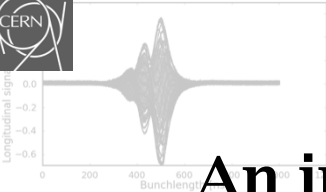
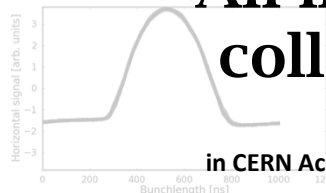
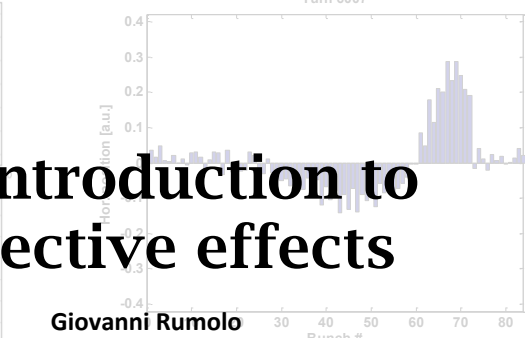
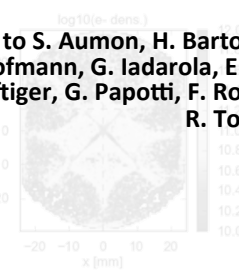





An introduction to collective effects
 Giovanni Rumolo
 in CERN Accelerator School, Chavannes de Bogis
 Friday, 8 November, 2013

Thanks to S. Aumon, H. Bartosik, P. Chiggiato, A. Findlay, S. Gilardoni, W. Herr,
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 R. Tomás, R. Wasef, C. Zannini



The CERN Accelerator School

What are the collective effects?

- A general definition of collective effects
 - Class of phenomena in beam dynamics, in which the evolution of a particle in a beam depends on both the external EM fields and the extra EM fields created by the presence of other particles.
- How other particles can affect a single particle's motion:
 - **Self-induced EM fields**
 - Space charge from beam particles
 - EM interaction of whole beam with surrounding environment
 - EM interaction of whole beam with its own synchrotron radiation
 - **Coulomb collisions**
 - Long range and multiple two beam particle encounters → Intra-beam scattering
 - Short range and single events two beam particle encounters → Touschek effect
 - Elastic and inelastic scattering against residual gas
 - **EM fields from another charge distribution** (generated or not by the beam itself), like a second "beam"
 - Beam-beam in colliders
 - Ion trapping for electron beams
 - Electron clouds for positron/hadron beams
 - Interactions with electron lens or electron cooling system



2

Types of collective effects

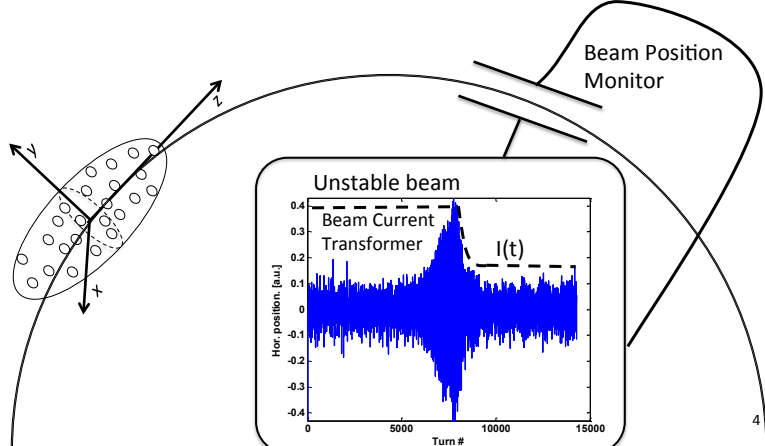
- Collective effects start playing a role when the beam density is very high
 - They are also referred to as “high current”, “high intensity”, “high brightness” effects and exhibit a threshold behaviour
 - They result into a measurable response of the beam to the collective interaction, which can be **detrimental and lead to beam degradation and loss**
- **Transverse coherent collective effects**
 - Due to self-induced EM fields
 - The beam centroid is affected, resulting in betatron tune shift and possibly in exponential growth (single or multi-bunch instabilities, strong head-tail)
 - Can be seen with standard BPMs
- **Transverse incoherent collective effects**
 -
 -
 - the beam centroid is not affected
 - Typically leading to slow losses and emittance growth, diffusion, halo and tail formation

3



Transverse coherent instability An example

- Occurrence of a transverse coherent instability
 - The beam centroid, as detected by a BPM, exhibits an exponential growth typically on the time scale of tens to thousands of turns, usually associated with beam loss and/or emittance growth!



The diagram illustrates a particle accelerator ring with a beam position monitor (BPM) and a beam current transformer (BCT). A beam is shown circulating in the ring, with a coordinate system (x, y, z) indicating its position. The BPM is located at a specific point in the ring, and the BCT is also located at a different point. The graph shows the beam current $I(t)$ over time (Turn #), with a clear exponential growth in the current, indicating an unstable beam. The y-axis is labeled 'Hor. position, [au]' and ranges from -0.4 to 0.4. The x-axis is labeled 'Turn #' and ranges from 0 to 15000. The graph shows a blue signal that starts at 0 and grows exponentially, reaching a peak of approximately 0.4 at around 10000 turns. The signal is labeled 'Unstable beam' and 'Beam Current Transformer $I(t)$ '.



4

Types of collective effects

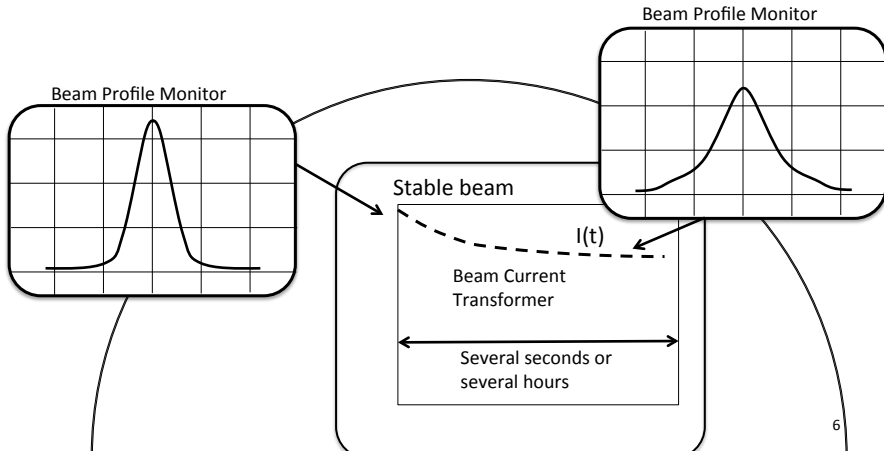
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 - They result into a measurable response of the beam to the collective interaction, which can be **detrimental and lead to beam degradation and loss**
- **Transverse coherent collective effects**
 - Due to self-induced EM fields
 - The beam centroid is affected, resulting in betatron tune shift and possibly in exponential growth (single or multi-bunch instabilities, strong head-tail)
 - Can be seen with standard BPMs
- **Transverse incoherent collective effects**
 - Due to self-induced EM fields (and their interaction with machine optics)
 - The strength of the excitation is not such as to build up into a coherent effect, i.e. the beam centroid is not affected
 - Typically leading to slow losses and emittance growth, diffusion, halo and tail formation

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Transverse incoherent effect An example

- Transverse incoherent effect
 - A beam exhibits slow losses (on the time scale of the cycle or store) and emittance growth visible from a beam profile measurement device, possibly associated to development of halo or tails





6

Types of collective effects

- Collective effects start playing a role when the beam density is very high
 - They are also referred to as “high current”, “high intensity”, “high brightness” effects and exhibit a threshold behaviour
 - They result into a measurable response of the beam to the collective interaction, which can be **detrimental and lead to beam degradation and loss**
- **Longitudinal collective effects**
 - Due to self-induced EM fields
 - Energy loss, potential well distortion (synchronous phase shift, bunch lengthening)
 - Instabilities (single or coupled bunch instabilities, microwave instability)
- **Collisional effects (transverse and longitudinal)**
 -
 -
 - emittance growth
- **Two-stream effects (transverse and longitudinal)**
 - Due to the interaction with another set of charged particles
 - Can cause coherent motion as well as incoherent emittance growth and losses

7

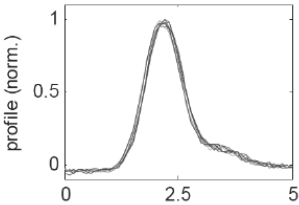



Longitudinal coherent modes An example

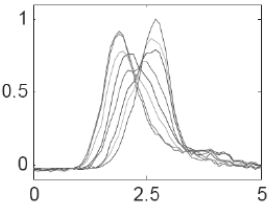
- Longitudinal coherent modes
 - The beam profile, measured at a Wall Current Monitor, shows bunches oscillating in their buckets (plot 2) or executing quadrupole oscillations (plot 3)

Observations in the CERN SPS in 2007

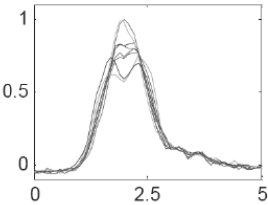
stable bunch





dipole osc.



quadrupole osc.

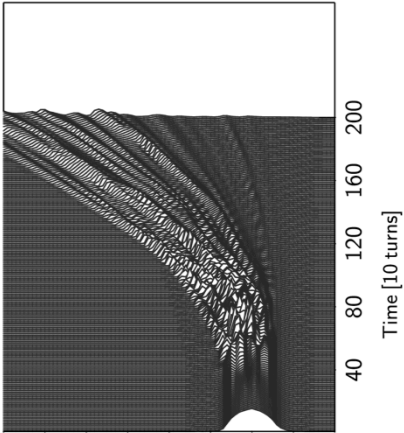


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Longitudinal microwave instability An example

- Debunching long bunch in the SPS during Machine Development
 - For impedance identification purpose, a long bunch is injected into the SPS with the RF off.
 - A microwave instability develops on the beam as it debunches
 - From the Fourier analysis of the resulting micro-bunching it is possible to reconstruct the most important frequency components of the longitudinal impedance



z [m]



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Types of collective effects

- Collective effects start playing a role when the beam density is very high
 - They are also referred to as “high current”, “high intensity”, “high brightness” effects and exhibit a threshold behaviour
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 - Energy loss, potential well distortion (synchronous phase shift, bunch lengthening)
 - Instabilities (single or coupled bunch instabilities, microwave instability)
- **Collisional effects (transverse and longitudinal)**
 - Due to scattering
 - Tend to depopulate the denser beam core and degrade emittance and lifetime, similar to what is caused by incoherent collective effects.
- **Two-stream effects (transverse and longitudinal)**
 - Due to the interaction with another set of charged particles
 - Can cause coherent motion as well as incoherent emittance growth and losses



10

Types of collective effects

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 - Due to scattering
 - Tend to depopulate the denser beam core and degrade emittance and lifetime, similar to what is caused by incoherent collective effects.
- **Two-stream effects (transverse and longitudinal)**
 - Due to the interaction with another set of charged particles (e.g. electron cloud)
 - Can cause coherent motion as well as incoherent emittance growth and losses

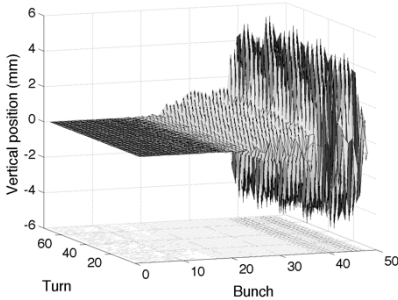
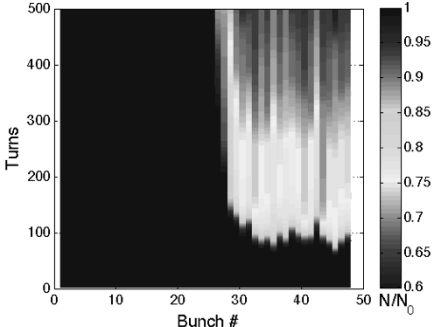
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Electron cloud instability An example

- Electron cloud instability
 - A coherent instability is visible for the last bunches of a train (BPM signal and beam losses), because an electron cloud has formed along the train and can only make these bunches unstable

48b injection test in LHC (26/08/11)

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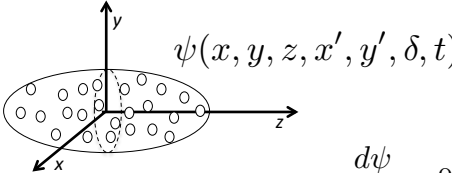



Modeling of collective effects

- Self-induced EM fields
 - Single particle motion under the overall effect of externally applied fields (RF, magnets) and those created by the beam itself with the proper boundary conditions.

→ **No single particle dynamics, need to describe a system of many particles**



- ✓ **Theory:** kinetic models based on distribution functions (Vlasov-Maxwell)
- ✓ **Simulation:** macroparticles



$$\frac{d\psi}{dt} = 0 \iff \begin{cases} \vec{E} = \vec{E}_{\text{ext}} + \vec{E}(\psi) \\ \vec{B} = \vec{B}_{\text{ext}} + \vec{B}(\psi) \end{cases}$$

in Maxwell's equations

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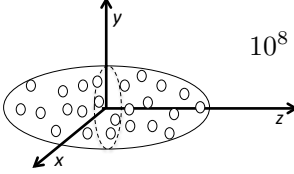



Modeling of collective effects

- Self-induced EM fields
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→ **No single particle dynamics, need to describe a system of many particles**

- ✓ **Theory:** kinetic models based on distribution functions (Vlasov-Maxwell)
- ✓ **Simulation:** solve numerically the equations of motion of a set of macroparticles and use the EM fields of the macroparticle distribution





$10^8 - 10^{11}$ particles $\rightarrow 10^4 - 10^6$ macroparticles

$$\frac{d\vec{p}_{\text{mp}}}{dt} = q \left(\vec{E} + \vec{v}_{\text{mp}} \times \vec{B} \right)$$

$$\begin{cases} \vec{E} = \vec{E}_{\text{ext}} + \vec{E}(\psi_{\text{mp}}) \\ \vec{B} = \vec{B}_{\text{ext}} + \vec{B}(\psi_{\text{mp}}) \end{cases}$$

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Modeling of collective effects



- Self-induced EM fields
 - Single particle motion under the overall effect of externally applied fields (RF, magnets) and those created by the beam itself with the proper boundary conditions.

→ **No single particle dynamics, need to describe a system of many particles**

- ✓ **Theory:** kinetic models based on distribution functions (Vlasov-Maxwell)
- ✓ **Simulation:** solve numerically the equations of motion of a set of macroparticles and use the EM fields of the macroparticle distribution
- **Direct space charge** refers to the EM fields created by the beam as if it was moving in open space,
- **Impedances** are used to describe EM interaction of beam with boundaries



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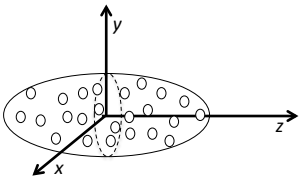
Modeling of collective effects

- Self-induced EM fields + Coulomb collisions
 - Single particle motion under the overall effect of externally applied fields (RF, magnets) and those created by the beam itself with the proper boundary conditions.

→ **No single particle dynamics, need to describe a system of many particles**

- ✓ **Theory:** kinetic models based on distribution functions (Vlasov-Maxwell)
- ✓ **Simulation:** solve numerically the equations of motion of a set of macroparticles



✦ **Probability of close encounters can be included through the appropriate models**



$$\frac{d\psi}{dt} = \left(\frac{\partial \psi}{\partial t} \right)_{\text{coll}} \longleftrightarrow \begin{cases} \vec{E} = \vec{E}_{\text{ext}} + \vec{E}(\psi) \\ \vec{B} = \vec{B}_{\text{ext}} + \vec{B}(\psi) \end{cases}$$

Vlasov-Fokker-Planck formalism

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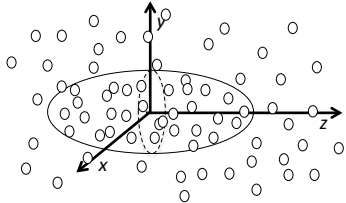



Modeling of collective effects

- EM fields from another charge distribution
 - Single particle motion under the overall effect of externally applied fields (RF, magnets) and those created by the second “beam”.

→ **No single particle dynamics, need to describe evolution (and sometimes generation) of the other system of particles to derive its EM fields**

- ✓ **Theory:** simplified models to include the effect of the second “beam”
- ✓ **Simulation:** describe numerically the second “beam” and calculate its fields as driving terms in the equations of motion of the set of macroparticles representing the beam



$$\frac{d\vec{p}_{mp1,mp2}}{dt} = q \left(\vec{E} + \vec{v}_{mp1,mp2} \times \vec{B} \right)$$

$$\begin{cases} \vec{E} = \vec{E}_{ext} + \vec{E}(\psi_{mp1}, \psi_{mp2}) \\ \vec{B} = \vec{B}_{ext} + \vec{B}(\psi_{mp1}, \psi_{mp2}) \end{cases}$$


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- Space charge
 - Low energy machines
- Machine impedance
- Electron cloud
 - Machines with short bunch spacing


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- **Space charge**
 - Low energy machines
- Machine impedance
- Electron cloud
 - Machines with short bunch spacing

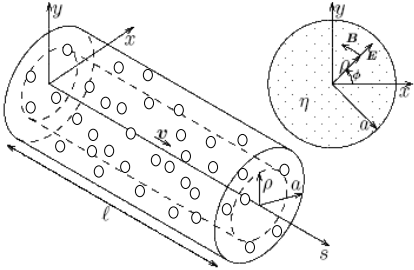
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Direct space charge




- Simple calculation of direct space charge
 - Cylindrical distribution
 - Calculate electric and magnetic forces acting on each beam particle through Maxwell's equations
 - The electric and magnetic components have different signs and differ by a factor β^2 . Perfect cancellation only when $\beta = 1$




$$\begin{aligned}
 \vec{F} &= \vec{F}_E + \vec{F}_B = e \left(\vec{E} + \vec{v} \times \vec{B} \right) = \\
 &= \frac{e\lambda\vec{\rho}}{2\epsilon_0\pi a^2} (1 - \beta^2) = \frac{e\lambda\vec{\rho}}{2\pi\epsilon_0\gamma^2 a^2} \\
 &= \frac{e\lambda}{2\pi\epsilon_0\gamma^2 a^2} \cdot (x \cdot \hat{x} + y \cdot \hat{y})
 \end{aligned}$$

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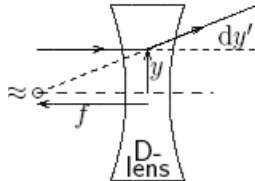


Direct space charge




- Space charge is a constant defocusing force in both x and y. For instance, in the vertical plane:
 - Corresponds to a continuous gradient error $dK(s)=dy'(s)/y$ along the ring
 - Translates into contributions to the tune shift $dQ_y(s)$
 - Can be integrated all over the circumference $C = 2\pi R$ to provide the total tune shift ΔQ_y for each particle (which is a tune spread over the beam)

$$dQ_y(s) = -\frac{\beta_y(s)}{4\pi} \frac{dy'(s)}{y} = -\frac{r_0 \lambda \beta_y(s) ds}{2\pi e \beta^2 \gamma^3 a^2(s)}$$




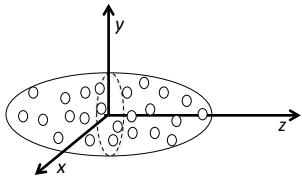
$$\Delta Q_y = \oint dQ_y(s) = -\frac{r_0 \lambda}{2\pi e \beta^2 \gamma^3} \oint \frac{\beta_y(s) ds}{a^2(s)} = -\frac{r_0 \lambda R}{e \beta \gamma^2 \epsilon_{yn}}$$

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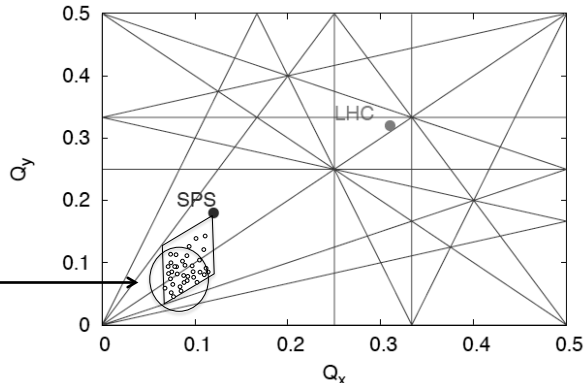


Direct space charge







$$\Delta Q_{x,y}(z) = -\frac{r_0 \lambda(z) C}{2\pi e \beta \gamma^2 \epsilon_{xn,yn}}$$

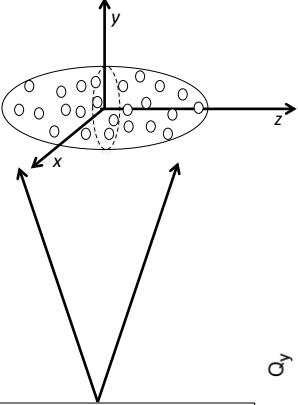


Particles around λ_{max} feeling the largest defocusing force and therefore suffering the largest tune shift

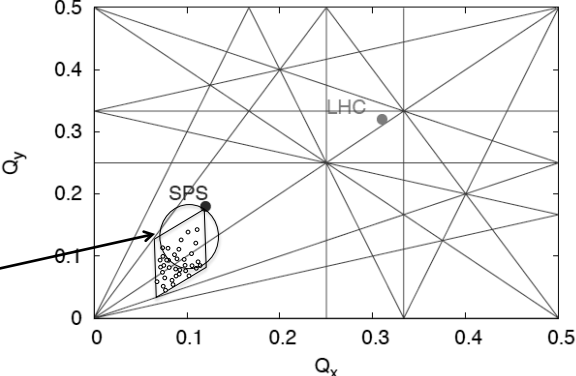


Direct space charge







$$\Delta Q_{x,y}(z) = -\frac{r_0 \lambda(z) C}{2\pi e \beta \gamma^2 \epsilon_{xn,yn}}$$

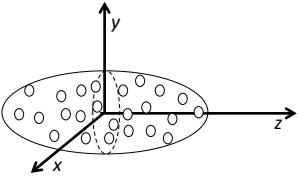


Particles at tails of longitudinal distribution, feeling the weakest defocusing force and therefore suffering the lowest tune shift



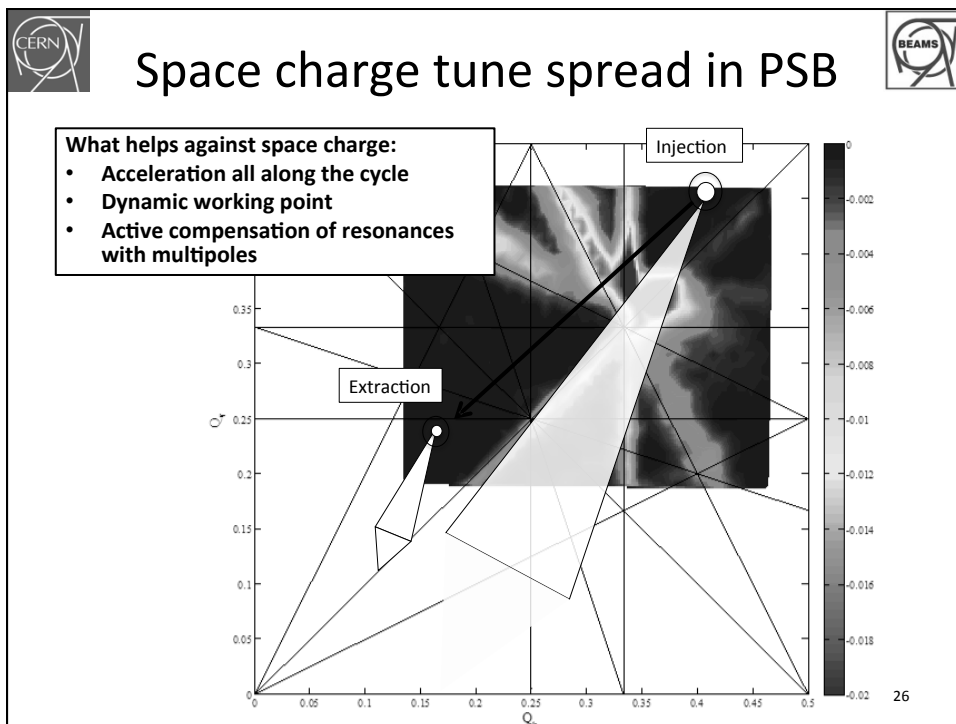
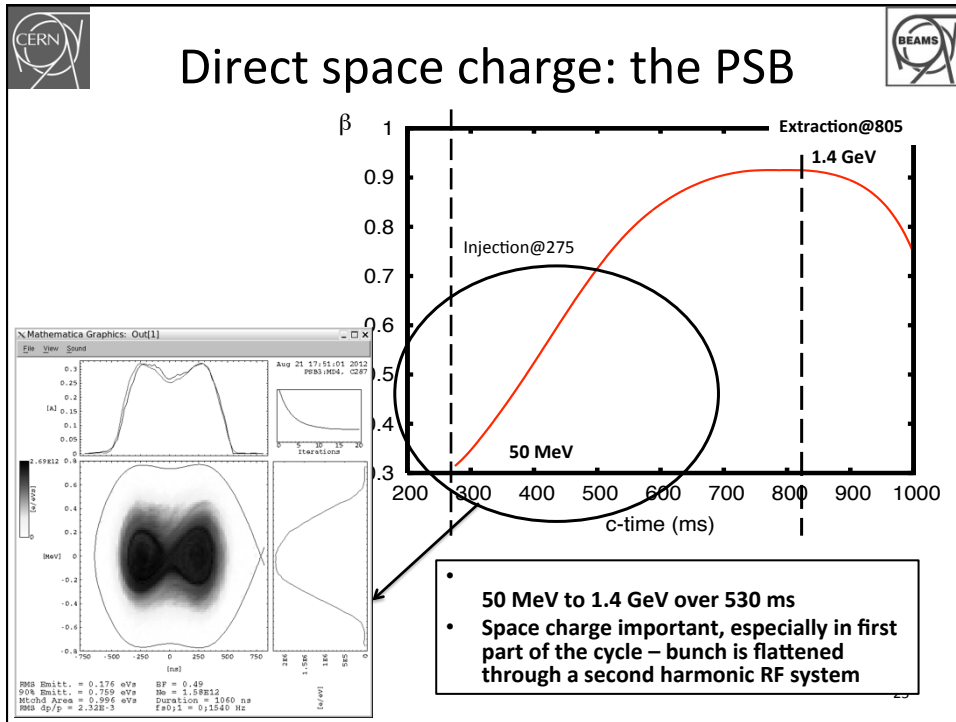
Direct space charge

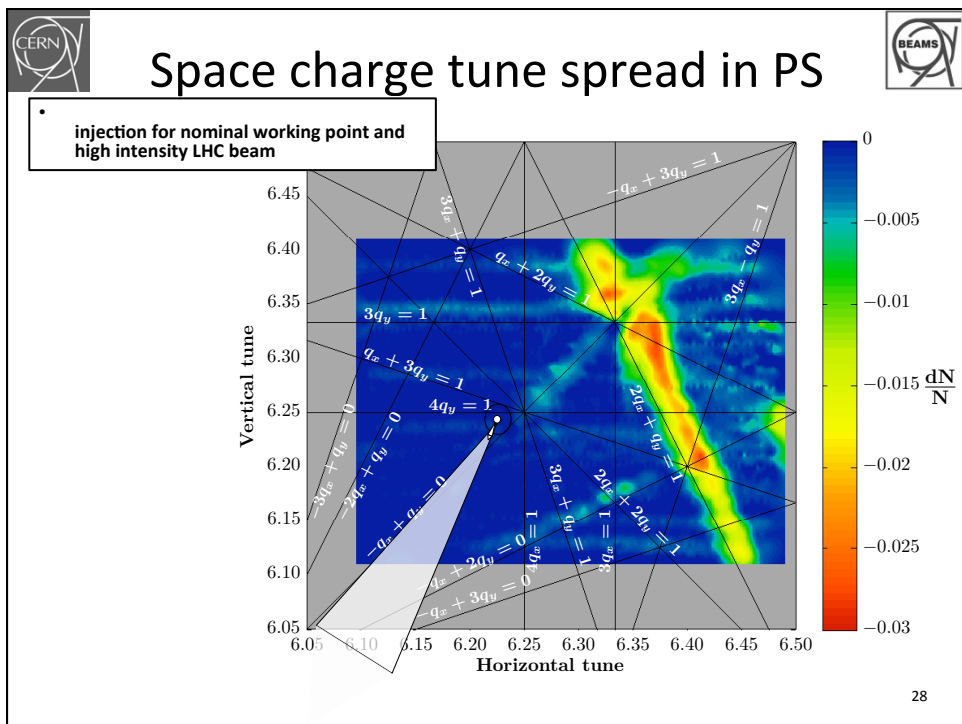
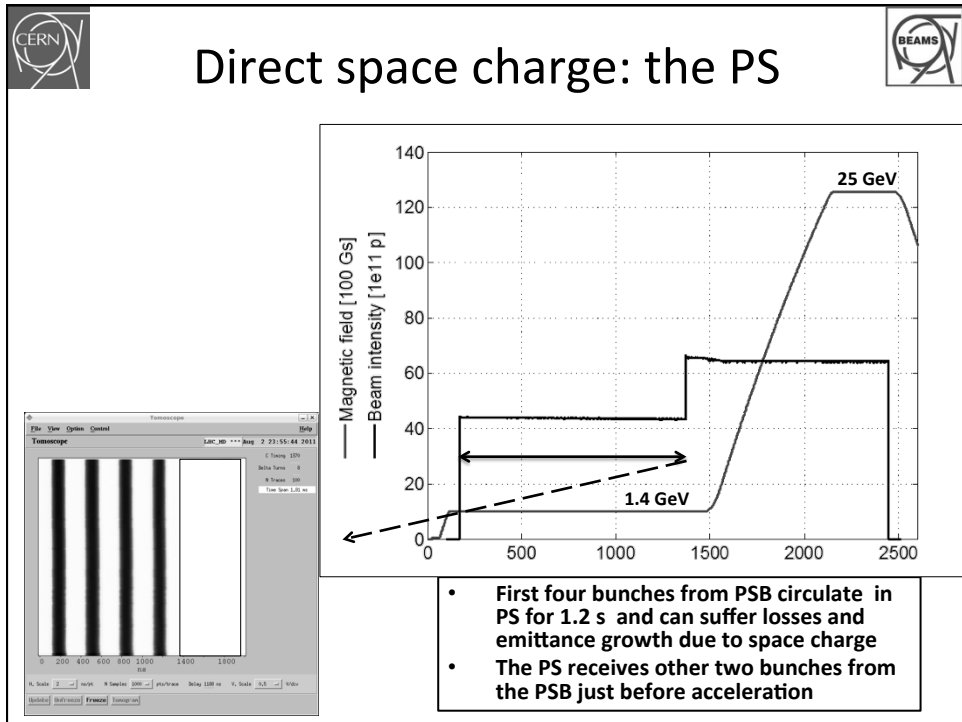


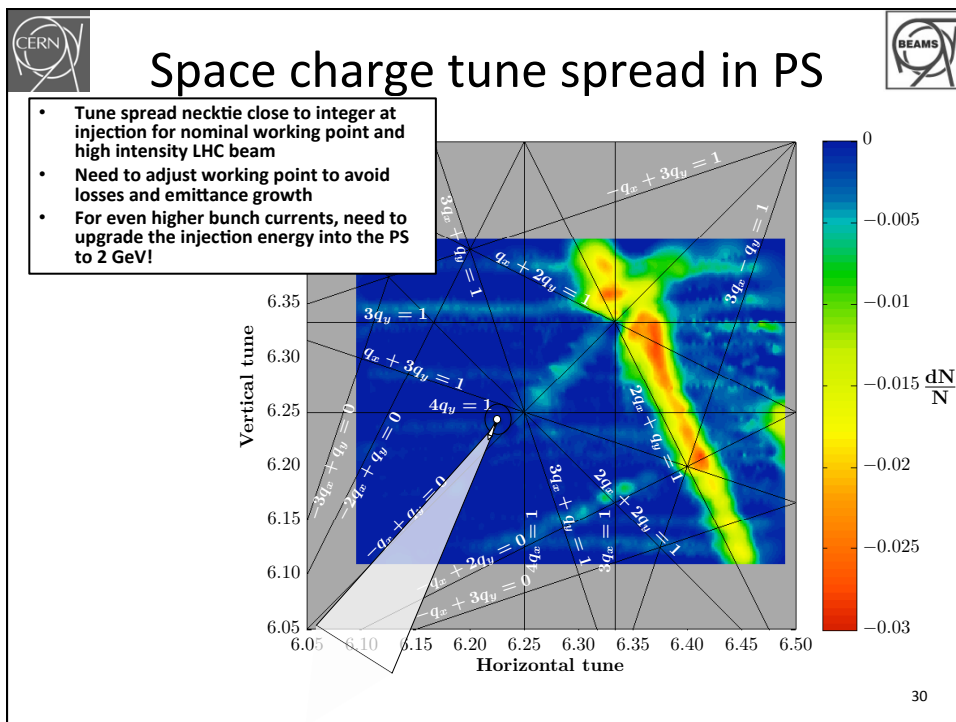
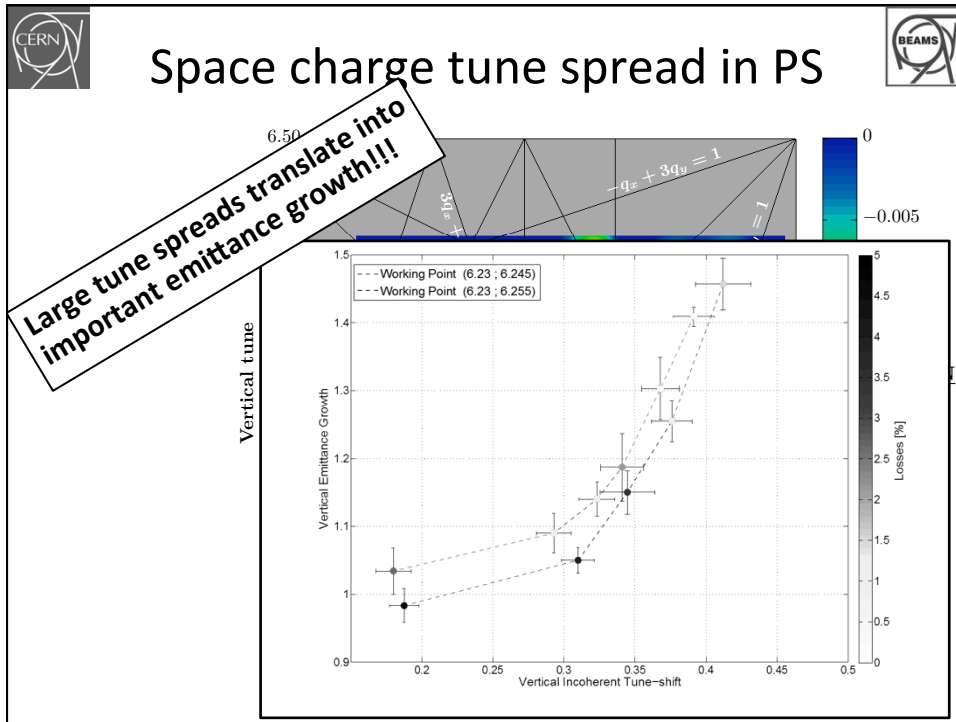


$$\Delta Q_{x,y}^{\max} = -\frac{r_0 \lambda_{\max} C}{2\pi e \beta \gamma^2 \epsilon_{xn,yn}}$$

$\propto \lambda_{\max}$	Bunches with higher peak current suffer larger space charge tune spreads
$\propto 1/\epsilon_n$	Lower emittance bunches suffer larger space charge tune spreads
$\propto 1/(\beta\gamma^2)$	Lower energy beams suffer larger space charge tune spreads
$\propto C$	Longer machines can build up larger space charge tune spreads

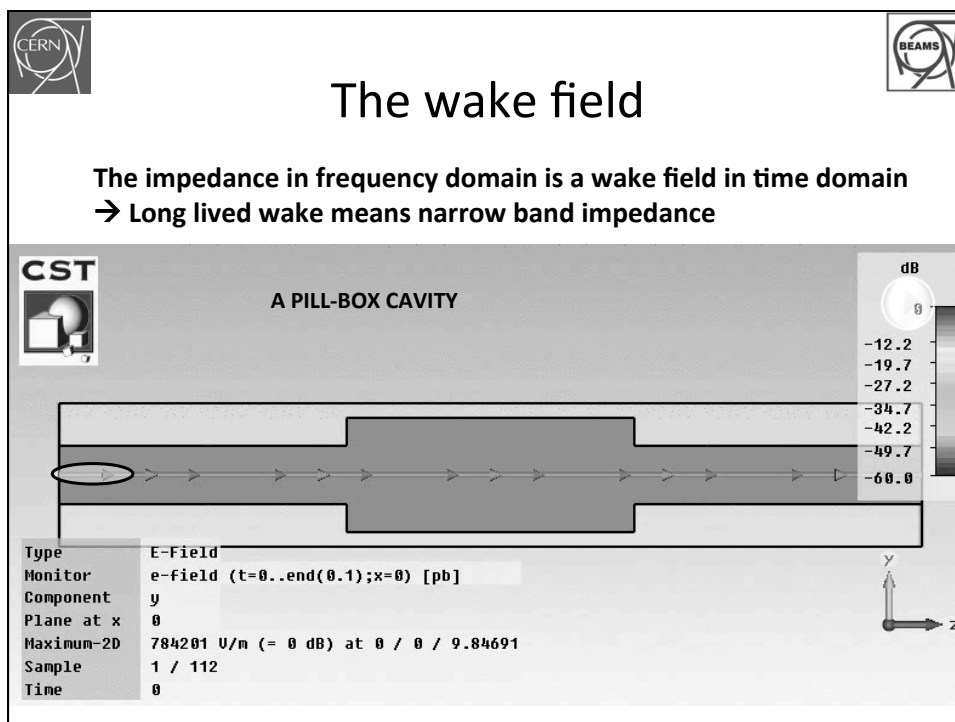


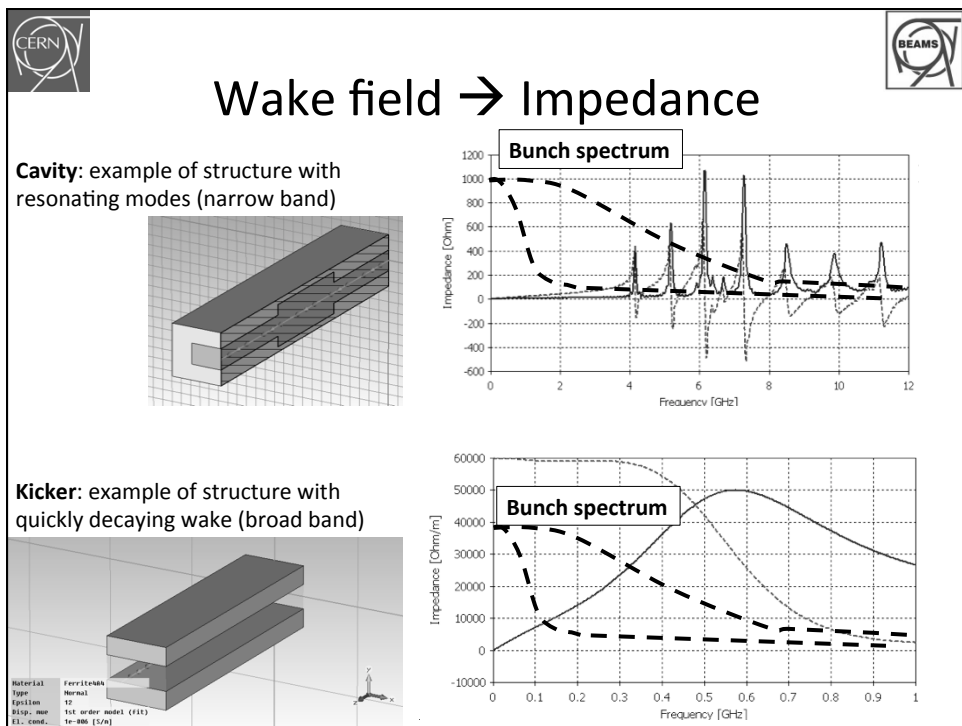
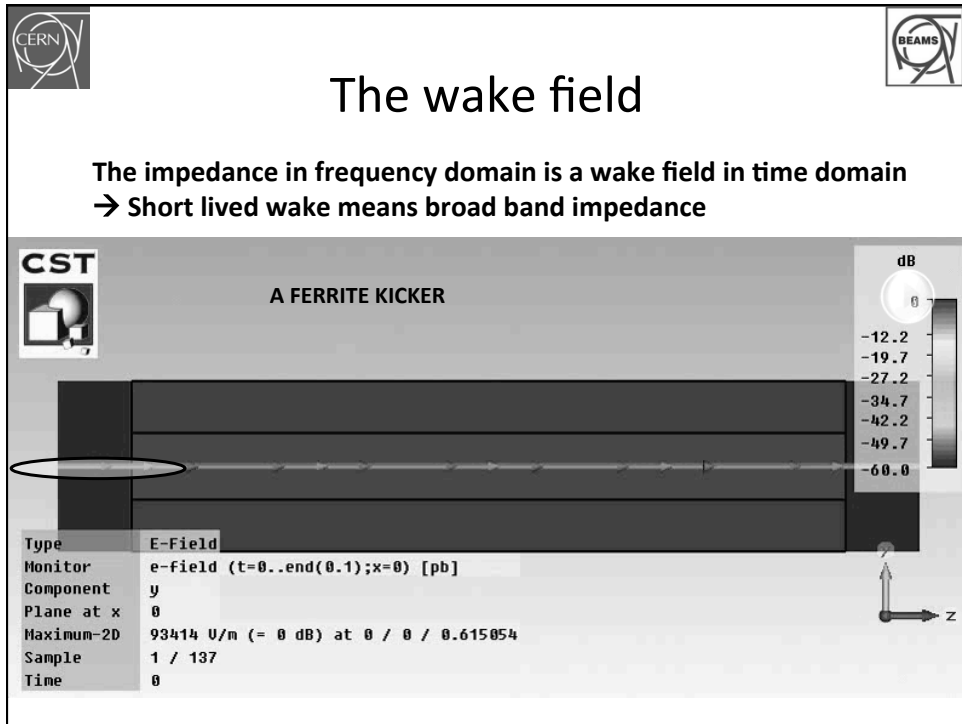






- Space charge
 - Low energy machines
- **Machine impedance**
- Electron cloud
 - Machines with short bunch spacing

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Effects of the impedance

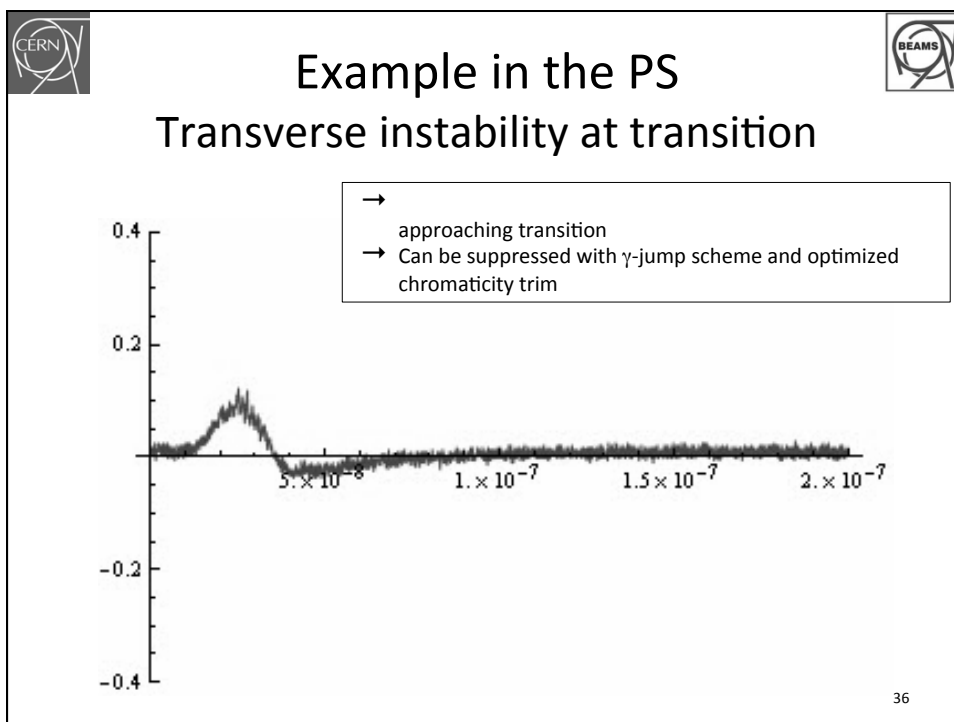
- When a bunch propagates in a resistive pipe or is exposed to ferric material, its wake field has a fast decay and can either couple its head and tail or couple it to few subsequent bunches
- When a bunch encounters a discontinuity (e.g., cavity, diagnostics device), its wake field can partly remain trapped in the structure and resonate for long time. Thus, it may affect several subsequent bunches, or even itself over several turns
- In either case, the bunch loses energy on the production of the EM field

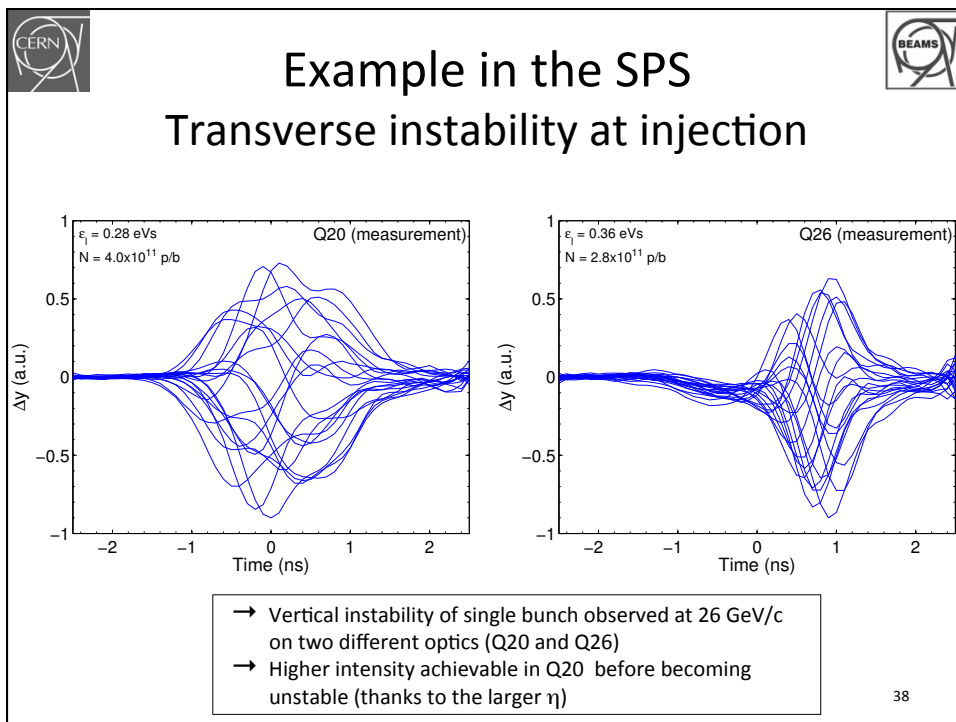
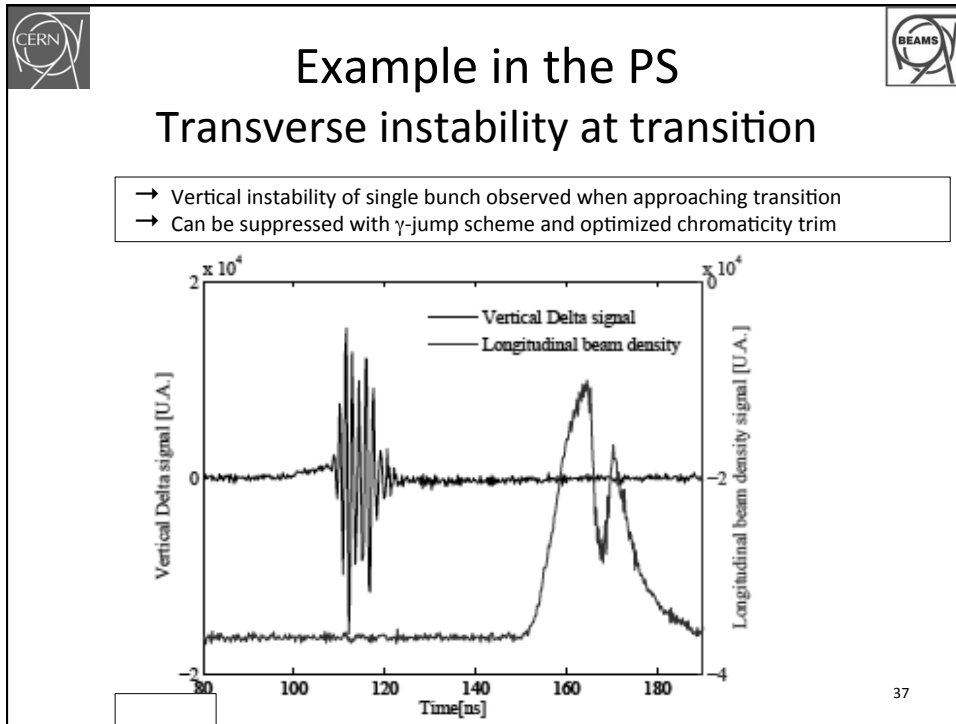
} Tune shift, single bunch or single train instabilities

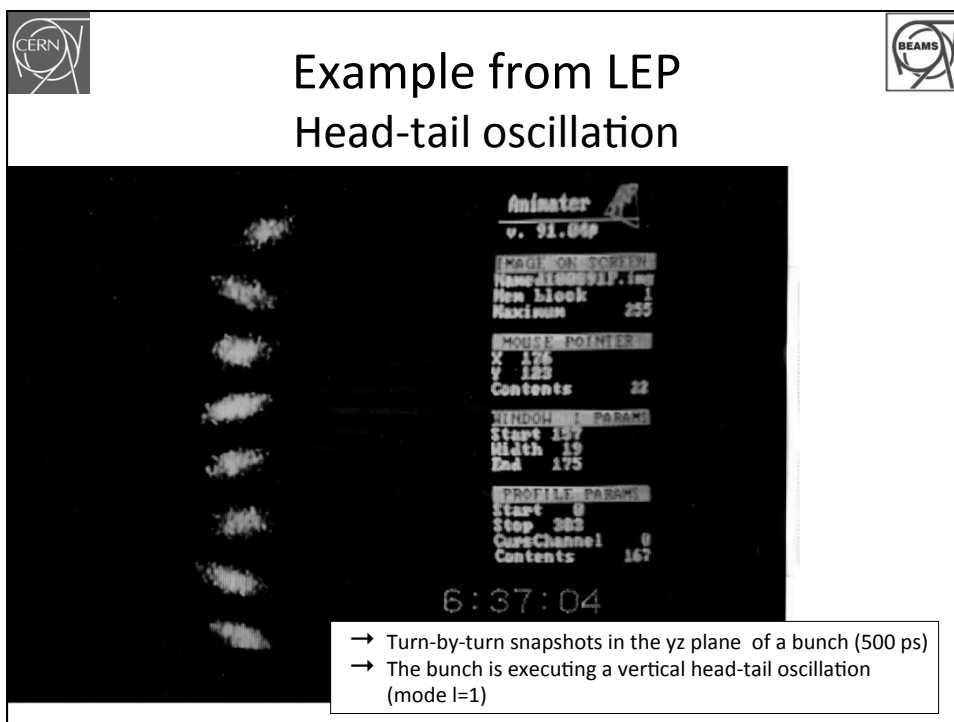
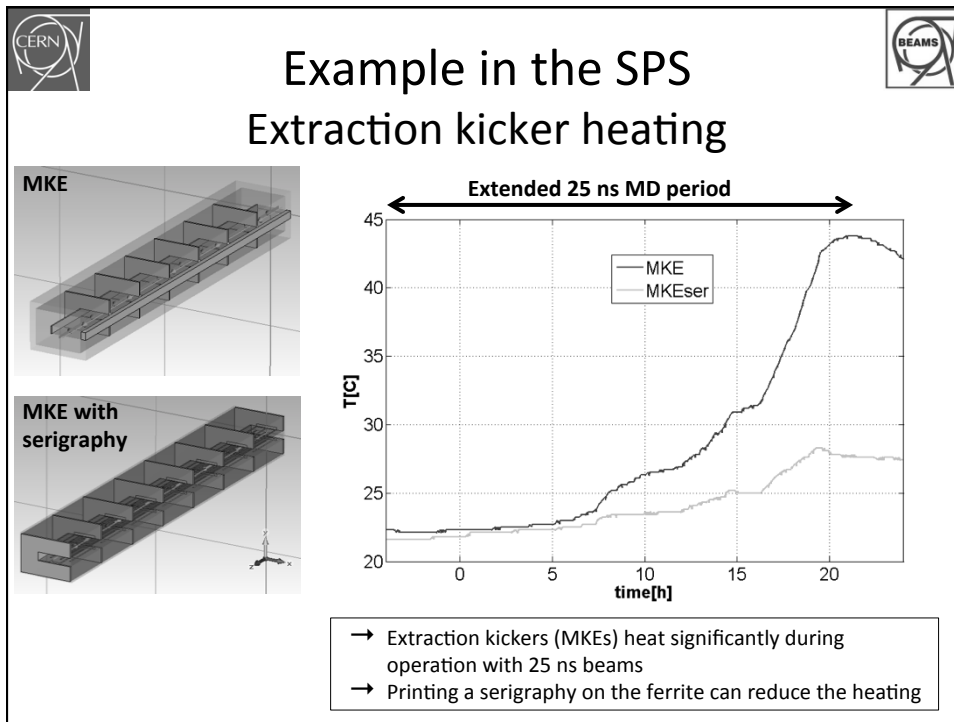
} Tune shift, coupled bunch or multi-turn instabilities

} Beam energy loss (compensated by the RF) + beam induced heating

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How to fight impedance effects

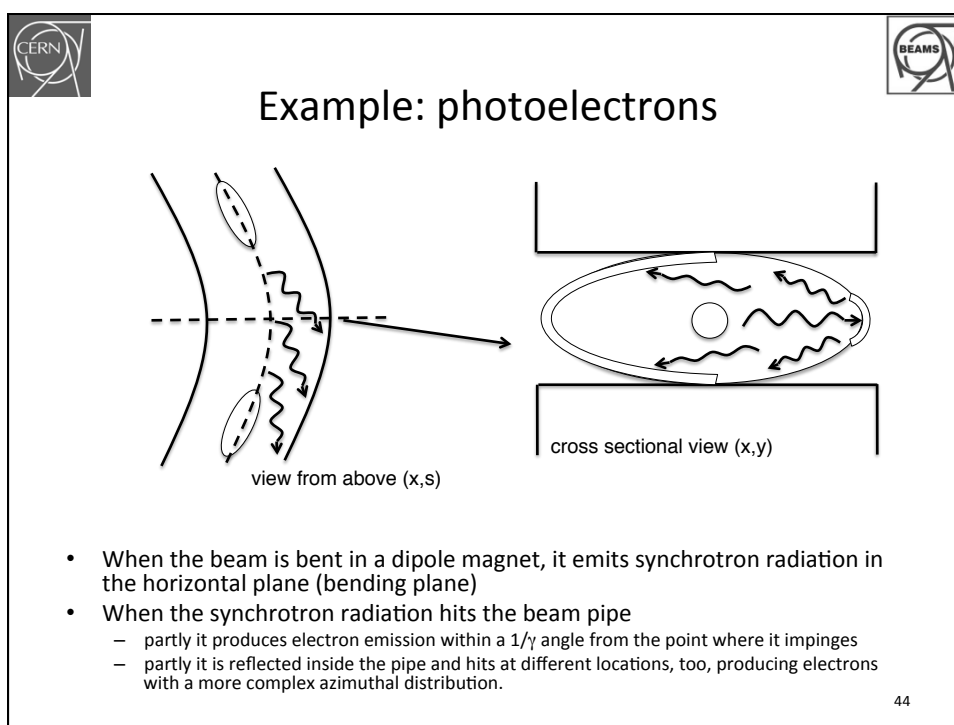
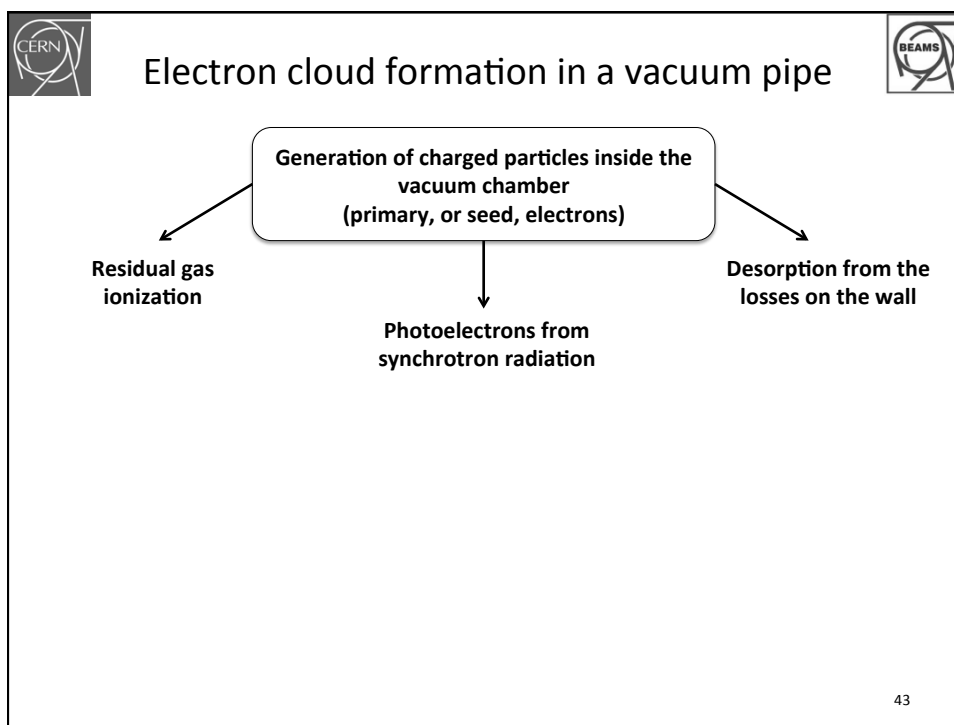
In running accelerators the **impedance effects are mitigated** relying on some mechanisms (passive or active)



- **Spreads and nonlinearities** keep the beam stable (through the mechanism of Landau damping)
 - Longitudinal: momentum spread, synchrotron frequency spread (Landau cavity)
 - Transverse: chromaticity, betatron tune spreads (e.g from machine nonlinearities)
 - E.g. octupoles, RFQ)
- **Active feedback systems** are routinely employed to control/suppress all types of instabilities
 - ✓ Coherent motion is detected (pick-up) and damped (kicker) before it can degrade the beam
 - ✓ Sometimes bandwidth/power requirements can be very stringent, but in general very efficient against coupled bunch phenomena
- **Impedance identification and reduction techniques** are applied to old accelerators as well as for the design of new accelerators to extend their performance reach!
 - Longitudinal: efficient to raise longitudinal instability thresholds as well as reduce equipment heating caused by the power loss
 - Transverse: raise transverse instability thresholds and limit incoherent effects

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- Space charge
 - Low energy machines
- Machine impedance
- **Electron cloud**
 - **Machines with short bunch spacing**

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Electron cloud formation in a vacuum pipe

Generation of charged particles inside the vacuum chamber
(primary, or seed, electrons)

↓

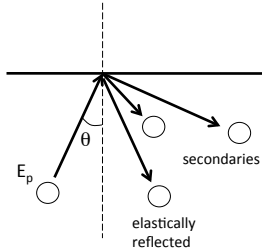
- Acceleration of primary electrons in the beam field
- Secondary electron production when hitting the wall

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Secondary electron emission

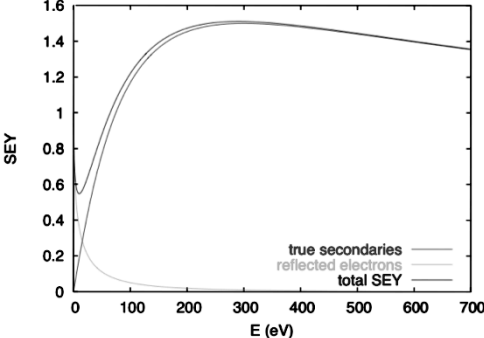
- When electrons hit the pipe wall, they do not just disappear.....
 - High energy electrons easily survive and actually multiply through **secondary electron emission**
 - Low energy electrons tend to survive long because they are likely to be elastically reflected.
- **Secondary electron emission is governed by the curve below**



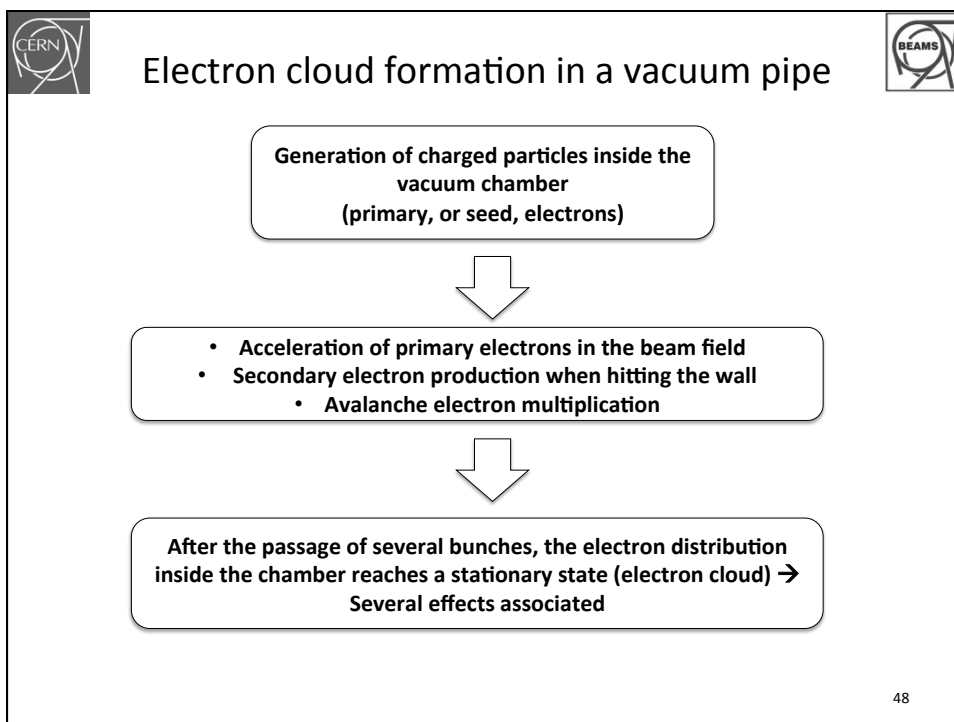
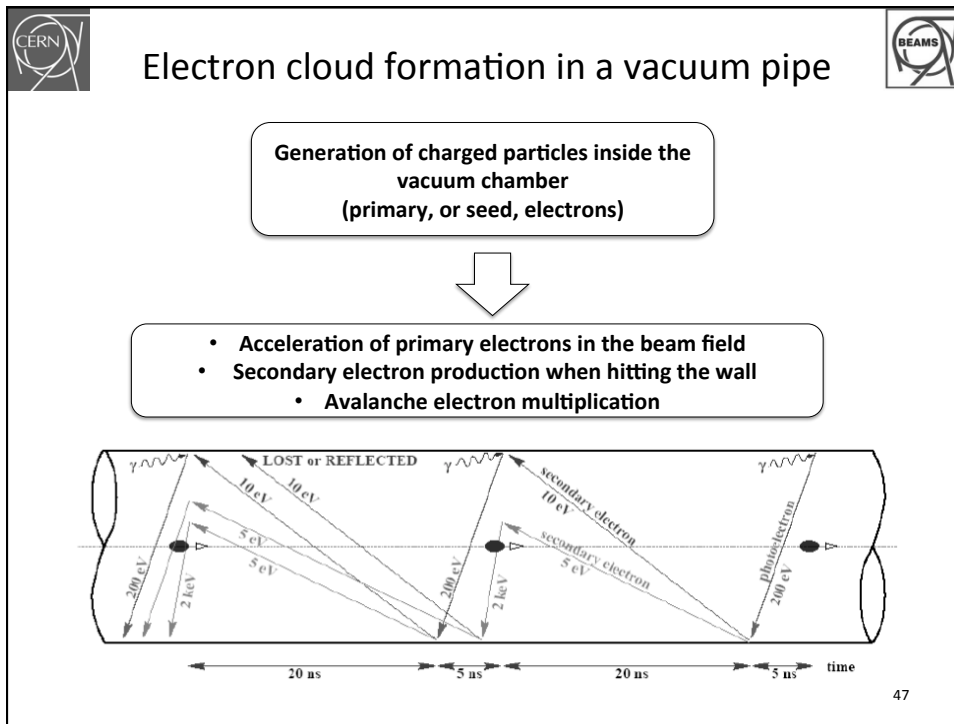
$$\delta_{\text{true}} = \delta_{\text{max}} \frac{sx}{s-1+x^s} \quad x = \frac{E}{E_{\text{max}}}$$

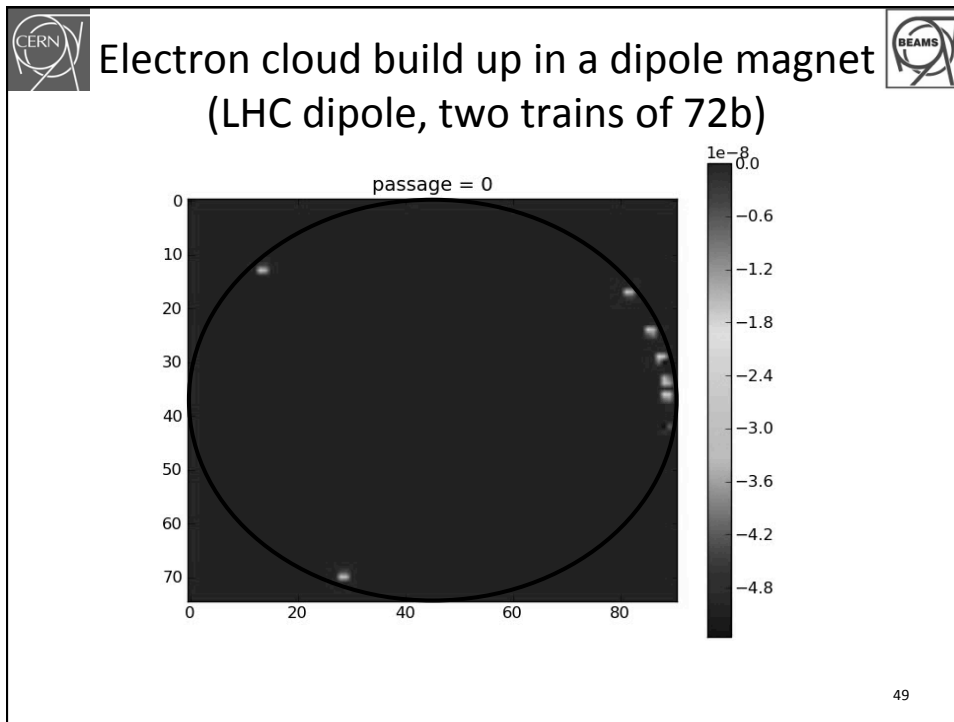
$$\delta_{\text{elas}} = \frac{(\sqrt{E} - \sqrt{E+E_0})^2}{(\sqrt{E} + \sqrt{E+E_0})^2}$$

$$\delta_{\text{tot}}(E) = \delta_{\text{true}}(E) + R_0 \cdot \delta_{\text{elas}}(E)$$



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CERN

Effects of the electron cloud

BEAMS

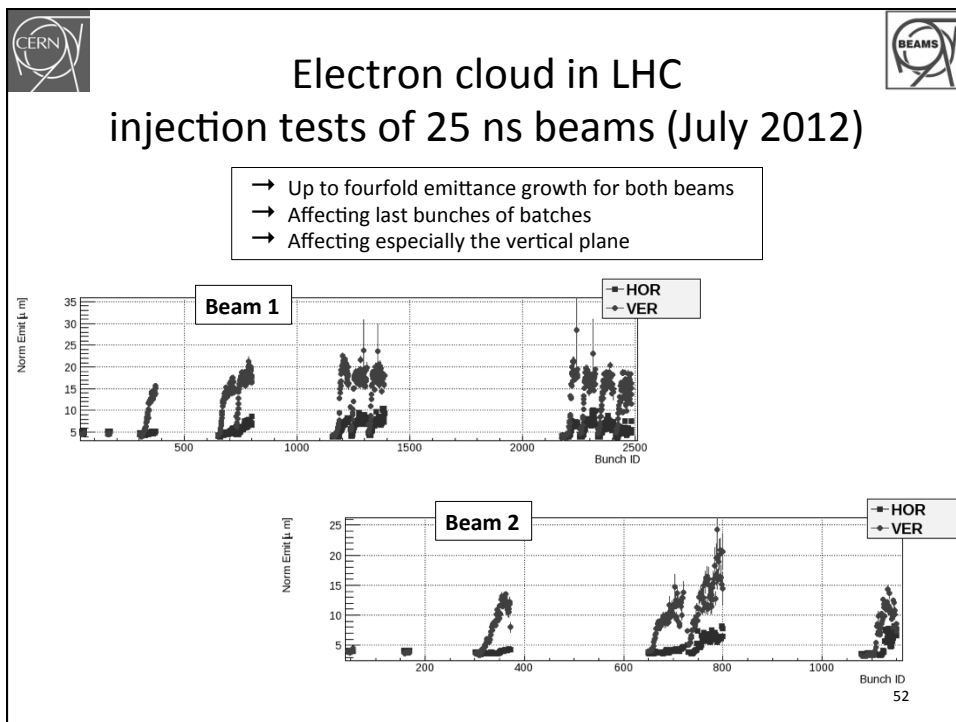
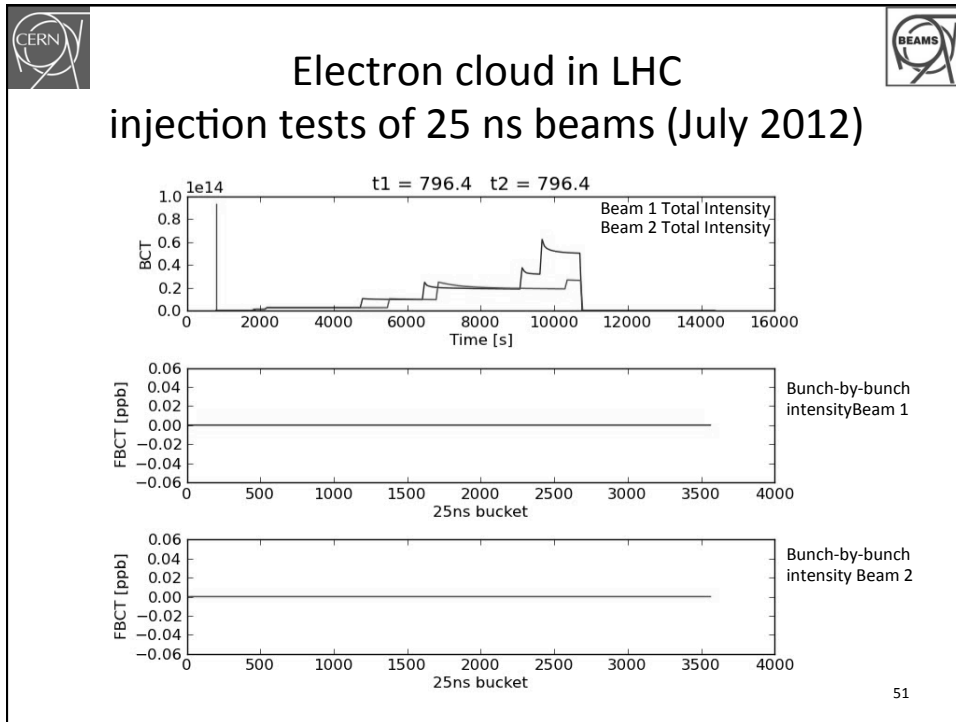
The presence of an electron cloud inside an accelerator ring is revealed by several **typical signatures**

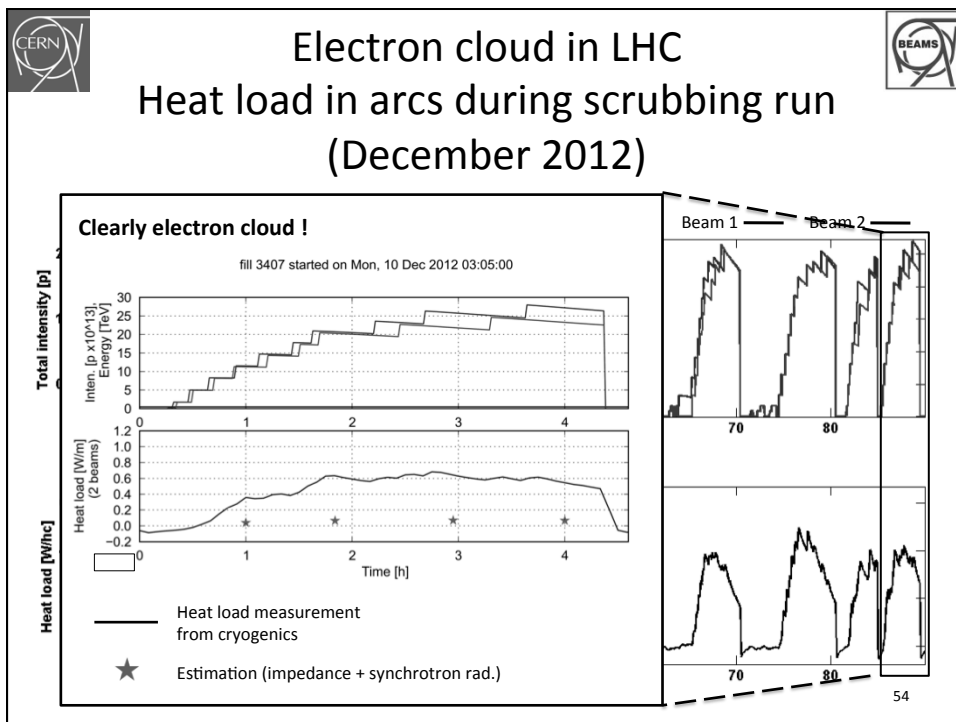
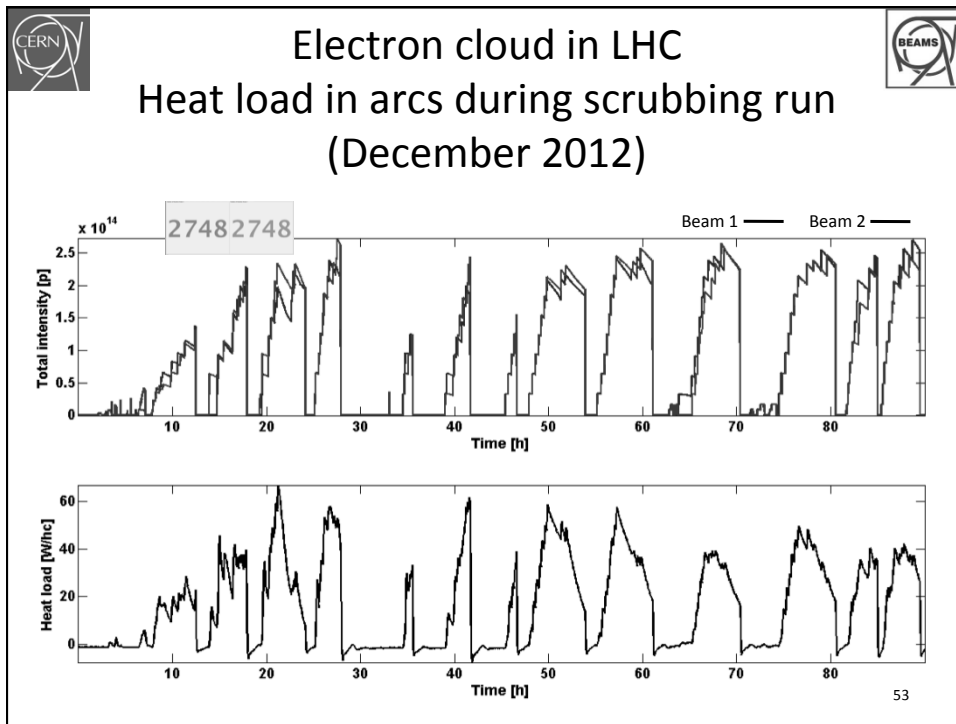
- ✓ Fast pressure rise, outgassing
- ✓ Additional heat load
- ✓ Baseline shift of the pick-up electrode signal
- ✓ Tune shift along the bunch train
- ✓ Coherent instability
 - Single bunch affecting the last bunches of a train
 - Coupled bunch
- ✓ Beam size blow-up and emittance growth
- ✓ Luminosity loss in colliders
- ✓ Energy loss measured through the synchronous phase shift
- ✓ Active monitoring: signal on dedicated electron detectors (e.g. strip monitors) and retarding field analysers

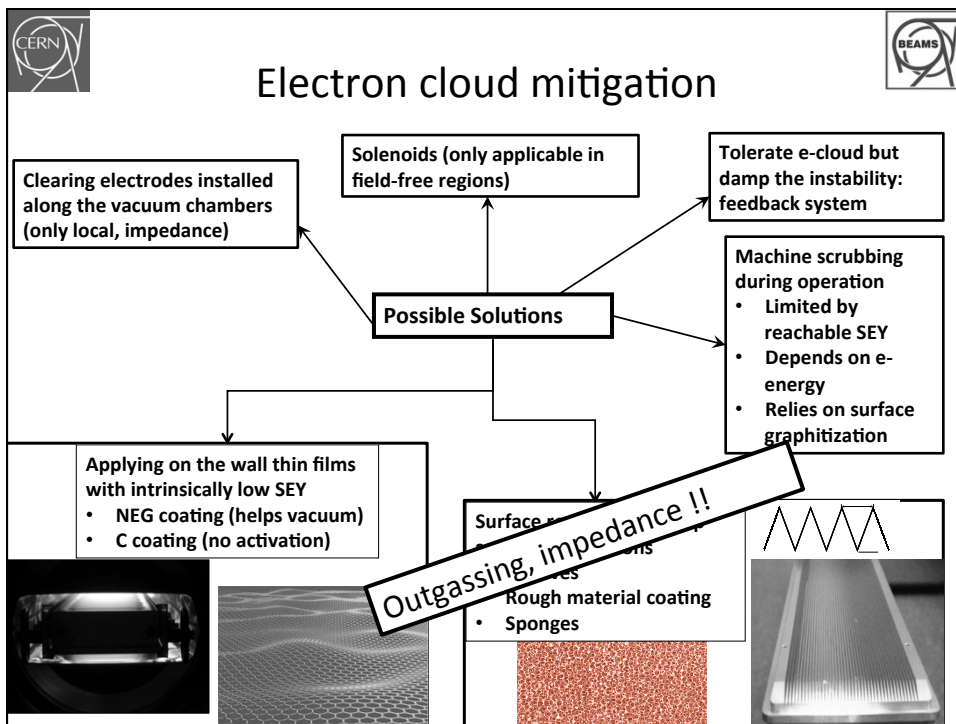
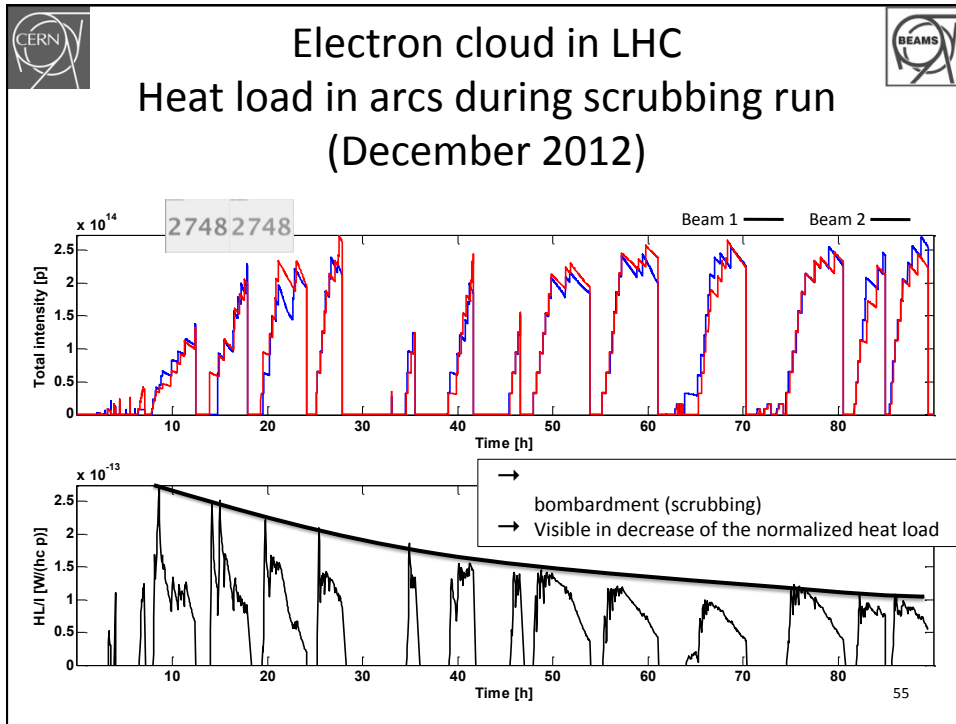
Machine observables

Beam observables

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To summarize and conclude

- **Collective effects are a threat to the preservation of the beam quality in an accelerator and usually define a performance limitation.** For ex.
 - Space charge → emittance growth, poor lifetime
 - Impedance → instabilities, beam induced heating
 - Electron cloud → instabilities, heating, vacuum degradation
- Theoretical and numerical models are constantly under development to explain the underlying mechanisms and be able to anticipate the effects on the beam
 - Essential for identification of the problems while designing a new machine or upgrading an existing one → to steer and optimize the design!
 - Allow understanding the source of problems in running machines → to study and implement the necessary countermeasures
- The CERN accelerator rings (PSB, PS, SPS, LHC) provide a varied range of examples of these effects and of the continued efforts to explain/suppress them