Accelerators for Newcomers

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Why this Introduction?

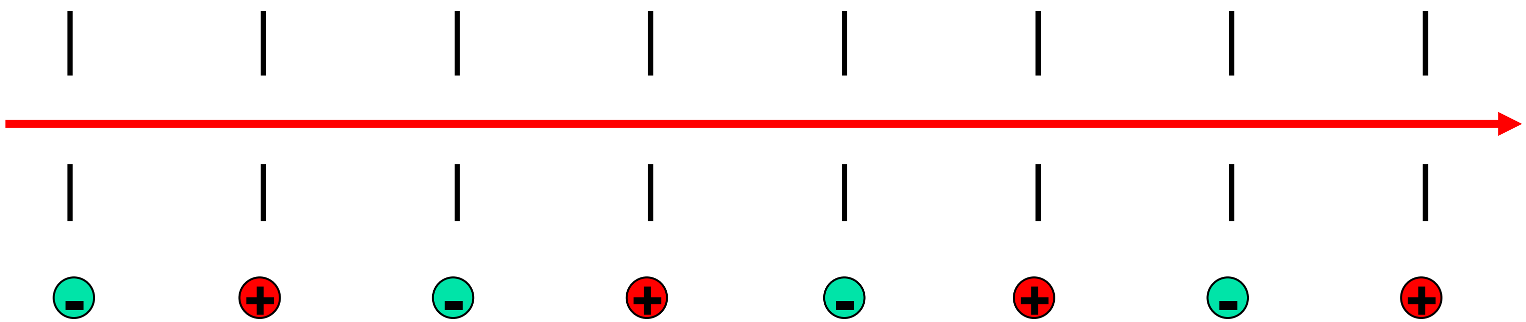
- During this school, you will learn about beam dynamics in a rigorous way…
- but some of you are completely new to the field of accelerator physics.
- It seemed therefore justified to start with the introduction of a few very basic concepts, which will be used throughout the course.

This is a completely intuitive approach (no mathematics) aimed at highlighting the physical concepts, without any attempt to achieve any scientific derivation.

What is a Particle Accelerator?

- a machine to accelerate some particles ! How is it done ?

- Many different possibilities (see following lectures), but rather easy from the general principle:



Beam Dynamics (1)

<u>In order to describe the motion of the particles, each particle is characterised by:</u>

- Its azimuthal position along the machine: s
- Its momentum: p
- Its horizontal position: x
- Its horizontal slope: x'
- Its vertical position: y
- Its vertical slope: y'

i.e. a sixth dimensional phase space

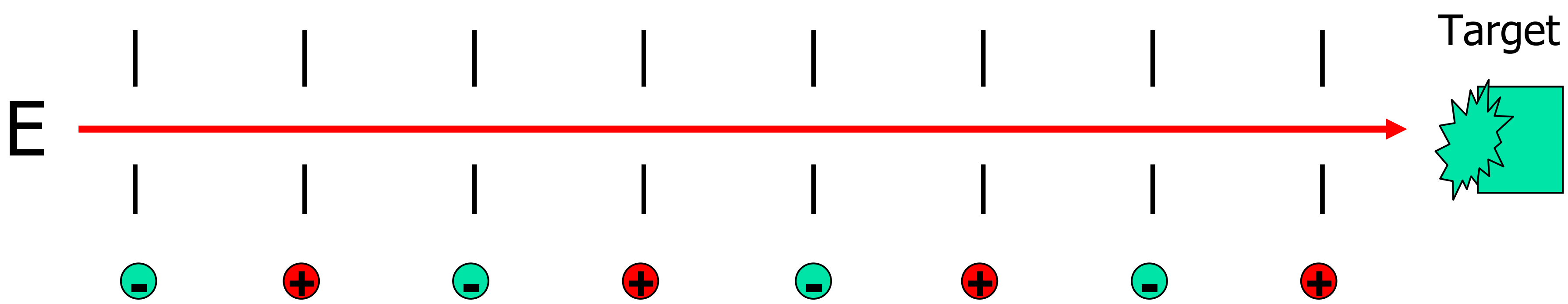
(s, p, x, x', y, y')

Beam Dynamics (2)

- In an accelerator designed to operate at the energy E_{nom}, all particles having $(s, E_{nom}, 0, 0, 0, 0)$ will happily fly through the center of the vacuum chamber without any problem. These are "ideal particles".

- The difficulties start when:
  - one introduces dipole magnets
  - the energy $E \neq E_{nom}$ or $(p-p_{nom}/p_{nom}) = \Delta p/p_{nom} \neq 0$
  - either of $x, x', y, y' \neq 0$

Ideal linear machines (linacs)



Available Energy : $E_{c.m.} = m\ .\ (2+2\gamma)^{1/2} = (2m.(m+E))^{1/2}$

with $\gamma = E/E_0$

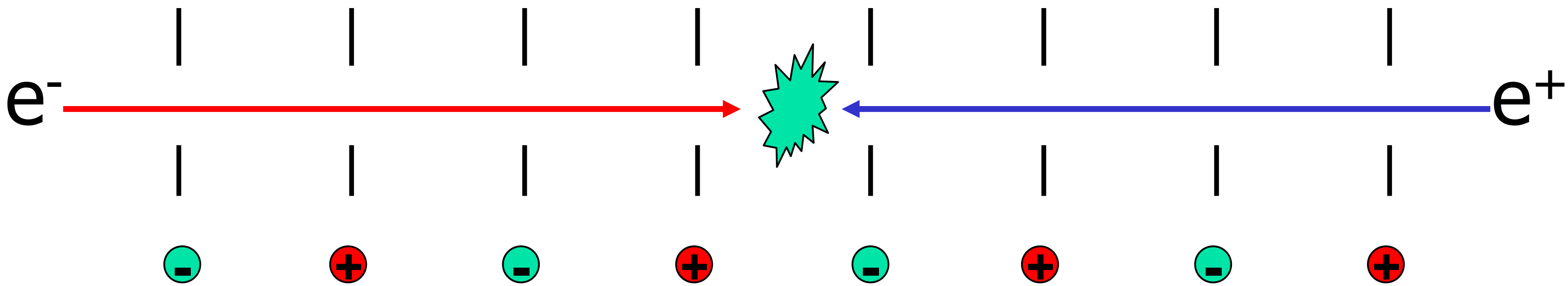
<u>Advantages</u>: Single pass

High intensity

<u>Drawbacks</u>: Single pass

Available Energy

Improved solution for $E_{c.m.}$



Available Energy : $E_{c.m.} = 2m\gamma = 2E$

with $\gamma = E/E_0$

Advantages: High intensity

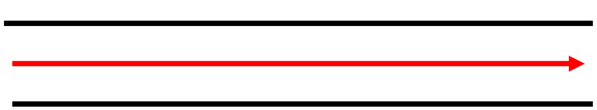
Drawbacks: Single pass

Space required

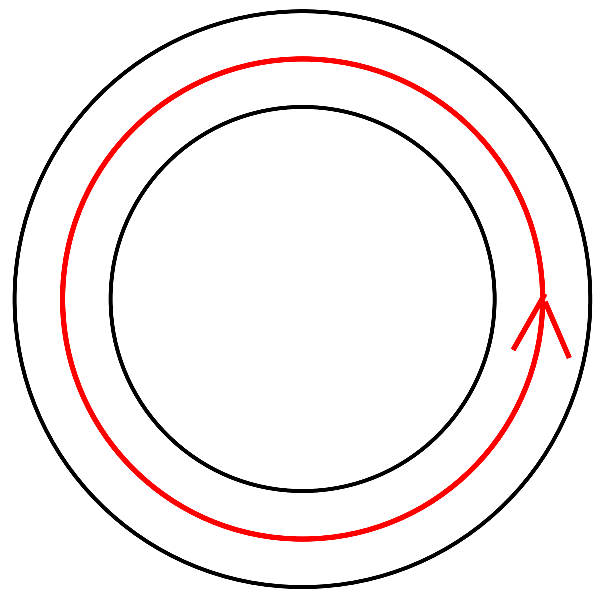
Keep particles: circular machines

Basic idea is to keep the particles in the machine for many turns.

Move from the linear design



To a circular one:

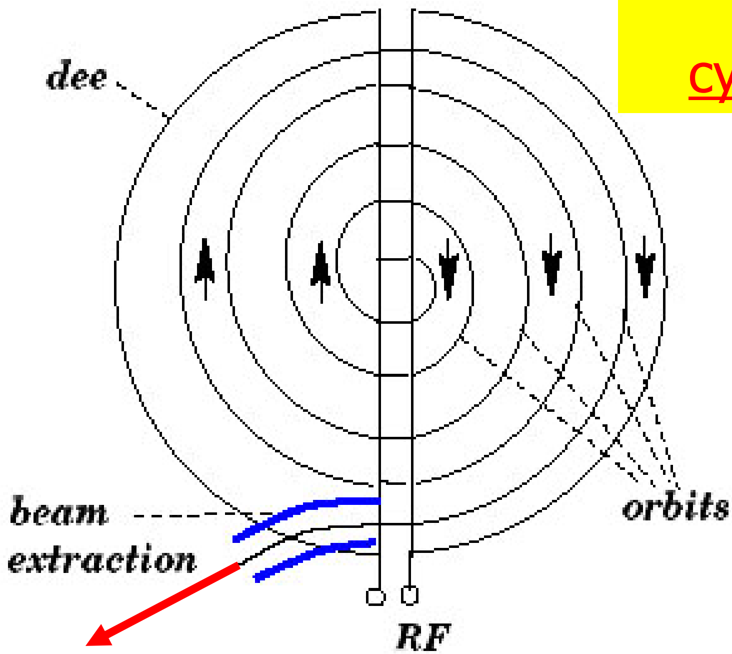


- Need Bending
- Need Dipoles!

Circular machines ($E_{c.m.} \sim (mE)^{1/2}$)

fixed target:

cyclotron



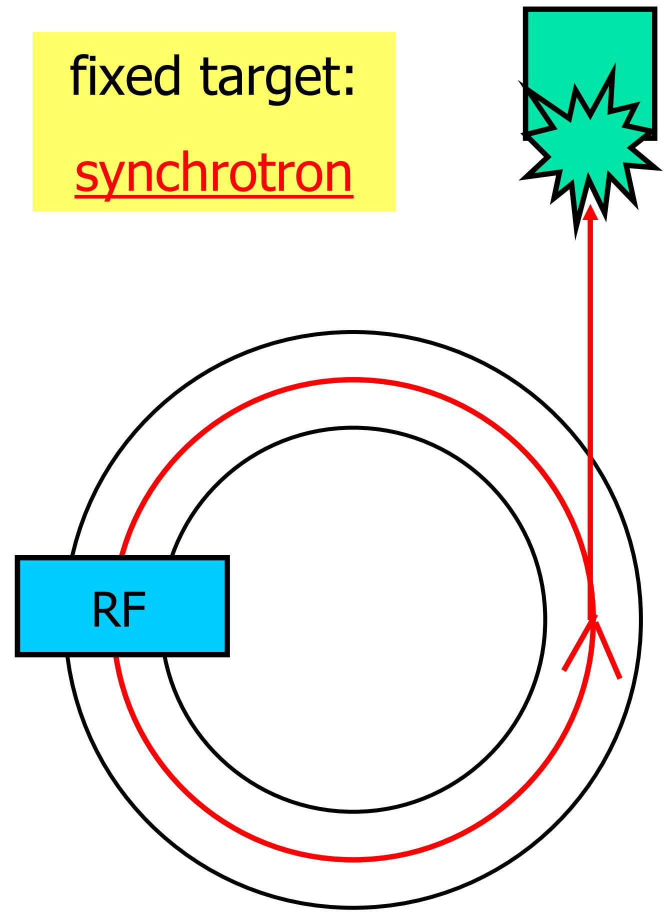
huge dipole, compact design,

B = constant

low energy, single pass.

fixed target:

synchrotron



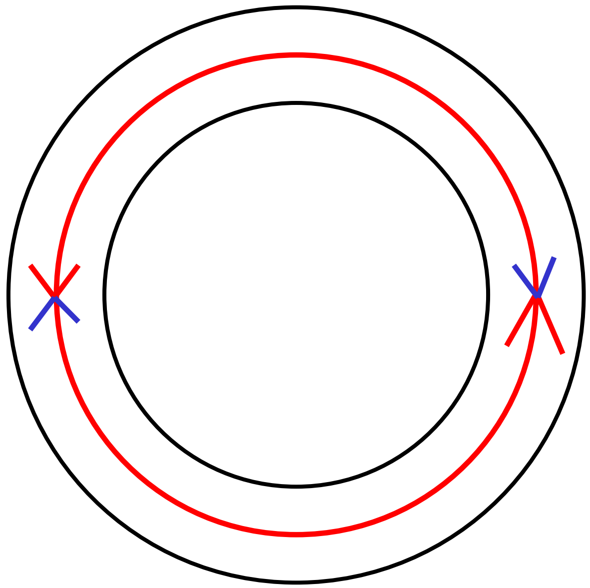
varying B, small magnets, high energy

Colliders ($E_{c.m.}$=2E)

<u>Colliders:</u>

electron – positron

proton - antiproton



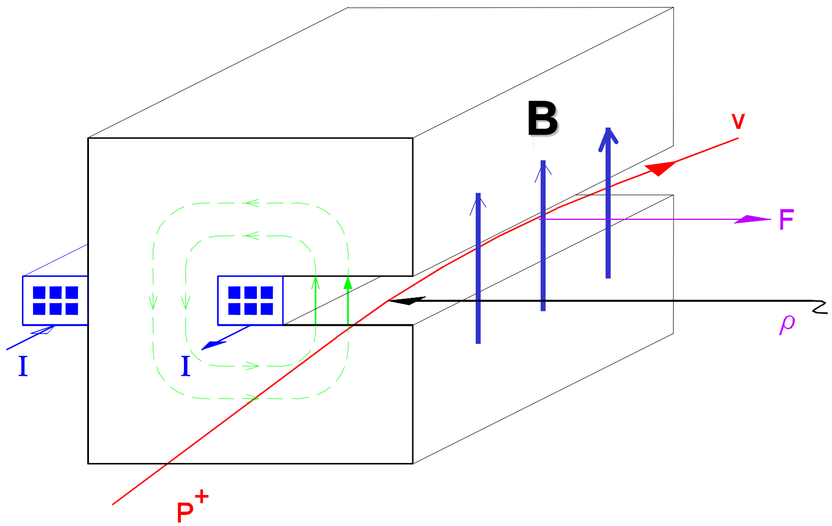
Colliders with the same type of particles (e.g. p-p) require two separate chambers. The beam are brought into a common chamber around the interaction regions

Ex: LHC

8 possible interaction regions

4 experiments collecting data

Circular machines: Dipoles



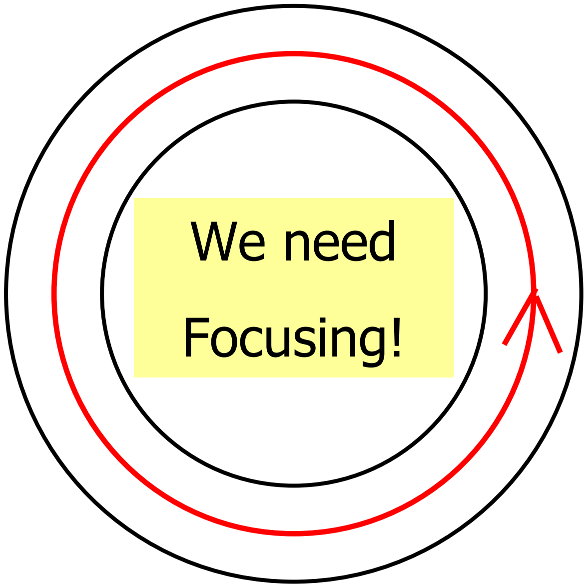
In the dipoles, the Lorentz force bends the trajectory of the particles.

This very simple picture will allow to derive one of the fundamental relation of beam dynamics !

Ideal circular machine:

- Neglecting radiation losses in the dipoles
- Neglecting gravitation

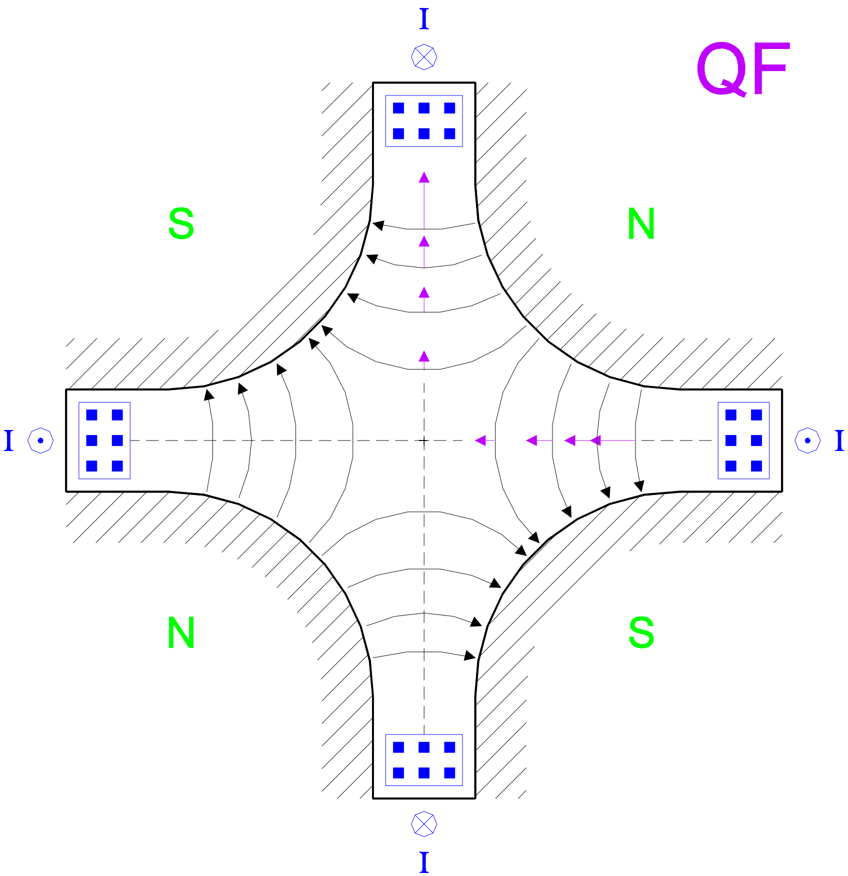
ideal particle would happily circulate on axis in the machine for ever!



Unfortunately: real life is different!

Gravitation: Δy = 20 mm in 64 msec!	
Alignment of the machine	Limited physical aperture
Ground motion	Field imperfections
Energy error of particles and/or $(x, x')_{inj} \neq (x, x')_{nominal}$	
Error in magnet strength (power supplies and calibration)	

Focusing with quadrupoles



$$F_x = -g.x$$

$$F_y = g.y$$

Force increases linearly with displacement.

Unfortunately, effect is opposite in the two planes (H and V).

Remember: this quadrupole is focusing in the horizontal plane but defocusing in the vertical plane!

Focusing properties …

A quadrupole provides the required effect in one plane…

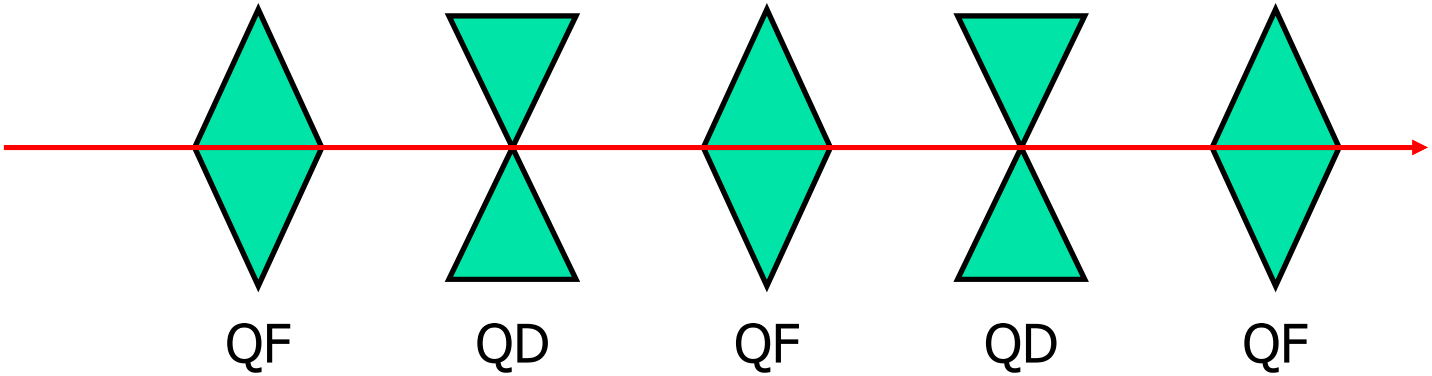
but the opposite effect in the other plane!

Is it really interesting ?

Alternating gradient focusing

Basic new idea:

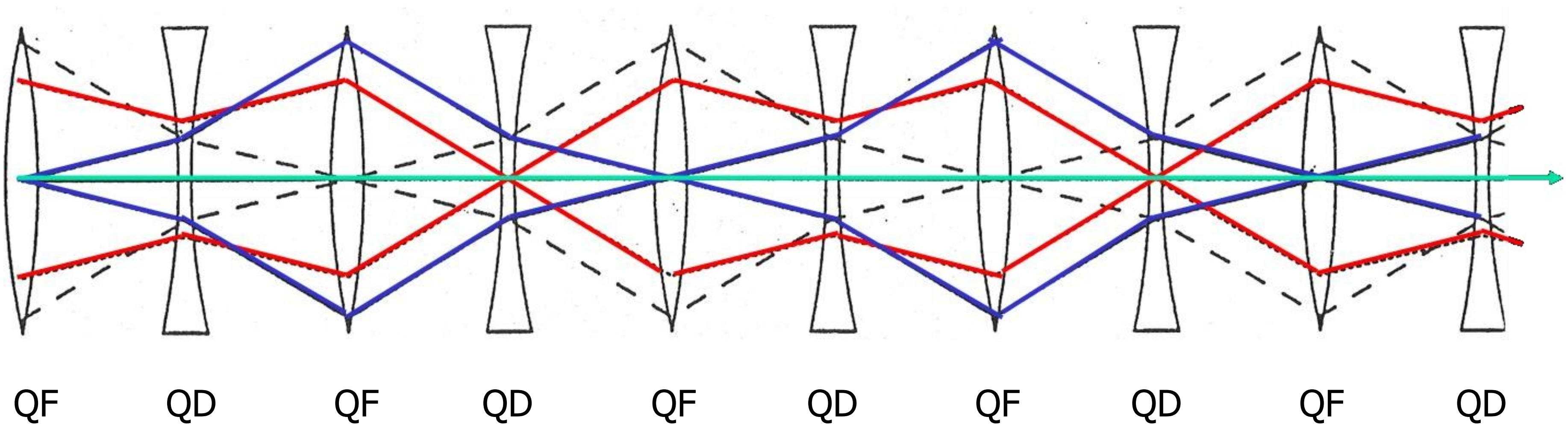
Alternate QF and QD



valid for one plane only (H or V) !

Alternating gradient focusing

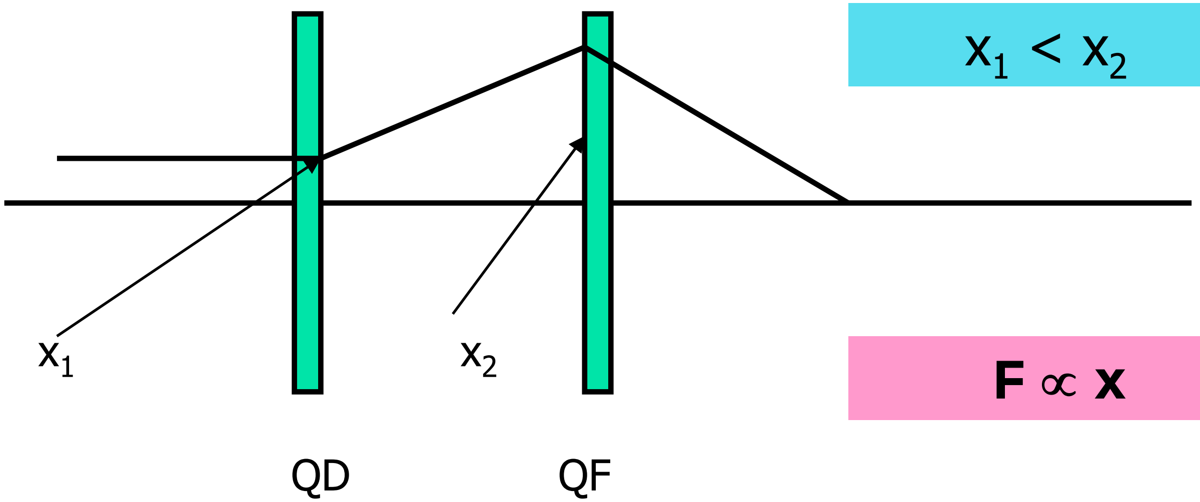
What happens to "non-ideal" particles for which x, x′, y, y′ ≠ 0 ?



The « non-ideal » particles perform an oscillation around the « ideal » trajectory.

Why net focusing effect?

Purely intuitively:

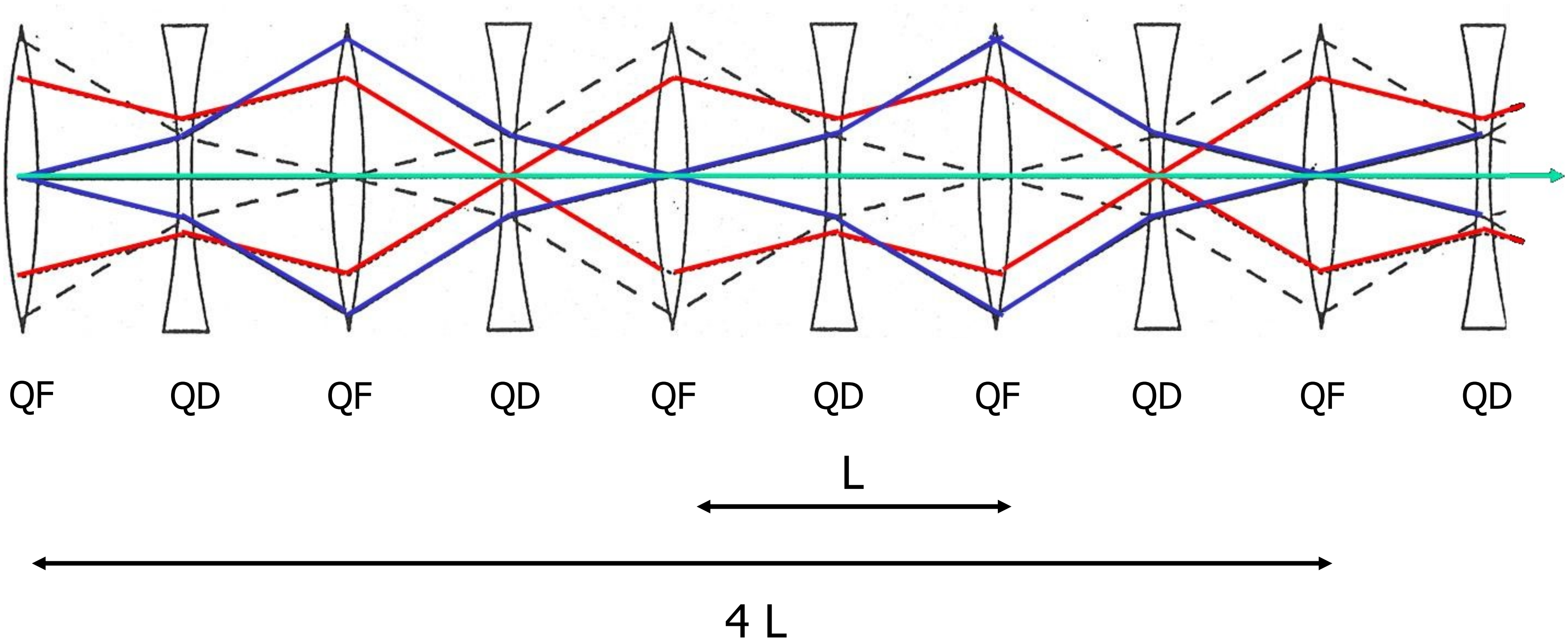


$x_1 < x_2$

$\mathbf{F} \propto \mathbf{x}$

Rigorous treatment in the dedicated lecture !

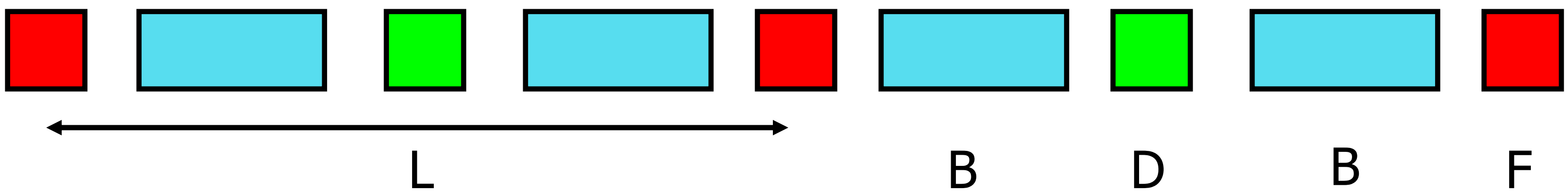
The concept of a « cell »



One complete oscillation in 4 cells ⇒ 90°/ cell ⇒ **μ = 90°**

Circular machines (no errors!)

The accelerator is composed of a periodic repetition of cells:



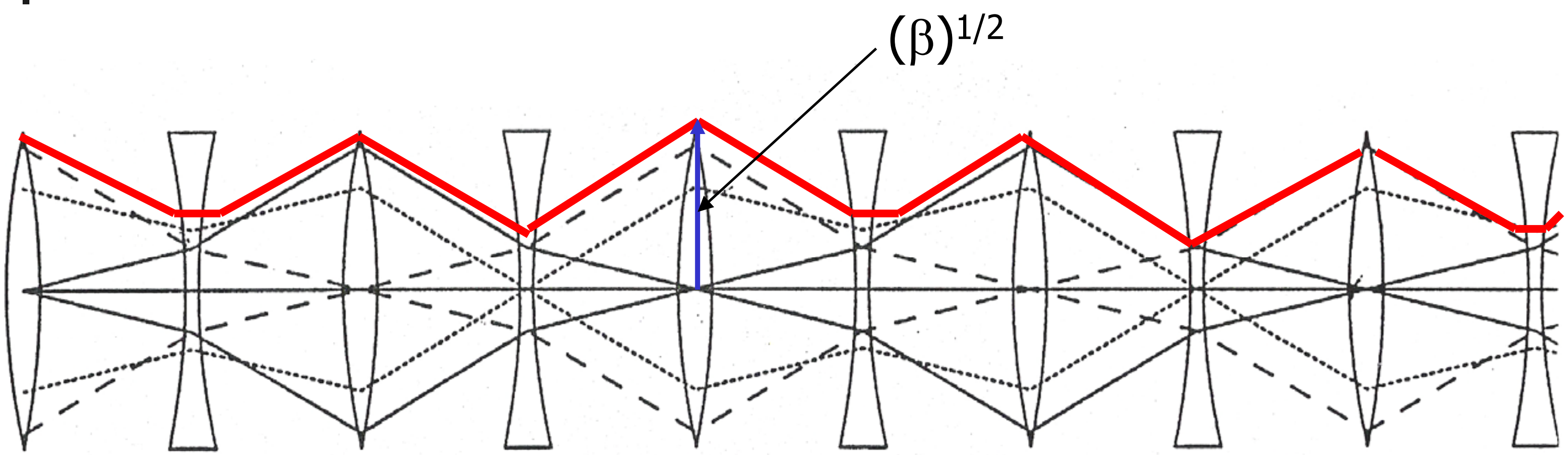
- The phase advance per cell μ can be modified, in each plane, by varying the strength of the quadrupoles.

- The ideal particle will follow a particular trajectory, which closes on itself after one revolution: the closed orbit.

- The real particles will perform oscillations around the closed orbit.

- The number of oscillations for a **complete revolution** is called the **Tune Q** of the machine (Qx and Qy).

The beta function β(s)



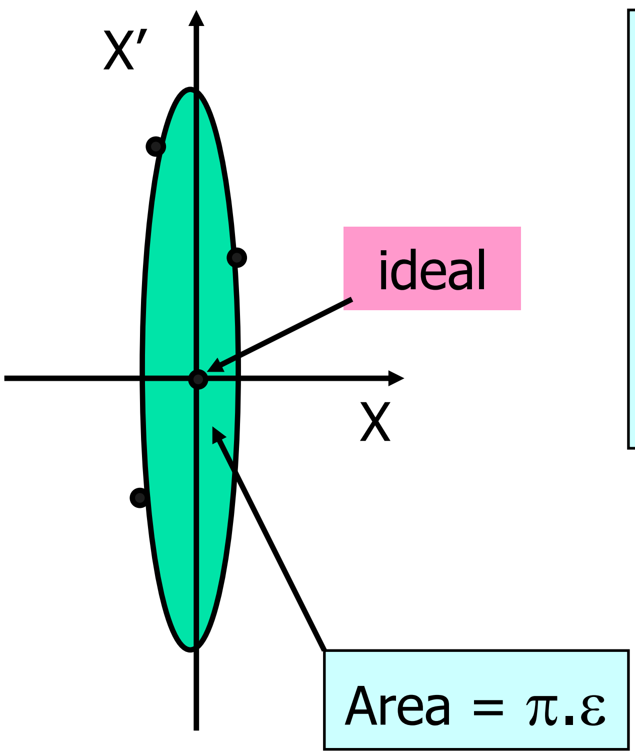
The β-function is the envelope around all the trajectories of the particles circulating in the machine (see lecture on Transv. Dyn.!).

The β-function has a minimum at the QD and a maximum at the QF, ensuring the net focusing effect of the lattice.

It is a periodic function (repetition of cells). The oscillations of the particles are called betatron motion or **betatron oscillations**.

Phase space at some position (s)

- Select the particle in the beam with the largest betatron motion and plot its position vs. its phase (x vs. x′) at some location in the machine for many turns.

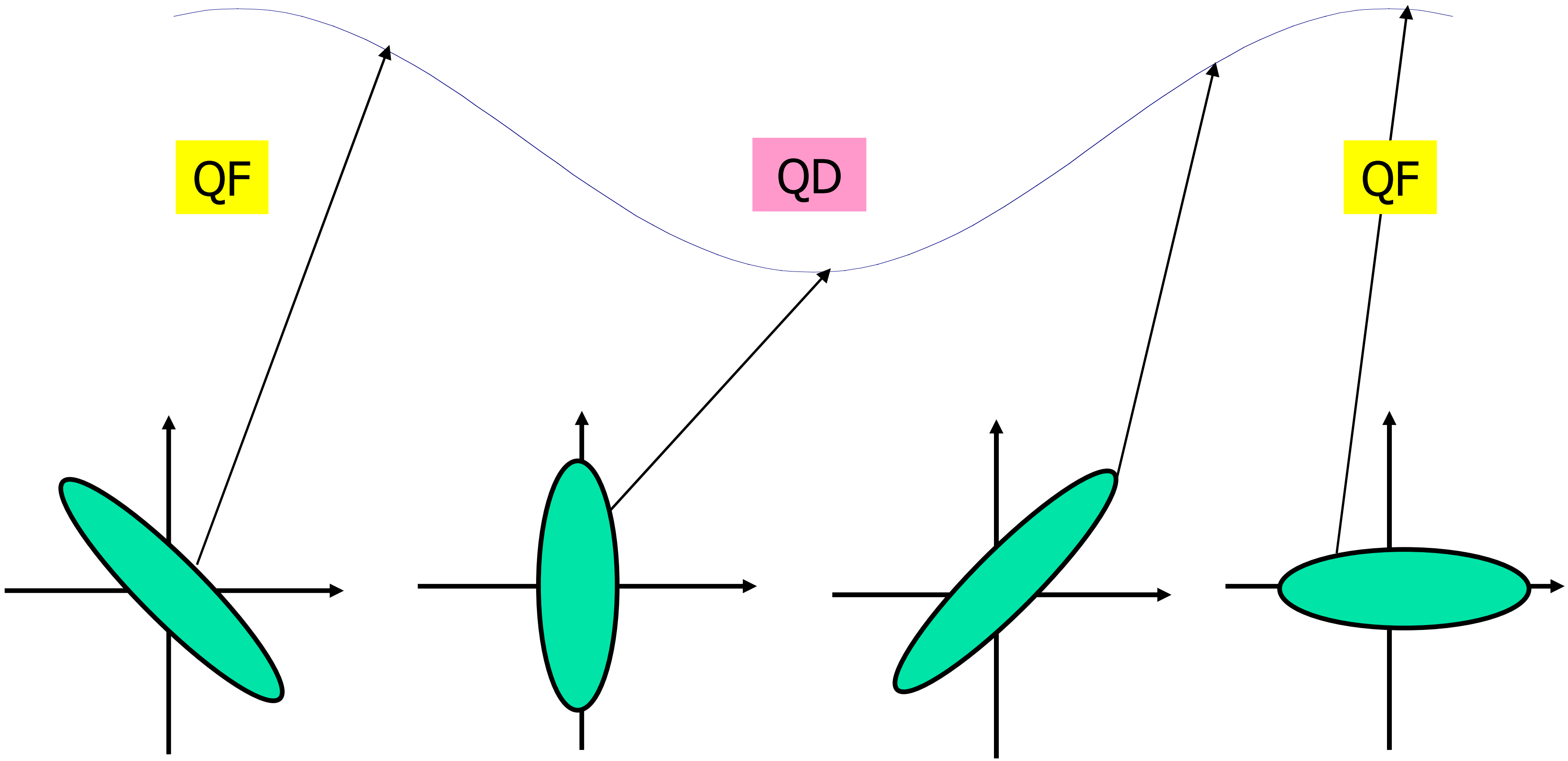


- ε Is the emittance of the beam [π mm mrad]
- ε is a property of the beam (quality)
- Measure of how much particle depart from ideal trajectory.
- β is a property of the machine (quadrupoles).

Beam size [m]

$$\sigma(s) = (\varepsilon.\beta(s))^{1/2}$$

Emittance conservation



The shape of the ellipse varies along the machine, but its area (the emittance ε) remains constant for a given energy.

Recapitulation 1

- The **fraction** of the oscillation performed in a periodic cell is called the **phase advance μ per cell** (x or y).

- The total number of oscillations over one full turn of the machine is called the **betatron tune Q** (x or y).

- The envelope of the betatron oscillations is characterised by the **beta function $\beta(s)$.** This is a property of the quadrupole settings.

- The quality of the (injected) beam is characterised by the **emittance ε**. This is a property of the beam and is invariant around the machine.

- The r.m.s. beam size (measurable quantity) is $\sigma = (\beta.\varepsilon)^{1/2}$.

Off momentum particles:

- These are “non-ideal” particles, in the sense that they do not have the right energy, i.e. all particles with $\Delta p/p \neq 0$

What happens to these particles when traversing the magnets ?

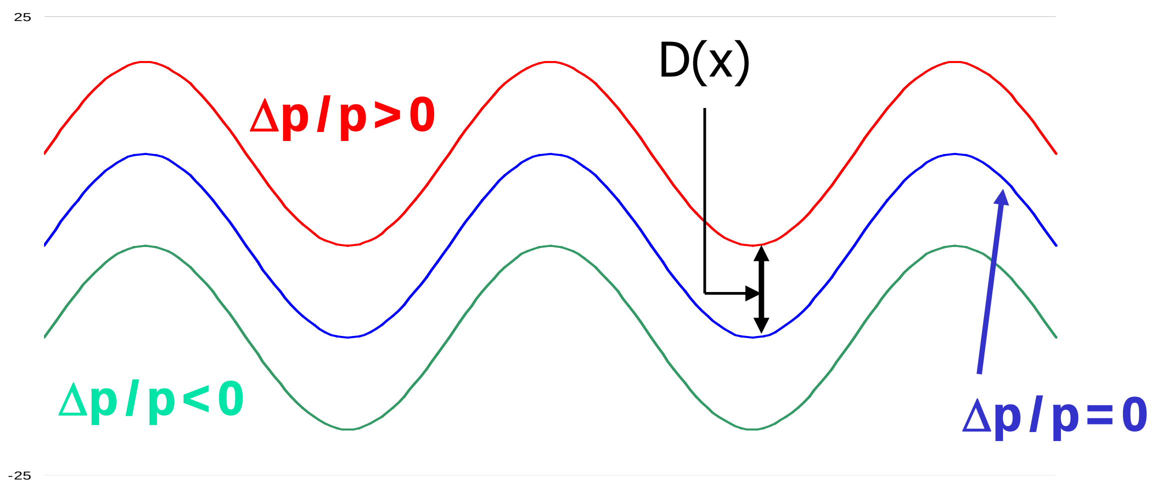
Off momentum particles ($\Delta p/p \neq 0$)

Effect from Dipoles

- If $\Delta p/p > 0$, particles are less bent in the dipoles ➔ should spiral out !
- If $\Delta p/p < 0$, particles are more bent in the dipoles ➔ should spiral in !

No!

There is an equilibrium with the restoring force of the quadrupoles

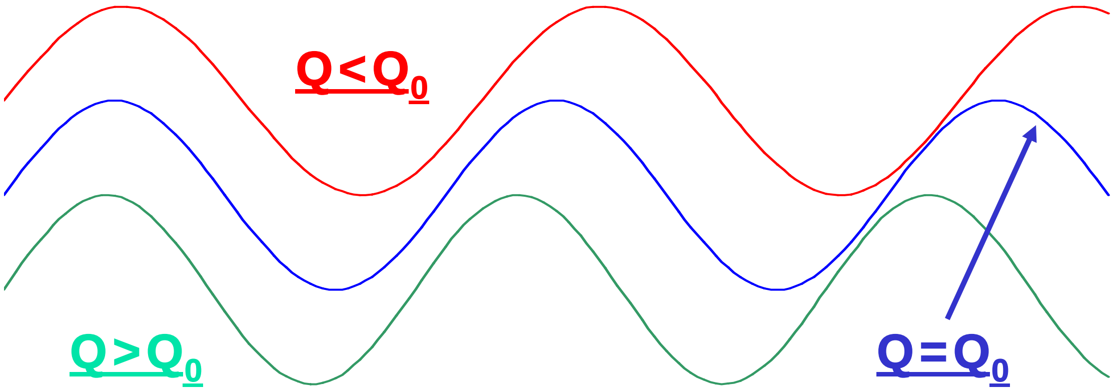


Off momentum particles ($\Delta p/p \neq 0$)

Effect from Quadrupoles

- If $\Delta p/p > 0$, particles are less focused in the quadrupoles ➔ **lower Q !**
- If $\Delta p/p < 0$, particles are more focused in the quadrupoles ➔ **higher Q !**

Particles with different momenta would have a different betatron tune $Q=f(\Delta p/p)$!



The chromaticity Q′

Particles with different momenta ($\Delta p/p$) would thus have different tunes Q.
So what ?

unfortunately

- The tune dependence on momentum is of fundamental importance for the stability of the machine. It is described by the chromaticity of the machine Q′:

$$Q' = \Delta Q / (\Delta p/p)$$

The chromaticity has to be carefully controlled for different reasons

(see dedicated lectures)

Recapitulation 2

- For off momentum particles ($\Delta p/p \neq 0$), the magnets induce other important effects, namely:

  - The dispersion (dipoles)
  - The chromaticity (quadrupoles)

Longitudinal plane

- So far, we considered only the motion in the transverse planes from an intuitive point of view. The corresponding rigorous treatment will be given in the lectures on "**Transverse Beam Dynamics**".

- The lectures on "**Longitudinal Beam Dynamics**" will explain the details of the corresponding longitudinal motion as well as the RF acceleration of the particles.

The course:

Beam Dynamics is certainly a "core" topic of accelerator physics, but the objective of this course is to give you a broader introduction covering:

- Relativity and E.M. Theory
- Particle sources
- Transfer Lines
- Beam Diagnostics
- Linear Imp. and Resonances
- Synchrotron Radiation, Electron Dynamics, SLS, FELs
- Multi particle Effects

History, physics and applications

Injection, Extraction

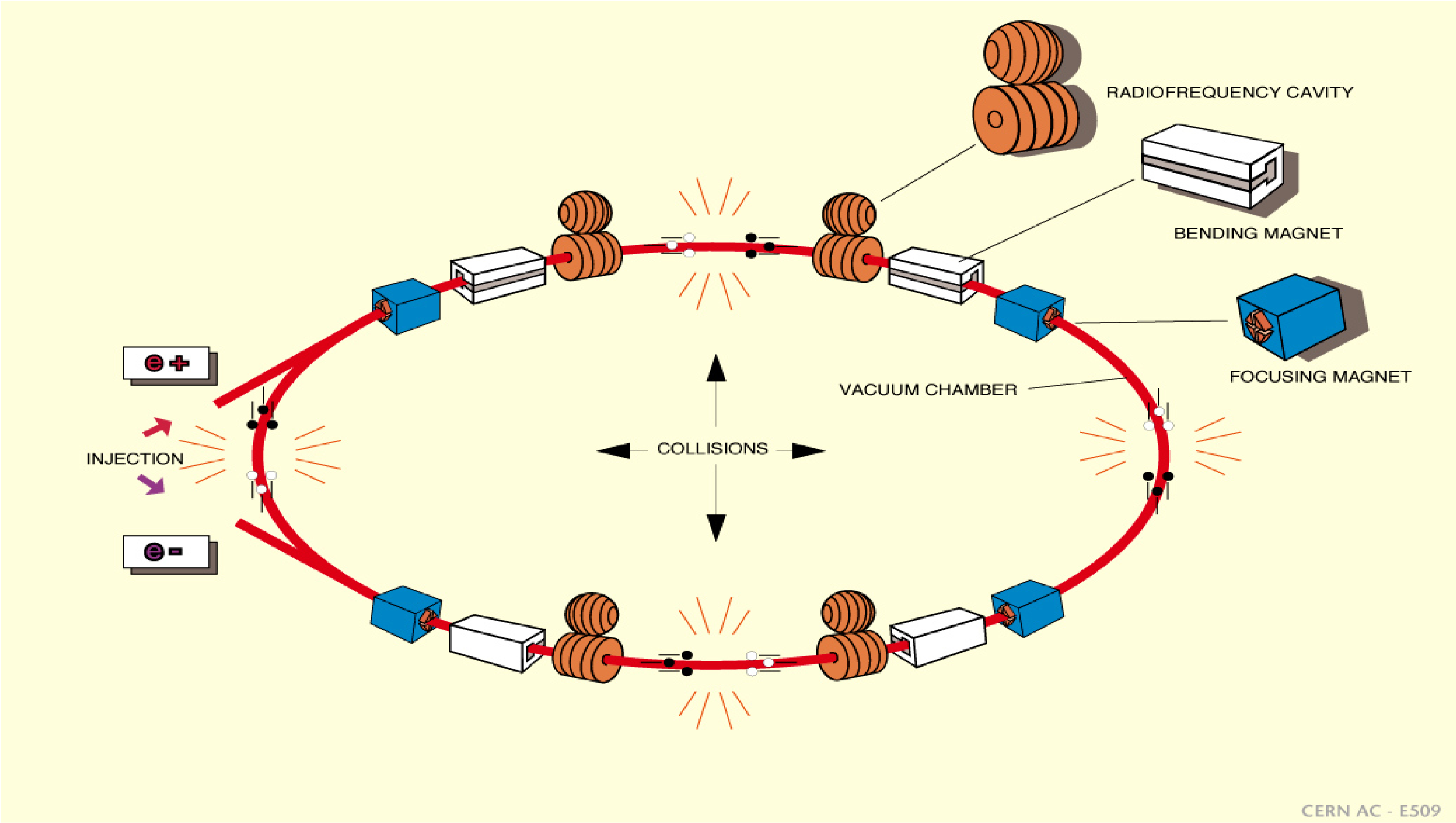
Magnets

Apertures

Vacuum

Computer Tools

Basic high energy collider



An Accelerator Complex…

Accelerator chain of CERN (operating or approved projects)