

# Injection, extraction and transfer

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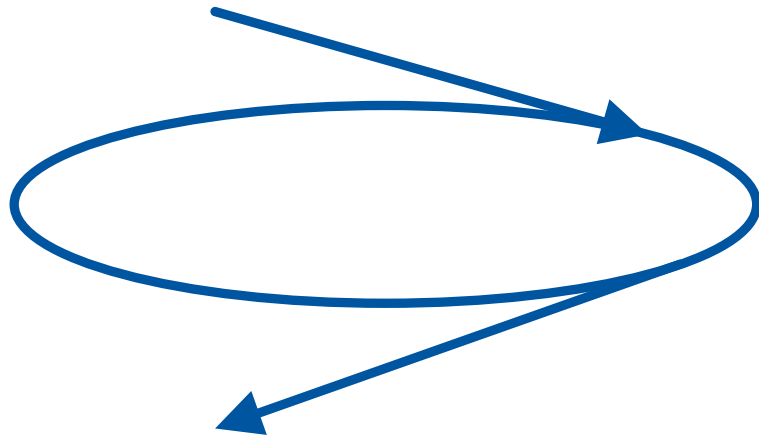
CAS: Basics of Accelerator Science and Technology at CERN

Chavannes 2017

Based on lectures by Brennan Goddard, Matthew Fraser and Rende Steerenberg



# Overview

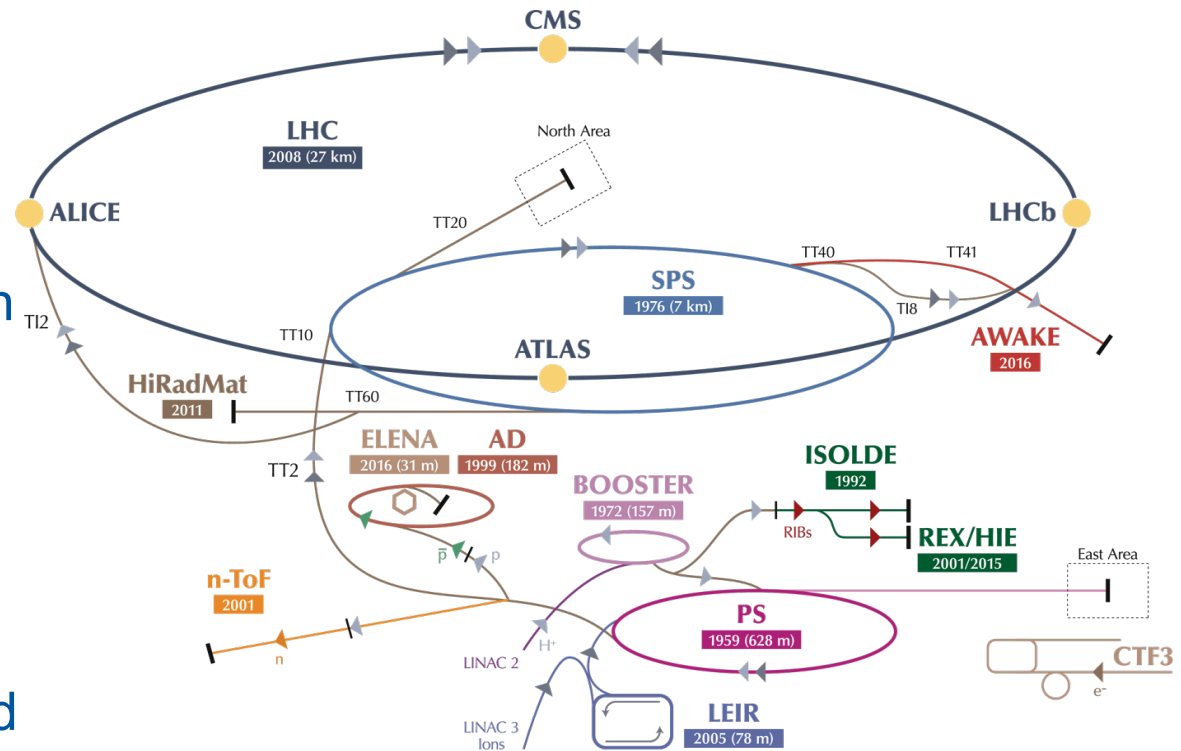


- **Introduction**
- **Single-turn methods**
  - Injection
  - Fast extraction
- **Multi-turn methods**
  - Multi-turn hadron injection
  - Charge-exchange H- injection
  - Multi-turn extraction
- **Resonant slow extraction**
- **Summary**

# Injection, extraction and transfer

## CERN Accelerator Complex

- An accelerator has limited dynamic range
- Chain of stages is needed to reach high energy
- Periodic re-filling of storage rings, like LHC
- External facilities and experiments:
  - e.g. ISOLDE, HiRadMat, AWAKE...

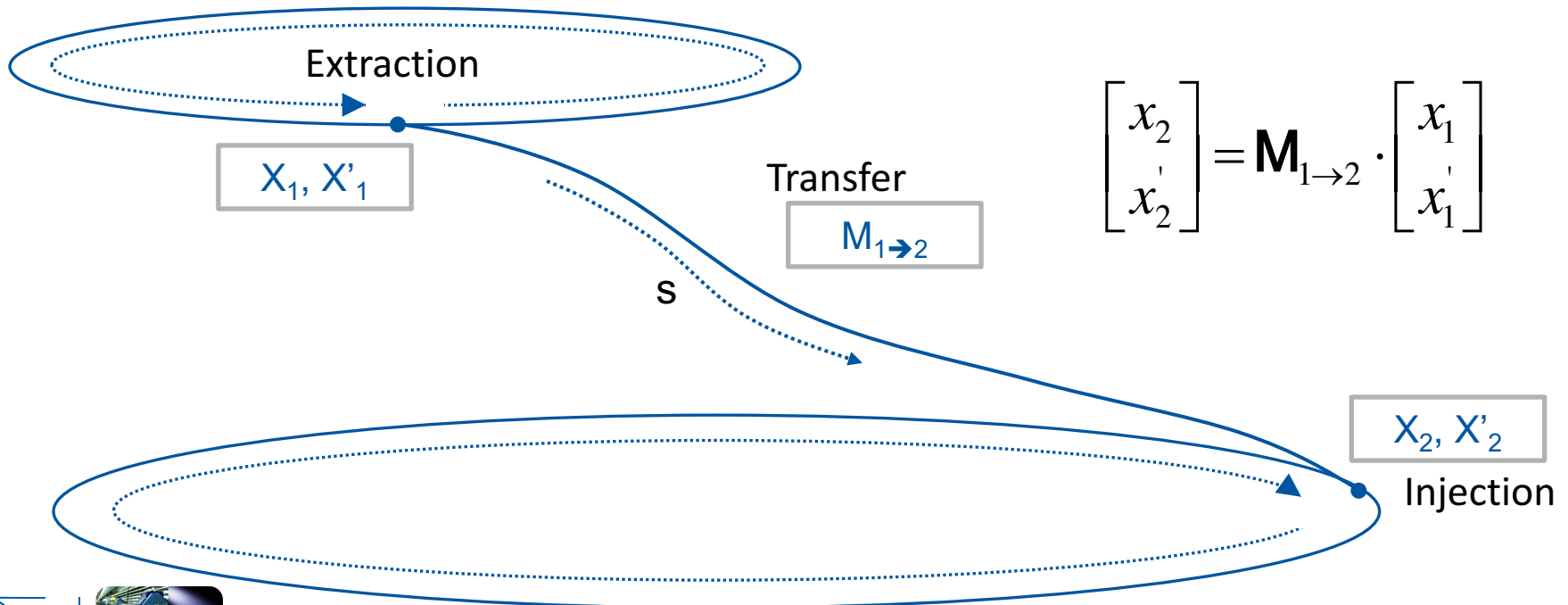


Beam transfer (into, out of, and between machines) is necessary.



# Linking Machines

1. **Extract** a beam out of one machine  
→ initial beam parameters  $X_1, X'_1$
2. **Transport** this beam towards the following machine (or experiment)  
→ apply transfer matrix
3. **Inject** this beam into a following machine with a predefined acceptance  
→ produce required beam parameter for matching  $X_2, X'_2$



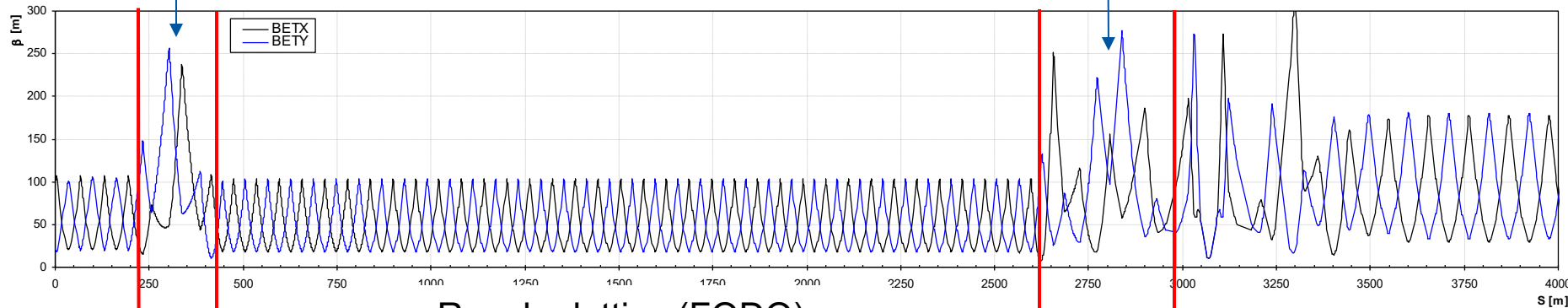
# Optics Matching

## Initial matching section

Independently powered (tuneable) quadrupoles

## Final matching section

Independently powered (tuneable) quadrupoles and (in this case) passive protection devices



SPS

Regular lattice (FODO)  
(elements all powered in series  
with same strengths)

LHC

SPS to LHC Transfer Line (3 km)

Extraction  
point

Injection  
point

Need to “match” 8 variables (TWISS parameter) for propagation from start to end of a transfer

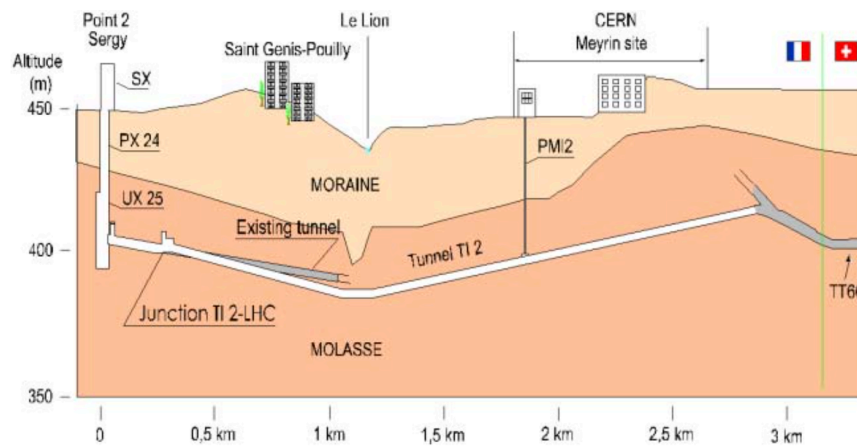


# Linking Machines – constraints

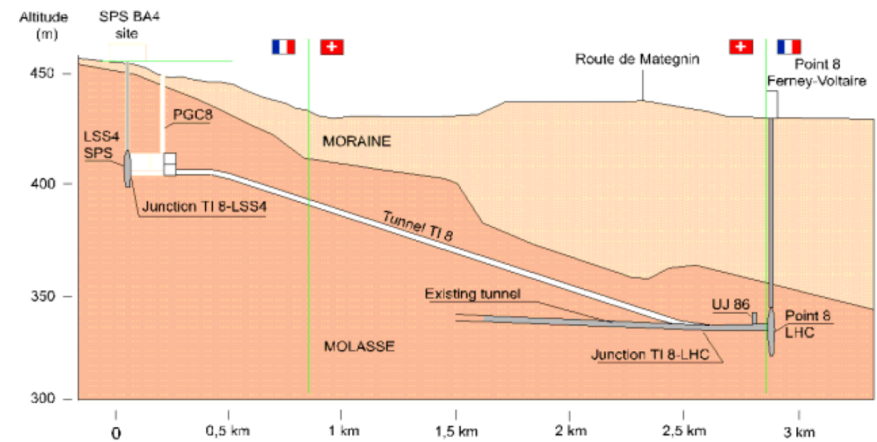
- Apertures of beam line elements define limitations for maximum  $\beta$  and dispersion values

$$\text{Envelope}(S) = \sqrt{\epsilon_{geo} \cdot \beta(S)} + \text{Dispersion}(S) \cdot \frac{\Delta p}{p} + \text{mechanical alignment} + \text{orbit error} \cdot \sqrt{\frac{\beta(S)}{\beta_{max}}}$$

- Minimum bend radius, maximum quadrupole gradient, magnet aperture, cost, geology or other obstacles, etc.
- Insertions for special equipment (like stripping foils)



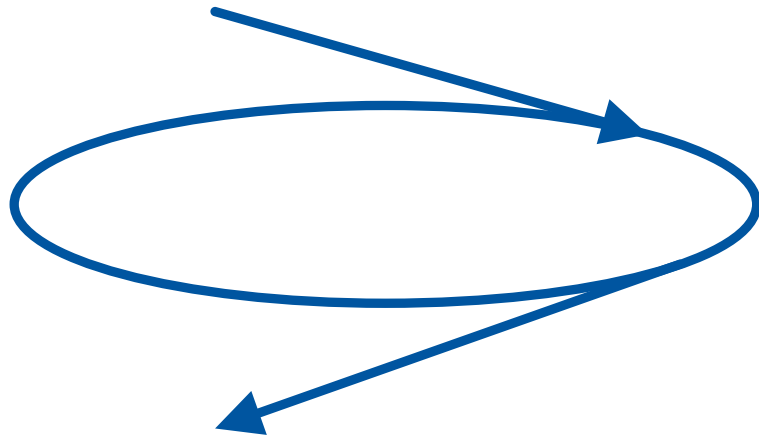
SPS to LHC transfer tunnel TI2 (Beam 1)



SPS to LHC transfer tunnel TI8 (Beam 2)



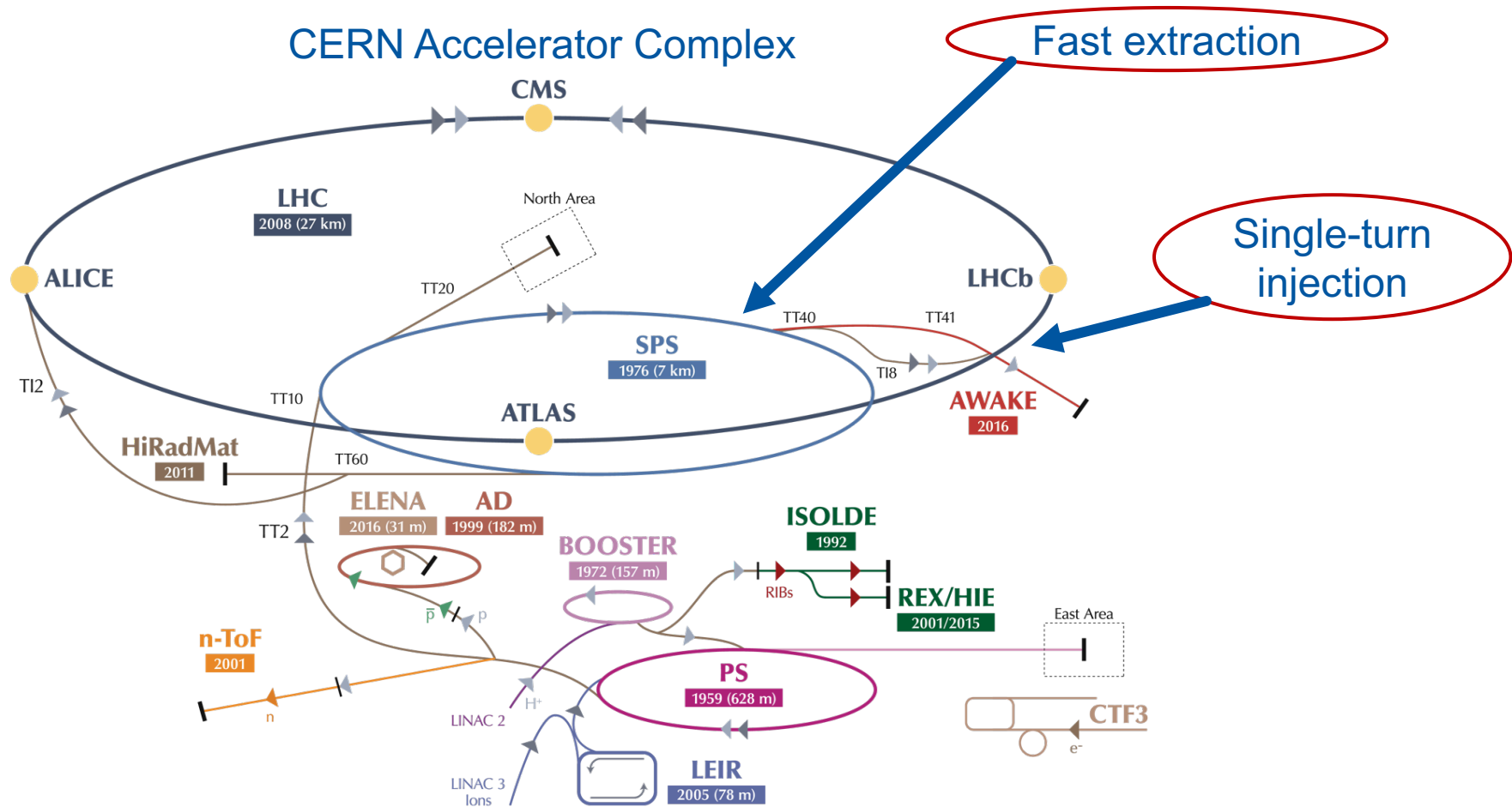
# Overview



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- **Single-turn methods**
  - **Injection**
  - **Fast extraction**
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  - Multi-turn hadron injection
  - Charge-exchange H- injection
  - Multi-turn extraction
- Resonant slow extraction
- Summary



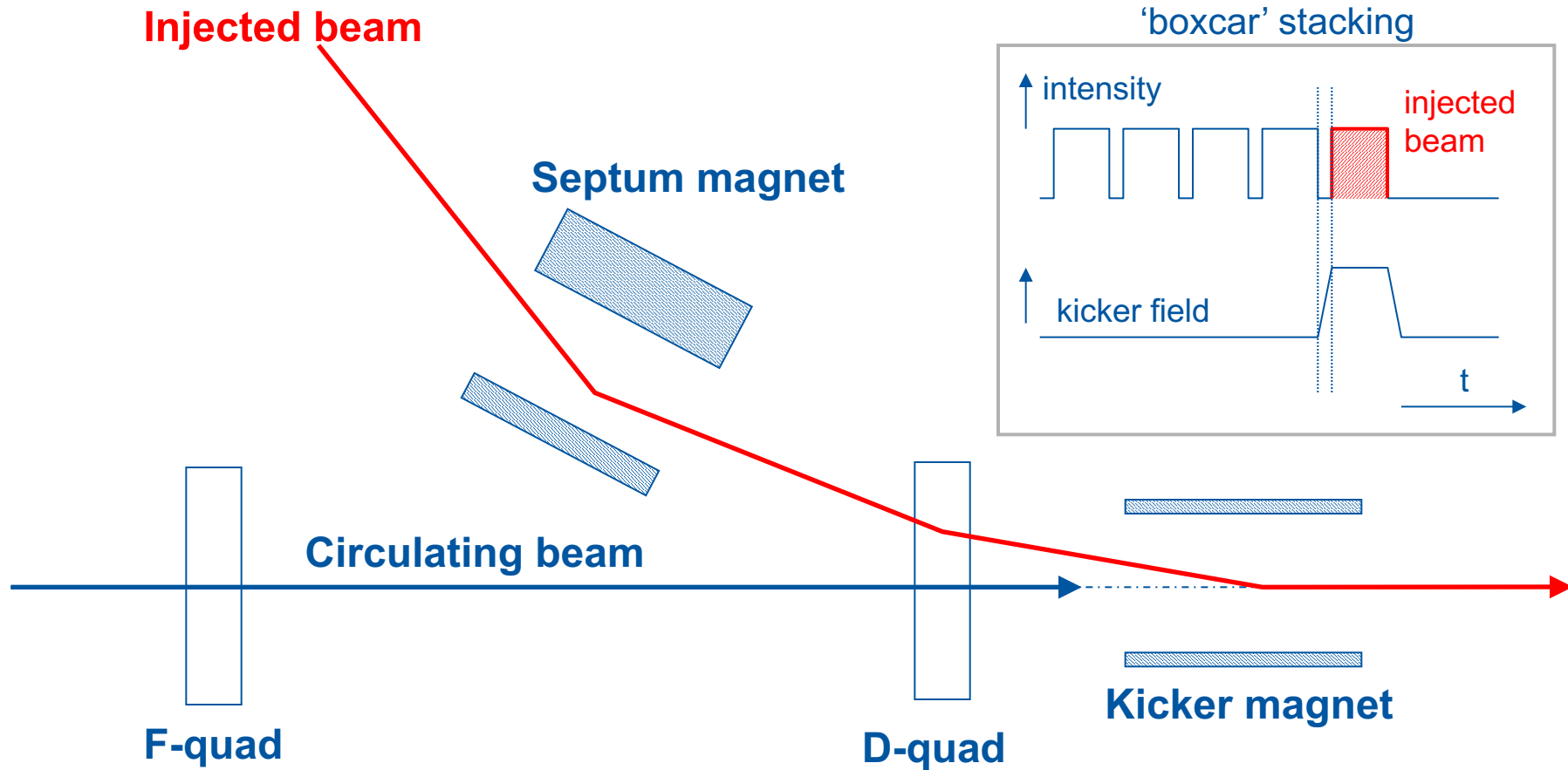
# Single-turn methods



Injection / extraction of a single bunch or a bunch train within one turn.



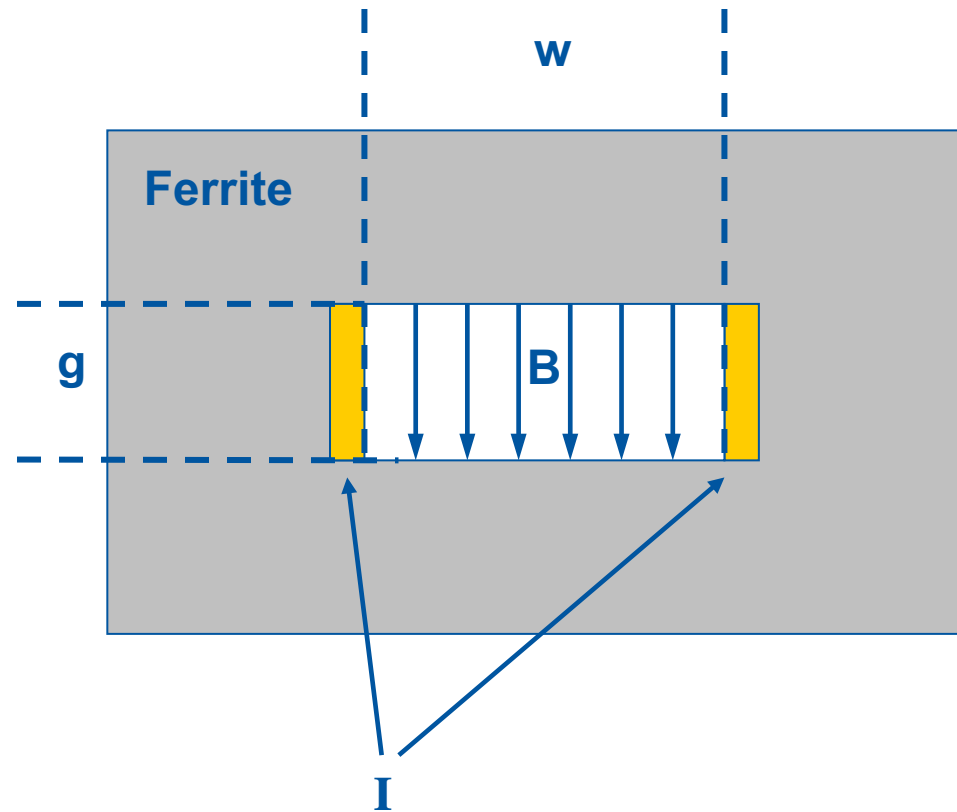
# Single-turn injection – same plane



- Septum deflects the beam onto the closed orbit at the centre of the kicker
- Kicker compensates for the remaining angle
- Septum and kicker either side of D quad to minimize kicker strength

# Kicker magnet

- Pulsed magnet with very fast rise time (100 ns – few  $\mu$ s)
- Typically 3 kA in 1  $\mu$ s rise time



$$B = \mu_0 I / g$$

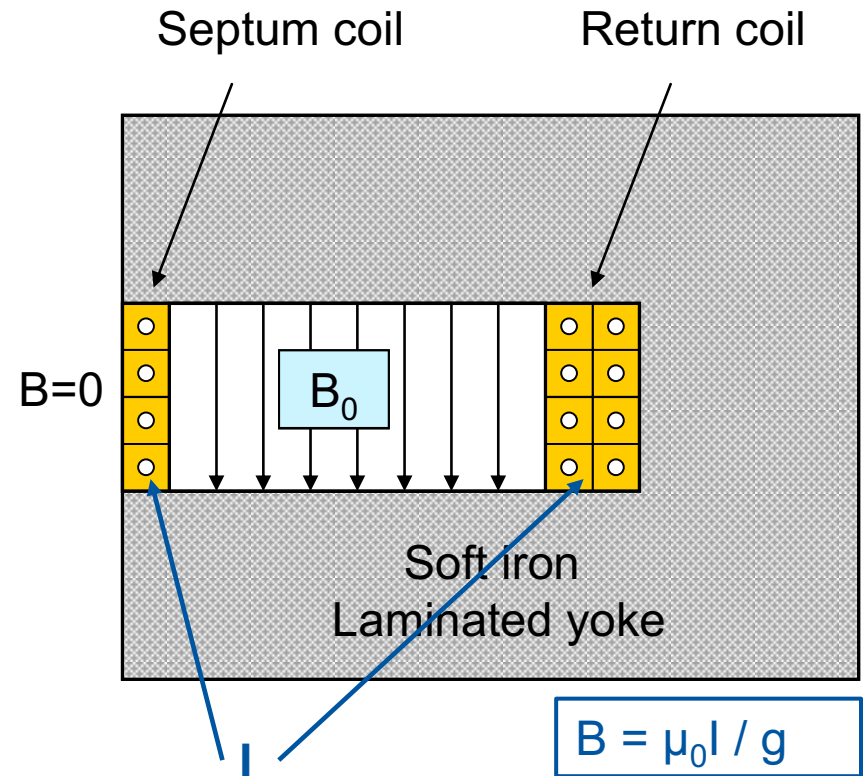
$$L \text{ [per unit length]} = \mu_0 w / g$$

$$dI/dt = V / L$$

Example – SPS fast extraction  
5 kicker with 0.5 mrad total deflection

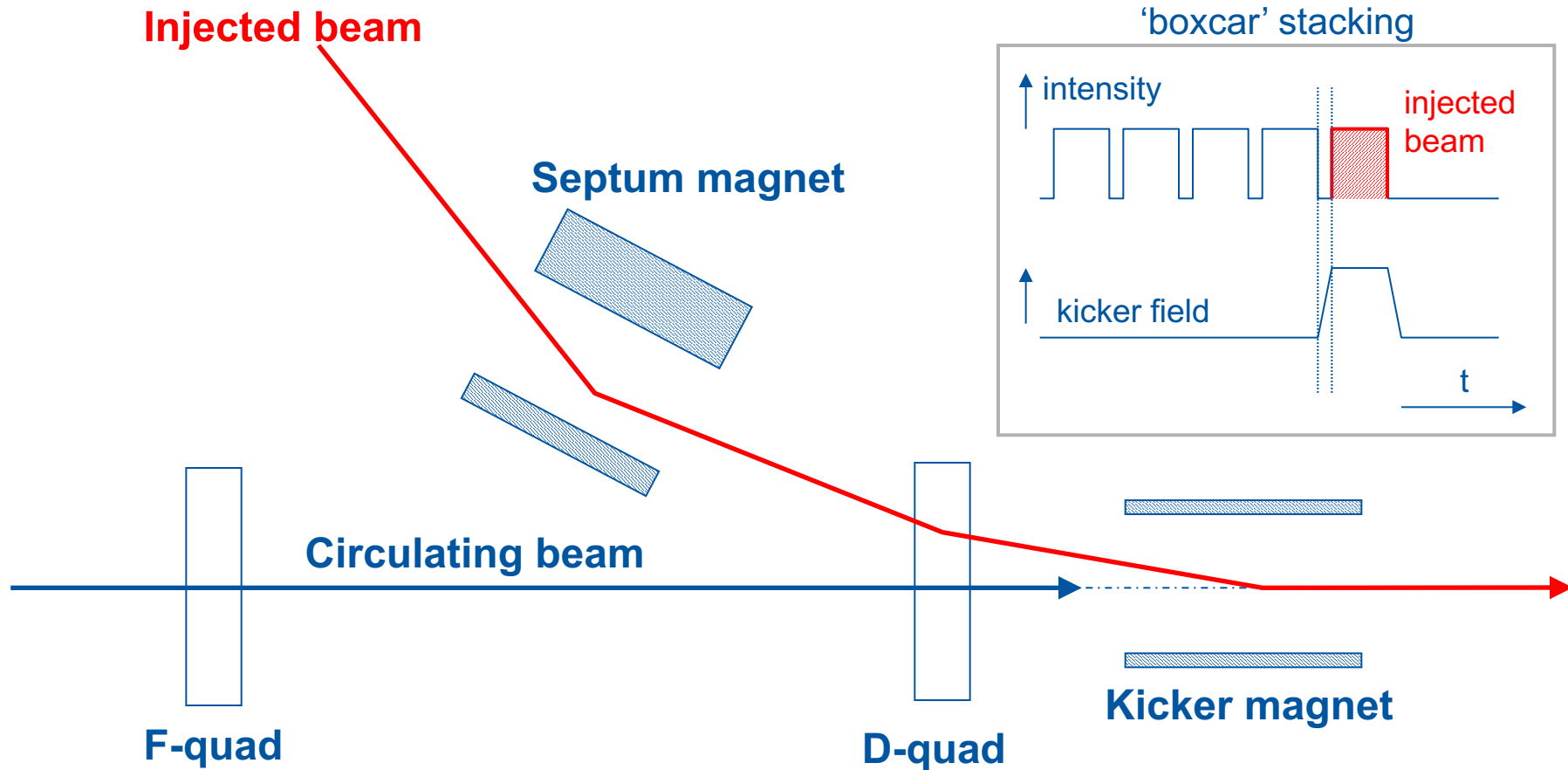
# Magnetic septum

- Pulsed or DC magnet with thin (2 – 20 mm) Septum between zero field and high field region
- Typically
  - ~10x more deflection given by magnetic septa, compared to kickers
  - $I \sim 5 - 25 \text{ kA}$



Example – SPS fast extraction  
2.25 mrad total deflection

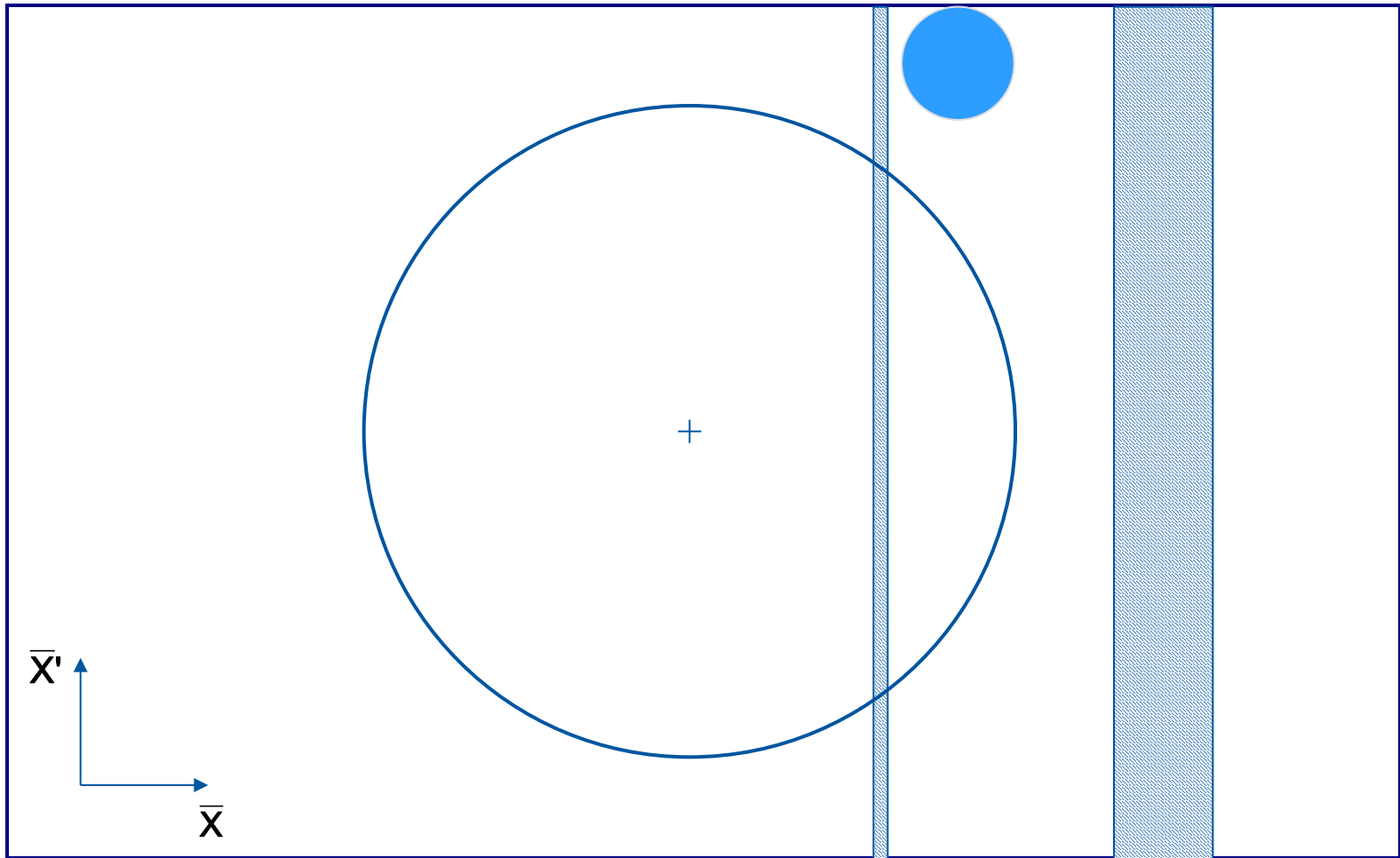
# Single-turn injection – same plane



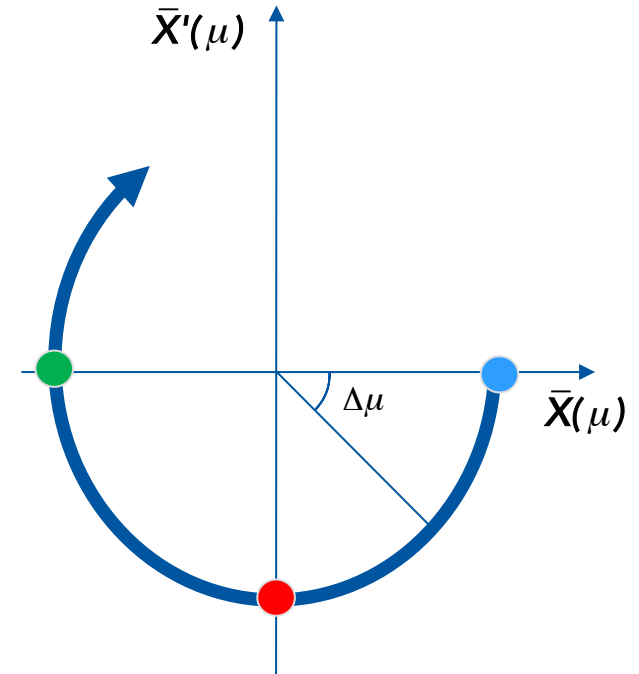
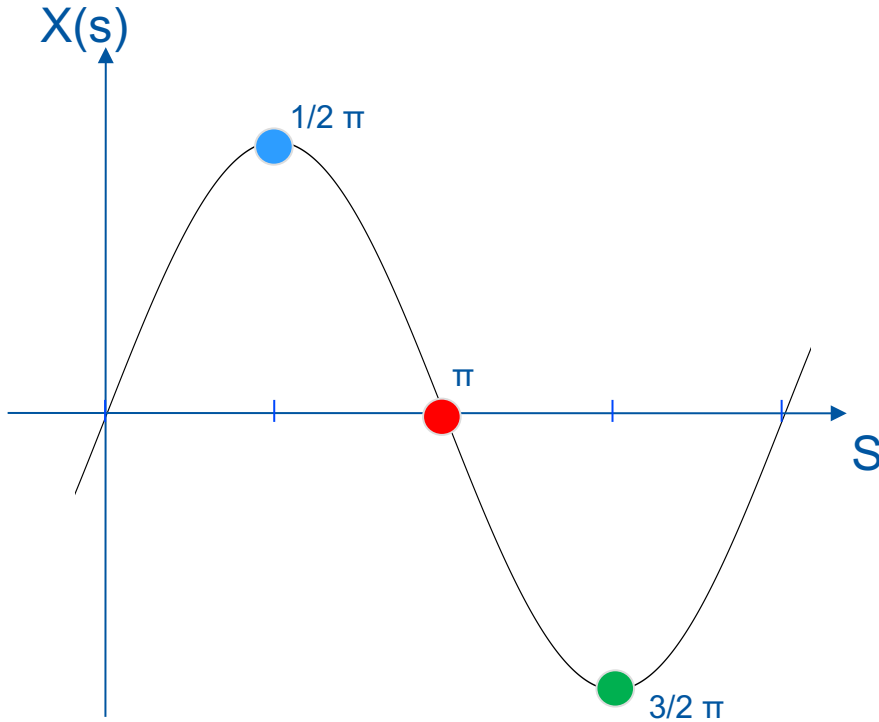
- Septum deflects the beam onto the closed orbit at the centre of the kicker
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# Single-turn injection

Normalised phase space at centre of idealised septum

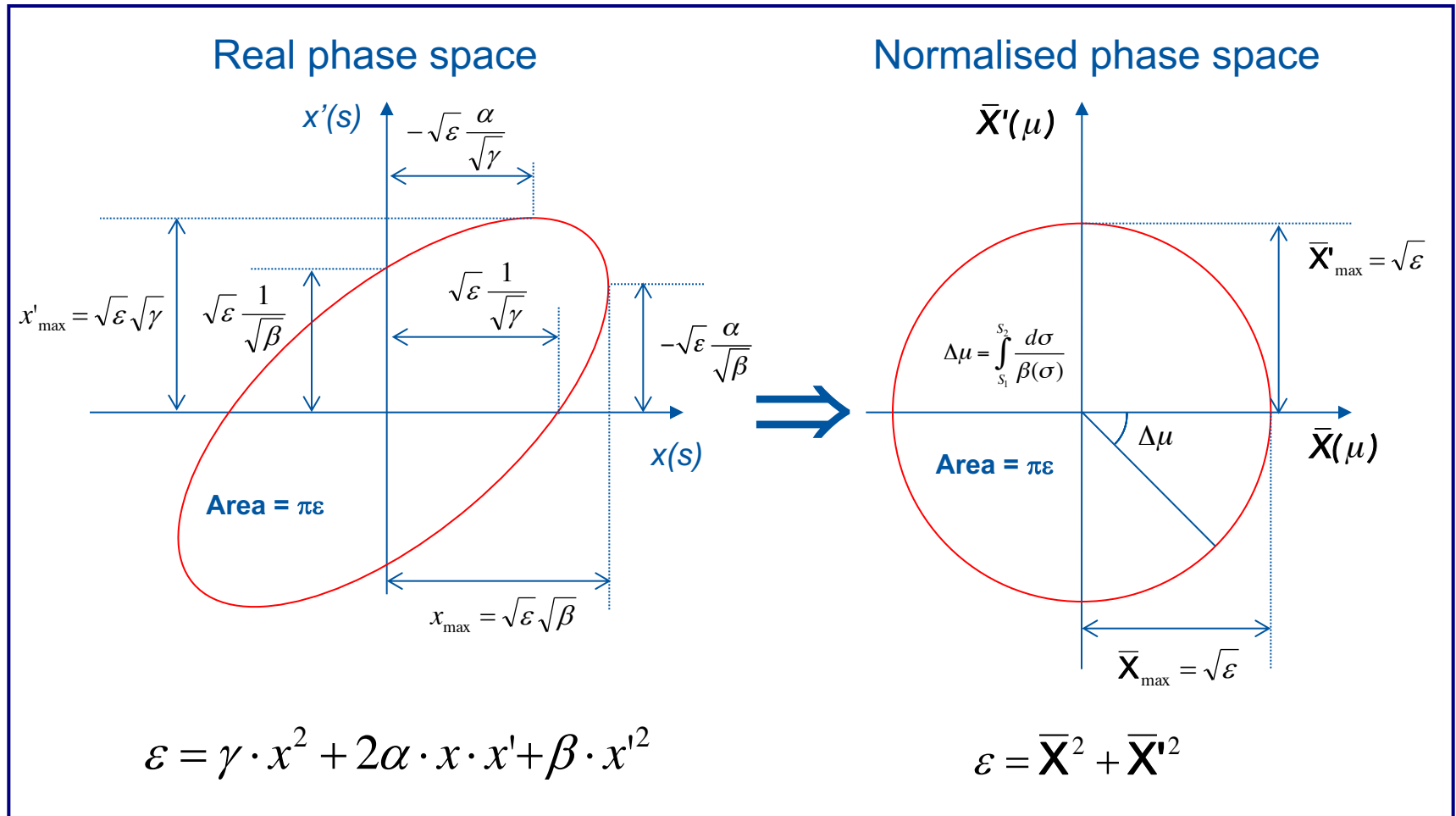


# Normalised phase space



An oscillation in the longitudinal coordinate  $S$  can be translated into a rotation in phase.

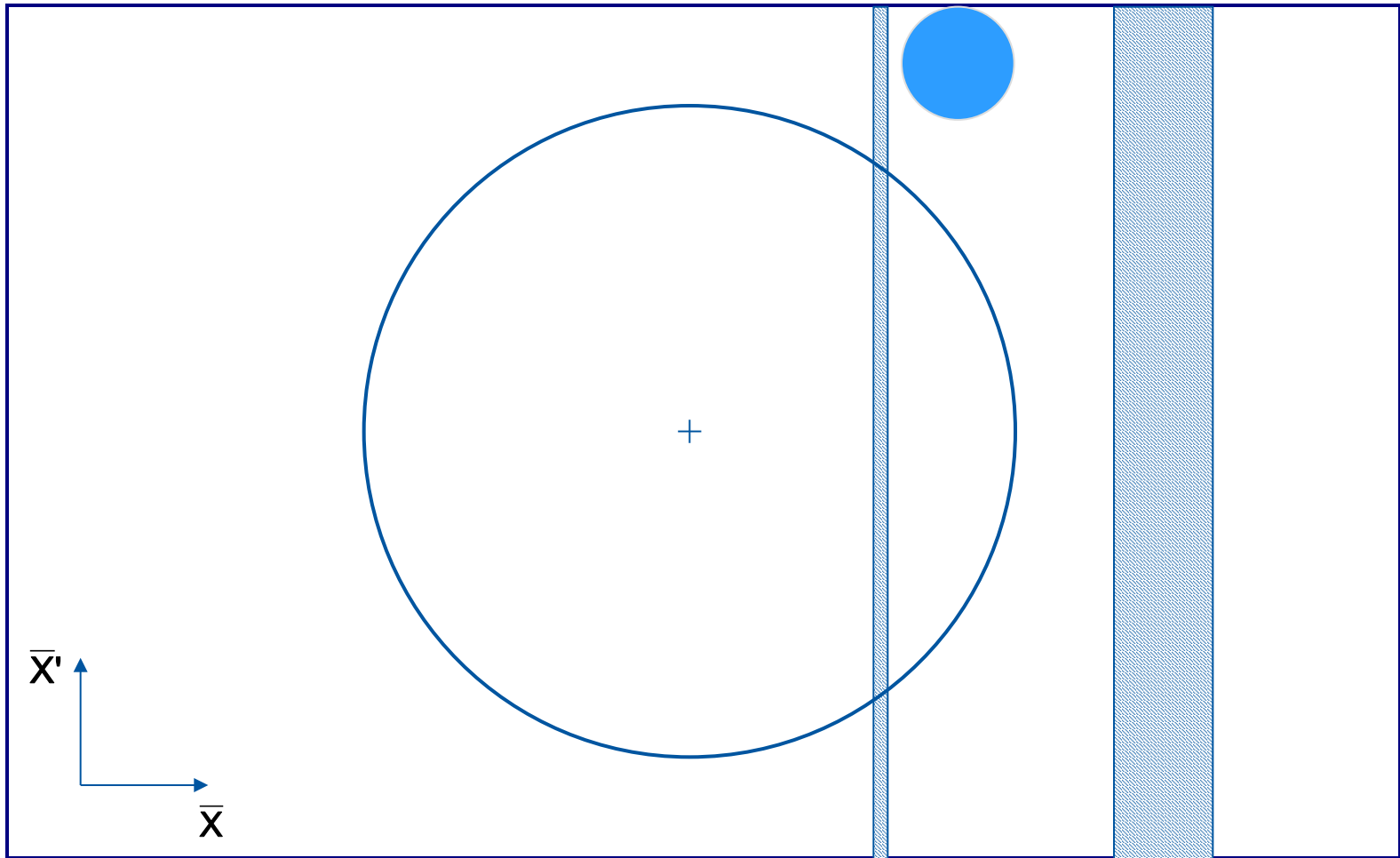
# Normalised phase space





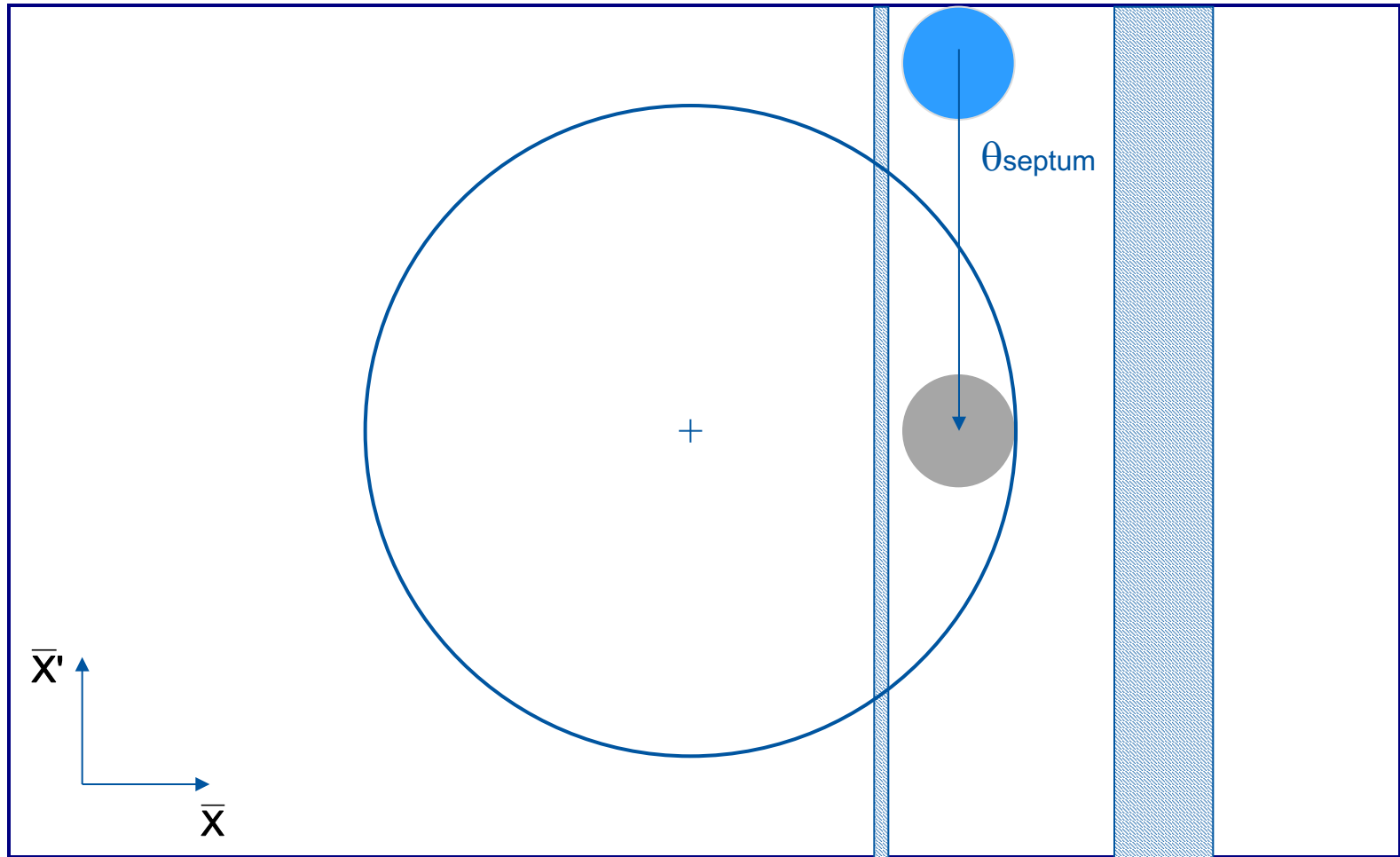
# Single-turn injection

Normalised phase space at centre of idealised septum



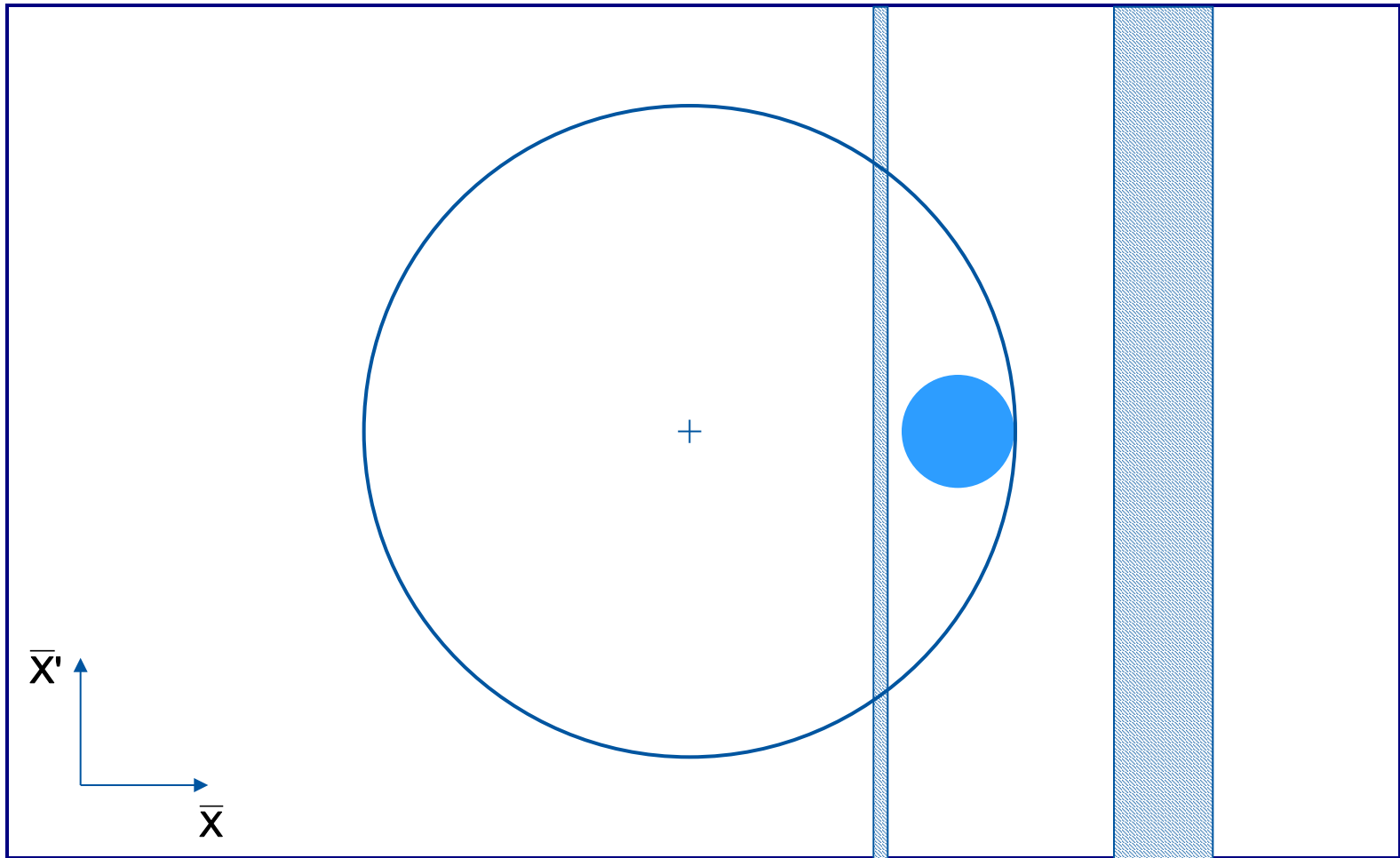
# Single-turn injection

Normalised phase space at centre of idealised septum



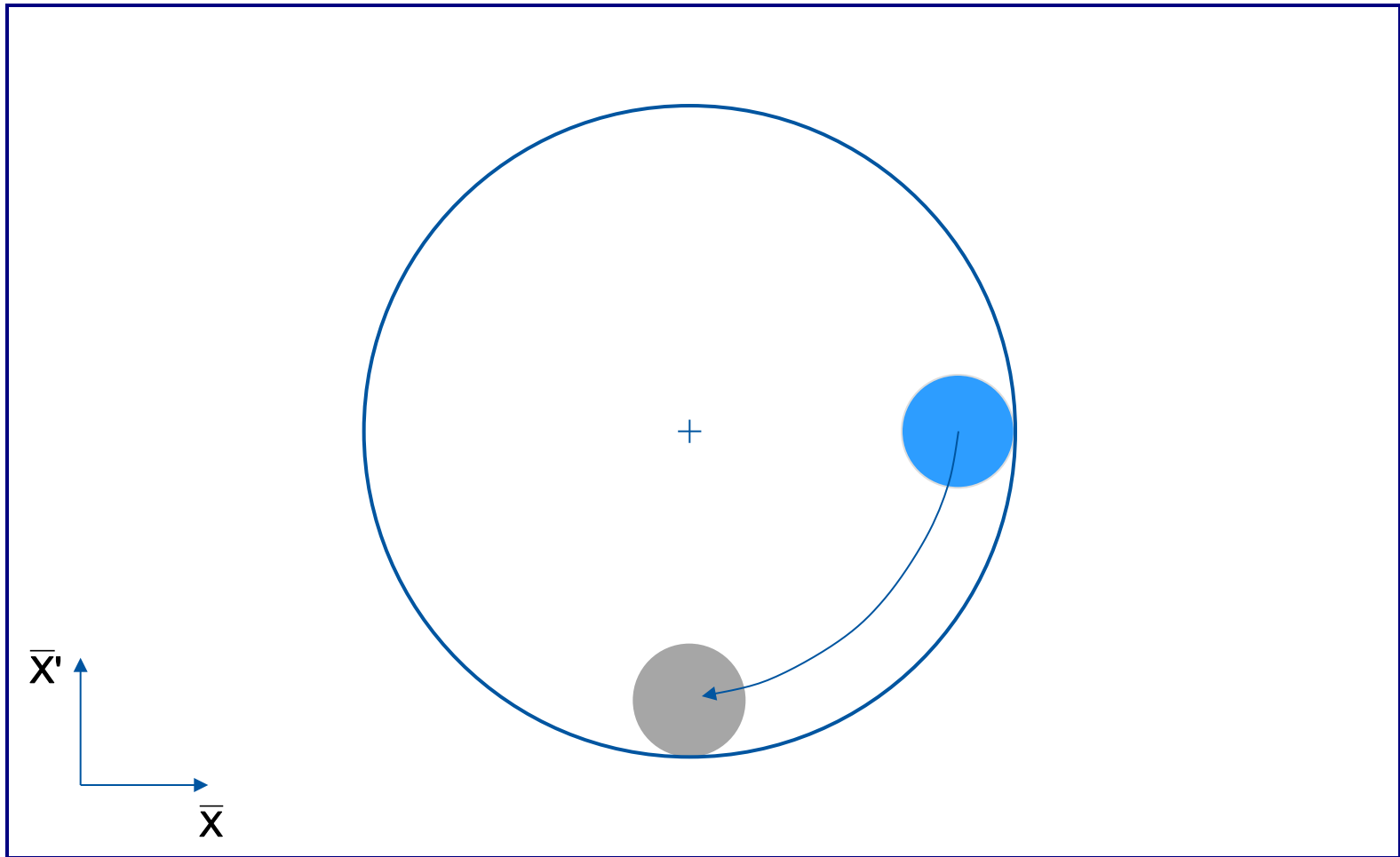
# Single-turn injection

Normalised phase space at centre of idealised septum



# Single-turn injection

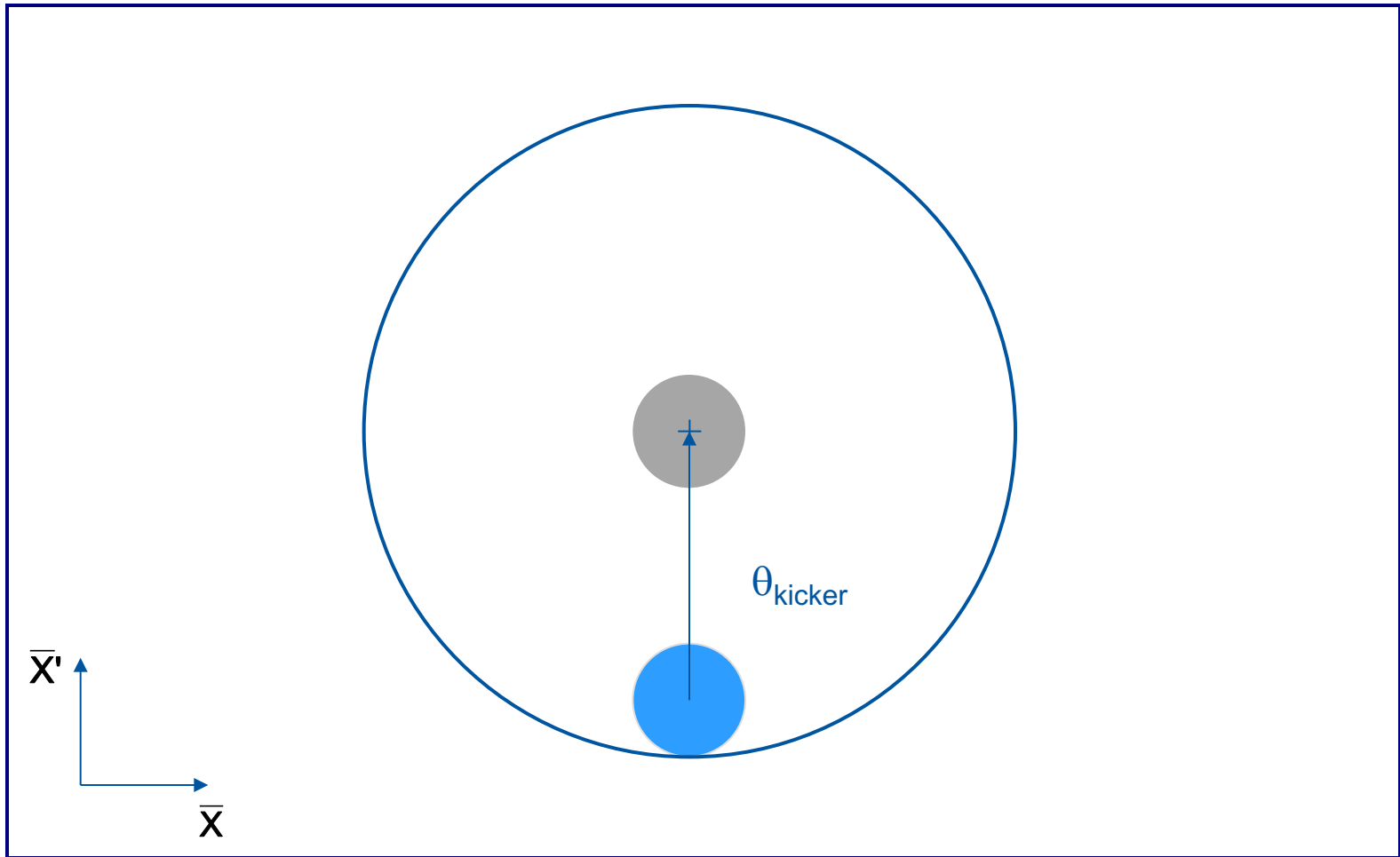
$\pi/2$  phase advance to kicker location



# Single-turn injection

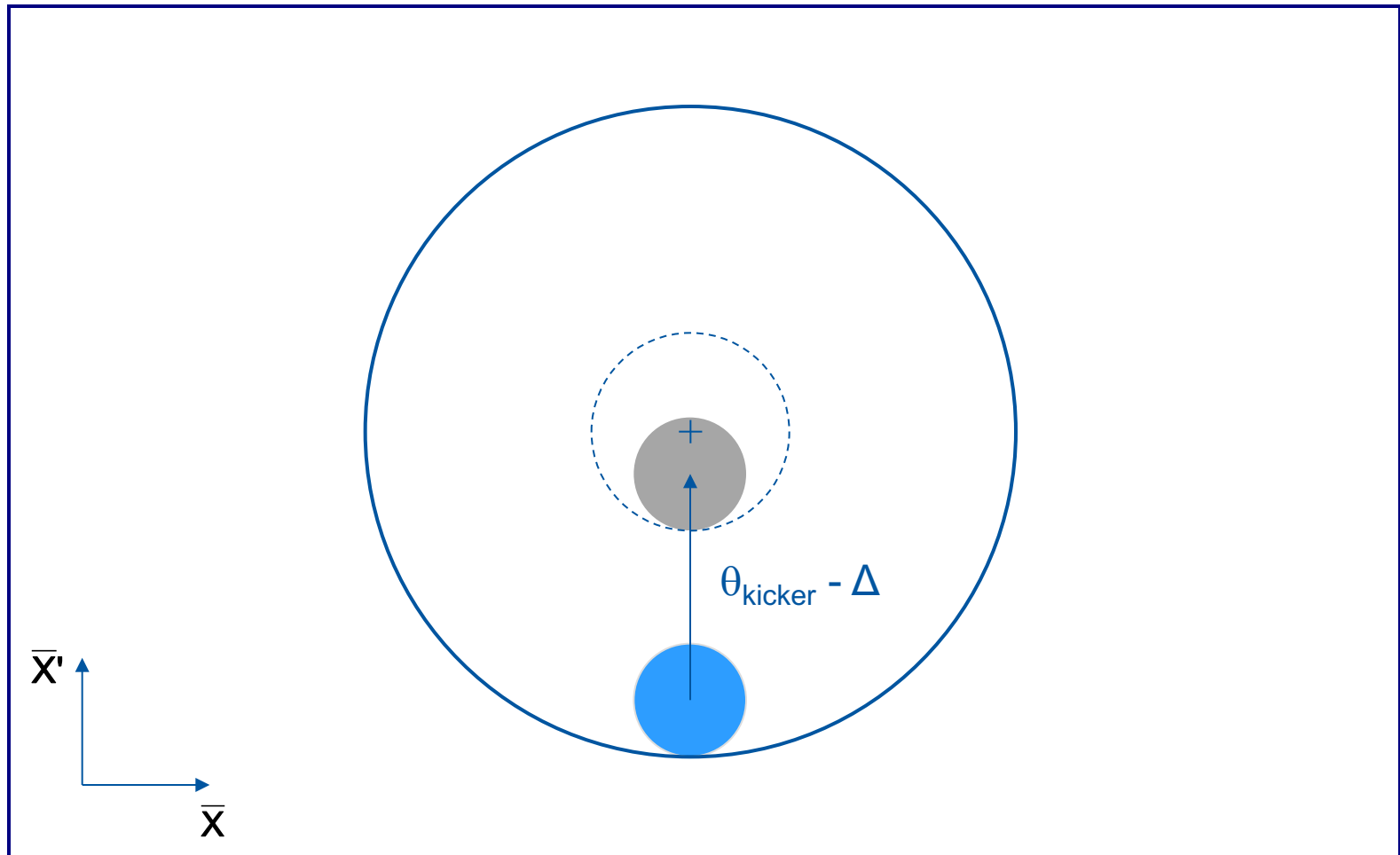
Normalised phase space at centre of idealised septum

Kicker deflection places beam on central orbit:



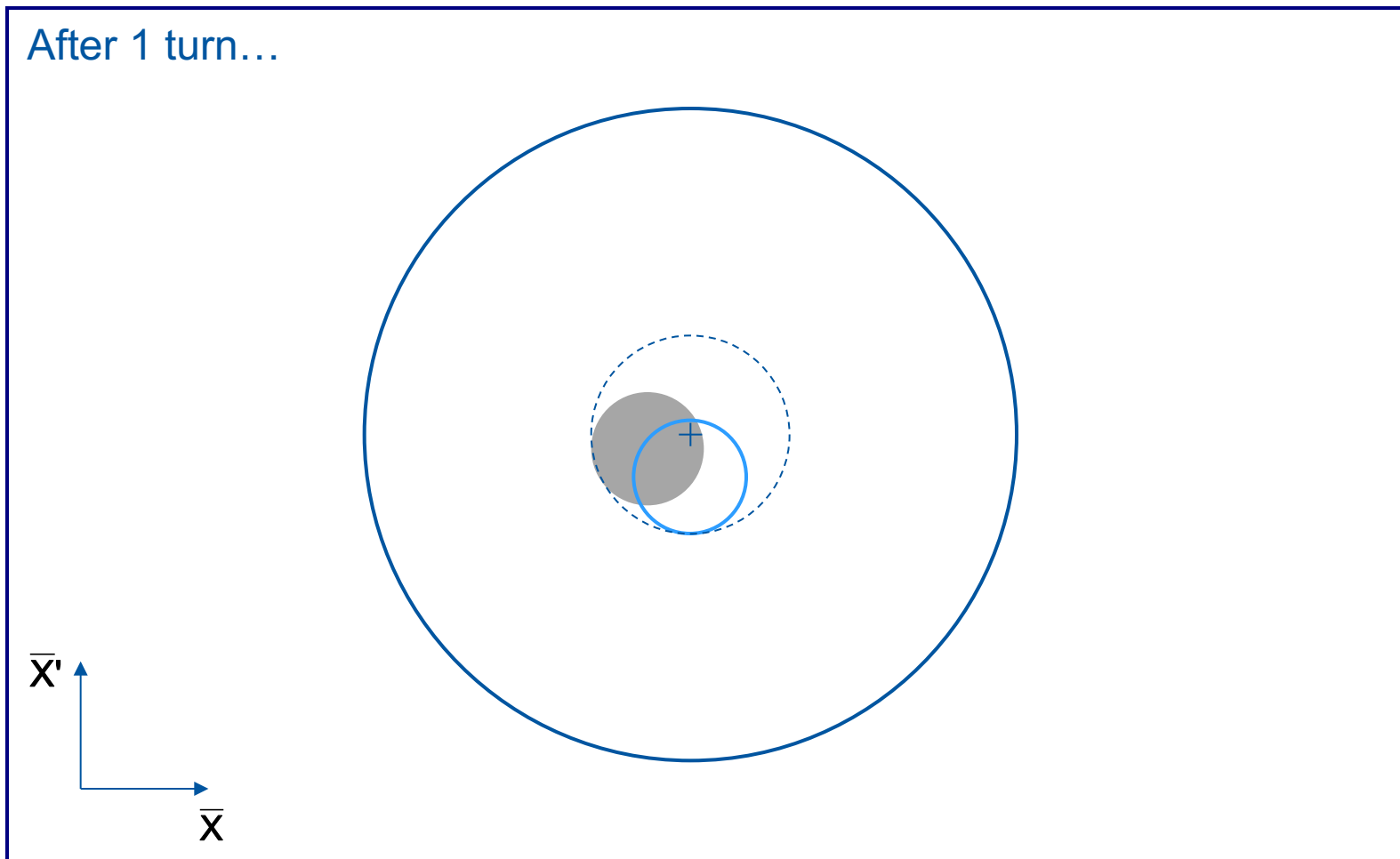
# Injection oscillations

For imperfect injection the beam oscillates around the central orbit, e.g. kick error,  $\Delta$ :



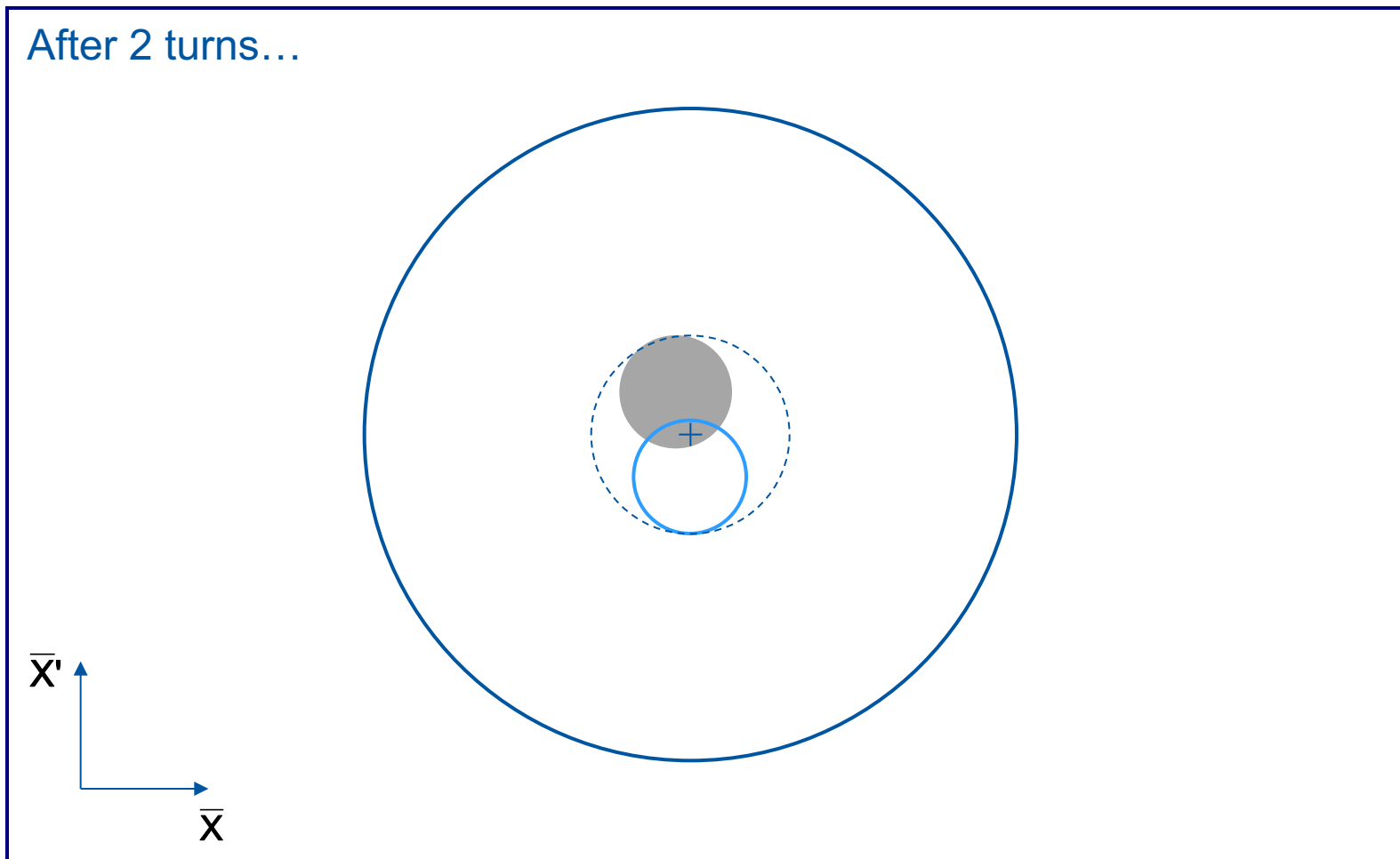
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# Injection oscillations

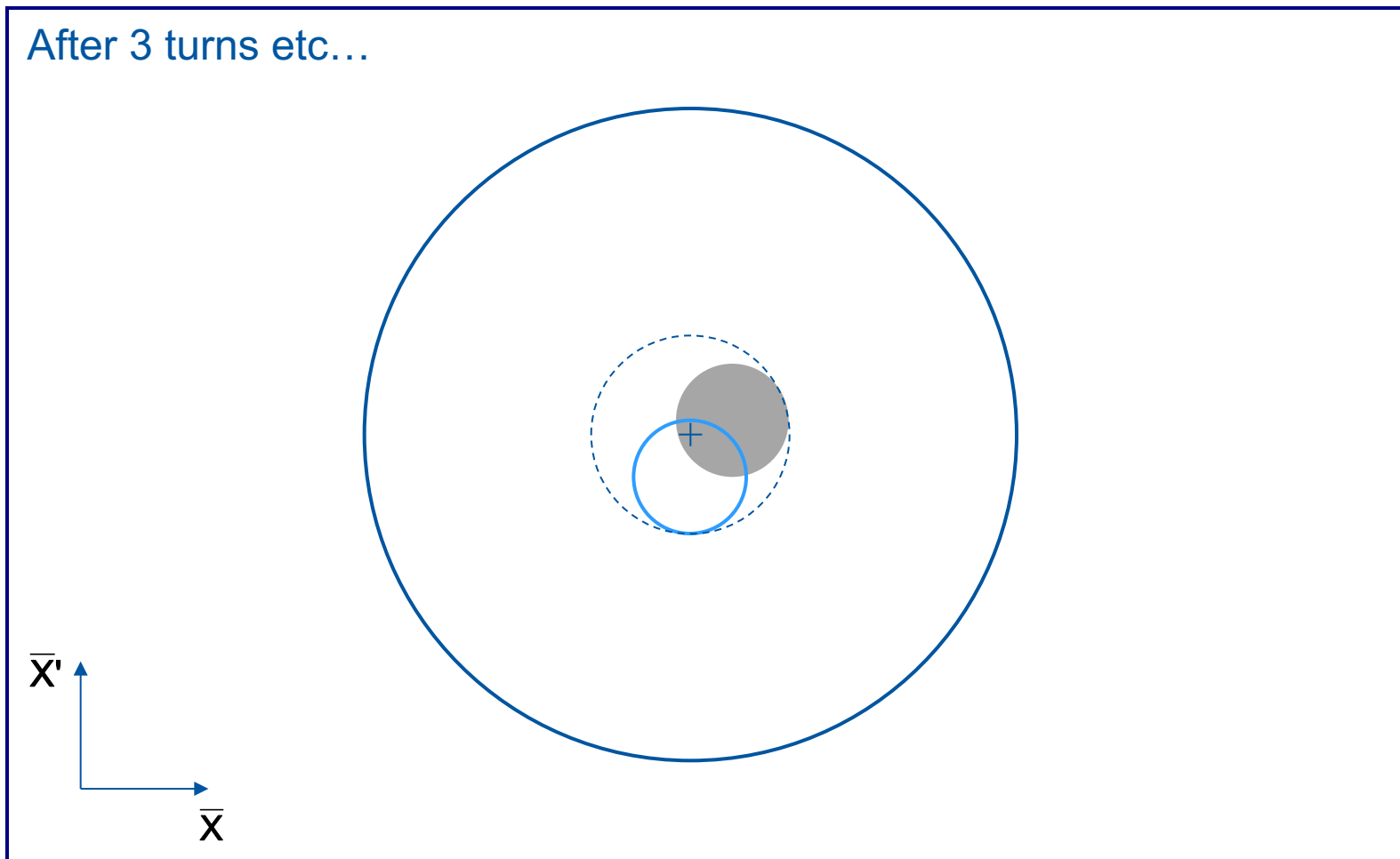
For imperfect injection the beam oscillates around the central orbit, e.g. kick error,  $\Delta$ :





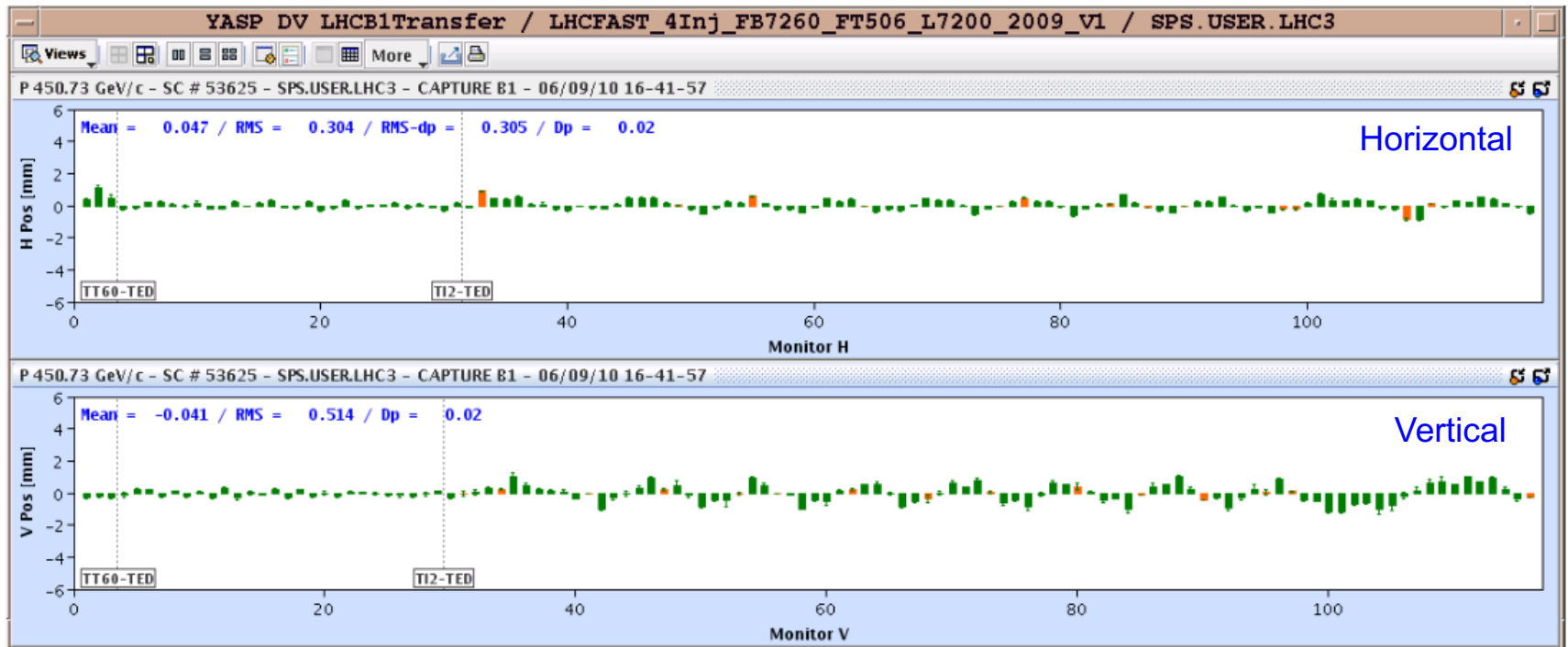
# Injection oscillations

For imperfect injection the beam oscillates around the central orbit, e.g. kick error,  $\Delta$ :



# Injection oscillations

Betatron oscillations with respect to the Closed Orbit:



Transfer line

LHC (first turn)

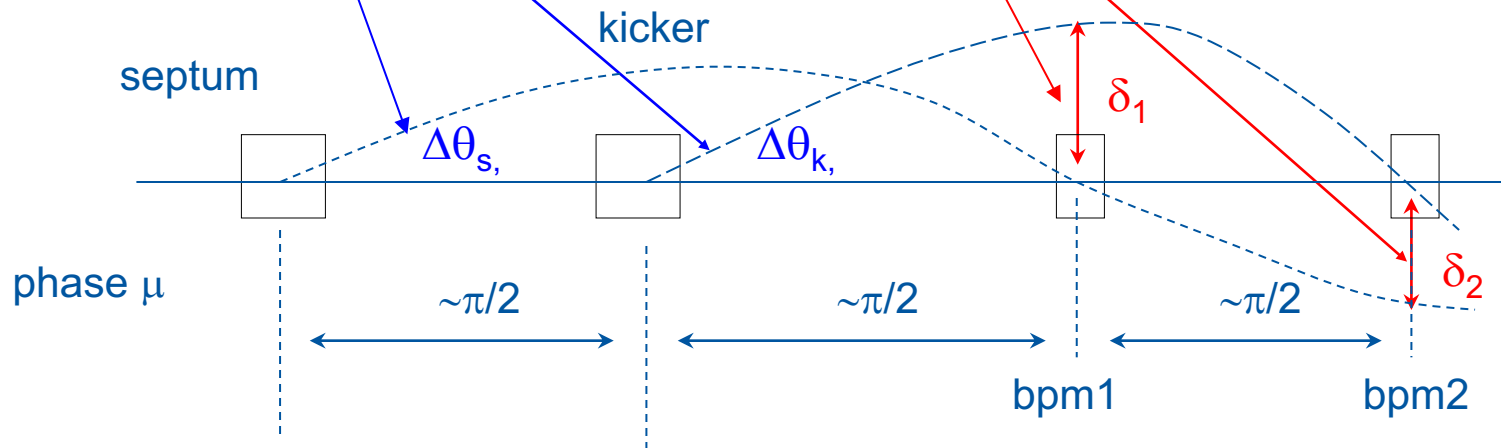
# Injection errors

Angle errors

$$\Delta\theta_{s,k}$$

Measured  
Displacements

$$\delta_{1,2}$$



$$\delta_1 = \Delta\theta_s \sqrt{\beta_s\beta_1} \sin(\mu_1 - \mu_s) + \Delta\theta_k \sqrt{\beta_k\beta_1} \sin(\mu_1 - \mu_k)$$

$$\approx \Delta\theta_k \sqrt{\beta_k\beta_1}$$

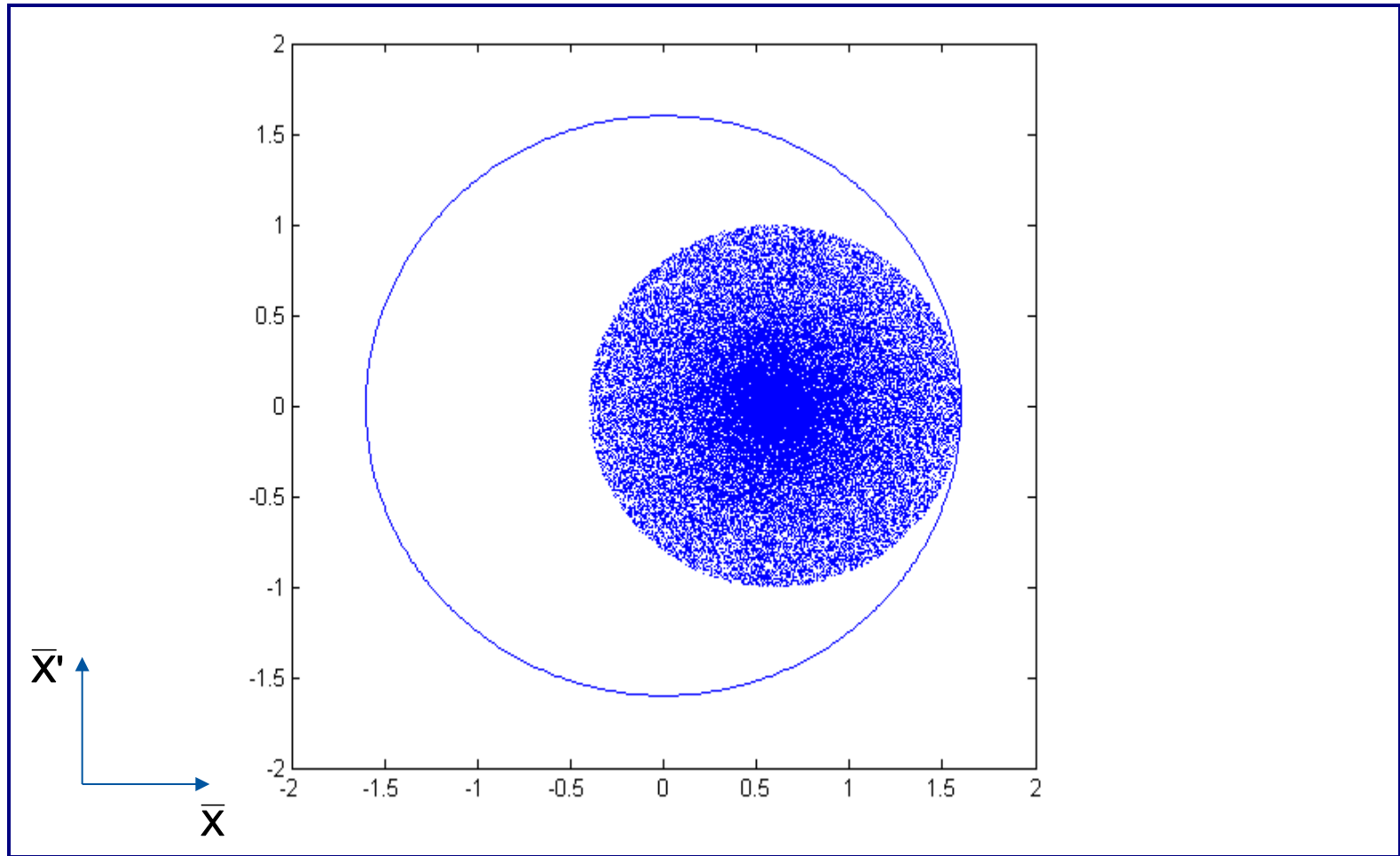
$$\delta_2 = \Delta\theta_s \sqrt{\beta_s\beta_2} \sin(\mu_2 - \mu_s) + \Delta\theta_k \sqrt{\beta_k\beta_2} \sin(\mu_2 - \mu_k)$$

$$\approx -\Delta\theta_s \sqrt{\beta_s\beta_2}$$

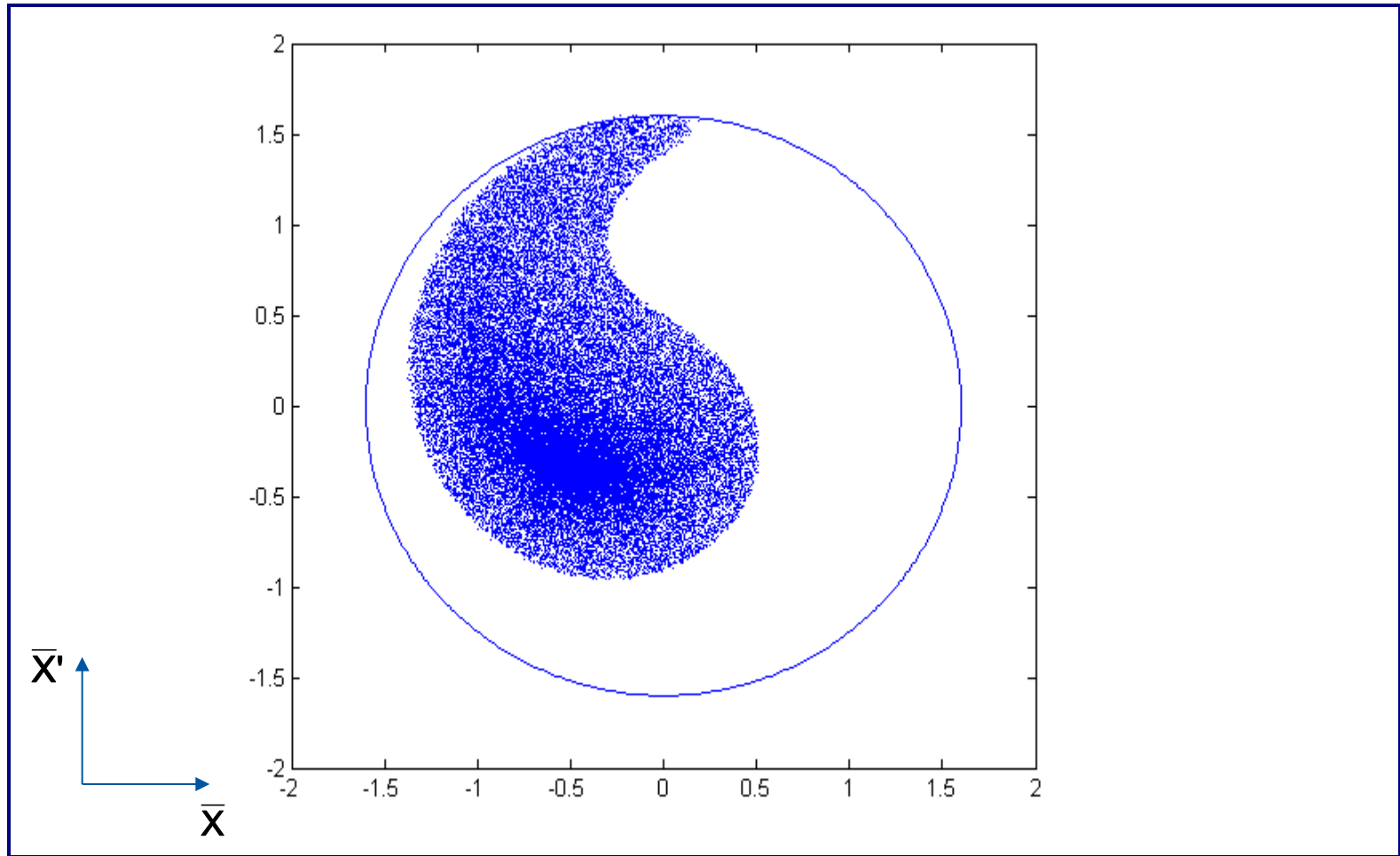
# Filamentation

- **Non-linear effects** (e.g. higher-order field components) introduce amplitude-dependent effects into particle motion.
- Over many turns, a phase-space oscillation is transformed into an emittance increase.
- So any residual transverse oscillation will lead to an emittance blow-up through filamentation
- Remark:
  - Chromaticity coupled with a non-zero momentum spread at injection can also cause filamentation, often termed *chromatic decoherence*.
  - “Transverse damper” systems are used to damp injection oscillations - bunch position measured by a pick-up, which is linked to a kicker

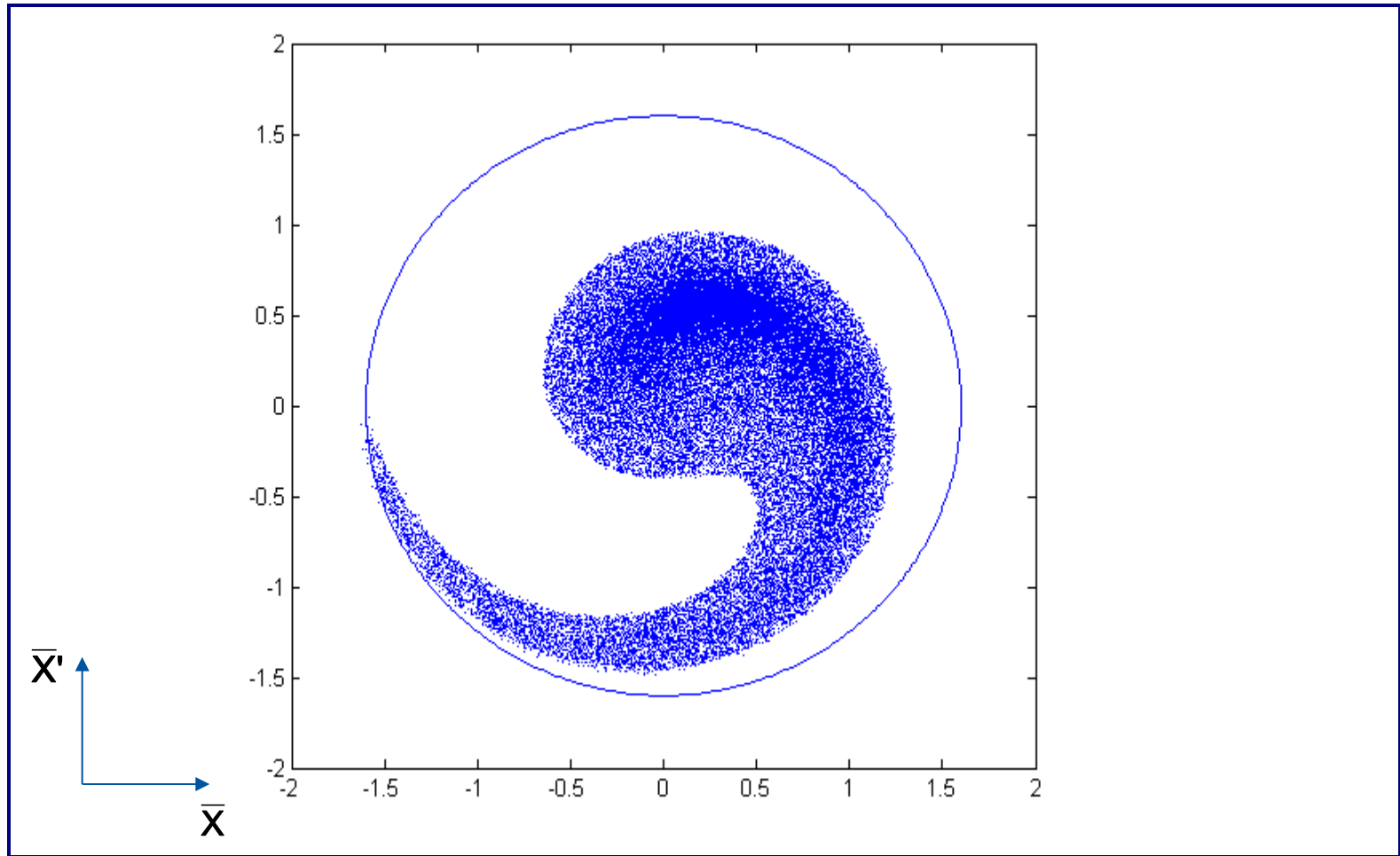
# Filamentation



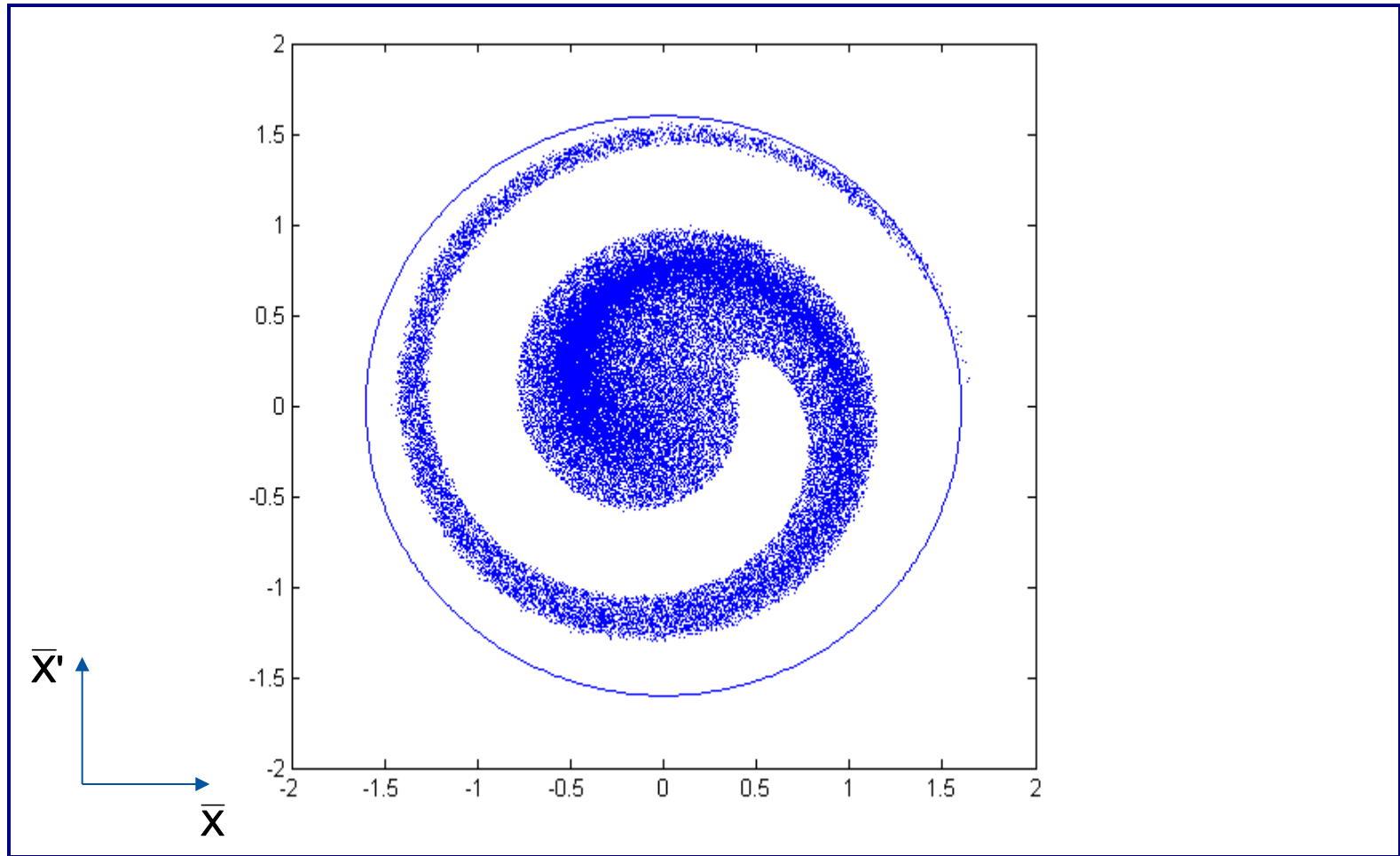
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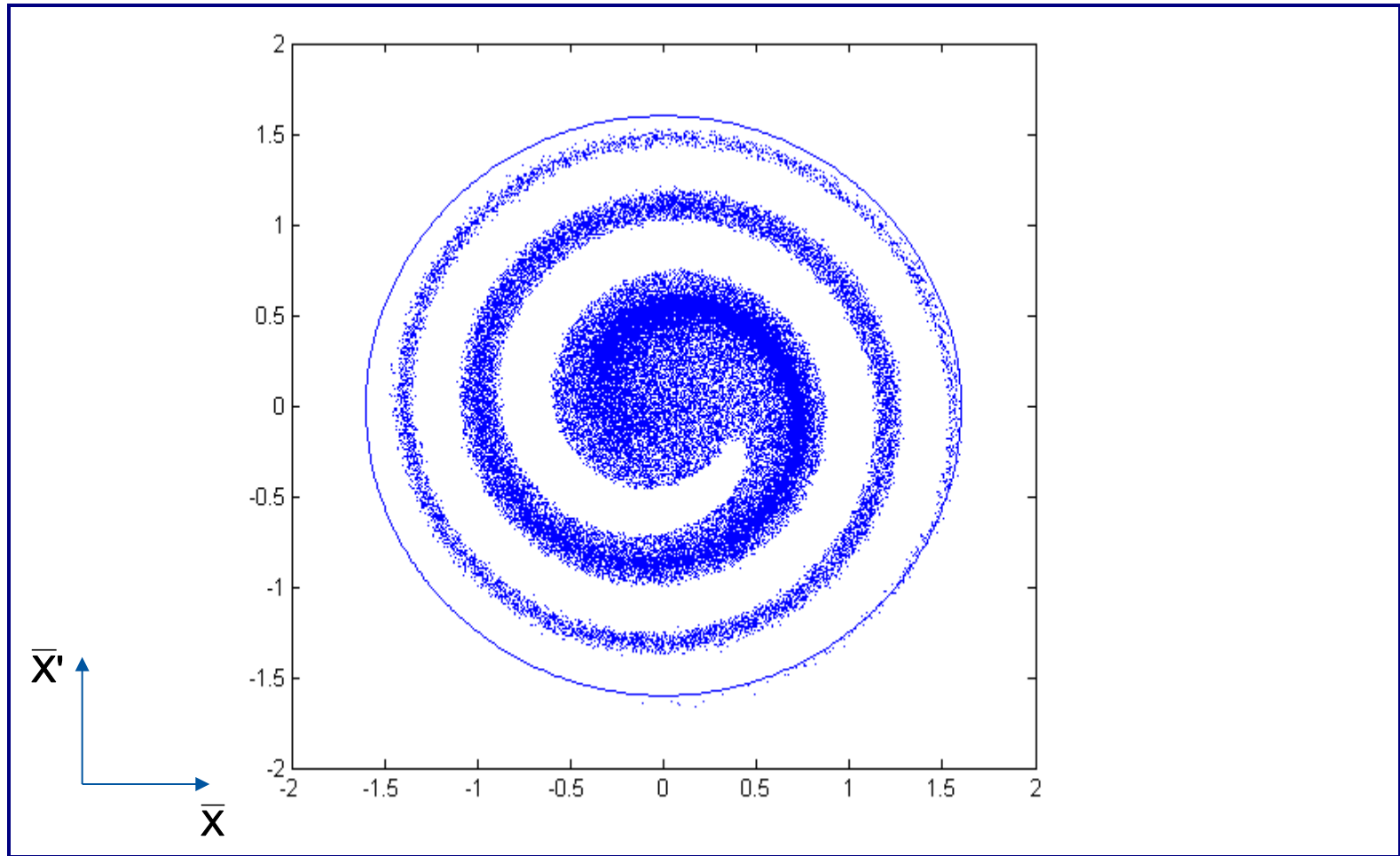


# Filamentation

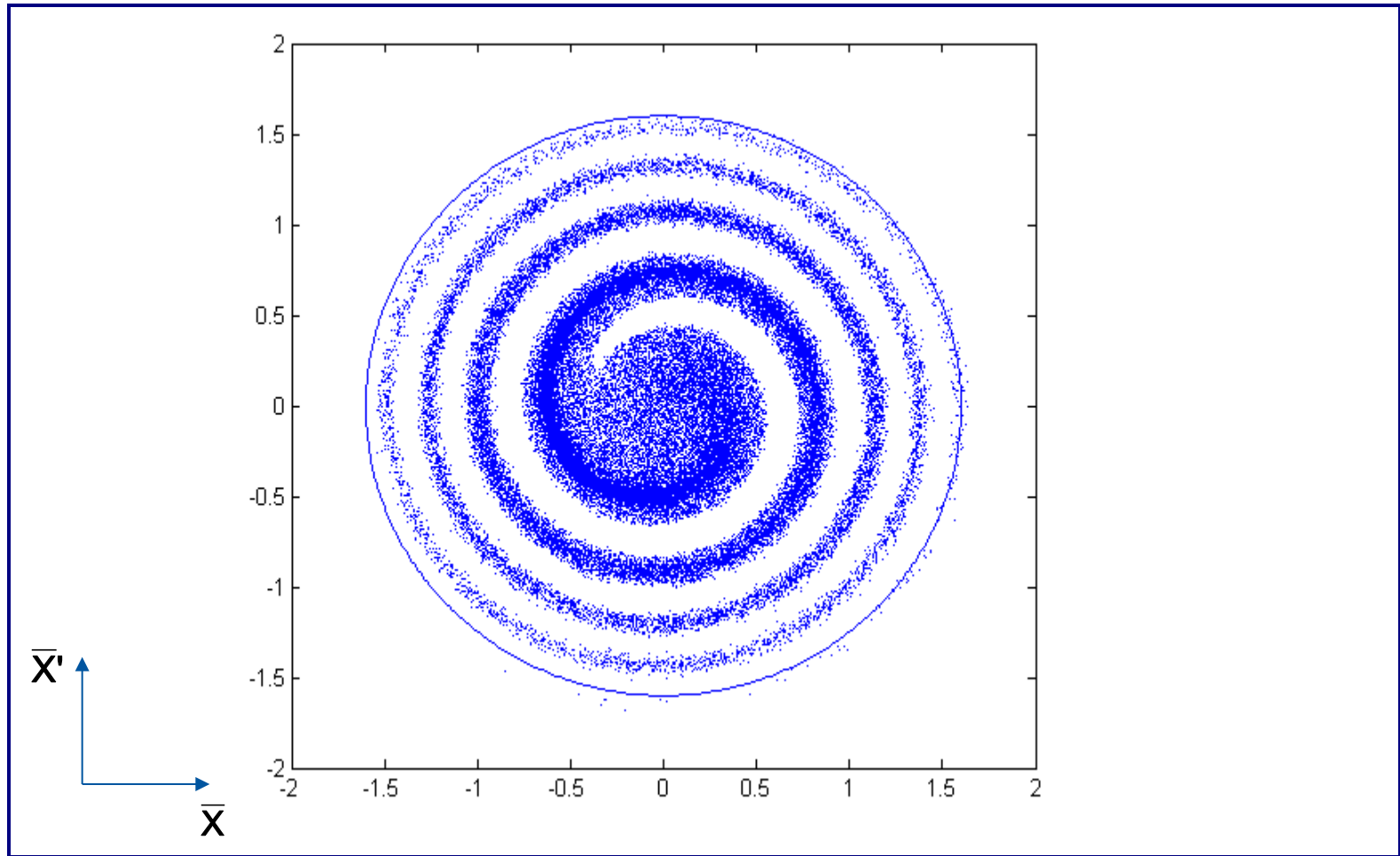




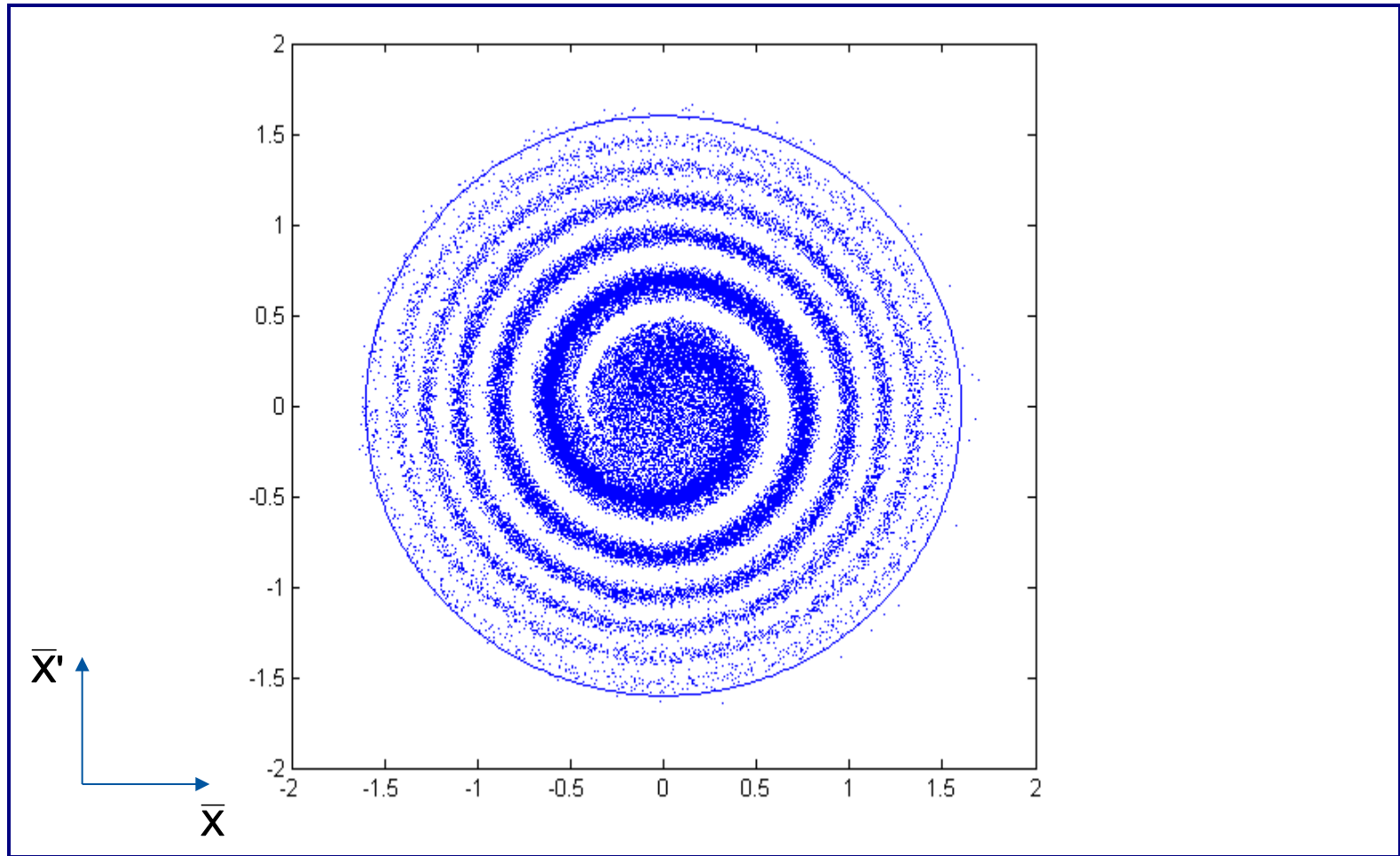
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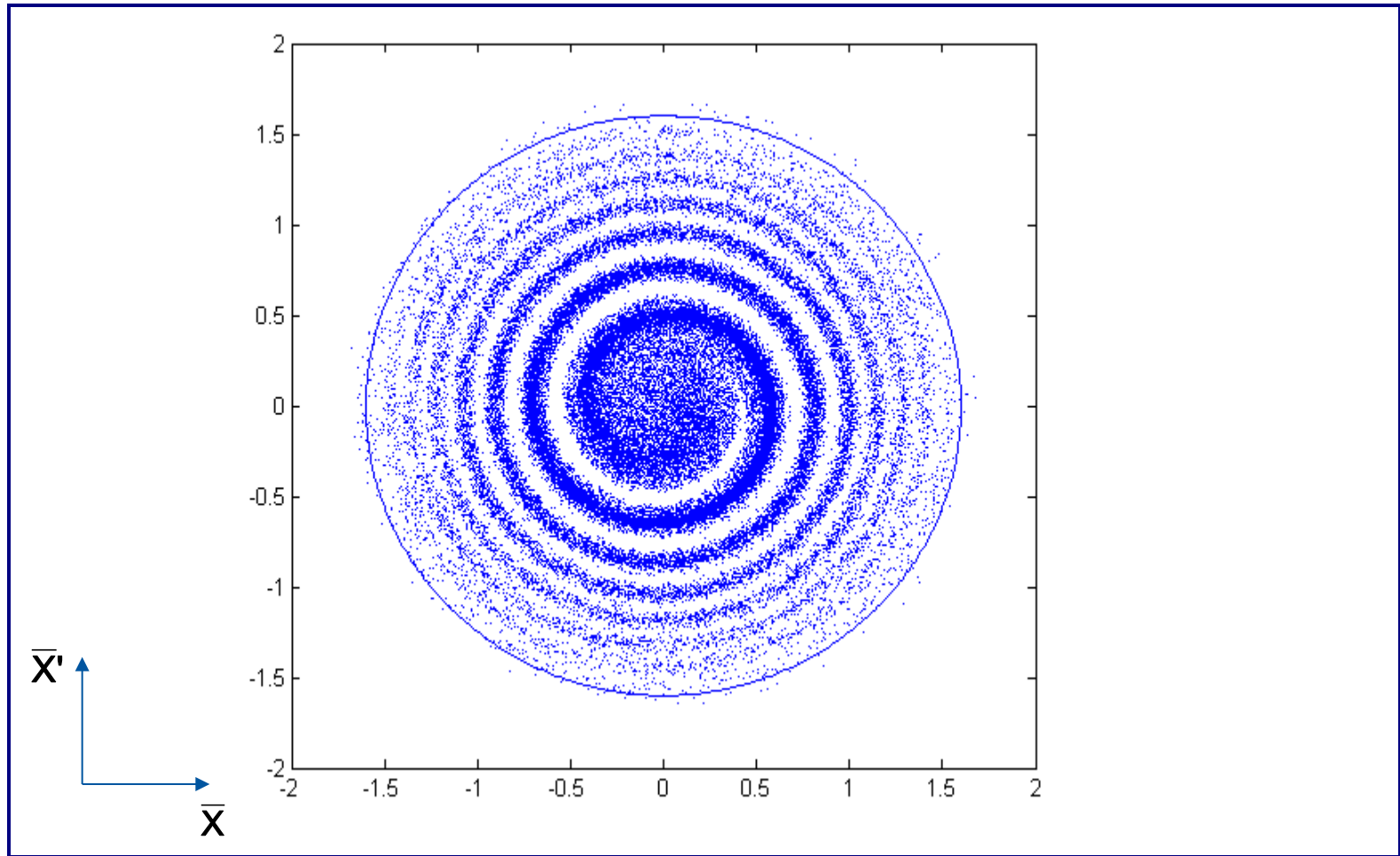
# Filamentation



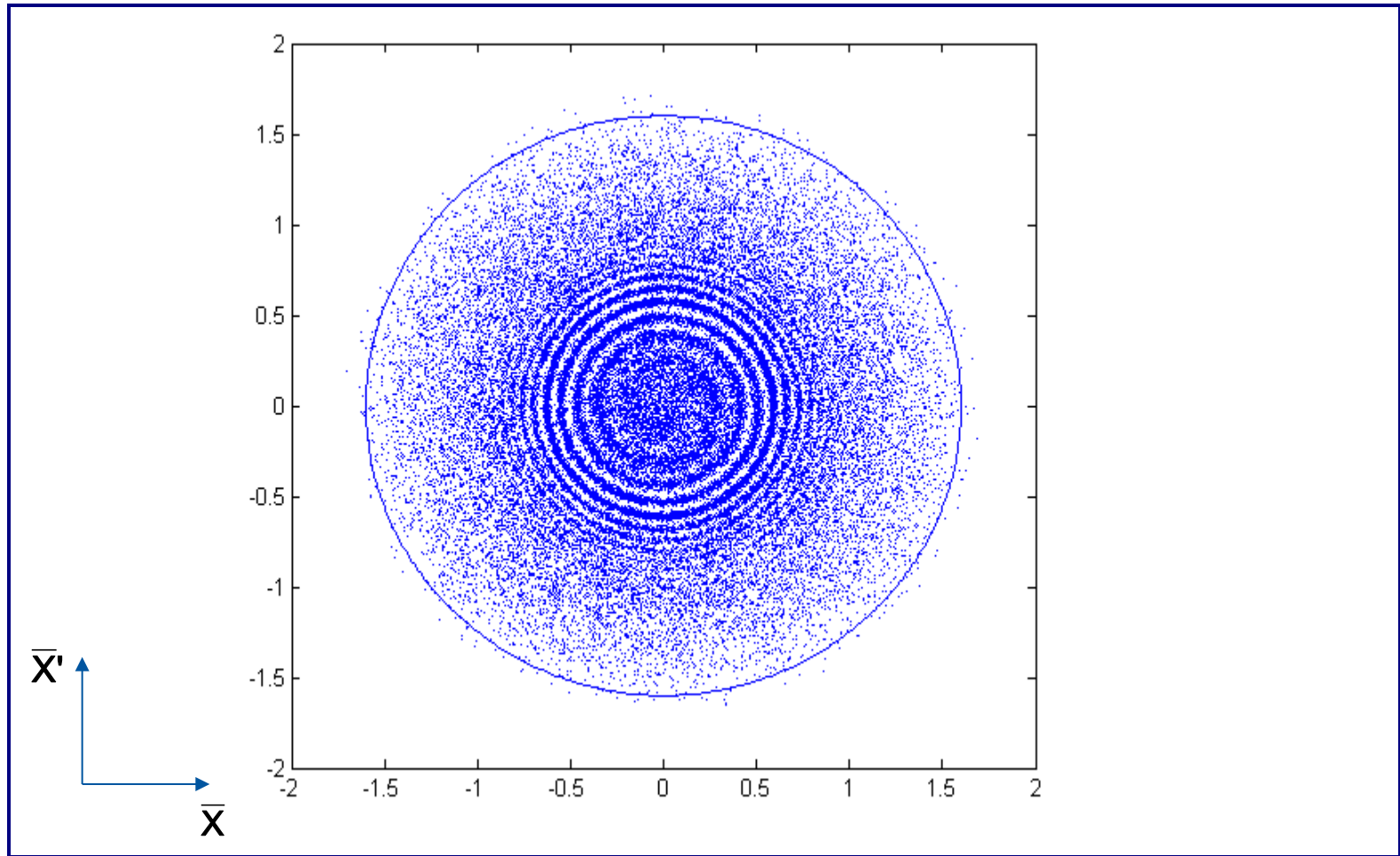
# Filamentation



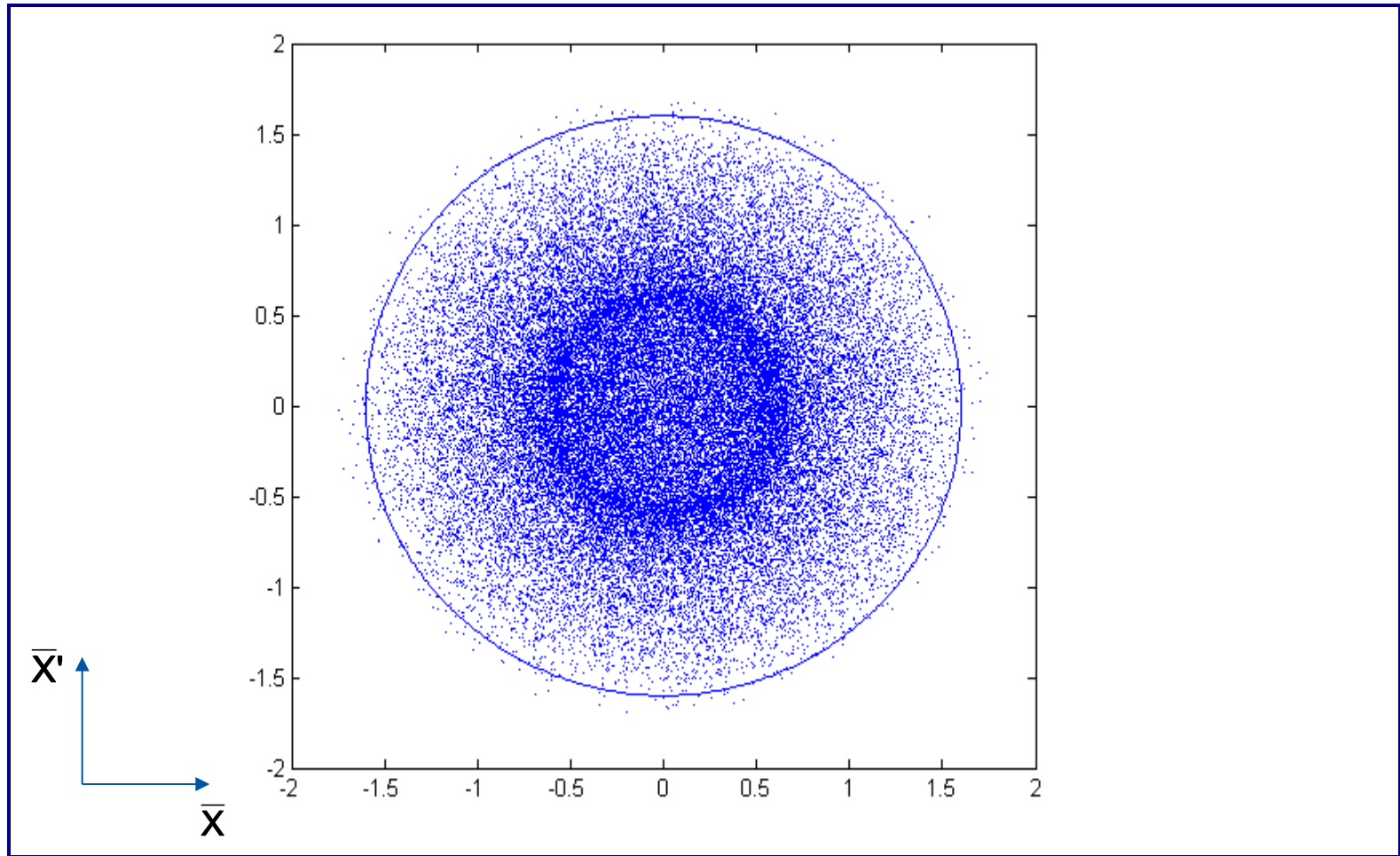
# Filamentation



# Filamentation



# Filamentation



# Blow-up from steering error

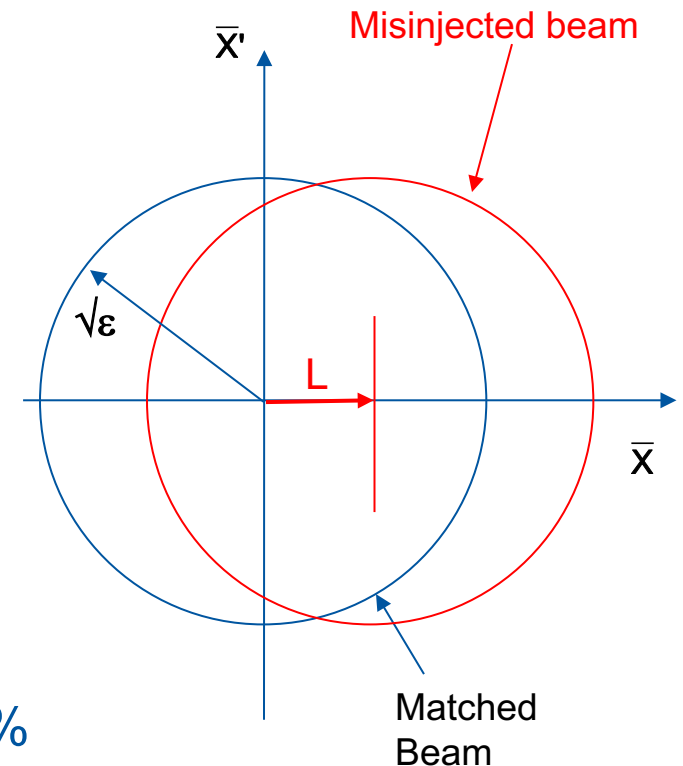
A numerical example....

Consider an offset  $\Delta a = 0.5\sigma$  for injected beam:  $L = \Delta a \sqrt{\epsilon_{matched}}$

$$\begin{aligned}\epsilon_{diluted} &= \epsilon_{matched} + \frac{L^2}{2} \\ &= \epsilon_{matched} \left[ 1 + \frac{\Delta a^2}{2} \right] \\ &= \epsilon_{matched} [1.125]\end{aligned}$$

For nominal LHC beam:

...allowed growth through LHC cycle ~10 %

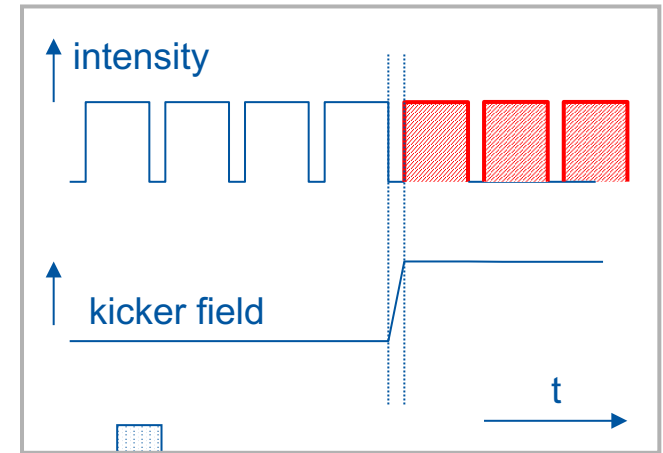


# Fast single turn extraction

Entire beam kicked into septum gap and extracted over a single turn

**Extracted beam**

**Septum magnet**



**Circulating beam**

**D-quad**

**F-quad**

**D-quad**

**Kicker magnet**

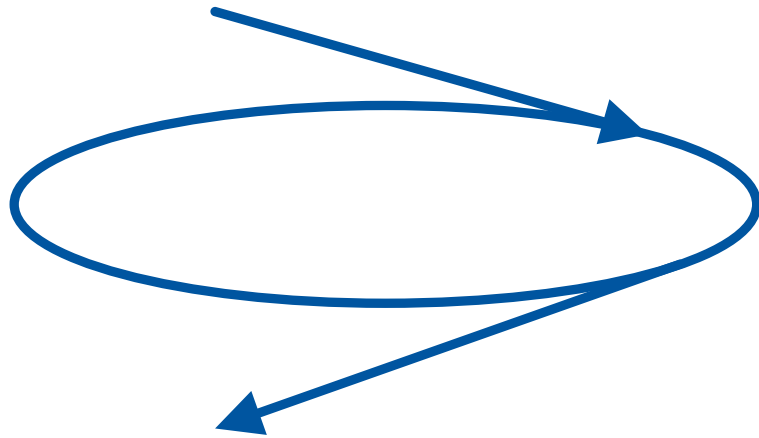
**Closed orbit bumpers**

- Bumpers move circulating beam close to septum to reduce kicker strength
- Kicker deflects the entire beam into the septum in a single turn
- Most efficient (lowest deflection angles required) for  $\pi/2$  phase advance between kicker and septum





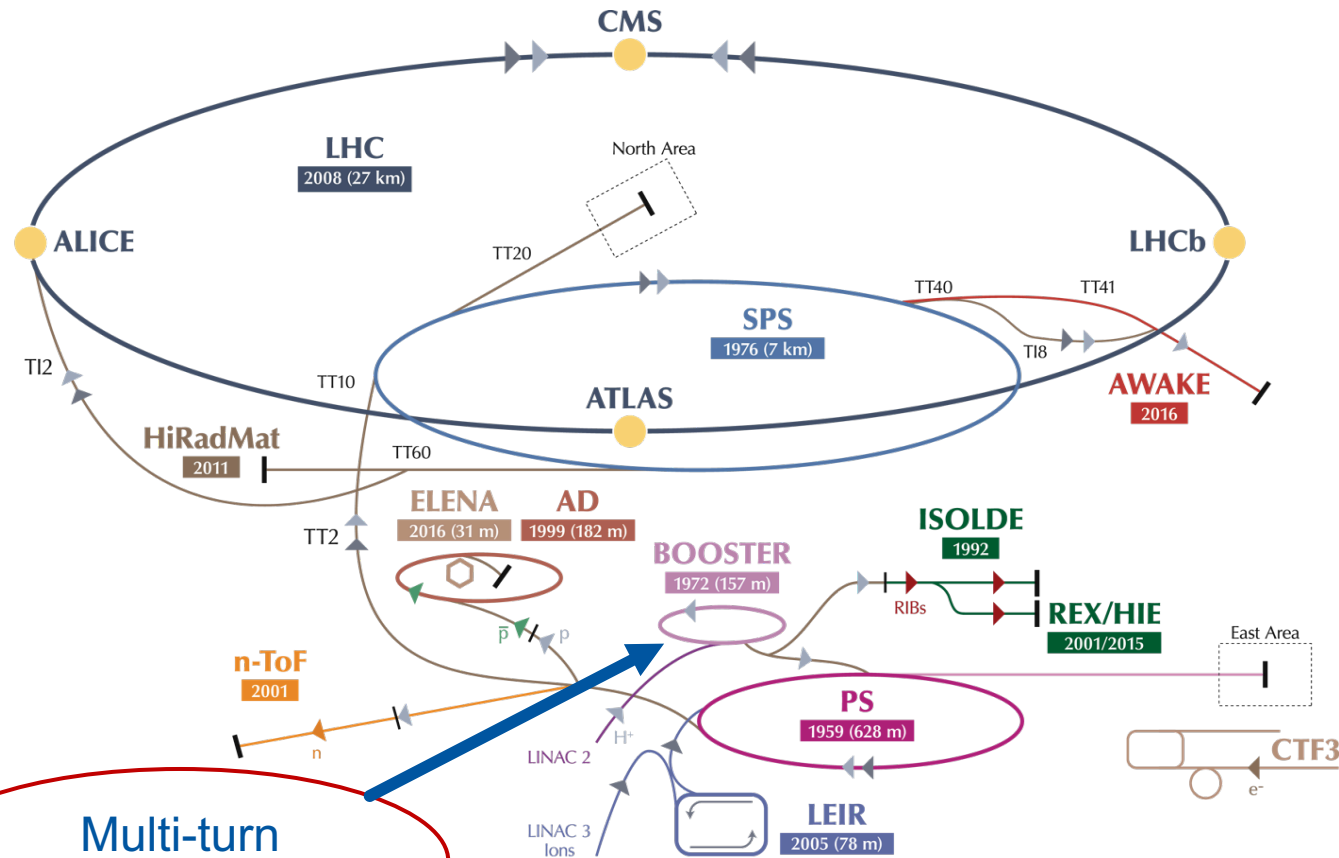
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- **Multi-turn methods**
  - **Multi-turn hadron injection**
  - **Charge-exchange H-injection**
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- Resonant slow extraction
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# Multi-turn methods

## CERN Accelerator Complex



Multi-turn injection

Filling of acceptance of receiving machine in multiple turns



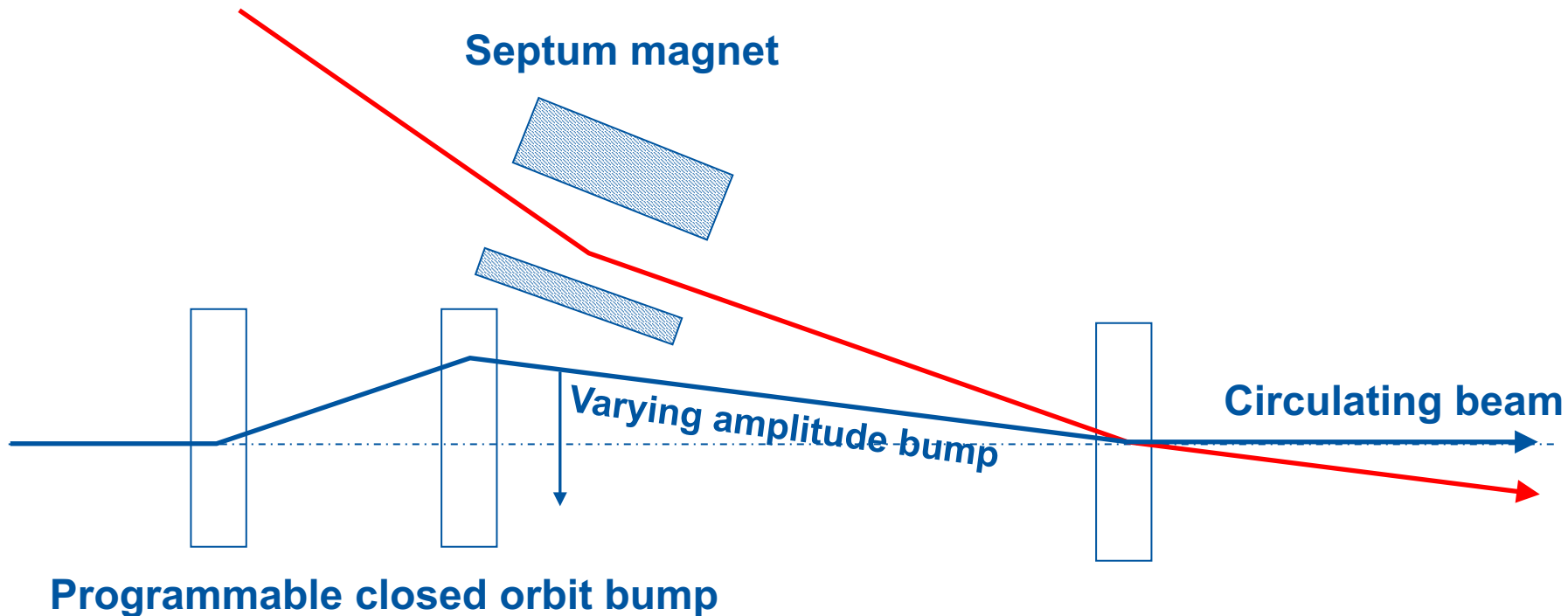
# Multi-turn injection

- Limitation of beam density at injection (for hadrons) by:
  - space charge effects
  - the injector capacity
- Increase overall injected intensity : fill the horizontal phase space
  - Requires large acceptance of receiving machine compared to beam emittance from injector
  - → no increase of beam density!



# Multi-turn injection for hadrons

**Injected beam  
(usually from a linac)**



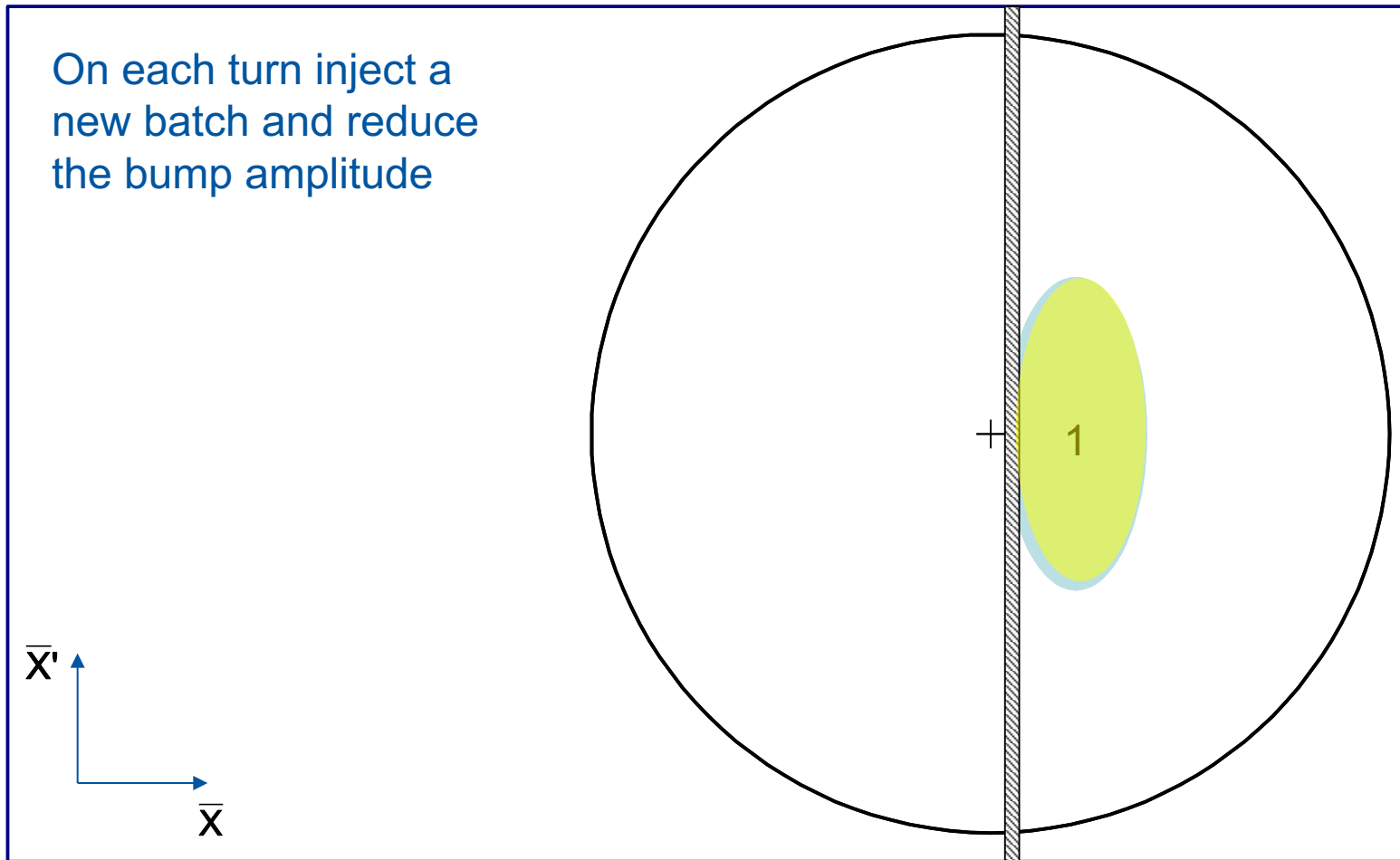
- No kicker but fast programmable bumpers
- Bump amplitude decreases and a new batch injected turn-by-turn
- Phase-space “painting”

# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 1

On each turn inject a  
new batch and reduce  
the bump amplitude



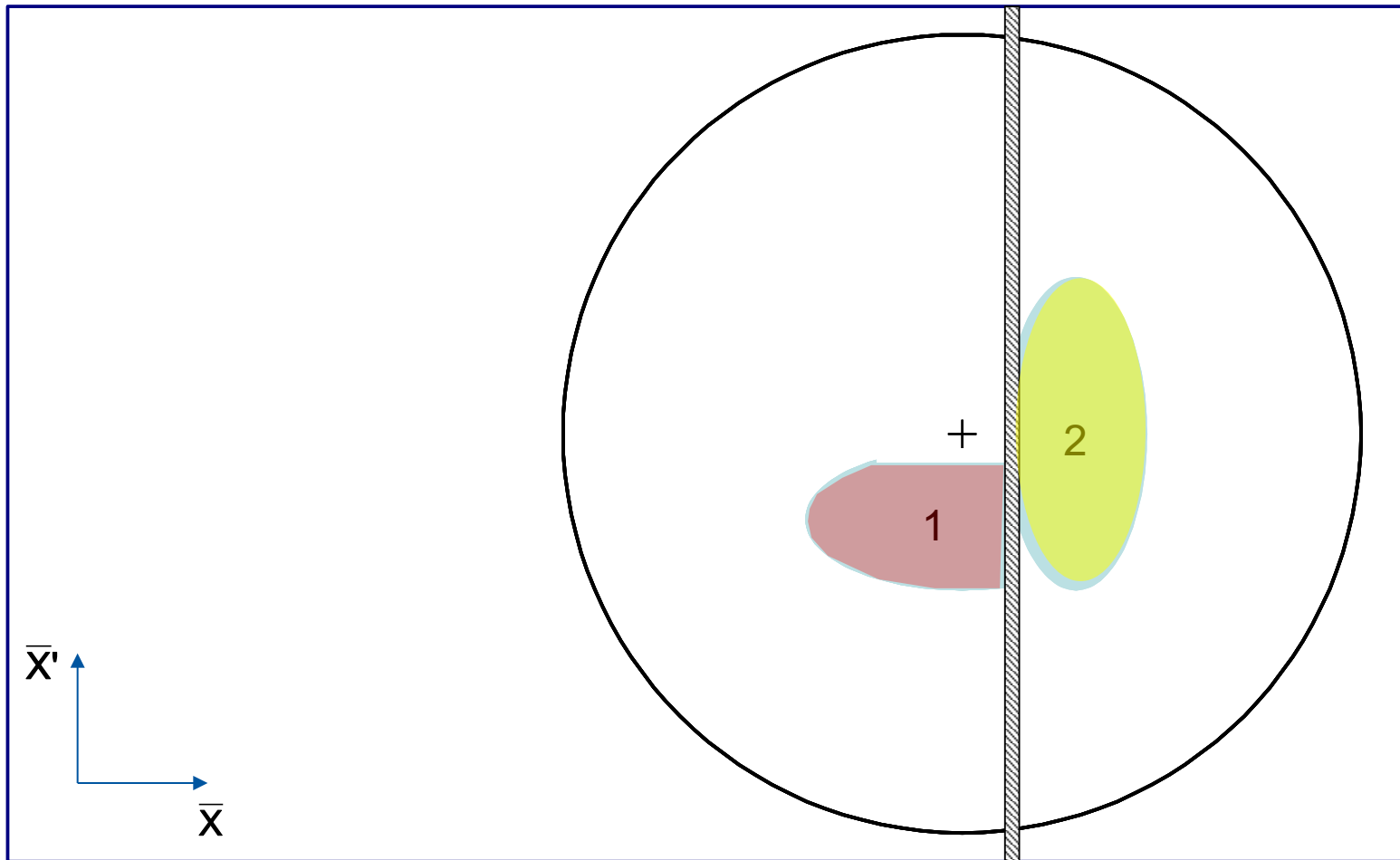
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 2



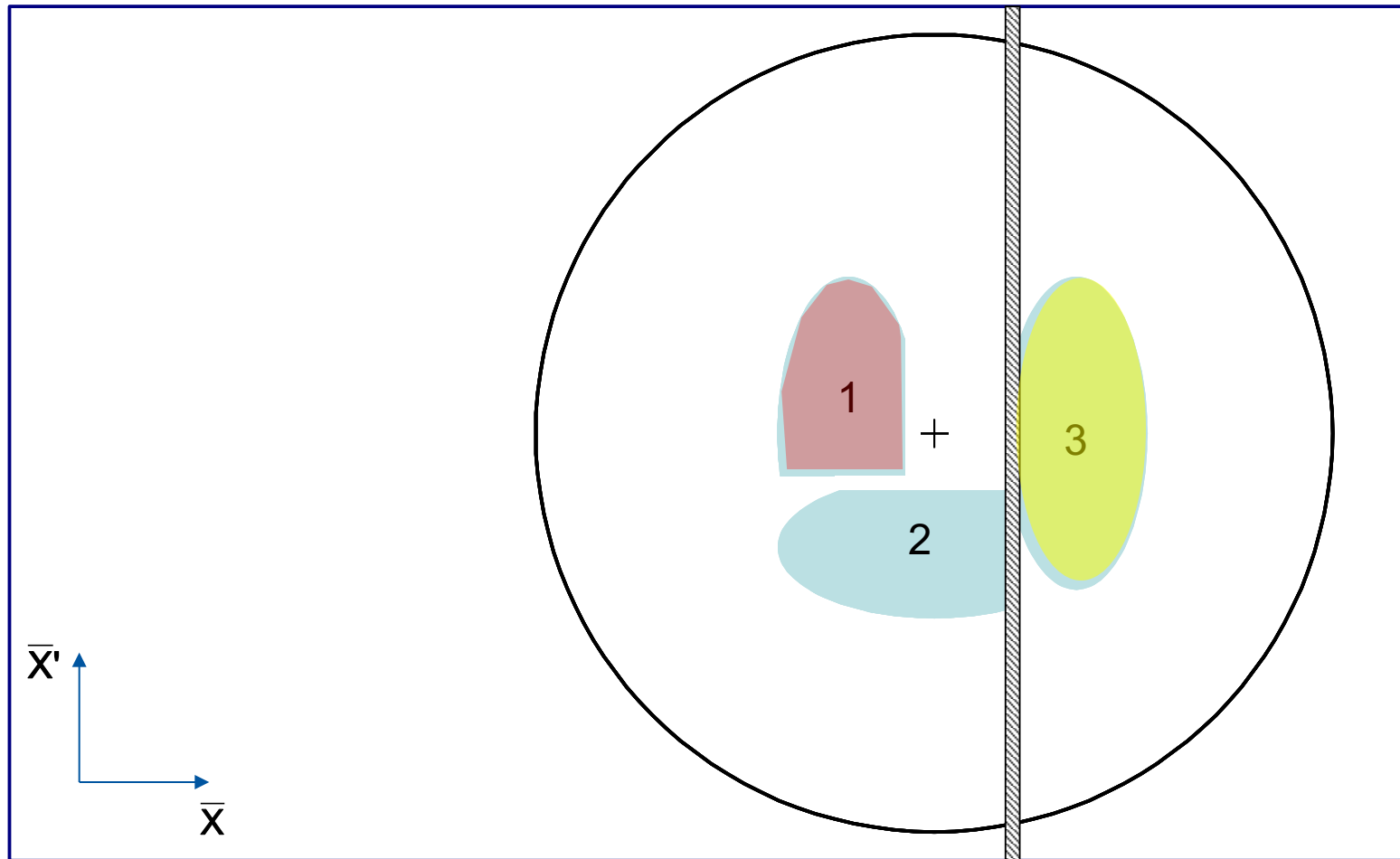
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 3



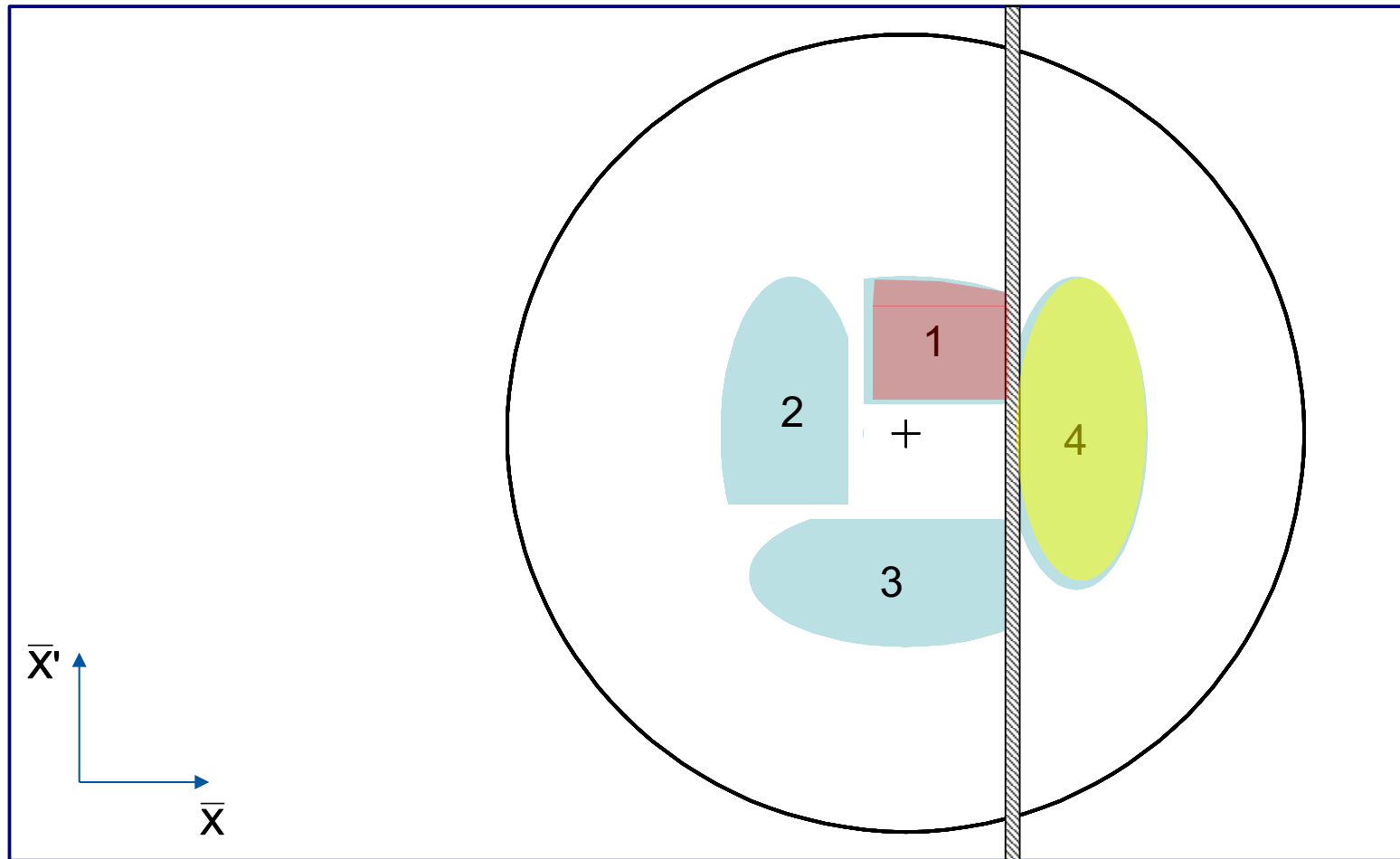
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 4



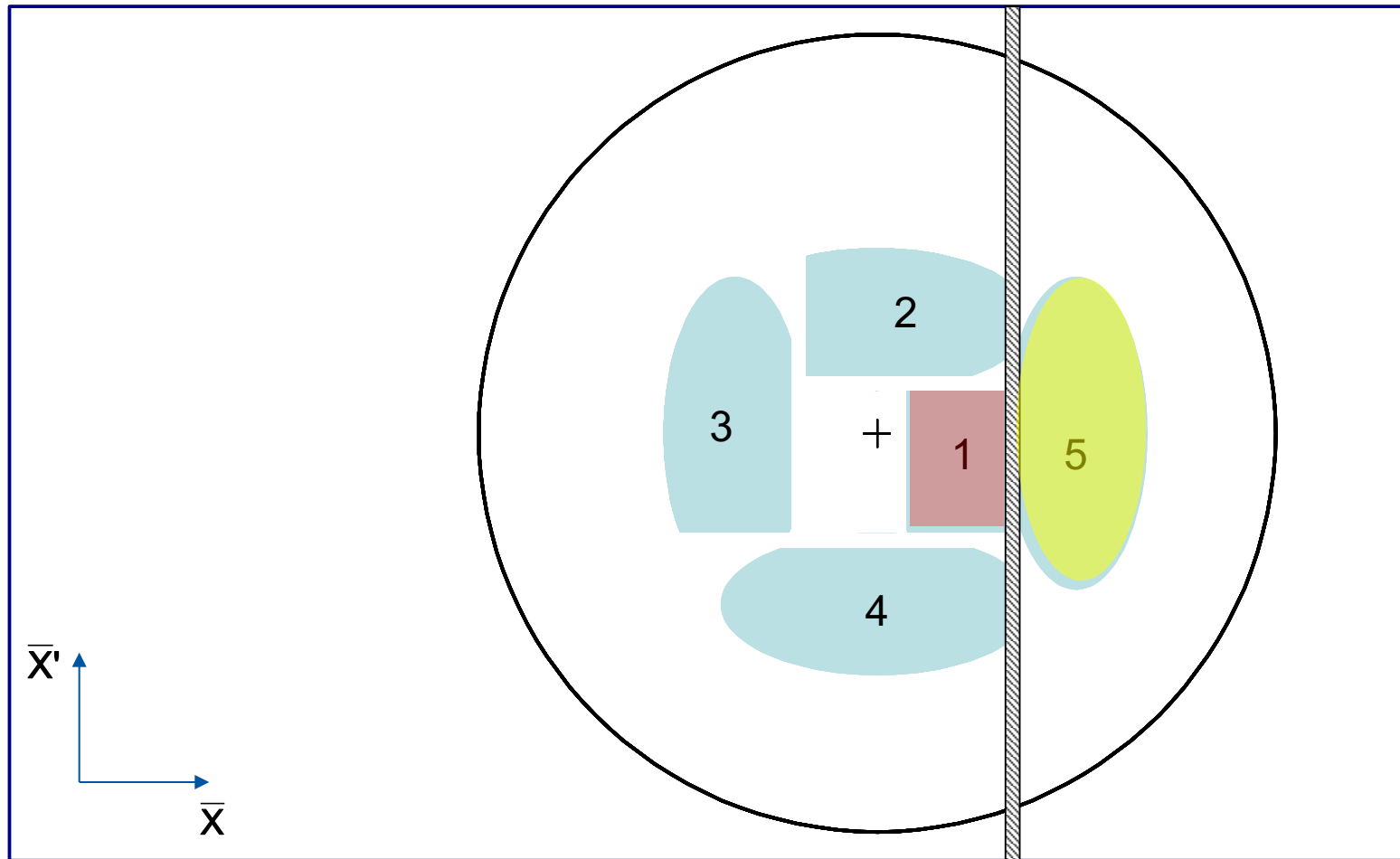
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 5

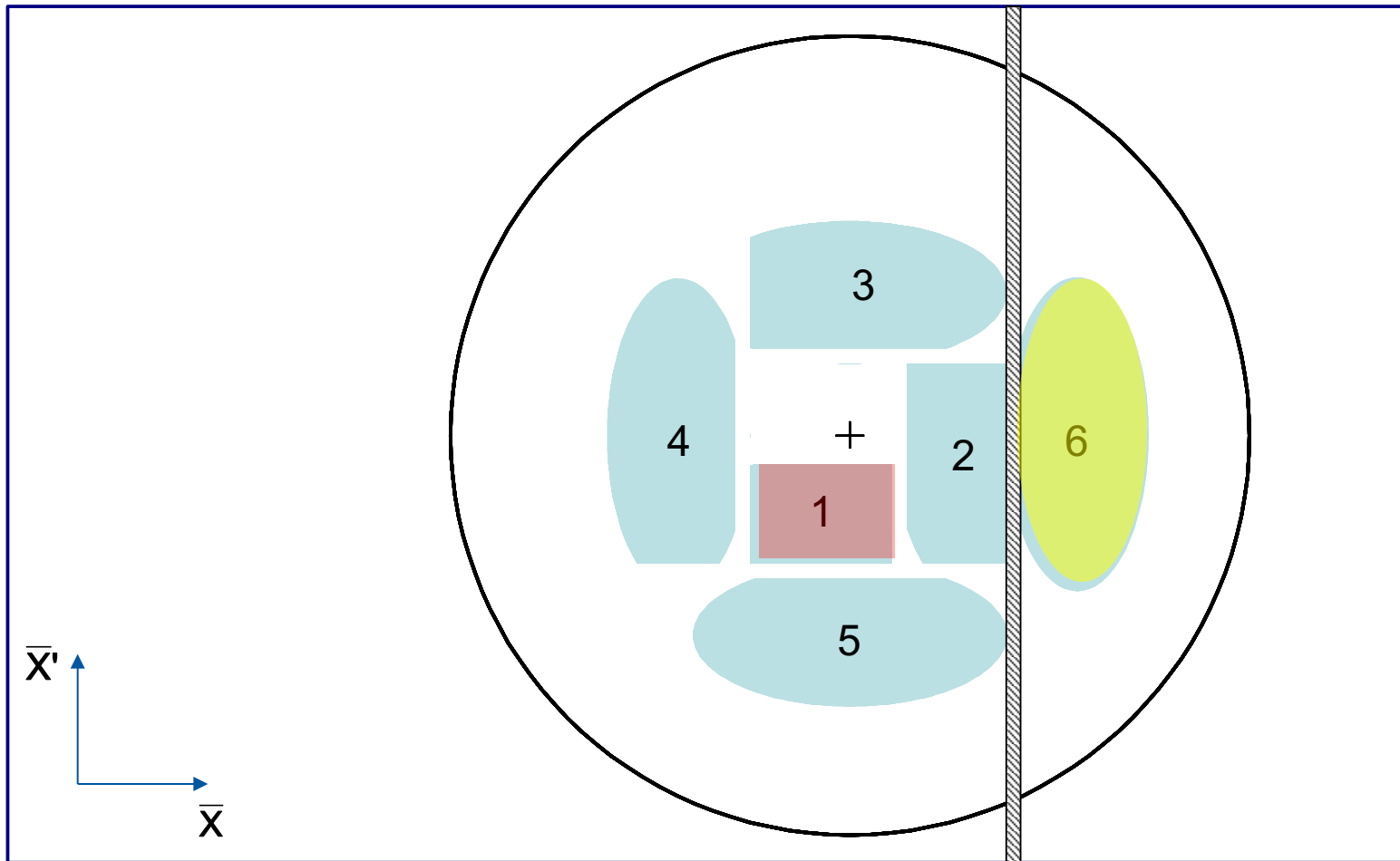


Septum

# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 6

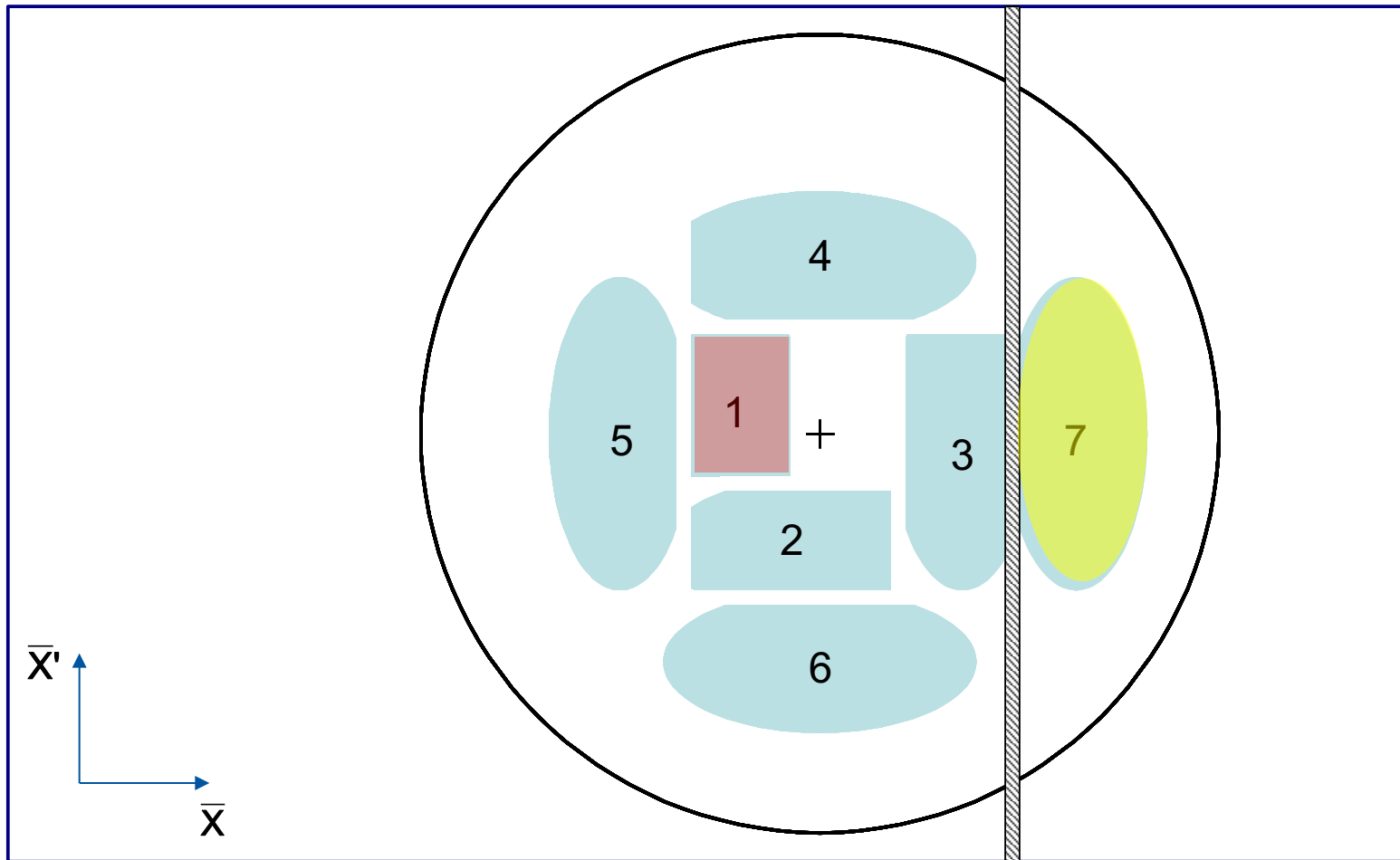


Septum

# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 7

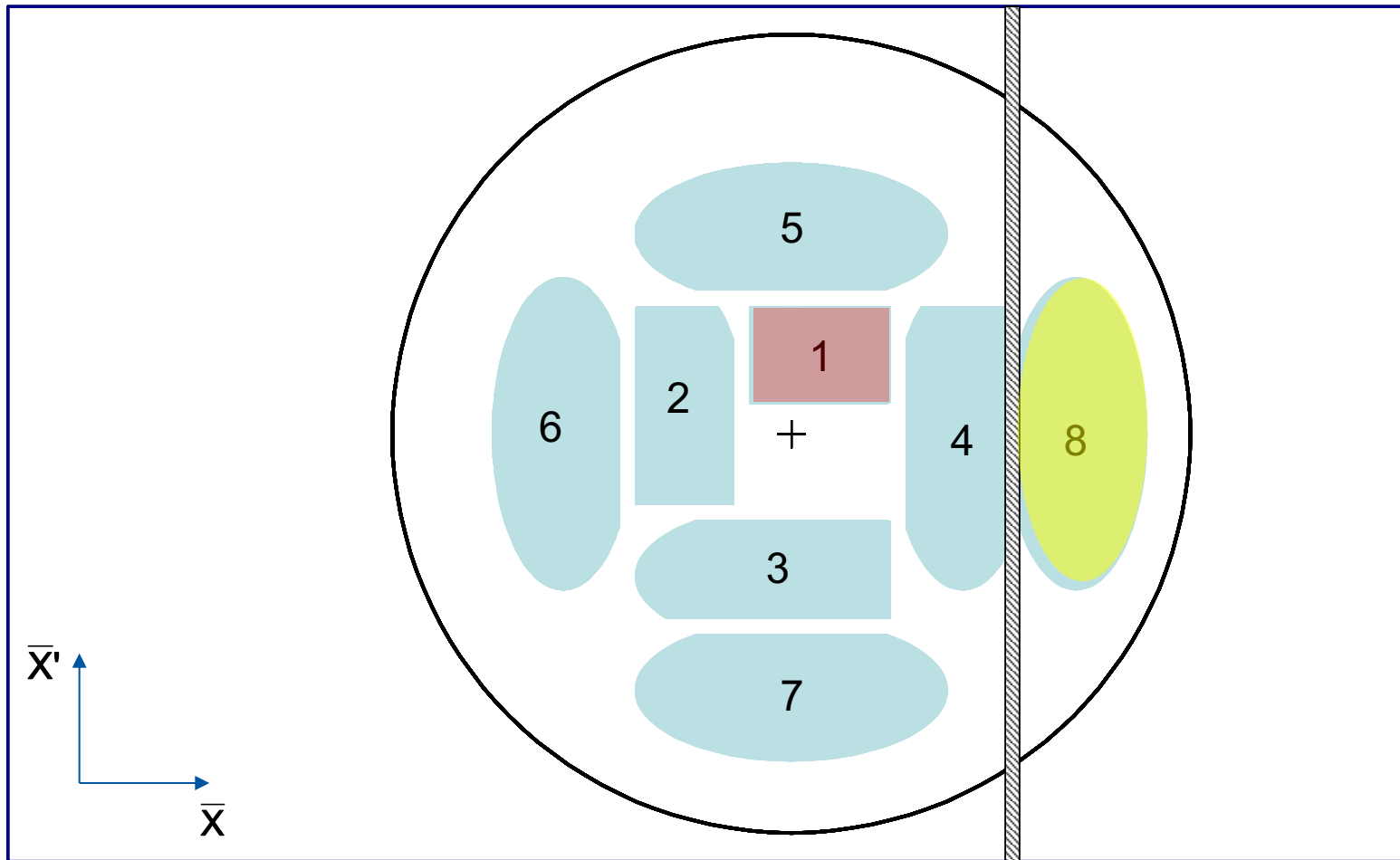


Septum

# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 8



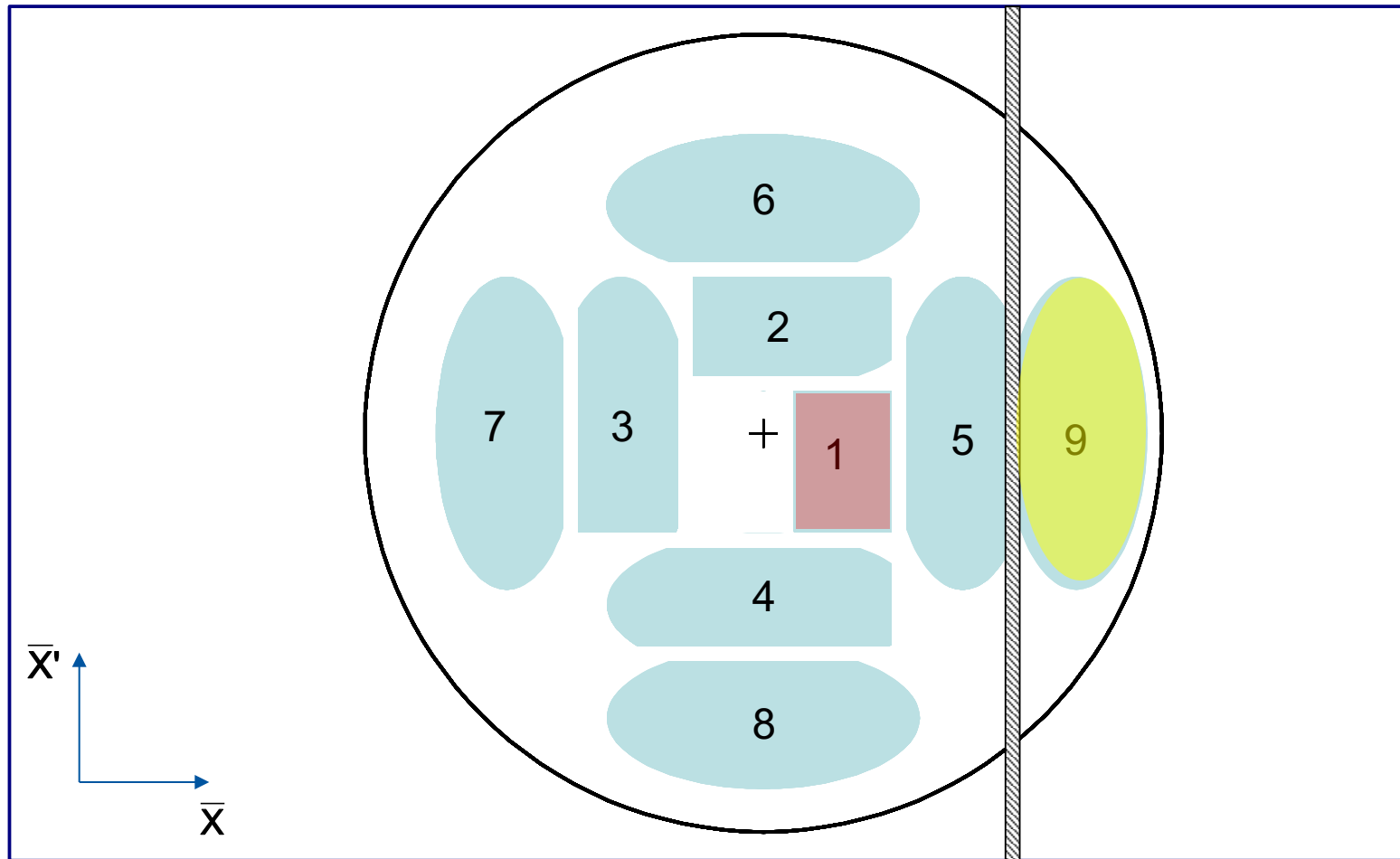
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 9

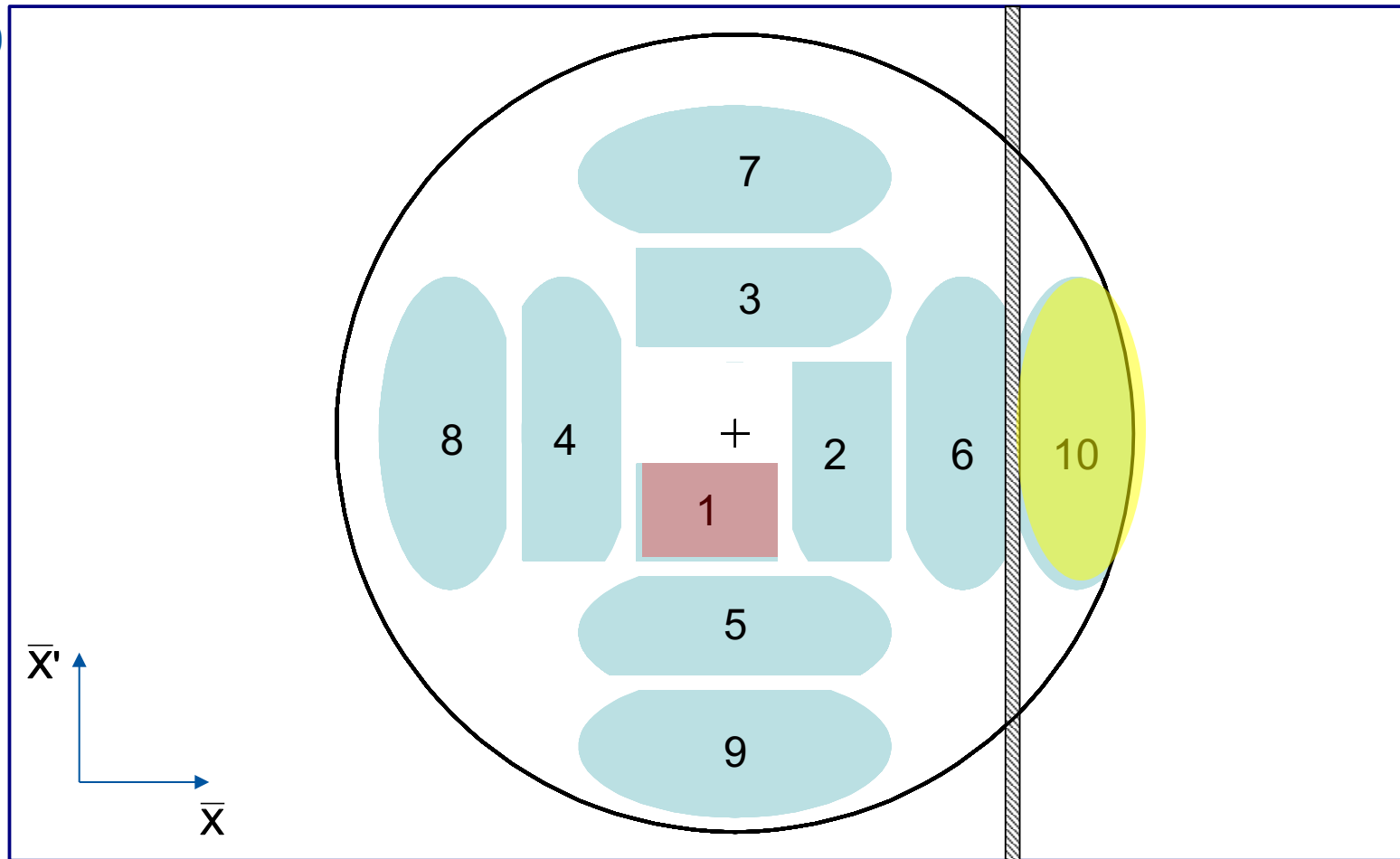


Septum

# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 10

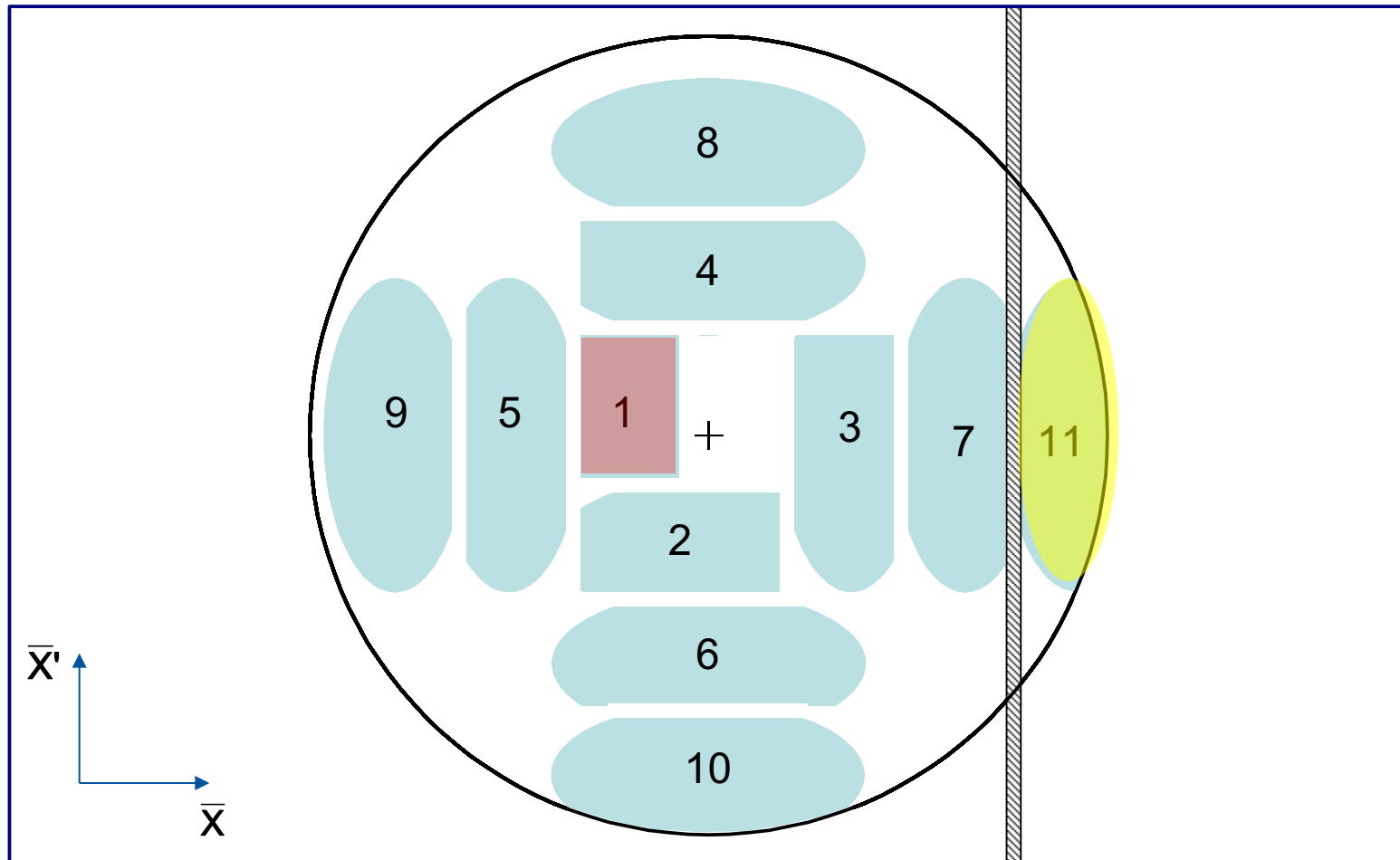


Septum

# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 11



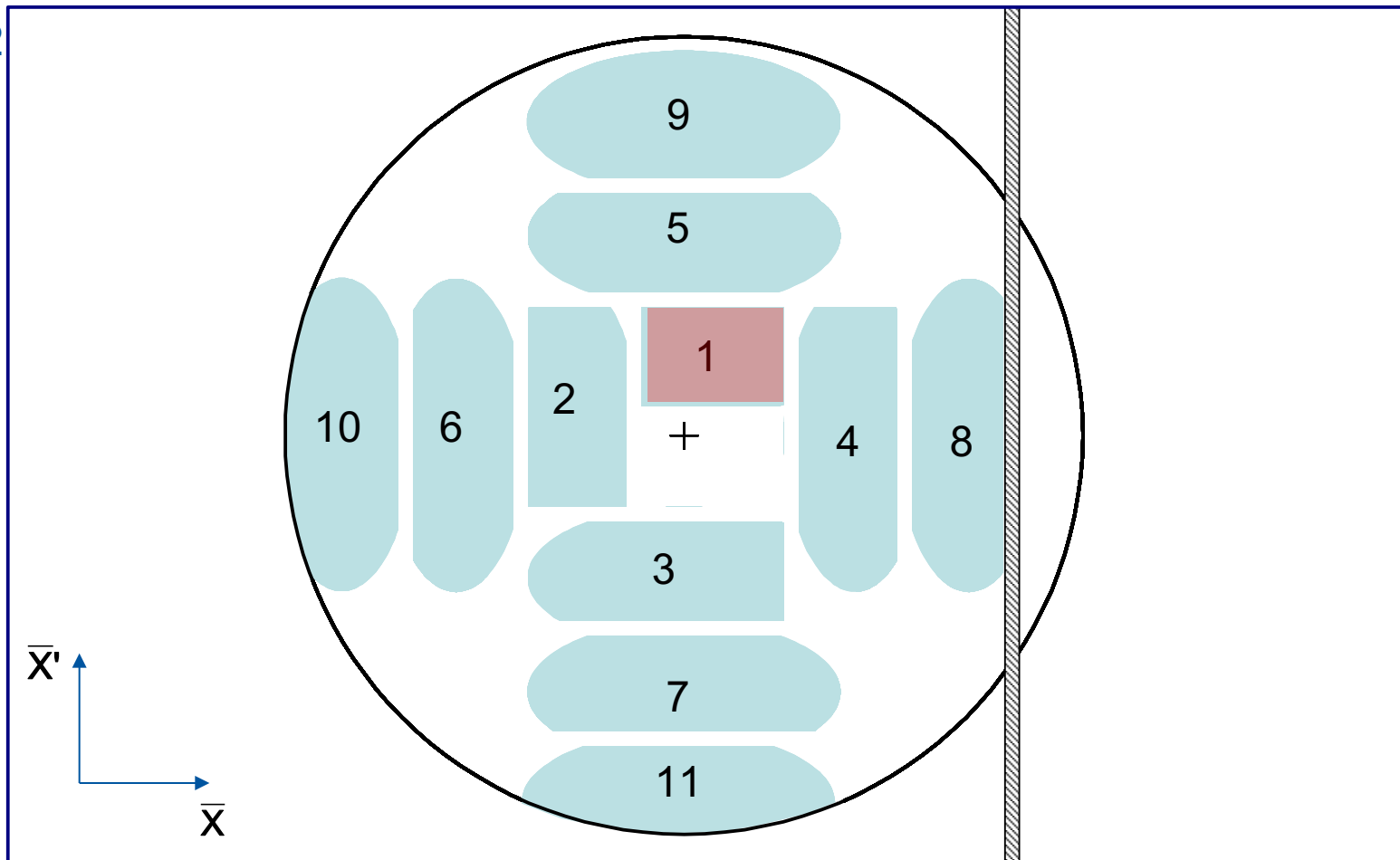
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 12



Septum

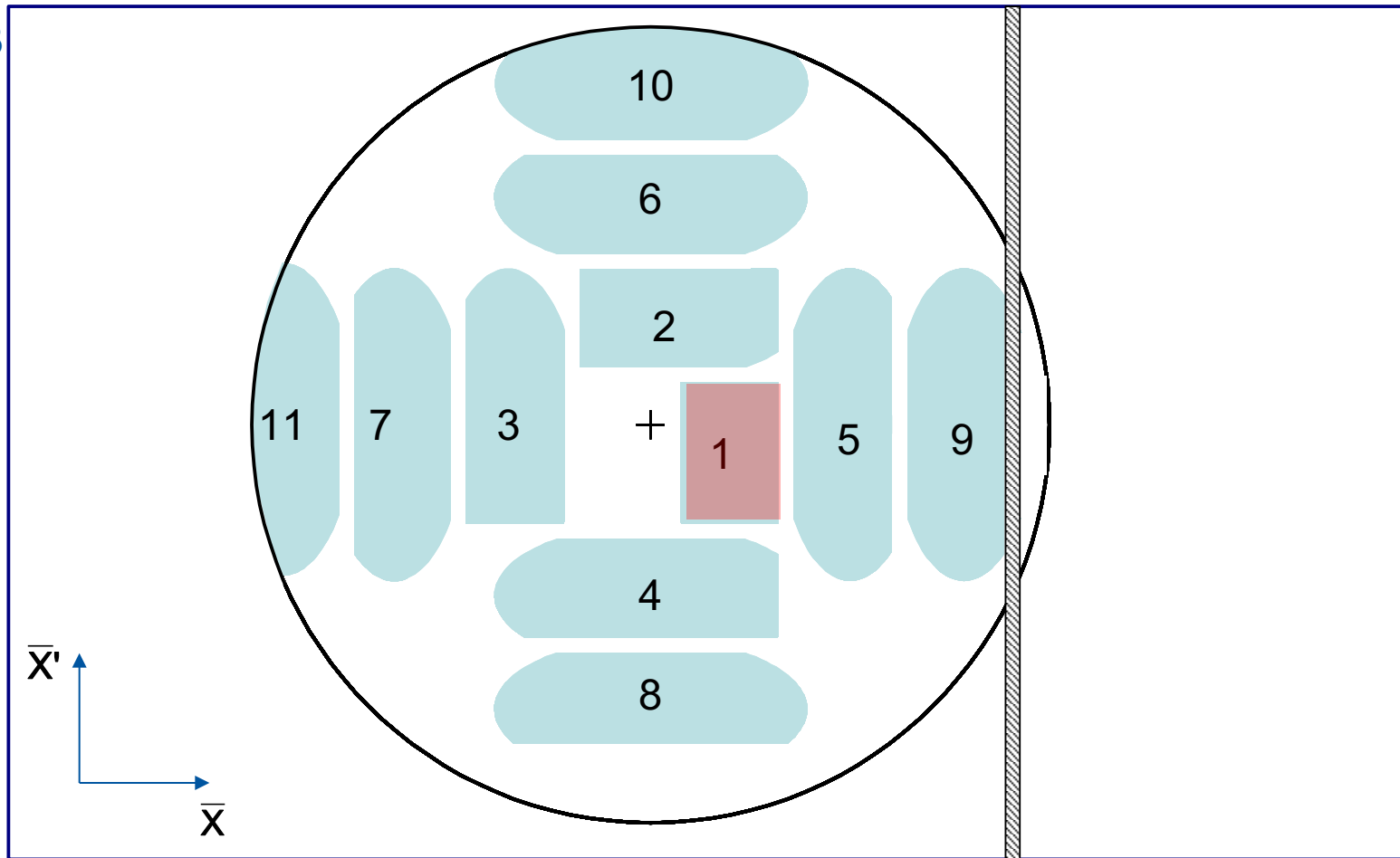




# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 13



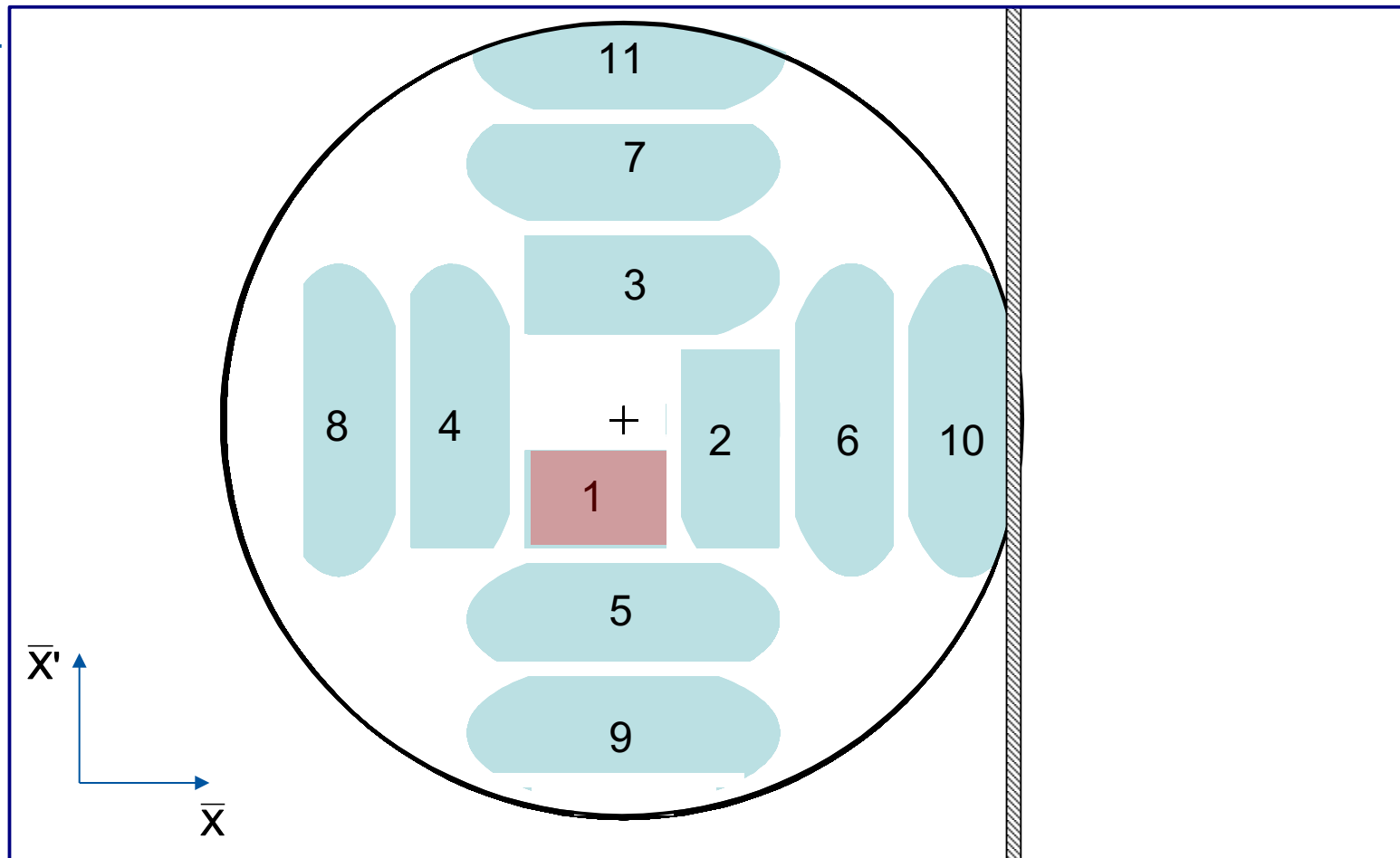
Septum



# Multi-turn injection for hadrons

Example: CERN PSB injection, high intensity beams,  
fractional tune  $Q_h \approx 0.25 \rightarrow$  beam rotates  $\pi/2$  per turn in phase space

Turn 14



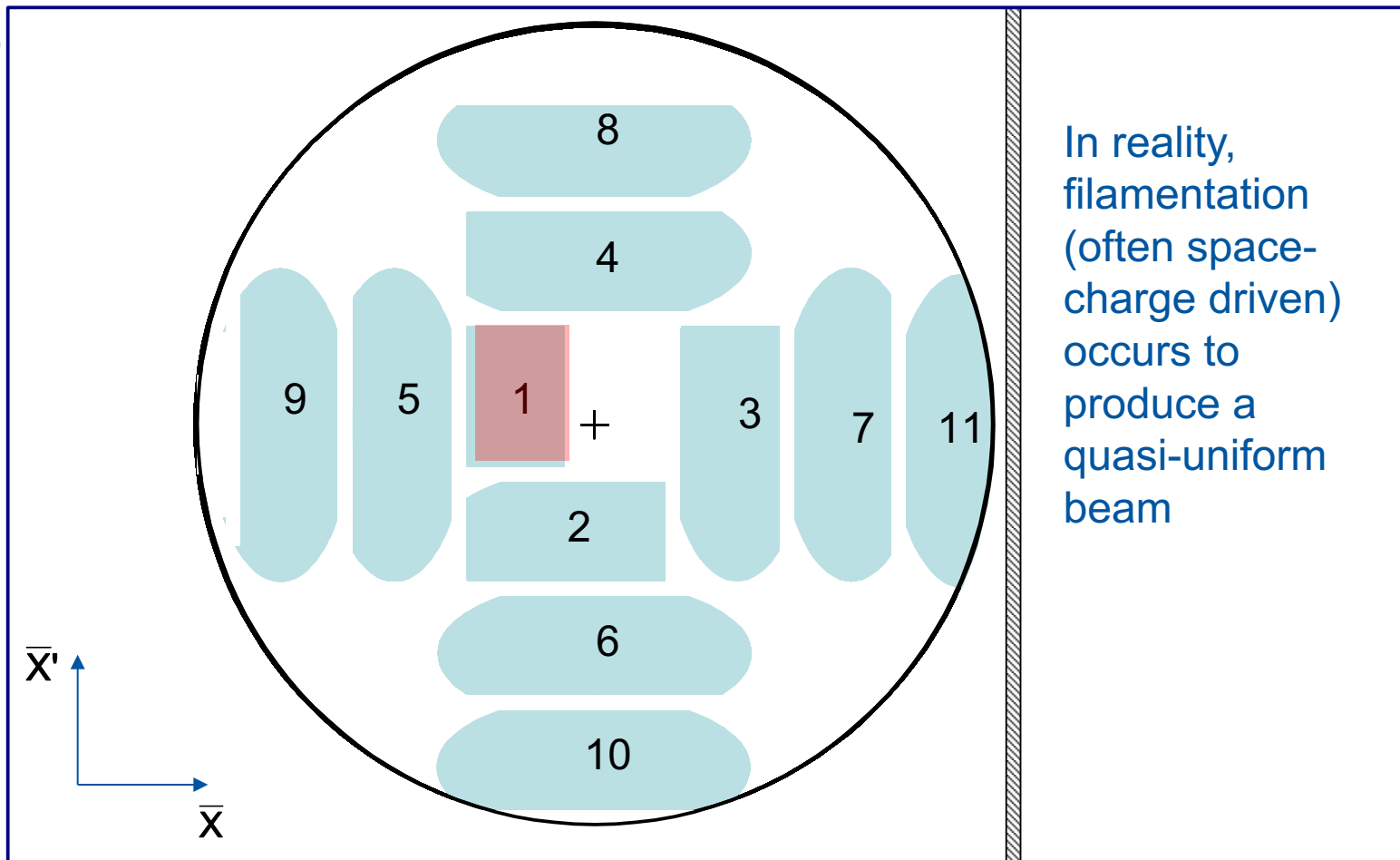
Septum



# Multi-turn injection for hadrons

Phase space has been “**Painted**”

Turn 15



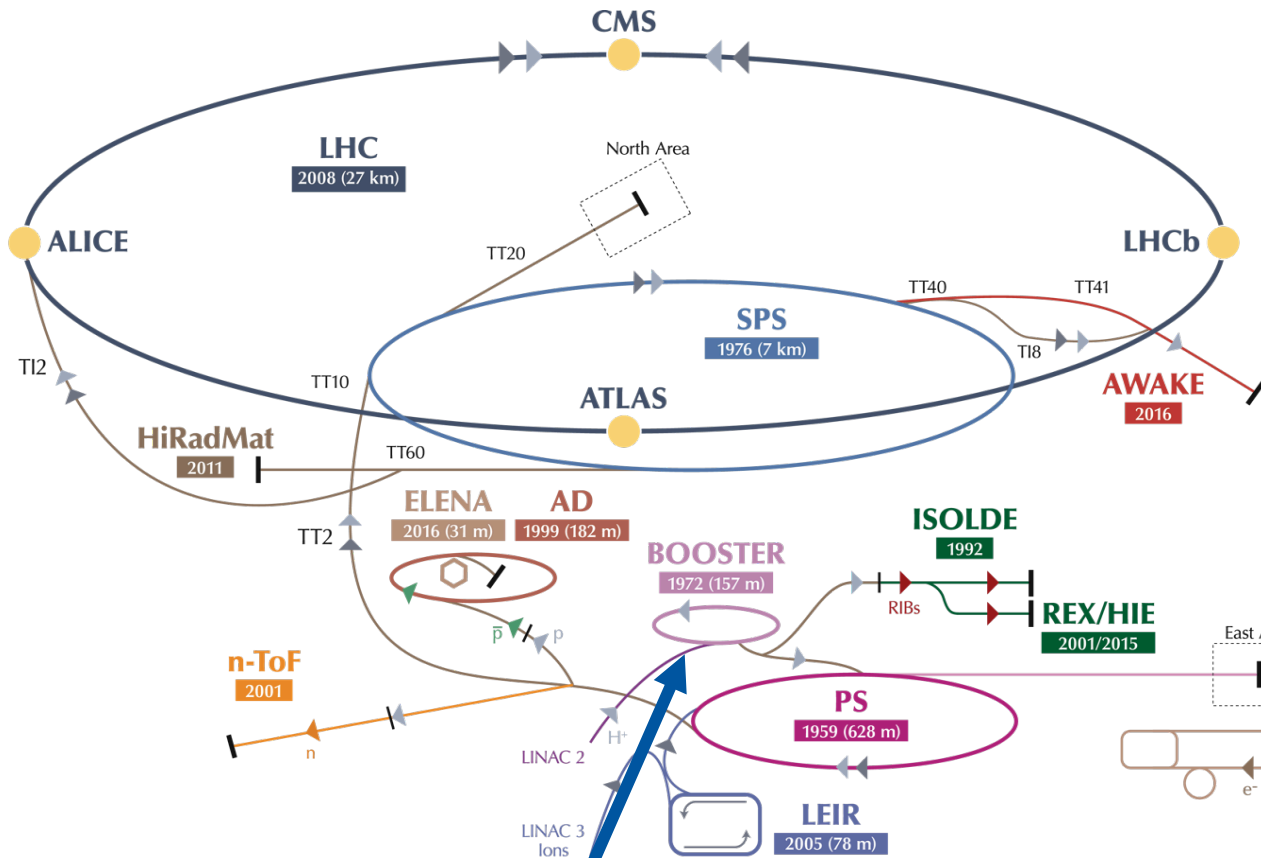
In reality, filamentation (often space-charge driven) occurs to produce a quasi-uniform beam

# Charge exchange H- injection

- Multi-turn injection is essential to accumulate high intensity
  - Disadvantages inherent in using an injection septum:
    - Width of several mm reduces aperture
    - Beam losses from circulating beam hitting septum:
      - typically 30 – 40 % for the CERN PSB injection at 50 MeV
    - Limits number of injected turns to 10 – 20
  - **Charge-exchange injection** provides elegant alternative
    - Convert  $H^-$  to  $p^+$  using a thin stripping foil, allowing **injection into the same phase space area**
- ➔ **increase of beam density**

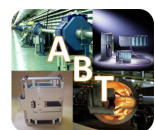
# Multi-turn methods

## CERN Accelerator Complex



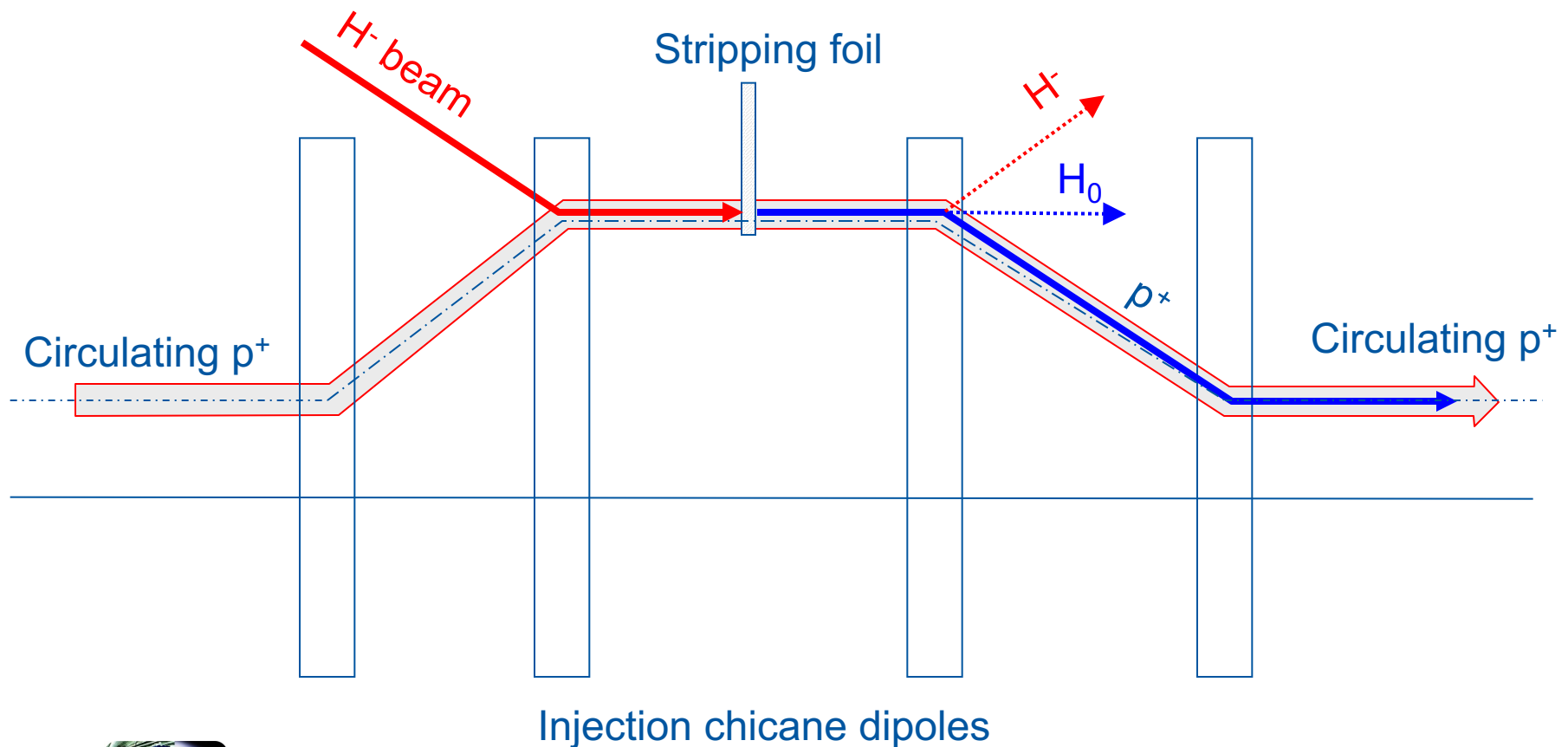
With LINAC4:  
Charge exchange H-  
injection

Accumulate high intensity and density by "cheating" Liouville



# Charge exchange H- injection

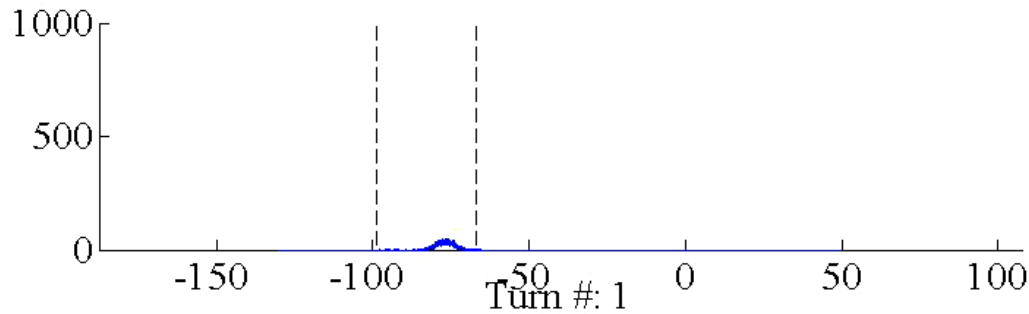
Start of injection process



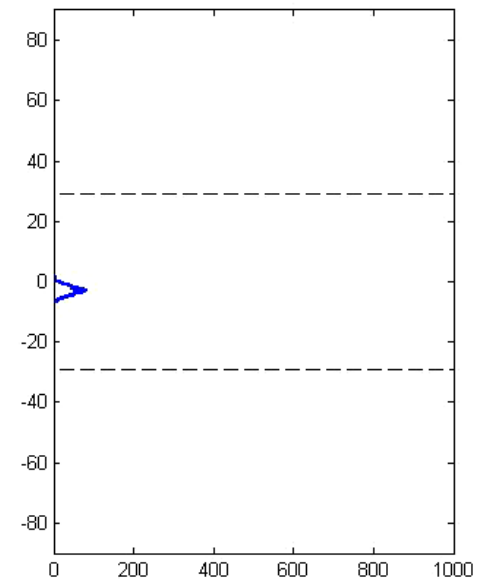
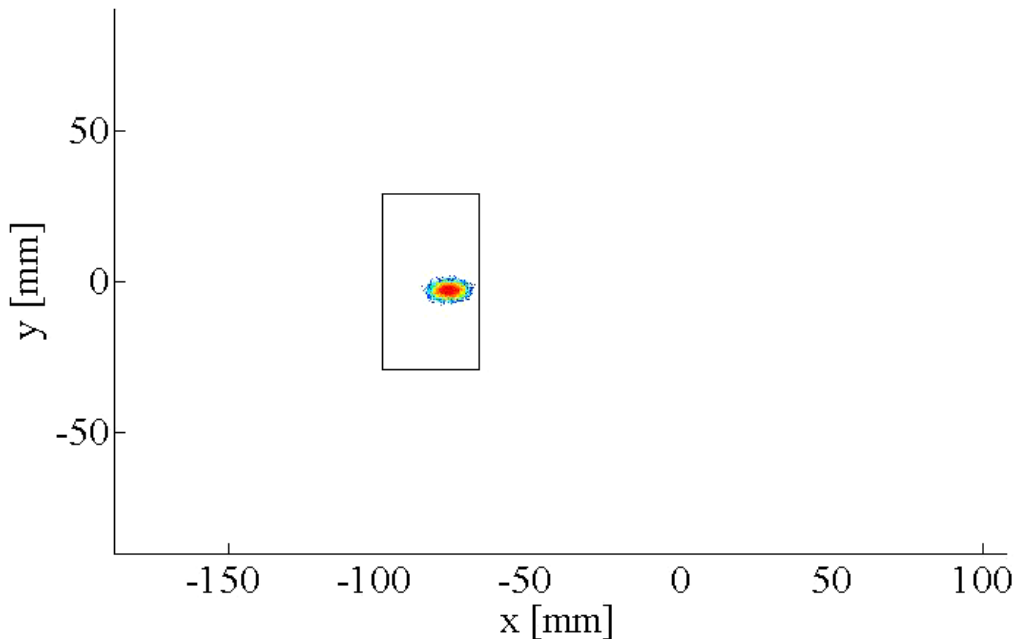
# Accumulation process on foil

Linac4 connection to the PS booster at 160 MeV:

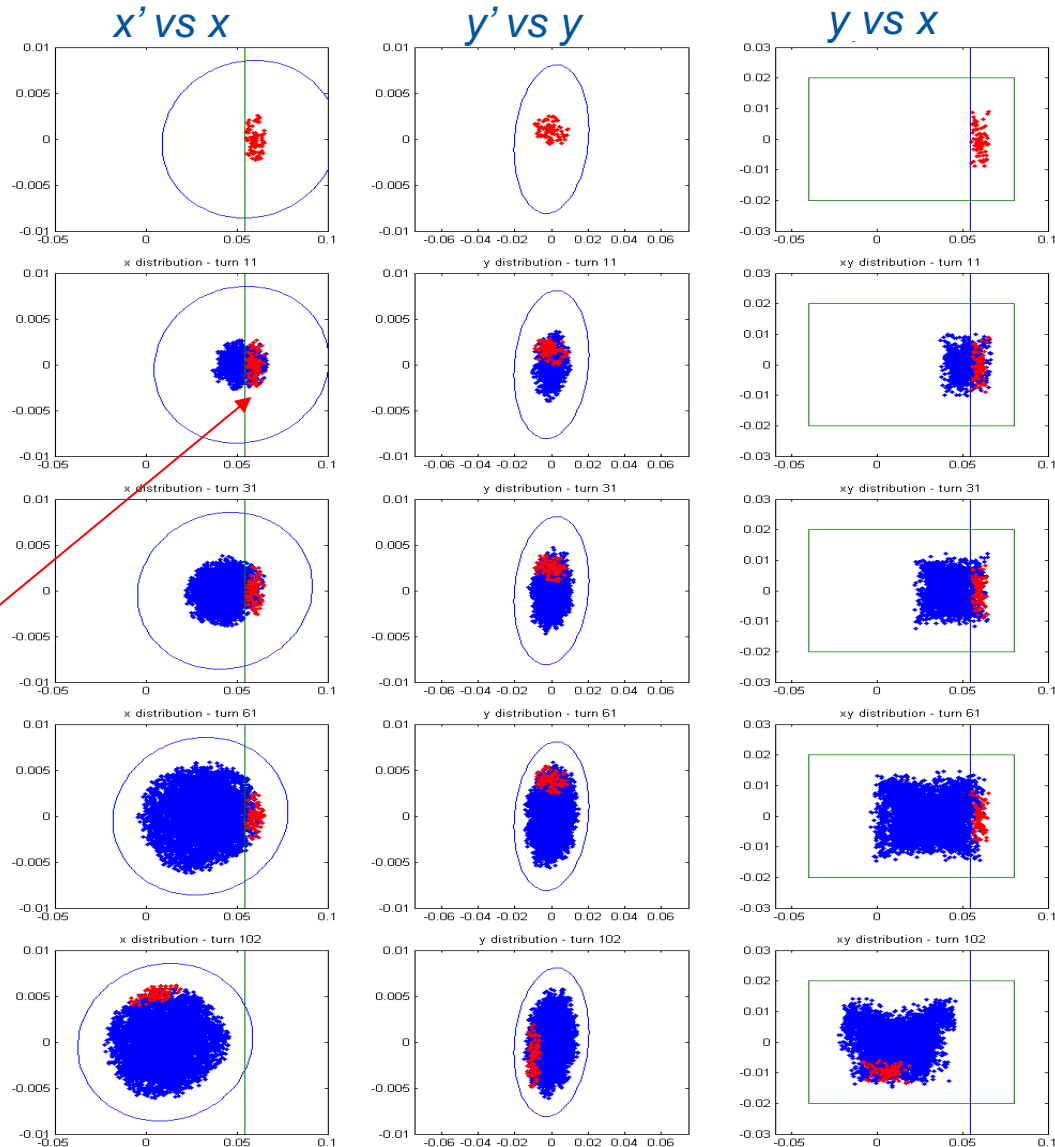
H<sup>-</sup> stripped to p<sup>+</sup> with an estimated efficiency  $\approx 98\%$  with C foil  $200 \mu\text{g}\cdot\text{cm}^{-2}$



V. Forte, Performance of the CERN PSB at 160 MeV with H-charge exchange injection, PhD thesis – CERN and Université Blaise Pascal



# H- injection - painting



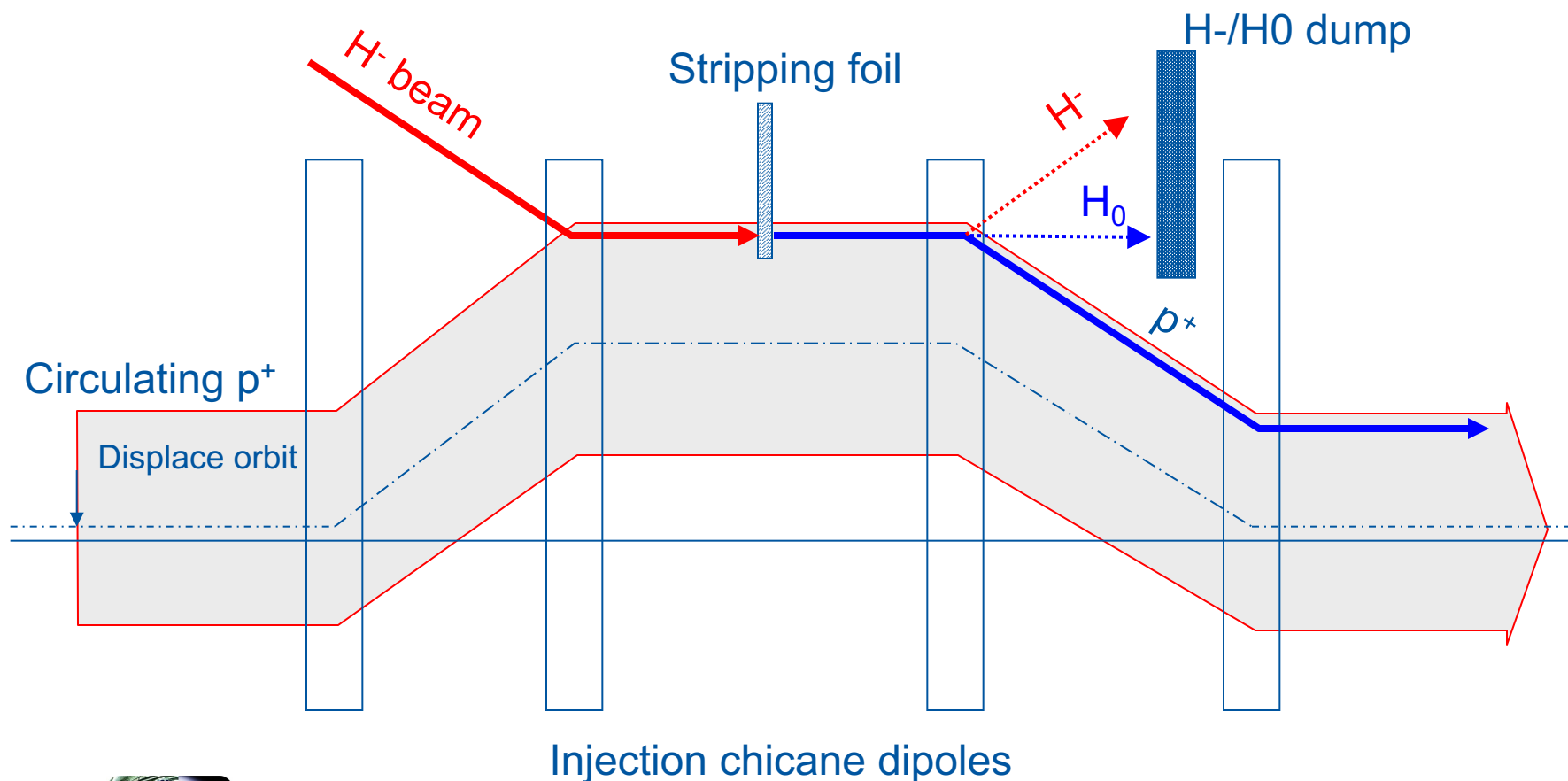
Note injection into same phase space area as circulating beam





# Charge exchange H- injection

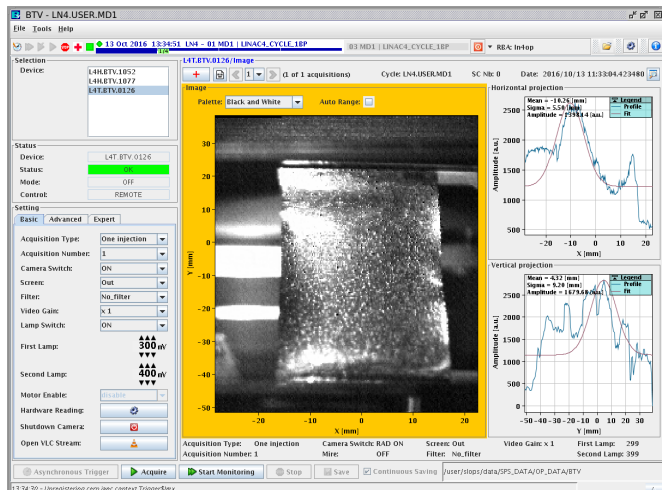
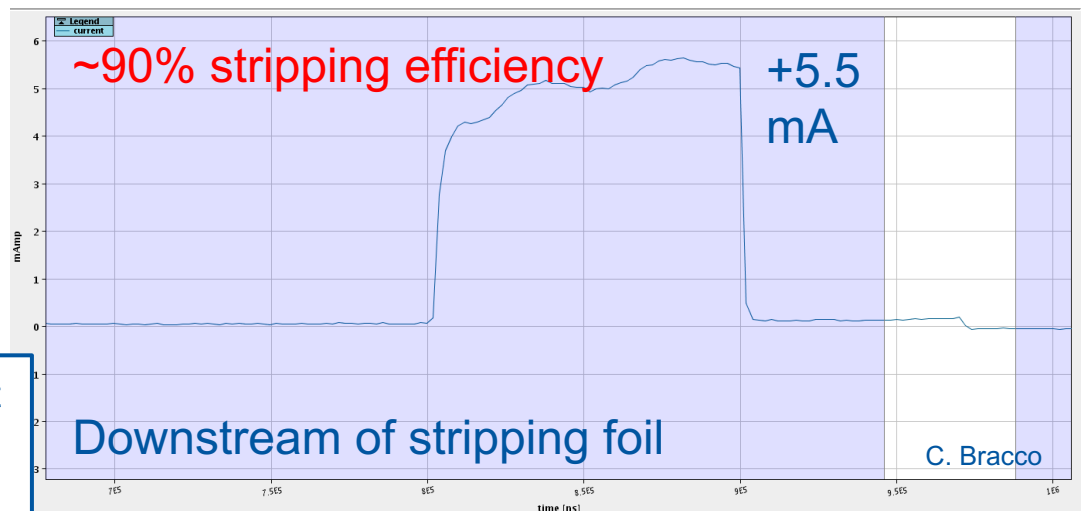
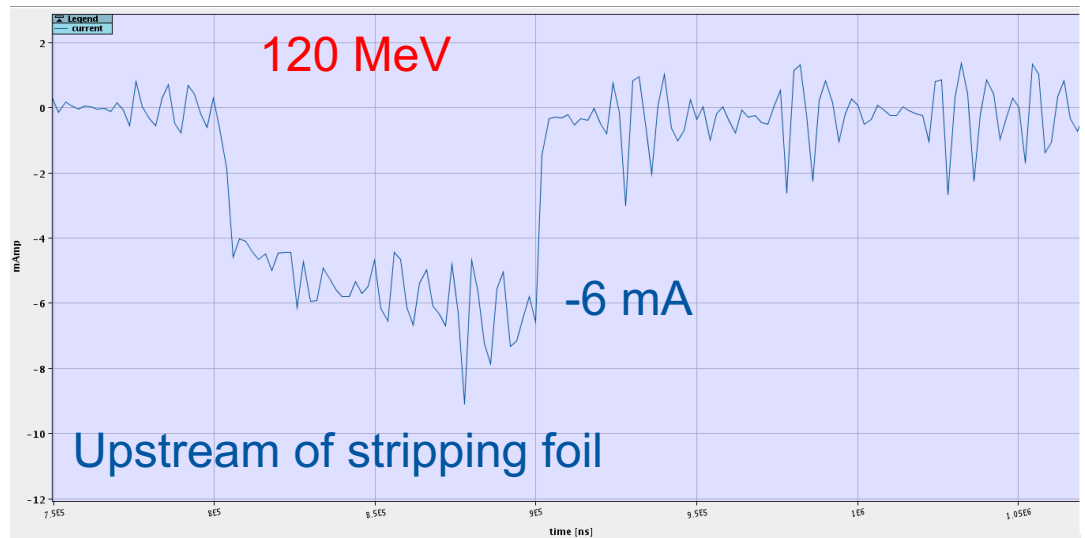
End of injection process with painting



# Charge exchange H- injection

- Paint uniform transverse phase space density by modifying closed orbit bump and steering injected beam
- Injection chicane reduced or switched off after injection, to avoid excessive foil heating and beam blow-up
- Longitudinal phase space can also be painted turn-by-turn:
  - Variation of the injected beam energy turn-by-turn (linac voltage scaled)
  - Chopper system in linac to match length of injected batch to bucket

# Stripping Foil Tests – Oct'16

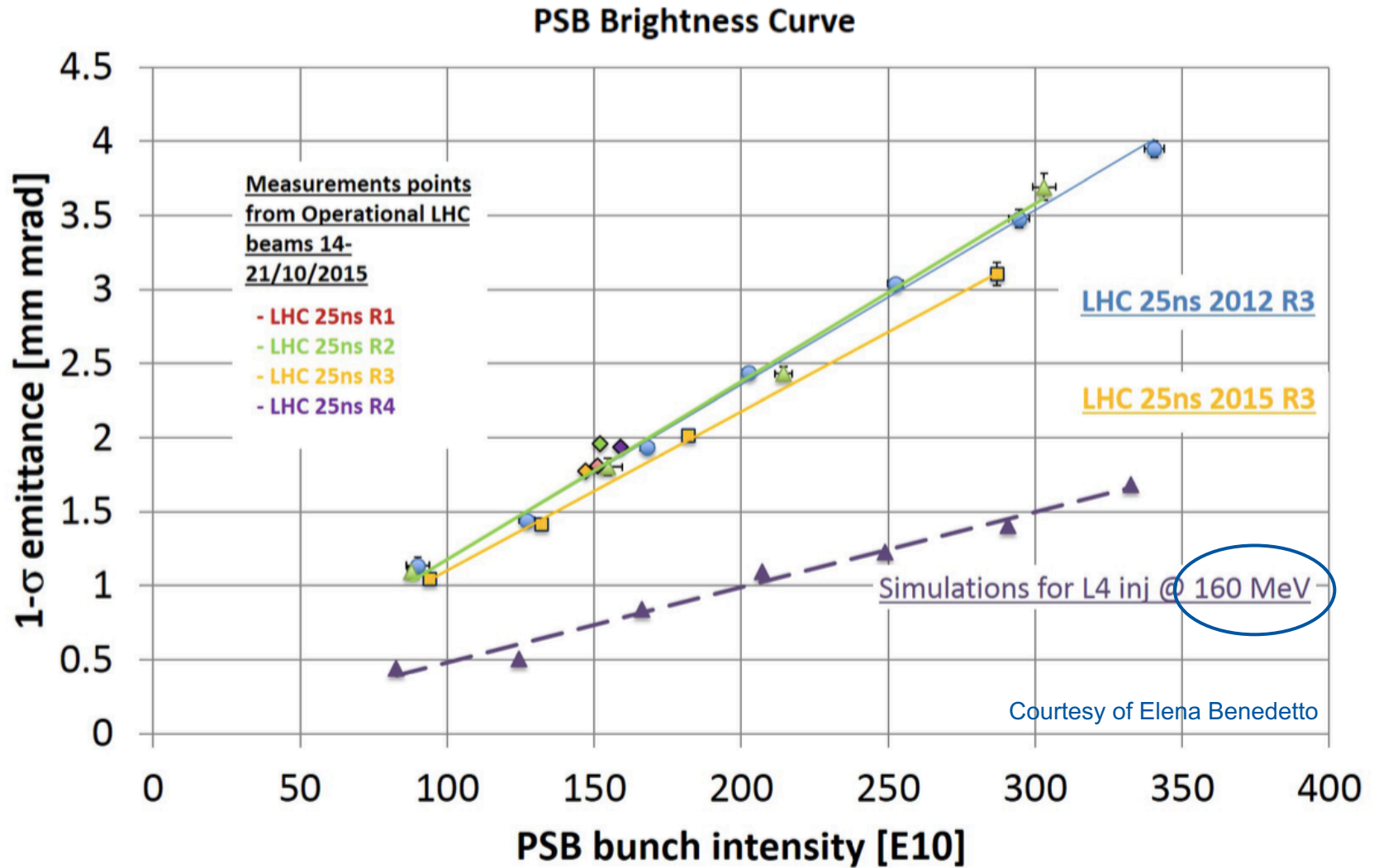


Foil thickness calculated to double-strip most ions ( $\approx 99\%$ )

50 MeV –  $50 \mu\text{g.cm}^{-2}$

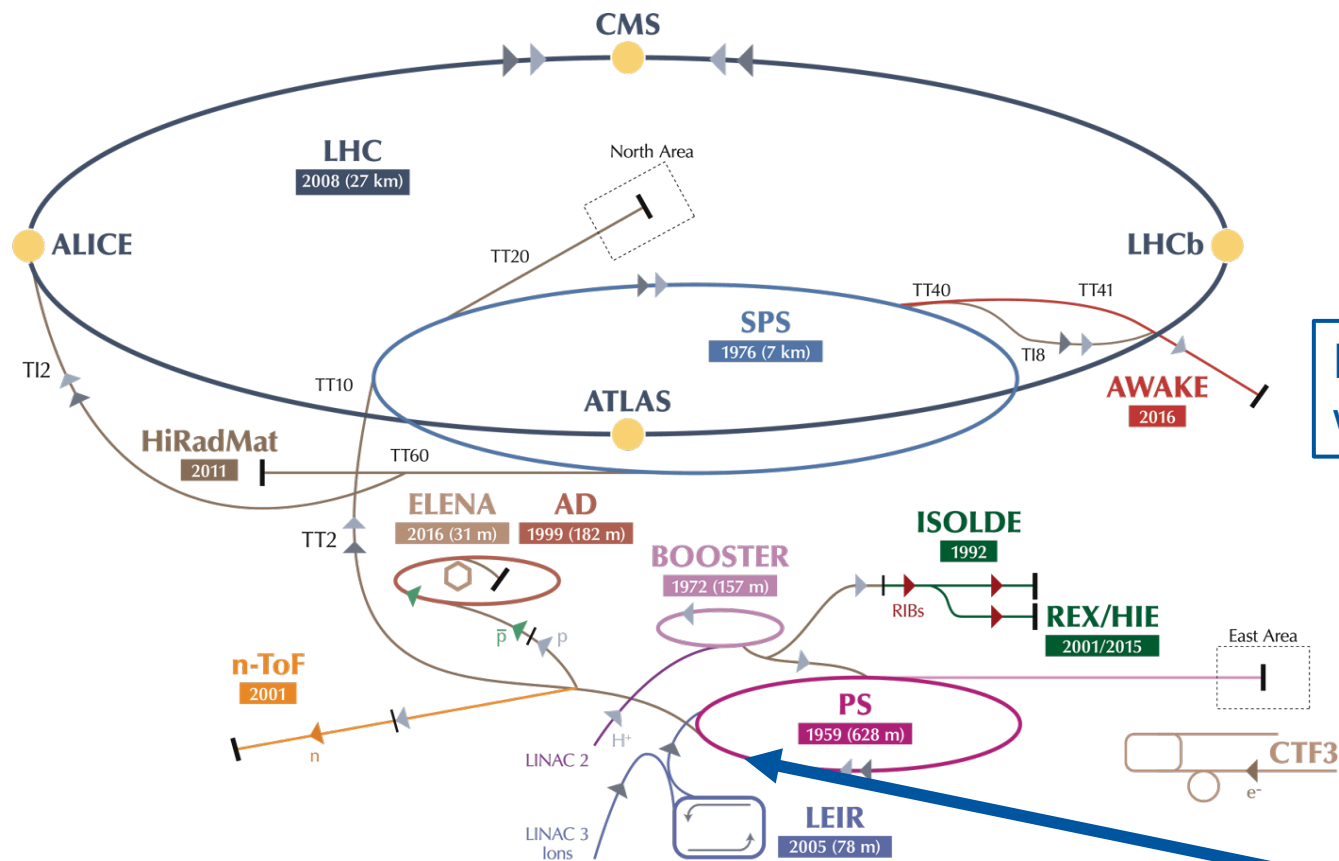
800 MeV –  $200 \mu\text{g.cm}^{-2}$  ( $\approx 1 \mu\text{m}$  of C!)

# Effect on beam emittance



# Multi-turn methods

## CERN Accelerator Complex



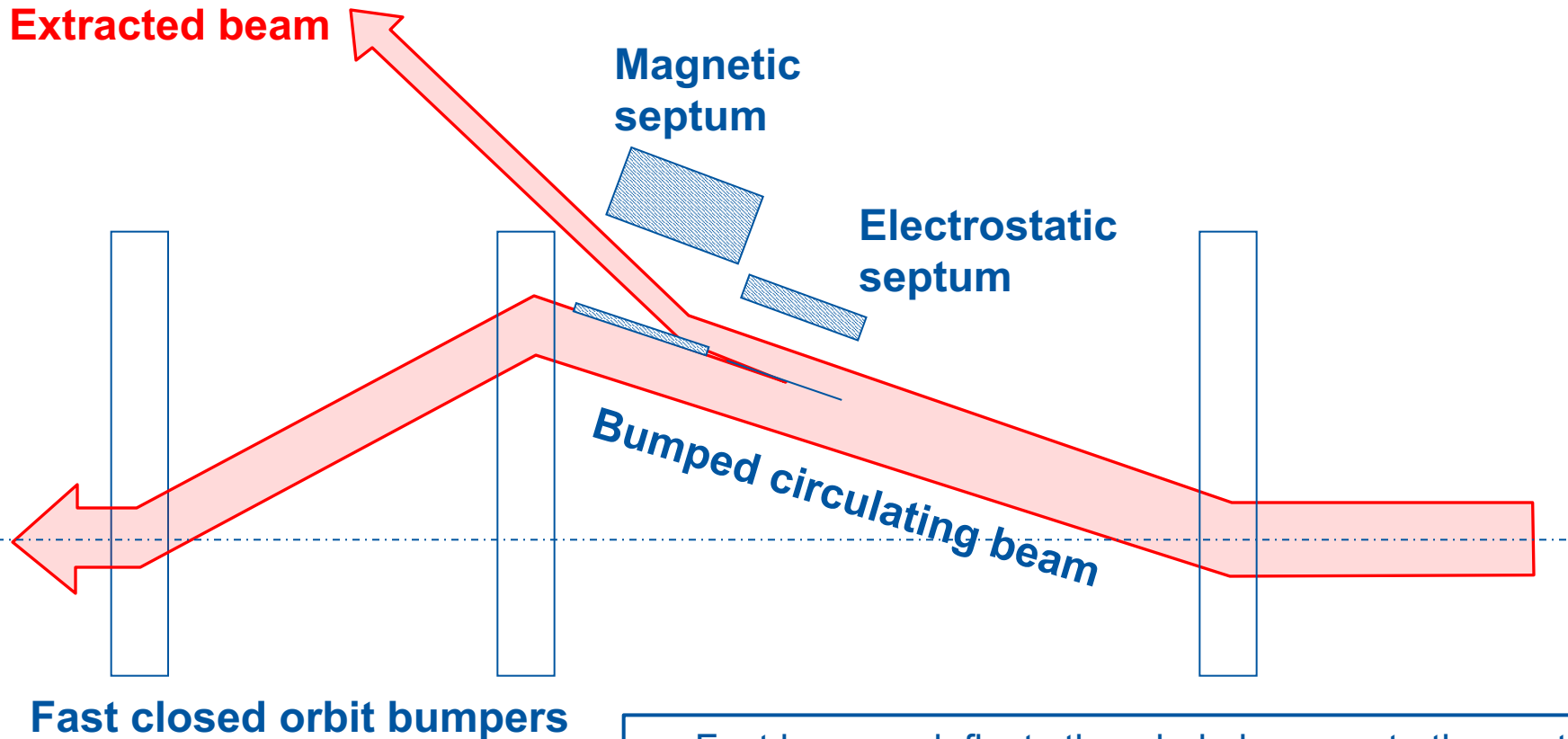
Extraction of beams within several turns

Multi-turn extraction



# Non-resonant multi-turn extraction

Beam bumped to septum; part of beam 'shaved' off each turn



- Fast bumper deflects the whole beam onto the septum
- Beam extracted in a few turns, with the machine tune rotating the beam
- Intrinsicly a high-loss process: thin septum essential
- Often combine thin electrostatic septa with magnetic septa

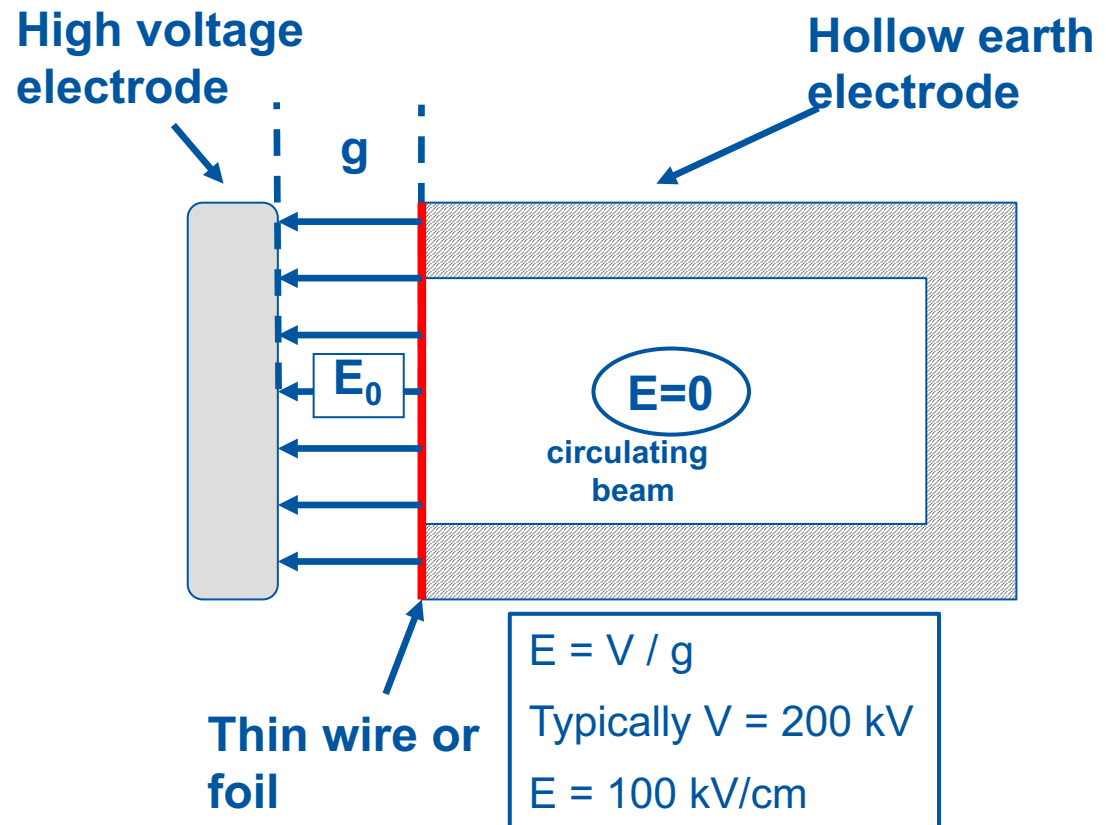
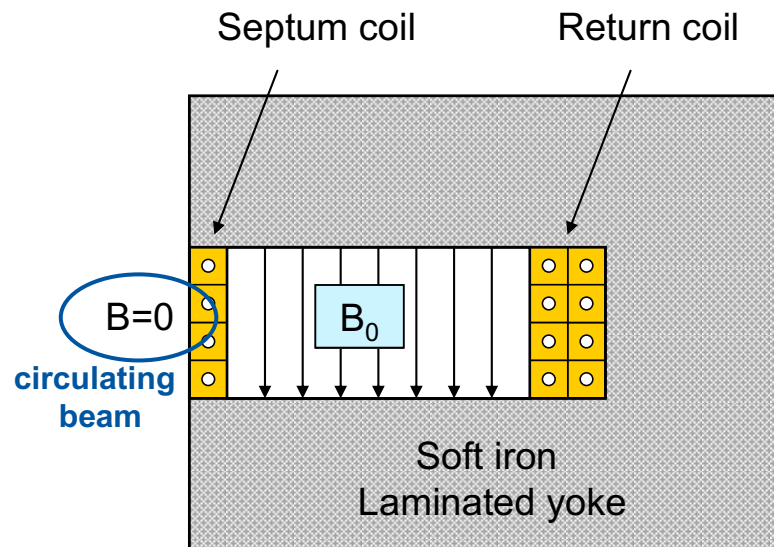
# Magnetic vs. electrostatic septum

Magnetic

Septum coil: 2 – 20 mm

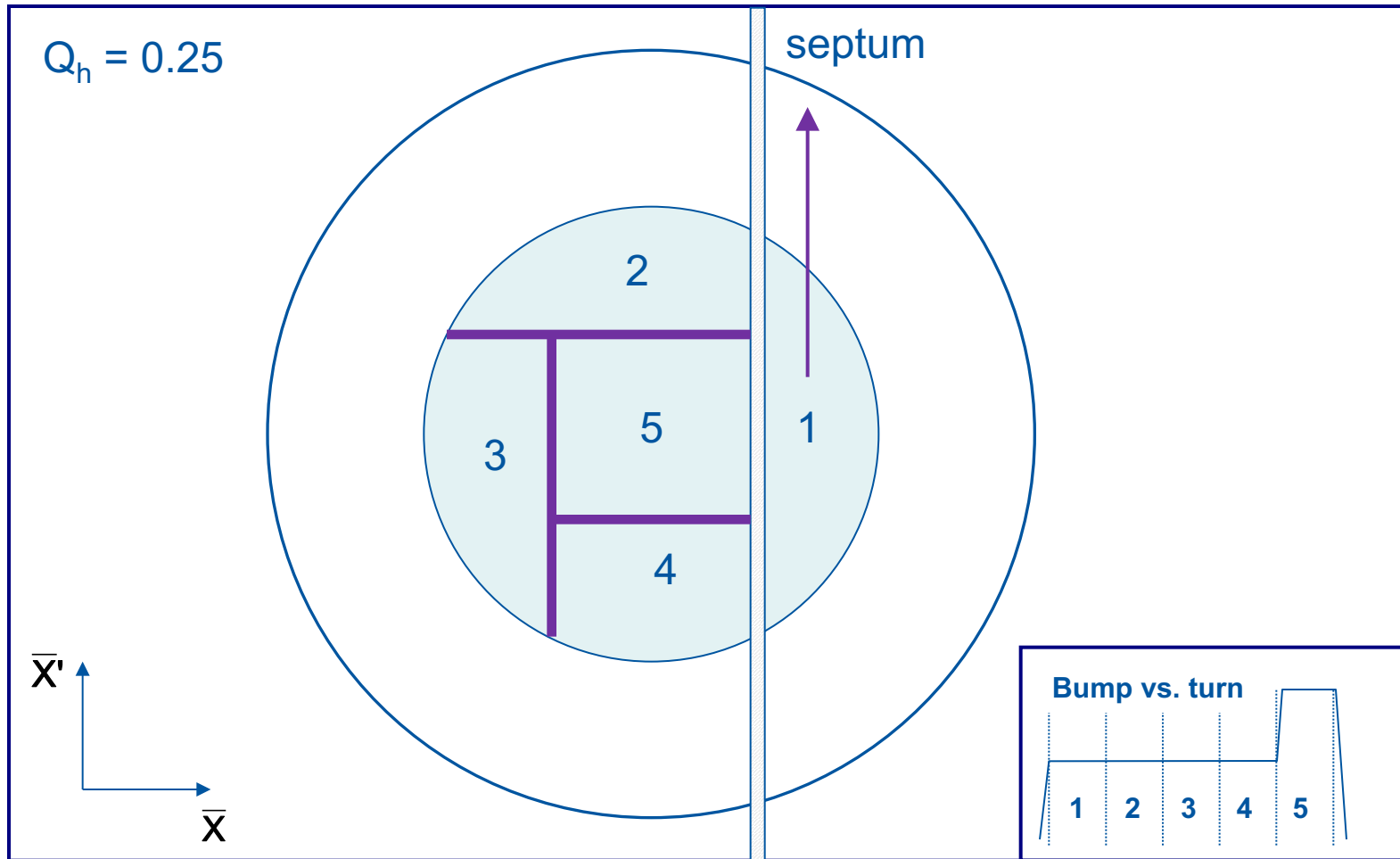
Electrostatic

Thin wire or coil: ~0.1 mm



# Non-resonant multi-turn extraction

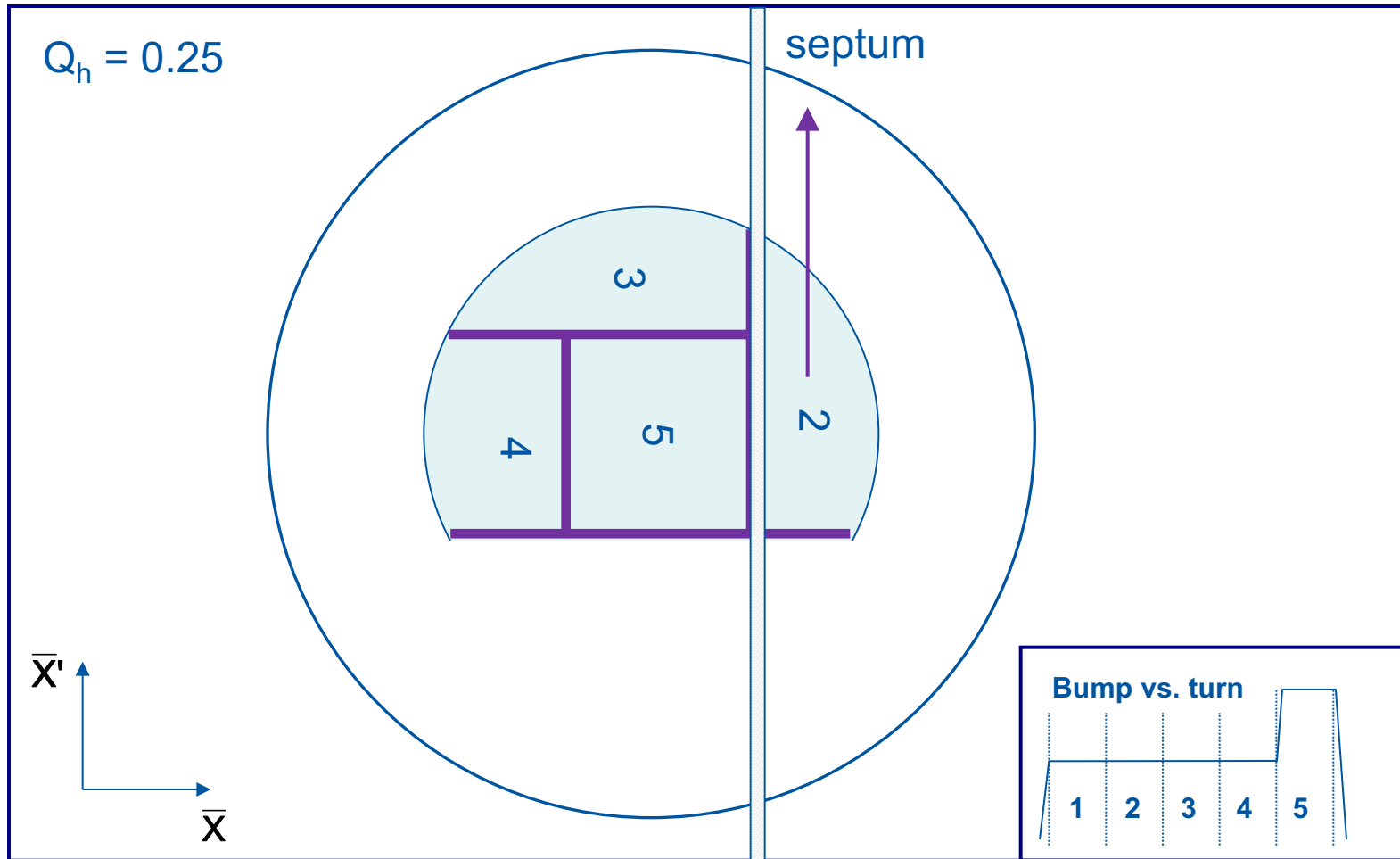
CERN PS to SPS: 5-turn continuous transfer – 1<sup>st</sup> turn





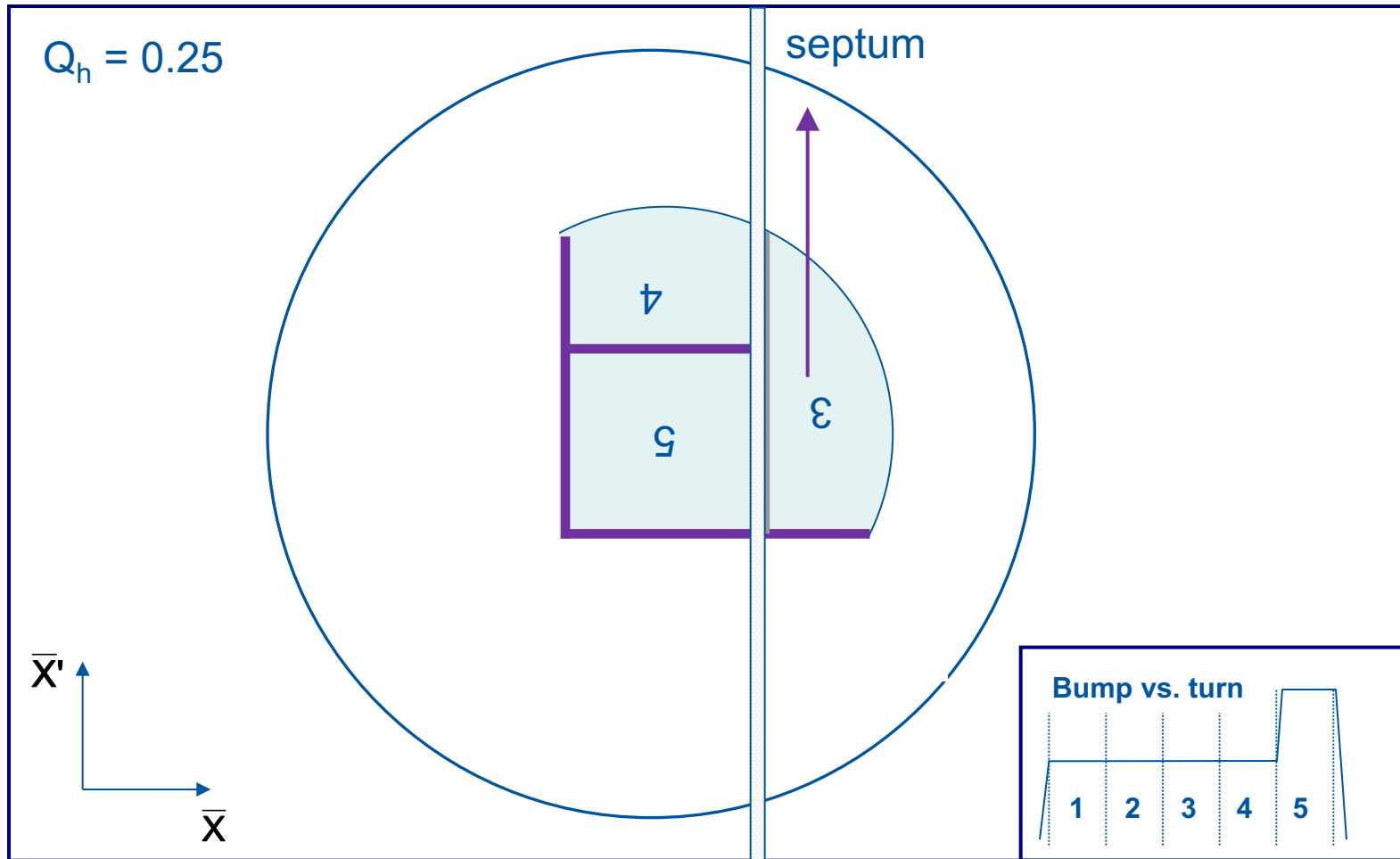
# Non-resonant multi-turn extraction

CERN PS to SPS: 5-turn continuous transfer – 2<sup>nd</sup> turn



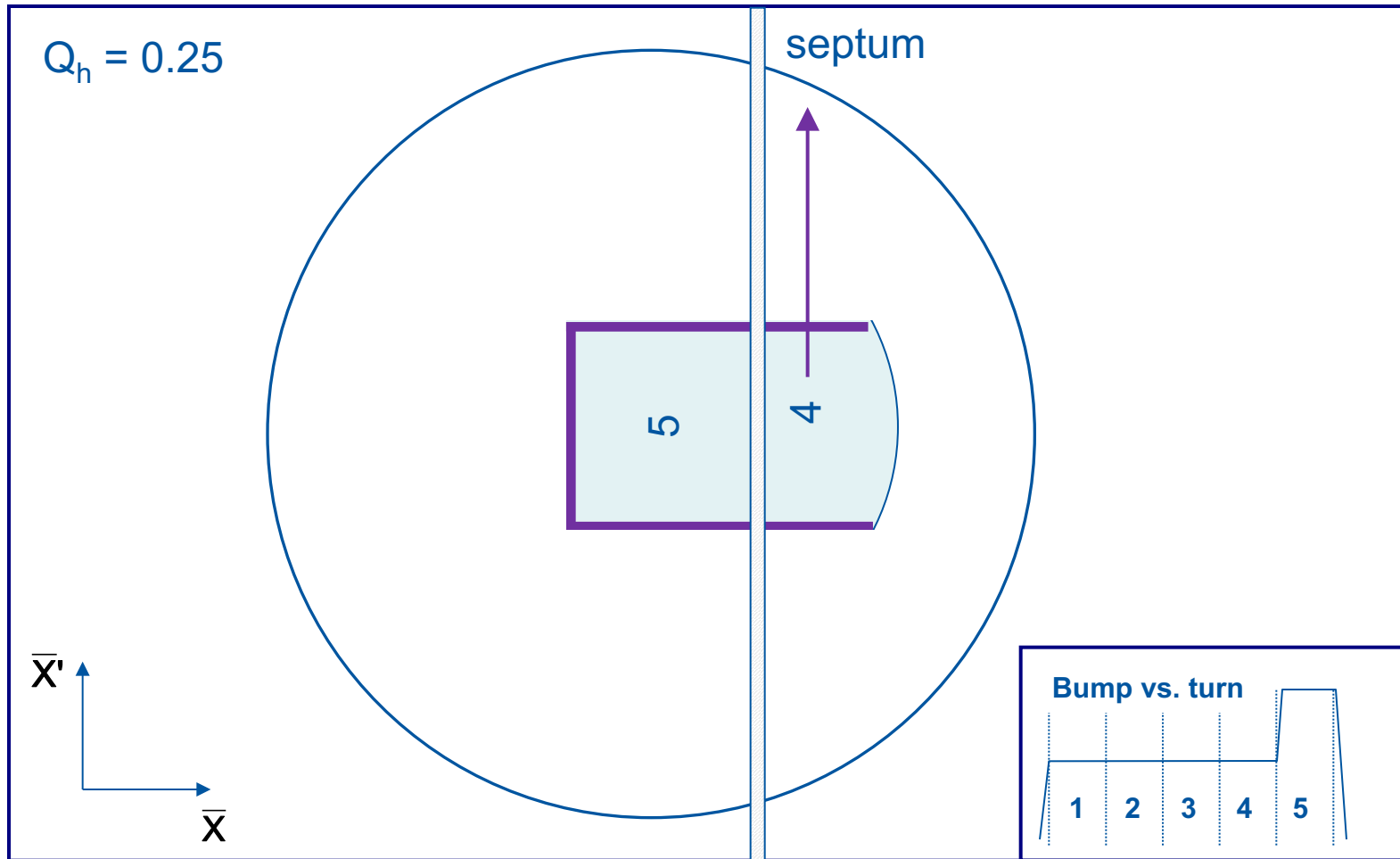
# Non-resonant multi-turn extraction

CERN PS to SPS: 5-turn continuous transfer – 3<sup>rd</sup> turn



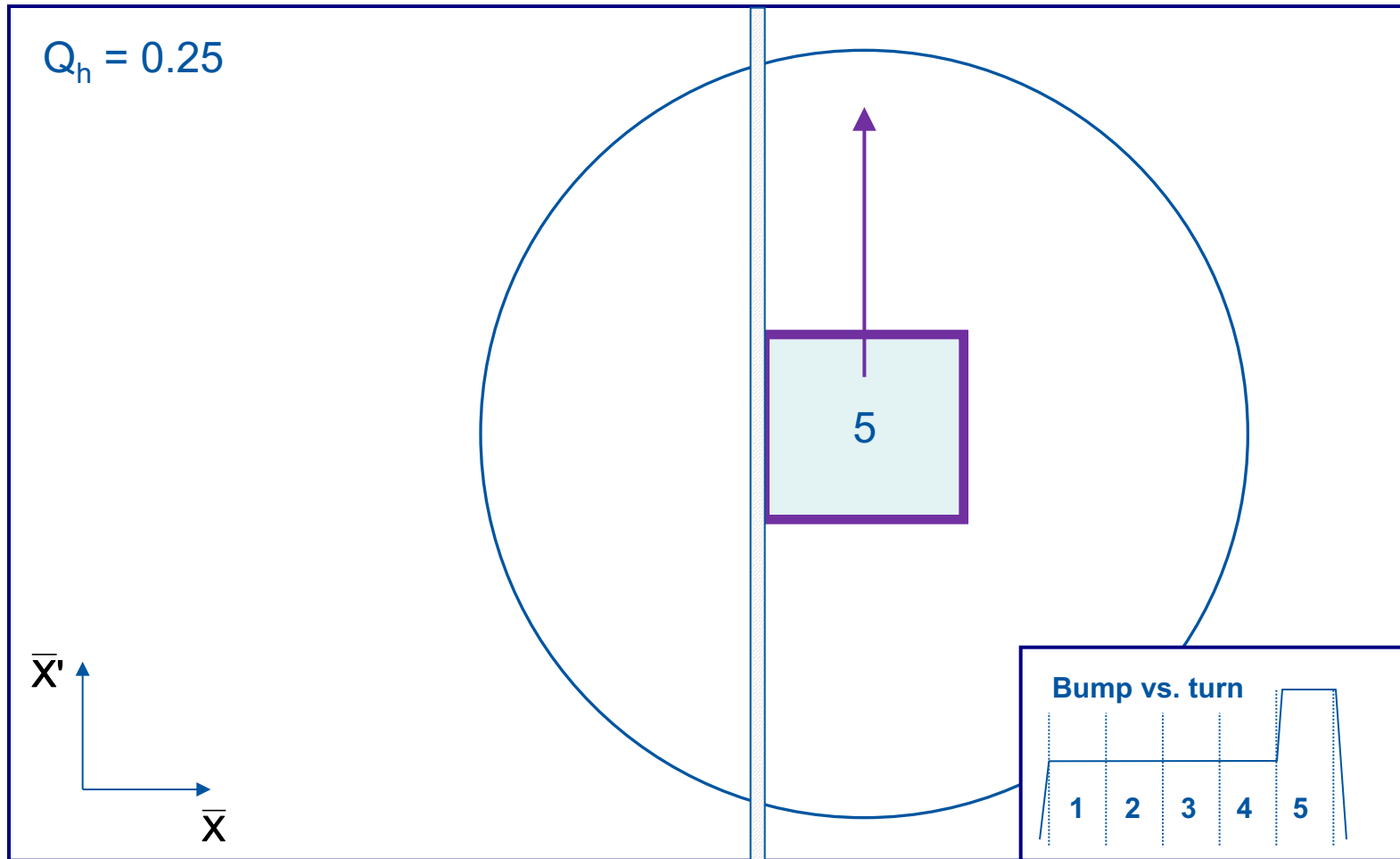
# Non-resonant multi-turn extraction

CERN PS to SPS: 5-turn continuous transfer – 4<sup>th</sup> turn



# Non-resonant multi-turn extraction

CERN PS to SPS: 5-turn continuous transfer – 5<sup>th</sup> turn

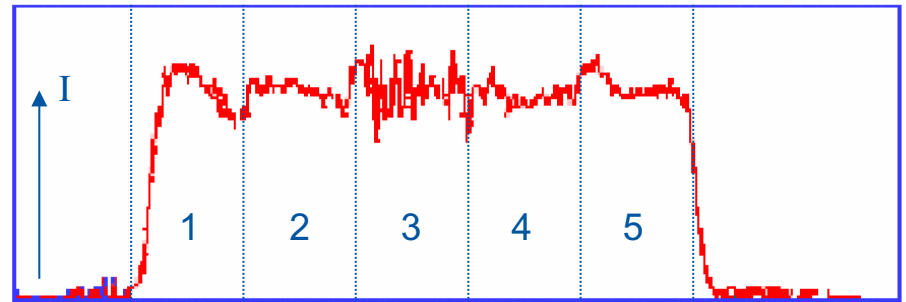


# Non-resonant multi-turn extraction

- CERN PS to SPS: 5-turn continuous transfer

Fill SPS with 2 times 5-turn  
extractions (and 2 x 1  $\mu$ s gap)

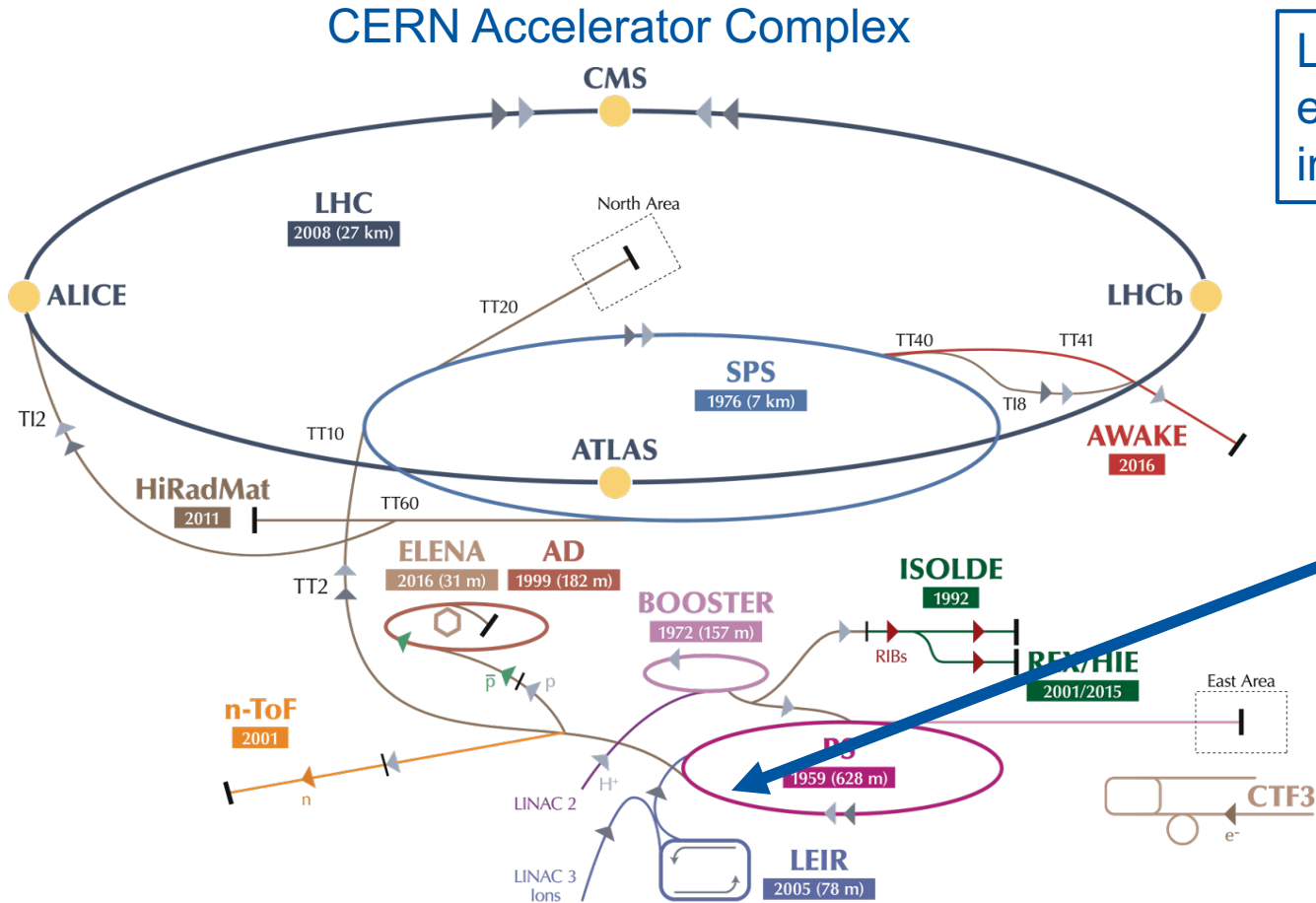
Total intensity in SPS  $5 \times 10^{13}$  p+



- Beamlets can have slightly different emittance
- Still about 15 % of beam lost in PS-SPS CT
  - Issue for maintenance of equipment

Different method needed to extract very high intensity beams → **use resonance**

# Multi-turn methods



Low-loss multi-turn extraction for high intensity beams

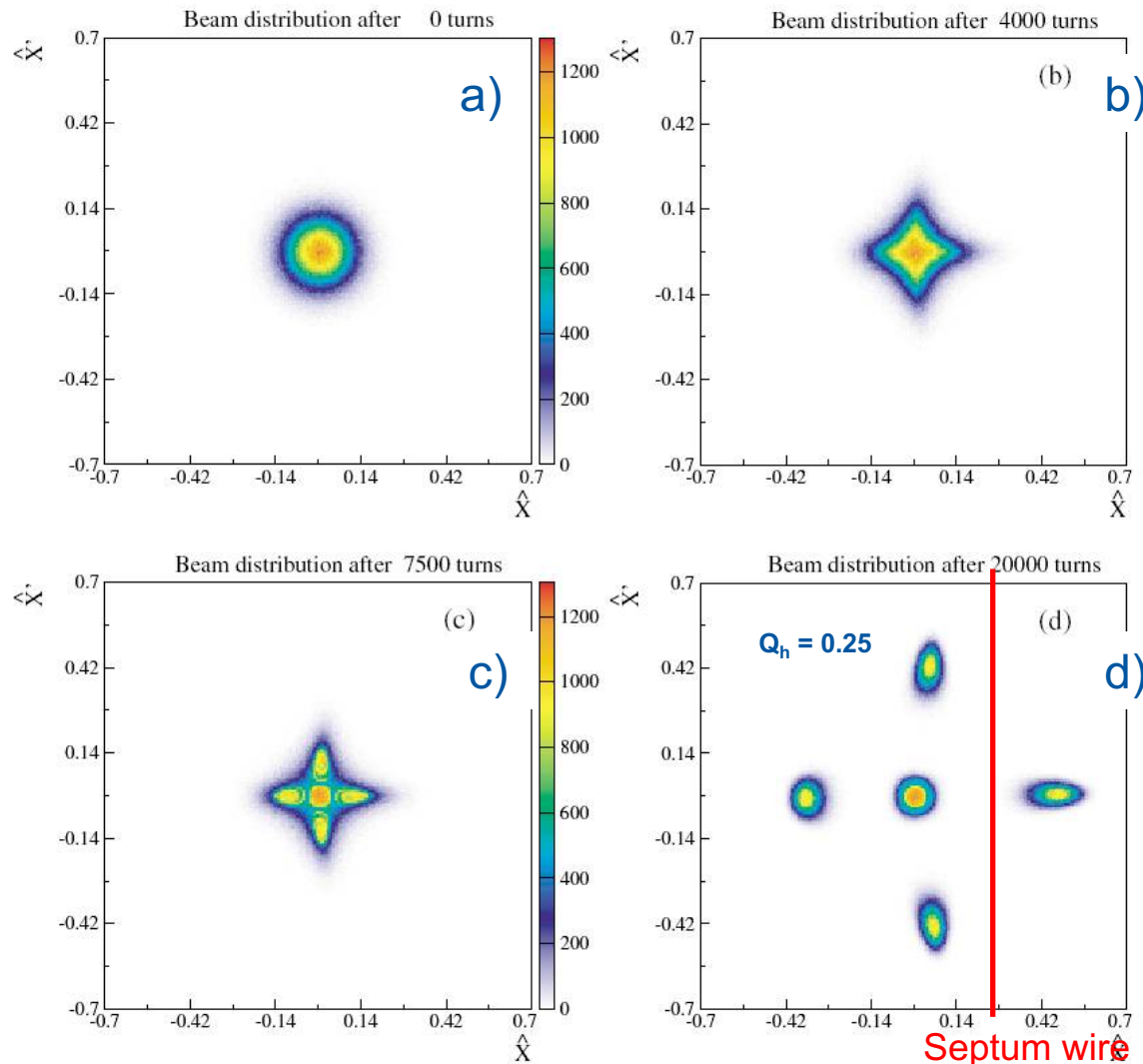
Resonant multi-turn extraction



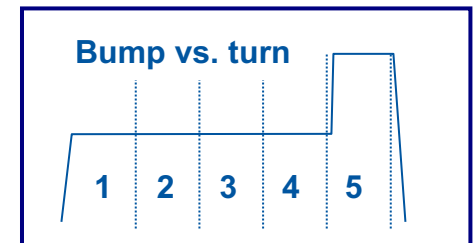
# Resonant low-loss multi-turn extraction

- Adiabatic capture of beam in stable “islands”
  - Use non-linear fields (sextupoles and octupoles) to create islands of stability in phase space
  - A slow (adiabatic) tune variation to cross a resonance and to drive particles into the islands (capture) with the help of transverse excitation (using damper)
  - Variation of field strengths to separate the islands in phase space
- Several big advantages:
  - Losses reduced significantly (no particles at the septum in transverse plane)
  - Phase space matching improved with respect to existing non-resonant multi-turn extraction - ‘beamlets’ have similar emittance and optical parameters

# Resonant low-loss multi-turn extraction



- a) Unperturbed beam
- b) Increasing non-linear fields
- c) Beam captured in stable islands
- d) Islands separated and beam bumped across septum – extracted in 5 turns

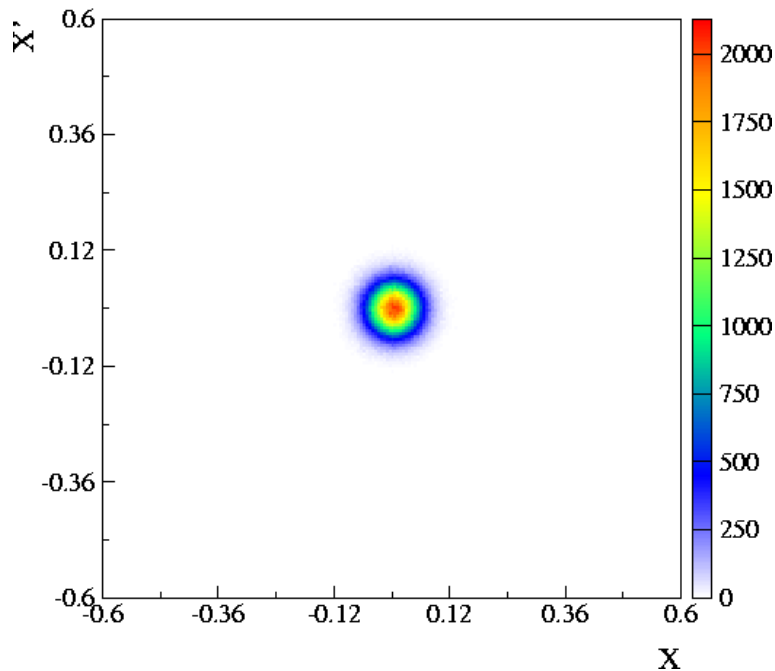
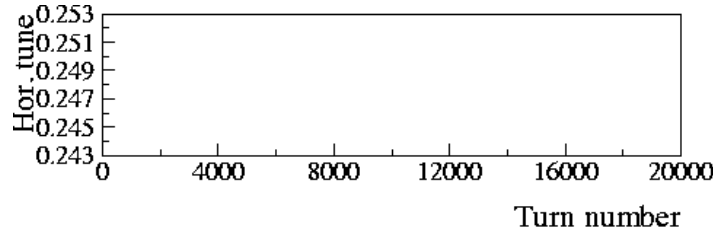


Courtesy M. Giovannozzi: MTE Design Report, CERN-2006-011, 2006



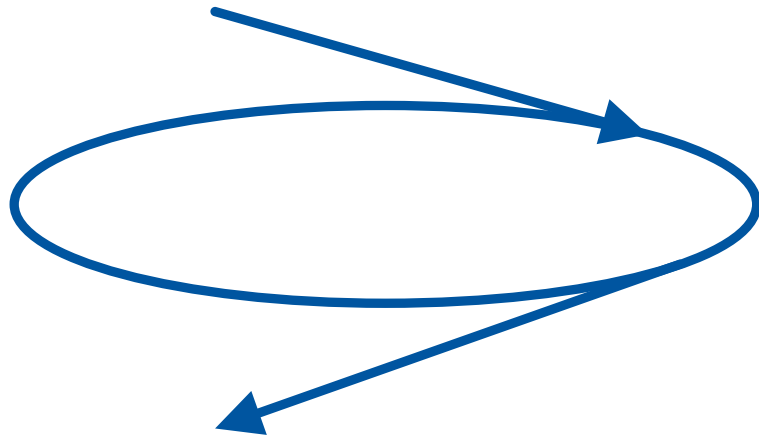
# Resonant low-loss multi-turn extraction

- a) Unperturbed beam
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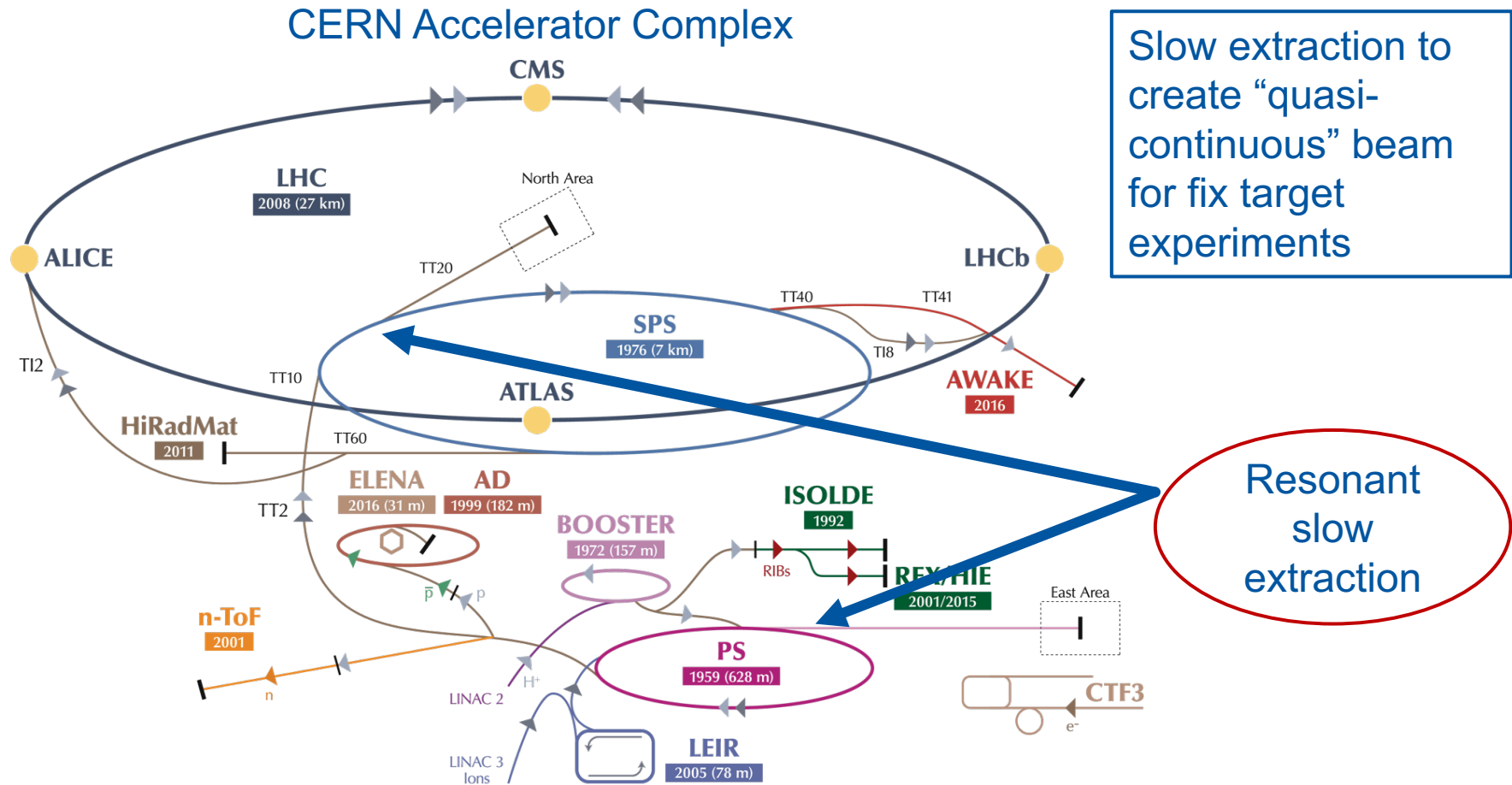
Courtesy M. Giovannozzi: MTE Design Report, CERN-2006-011, 2006

# Overview



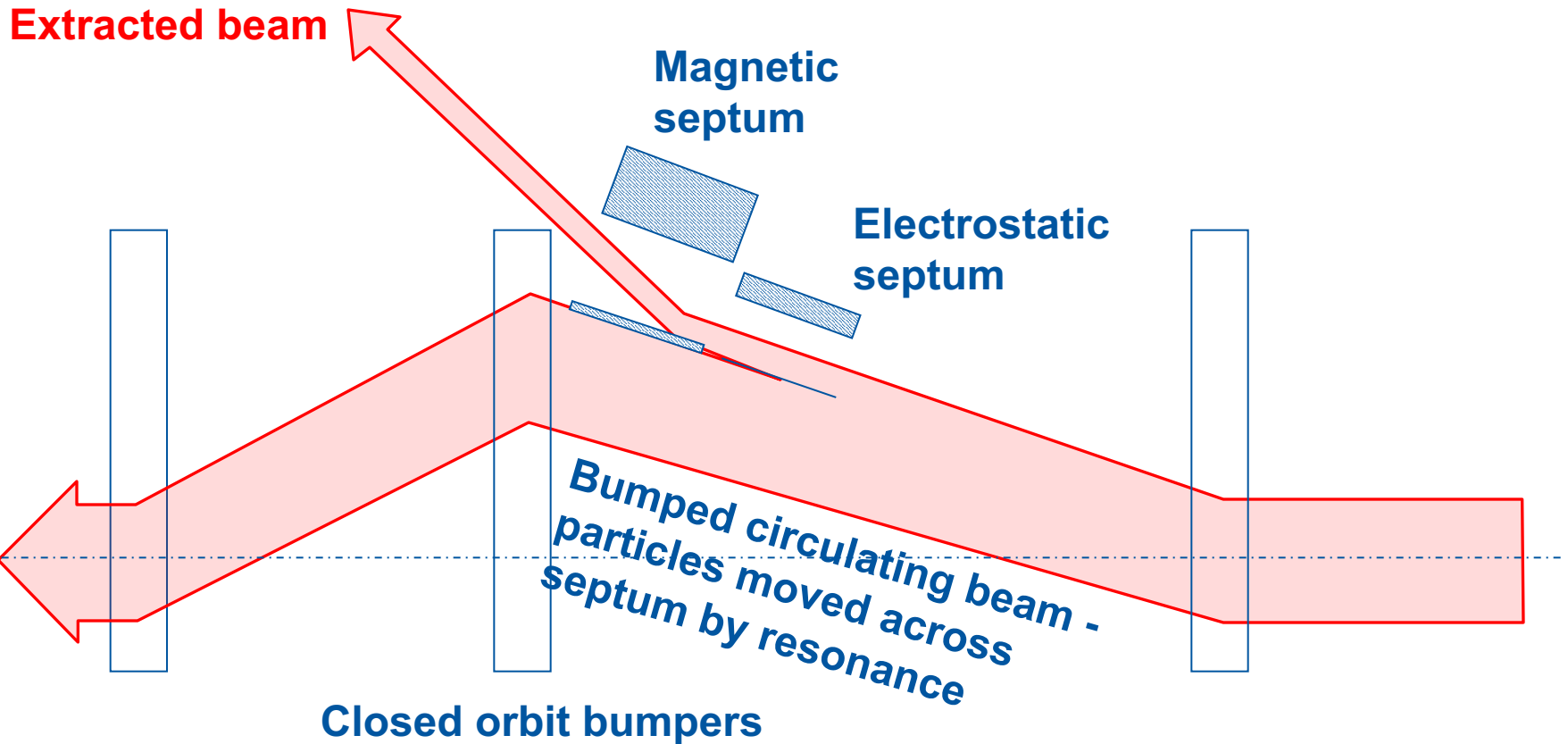
- Introduction
- Single-turn methods
  - Injection
  - Fast extraction
- Multi-turn methods
  - Multi-turn hadron injection
  - Charge-exchange H- injection
  - Multi-turn extraction
- **Resonant slow extraction**
- Summary

# Resonant slow extraction



# Resonant slow extraction

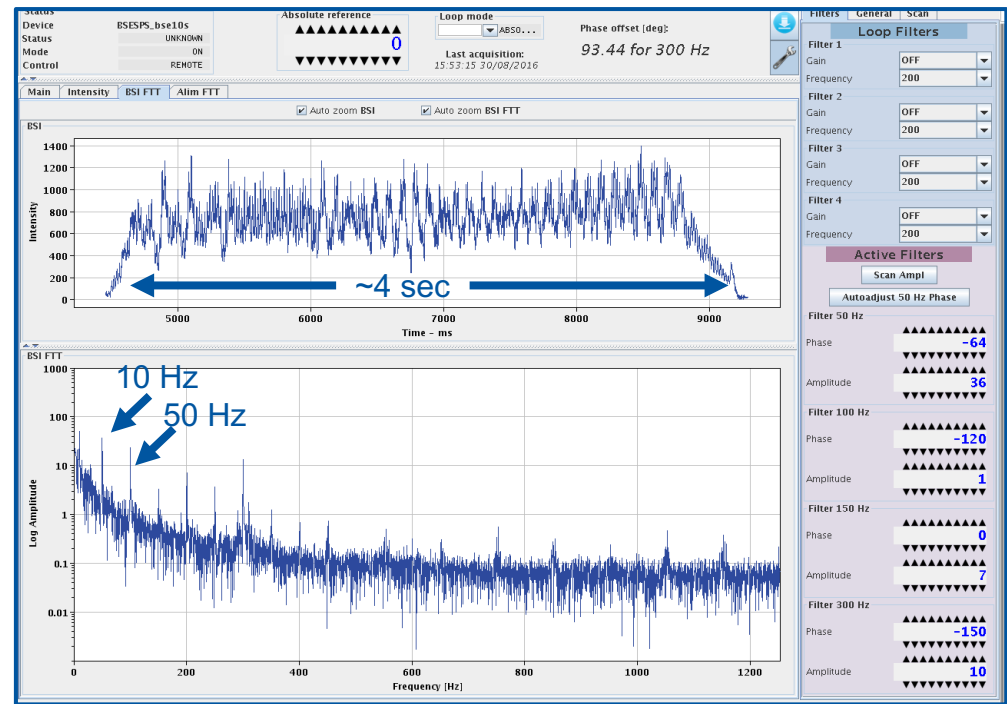
Non-linear fields excite resonances that drive the beam slowly across the septum



- Slow bumpers move the beam near the septum
- Tune adjusted close to  $n^{\text{th}}$  order betatron resonance
- Multipole magnets excited to define stable area in phase space, size depends on  $\Delta Q = Q - Q_r$

# 3rd-order resonant slow extraction

- Sextupoles are used to excite a resonance for extraction
- This resonance slowly drives particles over septum for extraction (> 1000 turns)
- Results in long spills for experiments (milliseconds to hours)

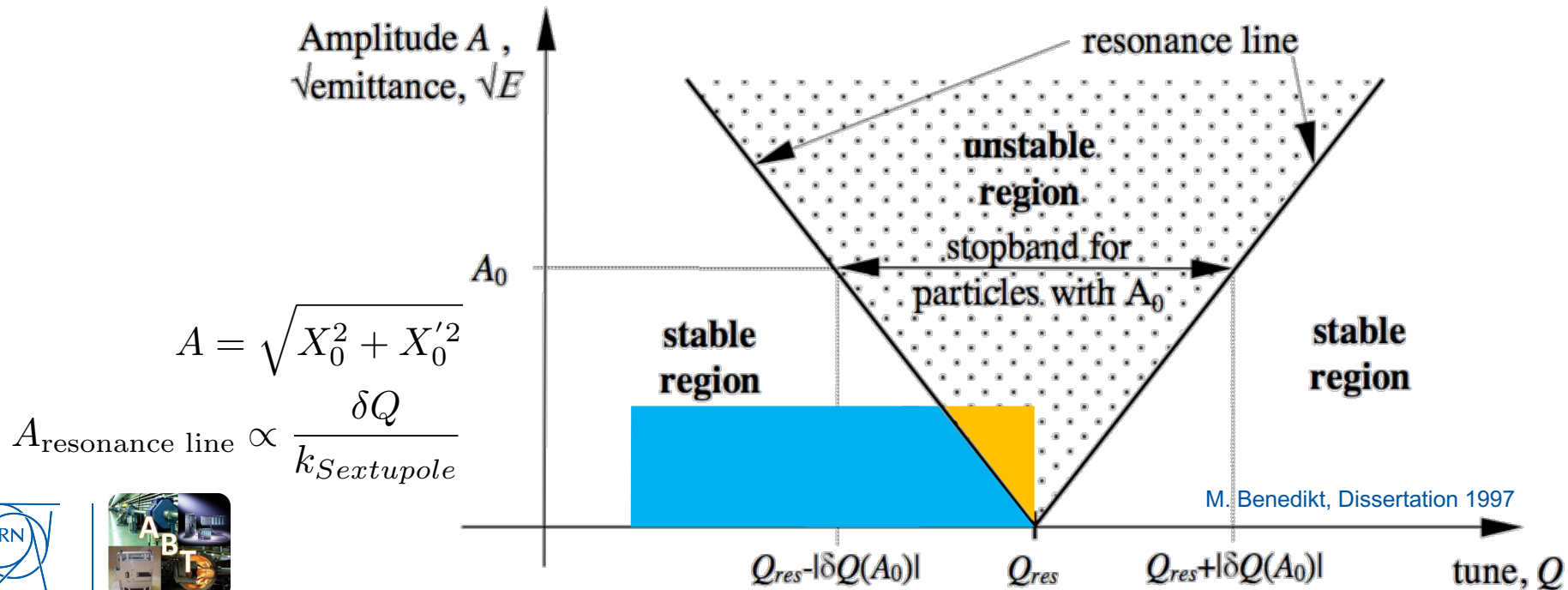


Example of a spill at SPS to the North Area with large  $n \times 50$  Hz components and another noise source at 10 Hz

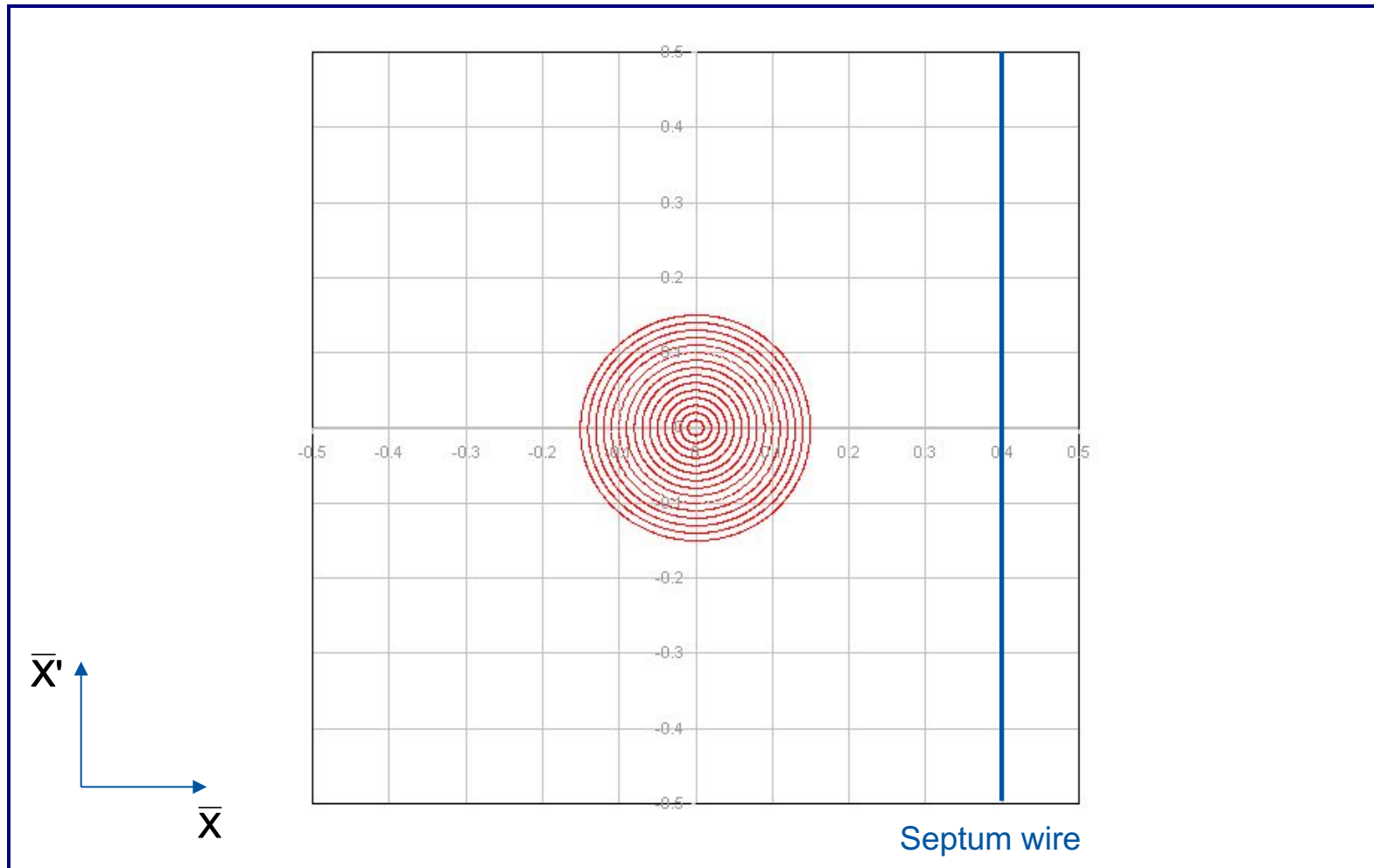


# Extraction process

- Increase the sextupole strength to excite resonance
- Large tune spread created with RF gymnastics (large momentum spread) and large chromaticity to reduce stable region in phase space
- Move beam into the resonance by changing the tune

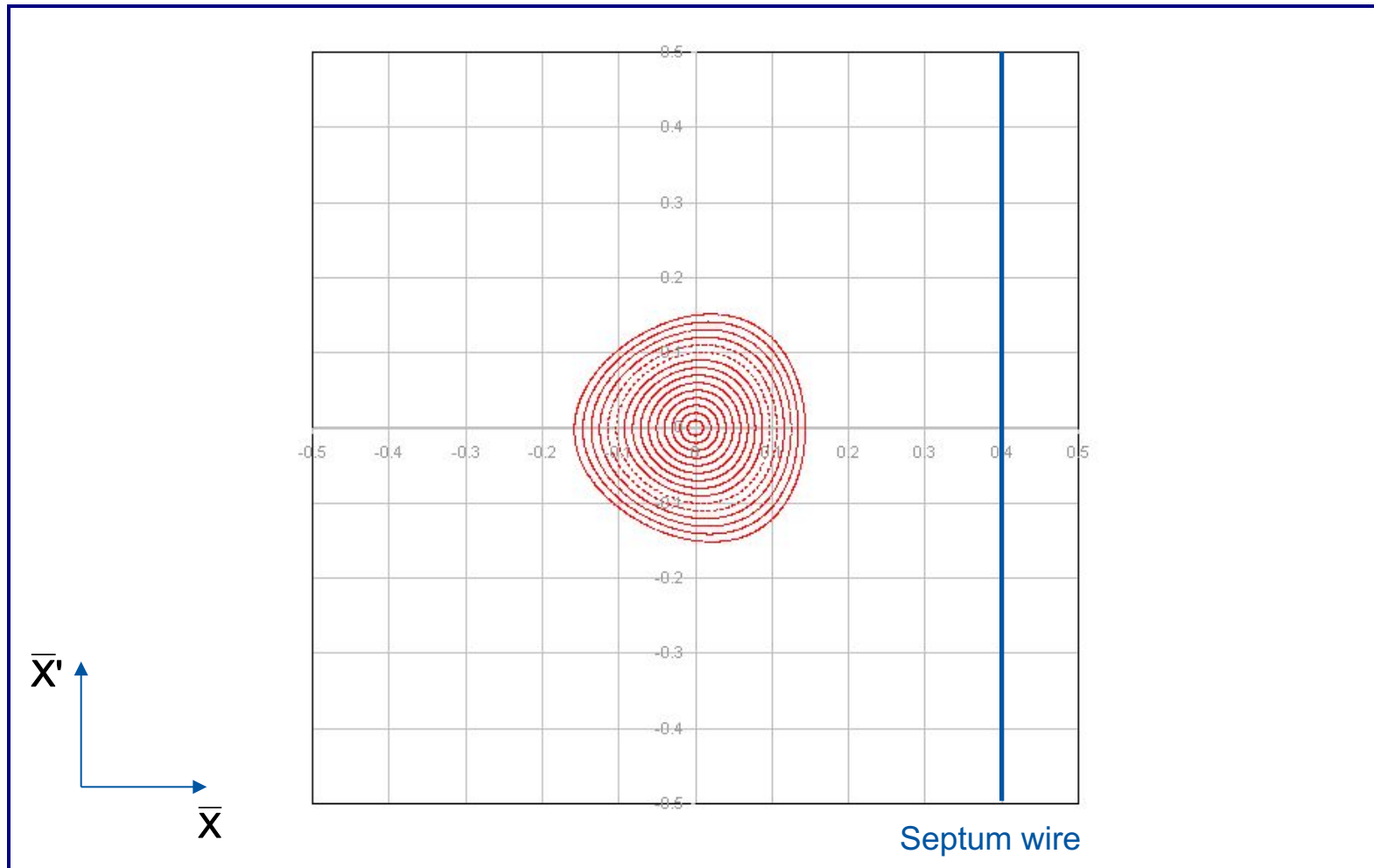


# 3rd-order resonant slow extraction



- Particles distributed on emittance contours
- $\Delta Q$  large – no phase space distortion

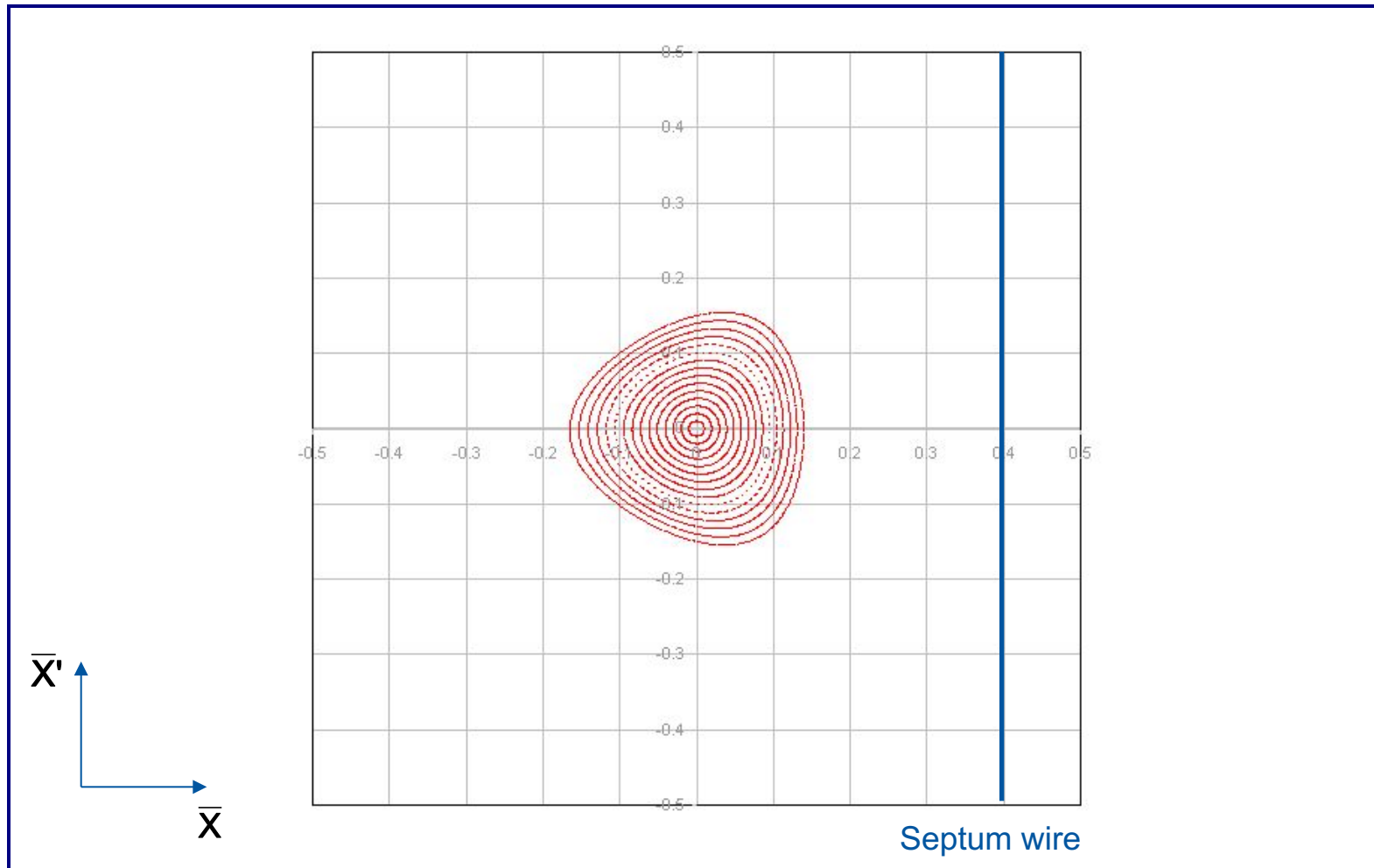
# 3rd-order resonant slow extraction



- Sextupole magnets produce a triangular stable area in phase space
- $\Delta Q$  decreasing – phase space distortion for largest amplitudes

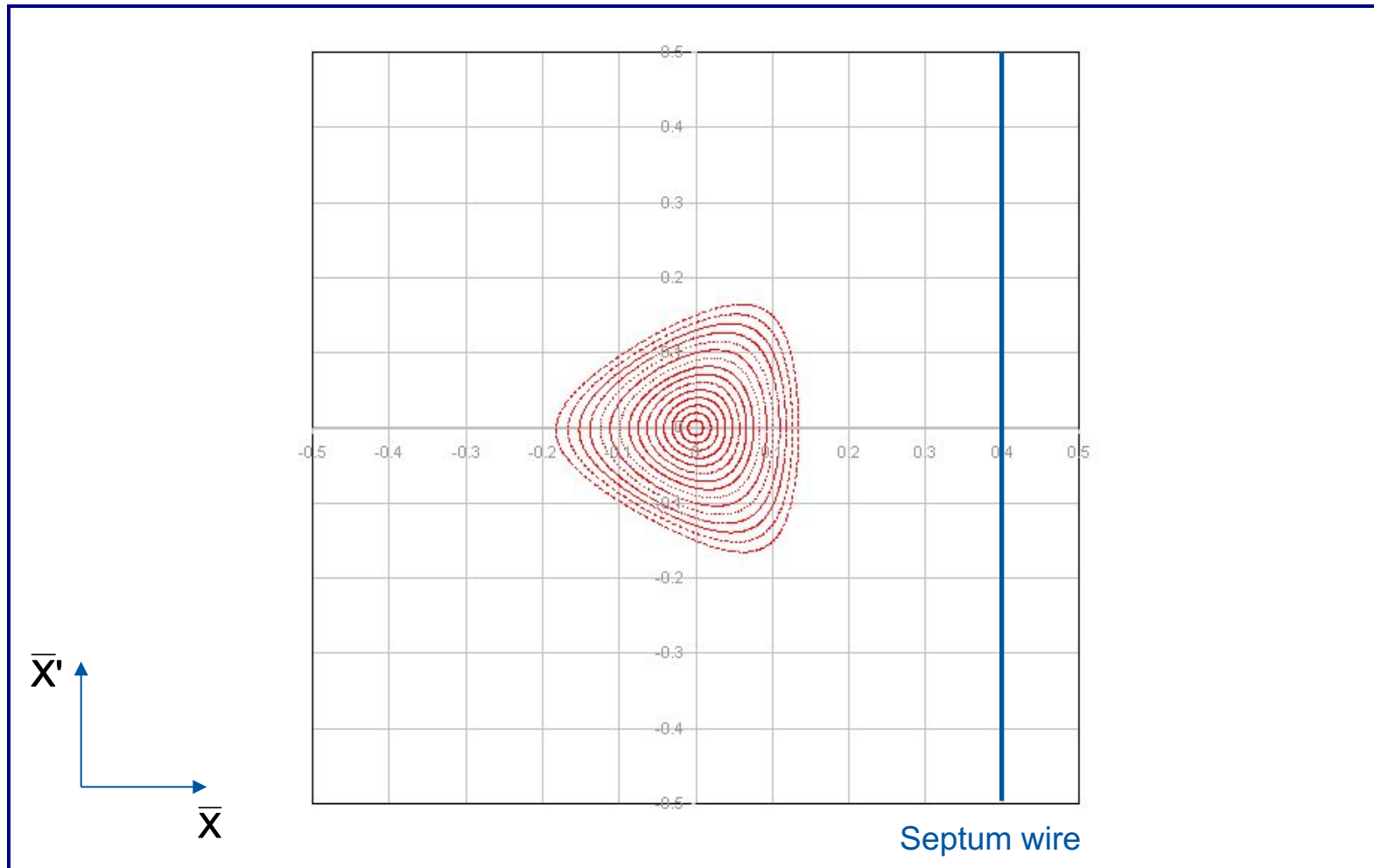


# 3rd-order resonant slow extraction



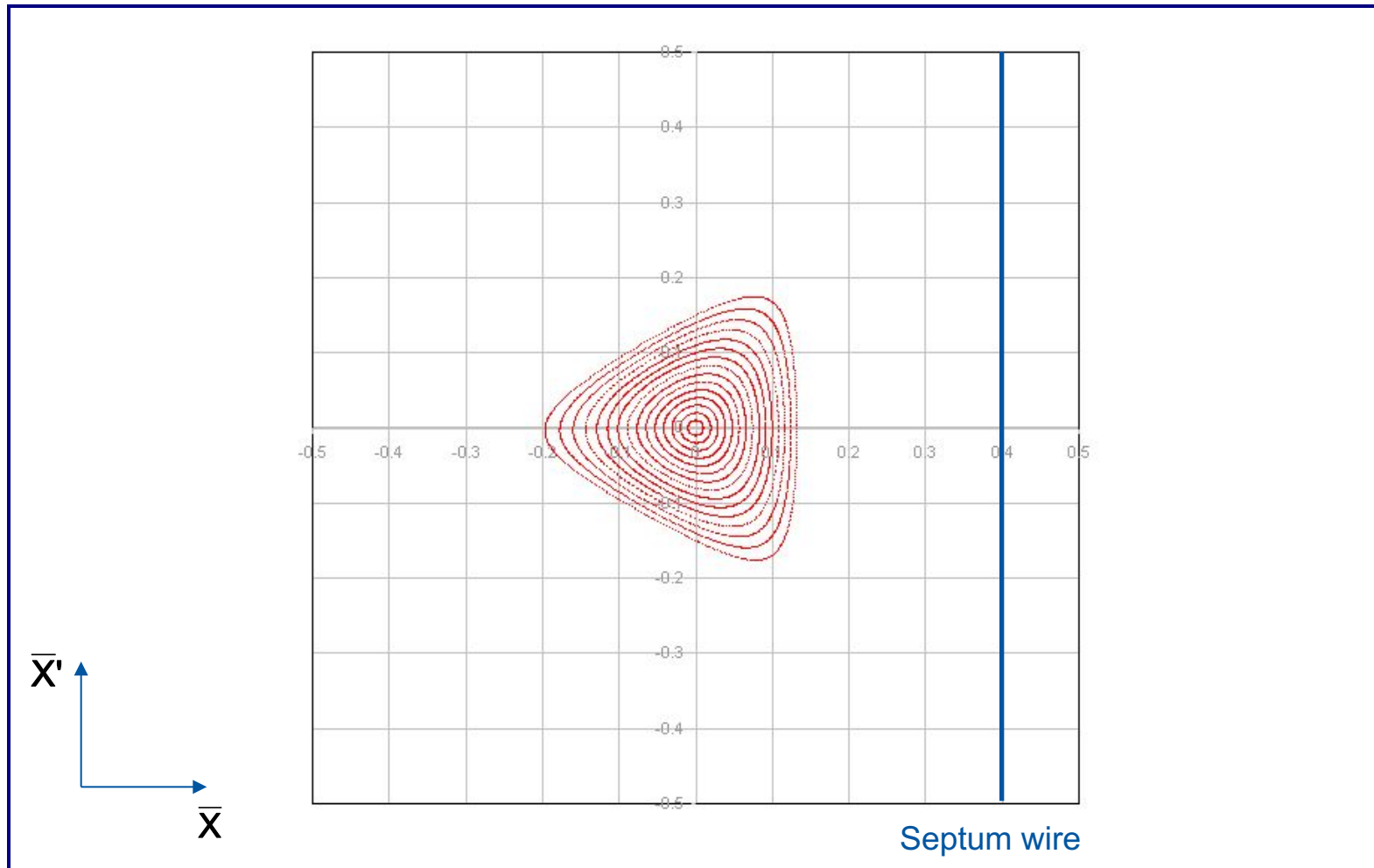
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# 3rd-order resonant slow extraction



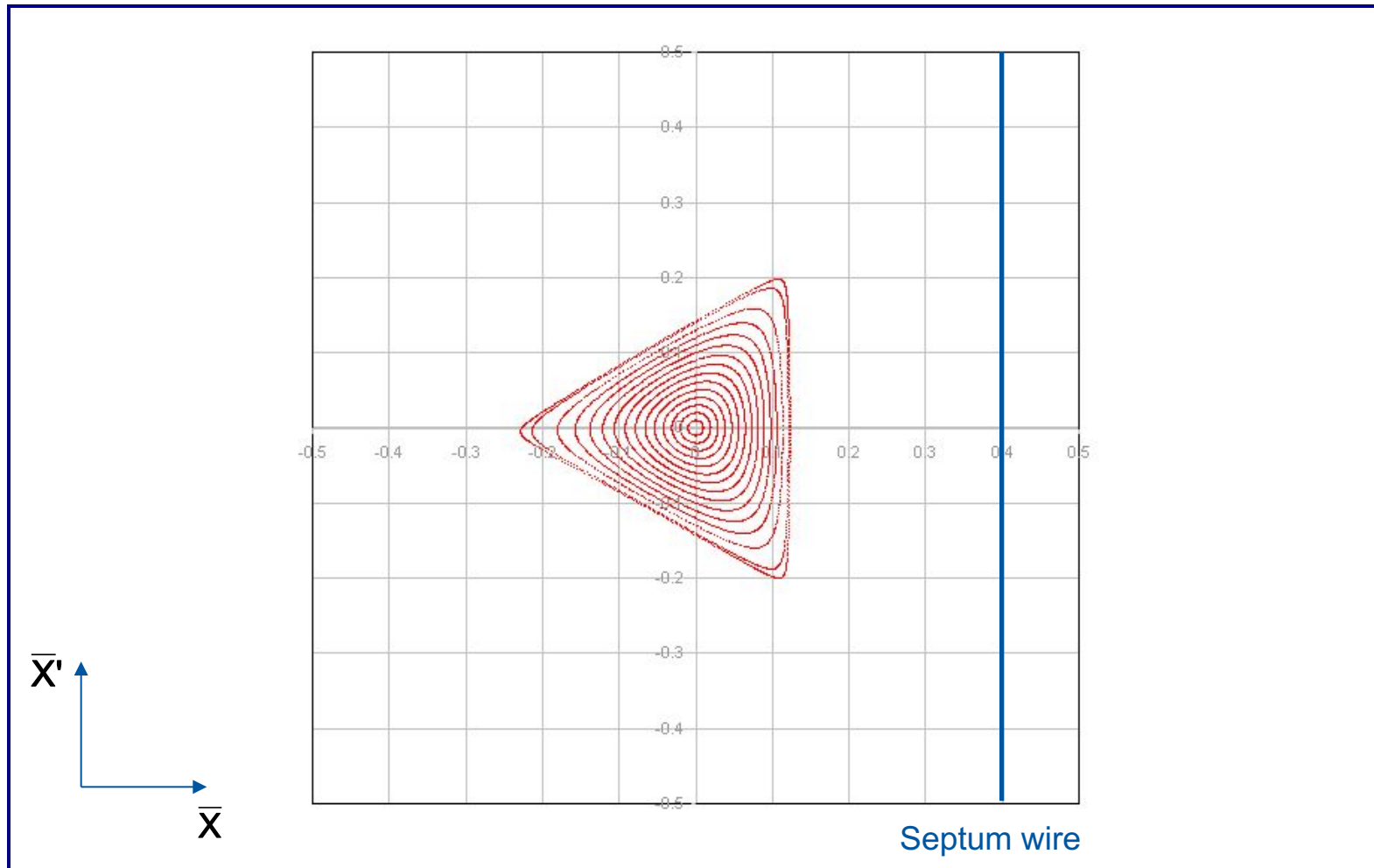
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# 3rd-order resonant slow extraction



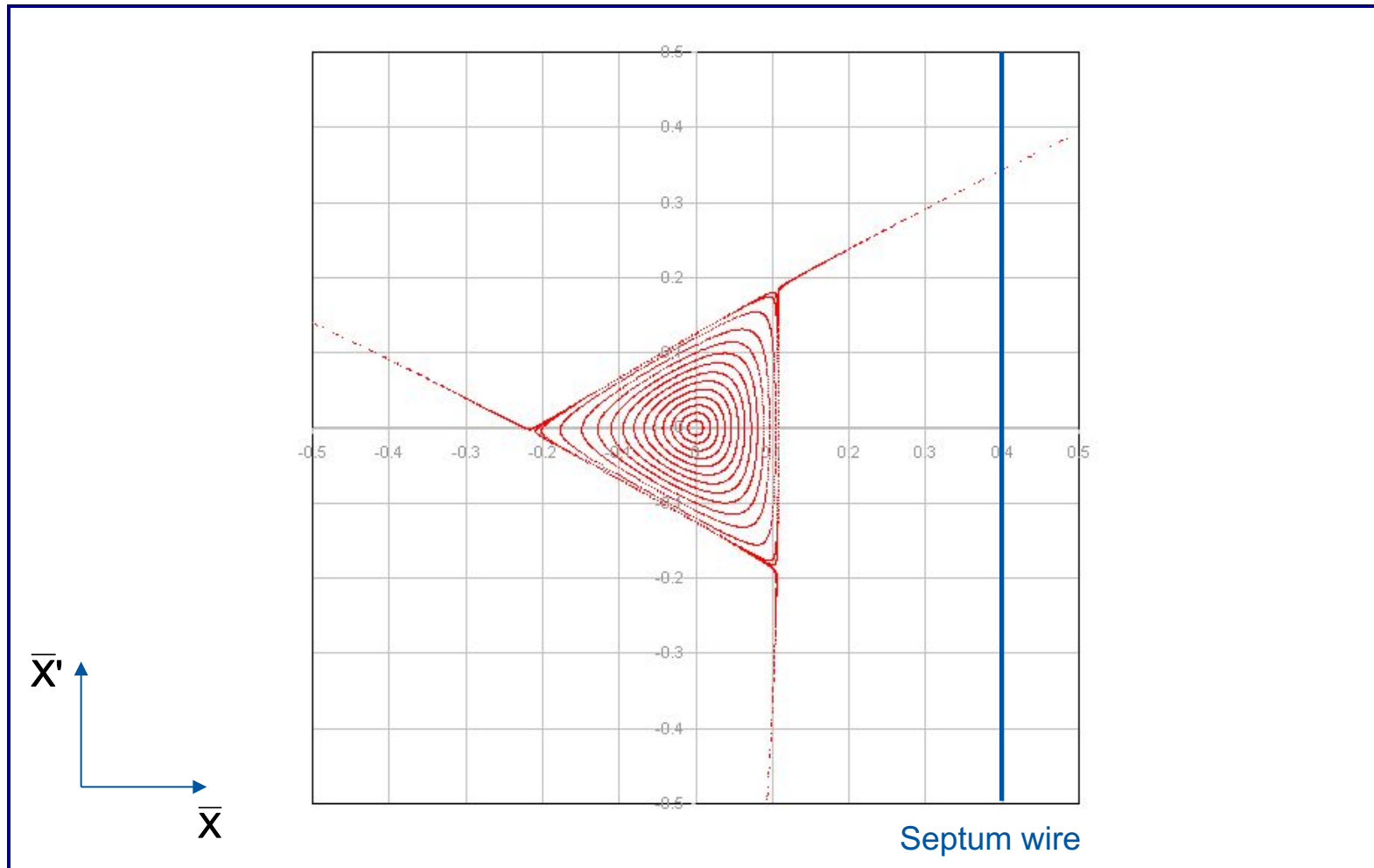
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# 3rd-order resonant slow extraction



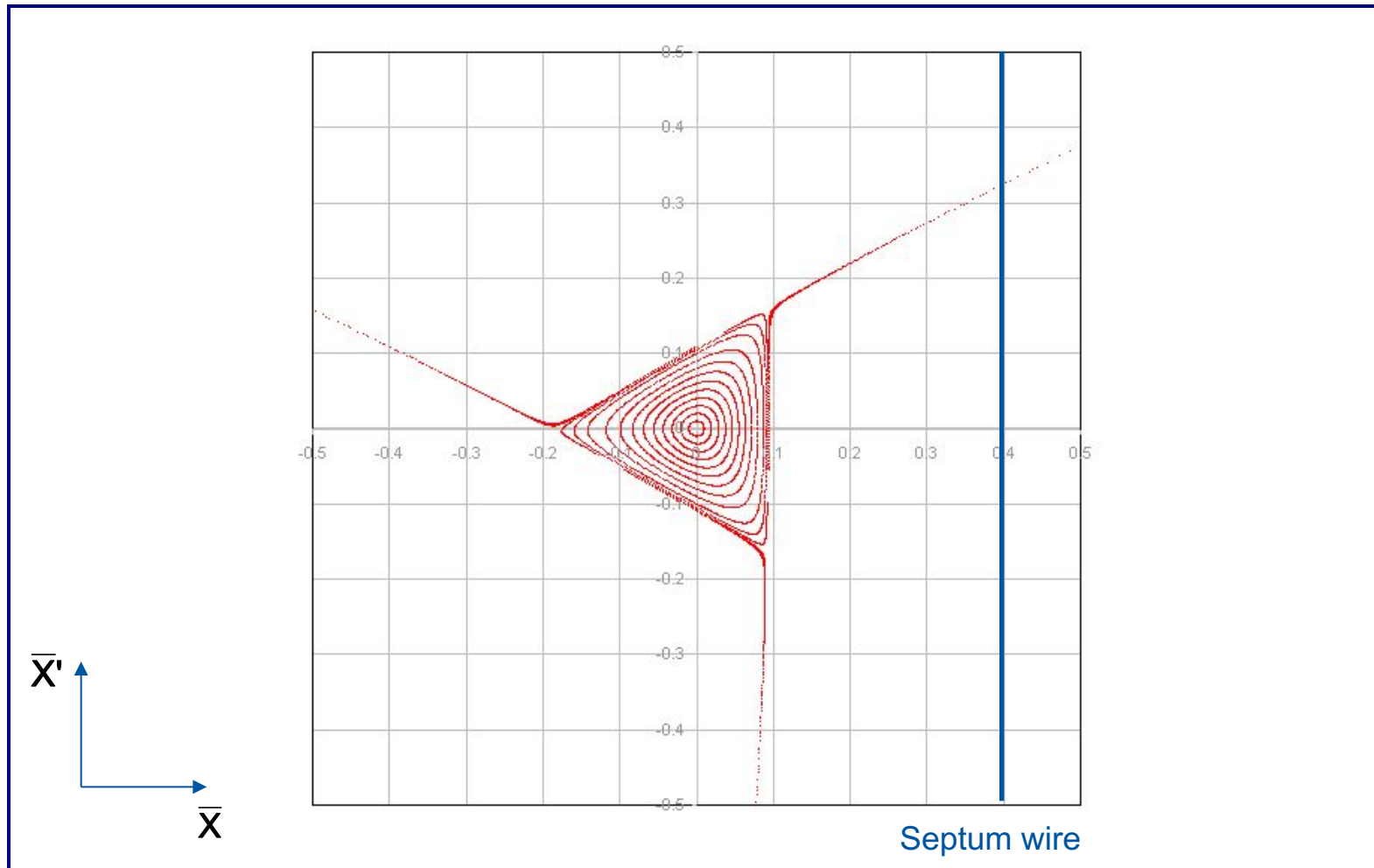
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# 3rd-order resonant slow extraction



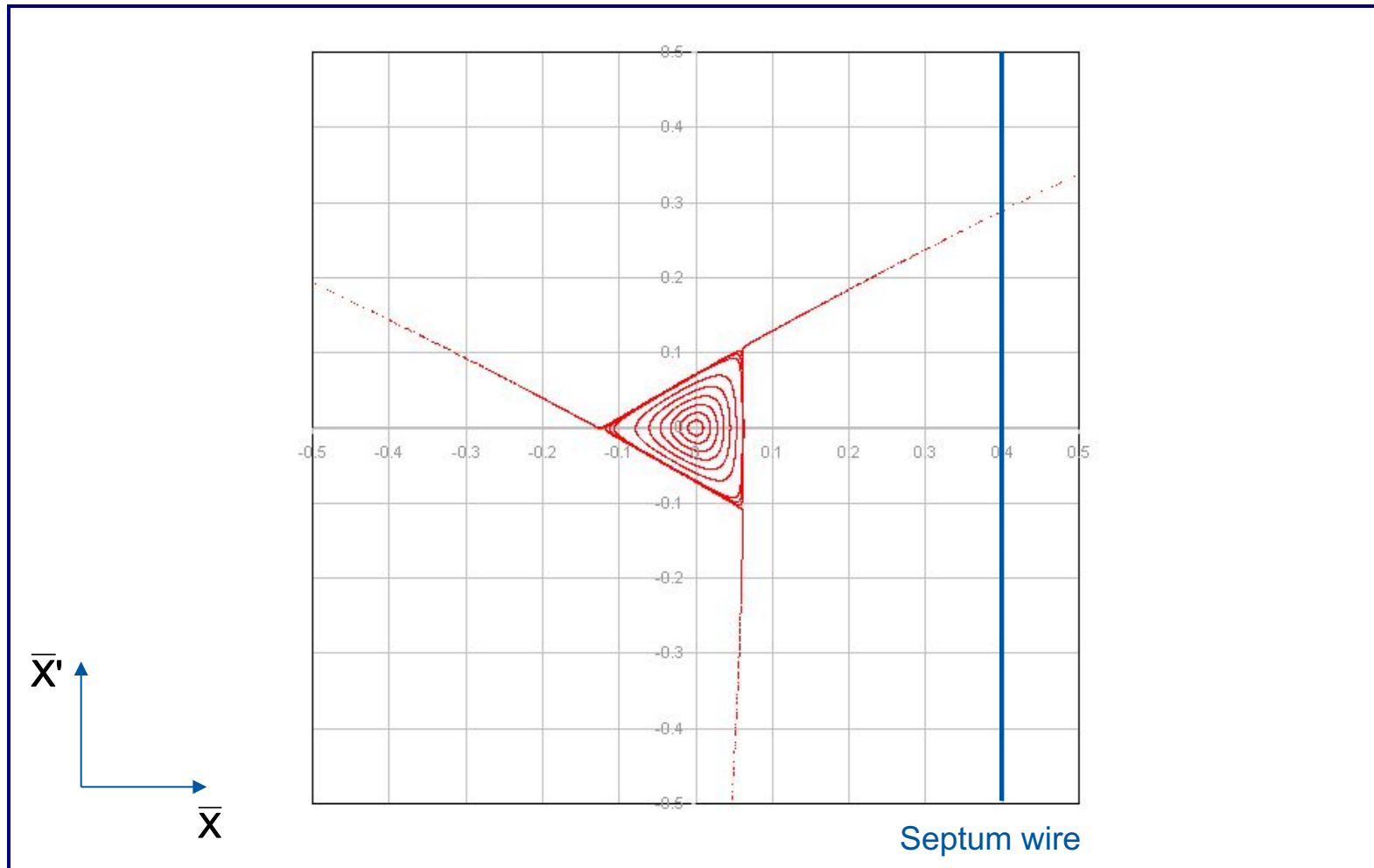
- Sextupole magnets produce a triangular stable area in phase space
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# 3rd-order resonant slow extraction



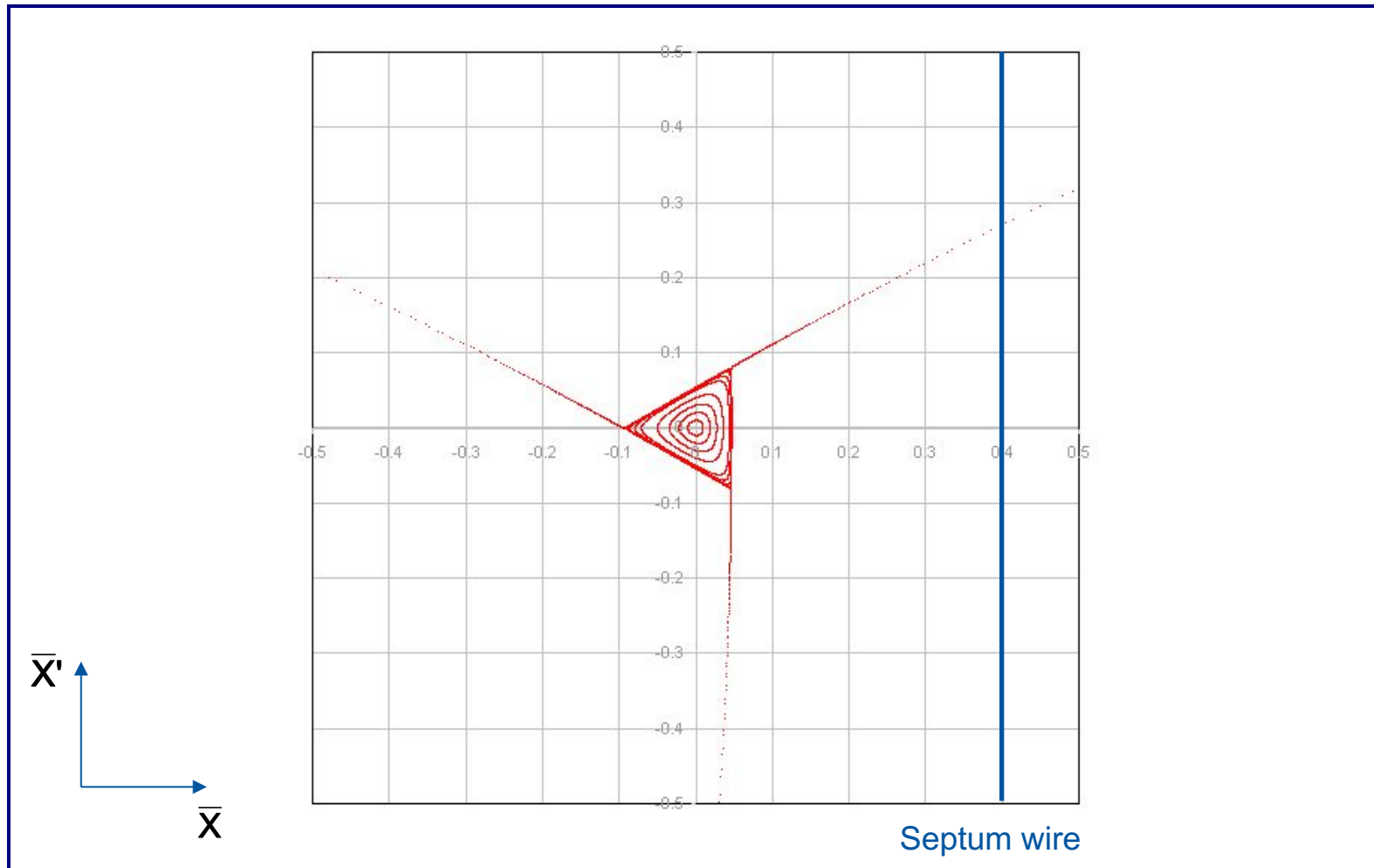
- Stable area shrinks as  $\Delta Q$  becomes smaller

# 3rd-order resonant slow extraction



- Separatrix position in phase space shifts as the stable area shrinks

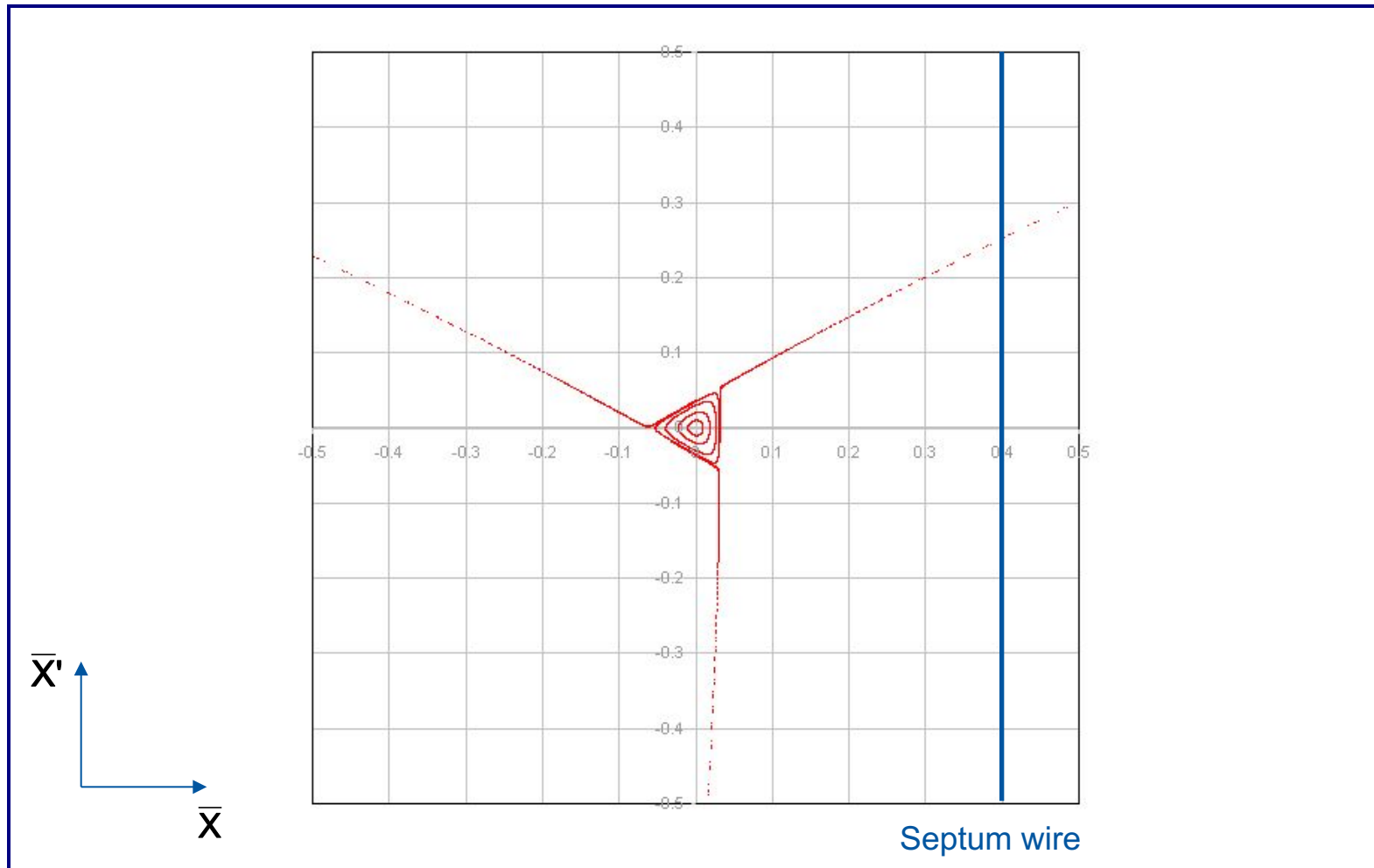
# 3rd-order resonant slow extraction



- As the stable area shrinks, the circulating beam intensity drops since particles are being continuously extracted

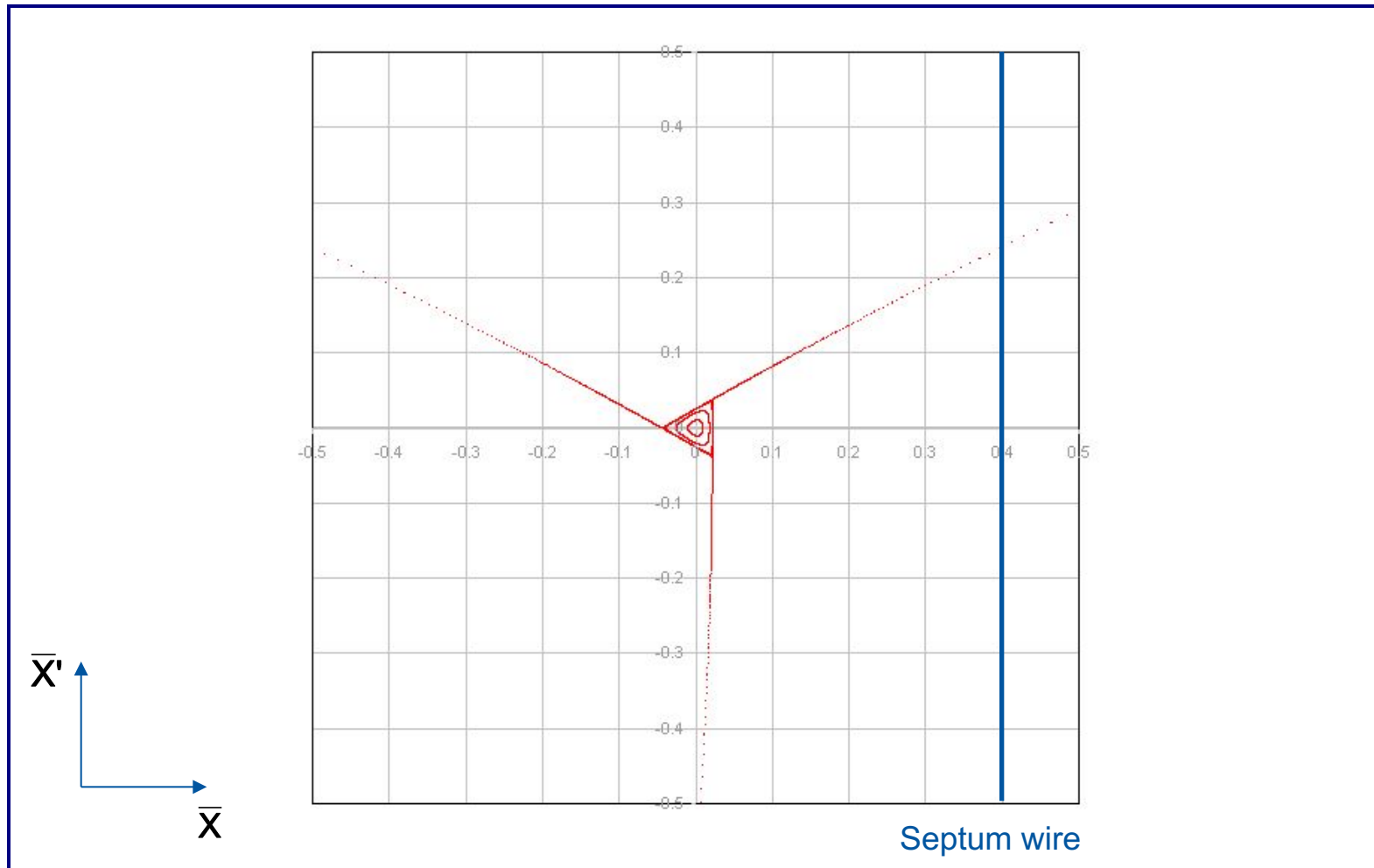


# 3rd-order resonant slow extraction



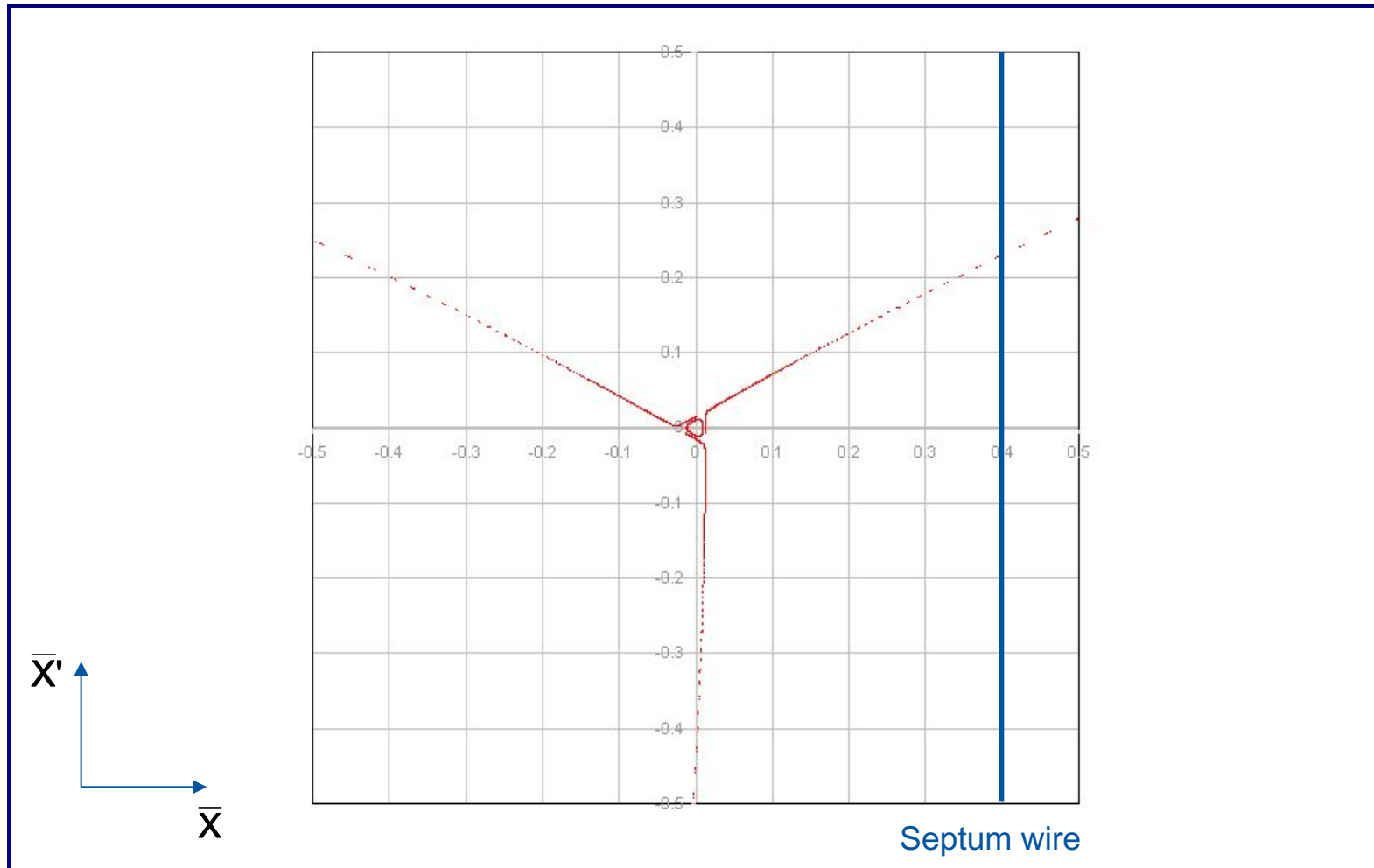
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# 3rd-order resonant slow extraction



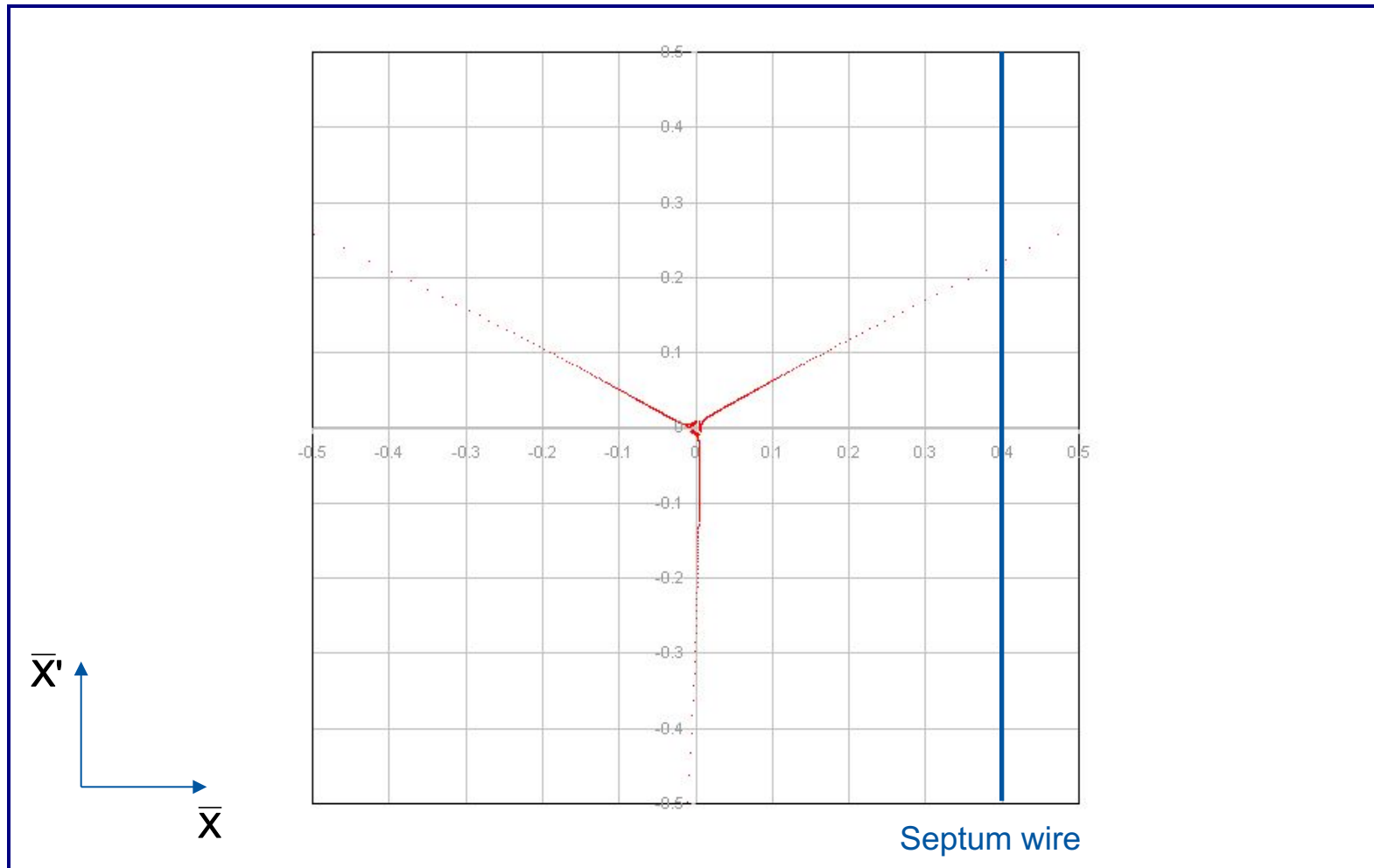
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# 3rd-order resonant slow extraction



- As the stable area shrinks, the circulating beam intensity drops since particles are being continuously extracted

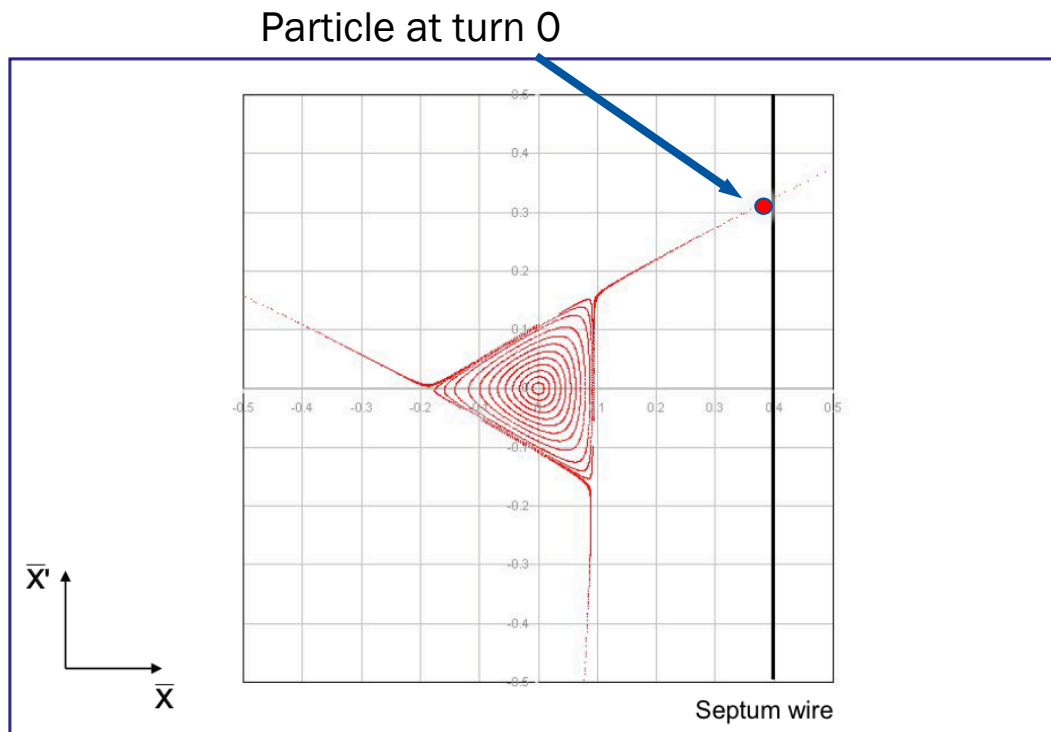
# 3rd-order resonant slow extraction



- As  $\Delta Q$  approaches zero, the particles with very small amplitude are extracted

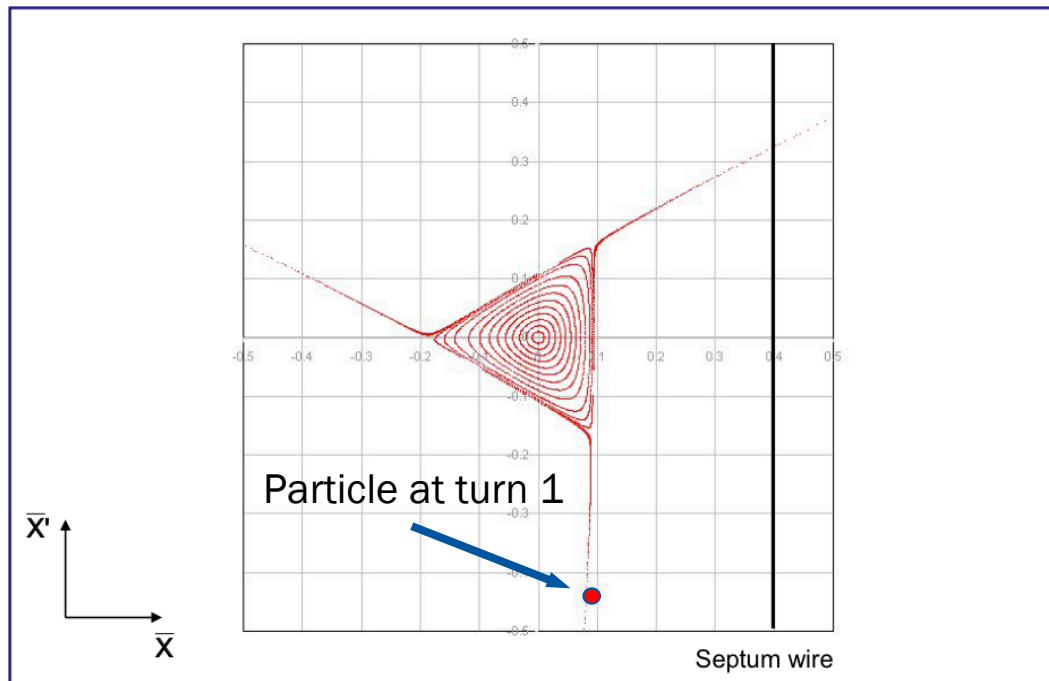
# 3rd-order resonant slow extraction

- On resonance, sextupole kicks add-up driving particles over septum



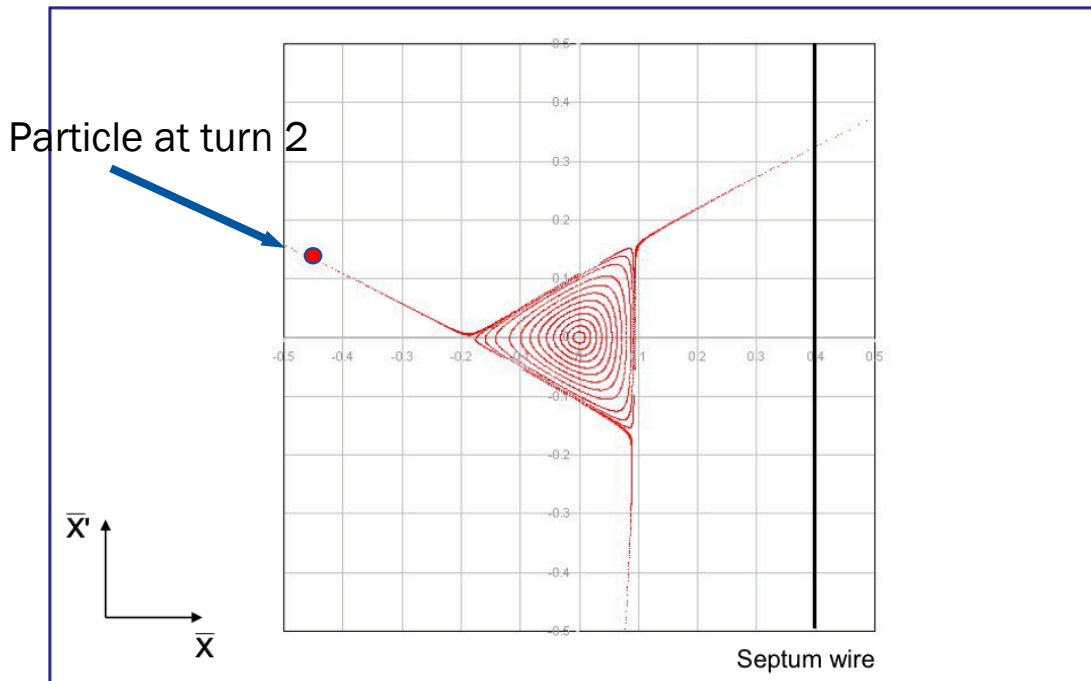
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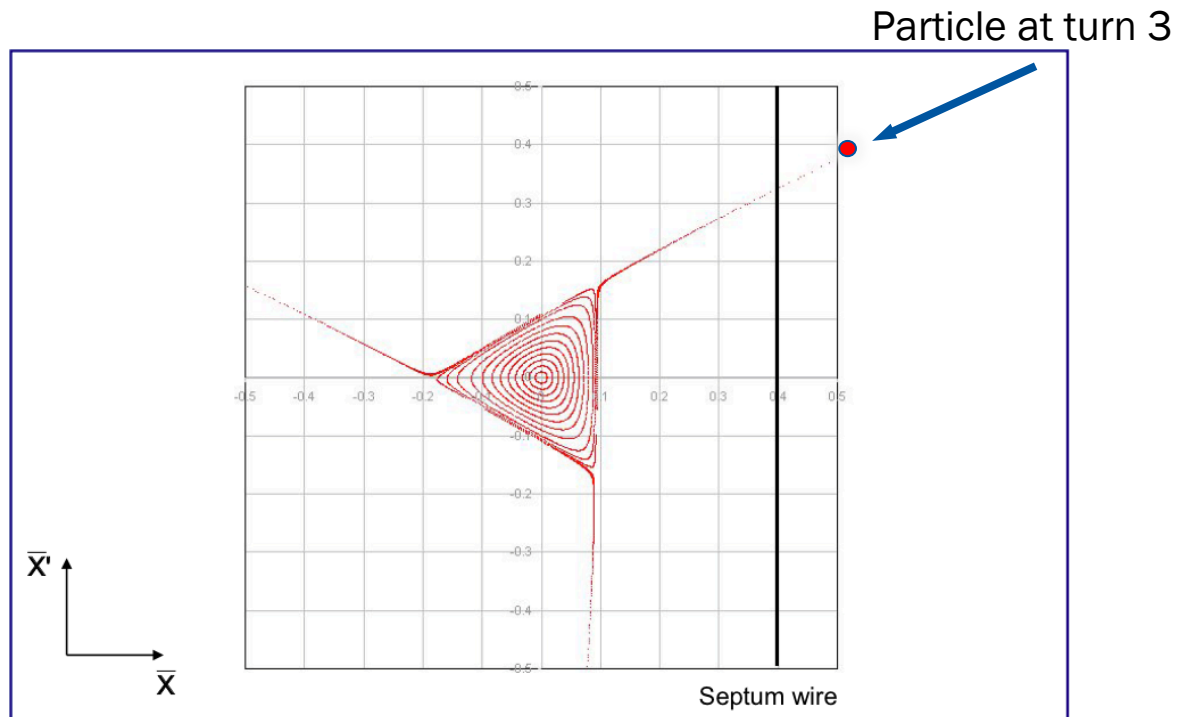
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# 3rd-order resonant slow extraction

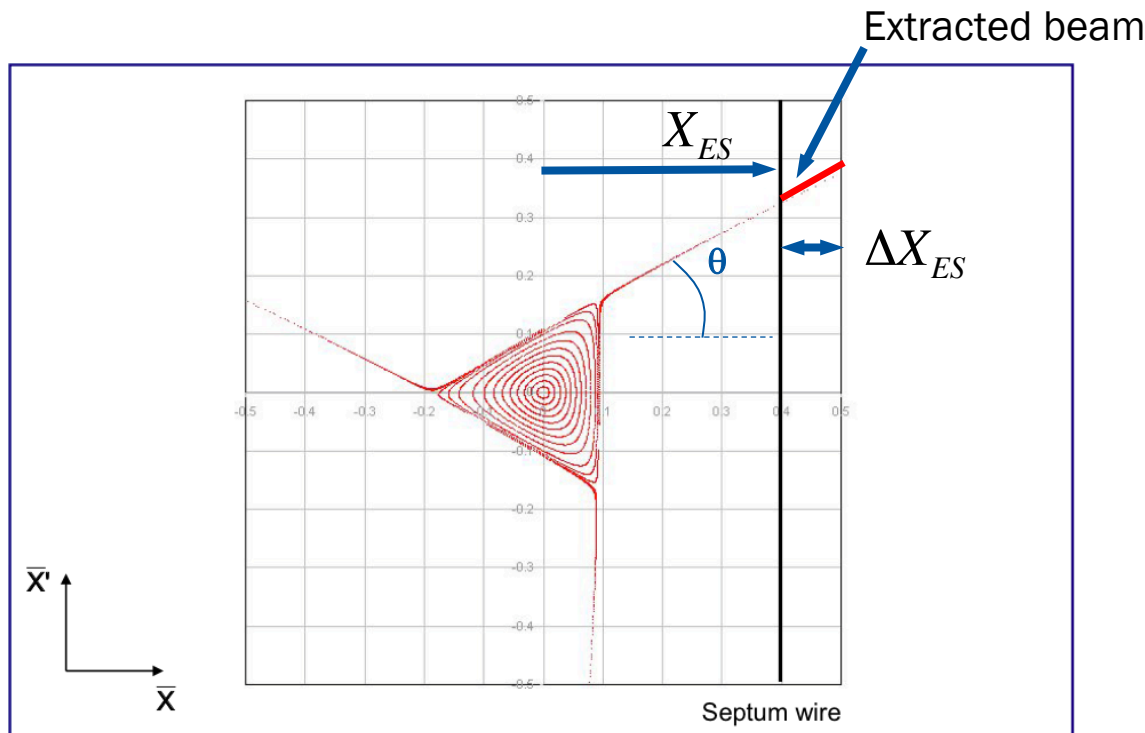
- On resonance, sextupole kicks add-up driving particles over septum





# 3rd-order resonant slow extraction

- On resonance, sextupole kicks add-up driving particles over septum



Distance travelled in these final three turns is termed the “spiral step,”  $\Delta X_{ES}$

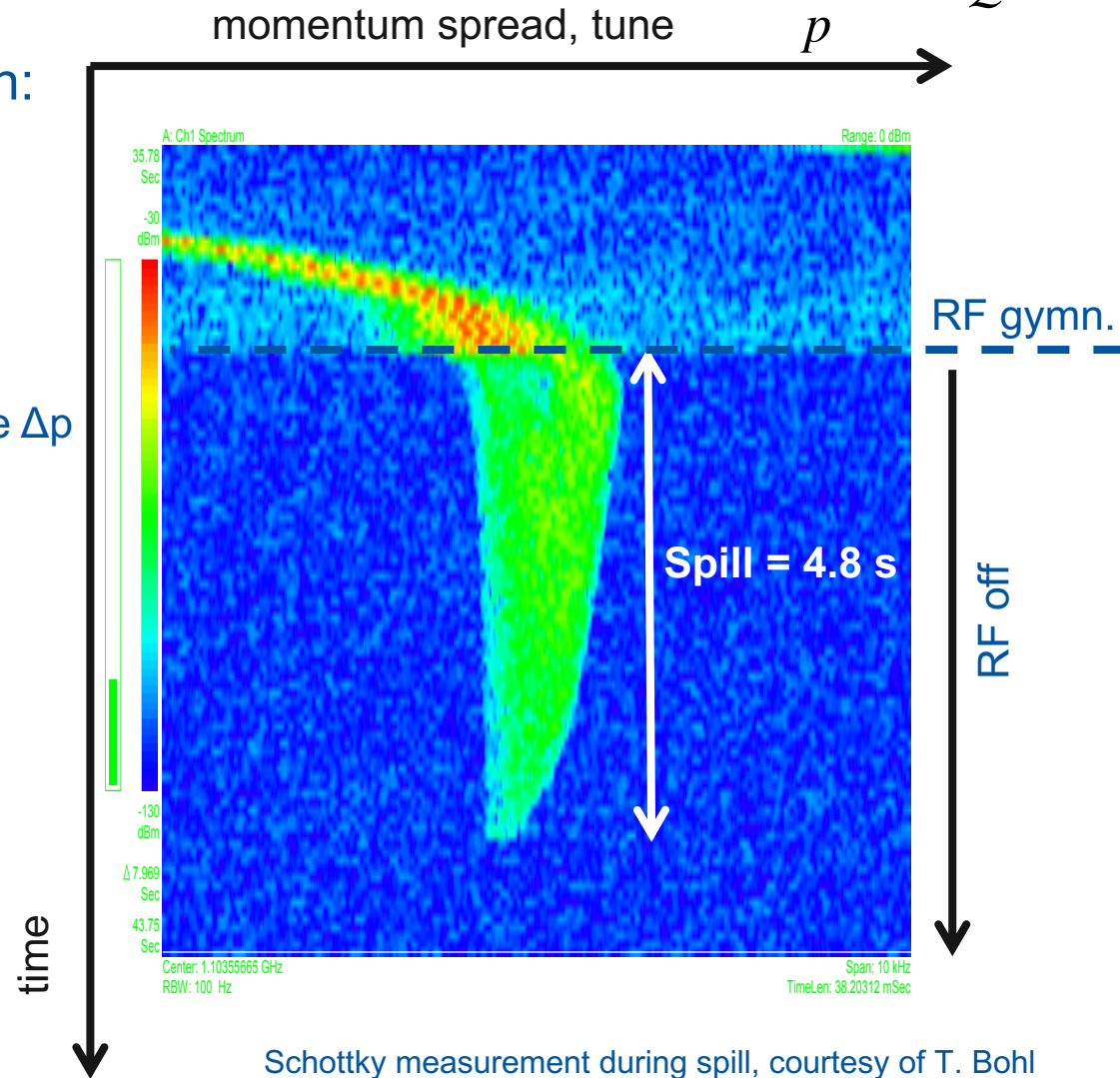
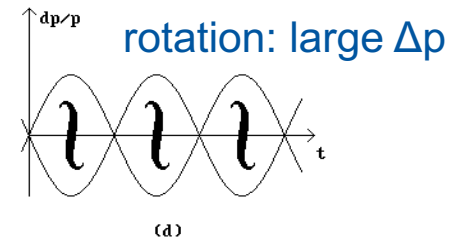
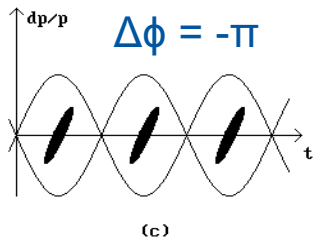
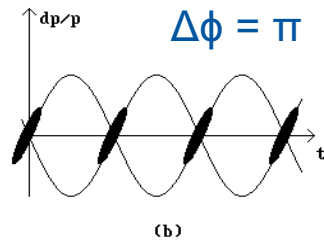
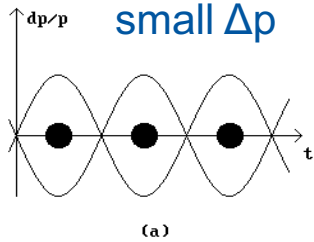
Extraction bump trimmed in the machine to adjust the spiral step

$$\Delta X_{ES} \propto |k_2| \frac{X_{ES}^2}{\cos \theta}$$

# 3rd-order resonant slow extraction

$$\frac{\Delta p}{p} \propto -\Delta Q$$

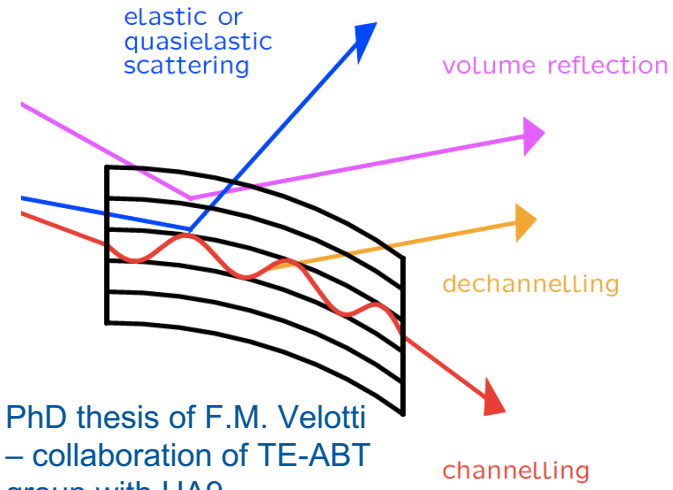
RF gymnastics before extraction:



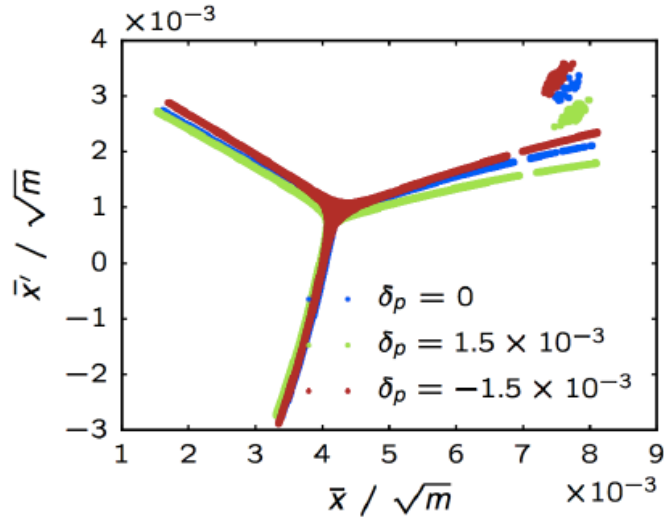
Schottky measurement during spill, courtesy of T. Bohl



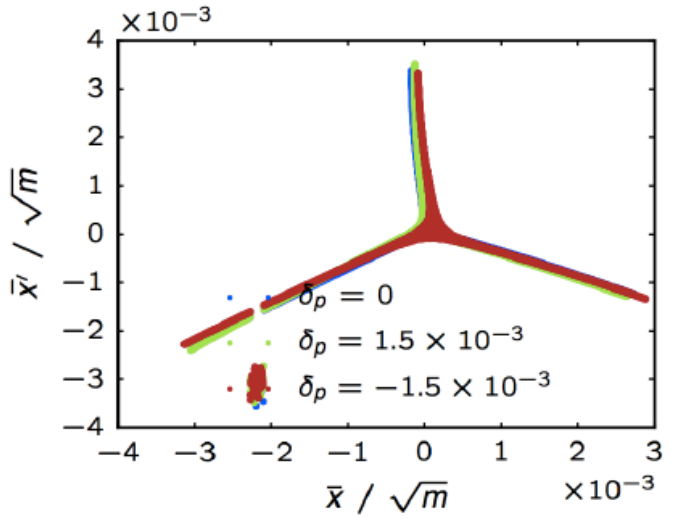
# Reduction of losses on the septum – shadowing with crystals



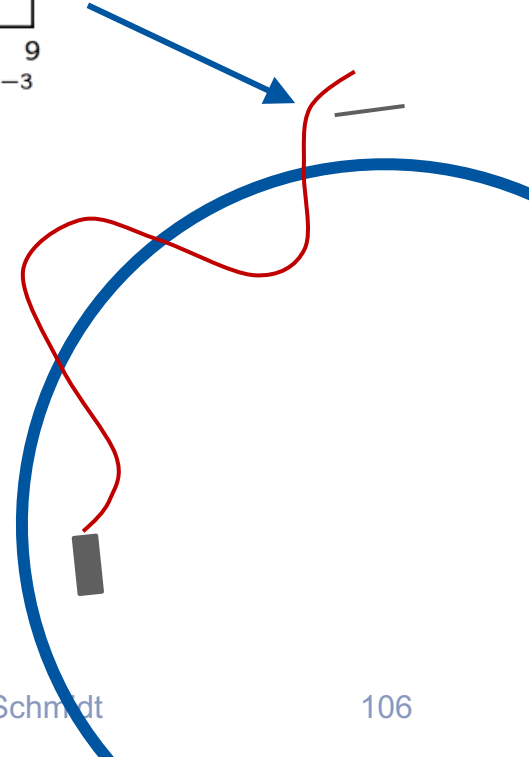
PhD thesis of F.M. Velotti  
– collaboration of TE-ABT  
group with UA9



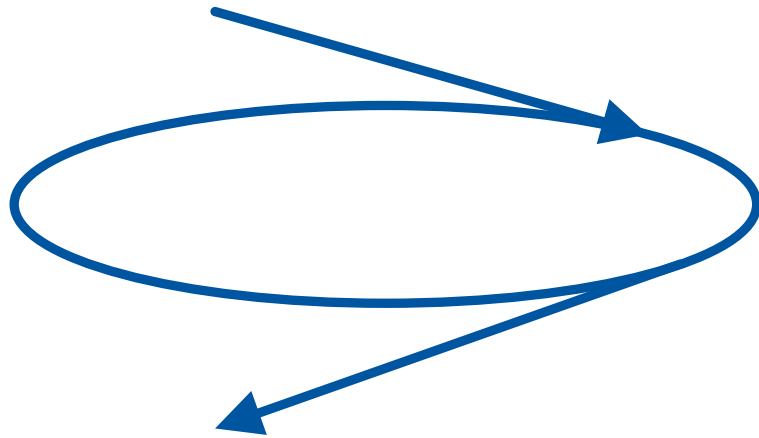
Extraction septum  
Particles, which were  
kicked by the crystal  
have entered the  
extraction channel



Crystal location  
Particles, which hit the thin  
crystal are kicked



# Overview



- Introduction
- Single-turn methods
  - Injection
  - Fast extraction
- Multi-turn methods
  - Multi-turn hadron injection
  - Charge-exchange H- injection
  - Multi-turn extraction
- Resonant slow extraction
- **Summary**

# Beam transfer - summary

Transfer lines transport beams between accelerators (from extraction of one to injection of the next) and onto experimental targets and beam dumps

- Requirements:
  - Geometric link between machines/experiment
  - Match optics between machines/experiment
  - Preserve emittance
  - Change particles' charge state (stripping foils)
  - Measure beam parameters (measurement lines)
  - Protect downstream machine/experiment

# Injection - summary

Several different techniques using kickers, septa and bumpers

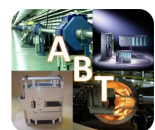
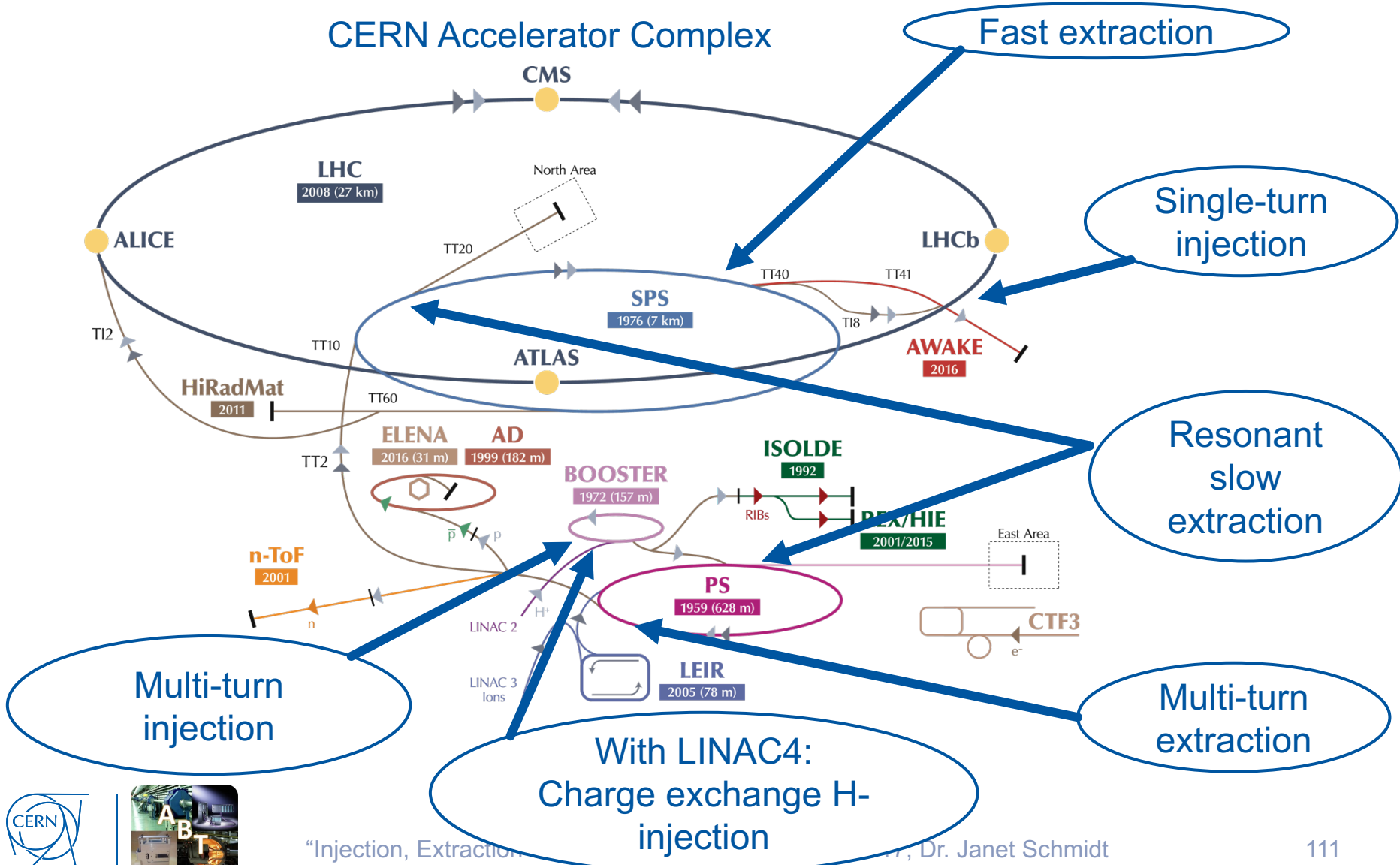
- Single-turn injection for hadrons
  - Boxcar stacking: transfer between machines in accelerator chain
  - Angle / position errors  $\Rightarrow$  injection oscillations
  - Uncorrected errors  $\Rightarrow$  filamentation  $\Rightarrow$  emittance increase
- Multi-turn injection for hadrons
  - Phase space painting to increase intensity
  - H- injection allows injection into same phase space area

# Extraction - summary

Extraction technique is chosen depending on “receivers” requirements

- Single-turn fast extraction:
  - for transfer between machines in accelerator chain, beam abort or experiments with requests for short pulses
- Non-resonant multi-turn extraction
  - slice beam into equal parts for transfer between machine over a few turns.
- Resonant low-loss multi-turn extraction
  - create stable islands in phase space: extract over a few turns.
- Resonant slow extraction
  - create stable area in phase space → slowly drive particles into resonance → long spill over many thousand turns.

# Linking the machines





# Help! What do I do when???

Application	Method
<b>Direct transfer</b> between machines with minimal effect on beam emittance	Single-turn injection and extraction
Fill up acceptance of receiving machine to create <b>higher beam intensity</b>	Multi-turn injection with phase space painting
Create <b>higher particle density</b> ( <i>and beam intensity</i> )	Charge exchange injection ( <i>with phase space painting</i> )
<b>Fill following machine</b> with minimum number of extractions ( <i>with minimized losses</i> )	Multi-turn extraction ( <i>using a resonance to split beam into several stable islands in phase space</i> )
<b>Send long "quasi-constant" spills</b> to fixed target experiment	Resonant slow extraction, using a resonance to drive particles into the extraction channel

# Literature



Thank you

- General accelerator physics course of the CAS
- Lectures of Brennan Goddard at CAS and Rende Steerenberg at OP AXEL lectures
- M. Pullia, "Beamlines and matching to gantries" CAS 2015, Vösendorf, Austria
- K. Wille, "The Physics of Particle Accelerators: An Introduction", 2000
- H. Wiedemann, "Particle Accelerator Physics"
- LHC design report (Vol.III), CERN-2004-003
- A. Hilaire, "Beam transfer to and injection into LHC", EPAC'98 Conference, Stockholm, June 1998
- C. Bovet, "The fast shaving ejection for beam transfer from the CPS to the CERN 300 GeV machine", IEEE 1973
- R. Cappi, M. Giovannozzi, "Multiturn extraction: performance analysis of old and new approaches", Phys. Rev. Spec. Top. Accel. Beams 7 (2004) 024001
- V. Forte, "Performance of the CERN PSB at 160 MeV with H- charge exchange injection", PhD thesis 2016
- E. Benedetto et al, "Space Charge Effects and Mitigation in the CERN PS Booster, in View of the Upgrade", HB2016 Workshop, CERN-ACC-2016-0108
- M. Benedikt, "Optical design of a synchrotron with optimisation of the slow extraction for hadron therapy", PhD thesis 1997
- F. M. Velotti, "Higher Brightness Beams from the SPS for the HL-LHC Era", PhD thesis 2016

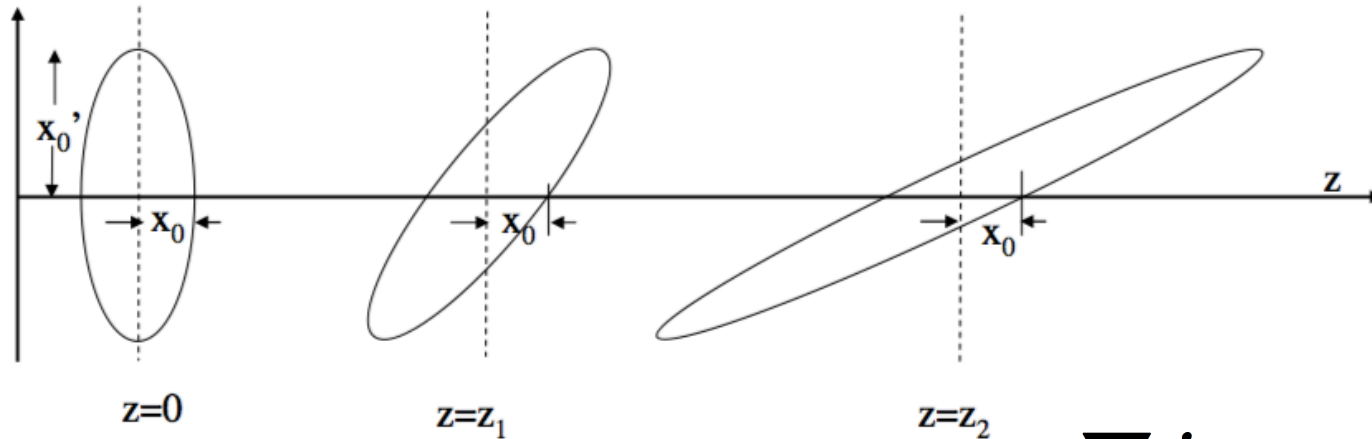


# Appendix



# Liouville's Theorem

- “... under the influence of conservative forces the particle density in phase space stays constant” (H. Wiedemann, Particle Accelerator Physics)



$$\frac{\partial \Psi}{\partial \tau} + \overbrace{\nabla_r \Psi \dot{\mathbf{r}} + \nabla_p \Psi \dot{\mathbf{p}}}^{\nabla j} = \frac{d\Psi}{d\tau} = 0$$

# Normalised phase space

- Transform real transverse coordinates  $(x, x', s)$  to normalised coordinates  $(\bar{X}, \bar{X}', \mu)$  where the independent variable becomes the phase advance  $\mu$ :

$$\begin{bmatrix} \bar{X} \\ \bar{X}' \end{bmatrix} = \mathbf{N} \cdot \begin{bmatrix} x \\ x' \end{bmatrix} = \sqrt{\frac{1}{\beta(s)}} \cdot \begin{bmatrix} 1 & 0 \\ \alpha(s) & \beta(s) \end{bmatrix} \cdot \begin{bmatrix} x \\ x' \end{bmatrix}$$

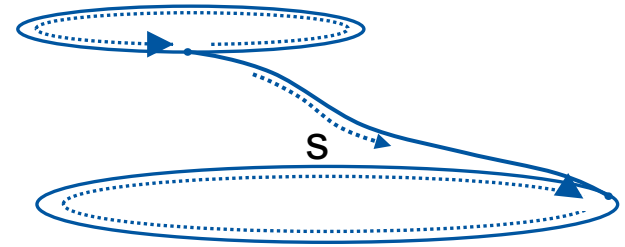
$$x(s) = \sqrt{\varepsilon} \sqrt{\beta(s)} \cos[\mu(s) + \mu_0]$$

$$\mu(s) = \int_0^s \frac{d\sigma}{\beta(\sigma)}$$

$$\bar{X}(\mu) = \sqrt{\frac{1}{\beta(s)}} \cdot x = \sqrt{\varepsilon} \cos[\mu + \mu_0]$$

$$\bar{X}'(\mu) = \sqrt{\frac{1}{\beta(s)}} \cdot \alpha(s)x + \sqrt{\beta(s)}x' = -\sqrt{\varepsilon} \sin[\mu + \mu_0] = \frac{d\bar{X}}{d\mu}$$

# Transfer matrix



One pass: 
$$\begin{bmatrix} x_2 \\ x_2' \end{bmatrix} = \mathbf{M}_{1 \rightarrow 2} \cdot \begin{bmatrix} x_1 \\ x_1' \end{bmatrix}$$

$$\mathbf{M}_{1 \rightarrow 2} = \begin{bmatrix} \sqrt{\beta_2/\beta_1} (\cos \Delta\mu + \alpha_1 \sin \Delta\mu) & \sqrt{\beta_1\beta_2} \sin \Delta\mu \\ \sqrt{1/\beta_1\beta_2} [(\alpha_1 - \alpha_2) \cos \Delta\mu - (1 + \alpha_1\alpha_2) \sin \Delta\mu] & \sqrt{\beta_1/\beta_2} (\cos \Delta\mu - \alpha_2 \sin \Delta\mu) \end{bmatrix}$$

- Straight propagation of TWISS parameters (no periodic conditions)
- At any point in line,  $\alpha(s)$   $\beta(s)$  are functions of  $\alpha_1$  and  $\beta_1$

- For a ring the transfer matrix can be simplified (periodic conditions →

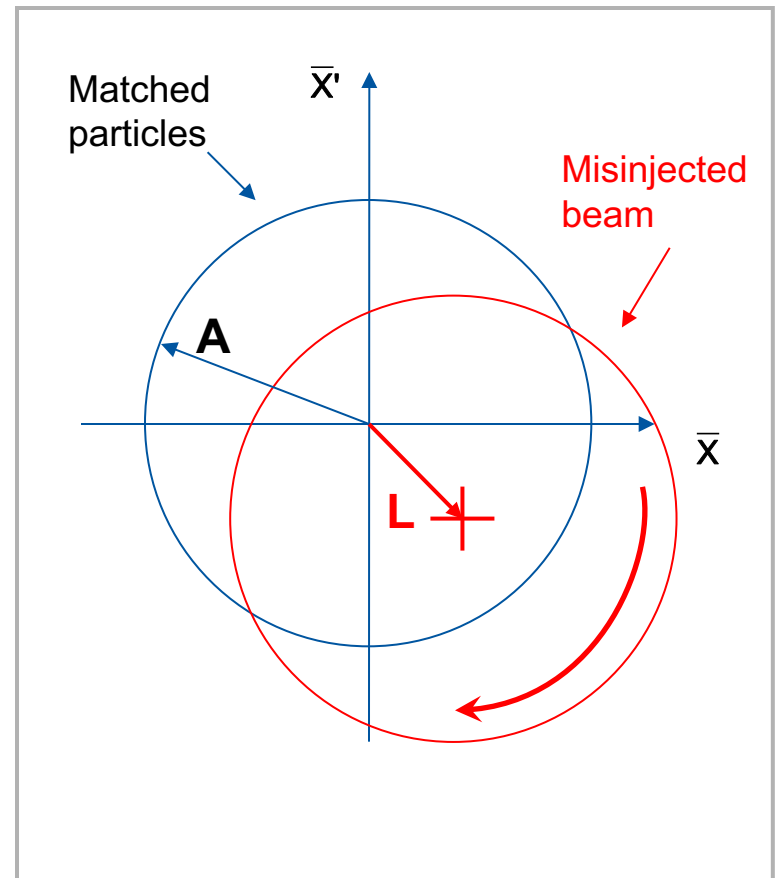
$$\Delta\mu = 2\pi Q$$

$$\mathbf{M}_{1 \rightarrow 2} = \mathbf{M}_{0 \rightarrow L} = \begin{bmatrix} \cos 2\pi Q + \alpha \sin 2\pi Q & \beta \sin 2\pi Q \\ -1/\beta (1 + \alpha^2) \sin 2\pi Q & \cos 2\pi Q - \alpha \sin 2\pi Q \end{bmatrix}$$



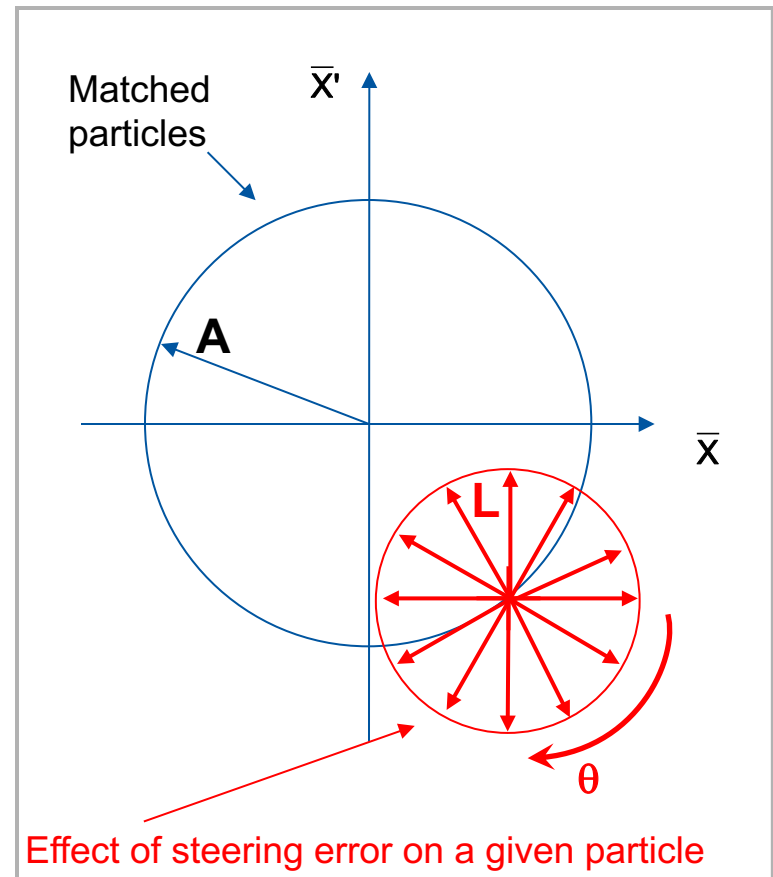
# Blow-up from steering error

- Consider a collection of particles with max. amplitudes  $A$
- The beam can be injected with an error in angle and position.
- For an injection error  $\Delta a$ , in units of  $\sigma = \sqrt{\beta\varepsilon}$ , the mis-injected beam is offset in normalised phase space by an amplitude  $L = \Delta a\sqrt{\varepsilon}$



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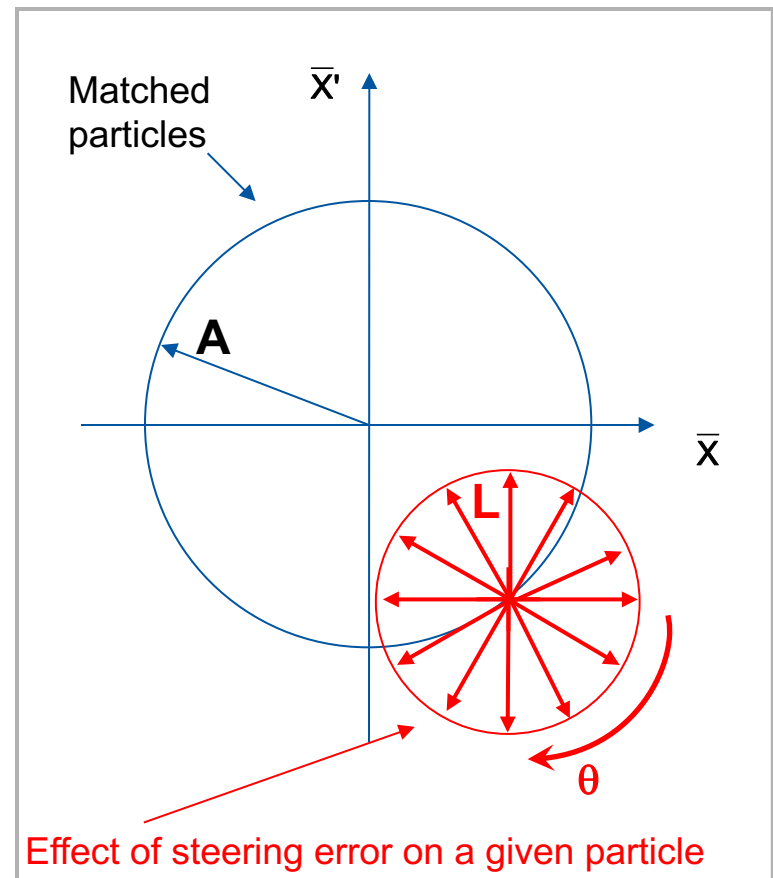




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- For a general particle distribution, where  $A_i$  denotes amplitude in normalised phase of particle  $i$ :

$$\varepsilon_{matched} = \langle \mathbf{A}_i^2 \rangle / 2$$



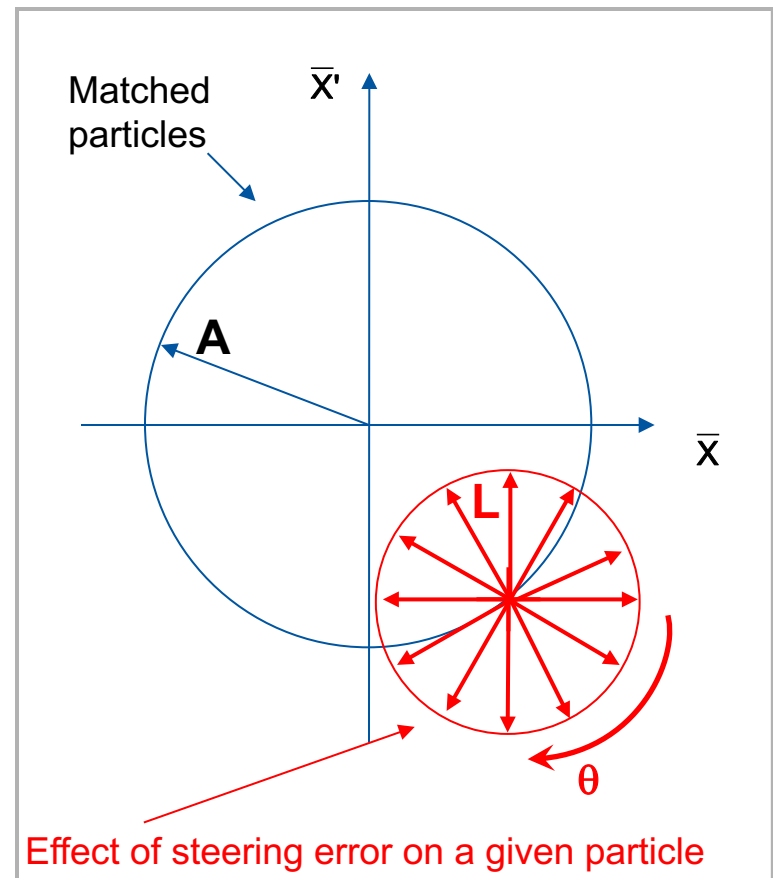
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- After filamentation:

$$\varepsilon_{diluted} = \varepsilon_{matched} + \frac{L^2}{2}$$



# Blow-up from steering error

- The new particle coordinates in normalised phase space are:

$$\bar{X}_{error} = \bar{X}_0 + L \cos \theta$$

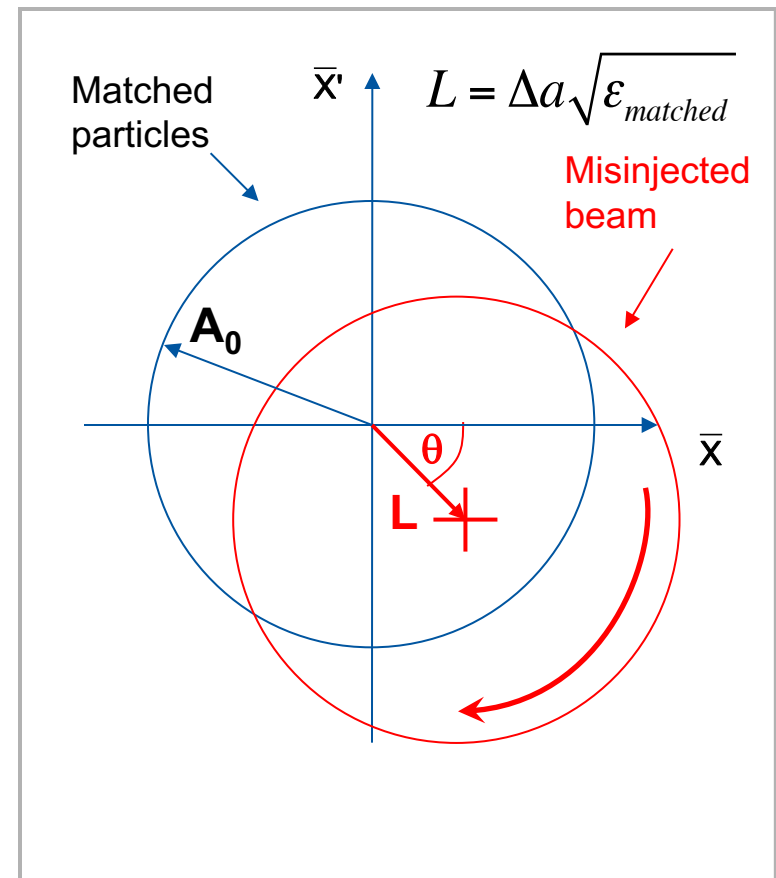
$$\bar{X}'_{error} = \bar{X}'_0 + L \sin \theta$$

- For a general particle distribution, where  $A_i$  denotes amplitude in normalised phase of particle  $i$ :

$$\mathbf{A}_i^2 = \bar{X}_{0,i}^2 + \bar{X}'_{0,i}^2$$

- The emittance of the distribution is:

$$\mathcal{E}_{matched} = \langle \mathbf{A}_i^2 \rangle / 2$$



# Blow-up from steering error

- So we plug in the new coordinates:

$$\begin{aligned}
 \mathbf{A}_{error}^2 &= \bar{X}_{error}^2 + \bar{X}'_{error}{}^2 && \cos^2 \theta + \sin^2 \theta = 1 \\
 &= (\bar{X}_0 + L \cos \theta)^2 + (\bar{X}'_0 + L \sin \theta)^2 \\
 &= \bar{X}_0^2 + \bar{X}'_0{}^2 + 2L(\bar{X}_0 \cos \theta + \bar{X}'_0 \sin \theta) + L^2
 \end{aligned}$$

- Taking the average over distribution:

$$\begin{aligned}
 \langle \mathbf{A}_{error}^2 \rangle &= \langle \mathbf{A}_0^2 \rangle + 2L(\langle \bar{X}_0 \cos \theta \rangle + \langle \bar{X}'_0 \sin \theta \rangle) + \langle L^2 \rangle \\
 &= 2\epsilon_{matched} + L^2
 \end{aligned}$$

- Giving the diluted emittance as:

$$\begin{aligned}
 \epsilon_{diluted} &= \epsilon_{matched} + \frac{L^2}{2} \\
 &= \epsilon_{matched} \left[ 1 + \frac{\Delta a^2}{2} \right]
 \end{aligned}$$

