



# Magnets for accelerator, an accelerated view

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TE-MSC-MNC



# Acknowledgments

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# References

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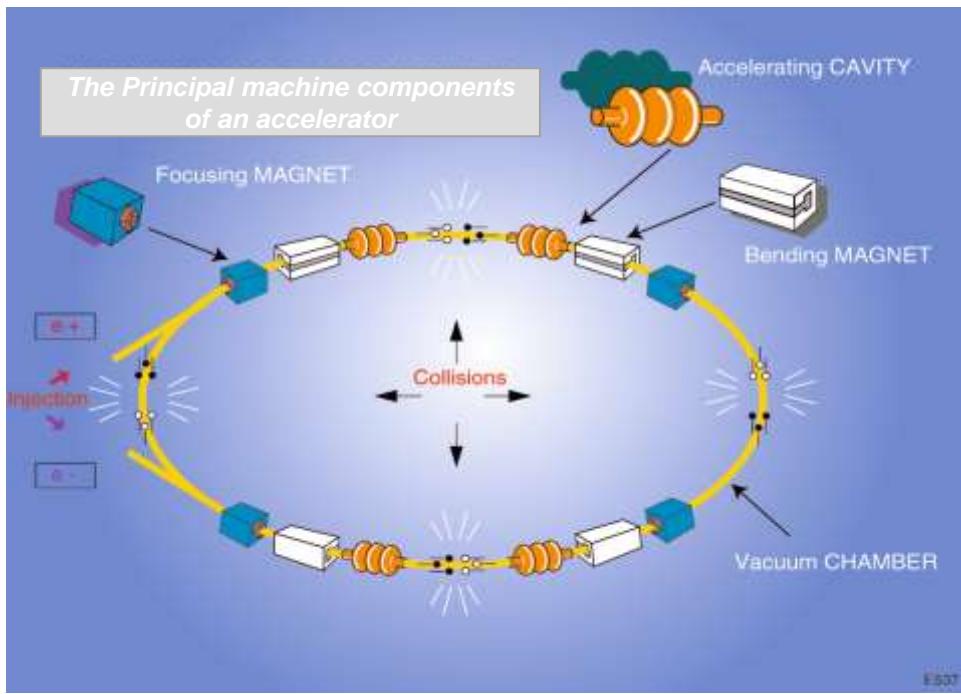
# Outline

- Introduction to magnets for accelerators
- Normal conducting magnets or iron dominated magnets
  - Field
  - Forces
  - Cooling
  - Construction
  - An example of technological issue: the insulation radiation resistance
- Superconducting materials
- Superconducting magnets
  - Field, forces and structures
  - An example of technological issue: the insulation
- Superconducting magnet construction

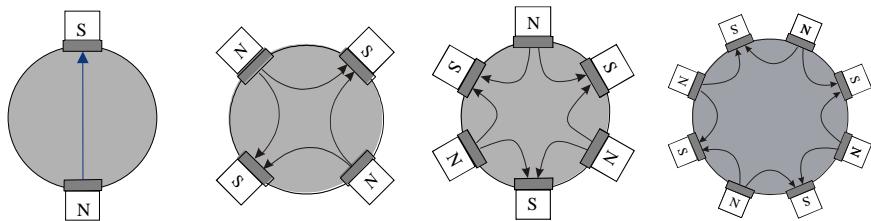


## INTRODUCTION

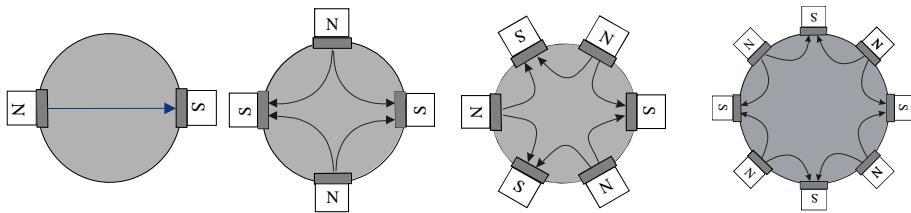




## Magnet types : field harmonics



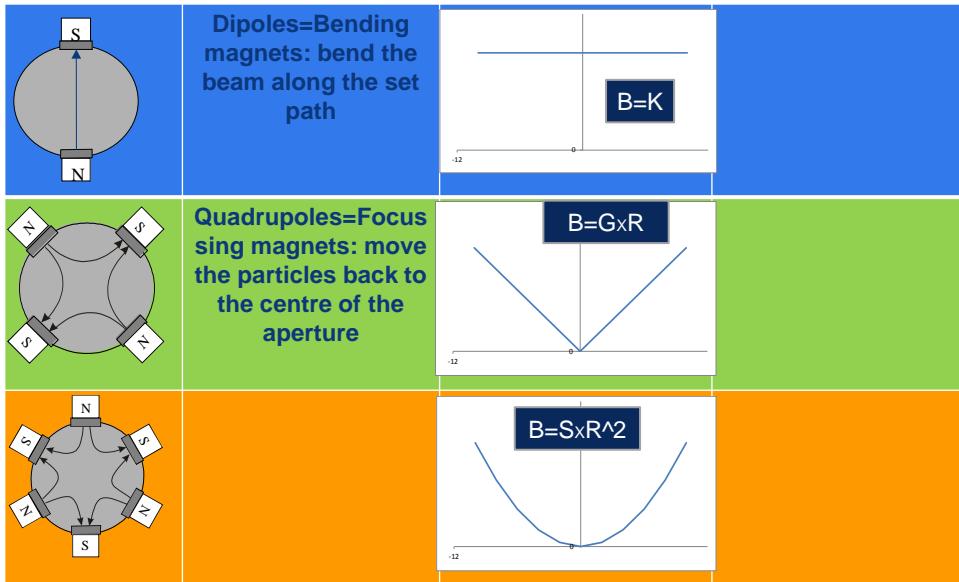
NORMAL : vertical field on mid-plane



SKEW : horizontal field on mid-plane



# Field type: shape and function I



## Why sextupole ?

$$B\rho = \frac{1}{qc} \sqrt{T^2 + 2TE_0}$$

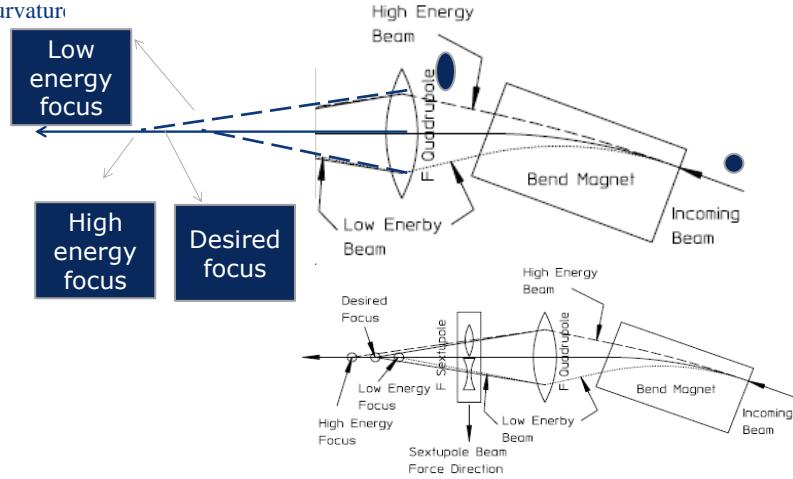
q = charge in Coulombs

c = the speed of light in m/sec

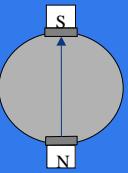
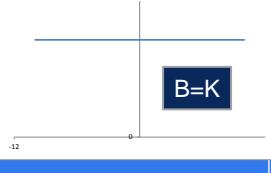
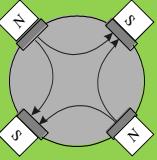
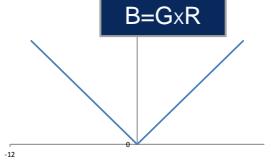
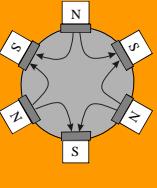
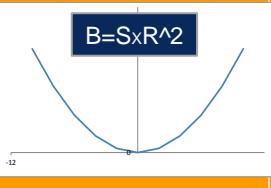
T = beam energy

E0 = the particle rest mass energy

$\rho$ = radius of curvature



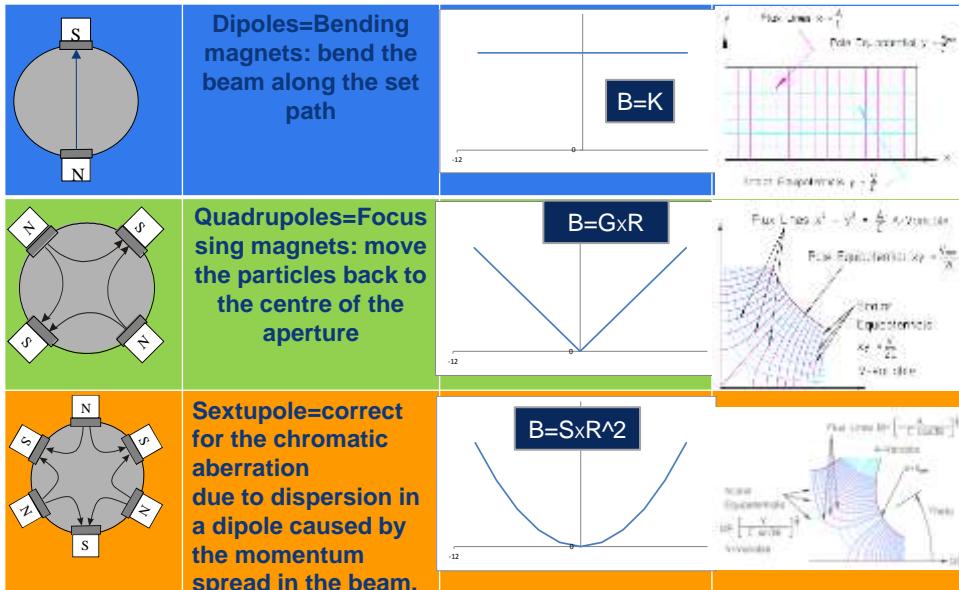
## Field type: shape and function II

	Dipoles=Bending magnets: bend the beam along the set path		
	Quadrupoles=Focus ing magnets: move the particles back to the centre of the aperture		
	Sextupole=correct for the chromatic aberration due to dispersion in a dipole caused by the momentum spread in the beam.		

## NORMAL CONDUCTING MAGNET OR IRON DOMINATED MAGNETS



## Field type: shape and function III



## Shaping the field

$$(\vec{B}_2 - \vec{B}_1) \cdot \vec{n} = 0$$

$$(\vec{H}_2 - \vec{H}_1) \times \vec{n} = \frac{4\pi}{c} \vec{K}$$

$$\vec{B}_2 \cdot \vec{n} = \vec{B}_1 \cdot \vec{n}$$

$$\frac{\vec{B}_2}{\mu_2} \times \vec{n} = \frac{\vec{B}_1}{\mu_1} \times \vec{n} \rightarrow \vec{B}_2 \times \vec{n} = \frac{\mu_2}{\mu_1} \vec{B}_1 \times \vec{n}$$

$$B_2 \cos \alpha_2 = B_1 \cos \alpha_1$$

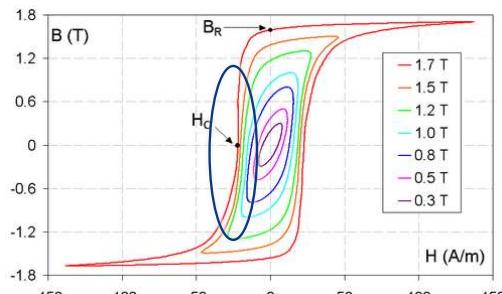
$$B_2 \sin \alpha_2 = \frac{\mu_2}{\mu_1} B_1 \sin \alpha_1$$

$$\tan \alpha_2 = \frac{\mu_2}{\mu_1} \tan \alpha_1$$

$$\tan \alpha_2 = \frac{\mu_{r2}\mu_0}{\mu_{r1}\mu_0} \tan \alpha_1$$

$$\tan \alpha_2 = \frac{1}{\mu_{r1}} \tan \alpha_1$$

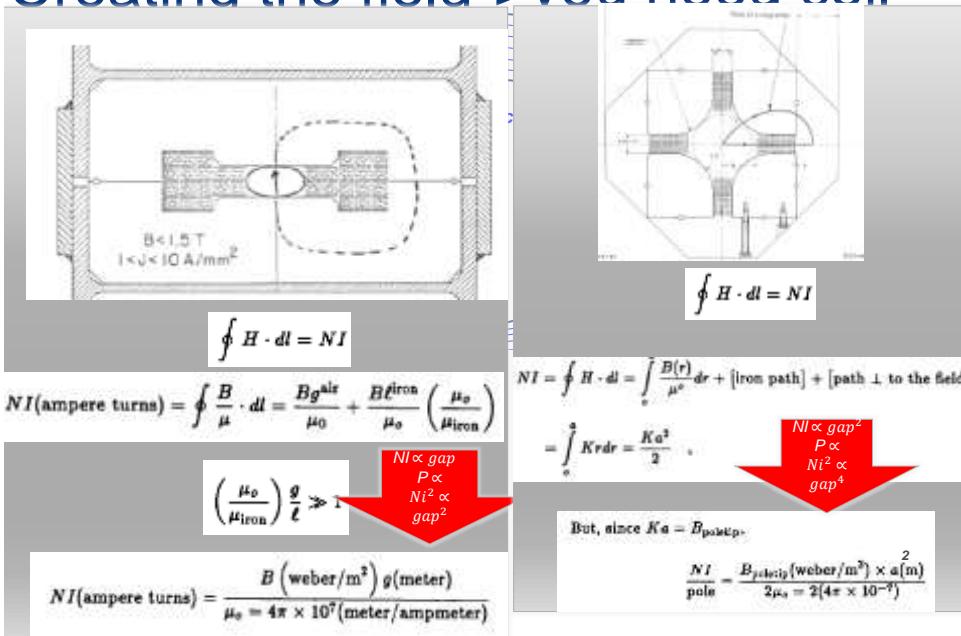
$$\mu_{r1} \gg 1 \rightarrow \alpha_2 \sim \frac{\pi}{2}$$



Therefore the flux line (to which the  $\vec{B}$  is tangent point by point) is perpendicular to the shape of the interface between a material with high  $\mu_r$  and the air independently of the shape of the flux lines in that materials



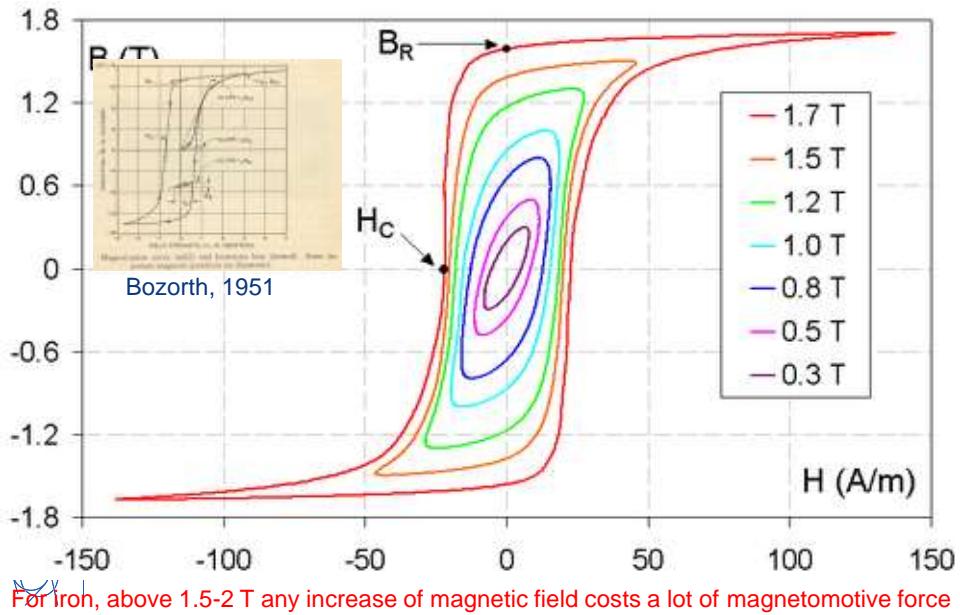
# Creating the field->you need coil



## Field type: shape and function, real magnet

<p>Dipoles=Bending magnets: bend the beam along the set path</p>	<p><math>B=K</math></p>	<p>Quadrupoles=Focus ing magnets: move the particles back to the centre of the aperture</p>	<p><math>B=GxR</math></p>	<p>Sextupole=correct for the chromatic aberration due to dispersion in a dipole caused by the momentum spread in the beam.</p>	<p><math>B=SxR^2</math></p>
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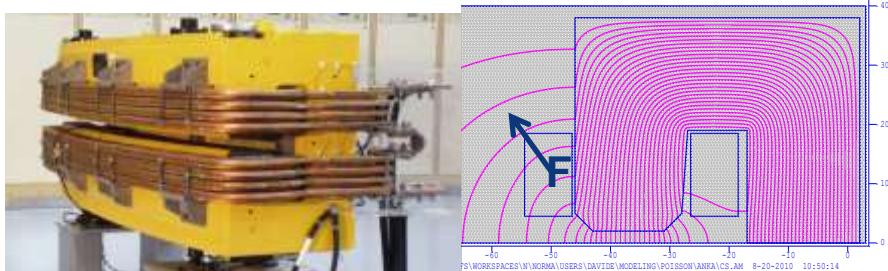
But iron saturates ,.....



Effect of interaction field with the coil current:

On a conductor immersed in magnetic field

$$\mathbf{F} = I \cdot \mathbf{L} \times \mathbf{B}$$



Example for the Anka dipole:  
On a the external coil side with  $N=40$  turns,  $I=700A$ ,  $L\sim 2.2$  m  
in an average field of  $B=0.25$  T



$$F = 40 \cdot 700 \cdot 2.2 \cdot 0.25 = 15400 \text{ N} = 0.015 \text{ MN} \sim 1.5 \text{ tons}, \\ 0.007 \text{ MN/m}$$

# Losses and heat removal

In a coil of cross section  $S$ , total current  $I$ , per unit of length  $l$ ,

$$P/l[W/m] = \frac{\rho}{S} \cdot I^2$$

$$\rho_{cu} = 1.72 \cdot (1 + 0.0039 \cdot (T - 20)) \cdot 10^{-8} \Omega \cdot m$$

In the yoke we have losses due to:

- hysteresis: up to 1.5 T we can use the Steinmetz law

$$P[W/kg] = \eta \cdot f \cdot B^{1.6}$$

with  $\eta = 0.01 \div 0.1$ , about 0.02 for silicon steel

- eddy currents: for silicon iron, an approximate formula is

$$P[W/kg] = 0.05 \cdot (d_{lam} \cdot \frac{f}{10} \cdot B_{av})^2$$

where  $d_{lam}$  is the lamination thickness in mm



To increase the temperature of 1 kg of water by 1 degree C we need 1 kcal = 1/4.186 kJ

$$Q[l/min] = 14.3 \cdot \frac{P[kW]}{\Delta T}$$

To efficiently cool a pipe you need the fluid velocity be greater than zero on the wall, i.e. the flow being moderately turbulent ( $Reynolds > 2000$ ):

$$R_e = \frac{d \cdot v}{\nu} \sim 1400 \cdot d [mm] \cdot v [m/s] \text{ for water at } \sim 40^\circ C$$

Small pipes need high velocity, however attention to erosion ( $v > 3 \text{ m/s}$ )!

As cooling pipes in magnets can be considered smooth, a good approximation of the pressure drop  $\Delta P$  as a function of the cooling pipe length  $L$ , the cooling flow  $Q$  and the pipe hole diameter  $d$  is derived from the Blasius law, giving:

$$\Delta P[bar] = 60 \cdot L[m] \cdot \frac{Q[l/min]^{1.75}}{d[mm]^{4.75}}$$

## Normal conducting magnet construction

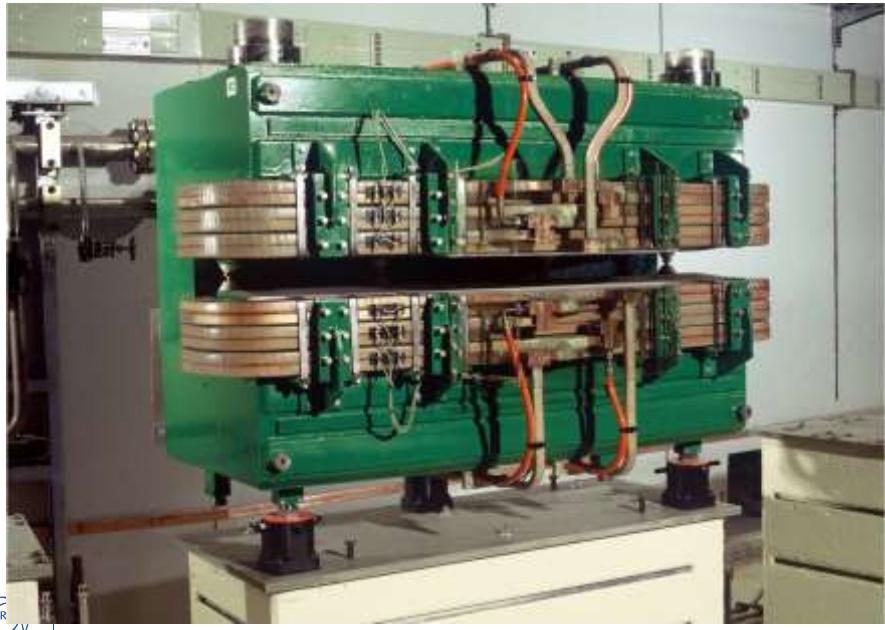


## Coil production



## Iron yoke production

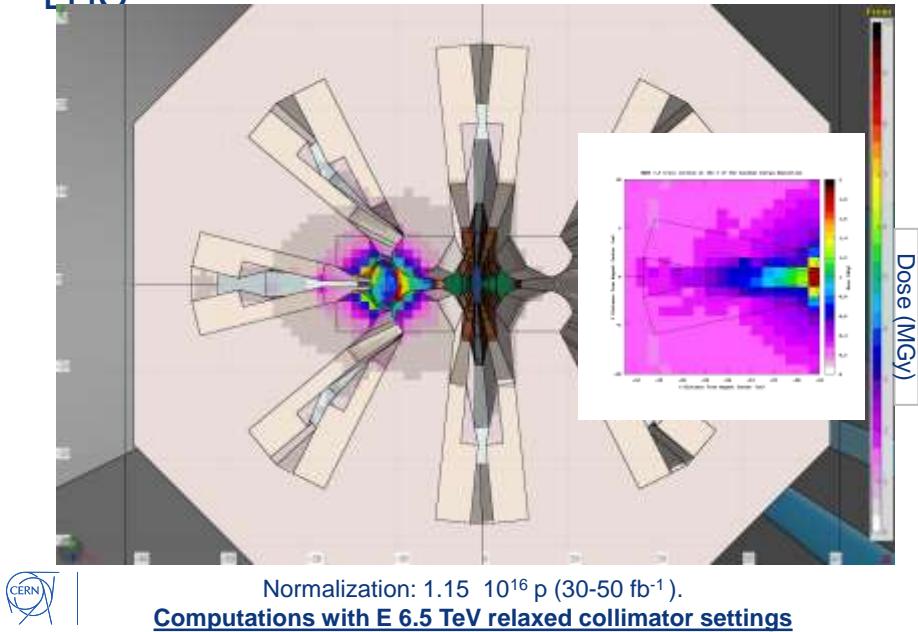




*An example of technological issue:  
the insulation radiation resistance*



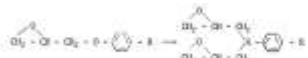
## Dose on a normal conducting magnet in the LHC



## Different epoxy

Resins	Hardeners	Additives	Composition (p.p.)	Mix Temp (°C)	Viscosity (cPs)	Service life (min)	Fig	Dose for 50% flex. (MGy)	Dose Range (MGy)
EDBAH	MA						5.4	1.4	
EDRAH	MA	BDMA	100-105-0.2	80	45	>180	5.1	1.6	
BECP	MA						5.4	2.5	
BECP	MA	BDMA	100-110-0.2	80	40	>180	5.1	2.3	
ECC	MA			100-72	80	>20	5.5	1.8	
VCD	MA	BDMA	100-160-0.05	60	20	>180	5.4	3.7	
DADD	MA			100-65	80	>240	5.4	5.5	
DGEBA + EDG09	TETA		100-20-12	25			5.21	1.3	
DGEBA	TETA	DBP	83-9-17	50	500	few	5.22	1.2	
DGEBA	DADPS		100-35	130	60	180	4.2	5.1	
DGEBA + EDG09	MDA		100-20-30	80			5.21	8.2	
DGEBA	MDA		100-27	80	100	50	5.9	13.0	
DGEBA	MPDA		100-14.5	65	200	30	5.7	23.5	
DGEBA	MDA		100-40	100	150	30	5.26	45	
DGEBA	DEA	BDMA	100-130-1	80	70	120	5.2	4.2	
DGEBA	NMA	BDMA	100-80-1	80	80	120	5.2	5.9	
DGEBA	MA		100-100	60	69	>1440	5.23	7.1	
DGEBA	MA	BDMA					5.1	12.0	
DGEBA	MA	BDMA + Po. Gl.	100-100-0.1-10	60	65	300	5.23	12.1	
DGEBA	AP		100-70	120	26	180	5.2	13.0	
DGPP	DADPS		100-28	130			5.6	8.2	
DGPP	MA		100-135	120			5.3	13.0	
EDTC	MDA		100-20	80		40	5.9	10.0	
TGTPE	DADPS		100-34	125	>20000		5.6	12.1	
TGTPE	MA	BDMA	100-100-0.2	125	>15000		5.3	10.6	
EPN	DADPS		100-35	100		30	5.6	23.5	
EPN	MDA		100-29	100		35	5.10	37.2	
EPN	HPA	BDMA	100-76-1	80		40	5.10	13.0	
EPN	MA	BDMA	100-105-0.5	80		100	5.3+25	15.0	
EPN	NMA	BDMA	100-85-1	100		80	5.10	20.6	
TGMD	DADPS		100-40	80		50	5.6	20.6	
TGMD	MA	BDMA	100-136-0.5	60		30	5.3	11.4	
TGMD	NMA	BDMA	100-130-1	80	500	20	5.8	16.0	
TGDP	NMA		100-137	80	<20		5.8	23.5	
DGA	MDA		100-20	25		120-420	5.7	23.5	
DGA	NMA		100-115	25	5 - 20	30-5760	5.8	28.6	

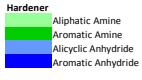
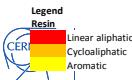
Legend  
 Resin | Hardener  
 Red | Aliphatic Amine  
 Yellow | Cycloaliphatic  
 Green | Aromatic  
 Blue | Aliphatic  
 Cyan | Cycloaliphatic  
 Magenta | Aromatic Anhydride  
 Orange | Alicyclic Anhydride  
 Purple | Aromatic Anhydride



- Aromatic >
- Cycloaliphatic >
- Linear Aliphatic
- Aliphatic amine hardener → poor radio-resistance
- Aromatic amine hardener > Anhydride hardener
- H: Too high local concentration of benzene may induce steric hindrance disturbance
- Good radio-resistance even if Cl (tendency to capture  $n_{\text{th}}$ )
- Novolac: HIGH Radio-resistance
  - Large nb of epoxy groups
  - Density = viscosity
- Glycidyl-amine: HIGH R.-resistance
  - Quaternary carbon → weakness
  - Ether group → Repl. by amine
  - weakness

# Filler contribution

Resins	Hardeners	Additives	Filler	Composition (p.p.)	Fig	Dose for 50% flex. (MGy)	Dose Range (MGy)
DGEBA	MDA		Papier	100-27-200	5.14	1.3	1 - 2
DGEBA	MDA		Silice	100-27-200	5.14	10	
DGEBA	MDA		Silice	100-27-200	5.18	11.4	
DGEBA	MDA		Silice (5 micron)	100-27-20	5.16	14.8	10 - 15
DGEBA	MDA		Silice (20 micron)	100-27-20	5.16	14.8	
DGEBA	MDA		Silice (40 micron)	100-27-20	5.16	14.6	
DGEBA	MDA		Silice (40 micron)	100-27-200	5.17	12.1	
DGEBA	HPA	BDMA	Silice (40 micron)	100-80-2-200	5.17	<10	<10
DGEBA	MDA		Aérosol + Sulphate de Barium	100-27-2-150	5.14	15.8	15
DGEBA	MDA		Magnésie	100-27-120	5.14	18	18
DGEBA	MDA		Graphite	100-27-60	4.6	26.8	25 - 30
DGEBA	MDA		Graphite	100-27-60	5.14	30.5	
(DGEBA)	MDA		Alumine	100-27-220	4.7	23.5	20 - 50
DGEBA	MDA		Alumine	100-27-220	5.14	51.7	
DGEBA	MDA		Alumine	100-27-100	5.15	20.6	
DGEBA	MDA		Alumine	100-27-220	5.15	42.5	
DGEBA	MDA		Fibre de verre	100-27-50	5.19	82	80 - 100
DGEBA	MDA		Fibre de verre	100-27-60	5.18	100	
EPN	MDA		Fibre de verre	100-29-50	5.19	>100	>100
TGMD	MDA		Fibre de silice	100-41-50	5.20	>100	
TGMD	DADPS		Fibre de silice	100-40-50	5.20	>100	>100



2 Categories of fillers:

1. Powder fillers

2. Glass/Silice

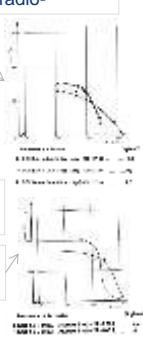
Paper [cellulose] ( $C_6H_{10}O_5)_n$ )  
→ Strong decrease of radio-resistance

The bigger the powder, the more radio-resistant

Hardener choice not influenced by filler

High r.-resistance for Graphite and Alumina

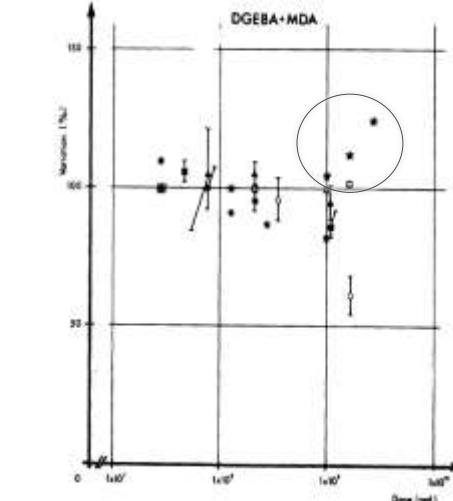
The more fillers, the more radio-resistant



Best Radio-Resistant materials are obtain with Glass/Silice (influence of boron) fibers and aromatic resins (Novolac and glycidyl-amine)

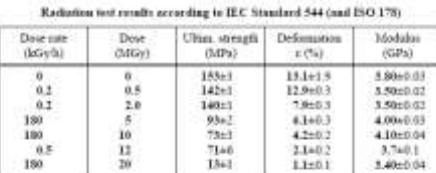
CERN 96-01/A/E

Material: Epoxy resin  
Type: MY 745 (50) + EPN 1130 (50) + CY 223 (20) + HY 905 (120) + DV 073 (0.5)  
Supplier: Ciba-Geigy  
Remarks: used for the ISR dipole

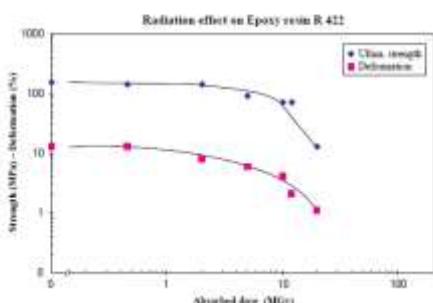


Modifications des propriétés mécaniques du DGEBA+MDA en fonction des doses absorbées

- 1 - Résistance à la flexion
- 2 - Résistance à la traction
- ▲ 3 - Modèle d'Arsène
- △ 4 - Allongement à la rupture
- 5 - Résistance au choc
- 6 - Durée
- 7 - Absorption d'eau - 25°C , 4 jours
- 8 - Pert de l'élasticité à la chaleur

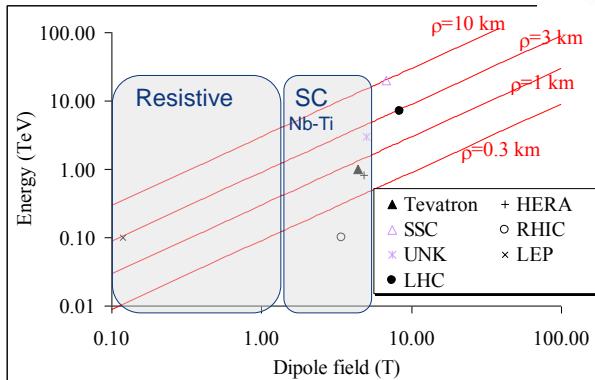
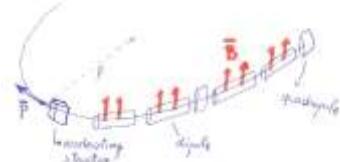


Radiation index (RI) = 6.9 of strength is the critical property  
Radiation index (RI) = 6.6 of deformation is the critical property



# The limits of NC magnet application

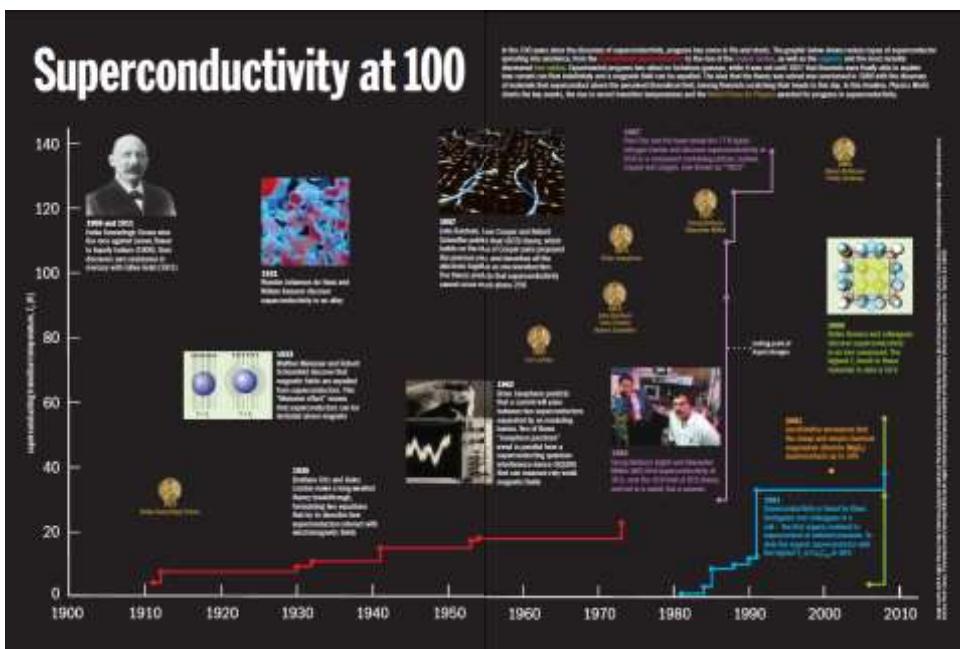
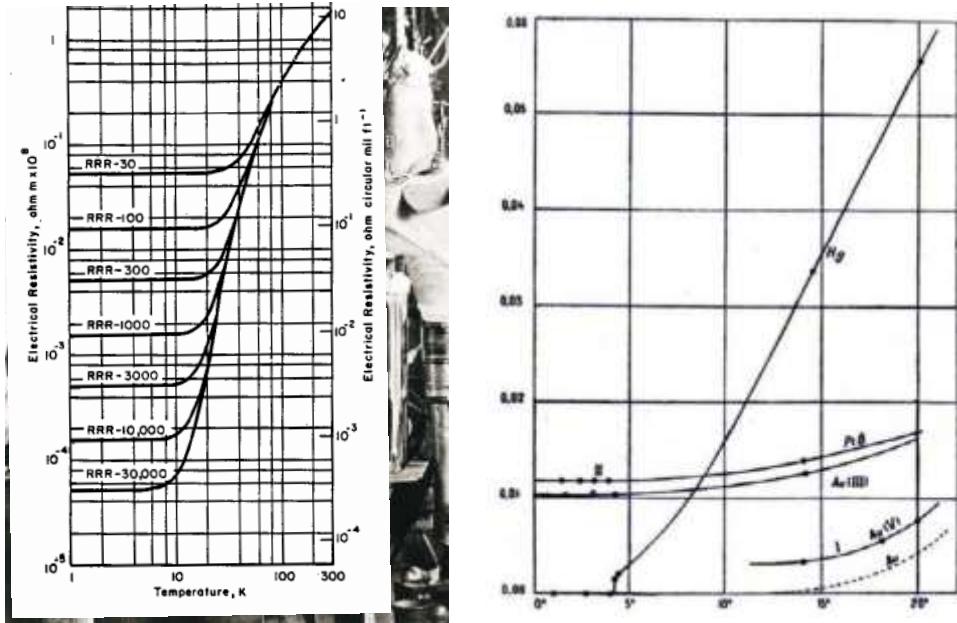
$$B\rho = \frac{1}{qc} \sqrt{T^2 + 2TE_0},$$

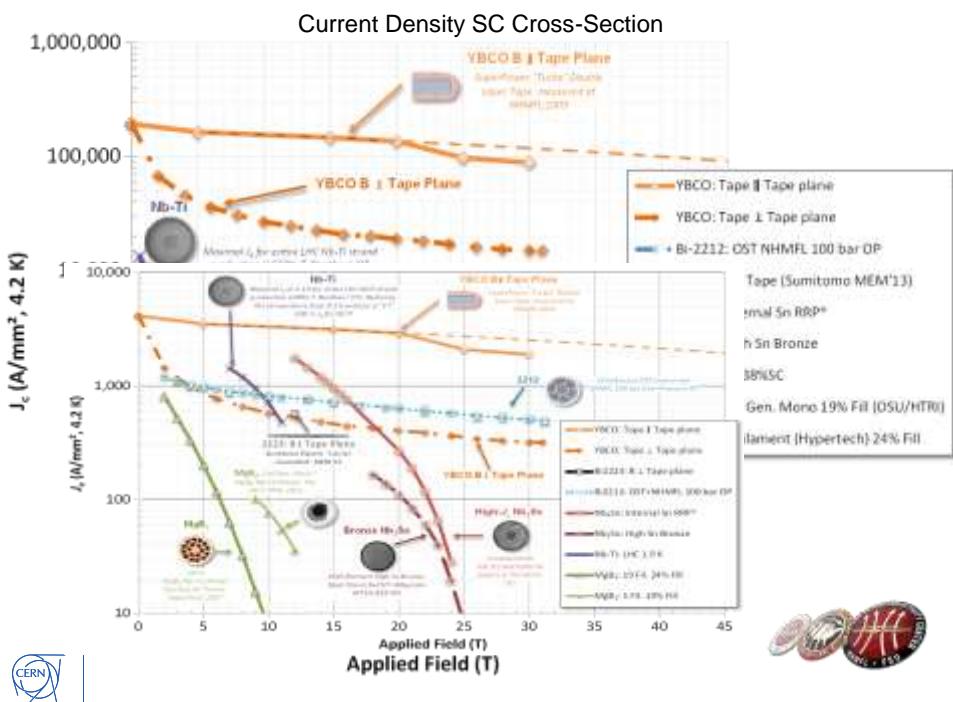
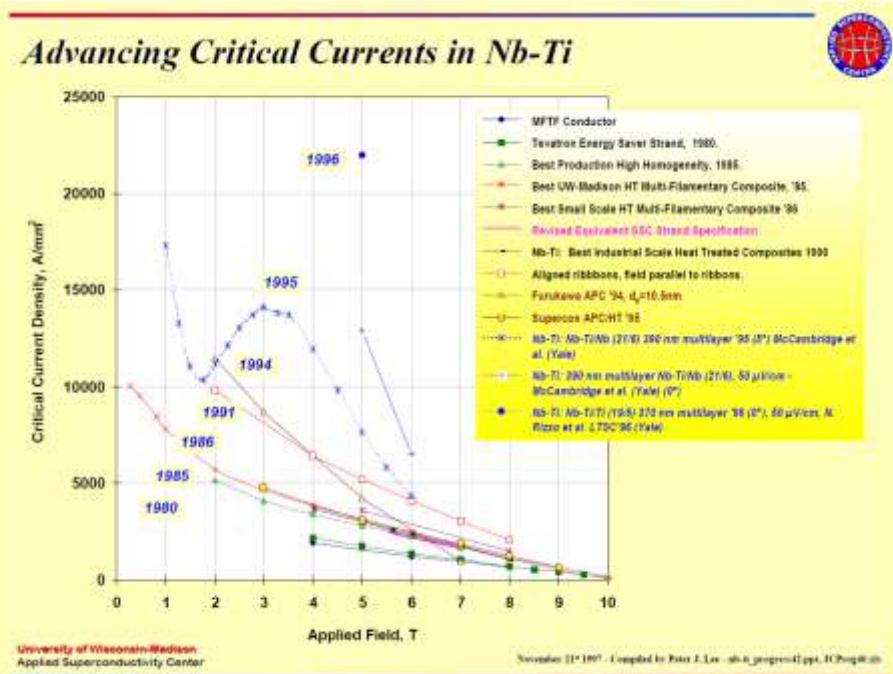


## SUPERCONDUCTING MATERIALS



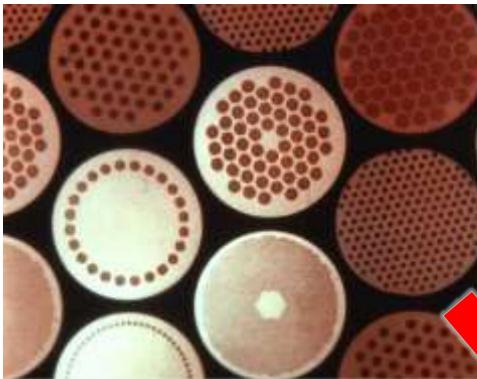
# Superconductivity





# Superconductor material, but under which conductor shape

for 5 to 10kA, we need 20 to 40 wires in parallel



- a single 5µm filament of Nb-Ti in 6T carries 50mA
- a composite wire of fine filaments typically has 5,000 to 10,000 filaments, so it carries 250A to 500A

$$V = \frac{LI}{t} = \frac{2E}{It}$$



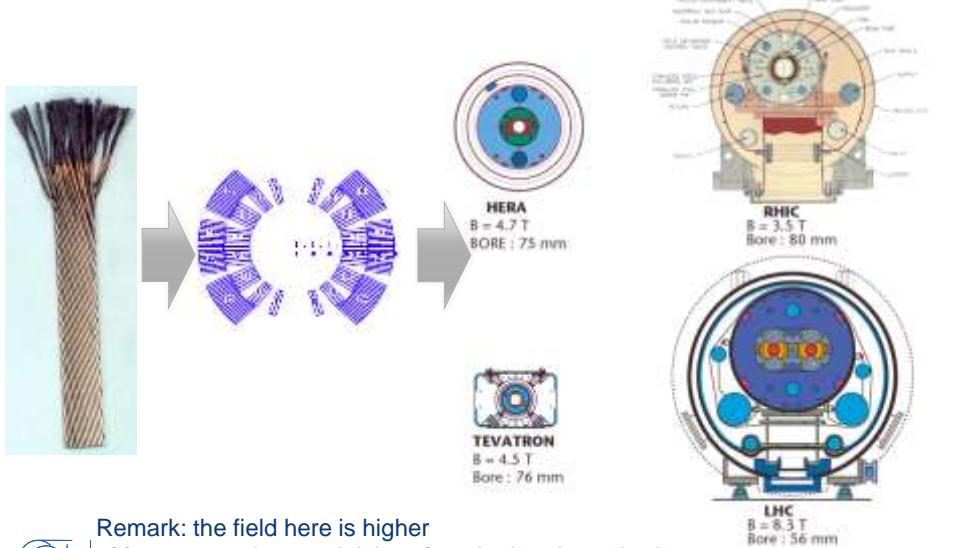
- The main reason why Rutherford cable succeeded where others failed was that it could be compacted to a high density (88 - 94%) without damaging the wires. Furthermore it can be rolled to a good dimensional accuracy (~ 10mm).
- Note the 'keystone angle', which enables the cables to be stacked closely round a circular aperture

## SUPERCONDUCTING MAGNETS



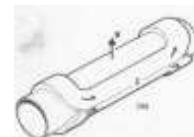
# How we can use the SC cable ?

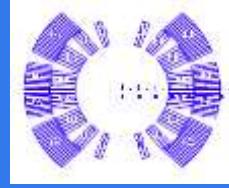
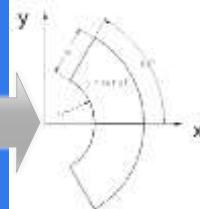
## DIPOLE MAGNETS



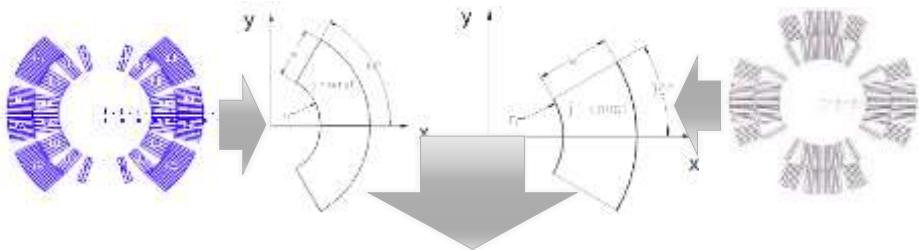
Remark: the field here is higher  
of ferromagnetic material therefore the iron is pushed out  
where the field is lower and closes the flux lines

## GENERATION OF MAGNETIC FIELDS: FIELD OF A WINDING

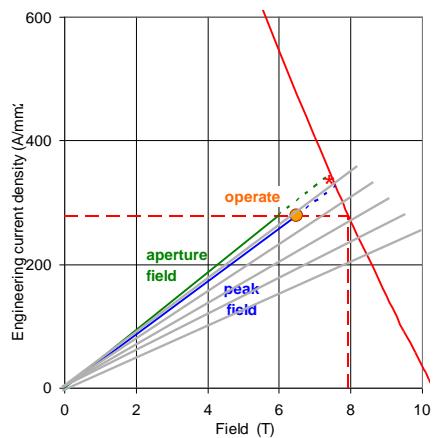
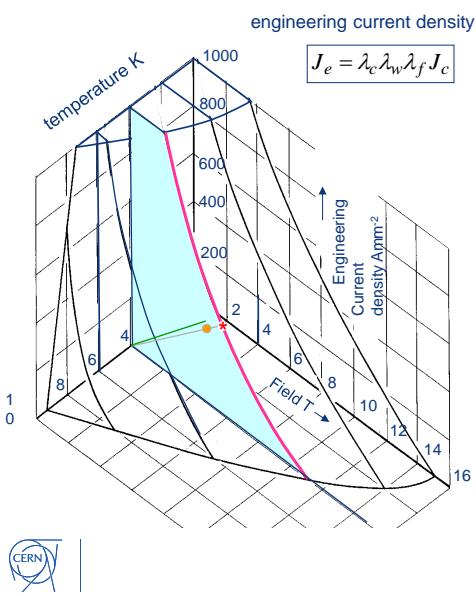


		$ B  = \frac{I\mu_0}{2\pi\rho}$ $I \rightarrow j\rho d\rho d\theta$	$B = -4 \frac{j\mu_0}{2\pi} \int_0^{r+w} \int_0^{\alpha} \frac{\cos\theta}{\rho} \rho d\rho d\theta = -\frac{2j\mu_0}{\pi} w \sin\alpha$	<b><math>B \propto</math> current density</b> <b><math>B \propto</math> coil width <math>w</math></b> <b><math>B</math> is independent of the aperture <math>r</math></b>
		$ B  = \frac{I\mu_0}{2\pi\rho}$ $I \rightarrow j\rho d\rho d\theta$	$G \propto \int_r^{r+w} \int_0^{\alpha} \frac{\rho d\rho d\theta}{\rho^2 e^{-2\rho}} \propto \sin(2\alpha) \log\left(1 + \frac{w}{r}\right)$ $G = j\gamma_0 \log\left(1 + \frac{w}{r}\right)$	<b><math>G \propto</math> current density</b> <b><math>G \propto</math> coil width <math>w</math></b> <b><math>G</math> is inversely proportional of the aperture <math>r</math></b>

# Approximate expression of the field

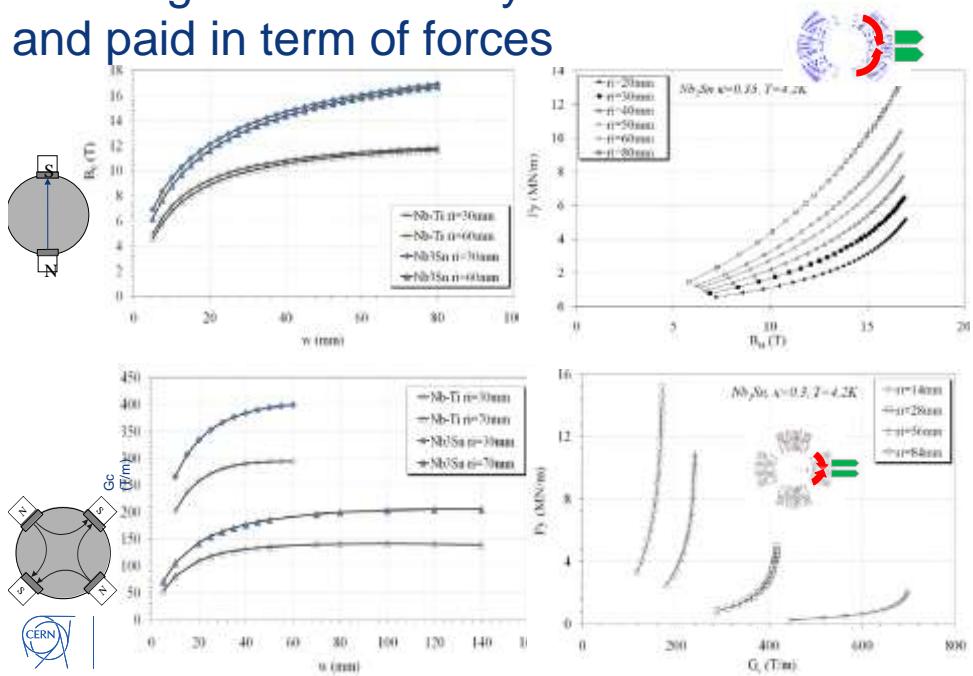


$\begin{aligned} & \text{In the aperture} \\ & \left\{ \begin{array}{l} B_r \\ B_\varphi \end{array} \right\} = -\frac{j\mu_0}{\pi} \left\{ ((r_i + w) - r_i) 2 \sin \alpha_0 \begin{pmatrix} \sin \varphi \\ \cos \varphi \end{pmatrix} \right\} \\ & \text{Outside the coil} \\ & \left\{ \begin{array}{l} B_r \\ B_\varphi \end{array} \right\} = -\frac{j\mu_0}{\pi} \left\{ \frac{(r_i + w)^3 - r_i^3}{3r^2} 2 \sin \alpha_0 \begin{pmatrix} \sin \varphi \\ \cos \varphi \end{pmatrix} \right\} \\ & \text{In the coil} \\ & \left\{ \begin{array}{l} B_r \\ B_\varphi \end{array} \right\} = -\frac{j\mu_0}{\pi} \left\{ ((r_i + w) - r_i) + \frac{(r_i^3 - r_i^3)}{3r^2} \right\} 2 \sin \alpha_0 \begin{pmatrix} \sin \varphi \\ \cos \varphi \end{pmatrix} \end{aligned}$	$\begin{aligned} & \text{In the aperture} \\ & \left\{ \begin{array}{l} B_r \\ B_\varphi \end{array} \right\} = -\frac{j\mu_0}{\pi} \left\{ 4r \ln \left( \frac{(r_i + w)}{r_i} \right) 2 \sin(2\alpha_0) \begin{pmatrix} \sin 2\varphi \\ \cos 2\varphi \end{pmatrix} \right\} \\ & \text{Outside the coil} \\ & \left\{ \begin{array}{l} B_r \\ B_\varphi \end{array} \right\} = -\frac{j\mu_0}{\pi} \left\{ \frac{(r_i + w)^4 - r_i^4}{r^3} 2 \sin(2\alpha_0) \begin{pmatrix} \sin 2\varphi \\ \cos 2\varphi \end{pmatrix} \right\} \\ & \text{In the coil} \\ & \left\{ \begin{array}{l} B_r \\ B_\varphi \end{array} \right\} = -\frac{j\mu_0}{\pi} \left\{ \left[ 4r \ln \left( \frac{(r_i + w)}{r_i} \right) \right. \right. \\ & \quad \left. \left. + \frac{(r^4 - r_i^4)}{r^3} \right] 2 \sin(2\alpha_0) \begin{pmatrix} \sin 2\varphi \\ \cos 2\varphi \end{pmatrix} \right\} \end{aligned}$
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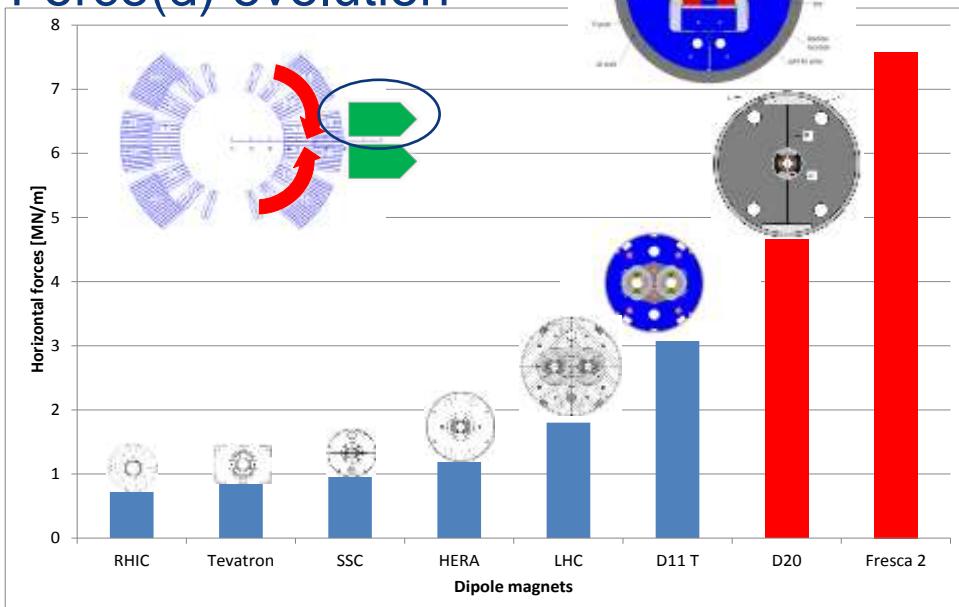


we expect the magnet to go  
resistive '**quench**' where the peak  
field load line crosses the critical  
current line \*  
usually back off from this extreme  
point and operate at ●

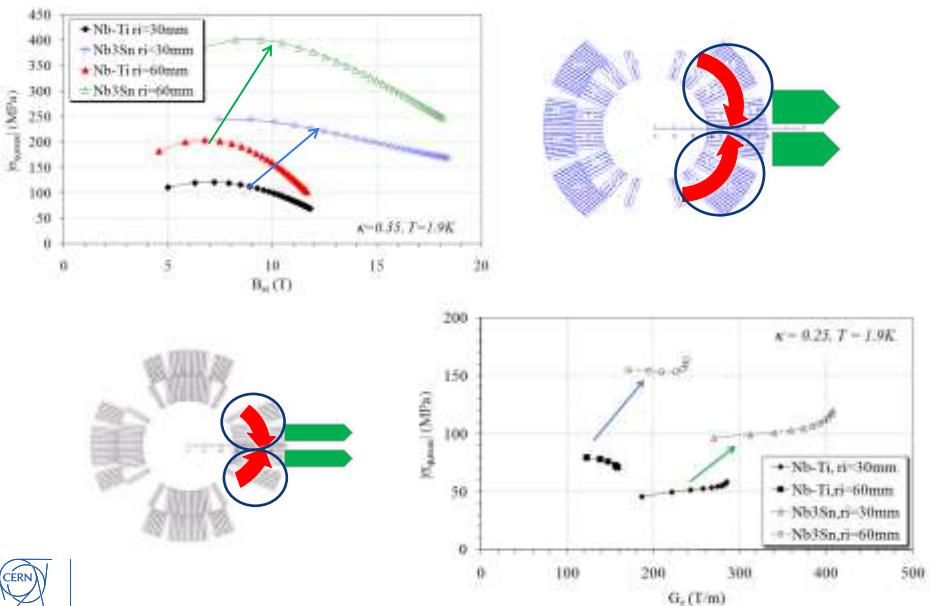
## Creating field: limited by the critical surface and paid in term of forces



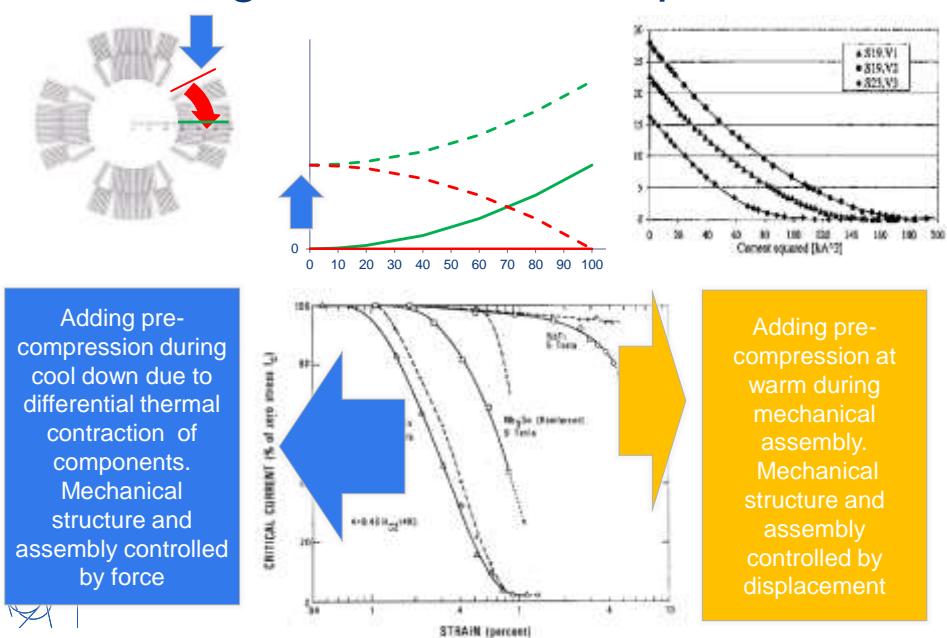
## Bending magnets: the Force(d) evolution

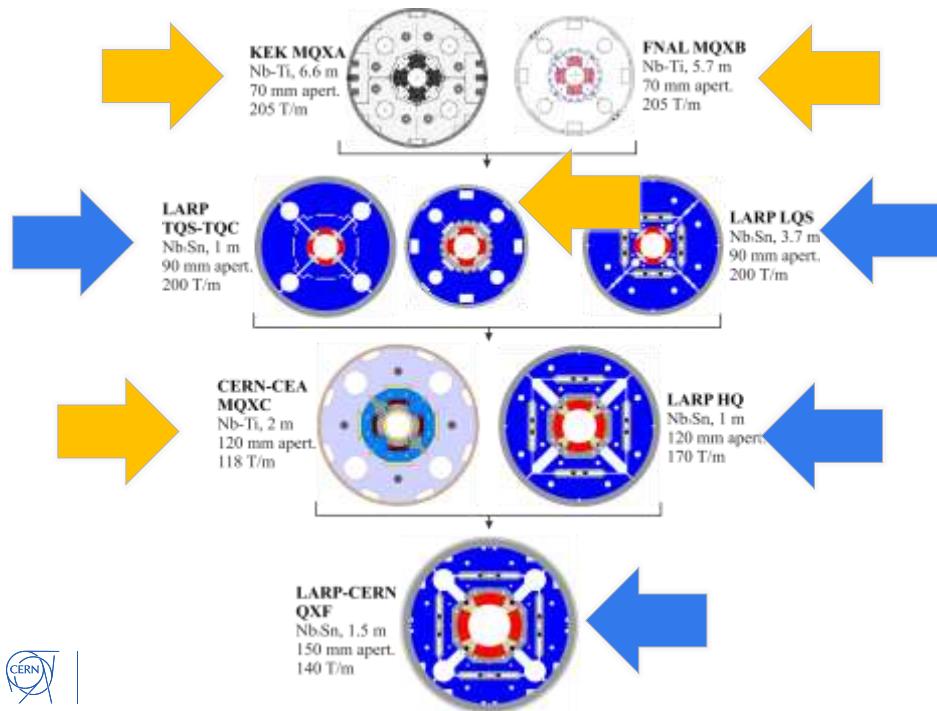


## And what about stresses ?



## Preventing coil movement: preload

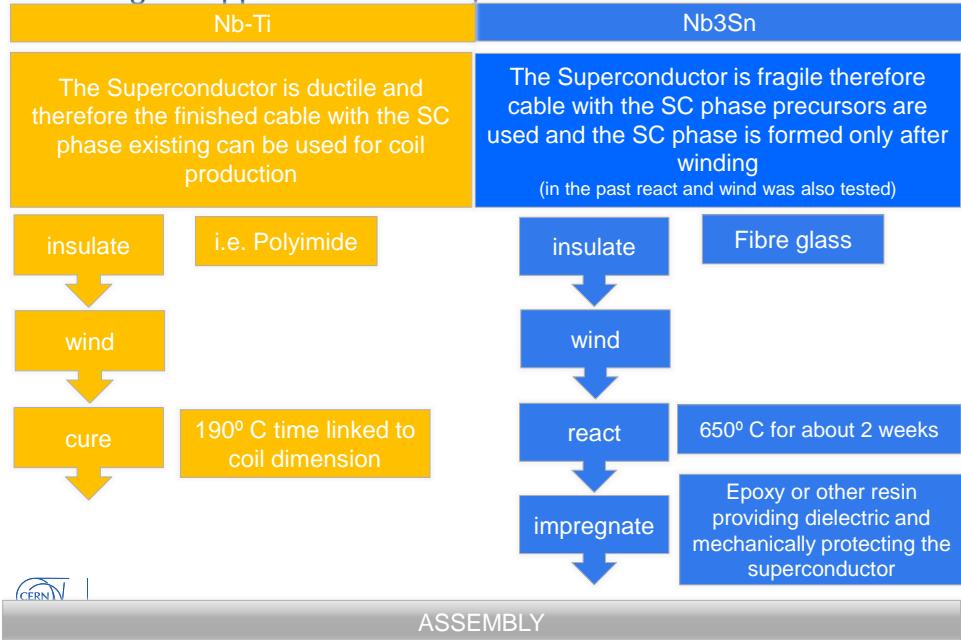




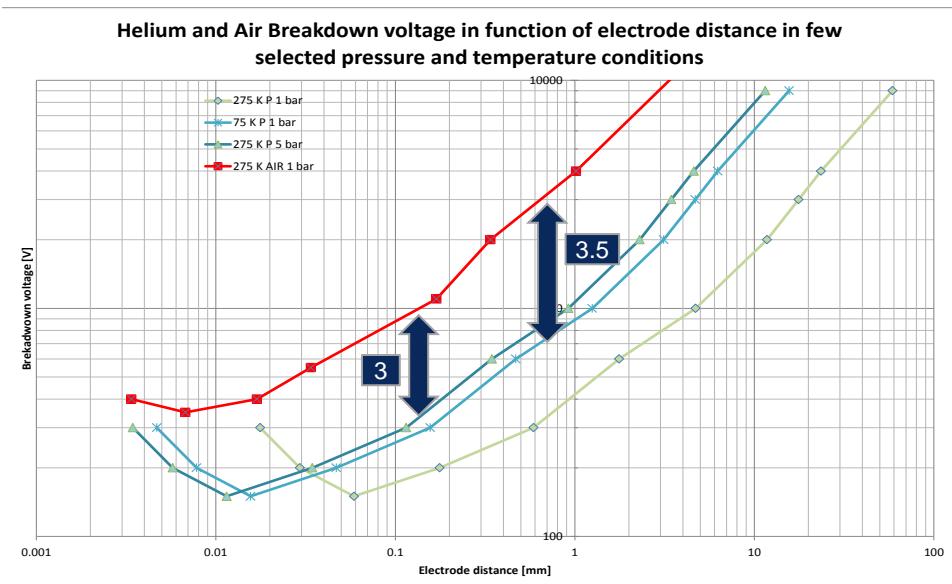
*Superconducting magnets an example of technological issue: the insulation*



## Stress sensitivity, different materials, new problems, new technological approaches to coil production



## The environment as dielectric



# The environment as dielectric

The liquid helium is a very good insulator, but the largest voltages in Sc devices appear during quench. Quench normally create local heating and therefore vaporization of He. Insulation design shall be performed therefore taking as reference gaseous helium

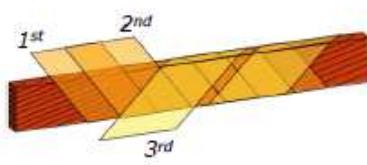
During component fabrication tests are performed in air. Therefore the test voltages shall be a large multiple (i.e. x 5) of the voltages to be withstood in gaseous helium condition



- Sc magnet insulation shall be
- 1) Capable of withstanding few thousands volts in gaseous helium
  - 2) Withstand high stress
  - 3) Working at cryogenic temperature
  - 4) As thin as possible to dilute as low as possible J
  - 5) Provide good heat transfer

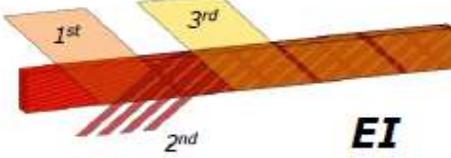
## Insulation for Nb-Ti

**MB**



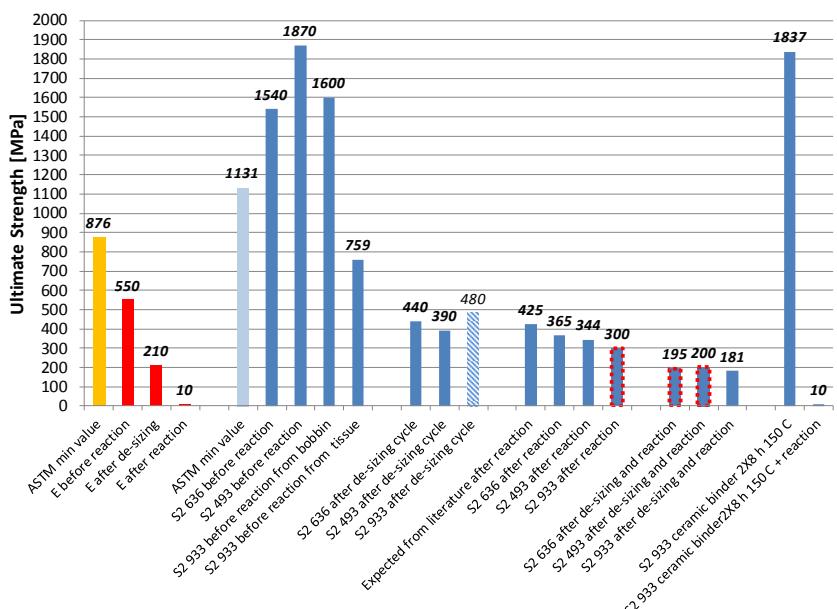
Enhanced insulation for improved heat transfer

**EI**



# Insulation for Nb<sub>3</sub>Sn magnets

- In Nb<sub>3</sub>Sn magnets, where cable are reacted at 600-700 °C, the most common insulation is a tape or sleeve of fiber-glass.
- Typically the insulation thickness varies between 70 and 200 µm.



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## *Superconducting magnets construction*



Example of assembly process: the LHC Nb-Ti main dipole



## Coil production I

	
Cable insulation	Coil winding I
	
Coil winding II	Preparation for curing

## Coil production and collaring

	
Curing press	Ready for collaring
	
Collaring press	Collared coils ready for cold mass assembly

## Cold mass assembly



Introducing collared coils in cold masses

Shell welding



Feet and alignment



Instrumentation completion



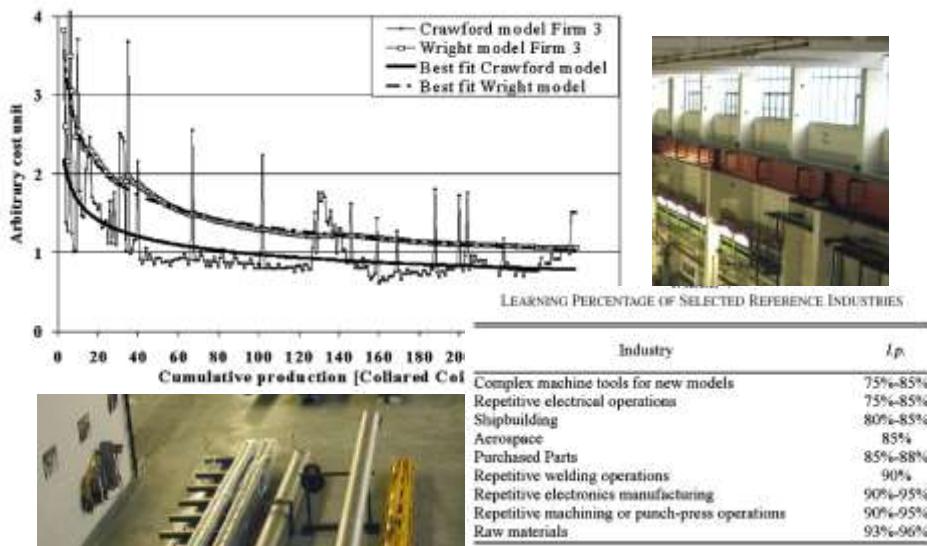


TABLE I  
LEARNING PERCENTAGE ACCORDING TO CRAWFORD AND WRIGHT MODELS  
COLLARED COILS PRODUCTION

Firm	Crawford Model	Wright Model
Firm 1	88%	83%
Firm 2	90%	86%
Firm 3	89%	82%

TABLE II  
LEARNING PERCENTAGE ACCORDING TO CRAWFORD AND WRIGHT MODELS  
COLD MASS PRODUCTION

Firm	Crawford Model	Wright Model
Firm 1	85%	81%
Firm 2	82%	81%
Firm 3	88%	82%

Thanks you for your attention





[www.cern.ch](http://www.cern.ch)