

## Landau Damping part 2

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Incomplete (!) mechanism of Landau Damping in beams for the end of the first part



Main ingredients of Landau damping:

- ✓ wave-particle collisionless interaction: Impedance driving field
- $\checkmark$  energy transfer: the wave  $\leftrightarrow$  the (few) resonant particles

#### **Existence of Landau damping**

In any accelerator, there are many Re(Z) sources

In any beam, there are many unsuppressed eigenmodes

$${
m Im}(\Delta Q_{
m coh}) = rac{\lambda_0 r_p}{\gamma Q_0} rac{{
m Re}(Z^\perp)}{Z_0/R}$$

driving dipole impedance here

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Still, the beams are often stable without an active mitigation

There must be a fundamental damping mechanism in beams

#### **Existence of Landau damping**

Additionally to Re(Z), deliberate excitation is often applied (tune measurements, optics control, ...)

Energy is directly transferred to the beam, mostly at the beam resonant frequencies



Tune measurements at PS, kick every 10 ms, M.Gasior, et al, CERN

The beams are stable and absorb some energy

#### There must be a fundamental damping mechanism in beams



Basic consideration of a collective mode stability

$$\Delta \Omega = \Delta \Omega_{\text{Re}} + i \gamma_{\text{drive}} + i \gamma_{\text{damping}}$$

$$\text{change the parameters and}_{\text{the source of the}_{\text{driving mechanism}}}$$

$$\text{use and enhance the}_{\text{intrinsic damping}_{\text{mechanism}}}$$

$$\frac{\gamma_{\text{drive}} + \gamma_{\text{damping}} > 0 \quad \text{Instability}}{\gamma_{\text{drive}} + \gamma_{\text{damping}} < 0 \quad \text{Stabilized mode}}$$

$$\frac{\gamma_{\text{drive}} > 0 \quad \text{Driven (unsuppressed) mode}}{\gamma_{\text{drive}} < 0 \quad \text{Mode suppressed by its drive}}$$



# Another Leading Actor: <u>Decoherence</u>

K.Y.Ng, Physics of Intensity Dependent Beam Instabilities, 2006 A.Hofmann, Proc. CAS 2003, CERN-2006-002 A.Chao, Phys. Coll. Beam Instab. in High Energy Acc. 1993 A.W. Chao, et al, SSC-N-360 (1987)



#### Decoherence

#### Collective beam oscillations after a short (one turn or shorter) kick

- Usually the beam displacement is comparable to the beam size
- In reality, signals can be very complicated
- A common diagnostics
- Decoherence is a process affected by many effects and mechanisms

#### A bunched beam Ar<sup>18+</sup> in SIS18. Transverse signal after a kick



#### V.Kornilov, O.Boine-F., PRSTAB 15, 114201 (2012)

#### **Pulse Response**



8 particles with different frequencies

Betatron oscillations: frequency spread

 $\delta \omega = Q_0 \xi \omega_0 \delta_p$ 

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$$egin{aligned} g(t) &= rac{\langle x(t) 
angle}{x_0} \ g(t) &= \int f(\omega) \cos(\omega t) d\omega \ g(t) &= ext{Fourier}^{-1} ig\{ R(\omega) ig\} &= rac{1}{2\pi} \int R(\omega) e^{-i\omega t} d\omega \end{aligned}$$

The Pulse Response is the Fourier image of BTF

## Phase-Mixing (Filamentation)

#### Phase-mixing of non-correlated particles with a tune spread



## Phase-Mixing, Coasting Beam



#### Phase-Mixing, Bunched Beam

Due to the particle synchrotron motion, the initial positions return after a synchrotron period

$$A(N) = A_0 \expigg\{-2ig(rac{\xi Q_0 \delta_p}{Q_{
m s}} \sin(\pi Q_{
m s} N)ig)^2igg\}$$



In reality, the decoherence is very different (other effects)

#### Decoherence



K.Y.Ng, Physics of Intensity Dependent Beam Instabilities, 2006 A.Hofmann, Proc. CAS 2003, CERN-2006-002 A.W. Chao, et al, SSC-N-360 (1987) V.Kornilov, O.Boine-F., PRSTAB 15, 114201 (2012) I.Karpov, V.Kornilov, O.Boine-F., PRAB 19, 124201 (2016)

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Vladimir Kornilov, CAS, June 9-21, 2019, Denmark

#### Decoherence





# Landau Damping: the wave & the tune spread





#### Loss of Landau damping due to coherent tune shift





#### Loss of Landau damping due to space-charge





#### Loss of Landau damping due to space-charge

Coherent dipole oscillations of four O<sup>8+</sup> bunches in the SIS18 of GSI Darmstadt at the injection energy 11.4 MeV/u

O.Boine-F., T.Shukla, PRSTAB **8**, 034201 (2005)





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#### Remark 1

Some analytical models or simulations predict Landau **antidamping**: unstable oscillations for zero or negative impedance

No antidamping for Gaussian-like distributions!



Vladimir Kornilov, CAS, June 9-21, 2019, Denmark

Remark 2

Head-tail modes in bunches:

- there is a tune spread (due to chromaticity ξ)
- the coherent frequency overlaps with the incoherent spectrum

still, there is NO Landau Damping!



#### a tune spread does not automatically means Landau Damping

## Landau Damping of 1<sup>st</sup> Type



Main ingredients of Landau damping:

- ✓ wave-particle collisionless interaction: Impedance driving field
- $\checkmark$  energy transfer: the wave  $\leftrightarrow$  the (few) resonant particles



#### Landau Damping: "Immune System"



#### Permanent process of keeping the beams stable



Different situation from  $\xi+\delta p$ : Tune spread due to amplitude-dependent tune shifts

For example, an octupole magnet:

$$egin{array}{rcl} B_x &=& O_3(3x^2y-y^3)\ B_y &=& O_3(x^3-3xy^2) \end{array}$$

First-order frequency shift of the anharmonic oscillations

$$\ddot{x}+\omega_0^2 x=arepsilon x^3 \ \omegapprox\omega_0-rac{3}{8}rac{arepsilon A^2}{\omega_0}$$

Amplitude-dependent betatron tune shifts



Thus, octupoles provide an ingredient for Landau damping: <u>tune spread</u>

Tune footprint due to octupoles for a Gaussian bunch

Color: the distribution density (norm. units)



#### Decoherence

Phase-Mixing is very different from the chromaticity case

- No recoherence
- Kick amplitude dependent
- Analytical model for:

$$egin{aligned} Q(a) &= Q_0 - \mu igg( rac{a}{\sigma_x} igg)^2 \ A(N) &= rac{A_0}{1+ heta^2} \expigg\{ -rac{A_0^2}{2\sigma_x^2} rac{ heta^2}{1+ heta^2}igg\} \ heta &= 2\pi\mu \; N \end{aligned}$$

A.W. Chao, et al, SSC-N-360 (1987) V.Kornilov, O.Boine-F., PRSTAB 15, 114201 (2012) I.Karpov, V.Kornilov, O.Boine-F., PRAB 19, 124201 (2016)



#### Tune spread due to amplitude-dependent tune shifts

Amplitude-dependent betatron tune shifts in a lattice:

$$egin{aligned} \Delta Q_x^{ ext{oct}} &= ig(\int rac{K_3eta_x^2}{16\pi} ext{d}sig)J_x - ig(\int rac{K_3eta_xeta_y}{8\pi} ext{d}sig)J_y \ K_3 &= rac{6O_3}{B
ho} \ x(s) &= \sqrt{2J_xeta_x(s)}\cos(\phi_x) \end{aligned}$$

Every particle has a different amplitude  $(J_x, J_y)$  $\rightarrow$  tune spread  $\rightarrow$  Landau damping?

The resonant particles drift away in tune from the resonance as they get excited





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Particle excitation for amplitude-dependent tune shifts

![](_page_27_Figure_2.jpeg)

We already guess: the distribution slope (*df/da*) might be involved

The dispersion relation for coasting beam

$$\Delta Q_{
m coh} \int rac{1}{\Delta Q_{
m ex} - \Omega/\omega_0} J_x rac{\partial f}{\partial J_x} dJ_x dJ_y = 1$$

 $\Delta Q_{coh}$ : coherent no-damping tune shift imposed by an impedance  $\Delta Q_{ex}(J_w,J_v)$ : external (lattice) incoherent tune shifts

L.Laslett, V.Neil, A.Sessler, 1965 D.Möhl, H.Schönauer, 1974 J.Berg, F.Ruggiero, CERN SL-96-71 AP 1996

The resulting damping is a complicated 2D convolution of the distribution  $\{df(J_x, J_y)/dJ_x\}$  and tune shifts  $\Delta Q_{ext}(J_x, J_y)$ 

![](_page_29_Figure_1.jpeg)

Main ingredients of Landau damping:

- ✓ wave-particle collisionless interaction: Impedance driving field
- $\checkmark$  energy transfer: the wave  $\leftrightarrow$  the (few) resonant particles

#### An example of the application: Beam stability studies for FCC

![](_page_30_Figure_2.jpeg)

V.Kornilov, FCC Week 2017, Berlin

Drawback: octupoles, like other nonlinearities, can reduce Dynamic Aperture and Lifetime.

![](_page_31_Figure_2.jpeg)

#### **Amplitude-Dependent Detuning**

Another source of amplitude-dependent tune-shifts: Tune-spread due to Beam-Beam effects produces Landau Damping

![](_page_32_Figure_2.jpeg)

#### X.Buffat, et al, PRSTAB 17, 111002 (2014)

![](_page_33_Picture_0.jpeg)

# Landau Damping in Beams of 3<sup>rd</sup> type

![](_page_33_Picture_2.jpeg)

Vladimir Kornilov, CAS, June 9-21, 2019, Denmark

#### **Different situation:** Wave–Particel interaction is due to space-charge $\Omega_{coh}$ Space-charge tune shift 2 **Flectric field** ω<sub>inc</sub> 1.5 $\Delta Q_{sc}$ / $\Delta Q_{KV}$ of the self-field tune spread space charge 0.5 0 2 3 5 0 1 $a_x / \sigma_x$

For the resonant particles Q<sub>inc</sub>≈Q<sub>coh</sub>, wave ↔ particles energy transfer should be possible

The dispersion relation

$$\int rac{\Delta Q_{
m coh} - \Delta Q_{
m sc}}{\Delta Q_{
m ex} + \Delta Q_{
m sc} - \Omega/\omega_0} J_x rac{\partial f}{\partial J_x} {
m d} J_x {
m d} J_y {
m d} p = 1$$

 $f(J_{x'}, J_{y'}, p)$   $\Delta Q_{coh} :$   $\Delta Q_{ex}(J_{x'}, J_{y'}, p) :$  $\Delta Q_{sc}(J_{x'}, J_{y'}) :$ 

no-damping coherent tune shift imposed external (lattice) incoherent tune shift space-charge tune shift

> L.Laslett, V.Neil, A.Sessler, 1965 D.Möhl, H.Schönauer, 1974

The resulting damping is a complicated 2D convolution of the distribution  $\{df(J_x, J_y)/dJ_x\}$  and tune shifts  $\Delta Q_{sc}(J_x, J_y), \Delta Q_{ext}(J_x, J_y)$ 

![](_page_36_Figure_0.jpeg)

E.Metral, F.Ruggiero, CERN-AB-2004-025 (2004) V.Korn

V.Kornilov, O.Boine-F, I.Hofmann, PRSTAB 11, 014201 (2008)

The dispersion relation

$$\int rac{\Delta Q_{
m coh} - \Delta Q_{
m sc}}{\Delta Q_{
m ex} + \Delta Q_{
m sc} - \Omega/\omega_0} J_x rac{\partial f}{\partial J_x} {
m d} J_x {
m d} J_y {
m d} p = 1$$

 $\Delta Q_{ex}$ =0: no pole, no damping!

Momentum conservation in a closed system

Even if Ω<sub>coh</sub> is inside the spectrum, and there are resonant particles Q<sub>inc</sub>≈Q<sub>coh</sub>, there is no Landau damping in coasting beams only due to space-charge LLaslett, V.Neil, A.Sessler, 1965 D.Möhl, H.Schönauer, 1974

V.Kornilov, O.Boine-F, I.Hofmann, PRSTAB 11, 014201 (2008)

A.Burov, V.Lebedev, PRSTAB 12, 034201 (2009)

#### Space Charge

#### Space charge is a beam-internal interaction

![](_page_38_Picture_2.jpeg)

#### Space Charge

![](_page_39_Picture_1.jpeg)

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#### Remark

Two examples:

- 1. Head-tail modes and the chromaticity tune-spread
- 2. Nonlinear space-charge in coasting beams
- there is a tune spread
- the coherent frequency overlaps the incoherent spectrum

still, there is **NO Landau Damping!** 

![](_page_40_Figure_8.jpeg)

a tune spread does not automatically means Landau Damping

![](_page_40_Picture_10.jpeg)

![](_page_41_Figure_1.jpeg)

Main ingredients of Landau damping:

- ✓ wave-particle collisionless interaction: *E*-field of Space-charge
- $\checkmark$  energy transfer: the wave  $\leftrightarrow$  the (few) resonant particles

M<sub>k</sub> (arb. units)

Landau damping in bunches

- There is damping due to only space charge
- Here: space-charge tune spread due to longitudinal bunch profile
- Additional spread due to transverse profile

A.Burov, PRSTAB 12, 044202 (2009) V.Balbekov, PRSTAB 12, 124402 (2009) V.Kornilov, O.Boine-F, PRSTAB 13, 114201 (2010)

![](_page_42_Figure_6.jpeg)

![](_page_42_Figure_7.jpeg)

Tune footprint due to space charge for a Gaussian bunch

Color: the distribution density (norm. units)

The role of space charge is still under study

![](_page_43_Figure_4.jpeg)

![](_page_43_Figure_5.jpeg)

#### Other concepts for Landau damping

![](_page_44_Figure_2.jpeg)

Electron lenses for Landau damping (V. Shiltsev et al, Phys Rev Lett 119, 134802, 2017)

RF Quadrupoles for Landau damping (M. Schenk et al, PRAB 20, 104402, 2017)

A new IOTA facility for more Landau damping (S. Antipov et al 2017 JINST 12 T03002)

#### Landau Damping in beams

- Waves: collective oscillations in a medium of particles
- Landau: Wave  $\leftrightarrow$  particles collisionless interaction
- **Dispersion relation and Stability Diagram**
- Decoherence is a result of Phase-Mixing, Landau damping, etc.
- Collective Frequency  $\leftrightarrow$  Tune Spread
- Different types of Landau damping (explanatory help here)  $\bullet$
- "Immune system" •
- A tune spread does not automatically means Landau damping
- A special role of space charge

![](_page_45_Picture_10.jpeg)