Switched Mode Converters (1 Quadrant)

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Summary

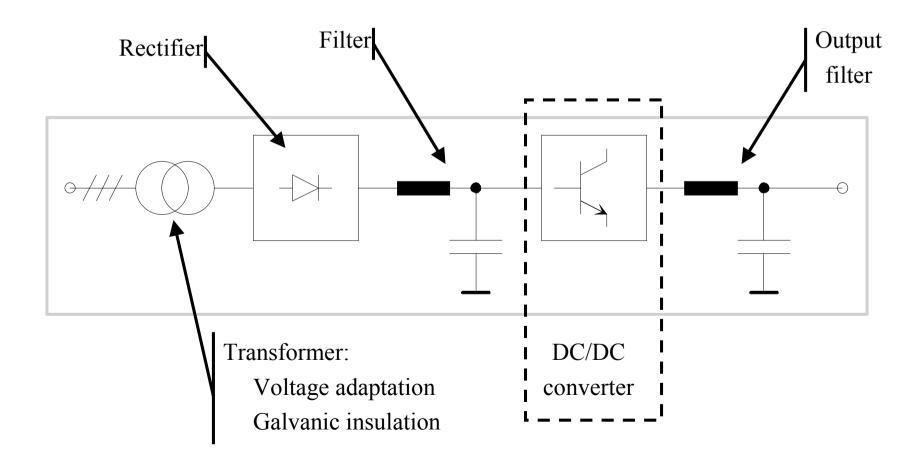
- Introduction
 - DC supplies: principle
 - Linear or Switched Mode Converters
 - Switched Mode Converters: main challenges
- DC/DC direct converters
 - Buck, boost, buck-boost converters
 - Multi channels converters
- Transformers for DC/DC converters
 - Principle, Model
 - Sizing of a transformer: weight, power and frequency
- DC/DC converters with transformers
 - Forward
 - Flyback
 - DC/AC/DC converters



- DC supplies: principle
 - Switched mode converters are DC/DC converters
 - They are generally supplied from an AC network, via:
 - A transformer
 - \Rightarrow For a galvanic insulation
 - \Rightarrow For voltage level adaptation
 - A rectifier
 - \Rightarrow In order to obtain a DC voltage source
 - Switched mode converters are used to generate controlled and adjustable DC voltage levels

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- DC supplies: principle
 - Typical (and possible) architecture

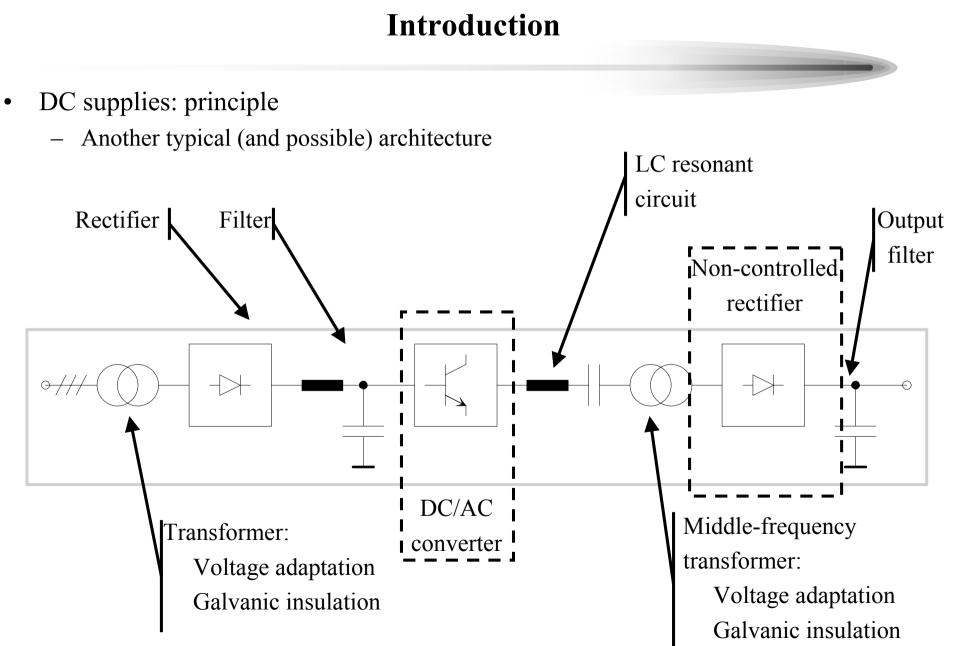


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- DC supplies: principle
 - Typical (and possible) architecture
 - Transformer : size and weight (?)
 - Rectifier: generally a diode rectifier
 - \Rightarrow No regulation of the output voltage
 - Filter
 - \Rightarrow Theoretically, a LC filter is needed
 - ⇒Taking into account the parasitic inductances of the AC network or the leakage inductances of the transformer, a single capacitor is generally used
 - \Rightarrow The aim of this filter is to supply the DC/DC converter with a voltage source
 - DC/DC converter: dedicated for the control and regulation of the output voltage. Theoretically, two solutions can be investigated:
 - \Rightarrow Linear converter
 - ⇒Switched mode converter: then an LC (or C) output filter is needed to lower ripple.





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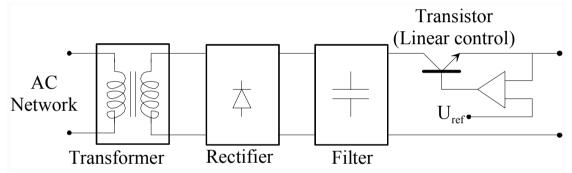


- DC supplies: principle
 - Another typical (and possible) architecture
 - Input Transformer (optional)
 - Rectifier, Filter
 - DC/AC converter
 - \Rightarrow In order to obtain transmit energy to an AC stage
 - LC resonant circuit (optional):
 - ⇒For efficiency reasons, to obtain soft-switching condition for the DC/AC converter
 - Middle-frequency transformer:
 - \Rightarrow Voltage adaptation, Galvanic insulation
 - \Rightarrow Middle-frequency: reduction of weight and size
 - \Rightarrow Should avoid the use of the input transformer
 - Rectifier:
 - \Rightarrow Controlled or non-controlled, to obtain DC output voltage
 - \Rightarrow A LC (or C) filter is needed to lower ripple

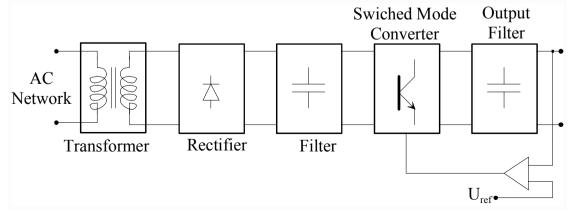
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- Linear or Switched mode converters
 - Linear converter
 - Transistor driven in its linear characteristics



- Switched mode converter
 - Output filter to lower output voltage ripple



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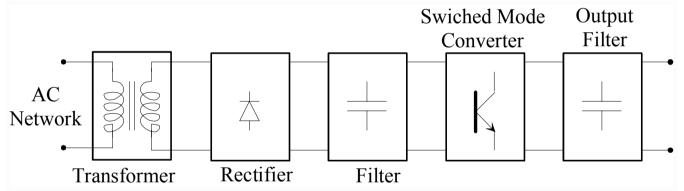
- Linear or Switched mode converters
 - Main properties: comparison

	Switched mode	Linear
Efficiency	65 à 90%	35 à 55%
Power per kilo	30 à 300W/kg	10 à 30W/kg
Power per 1	50 à 300W/l	20 à 50W/1
Input voltage range	0.85 à 1.2U _n	0.9 à 1.1U _n
Dynamic	5% - 1ms	1% - 50us
Ouput voltage ripple	1%	0.1%
EMC	Importantes	Négligeables

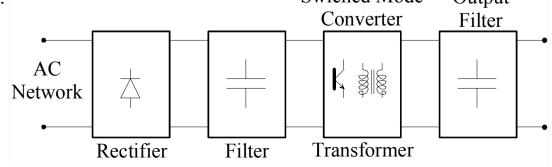
- Main interest for using switched mode power converters
 - Efficiency
 - Power density



- Switched Mode Converters: main challenges
 - Switched mode converter: Main topology
 - Low frequency input filter (50Hz, 60Hz, 400Hz): size and weight!

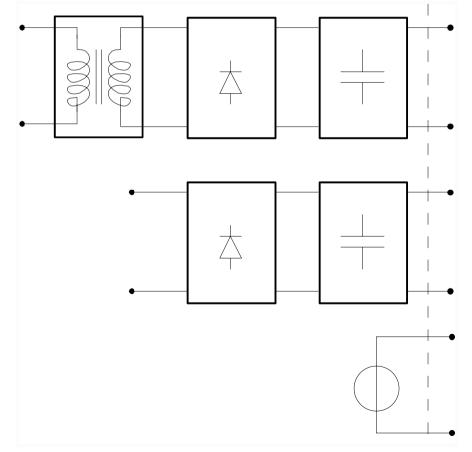


- Switched mode converter: DC/DC converter with transformer
 - Middle frequency transformer: Switching frequency of the converter: size and weight...
 Swiched Mode Output





- Switched Mode Converters: Convention
 - This contribution will focus on Switched Mode converter topologies
 - (Input transformer) + Rectifier + Filter = Ideal voltage source





DC/DC converters

• Introduction

—

- The aim of this presentation is to describe 1 quadrant switched mode converters
 - U_s is the output voltage
 - I_s is the output current
 - The power provided to the load is:

$$P_{s} = U_{s}I_{s}$$
Depending on the topology and the components, DC/DC converters can be reversible or non-reversible
• Converters affiliated with quadrant 1
$$(U_{s}>0 \text{ and } I_{s}<0) \text{ will be considered}$$

$$P_{s}>0$$

$$P_{s}>0$$

$$P_{s}<0$$

$$P_{s}<0$$

$$P_{s}<0$$

$$Q_{s}$$

L

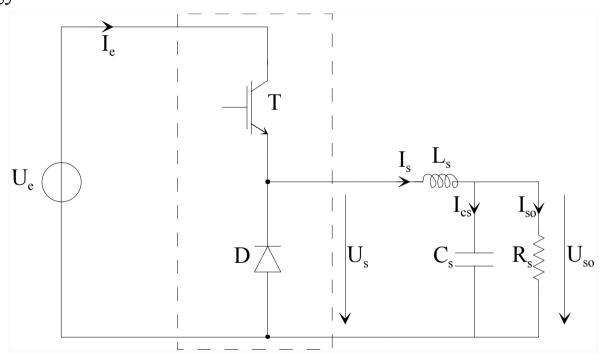


- Introduction
 - The aim of direct DC/DC converter is to manage an energy transfer between
 - A DC voltage source and a DC current source (Buck or step-down converter)
 ⇒Such a converter allows the supply of loads with an adjustable voltage, lower than the input voltage
 - A DC current source and a DC voltage source (Boost or step-up converter)
 ⇒Such a converter allows the supply of loads with an adjustable voltage, higher than the input voltage
 - A DC voltage source and a second DC voltage source (Buck-boost or step-up/down converter)
 - ⇒The control of the energy transfer between two voltage sources is allowed by an internal inductance, used as energy buffer in the energy flow process
 - ⇒Such a converter allows the supply of loads with an adjustable voltage, higher or lower than the input voltage
 - \Rightarrow The buck-boost converter is not the association of a buck and a boost converters

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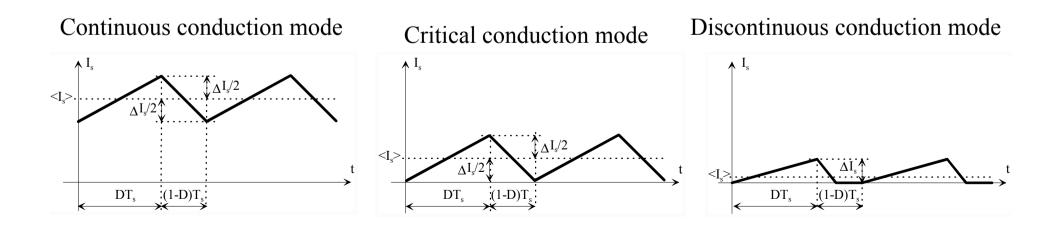
- Buck (step-down) converter:
 - Topology



- 1 Switching cell: transistor + Diode
- Main parameter:
 - switching period T_s

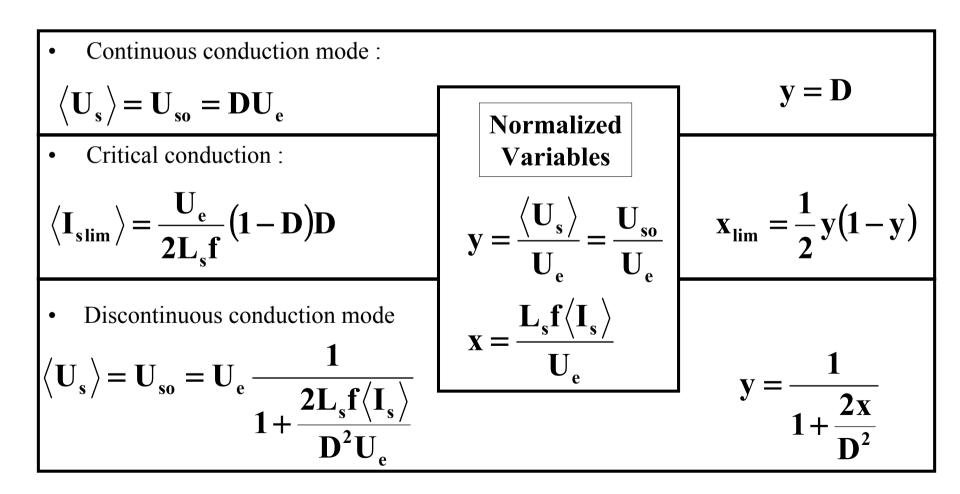
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- Buck (step-down) converter:
 - Continuous conduction mode:
 - The output current I_s is always positive
 - Each off-switching of the diode is trigged by the on-switching of the transistor
 - Discontinuous conduction mode:
 - Each off-switching of the diode is due to a natural decrease of the output current to 0, while the transistor is not immediately switched on.





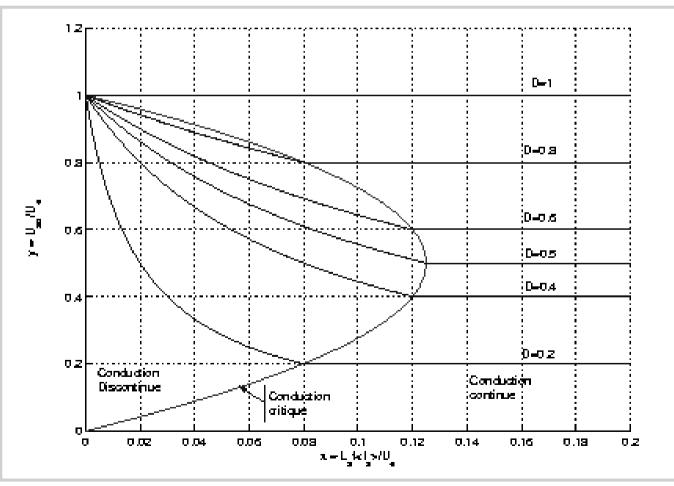
- Buck (step-down) converter:
 - Summary:



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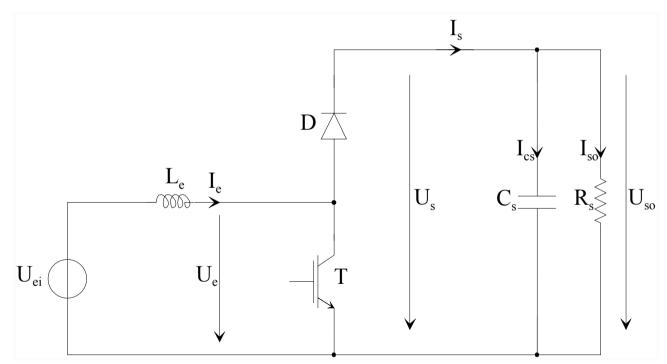


- Buck (step-down) converter:
 - Output characteristics





- Boost (step-up) converter:
 - Topology

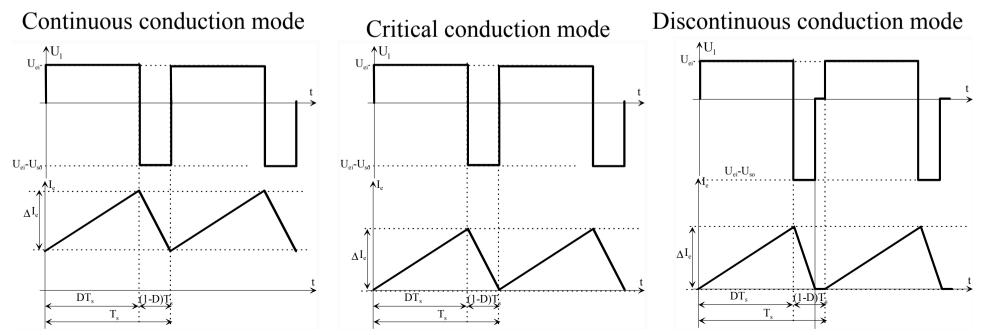


- 1 Switching cell: transistor+diode
- Main parameter
 - Switching period T_s

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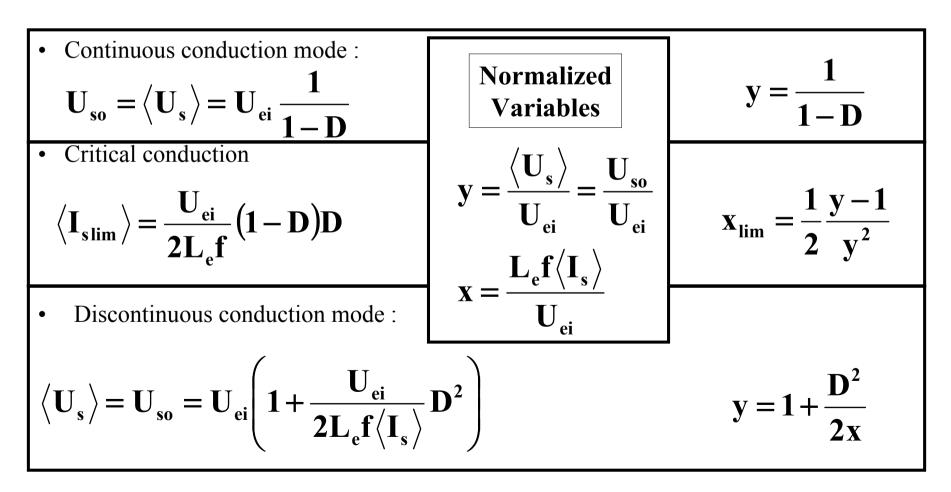


- Boost (step-up) converter:
 - Continuous conduction mode:
 - The input current is always positive
 - Each off-switching of the diode is trigged by the on-switching of the transistor
 - Discontinuous conduction mode
 - Each off-switching of the diode is due to a natural decrease of the input current to 0, while the transistor is not immediately switched on.





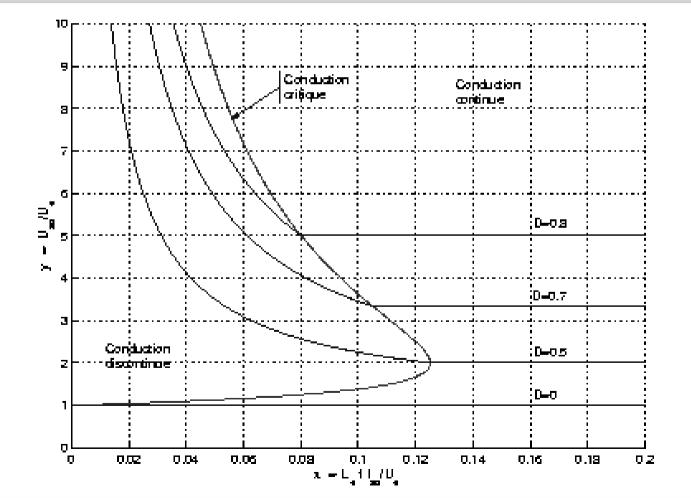
- Boost (step-up) converter:
 - Summary



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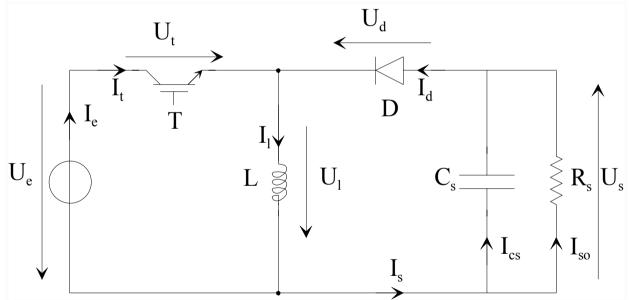
- Boost (step-up) converter:
 - Output Characteristics



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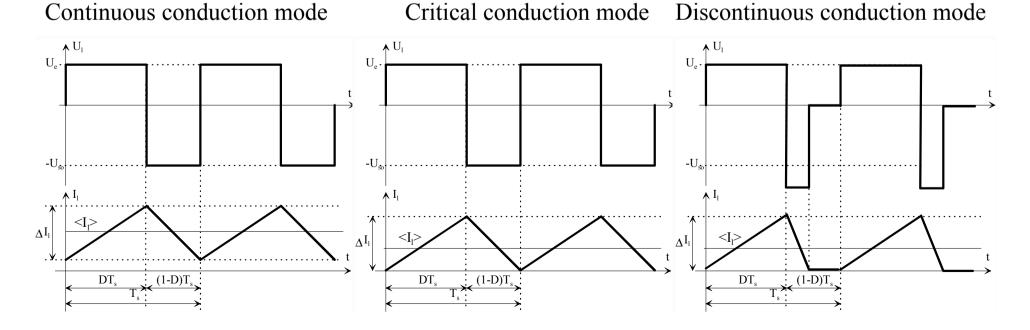
- Buck-Boost (step-up/down) converter:
 - Also know as DC/DC inverter
 - Topology



- Energy transfer between 2 voltage sources is allowed by the internal inductance L
- 1 Switching cell: transistor+diode
- Main parameter
 - Switching period T_s

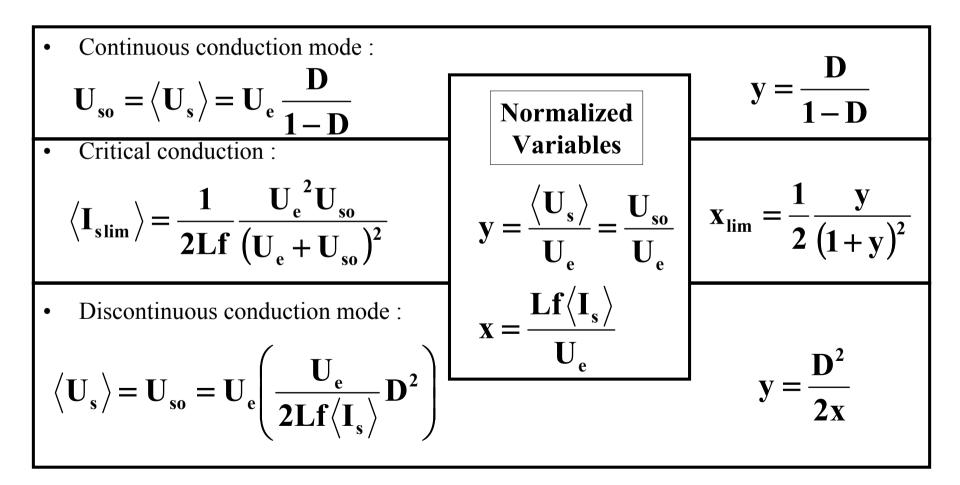


- Buck-Boost (step-up/down) converter:
 - Continuous conduction mode:
 - The current in the inductor is always positive
 - Each off-switching of the diode is trigged by the on-switching of the transistor
 - Discontinuous conduction mode
 - Each off-switching of the diode is due to a natural decrease of the current in the inductor to 0, while the transistor is not immediately switched on.





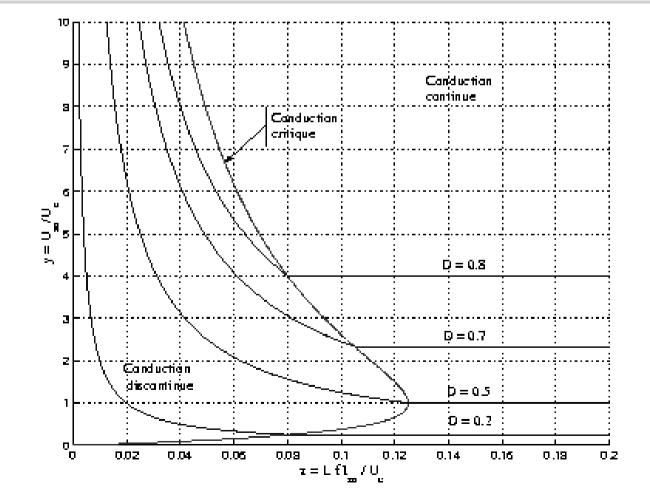
- Buck-Boost (step-up/down) converter:
 - Summary



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- Buck-Boost (step-up/down) converter:
 - Output Characteristics



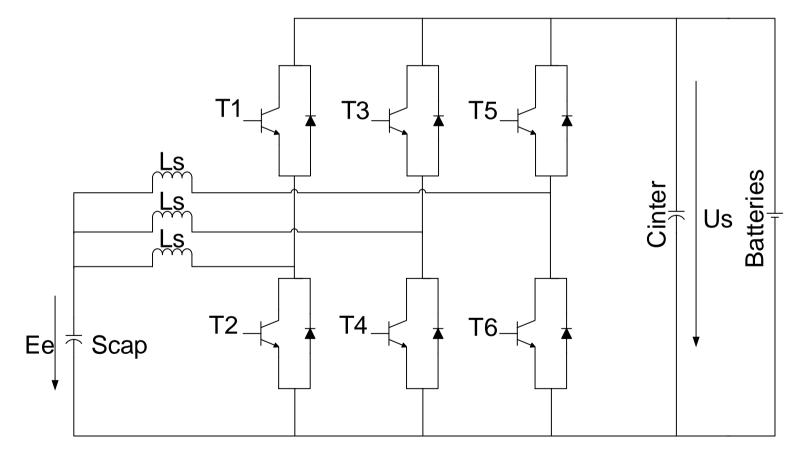
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- Multi channels converters
 - Conventional buck or boost topologies,
 - Reduction of cooling devices
 - Increase of the efficiency
 - Soft-switching conditions
 - This can be obtained in the discontinuous conduction mode
 - ⇒the off-switching of diodes is natural, and not due to the on-switching of transistors
 - \Rightarrow Switching current is 0A when transistors are switched on.



- Multi channels converters
 - Example of a multi-channel boost converter



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- Multi channels converters
 - Example of a multi-channel boost converter
 - Each channel works in discontinuous conduction mode
 - The associated coil is then reduced (few micro-henri)
 - Strong current ripple, poor averaged value
 - On the low-voltage source:
 - \Rightarrow averaged values of currents are summed
 - \Rightarrow As each leg is phase-shifted, current ripple are cancelled.
 - Such a solution offers high efficiency for applications of few kW.

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DC/DC Converters

- Multi channels converters
 - Example of a multi-channel boost converter

[TDS2024].CH1 200 mV 10 uS 2024].CH2 200 mV 10 uS [TDS 2024].CH3 200 mV 10 uS

Vin = 18 V

Vout = 37.5 - 75 V

Iin max = 255 A (maximal power 4600 W)

Switching frequency : 20 kHz

8 channels

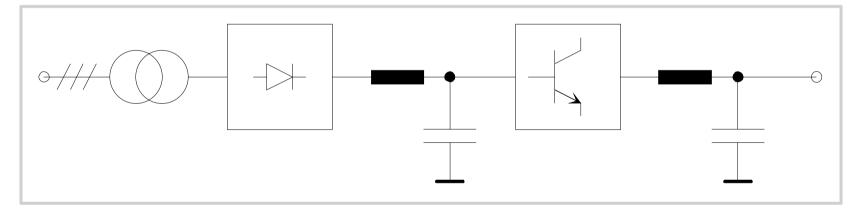
Inductors used : 7.8 uH

(typical inductor for a classical converter : some mH)

Current shown for 4 channels



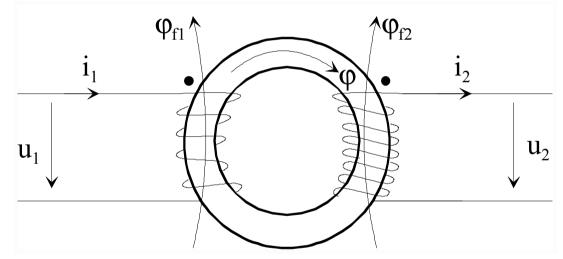
- Principle, Model
 - In switched mode converters, transformers are needed
 - To adapt voltage/current levels
 - To offer galvanic insulation



- In several applications, transformers are the first devices in the energy-flow chain:
 - Sizing?
 - Volume?
 - Weight?



- Principle, Model
 - General equations of a transformer:
 - Principle of a 2 windings transformer

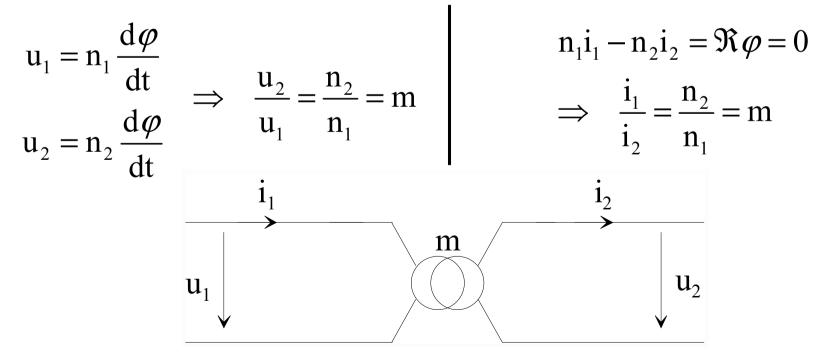


• Sign conventions

 \Rightarrow Voltages and currents are positives regarding conventions adopted in the figure



- Principle, Model
 - General equations of a transformer:
 - First hypothesis:
 - \Rightarrow No leakage flux
 - \Rightarrow Reluctance of the magnetic circuit is 0
 - \Rightarrow Windings with no electric resistance





- Principle, Model
 - General equations of a transformer:
 - Second hypothesis:
 - \Rightarrow No leakage flux
 - \Rightarrow Reluctance of the magnetic circuit
 - \Rightarrow Windings with no electric resistance

$$n_{1}i_{1} - n_{2}i_{2} = \Re \varphi \implies i_{1} = \frac{n_{2}}{\underbrace{n_{1}}_{Ideal}} i_{2} + \frac{\Re}{\underbrace{n_{1}}_{i\mu}} \varphi$$

transformer

~

$$\varphi_{t} = n_{1}\varphi \implies \varphi_{t} = \frac{n_{1}^{2}}{\underbrace{\Re}_{L_{m}}}i_{\mu}$$

– L_m: magnetic inductance of the transformer



- Principle, Model
 - General equations of a transformer:
 - L_m : magnetic inductance of the transformer

$$u_1 = L_M \frac{di_{\mu}}{dt}$$

 \Rightarrow The primary mean value of the voltage must be 0

• Magnetic energy stored into a transformer:

$$W = \frac{1}{2} L_{M} i_{\mu}^{2} = \frac{1}{2} \Re \varphi^{2}$$

 \Rightarrow The energy stored into the transformer cannot be discontinuous

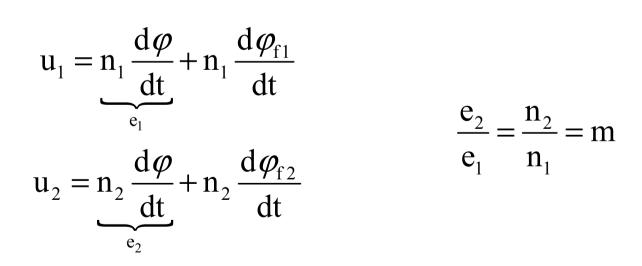
- The flux is then a state variable
- Currents:

$$\mathbf{n}_1\mathbf{i}_1 - \mathbf{n}_2\mathbf{i}_2 = \Re \varphi$$

⇒Each discontinuity of the input current must be compensated by an equivalent discontinuity of the secondary side current



- Principle, Model
 - General equations of a transformer:
 - third hypothesis:
 - \Rightarrow Leakage flux
 - \Rightarrow Reluctance of the magnetic circuit
 - \Rightarrow Windings with no electric resistance



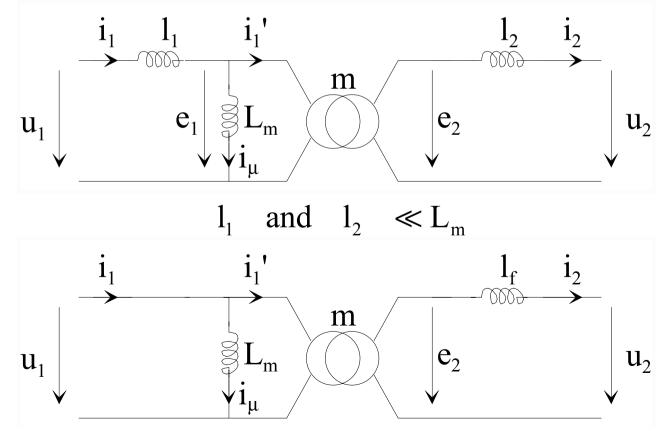


- Principle, Model
 - General equations of a transformer:
 - third hypothesis:
 - \Rightarrow Leakage flux
 - \Rightarrow Reluctance of the magnetic circuit
 - \Rightarrow Windings with no electric resistance
 - Introducing the notion of leakage inductances (considering that ϕ_{f1} and ϕ_{f2} are directly proportional to the primary and secondary currents)

$$n_1 \frac{d\varphi_{f1}}{dt} = l_1 \frac{di_1}{dt} \qquad u_1 = e_1 + l_1 \frac{di_1}{dt}$$
$$\Rightarrow \qquad u_1 = e_1 + l_1 \frac{di_1}{dt}$$
$$\Rightarrow \qquad u_2 = e_2 + l_2 \frac{di_2}{dt}$$

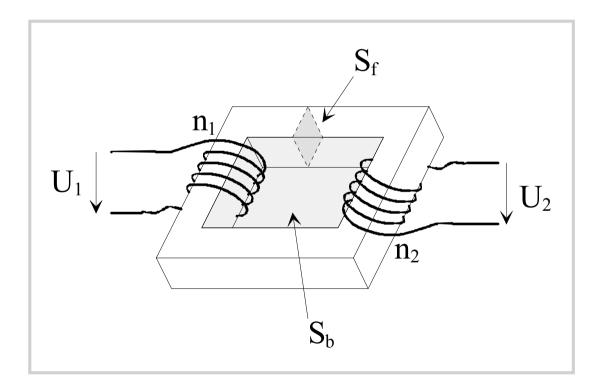


- Principle, Model
 - Model
 - Resistance of windings are neglected
 - Hysterese and iron losses are not takien into account





- Sizing of a transformer:
 - Main equations:



- S_f : section of the magnetic circuit
- S_b : surface allowed for windings

Switched Mode Converters CAS Power Converter course



- Sizing of a transformer:
 - Main equations: surface of the magnetic circuit

$$u_{1}(t) = n_{1} \frac{d\varphi}{dt}$$

$$\varphi = BS_{f} \Rightarrow u_{1}(t) = n_{1}S_{f} \frac{dB}{dt}$$

$$B = \frac{1}{n_{1}S_{f}} \int u_{1}(t)dt$$

$$\Rightarrow B_{M} = \frac{U}{n_{1}S_{f}f}$$

$$\Rightarrow S_{f} = \frac{U}{n_{1}B_{M}f}$$



- Sizing of a transformer:
 - Main equations: surface allowed for windings

$$S_{b} = n_{1}s_{1}K_{b1} + n_{2}s_{2}K_{b2} + \dots + n_{N}s_{N}K_{bN}$$
$$S_{b} = n_{1}\frac{I_{1eff}}{J_{1}}K_{b1} + n_{2}\frac{I_{2eff}}{J_{2}}K_{b2} + \dots + n_{N}\frac{I_{Neff}}{J_{N}}K_{bN}$$

$$u \sin g : n_i I_{ieff} = a_i n_1 I_{1eff}$$

$$S_b = n_1 I_{1eff} \sum_{i=1}^{N} \frac{a_i K_{bi}}{J_i}$$



- Sizing of a transformer:
 - Main equations: definition of A_{TR} , defining the volume of the transformer

$$\mathbf{A}_{\mathbf{TR}} = \mathbf{S}_{\mathbf{f}} \mathbf{S}_{\mathbf{b}}$$

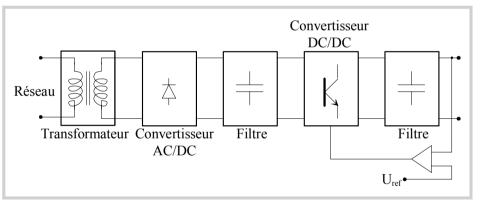
$$\mathbf{A}_{\mathrm{TR}} = \frac{\mathbf{UI}_{1\mathrm{eff}}}{\mathbf{B}_{\mathrm{M}}\mathbf{f}} \sum_{i=1}^{\mathrm{N}} \frac{\mathbf{a}_{i}\mathbf{K}_{\mathrm{bi}}}{\mathbf{J}_{i}}$$

$$\mathbf{A}_{\mathrm{TR}} = \frac{\mathbf{P}_{1}}{\mathbf{B}_{\mathrm{M}}\mathbf{f}} \sum_{i=1}^{\mathrm{N}} \frac{\mathbf{a}_{i}\mathbf{K}_{bi}}{\mathbf{J}_{i}}$$

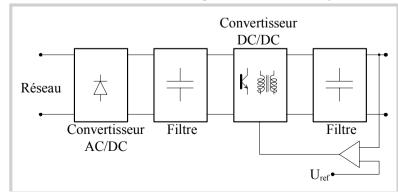
- The volume of the transformer (and is weight) are directly linked to
 - The power
 - The frequency
- The frequency has to be increased to lower volume and weight



- General principle
 - Such converters are identified from the conventional DC/DC converters
 - In conventional energy transfer chain, transformers are directly coupled to a low frequency power network



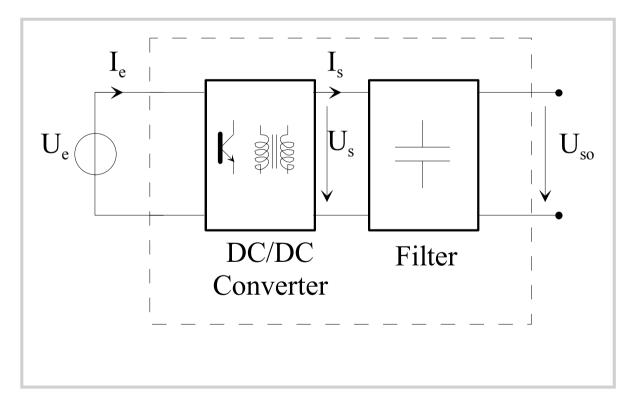
• The transformer can be integrated directly into the DC/DC converter (when possible)



The working frequency is given by the switching frequency of the converter

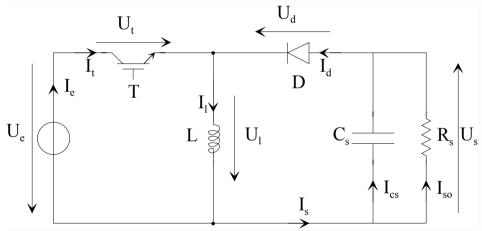


- General principle
 - Such converters are located directly of rectifier and an input filter
 - Convention:





- Flyback:
 - Converter deduced from the DC/DC Buck-boost converter



•When the transistor is ON, the primary side of the transformer is coupled to U_e

•When the diode is ON, the secondary side is coupled to the output

•Magnetic energy is alternatively stored in ${\rm L}_{\rm m}$ and then provided to the output

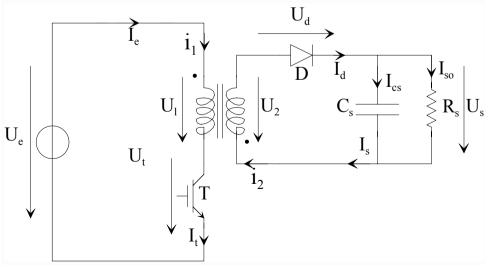
•The mean value of u_1 is 0

•When the transistor is ON, L is coupled to U_e

•When the diode is ON, L is coupled to the output

 $|R_s|_{U_s}$ •Magnetic energy is alternatively stored in L from U_e , and then provided to the ouput

•The mean value of U_1 is 0

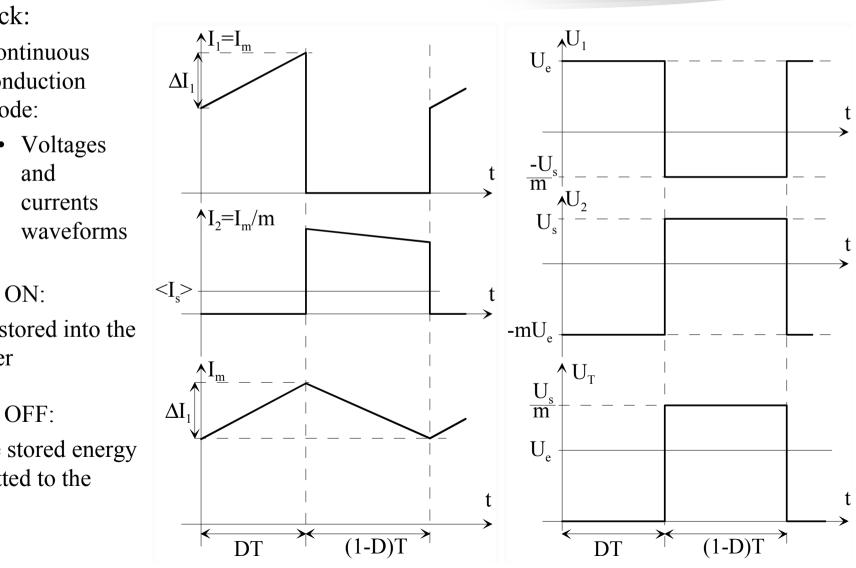




- Flyback: ۲
 - Continuous _ conduction mode:
 - Voltages and currents

Transistor ON: Energy is stored into the transformer

Transistor OFF: Part of the stored energy is transmitted to the output





- Flyback:
 - Continuous conduction mode:
 - Voltages and currents waveforms

 \Rightarrow The transistor has to be able to support not only the input voltage but:

$$U_{T} > U_{e} + \frac{1}{m}U_{s}$$

- ⇒As energy needs to be stored into the transformer, the magnetic circuit can be huge
- ⇒Strong fluctuations of secondary and primary currents, wit leakage inductances: strong constraints on the components



- Flyback:
 - Continuous conduction mode:
 - Main equations:

 \Rightarrow Duty cycle D: ratio between transistor conduction time and the switching period

$$D = \frac{t_1}{T}$$

 \Rightarrow Output voltage

$$U_{so} = \langle U_s \rangle = m \frac{D}{1-D} U_e$$

 \Rightarrow Current ripple: linked to the magnetization inductance

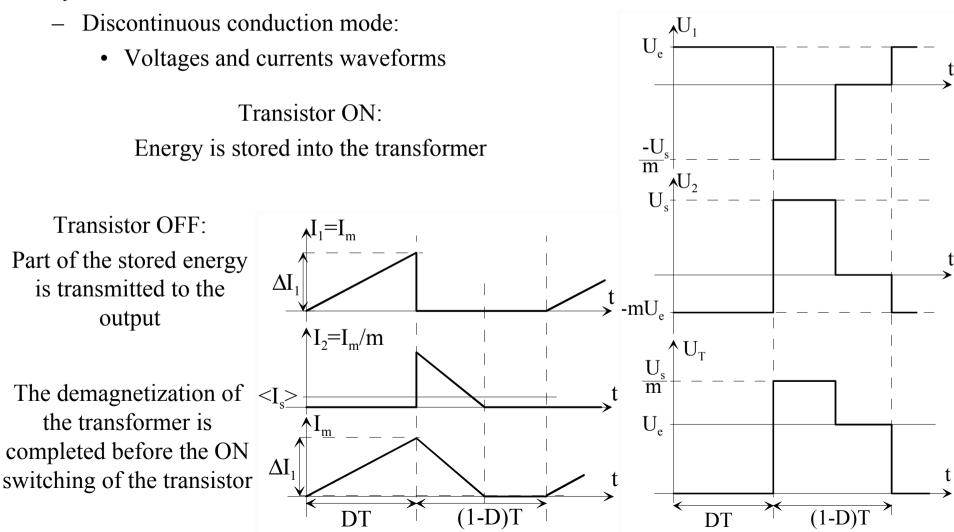
$$\Delta I_1 = \frac{U_e}{L_M f} D$$

 \Rightarrow Input and output currents

$$\langle I_e \rangle = \frac{D}{1-D} \langle I_s \rangle = \frac{D}{1-D} I_{so}$$



• Flyback:





- Flyback:
 - Discontinuous conduction mode:
 - Voltages and currents waveforms

 \Rightarrow The transistor has to be able to support not only the input voltage but:

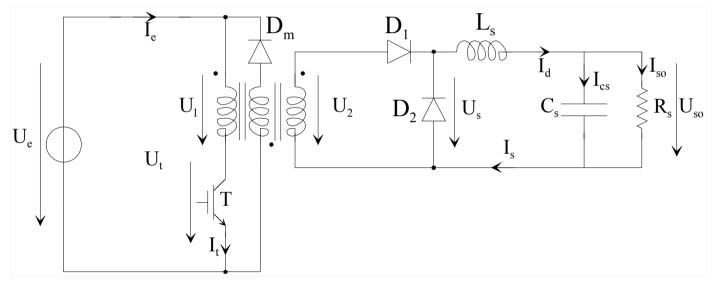
$$U_{T} > U_{e} + \frac{1}{m}U_{s}$$

- ⇒As energy needs to be stored into the transformer, the magnetic circuit can be huge, but less than the case of the continuous conduction mode
- ⇒Strong fluctuations of secondary and primary currents, regarding their mean values
- \Rightarrow The output voltage is no more dependent of the transformation ratio m, but dependent of the load:

$$U_{so} = \langle U_{s} \rangle = DU_{e} \sqrt{\frac{R}{2L_{m}f}}$$



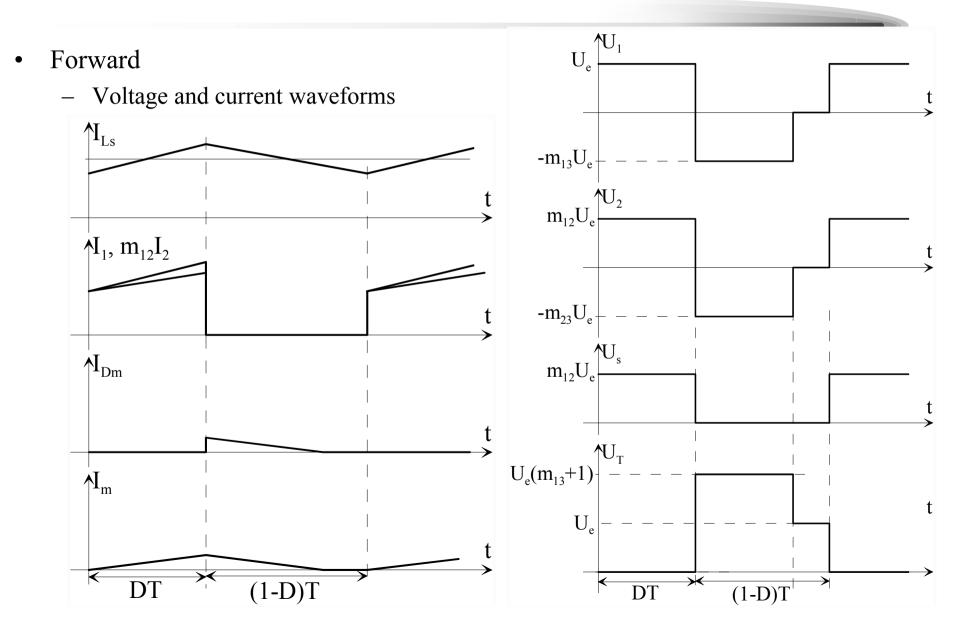
- Forward
 - Converter deduced from the DC/DC Buck converter



- Energy flows directly from the primary side to the secondary side of the transformer when the transistor is ON.
- A third winding is needed to control the magnetization current when the transistor is switched off.
- From the voltage U_s the behaviour is that one of a buck converter.

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- Forward
 - Voltage and current waveforms
 - When the transistor is ON:
 - \Rightarrow The secondary voltage and U_s are m₁₂U_e
 - \Rightarrow The primary current is the sum of the secondary current (modulo the ratio m₁₂) and the magnetization current.
 - When the transistor is switched off:
 - \Rightarrow Primary and secondary currents are 0
 - \Rightarrow The demagnetization circuit is ON
 - \Rightarrow Primary and secondary voltages are negative
 - \Rightarrow Transistor voltage is $m_{13}U_e + U_e$
 - When the demagnetization is completed:
 - \Rightarrow Primary and secondary voltages and currents are 0 (free-wheeling mode)
 - Condition for a complete demagnetization of the transformer (before the conduction of the transistor) m_{13}

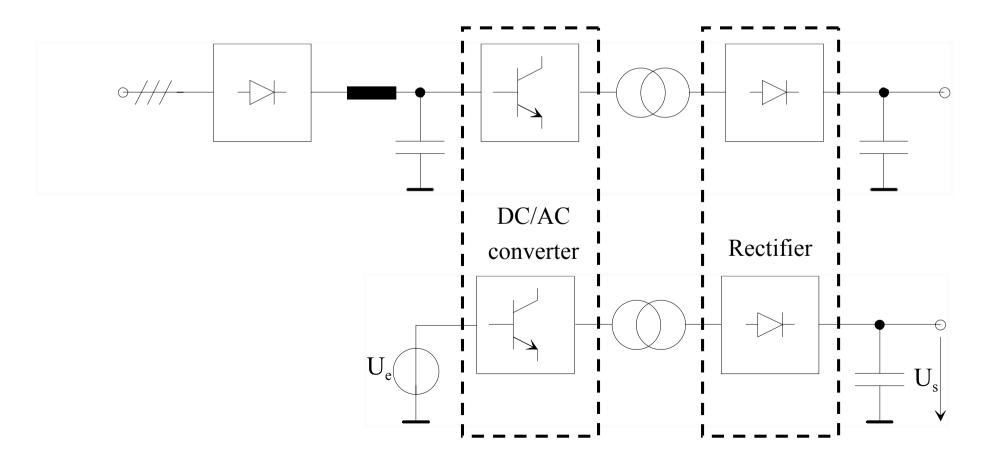
$$D < \frac{m_{13}}{1+m_{13}}$$



- Forward
 - From the voltage U_s , the behaviour of the forward is close of the buck
 - Limit: leakage inductances, with conduction of both D_1 and D_2 during the commutations of the transistor
 - Output characteristics of identical the the Buck, where the only difference is the factor m_{12} applied to U_e
 - Compared to the flyback, smaller transformer
 - Three windings are needed (more complex)
 - Leakage inductances need to be reduced as possible.



- DC/AC/DC Converters:
 - Principle:
 - Input Rectifier + input filter : voltage source

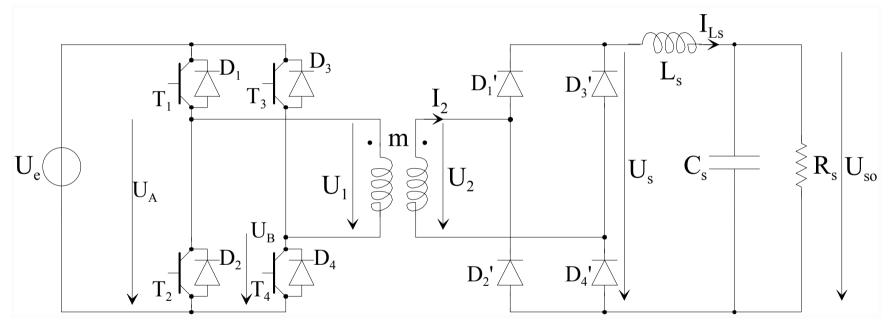




- DC/AC/DC Converters:
 - Principle:
 - First stage: Voltage inverter
 - \Rightarrow Able to manage energy transfer between
 - a DC voltage source : from an input filter (C)
 - an AC current source : the primary side of a transformer
 - Second stage: medium frequency transformer
 - ⇒Galvanic insulation, Voltage/current level adaptation
 - Third stage: rectifier
 - \Rightarrow Able to manage energy transfer between
 - An AC voltage source (secondary of the transformer. Leakage inductances?)
 - A DC current source
 - 1 quadrant converter:
 - Diodes for the rectifier
 - Output voltage level will be adjusted by the voltage inverter



- DC/AC/DC Converters:
 - H-bridge voltage inverter + full H-bridge diode rectifier

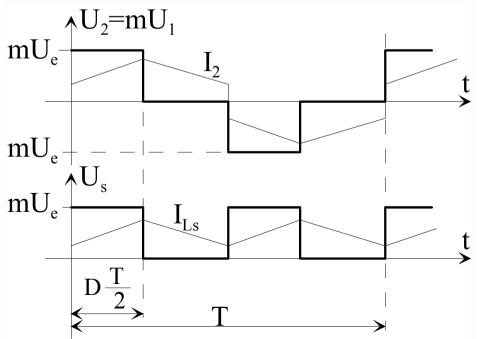


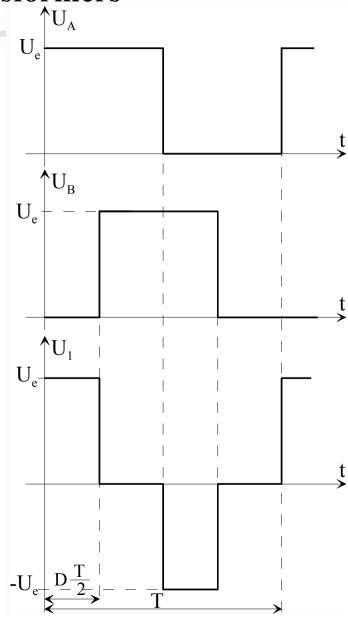
- Voltage inverter
 - 2 switching cells: $(T_1, D_1), (T_2, D_2)$ and $(T_3, D_3), (T_4, D_4)$
 - Each switching cell is controlled with the same switching frequency, duty cyle 50%
 - The 2nd switching cell can be phase-shifted from the first one

CAS Power Converter course



- DC/AC/DC Converters:
 - H-bridge voltage inverter + full H-bridge diode rectifier
 - The duty cycle D defines the time delay between the two switching cells
 - The Width of the positive and negative pulse varies from 0 to T/2 when D varies from 0 to 1







- DC/AC/DC Converters:
 - H-bridge voltage inverter + full H-bridge diode rectifier
 - From the voltage U_s, the behaviour is close to that one of a Buck Converter:
 ⇒Averaged output voltage

$$U_{so} = U_s = mDU_e$$

 \Rightarrow Current ripple in L_s:

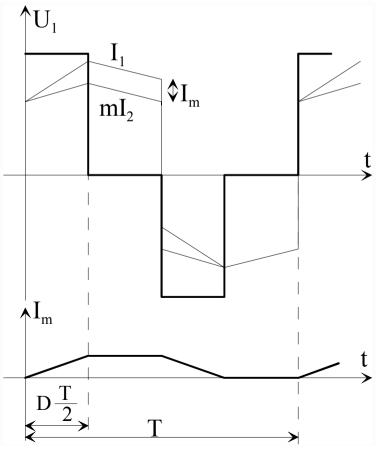
$$\Delta I_{Ls} = \frac{mU_e}{2L_sF} (1-D)D$$

 \Rightarrow Averaged output current:

• Defines mainly the magnitude of the AC current in the secondary side of the transformer



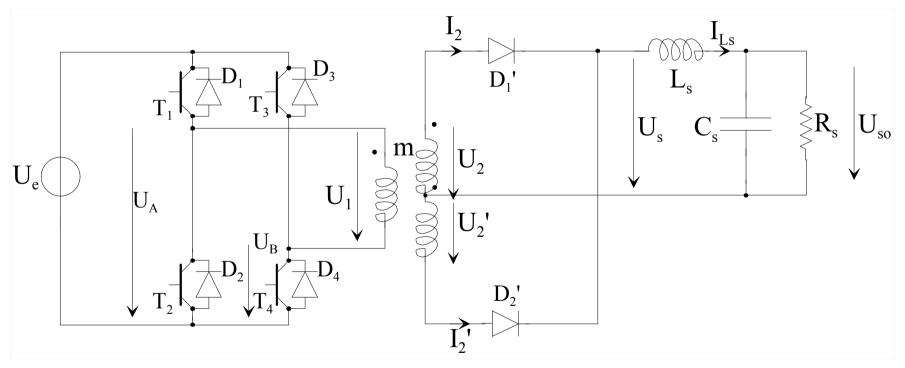
- DC/AC/DC Converters:
 - H-bridge voltage inverter + full H-bridge diode rectifier
 - Transformer Primary side currents



- The mean value of U_1 must be 0 to control the magnetization current of the transformer
 - The width of positive and negative pulse must be identical in one switching period



- DC/AC/DC Converters:
 - H-bridge voltage inverter + diode rectifier



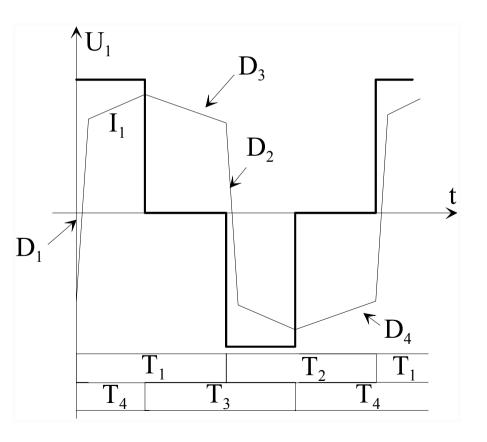
- Equivalent solution compared to the full-bridge rectifier



- DC/AC/DC Converters:
 - H-bridge voltage inverter + diode rectifier:
 - Efficiency:
 - \Rightarrow Conduction losses
 - \Rightarrow Switching losses:
 - Can be reduced if ZVT (Zero Voltage transition) is possible
 - Can be reduced if ZCS (Zero Current switching) is possible
 - Switching process must be analyzed to identify:
 - \Rightarrow If natural ZVT and/or ZCS occur
 - \Rightarrow The devices to add in order to allow ZVT and ZCS

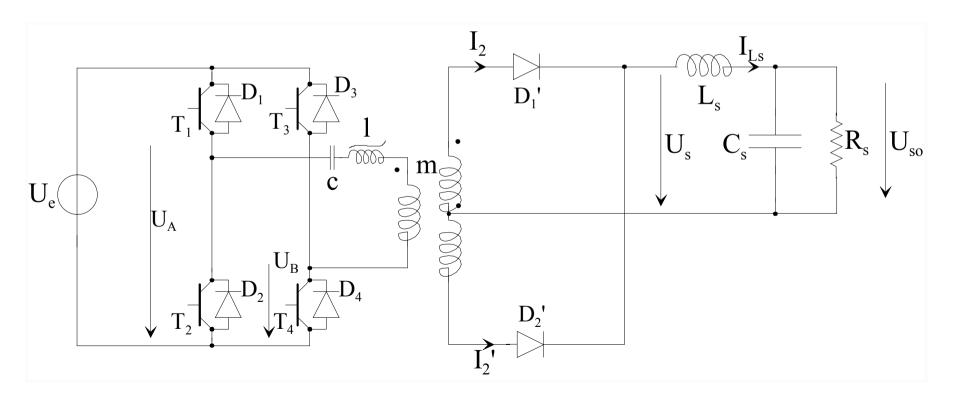


- DC/AC/DC Converters:
 - H-bridge voltage inverter + diode rectifier:
 - Taking into account leakage inductances of the transformer
 - switching cells $(T_3, D_3), (T_4, D_4)$:
 - ZVT thanks to the free-wheeling phase
 - switching cells $(T_1,D_1),(T_2,D_2)$:
 - ZVT only due to the leakage inductances of the transformer



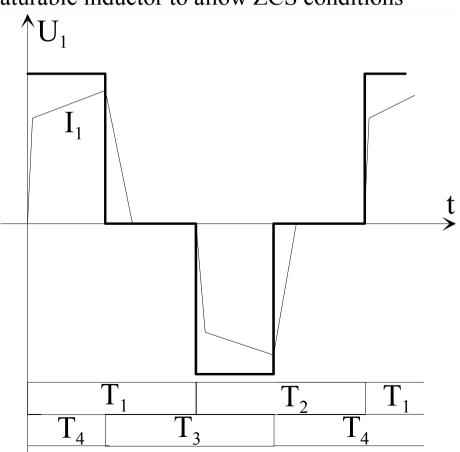


- DC/AC/DC Converters:
 - H-bridge voltage inverter + diode rectifier:
 - Adding a dc blocking capacitor and a saturable inductor to allow ZCS conditions





- DC/AC/DC Converters:
 - H-bridge voltage inverter + diode rectifier:
 - Adding a dc blocking capacitor and a saturable inductor to allow ZCS conditions
 - switching cells $(T_3, D_3), (T_4, D_4)$:
 - Each Turn ON of a transistor is made with ZCS and ZVS conditions
 - Each turn OFF of a transistor, capacitors are needed to limit the du/dt
 - switching cells $(T_1, D_1), (T_2, D_2)$:
 - Each Turn ON of a transistor is made with ZCS conditions
 - Each turn OFF of a transistor is also made with ZCS conditions





- DC/AC/DC Converters:
 - H-bridge voltage inverter + diode rectifier:
 - Adding a dc blocking capacitor and a saturable inductor to allow ZCS conditions ⇒Reduction of switching losses,

 \Rightarrow Components such as IGBTs can be used

 \Rightarrow High voltage, high power applications.