (CERN/PSI)



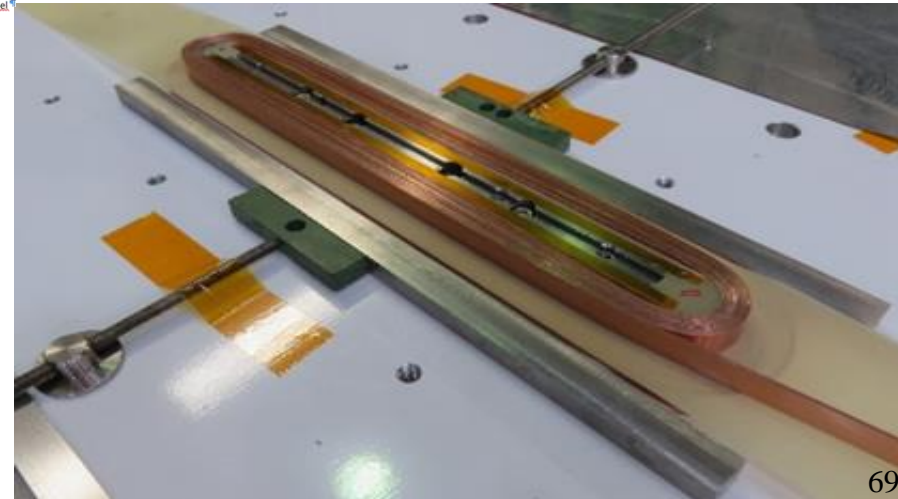
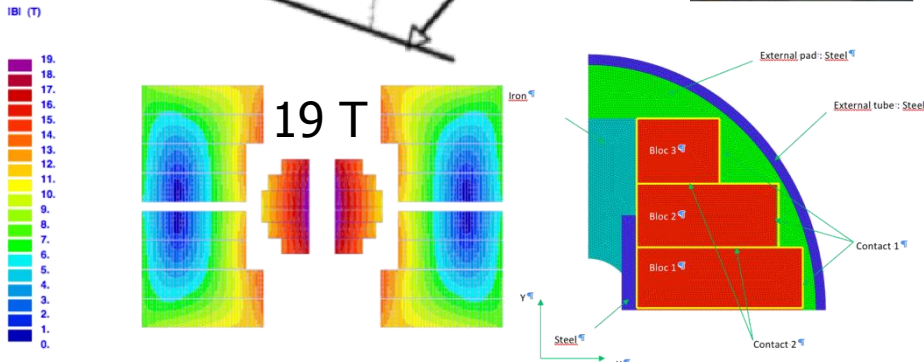
S. Farinon, P. Fabricatore (INFN)

F. Toral (CIEMAT)



6 T HTS (YBCO) insert for test in
FReSCa2
To get to 19 T
But without bore

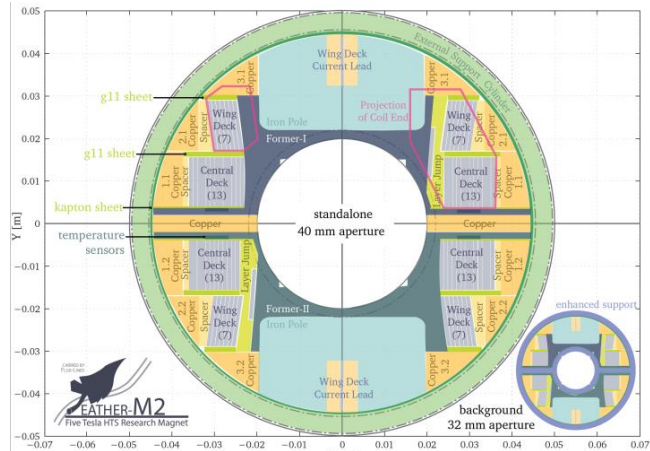
CEA + CRNS Grenoble



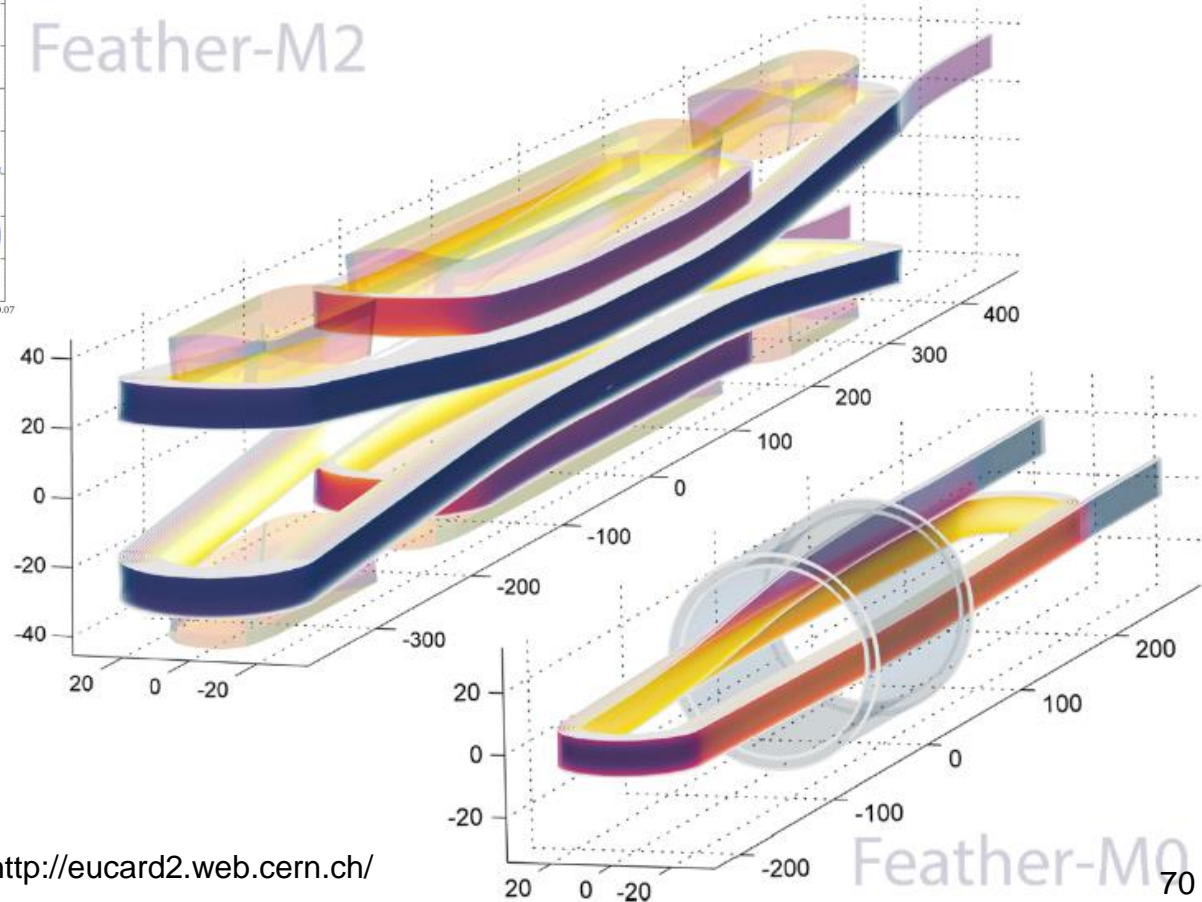


EuCARD2 5T accelerator quality ReBCO magnet

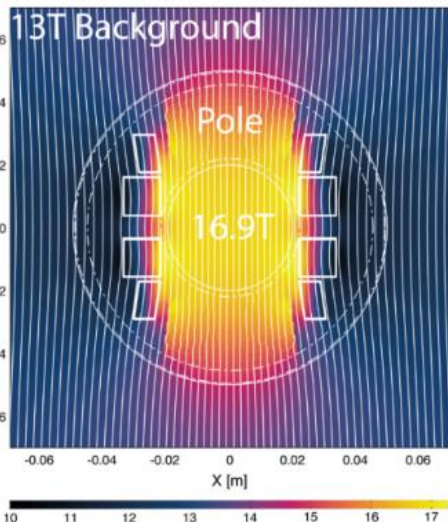
5 Tesla stand alone, (18 T in 13 T background), @ 4.5K, 40 mm aperture, 10 kA class cable, Accelerator Field quality



Feather-M2



CAC Racine, Chavanne, de Rooij, 7-Febr-2017, Magnets, GdR

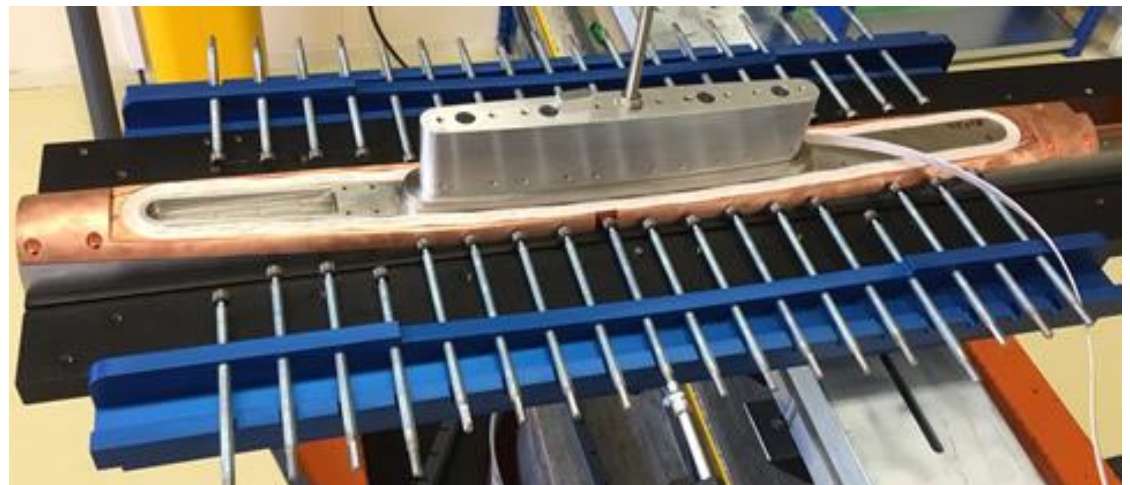
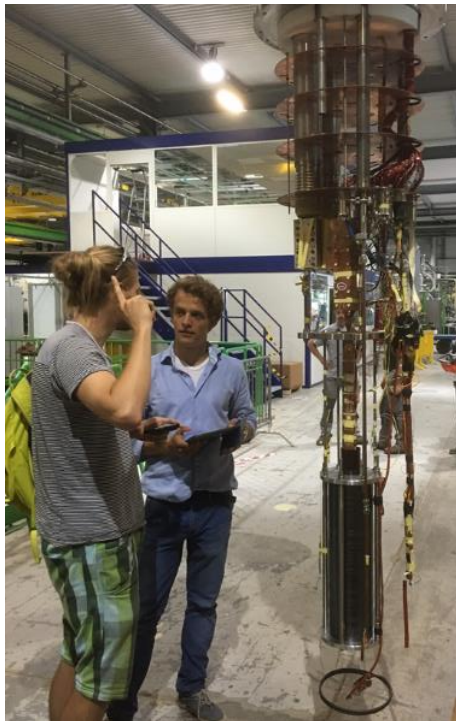
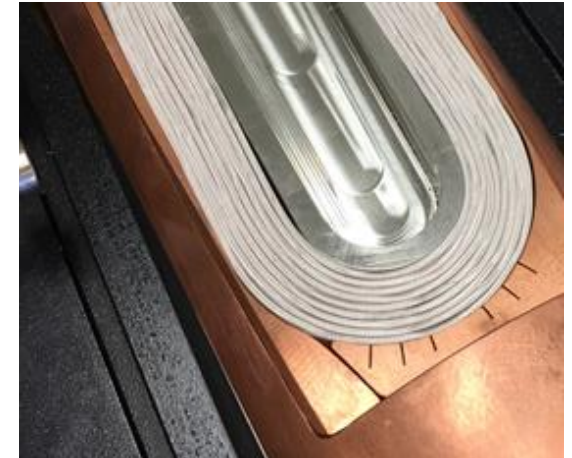
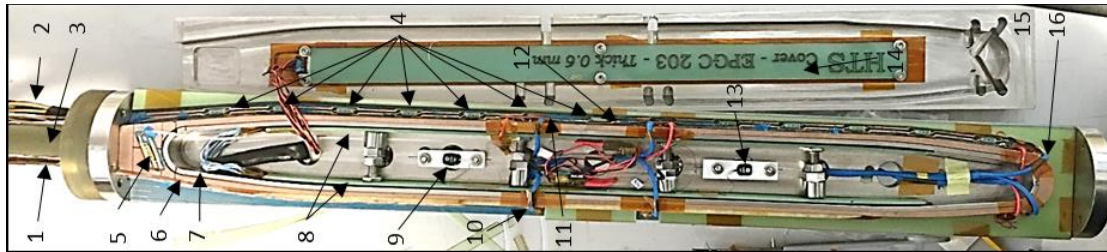


<http://eucard2.web.cern.ch/>

Feather-M0

EuCARD2 5T : Feather0 - Feather-M2.0

- Feather0: First coil in the test station
- Feather2: winding of first coil with dummy cable in progress





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- 6) 21st International Conference on Magnet Technology, Hefei, China, 18 - 23 Oct 2009, IEEE Trans. Appl. Supercond. 20 (2010)
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- 10) E. Todesco, L. Rossi, "Electromagnetic Design of Superconducting Dipoles Based on Sector Coils", *Phys. Rev. Spec. Top. Accel. Beams* 10 (2007) 112401
- 11) E. Todesco, L. Rossi, AN ESTIMATE OF THE MAXIMUM GRADIENTS IN SUPERCONDUCTING QUADRUPOLES, CERN/AT 2007-11(MCS),
- 12) P. Fessia, et al., Parametric analysis of forces and stresses in superconducting dipoles, *IEEE, trans. Appl, Supercond.* Vol 19, no3, June 2009.
- 13) P. Fessia, et al., Parametric analysis of forces and stresses in superconducting quadrupole sector windings, sLHC Project Report 0003

- Websites

- 15) <http://www.magnet.fsu.edu/magnettechnology/research/asc/plots.html>



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And to the people who taught me, years ago, all the fine details about magnets !



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