HISTORY
AND
APPLICATIONS
OF
ACCELERATORS

(Presented in 2 lectures)

CAS Varna, September 2010
P.J. Bryant
Contents

- Comment on accelerators
- Pre-accelerator era
- The main history line
- A second history line
- And another history line, but fainter
- Classification by Maxwell
- Status in 1940
- After 1940 in a nutshell…
- Classification of accelerators
- Where to next?
- A closer look at cyclotrons
- Recognising synchrotron lattices
- The FFAG.
Modern accelerators can accelerate particles to speeds very close to that of light.

At low energies, the velocity of the particle increases with the square root of the kinetic energy (Newton).

At relativistic energies, the velocity increases very slowly asymptotically approaching that of light (Einstein).

It is as if the velocity of the particle ‘saturates’.

One can pour more and more energy into the particle, giving it a shorter De Broglie wavelength so that it probes deeper into the sub-atomic world.
What’s in the name?

- What does special relativity tell us, e.g. for an electron?

<table>
<thead>
<tr>
<th>Energy</th>
<th>1 MeV</th>
<th>1 GeV</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta = \frac{v}{c}$</td>
<td>0.95</td>
<td>0.9999999</td>
</tr>
<tr>
<td>$\gamma = \frac{m}{m_0}$</td>
<td>3</td>
<td>7</td>
</tr>
</tbody>
</table>

- Yes, the speed increases, but not as spectacularly as the mass. In fact, it would be more correct to speak of the momentum ($mv$) increasing.

- Ginzton, Hansen and Kennedy* suggested, “Ponderator” or “Mass Agrandiser”, but this did not become fashionable and we are left with ‘Accelerator’.

<100 keV electrons from Wimshurst-type machines:

1895 Lenard electron scattering on gases (Nobel Prize 1905 for work on cathode rays).

1913 Franck and Hertz excited electron shells by electron bombardment.

Few MeV from natural alpha particles:

1906 Rutherford bombards mica sheet with natural alphas.

1919 Rutherford induces a nuclear reaction with natural alphas.
100 years ago physics experimentation was very popular with the general public who often built their own equipment.

*HOW TO MAKE A WIMSHURST MACHINE.*

centre of the diameter of the semicircle. Two similar \( \frac{1}{2} \)-in. holes are also to be put through the centres of the wider extremities of these standards, at 33 ins. up from the shoulders of the tenon. From

Fig. 1.

GUILBERT PITMAN

Cecil Court, St. Martin's Lane, W.C.

1903

CAS_10- P.J. Bryant - History and Applications of Accelerators - 2 lectures - Slide 6
A commercial Wimshurst-type machine
…Rutherford believes that he needs a source of many MeV to continue his research on the nucleus. This is far beyond the electrostatic machines then existing, but in …

- 1928 Gamov predicts ‘tunneling’ and perhaps 500 keV would suffice ????

…and so the first accelerator was built for physics research:

- 1928 Cockcroft & Walton start designing an 800 keV generator encouraged by Rutherford.

- 1932 the generator reaches 700 keV and Cockcroft & Walton split the lithium atom with only 400 keV protons. They received the Nobel Prize in 1951.
The players

- Ernest Rutherford:
  Born 30/8/1871, in Nelson, New Zealand.
  Died 1937.
  Professor of physics at McGill University, Montréal (1898-1907).
  Professor of physics at University of Manchester, UK (1907-1919).
  Professor of experimental physics and Director of the Cavendish Laboratory, University of Cambridge.

- Sir John Douglas Cockcroft:
  Born 27/5/1897, Todmorden, UK.
  Died 1967.

- Ernest Thomas Sinton Walton:
  Born 6/10/1903, Ireland.
Cockcroft & Walton’s generator
Cockcroft-Walton generators became standard equipment

70 MeV Cockcroft-Walton generator supplying the ion source which injected protons into NIMROD, the 7 GeV synchrotron at Rutherford laboratory.
**Van de Graaff, a competitor**

**DC voltage generator:**

Van de Graaff was an American Rhodes scholar in Oxford, UK in 1928 when he became aware of the need for a high-voltage generator. His first machine reached 1.5 MV in Princeton, USA, in the early 1930s.

These generators typically operate at 10 MV and provide stable low-momentum spread beams.

[Robert Van de Graaff 20/12/1901-1967]
DC generators produce conservative fields and the voltage can only be used once for acceleration.

The Tandem van de Graaff is a clever trick to use the voltage twice.
Theory and proof-of-principle:
- 1924 Ising proposes time-varying fields across drift tubes. This is a ‘true’ accelerator that can achieve energies above that given by the highest voltage in the system.
- 1928 Wideröe demonstrates Ising’s principle with a 1 MHz, 25 kV oscillator to make 50 keV potassium ions; the first linac.

And on to a practical device:
- 1929 Lawrence, inspired by Wideröe and Ising, conceives the cyclotron; a ‘coiled’ linac.
- 1931 Livingston demonstrates the cyclotron by accelerating hydrogen ions to 80 keV.
- 1932 Lawrence’s cyclotron produces 1.25 MeV protons and he also splits the atom just a few weeks after Cockcroft & Walton. Lawrence received the Nobel Prize in 1939.
The players

- **Gustaf Ising:**

- **Rolf Wideröe:**
  Born 11/7/1902 in Oslo, Norway.
  Died 1996.
  Also contributed to the fields of power lines and cancer therapy.

- **Ernest Orlando Lawrence:**
A glass envelope made from a flattened flask and silvered on the inside with a single ‘Dee’.
Cyclotron

**Centripetal force**

\[ F = evB = \frac{mv^2}{\rho} \]

**Constant revolution frequency**

\[ f_{\text{rev}} = \frac{v}{2\pi\rho} = \frac{v}{2\pi} \cdot \frac{eB}{mv} = \frac{eB}{2\pi n} \]

**Radius of gyration**

\[ \rho = \frac{mv}{eB} \]
Stanley Livingston and Ernest O. Lawrence (left to right) beside the 27 inch cyclotron at Berkeley circa 1933. The peculiar shape of the magnet’s yoke arises from its conversion from a Poulson arc generator of RF current, formerly used in radio communication.
The first ‘true’ accelerator

Prinzip einer Methode zur Herstellung von Kanalstrahlen hoher Voltzahl.

Von

GUSTAF ISING.

Mit 2 Figuren im Texte.

Mitgeteilt am 12. März 1924 durch C. W. Oseen und M. Siegbahn.

This principle is used in almost all of today’s accelerators. The ions can reach energies above the highest voltage in the system.
The first accelerator proposed by L. Szilard was a linac, appearing in a German patent application entitled "Acceleration of Corpuscles" and filed on 17 December 1928. The Figure shows the proposed layout. Though Szilard writes of "canal rays" in the patent application, he also refers to "corpuscles, e.g. ions or electrons." Considering the low-frequency RF sources available in those days, an apparatus of modest length would have worked only for rather heavy ions.

Leo Szilard was a professional inventor. He dropped the above patent perhaps because of ‘prior art’ by Ising.
Wideröe’s Linac

Wideroe’s first linac
Alvarez Linac

- Alvarez linac – the first practical linac 32 MeV at Berkeley 1946:
  - Particle gains energy at each gap.
  - Drift tube lengths follow increasing velocity.
  - The periodicity becomes regular as $v \Rightarrow c$.
  - His choice of 200 MHz became a de facto standard for many decades.

Luis W. Alvarez was born in San Francisco, CA., on 13/6/1911.
He received the Nobel physics prize in 1968.
Also the birth of a ‘true’ accelerator:

- **1923** Wideröe, a young Norwegian Ph.D. student draws in his laboratory notebook the design of the betatron with the well-known 2-to-1 rule. Two years later he adds the condition for radial stability, but does not publish.

- **1927** in Aachen, Wideröe makes a model betatron, but it does not work. Discouraged he changes course and builds the world’s first linac (see previous history line).

All is quiet until **1940**...

- **1940** Kerst re-invents the betatron and builds the first working machine for 2.2 MeV electrons (University of Illinois).

- **1950** Kerst also builds the world’s largest betatron (300 MeV).
Continuous acceleration – betatron:

Wideröe called this device a “strahlung transformator” because the beam effectively forms the secondary winding on a transformer. The above diagram is taken from his unpublished notebook (1923). This device is insensitive to relativistic effects and is therefore ideal for accelerating electrons. It is also robust and simple. The idea re-surfaced in 1940 with Kerst and Serber, who wrote a paper describing the beam oscillations. Subsequently the term ‘betatron oscillation’ was adopted for these oscillations in all devices.
Betatron
Classification by Maxwell

- Accelerators must use electric fields to transfer energy to/from an ion, because the force exerted by a magnetic field is always perpendicular to the motion.

- Mathematically speaking, the force exerted on an ion is:

\[ F = eE + e(v \times B) \]

so that the rate at which work can be done on the ion is:

\[ F \cdot v = eE \cdot v + e(v \times B) \cdot v \]

but \( (v \times B) \cdot v = 0 \).

- Each ‘history line’ can be classified according to how the electric field is generated and used.
Use of the electric field

\[ E = -\nabla \phi - \frac{\partial A}{\partial t} \]

**Acceleration by DC voltages:**
- Cockcroft & Walton rectifier generator
- Van de Graaff electrostatic generator
- Tandem electrostatic accelerator

**Acceleration by time-varying fields:**
\[ \nabla \times E = -\frac{\partial B}{\partial t} \]

- ‘Betatron’ or ‘unbunched’ acceleration
- ‘Resonant’ or ‘bunched’ acceleration
  - Linear accelerator (linac).
  - Synchrotron.
  - Cyclotron (‘coiled’ linac).
Three acceleration methods had been exploited:

- DC voltage (e.g. Cockcroft and Walton),
- ‘Resonant/bunched’ acceleration (e.g. cyclotron)
- ‘Betatron/unbunched’ acceleration.

Try to think of other possibilities for accelerating ions. *

Progress now turns to applying these basic concepts more efficiently and to improving the technology.

* This is an important question for the future.
1943  Once again, Wideröe is a pioneer and patents **colliding beams** (pub. 1953).

1944  McMillan and Veksler independently propose **synchronous acceleration with phase stability**. They use an electron synchrotron, as example.

1946  Goward and Barnes are first to make the synchrotron work in the UK.

1947  Oliphant and Hyde start a 1 GeV machine in Birmingham, UK, but an American group overtakes them and is first with the 3 GeV Cosmotron at BNL.

1952  Christofilos, and Courant, Livingston and Snyder independently invent **strong focusing**. CERN immediately drops its design for a weak-focusing, 10 GeV FFAG in favour of a strong-focusing, 28 GeV synchrotron.

1956  MURA, US proposes **particle stacking** to increase beam intensity, opening the way for circular colliders.

**Trick Question:** Why did McMillan receive the Nobel Prize and not Veksler?
Components of a synchrotron

The principal machine components of the LEP accelerator:
- Accelerating cavity
- Focusing magnet
- Bending magnet
- Vacuum chamber

Graphs showing:
- Kinematic variables: $f$ or $\beta$, $E$, $p$
- Momentum
- Time or energy
- Time

CAS_10- P.J. Bryant - History and Applications of Accelerators - 2 lectures - Slide 30
More progress...

- 1956  Tigner proposes linear colliders for high-energy electron machines.
- 1961  AdA, an electron-positron storage ring starts operation at Frascati, Italy. This is the first single-ring, particle-antiparticle collider.
- 1966  Budker and Skrinsky propose electron cooling.
- 1970  Kapchinski & Teplyakov propose the RFQ (radiofrequency quadrupole).
- 1971  CERN operates the ISR proton-proton collider. This is the first, particle-particle, intersecting-ring collider.
- 1971  Blewett proposes the twin-bore superconducting magnet design. Now used in LHC.
- 1972  van der Meer invents stochastic beam cooling opening the way for hadron, particle-antiparticle colliders.
- 1978  The CERN ISR operates the first superconducting magnets (quads) to be used in a synchrotron ring. They are industrially built.
And more…

- 1982  CERN converts its SPS to a single-ring proton-antiproton collider.
- 1984 C. Rubbia and S. van der Meer receive the Nobel physics prize for $W$ & $Z$ discoveries.
- 1989  CERN starts LEP, the world’s highest energy electron-positron collider.
- 1991  HERA at DESY becomes the first major facility for colliding protons with electrons or positrons.
- 1995  CERN runs superconducting rf cavities in LEP for physics.
- 1999  RHIC at BNL becomes the world facility for colliding ions.
- 10th September 2008 CERN starts the LHC, the world’s highest energy proton-proton collider (superconducting, twin-bore dipoles).
- 20??  CERN has plans for a TeV linear collider, CLIC.
Livingston chart

Bottom left corner, Milton Stanley Livingston’s original chart from his book “High energy accelerators” 1954.
Classification of accelerators

- **DC voltage generators:**
  - Cockcroft Walton generator.
  - Van de Graaff.
  - Tandem.

- **Unbunched/continuous acceleration:**
  - Betatron.
  - Betatron core.

- **Bunched/resonant acceleration:**
  - RFQ.
  - Linac.
  - Cyclotron, synchrocyclotron.
  - Microtron.
  - FFAG (Fixed Field Alternating Gradient).
  - Synchrotron.

- **Colliders:**
  - Circular (single-ring, particle v anti-particle and intersecting-rings, particle v particle).
  - Linear.

- **Other classifications:**
  - Weak/strong focusing.
  - Normal/superconducting magnets & cavities.
In the beginning there was HEP, but more money now passes through non-HEP applications…

- **Accelerator applications:**
  - Synchrotron light sources.
  - Spallation sources.
  - Isotope production.
  - Radiography.
  - Cancer therapy.
  - Ion implantation and surface metallurgy.
  - Sterilisation.
  - …

- **Proposed accelerator applications:**
  - Inertial fusion drivers.
  - Nuclear incinerators.
  - Rocket motors.
  - …

- **Spin-offs from HEP and accelerators:**
  - PET scanners.
  - NMR scanners.
  - CAT scanners.
  - Superconducting wires, cables and devices.
  - Large-scale UHV systems.
  - Large-scale cryogenic systems.
  - …
**Where to next?**

- Today’s HEP accelerators are nearing practical limits. What can be done?
  - The goal was a new acceleration technique capable of reaching PeV energies and higher with equipment of a practical size.

- Four essential ingredients are:
  - A new acceleration mechanism.
  - Transverse stability.
  - Longitudinal (phase) stability.
  - Stability against collective effects.

- The candidates were:
  - Plasma-beat-wave accelerator.
  - Wake-field accelerator.
  - Lasers with gratings.
  - Lasers on dense bunches.

- But the search is still on for a new HEP accelerator.
How far is beyond?

- The CERN LHC will operate $2 \times 7$ TeV (1 TeV ≡ $10^{12}$ eV) beams in head-on collision.

- Only cosmic rays provide a glimpse of what lies beyond.

- The cosmic ray spectrum is expected to extend up to the Planck energy ($1.22 \times 10^{28}$ eV about $10^{15}$ times higher than the LHC), above which the universe is thought to be opaque.

- The Planck energy is the order of magnitude expected for the energy of a vibrating string in string theory.

- The Planck energy is roughly 2 billion joules, the energy supplied when tanking up a car.
A closer look at cyclotrons

- Cyclotrons started in HEP, but today they are important for their industrial and medical applications.

- The cyclotron’s success is due to its robust and compact design with adequate intensity and quasi-continuous beam.
Cyclotron road map

1932  Lawrence’s first cyclotron works

1930s  Studies on neutron therapy using a cyclotron

Early 1990s  Superconducting cyclotron mounted directly on gantry for neutron therapy

1980s  IBA’s ‘Cyclone 30’ becomes the de facto standard for isotope production

Late 1990s  Cyclotron establishes itself as the proton-therapy standard with passive spreading

2000s  IBA proposes a superconducting machine for 400 MeV/u carbon ions. This machine could displace synchrotrons and take the world market.
**Evolution of cyclotrons**

<table>
<thead>
<tr>
<th>Decade</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1960s to 1970s</td>
<td>Classical isochronous cyclotrons using extraction by electrostatic deflection are limited by heating.</td>
</tr>
<tr>
<td></td>
<td>$\leq 200 , \mu A$ at 10 MeV</td>
</tr>
<tr>
<td>1980s</td>
<td>$H^- , beam$ from internal PIG source gives variable energy and multi-porting, but poor vacuum.</td>
</tr>
<tr>
<td></td>
<td>$\sim 200 , \mu A$ at 42 MeV (TCC Berkeley)</td>
</tr>
<tr>
<td>1987</td>
<td>External, multi-cusp, $H^- , beam$ source. With axial injection and deep valley magnet design</td>
</tr>
<tr>
<td></td>
<td>$500 , \mu A$ at 30 MeV (IBA Cyclone 30)</td>
</tr>
<tr>
<td>1990s</td>
<td>- Cyclone 30 upgrade 1-2 mA</td>
</tr>
<tr>
<td></td>
<td>- Superconducting cyclotrons...</td>
</tr>
</tbody>
</table>

Beam power [kW] | Current [\mu A]
--- | ---
64 | 1000
16 | 500
4  | 250
1  | 125
Cyclones 30 and 235 (courtesy IBA)
Gantry-mounted superconducting deuteron cyclotron for neutron therapy

Harper Hospital, Detroit

H. Blosser et al, Hadrontherapy in Onc, 1994
Recognising synchrotron lattices

Can we recognise the types of lattice and guess the application of a synchrotron from its lattice design?

Lets look at typical examples:
- Early accelerators for physics
- More recent accelerators for physics
- Spallation sources
- Synchrotron light sources
- Cancer therapy machines
An early synchrotron

- 3 GeV proton synchrotron “Saturne” at Saclay. A Van de Graaff injector lies out of view front-right.

- The magnet structure is quasi-continuous because the designers were not skilled in the design of long drift spaces.

- These machines are invariably plain accelerators for physics research with the experiments external to the machine.
A more advanced AG accelerator

- Uses a basic FODO cell with the F and D quads split into 2 units. Between the ‘split’ quadrupoles, the betatron amplitude functions are quasi constant.
- The dipoles are placed between the F quads to have minimum vertical beam size (i.e. min. cost).
- However, the drift spaces are still short.
Controlling dispersion

- The rings shown so far simply repeat a standard cell \( n \) times to reach \( 2\pi \) of bending.
- This works for plain accelerators and often leads to an economical solution in which all quadrupoles for example are powered by a single power converter.
- In more advanced lattices, we would like to have regions with zero dispersion e.g. in RF cavities. This is done in small rings by closing the dispersion in bumps.
- To close a dispersion bump one needs \( 180^\circ \) to \( 360^\circ \) of phase advance in the plane of bending.
- This leads to solutions for rings with two, or three or four or more closed dispersion bumps separated by dispersion-free sections.
- Each closed bump forms a ‘corner’ and the ring looks ‘triangular’ or ‘square’ or ‘pentagonal’ and so on.
A ‘triangular’ ring using a triplet

- A triplet is another possible cell for a ring.
- In this case, the large horizontal phase advance at the centre of the triplet is used to make 3 closed dispersion bumps.
- The ‘waist’ in the vertical betatron amplitude in long straight sections is used for the dipoles. This keeps the aperture requirements and cost down.
\textit{H minus stripping - a special feature of spallation sources}

- Inject H minus
- Unstripped H minus
- Partially stripped $H^0$

Main dipoles

Weak dipoles

\textit{AUSTRON}

Spallation source

\textit{Majority of beam continues on central orbit}
Light source lattice

- Chasman-Greene, double-bend achromat, high-brightness lattice. The aim is to minimise $D_x(s)$ and $\beta_x(s)$ in the dipoles.

- Each cell supports a closed dispersion bump. There are 4 bumps making a ‘square’ ring.
A medical synchrotron

- The PIMMS medical synchrotron is an example of a lattice customised for a particular use.
- Injection and extraction use electrostatic septa for quasi continuous operation.
- The long straight sections have zero dispersion for rf cavities and minimum beam size at injection/extraction.
- Phase advances are designed for the slow extraction.
Large rings

- Large rings, such as the LHC, often have a basic FODO cell in the arcs.
- The overall ring has an $n$-fold symmetry containing the $n$-arcs and $n$ straight regions in which the physics experiments are mounted.
- Between the arcs and the straight regions there is the so-called dispersion suppressor that brings the dispersion function to zero in the straight region in a controlled way. There are several schemes for dispersion suppressors (see one example on next slide).
- The straight regions contain the injection and extraction and the RF cavities, which, in an electron machine like LEP, can occupy hundreds of metres.
- A dispersion-free straight region may also contain a low-$\beta$ insertion for physics.
The lattice functions of the missing-magnet suppressor for a 60° FODO cell. Note how $\beta_x$ and $\beta_z$ hardly ‘notice’ the suppression of $D_x$. 

### Missing-magnet suppressor: Lattice Functions for a 60° FODO Cell

- **Horizontal betatron function**
- **Vertical betatron function**
- **Horizontal dispersion function**
- **Vertical dispersion function**

### Table: Lattice Elements (G-a-Axis)

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>PO</td>
<td>QUAD</td>
<td>1.0000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>-0.103513</td>
</tr>
<tr>
<td>2</td>
<td>mD</td>
<td>DRIFT</td>
<td>1.0000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.000000</td>
</tr>
<tr>
<td>3</td>
<td>Dipole</td>
<td>BEND</td>
<td>7.0000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.01500</td>
<td>0.01500</td>
<td>0.000004</td>
</tr>
<tr>
<td>4</td>
<td>mD</td>
<td>DRIFT</td>
<td>1.0000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.000000</td>
</tr>
<tr>
<td>5</td>
<td>PO</td>
<td>QUAD</td>
<td>1.0000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.00000</td>
<td>0.103513</td>
</tr>
</tbody>
</table>

- **Δ\(\mu_x\) = 60°**
- **2 missing dipoles**
- **Arc**
- **Zero dispersion straight section**

---

CAS_10- P.J. Bryant - History and Applications of Accelerators - 2 lectures - Slide 52
FFAG = Fixed Field Alternating Gradient

FFAGs are experiencing a rebirth, since their conception in the 1950s.

One could describe them as a solution looking for an application.

FFAGs have a large “momentum acceptance” when considered as a single aperture fixed-field magnet, but a small “momentum range” when considered as an accelerator. Fast cycling synchrotrons can approach a range of 1:10, while slow ramping synchrotrons can approach a ratio of 1:20, whereas FFAGs may approach a range of 1:5.