



# Accelerators for Newcomers

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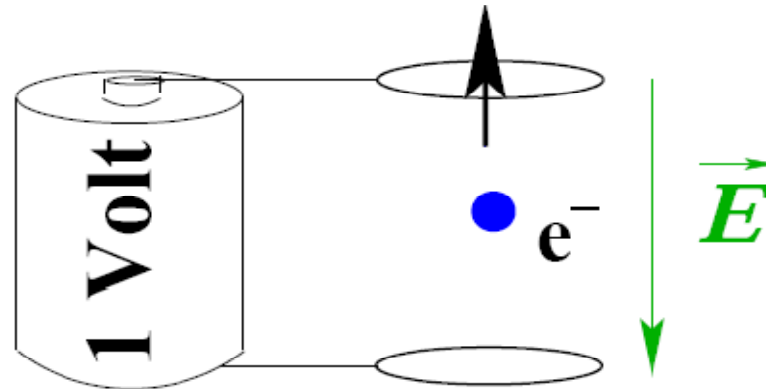
# Why this Introduction?

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- During this school, you will learn about **beam dynamics** in a rigorous way...
- but some of you are completely new to the field of accelerator physics.
- It seemed therefore justified to start with the introduction of a few very **basic concepts**, which will be used throughout the course.

This is a completely **intuitive approach** (no mathematics) aimed at highlighting the physical concepts, without any attempt to achieve any scientific derivation.

# Units: the electronvolt (eV)



The **electronvolt (eV)** is the energy gained by an electron travelling, in vacuum, between two points with a voltage difference of 1 Volt.  $1 \text{ eV} = 1.602 \cdot 10^{-19} \text{ Joule}$

We also frequently use the electronvolt to express masses from  $E=mc^2$ :  $1 \text{ eV}/c^2 = 1.783 \cdot 10^{-36} \text{ kg}$



# Beam Dynamics (1)

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In order to describe the motion of the particles, each particle is characterised by:

- Its azimuthal position along the machine:  $s$
- Its momentum:  $p$
- Its horizontal position:  $x$
- Its horizontal slope:  $x'$
- Its vertical position:  $y$
- Its vertical slope:  $y'$

i.e. a sixth dimensional phase space

$(s, p, x, x', y, y')$



## Beam Dynamics (2)

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- In an accelerator designed to operate at the energy  $E_{nom}$ , all particles having  $(s, E_{nom}, 0, 0, 0, 0)$  will happily fly through the center of the vacuum chamber without any problem. These are “ideal particles”.
- The difficulties start when:
  - one introduces **dipole magnets**
  - the energy  $E \neq E_{nom}$  or  $(p-p_{nom}/p_{nom}) = \Delta p/p_{nom} \neq 0$
  - either of  $x, x', y, y' \neq 0$



# Basic problem:

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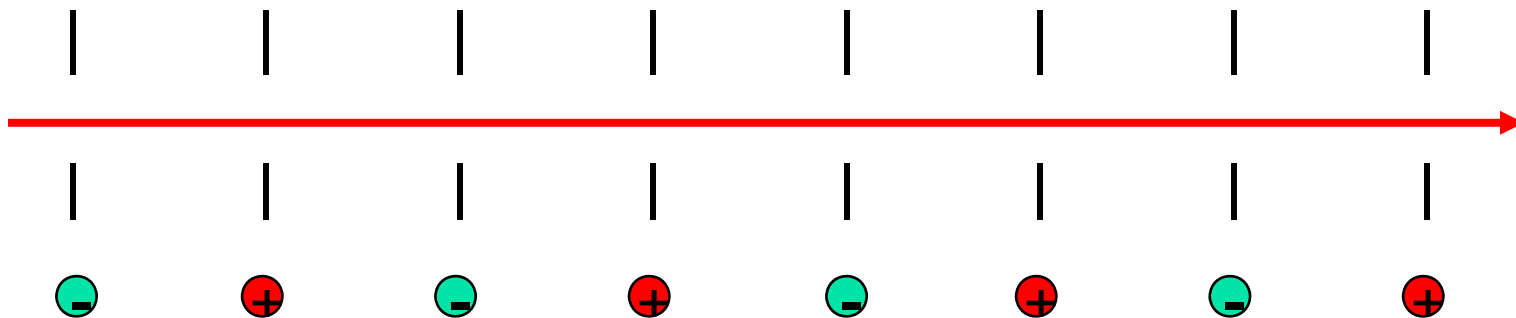
With more than  $10^{10}$  particles per bunch, most of them will **not** be **ideal particles**, i.e. they are going to be lost !

Purpose of this lecture: how can we keep the particles in the machine ?

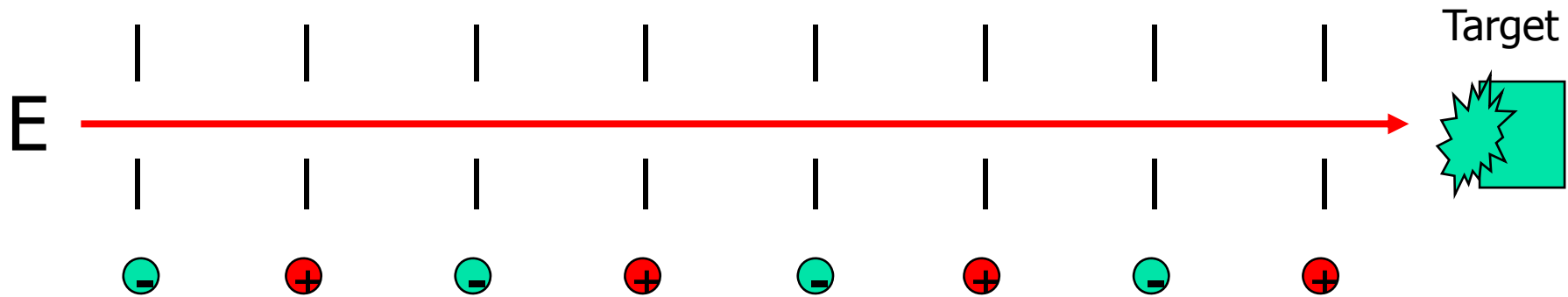
# What is a Particle Accelerator?

➤ a machine to accelerate some particles ! **How is it done ?**

➤ Many different possibilities, but rather easy from the general principle:



# Ideal linear machines (linacs)



$$\text{Available Energy : } E_{c.m.} = m \cdot (2+2\gamma)^{1/2} = (2m \cdot (m+E))^{1/2}$$

with  $\gamma = E/E_0$

Advantages: Single pass

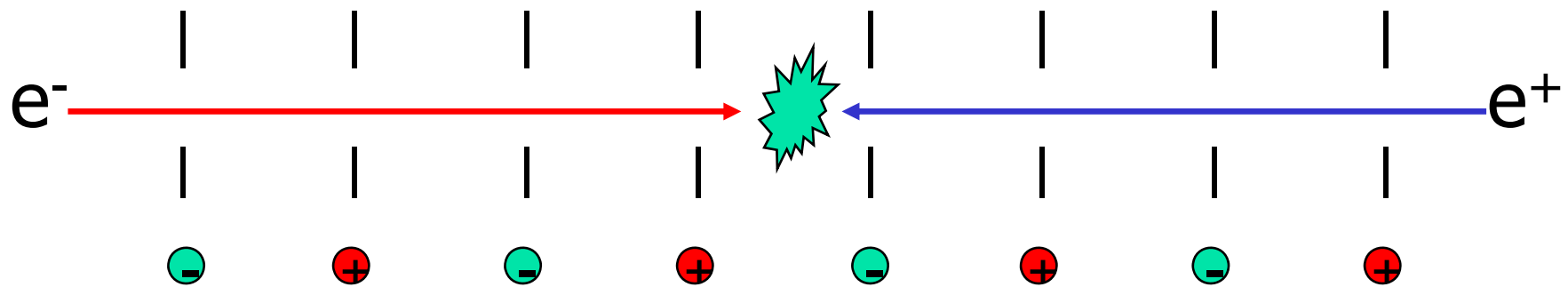
High intensity

Drawbacks: Single pass

Available Energy



# Improved solution for $E_{c.m.}$



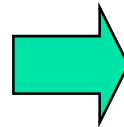
Available Energy :  $E_{c.m.} = 2m\gamma = 2E$   
with  $\gamma = E/E_0$

Advantages: High intensity

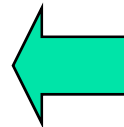
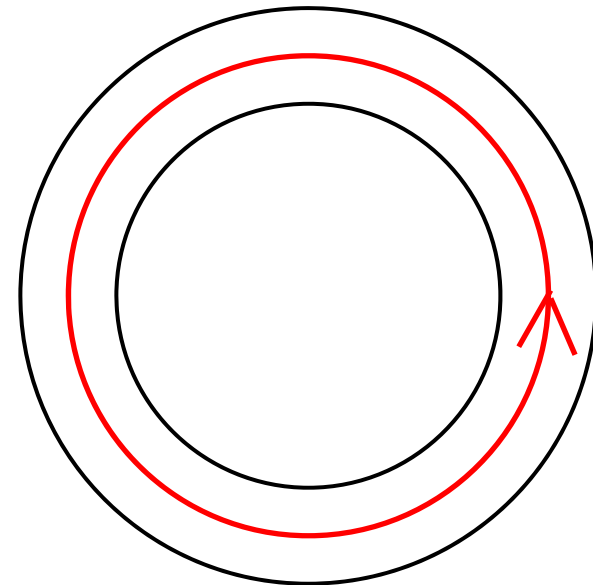
Drawbacks: Single pass  
Space required

# Keep particles: circular machines

Basic idea is to keep the particles in the machine for many turns.  
Move from the linear design

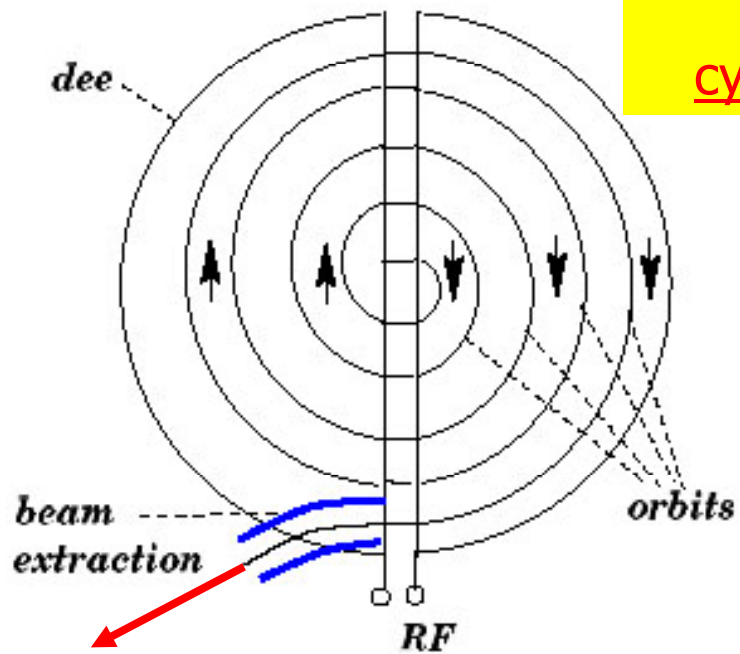


To a circular one:



- Need Bending
- Need **Dipoles!**

# Circular machines ( $E_{c.m.} \sim (mE)^{1/2}$ )



fixed target:

cyclotron

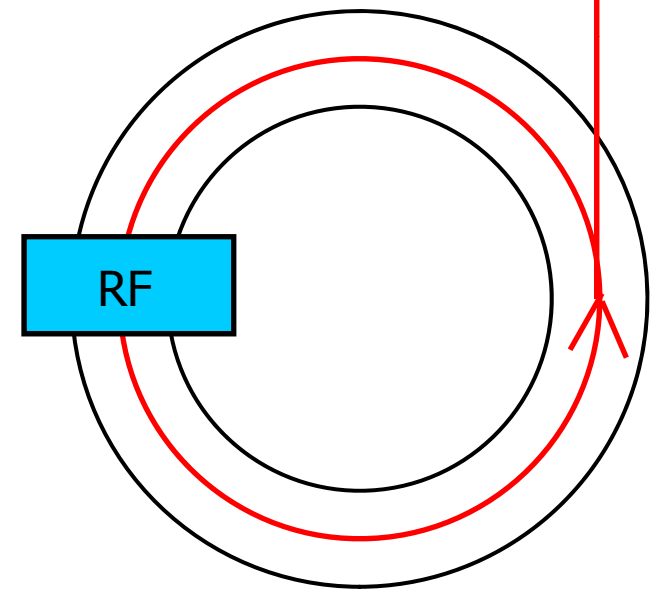
huge dipole, compact design,

$B = \text{constant}$

low energy, single pass.

fixed target:

synchrotron

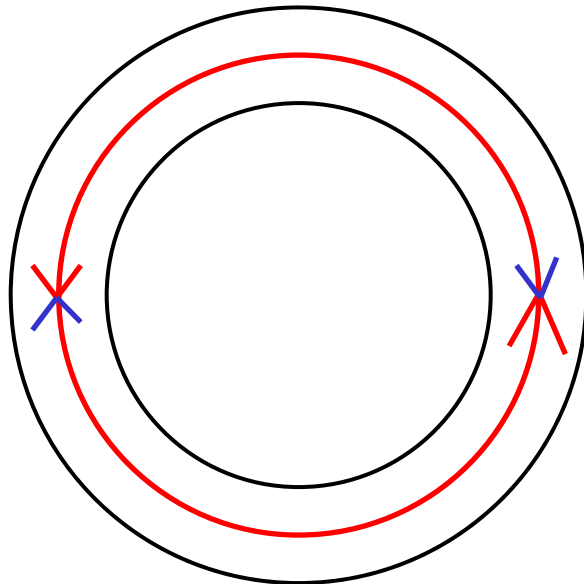


varying  $B$ , small magnets, high energy

# Colliders ( $E_{c.m.} = 2E$ )

## Colliders:

electron – positron  
proton - antiproton

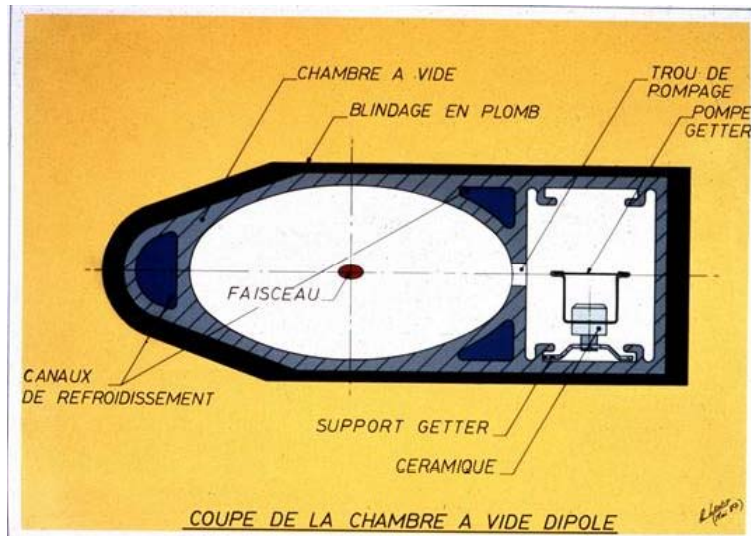


Colliders with the same type of particles (e.g. p-p) require two separate chambers. The beam are brought into a common chamber around the interaction regions

Ex: LHC

8 possible interaction regions  
4 experiments collecting data

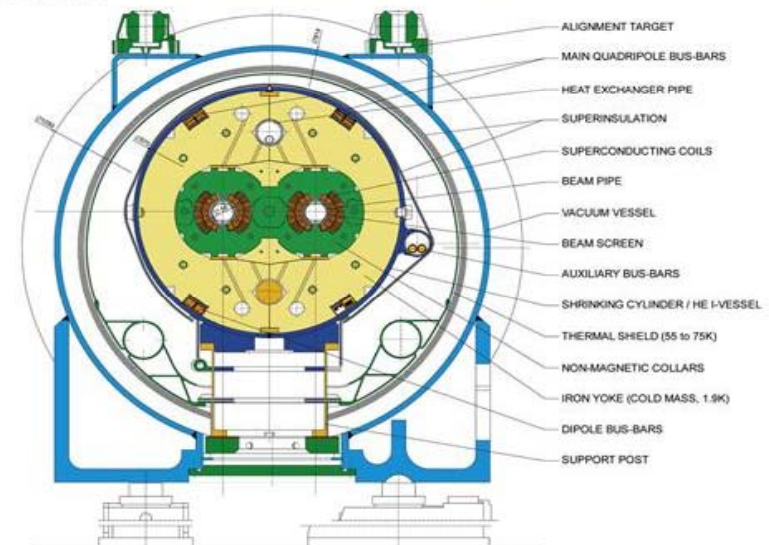
# Colliders ( $e^+ - e^-$ ) et ( $p - p$ )



LEP

LHC

## LHC DIPOLE : STANDARD CROSS-SECTION



# Circular machines: Dipoles

Classical mechanics:

Equilibrium between two forces

Lorentz force

Centrifugal force

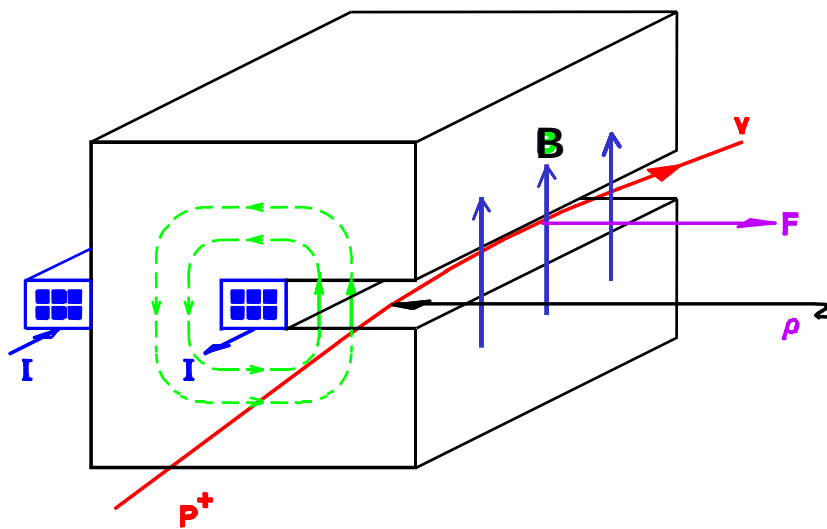
$$F = e \cdot (\underline{v} \times \underline{B})$$

$$F = mv^2/\rho$$

$$evB = mv^2/\rho$$

Magnetic rigidity:

$$B\rho = mv/e = p/e$$

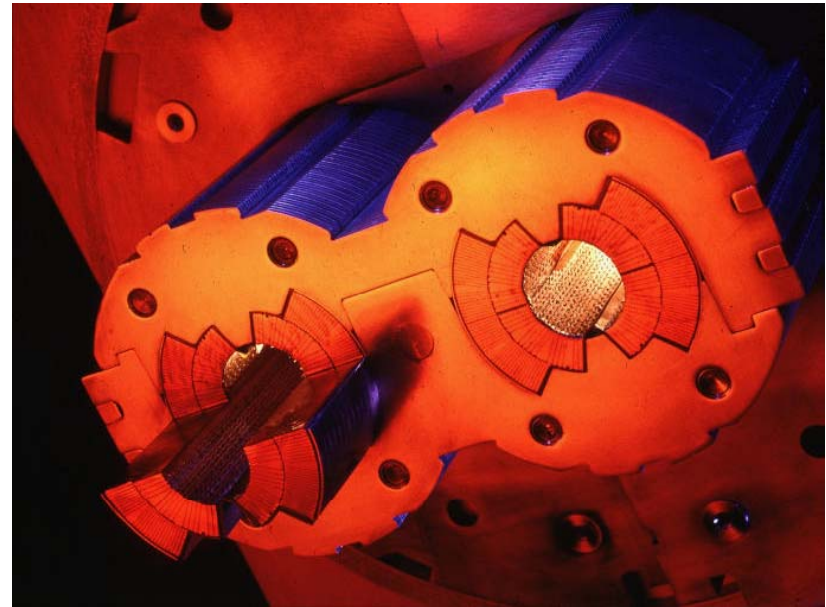


$$p = m_0 \cdot c \cdot (\beta\gamma)$$

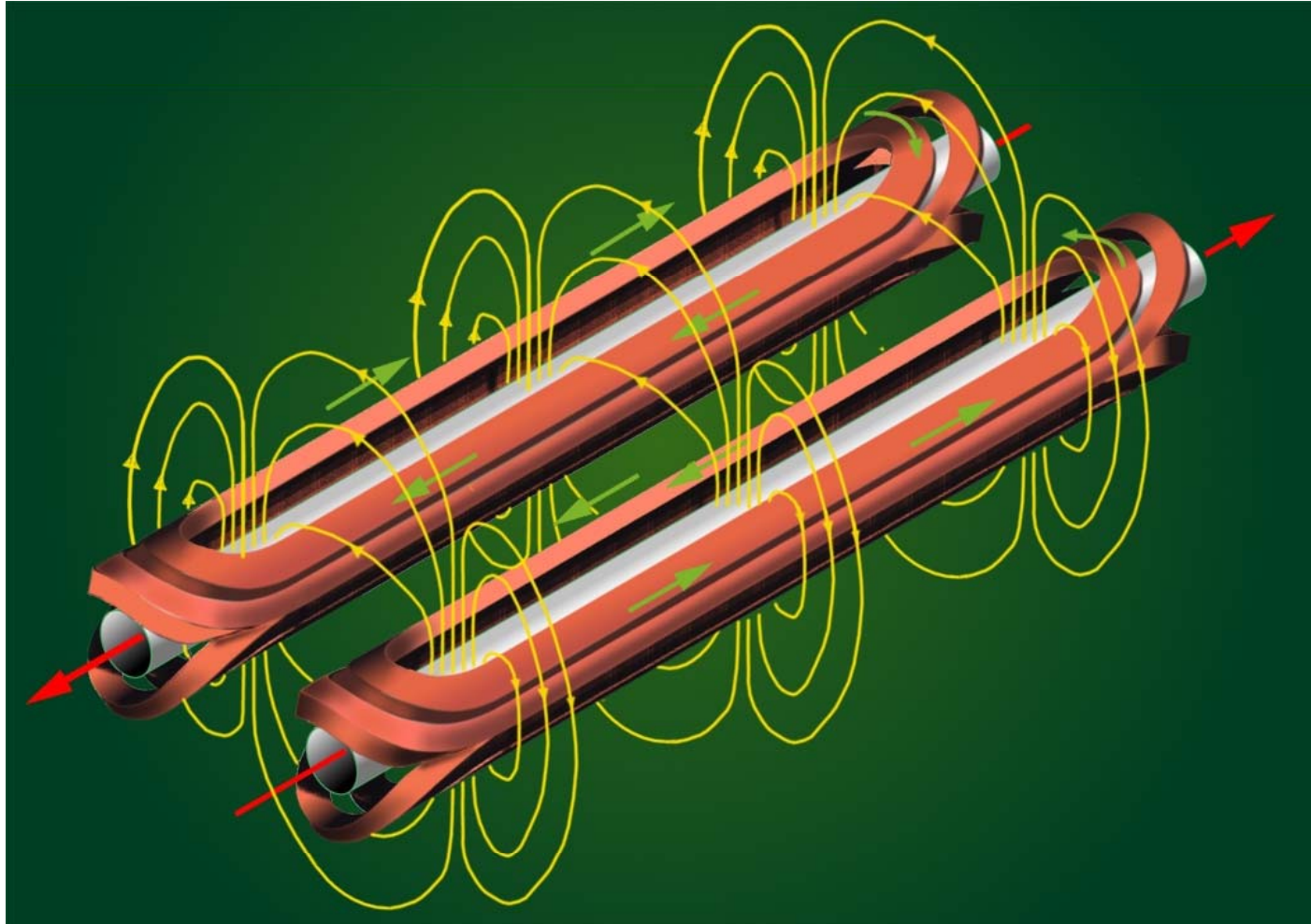


Relation also holds for relativistic case provided the classical momentum  $mv$  is replaced by the relativistic momentum  $p$

# Dipoles (1):



## Dipoles (2):

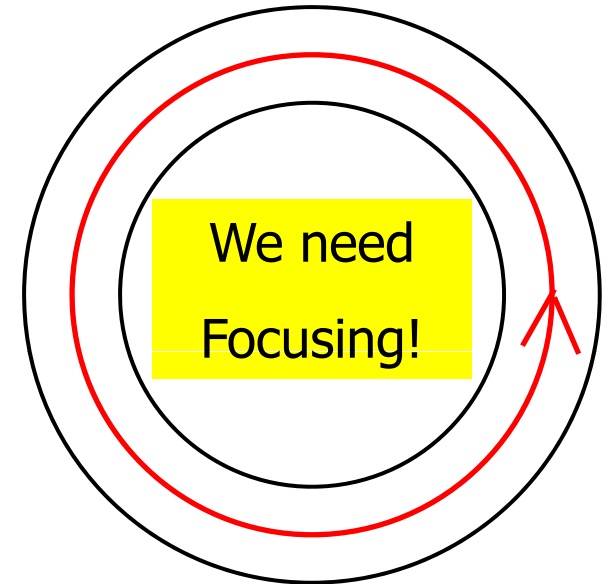




# Ideal circular machine:

- Neglecting radiation losses in the dipoles
- Neglecting gravitation

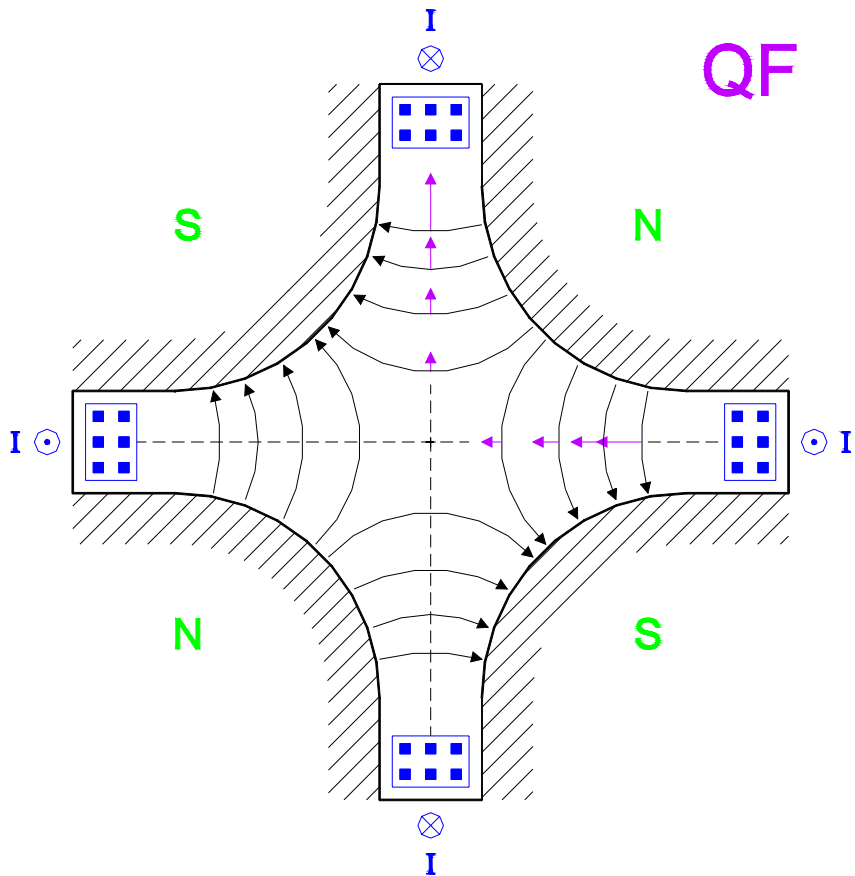
ideal particle would happily circulate on axis in the machine for ever!



Unfortunately: real life is different!

Gravitation: $\Delta y = 20$ mm in 64 msec!	
Alignment of the machine	Limited physical aperture
Ground motion	Field imperfections
Energy error of particles <b>and/or</b> $(x, x')_{inj} \neq (x, x')_{nominal}$	
Error in magnet strength (power supplies and calibration)	

# Focusing with quadrupoles



$$F_x = -g \cdot x$$

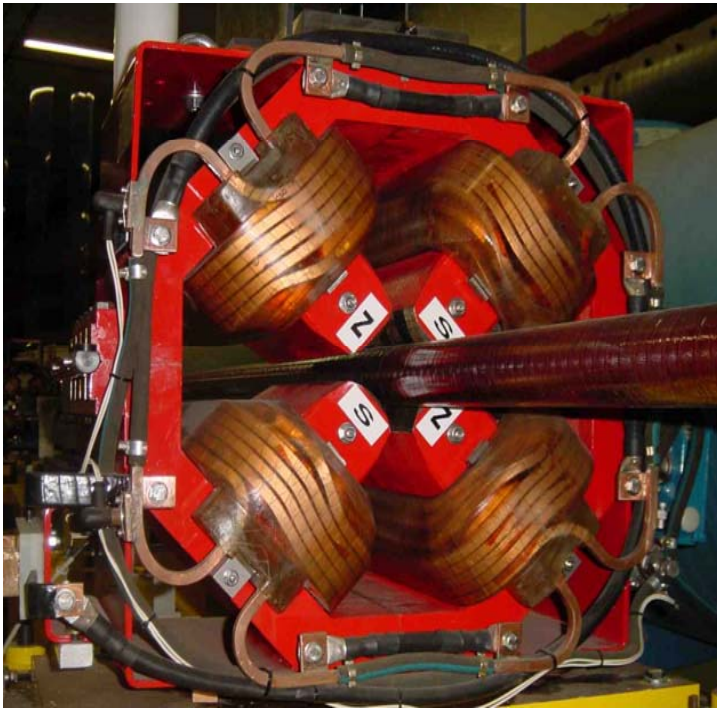
$$F_y = g \cdot y$$

Force increases **linearly** with displacement.

Unfortunately, effect is **opposite** in the two planes (H and V).

Remember: **this** quadrupole is **focusing** in the **horizontal** plane but **defocusing** in the **vertical** plane!

# Quadrupoles:





# Focusing properties ...

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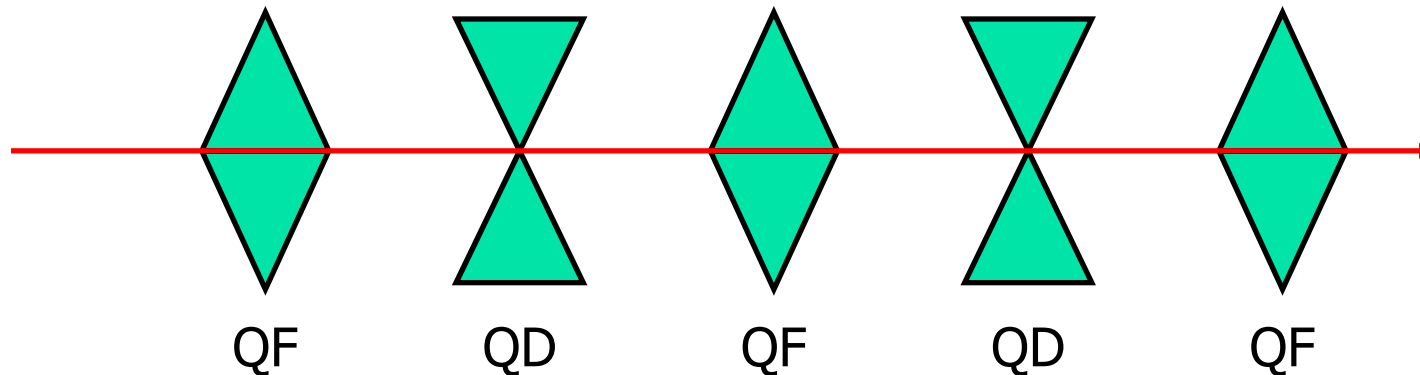
A quadrupole provides the required effect in one plane...

but the opposite effect in the other plane!

Is it really interesting ?

# Alternating gradient focusing

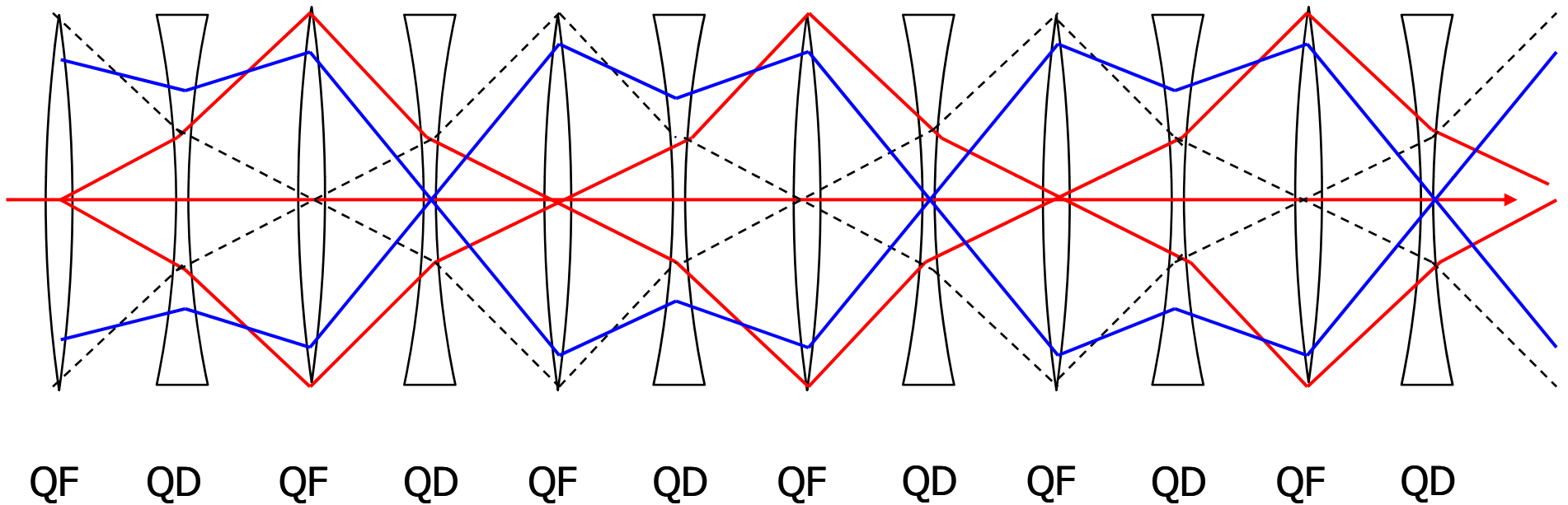
Basic new idea:  
Alternate QF and QD



valid for one plane only (H or V) !



# Alternating gradient focusing





# Alternating gradient focusing:

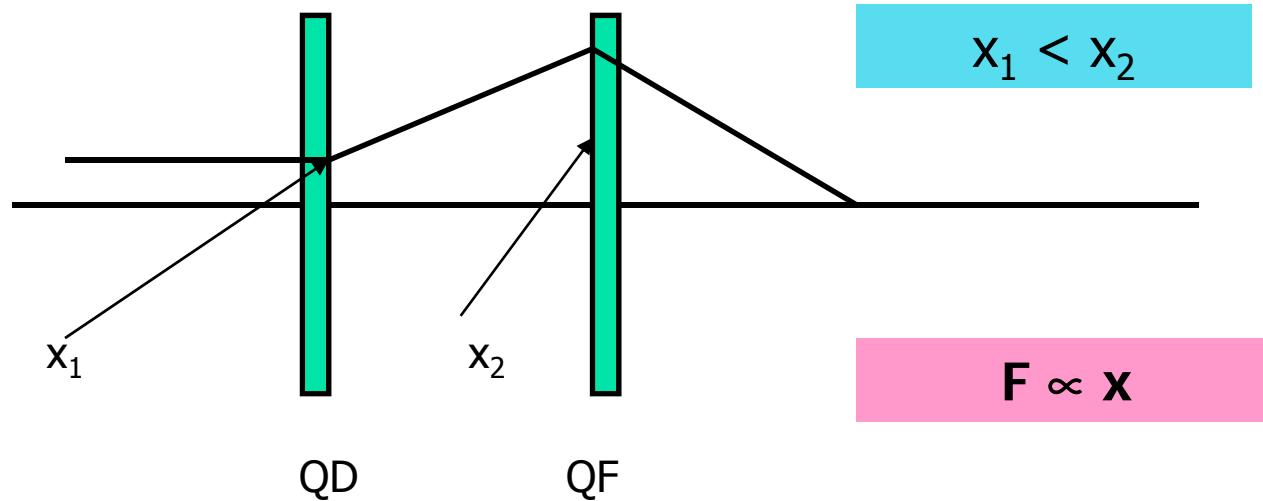
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Particles for which  $x, x', y, y' \neq 0$  thus oscillate around the ideal particle ...

but the trajectories remain inside the vacuum chamber !

# Why net focusing effect?

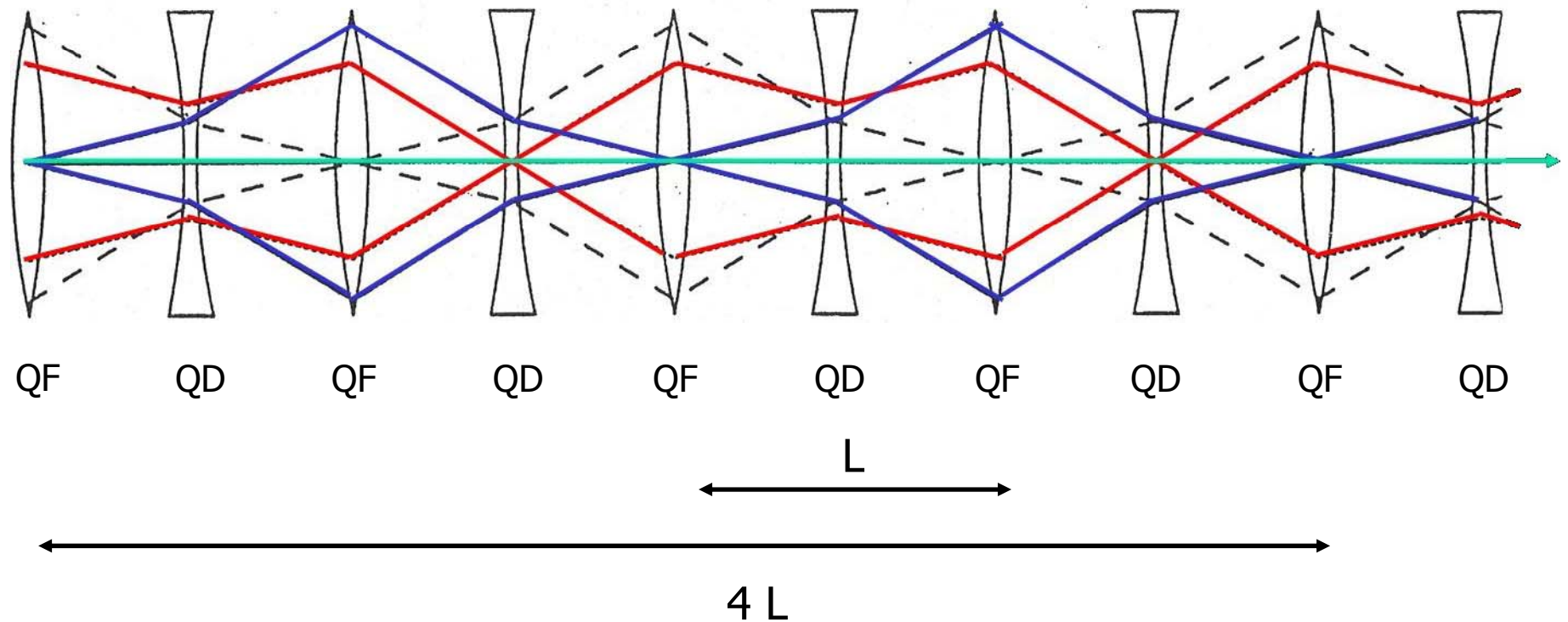
Purely intuitively:



Rigorous treatment rather straightforward !



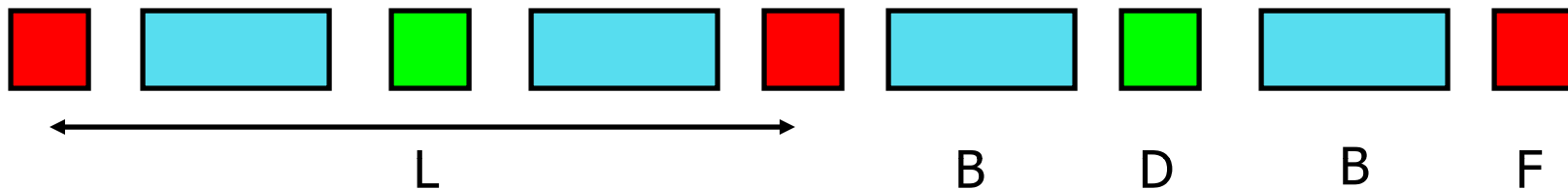
# The concept of the « FODO cell »



One complete oscillation in 4 cells  $\Rightarrow 90^\circ / \text{cell} \Rightarrow \mu = 90^\circ$

# Circular machines (no errors!)

The accelerator is composed of a **periodic** repetition of **cells**:



➤ The phase advance per cell  $\mu$  can be modified, in each plane, by varying the strength of the quadrupoles.

➤ The ideal particle will follow a **particular** trajectory, which **closes on itself** after one revolution: **the closed orbit**.

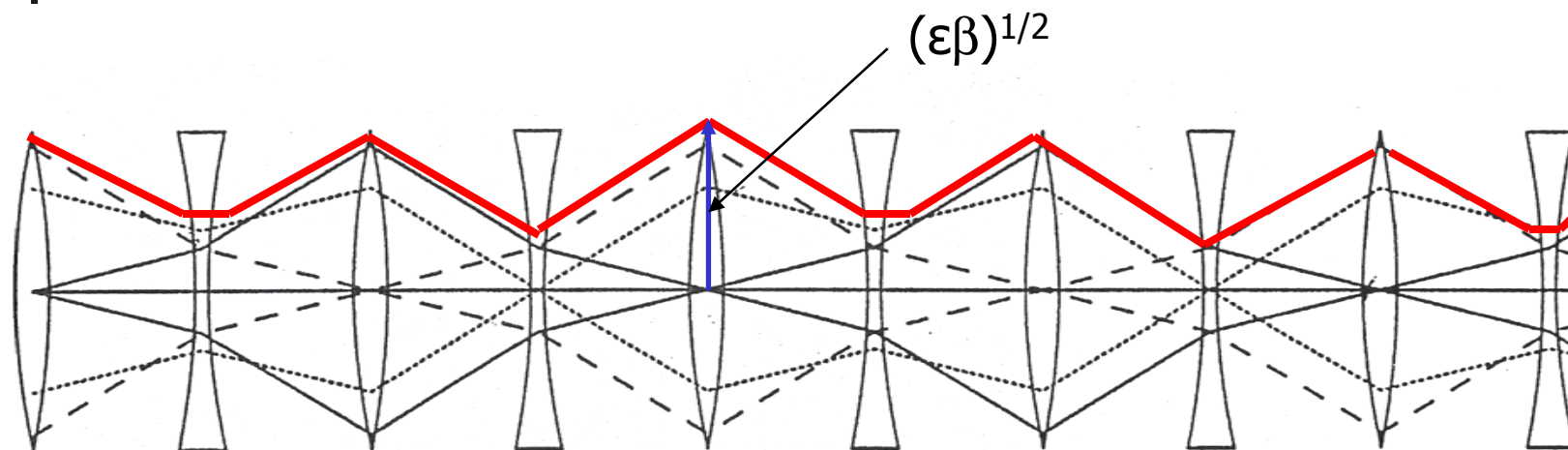
➤ The real particles will perform oscillations **around the closed orbit**.

➤ The number of **oscillations for a complete revolution** is called the **Tune Q** of the machine ( $Q_x$  and  $Q_y$ ).

# Regular periodic lattice: The Arc



# The beta function $\beta(s)$



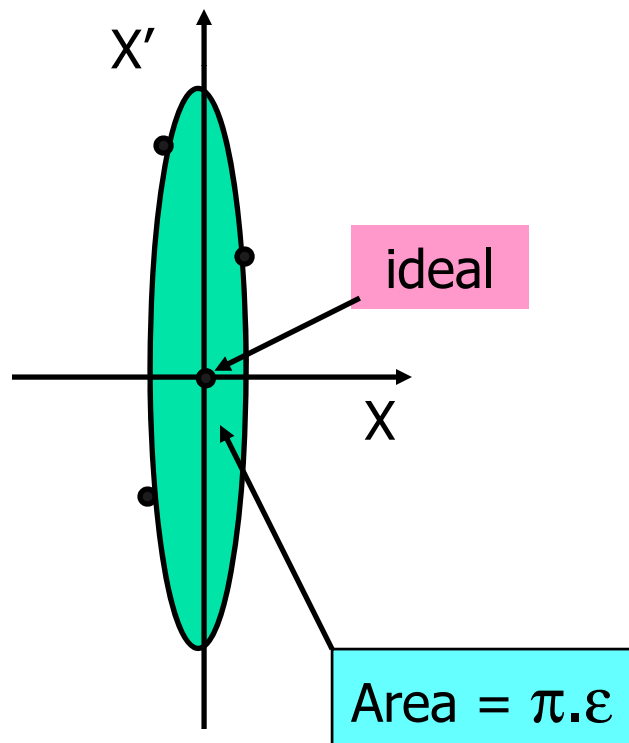
The  $\beta$ -function is the **envelope** around all the trajectories of the particles circulating in the machine.

The  $\beta$ -function has a **minimum at the QD** and a **maximum at the QF**, ensuring the net focusing effect of the lattice.

It is a **periodic function** (repetition of cells). The oscillations of the particles are called **betatron motion** or **betatron oscillations**.

# Phase space at some position (s)

- Select the particle in the beam with the **largest betatron motion** and plot its **position vs. its phase** (x vs. x') at some location in the machine for many turns.

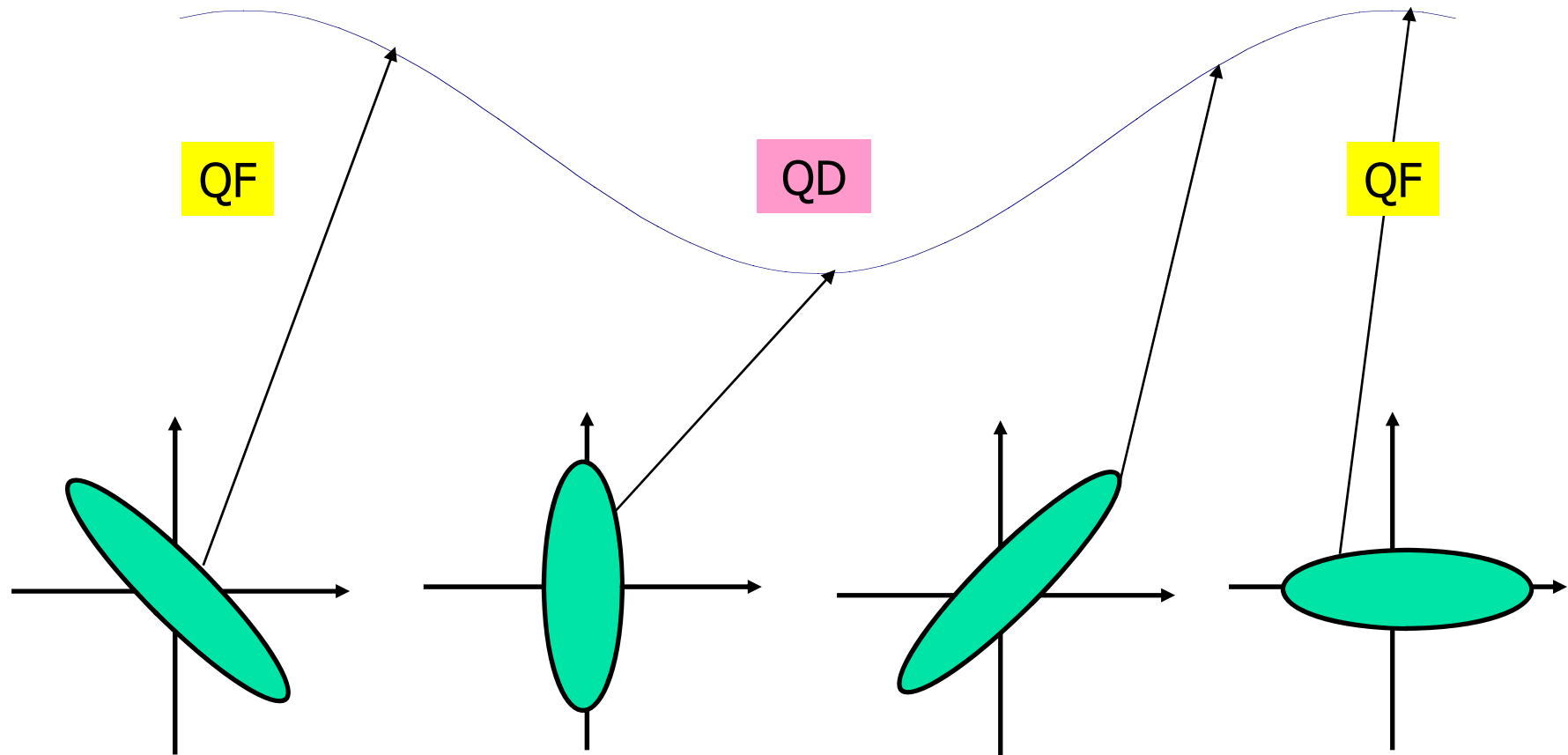


- $\epsilon$  Is the emittance of the beam [ $\pi$  mm mrad]
- $\epsilon$  is a **property of the beam** (quality)
- Measure of how much particle depart from ideal trajectory.
- $\beta$  is a **property of the machine** (quadrupoles).

Beam size [m]

$$\sigma(s) = (\epsilon \cdot \beta(s))^{1/2}$$

# Emittance conservation



The shape of the ellipse varies along the machine, but its area (the emittance  $\epsilon$ ) remains constant for a given energy.



# Recapitulation 1

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- The fraction of the oscillation performed in a periodic cell is called the phase advance  $\mu$  per cell (x or y).
- The total number of oscillations over one full turn of the machine is called the betatron tune  $Q$  (x or y).
- The envelope of the betatron oscillations is characterised by the beta function  $\beta(s)$ . This is a property of the quadrupole settings.
- The quality of the (injected) beam is characterised by the emittance  $\epsilon$ . This is a property of the beam and is invariant around the machine.
- The r.m.s. beam size (measurable quantity) is  $\sigma = (\beta \cdot \epsilon)^{1/2}$ .



# Off momentum particles:

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- These are “non-ideal” particles, in the sense that they do not have the right energy, i.e. all particles with  $\Delta p/p \neq 0$

What happens to these particles when traversing the magnets ?



# Off momentum particles ( $\Delta p/p \neq 0$ )

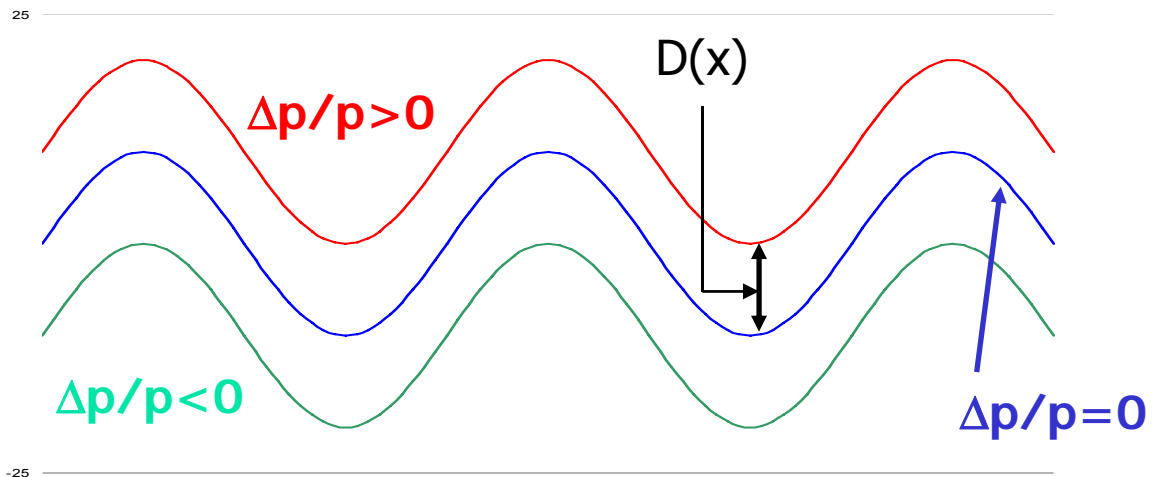
## Effect from Dipoles

➤ If  $\Delta p/p > 0$ , particles are **less** bent in the dipoles → should spiral out !

➤ If  $\Delta p/p < 0$ , particles are **more** bent in the dipoles → should spiral in !

**No!**

There is an equilibrium with the restoring force of the quadrupoles

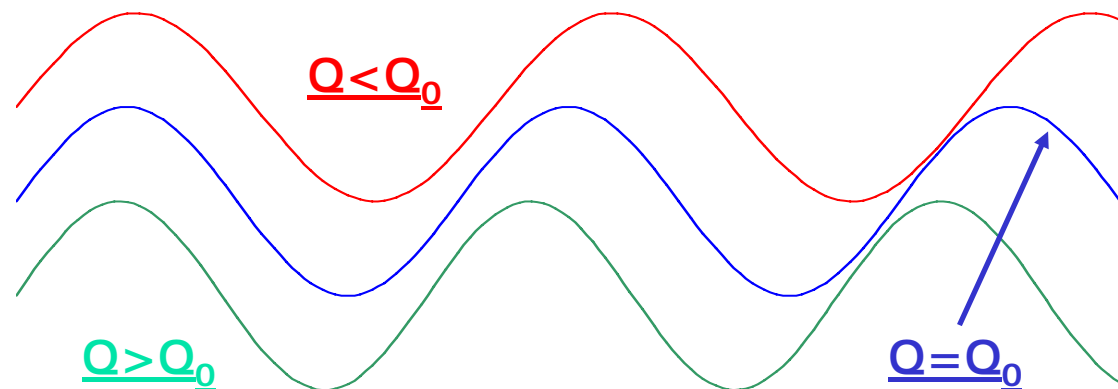


# Off momentum particles ( $\Delta p/p \neq 0$ )

## Effect from Quadrupoles

- If  $\Delta p/p > 0$ , particles are **less** focused in the quadrupoles → **lower Q !**
- If  $\Delta p/p < 0$ , particles are **more** focused in the quadrupoles → **higher Q !**

Particles with different momenta would have a different **betatron tune**  $Q=f(\Delta p/p)$ !





# The chromaticity $Q'$

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Particles with different momenta ( $\Delta p/p$ ) would thus have different tunes  $Q$ .  
So what ?

unfortunately

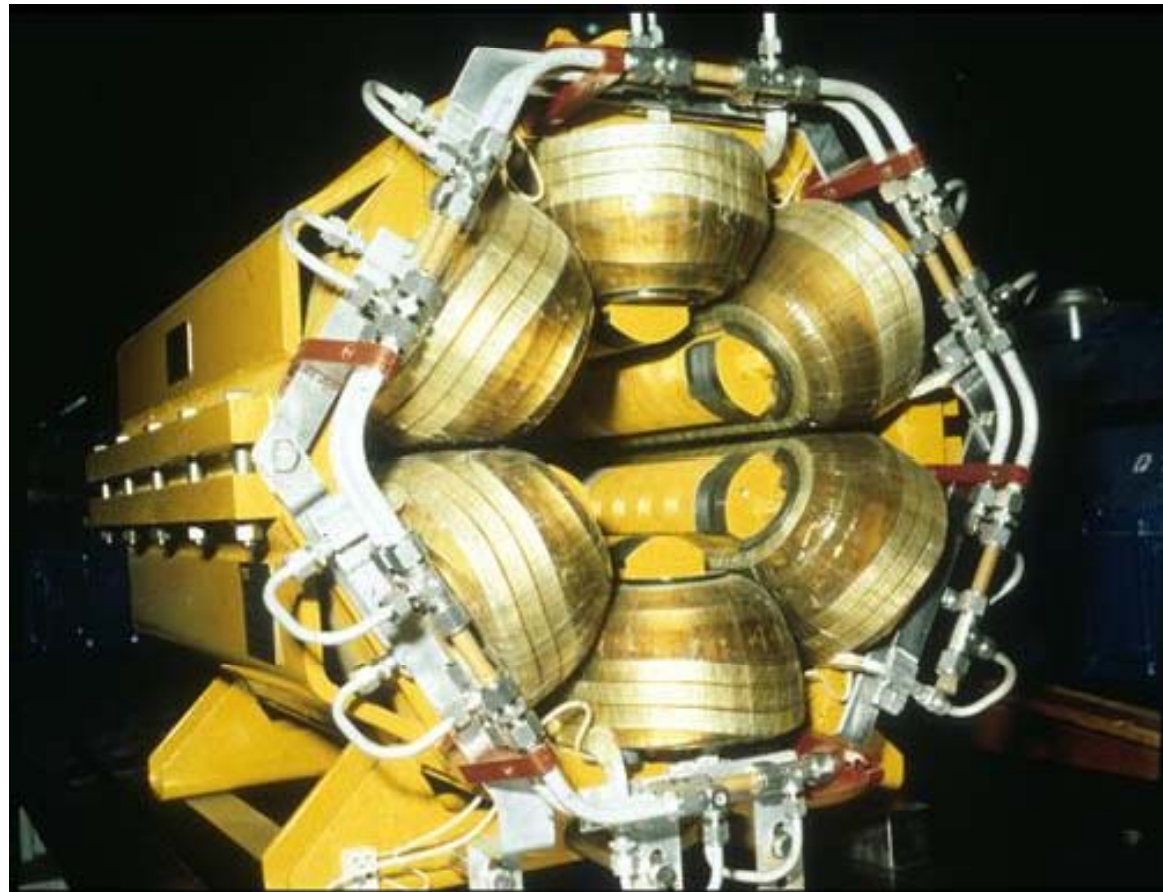
- The tune dependence on momentum is of **fundamental** importance for the **stability** of the machine. It is described by the **chromaticity** of the machine  $Q'$ :

$$Q' = \Delta Q / (\Delta p/p)$$

The chromaticity has to be carefully **controlled and corrected** for stability reasons. This is achieved by means of sextupoles.

# Sextupoles:

SPS





# Recapitulation 2

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- For off momentum particles ( $\Delta p/p \neq 0$ ), the magnets induce other important effects, namely:
  - The dispersion (dipoles)
  - The chromaticity (quadrupoles)



# Longitudinal plane

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➤ So far, we considered only the motion in the transverse planes from an intuitive point of view. The corresponding rigorous treatment will be given in the lectures on “Transverse Beam Dynamics”.

➤ The lectures on “Longitudinal Beam Dynamics” will explain the details of the corresponding longitudinal motion as well as the RF acceleration of the particles.



# The course:

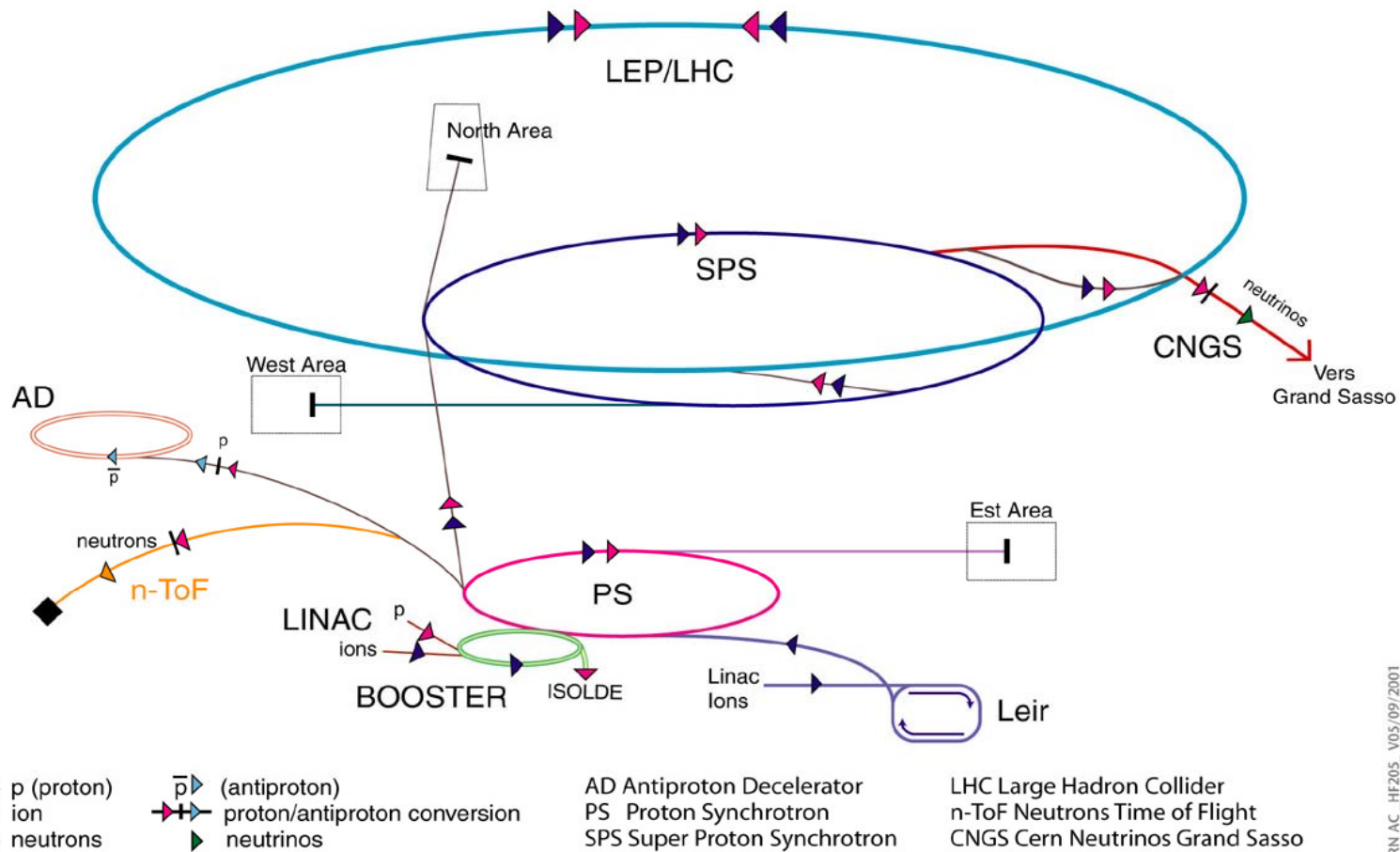
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Beam Dynamics is certainly a “core” topic of accelerator physics, but the objective of this course is to give you a broader introduction covering:

- Relativity and E.M. Theory                      History, physics and applications
- Particle sources                                      Injection, Extraction
- Transfer Lines                                        Magnets
- Beam Diagnostics                                  Apertures
- Linear Imp. and Resonances                      Vacuum
- Synchrotron Radiation, Electron Dynamics, SLS, FELs
- Multi particle Effects                                Numerical Tools

# An Accelerator Complex...

## Accelerator chain of CERN (operating or approved projects)



CERN AC\_HF205\_V05/09/2001