

Case 4 – Compact ERL for THz Radiation

- Goal: *Design a facility to provide high-rep THz radiation in the range of 1 to 20 THz with either single cycle emission or a bandwidth below 2%*

Results of group 8

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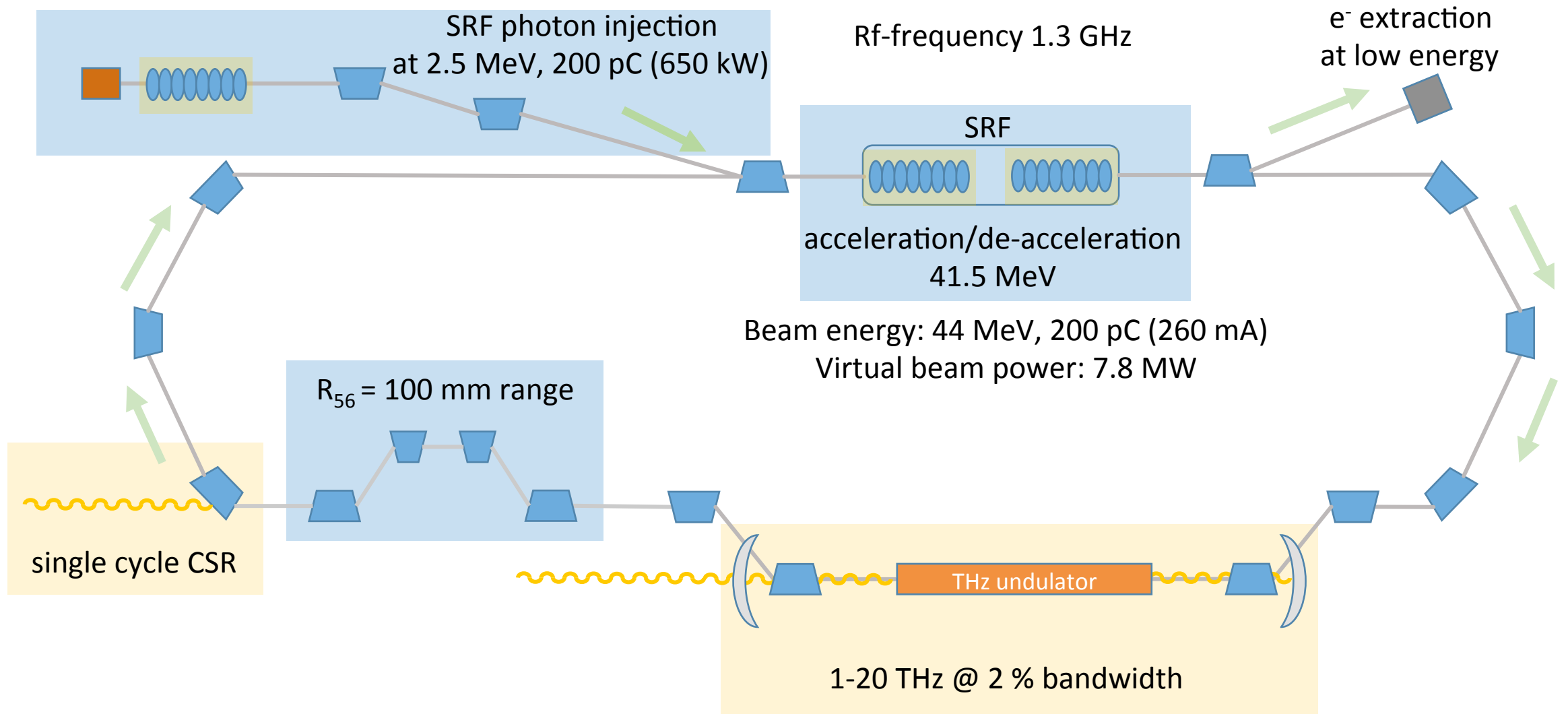
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General layout of the ERL THz facility



Design consideration for the FEL

- FEL for low bandwidth (2%)
- high gain FEL would require very short bunch length and peak current
 - low gain FEL oscillator → compact
 - fixed (ERL) beam energy and constrain on wavelength 1 – 20 THz
 - Use permanent magnet undulator with variable gap for wavelength tuning

$$\lambda_{FEL}(E, \lambda_u, K) = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} \right)$$

$$K = 93.6 B[T] \lambda_u[m]$$

- start with **K > 1**, **B** on axis < **1.0T**, reasonable dimensions of gap/undulator
- gap / vacuum chamber diameter > 30 mm (see next slide)

$$B_0 = 1.8 B_r \exp \left[-\pi \frac{gap}{\lambda_u} \right]$$

- -> $\lambda_u = 10$ cm

$$B_r = 1.4 \text{ T}$$

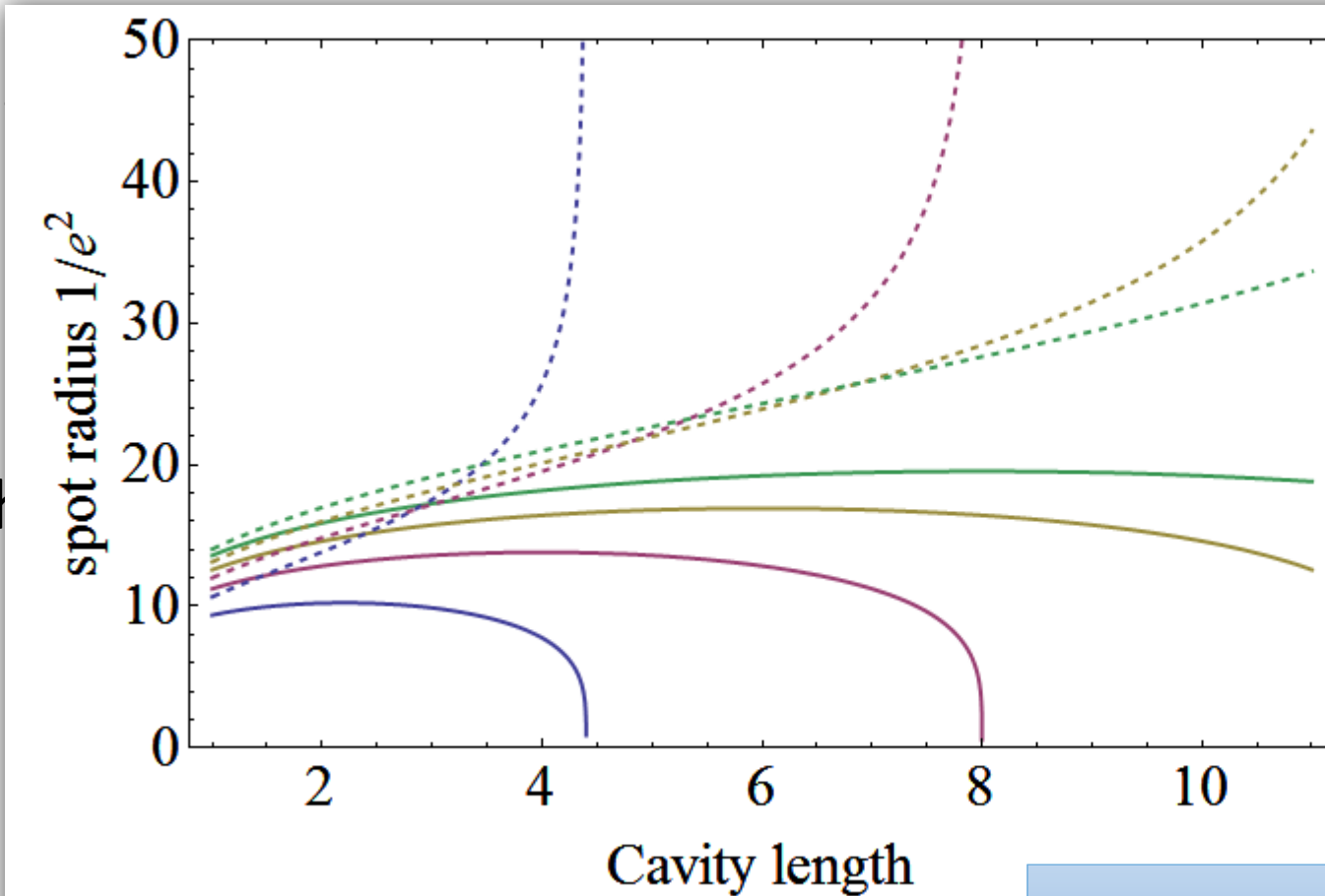
Design consideration for the FEL

• Re

• W

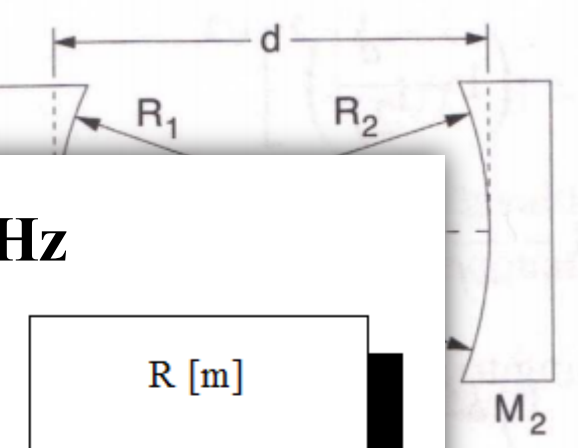
At waist:

At mirror:



$$\pi \sqrt{g_1(1 - g_1g_2)}$$

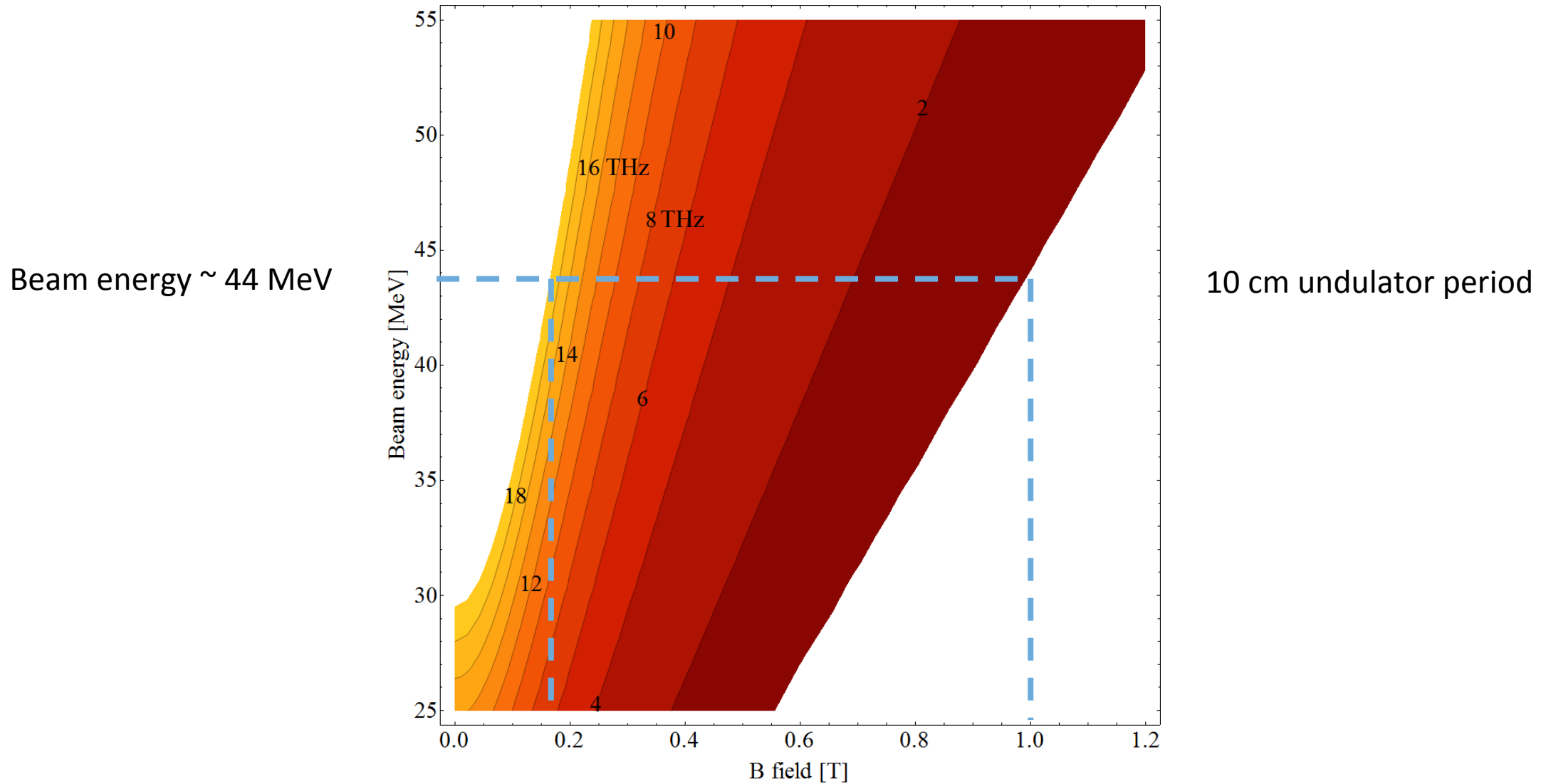
1 THz



R [m]	
---	2.2
---	4.0
---	6.0
---	8.0

Determines minimum gap of undulator

Tuning range and undulator give beam energy



Estimate on FEL peak power

Gain per turn:

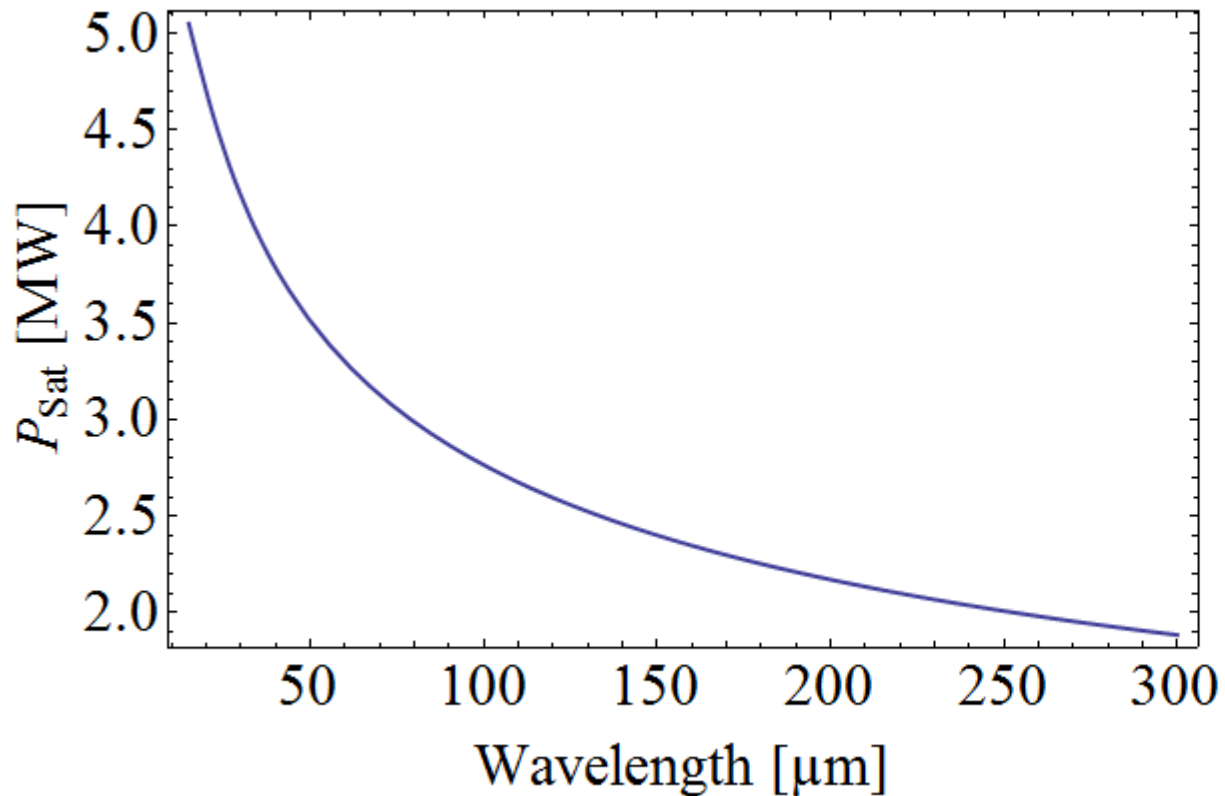
$$G_0 = \frac{(4\pi\rho N_u)^3}{\pi}$$

Saturation power:

$$P_{sat} = P_0(1 + G_{net})^m$$

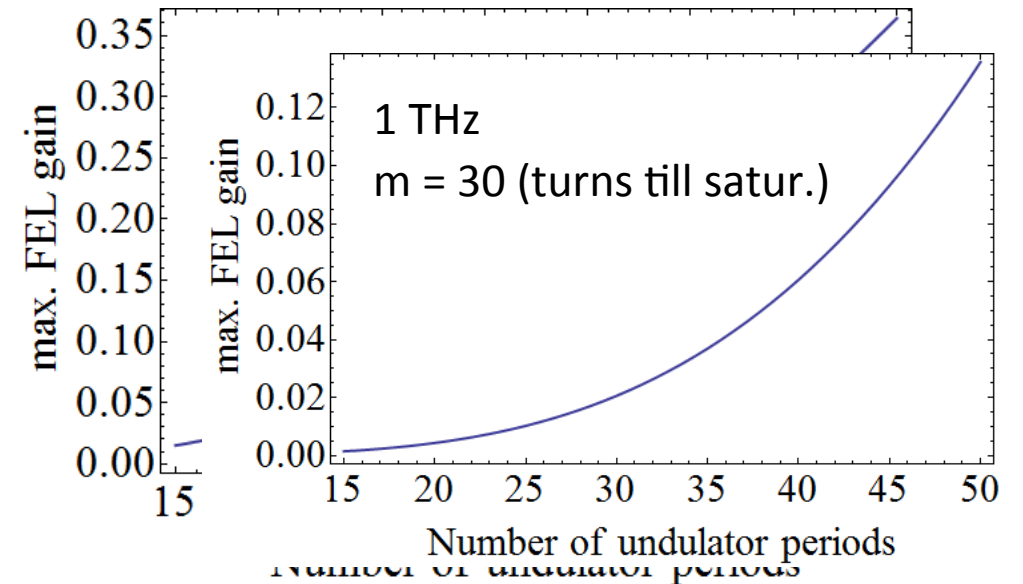
$$G_{net} = G_{max} - G_{loss}$$

$$G_{max} = 0.85G_0 \cdot F + 0.19(G_0 \cdot F)^2$$



Single pulse energy: **48 – 118 μJ**

Optical beam power: **150 kW**



Length of cavity is 6m

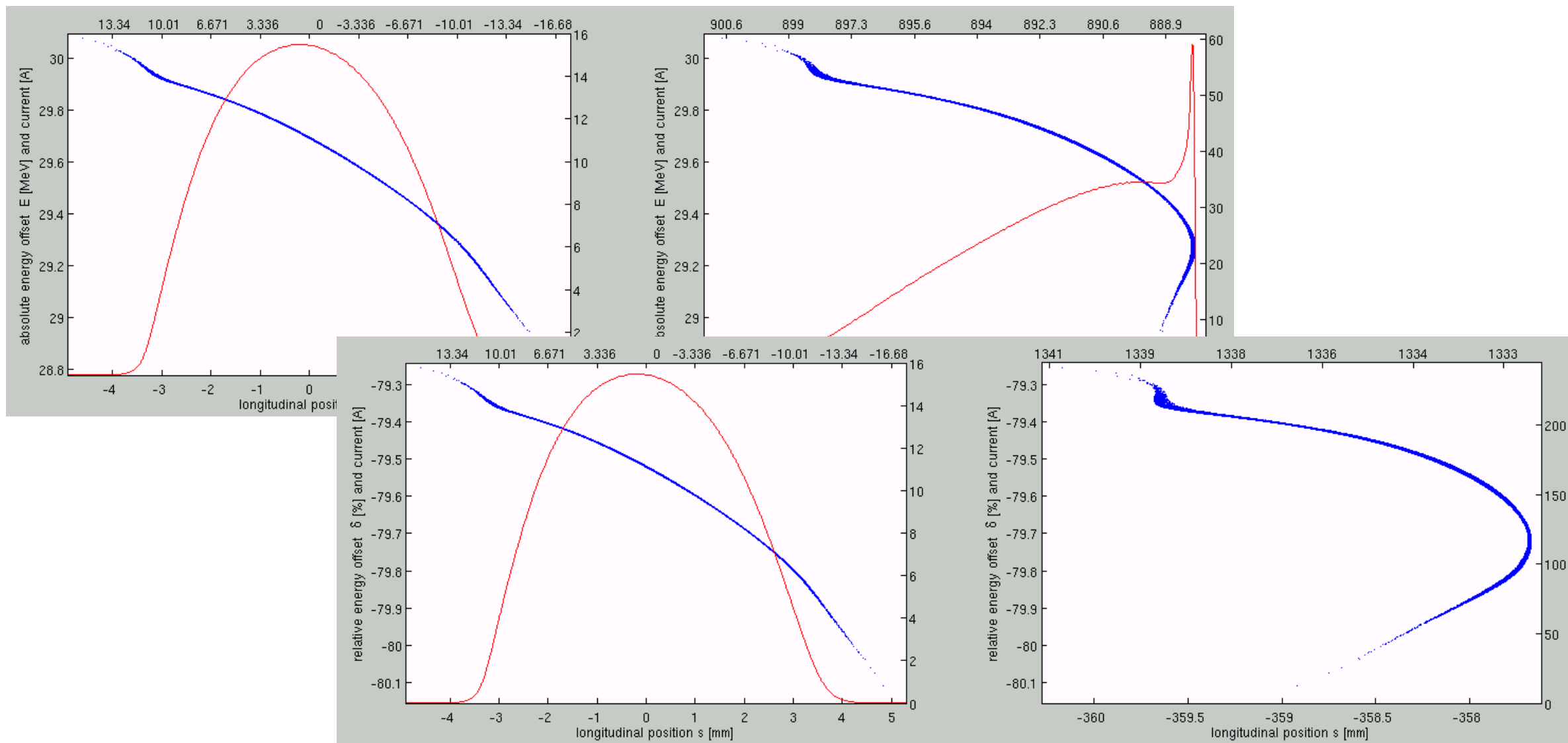
Compression

- initial bunch length 20 ps (needed for FEL oscillator)
 - final bunch length to get reasonable CSR in THz needs 0.5 ps
 - this gives a compression factor of 40 which is challenging using a single compression stage
 - other alternatives to get a short radiating pulse: foil, corrugated structure... not possible with ERL design
- ➔ use non linear compression schema – use “spike mode”

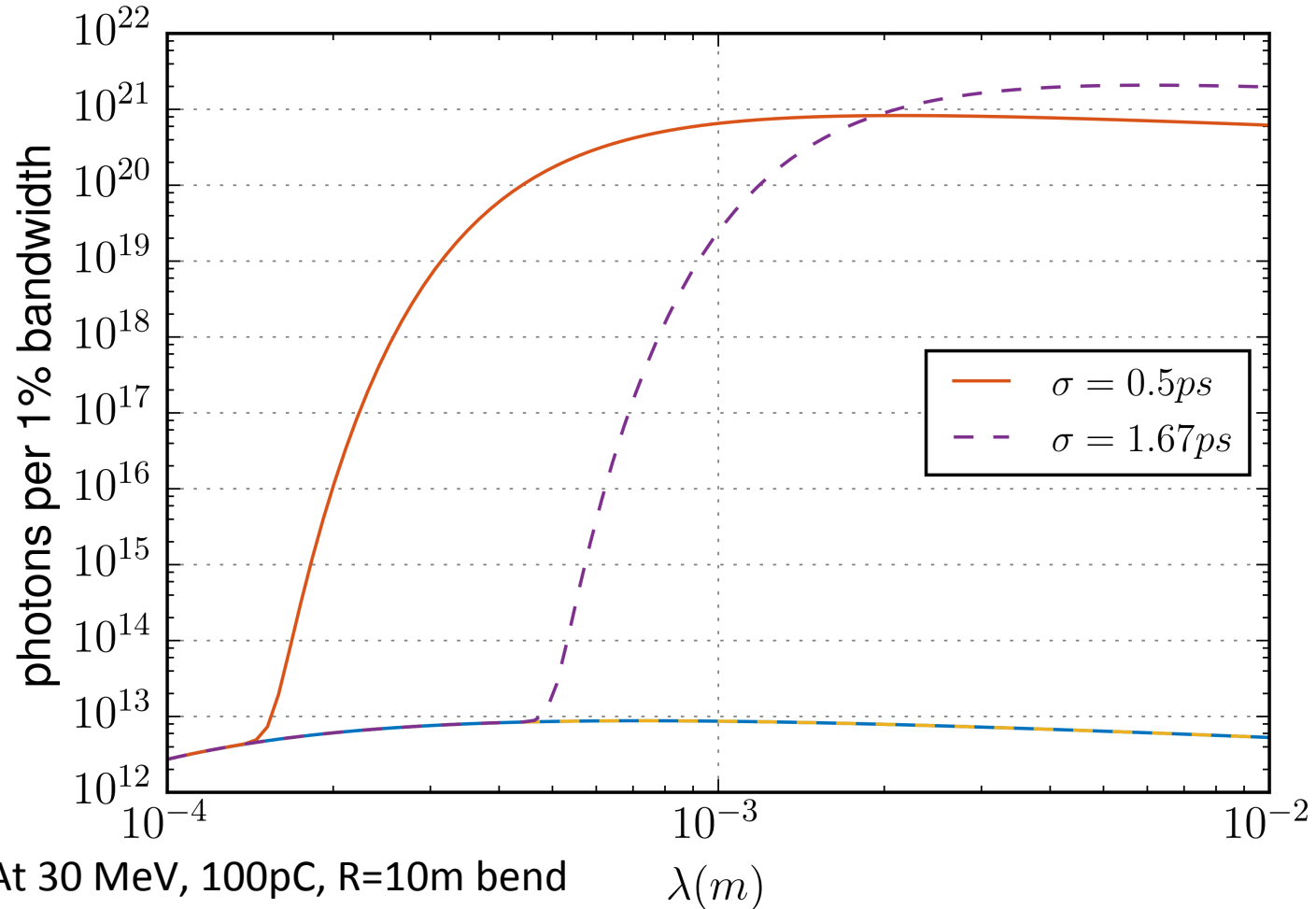
$$E(s) = E_0 + eV_{RF} \cos(ks + \varphi_{RF}) = E_0 + eV_{RF} [\cos(\varphi_{RF}) - k \sin(\varphi_{RF})s - k^2 \cos(\varphi_{RF}) s^2 + \dots]$$

$$s_f = s_i + \frac{R_{56}}{E_0} (-keV_{RF} \sin(\varphi_{RF}) s_i - k^2 eV_{RF} \cos(\varphi_{RF}) s_i^2)$$

Compression



single cycle CSR



Incoherent synchrotron radiation flux

$$\frac{d\dot{N}_{\text{ph}}}{d\psi} = \frac{4\alpha}{9} \gamma \frac{I}{e} \frac{\Delta\omega}{\omega} S\left(\frac{\omega}{\omega_c}\right)$$

$$S\left(\frac{\omega}{\omega_c}\right) = \frac{9\sqrt{3}}{8\pi} \frac{\omega}{\omega_c} \int_{\omega/\omega_c}^{\infty} K_{5/3}(\bar{x}) d\bar{x}$$

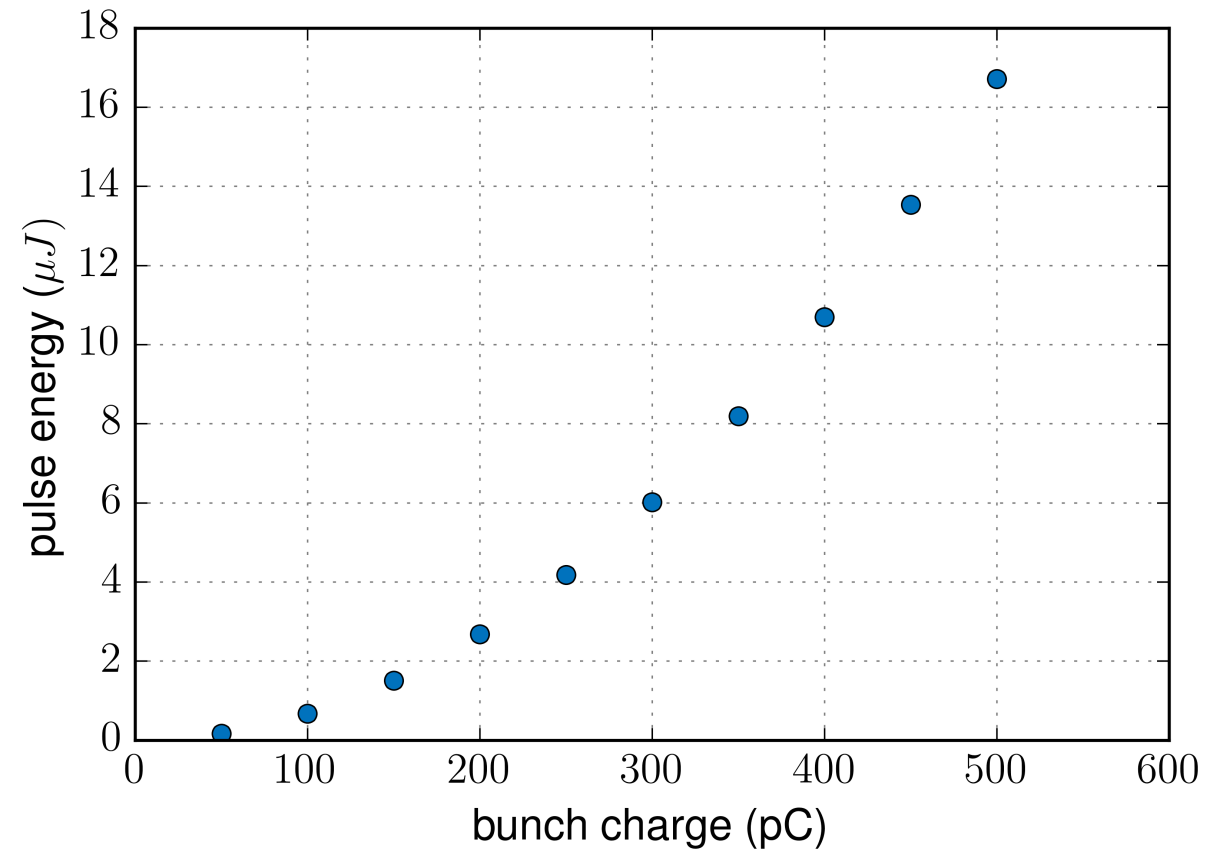
Wiedemann

Coherent radiation governed by form factor

$$g_{\lambda} = \left| \int n(z) e^{2\pi i z/\lambda} dz \right|^2$$

$$P_{\text{coh}} = N^2 e g_{\lambda} P_{\text{inc}}$$

single cycle CSR



Summary of determined parameters

- Machine parameters:
 - 260 mA average beam current
 - 200 pC @ 1.3 GHz
 - 20 ps bunch length (uncompressed down to 500 fs compressed)
 - Beam energy 44 MeV
- Undulator parameters:
 - gap 30 mm, 10 cm undulator period
 - $B = 0.16 \dots 1.0$ T ($K = 1.5 \dots 9.3$)