

THE COCKCROFT INSTITUTE *of*
ACCELERATOR SCIENCE AND TECHNOLOGY

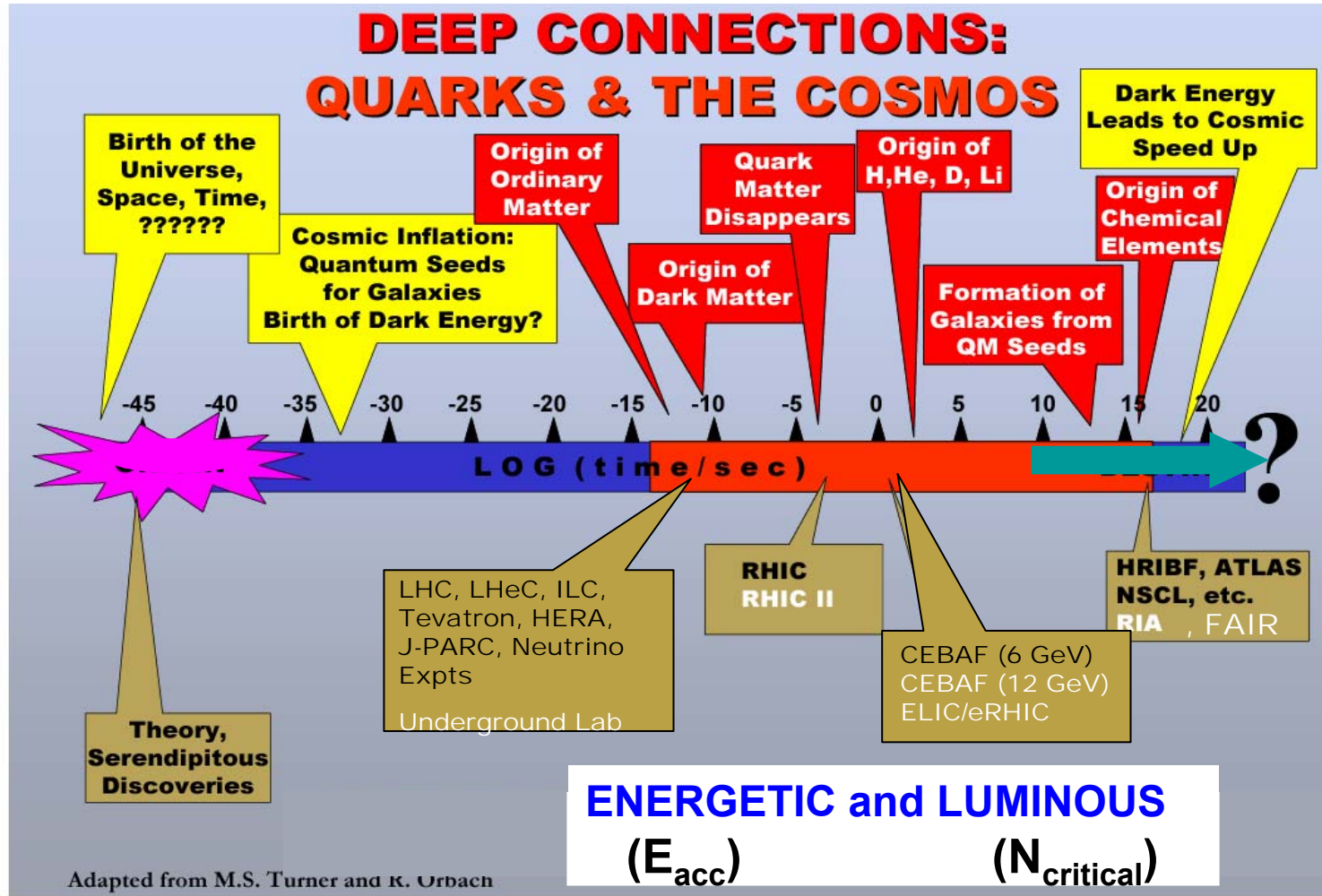
Particle Accelerators and Their Reach for Science: Present and Future

Swapan Chattopadhyay
Cockcroft Institute



Science and Instruments of Discovery and Innovation: Structures and Forces

Accelerator-driven Intense Charged Particle Beams serve Sciences from the Sub-atomic to the Cosmic



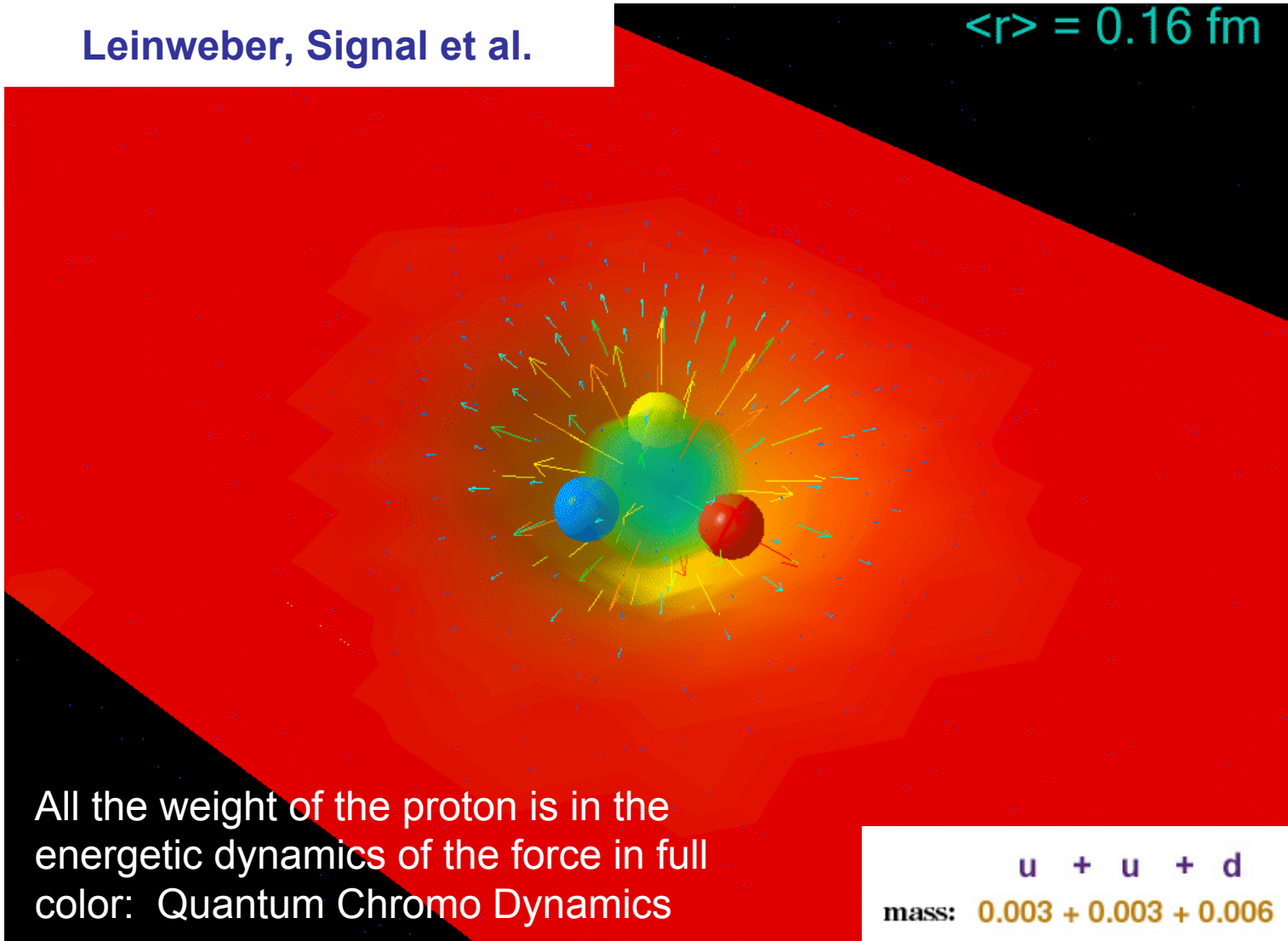
Leinweber, Signal et al.

$$\langle r \rangle = 0.16 \text{ fm}$$

$$E=mc^2$$

All the weight of the proton is in the energetic dynamics of the force in full color: Quantum Chromo Dynamics

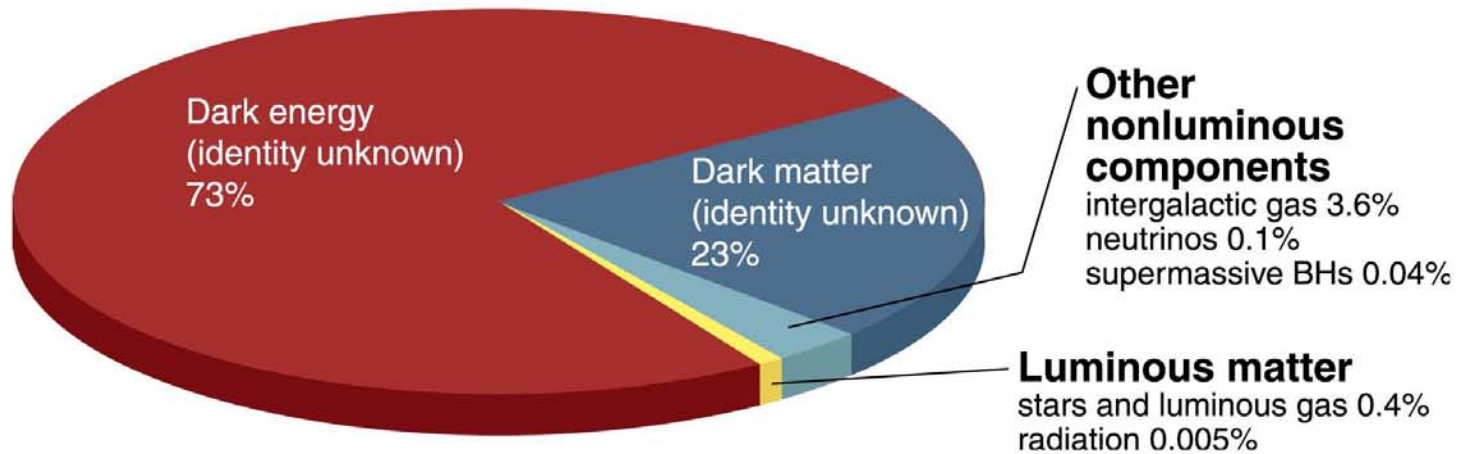
$$\begin{array}{l} u + u + d = \text{proton} \\ \text{mass: } 0.003 + 0.003 + 0.006 \neq 0.938 \end{array}$$

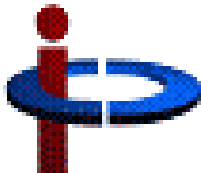


The cosmological inventory is now well-delineated

AXION

- But we know neither what the “dark energy” or the “dark matter” is
- A particle relic from the Big Bang is strongly implied for DM
 - WIMPs ?
 - Axions ?





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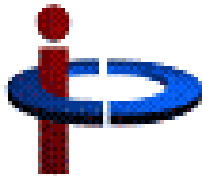


1st cyclotron, ~1930 E.O. Lawrence
11-cm diameter
1.1 MeV protons

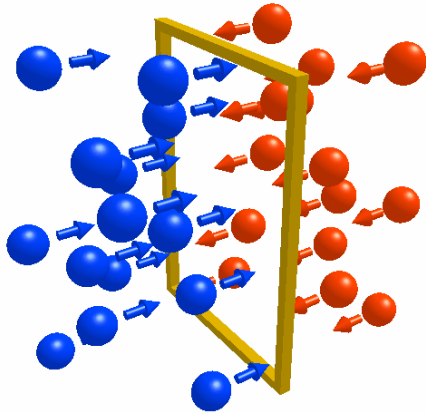


LHC, 2008
9-km diameter
7 TeV protons

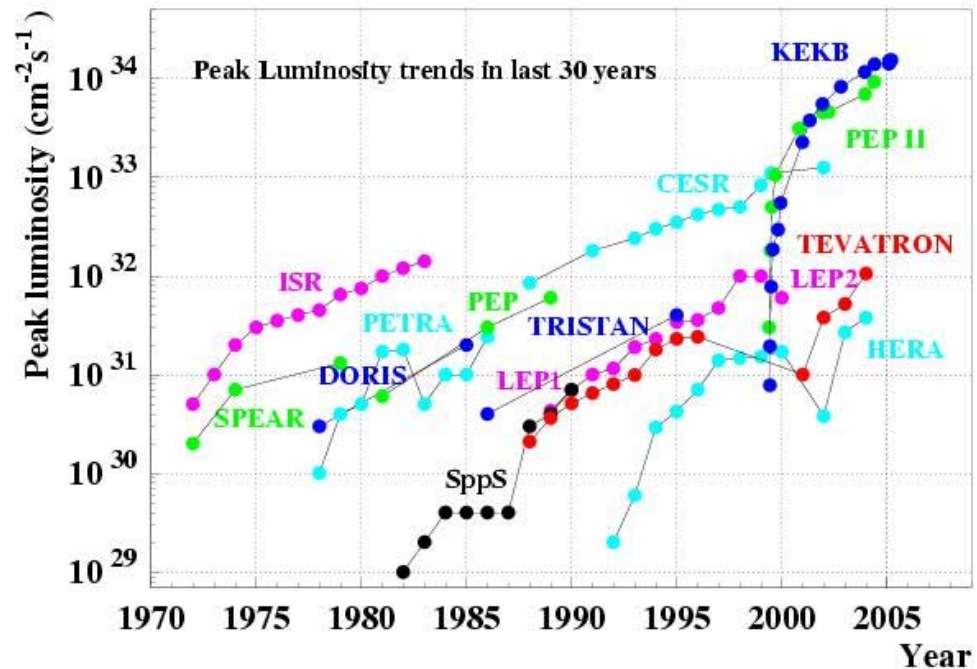
after ~80 years
~10⁷ x more energy
~10⁵ x larger



Luminosity and its continual improvement over time

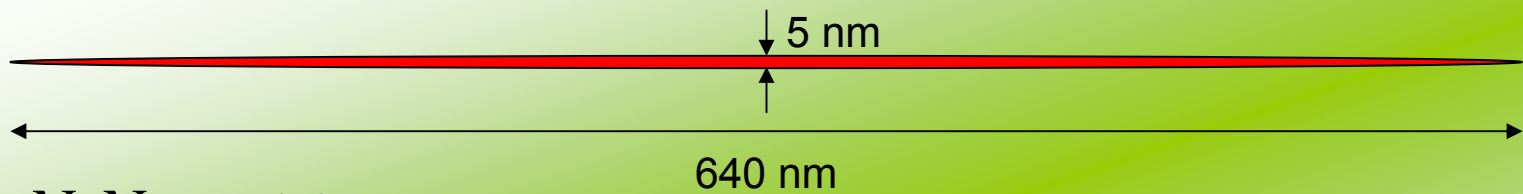
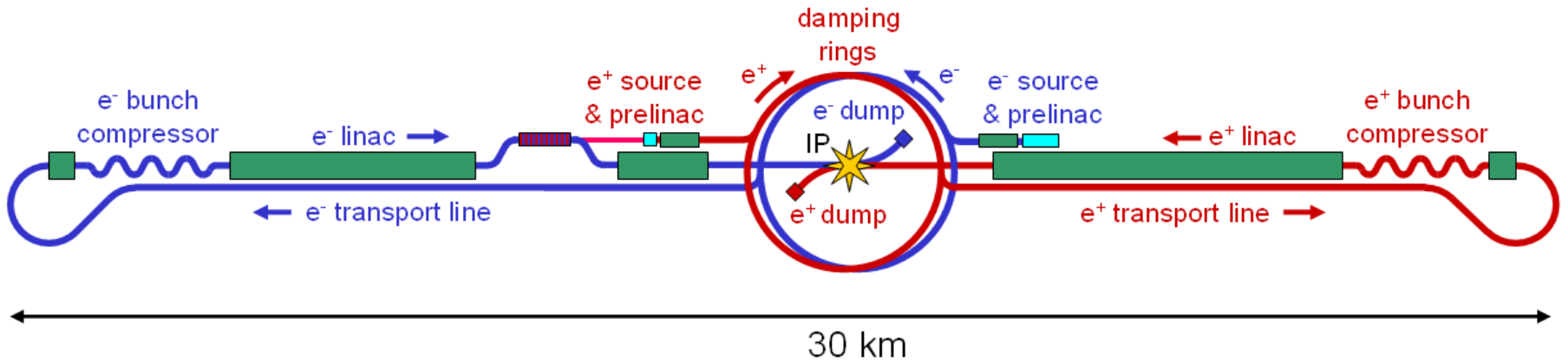


(number of events/unit time)
= (cross section) X (luminosity)



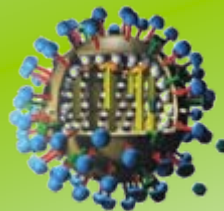
Beams in future e⁺e⁻ colliders must be on the nanometer scale

The International Linear Collider



$$L \sim \frac{N_1 N_2}{A} f \sim \frac{\lambda \lambda}{\gamma^{-1} \lambda} \lambda^{-1} \sim \underline{\underline{(\lambda)^0 \gamma}}$$

~constant

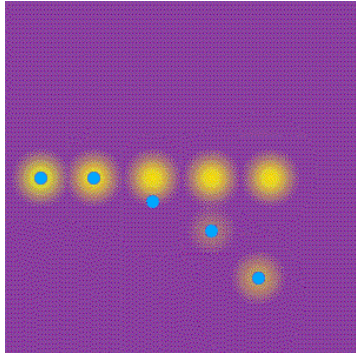


100 nm

Cross-section of the beam at the interaction point of the ILC should be 1/3 the cross-section of a flu virus.

Courtesy: Andy Wolski, Cockcroft Institute/
University of Liverpool

Ultrabright, Ultrashort Beams – Outlook



“only a few photons in coherence volume”



- Understanding “Quantum Optics” driven by accelerated charges will be critical in these studies. → Coherence and degeneracy of an attosecond light pulse in the THz!!
- Opportunities in Ultrafast Science, Nonlinear Dynamics, SCRF, THz Laboratory Astrophysics look exciting!!

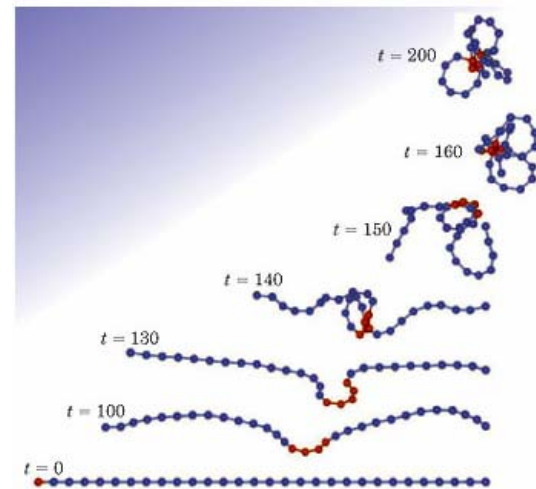
Fascinating graduate research!!



The science need

The fundamental requirement is to understand the *dynamic* behaviour of matter, often in very small (nm) units, on very fast (fs) timescales

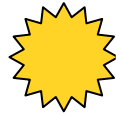
We need not just to determine *structure* with high precision, but to understand *how these structures work*



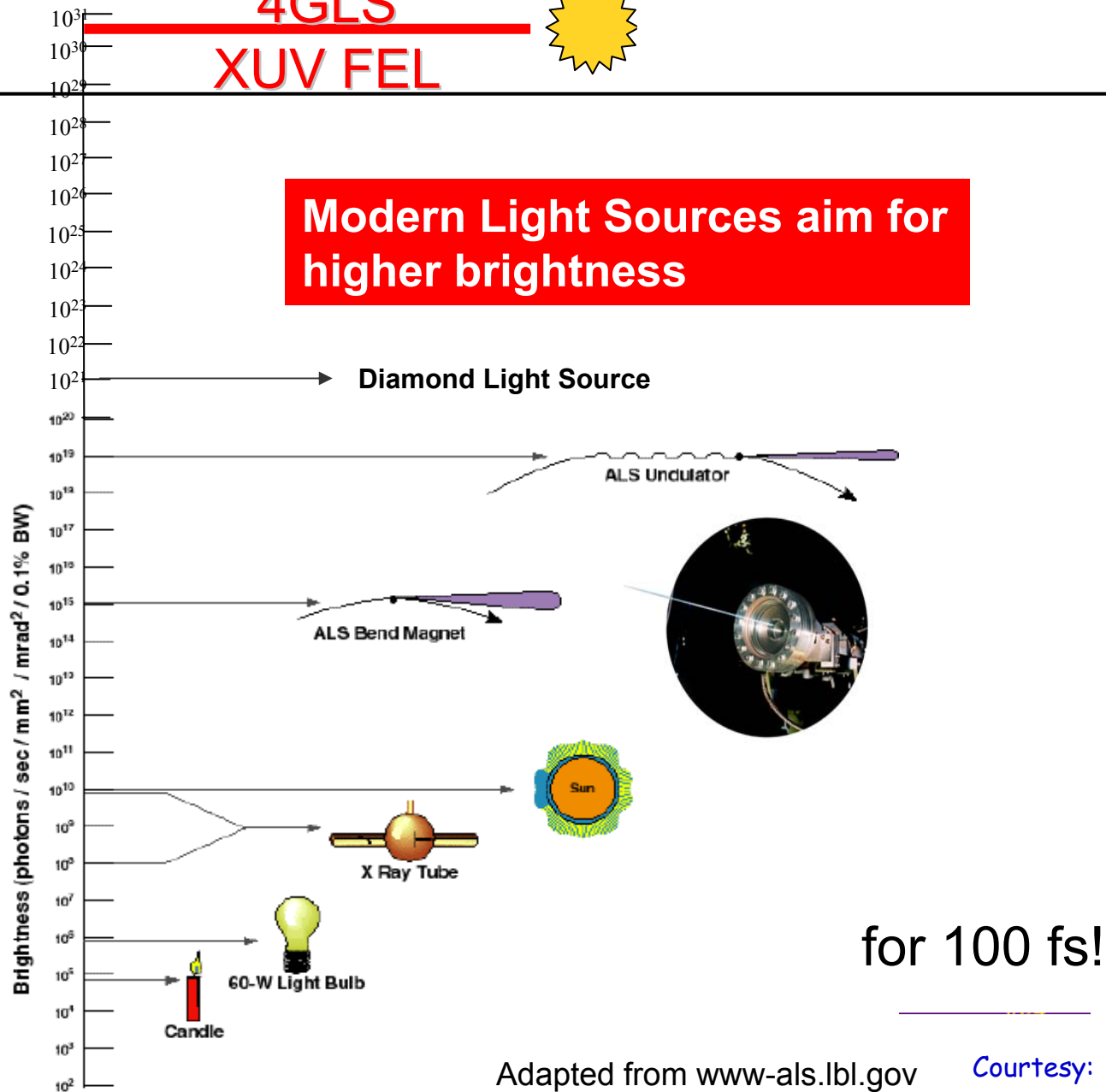
Courtesy: Wendy Flavell, University of Manchester

Light Fantastic and Bright!

4GLS
XUV FEL



Modern Light Sources aim for higher brightness



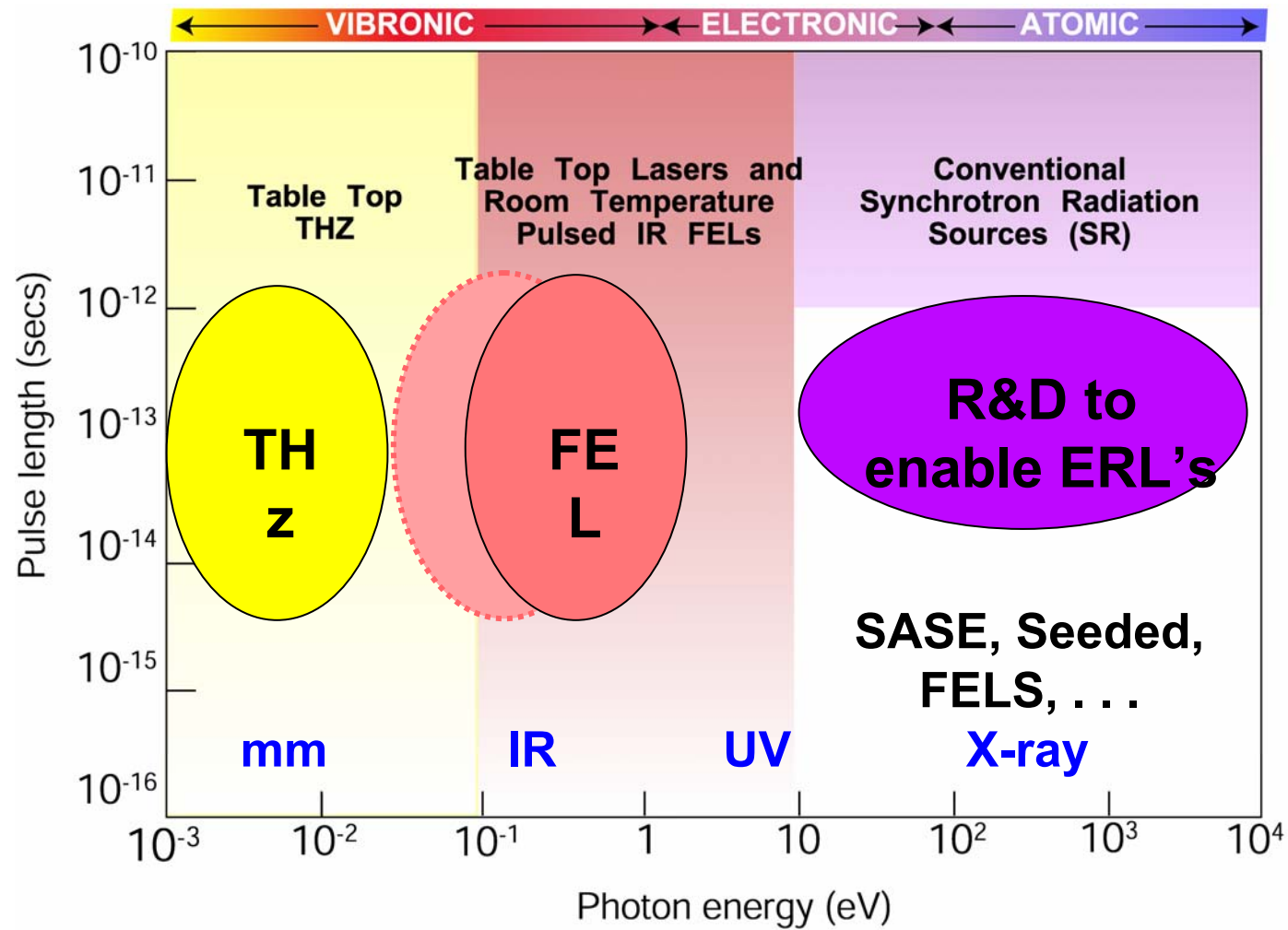
Off the scale
brightness....

>10⁸ x brighter than
3rd generation SR

peak power output
equivalent to that
needed to light every
home in London.....



Intense Charged Particle Beam-generated Photon Beams serve a Colorful Canvas of Photon Sciences



INTENSE, ULTRABRIGHT and ULTRASHORT

Discovery

21st CENTURY: AMAZING LIGHT!! Hidden Energies

Fundamentals at the Core of the Physical World

- Hidden Dimensions, Symmetries and Structures
- Origins of Mass, Dark Matter and Dark Energy
- Unification of Gravity
- Exotic States of Matter
- Ultrabright, Ultrashort and Ultrafast Light

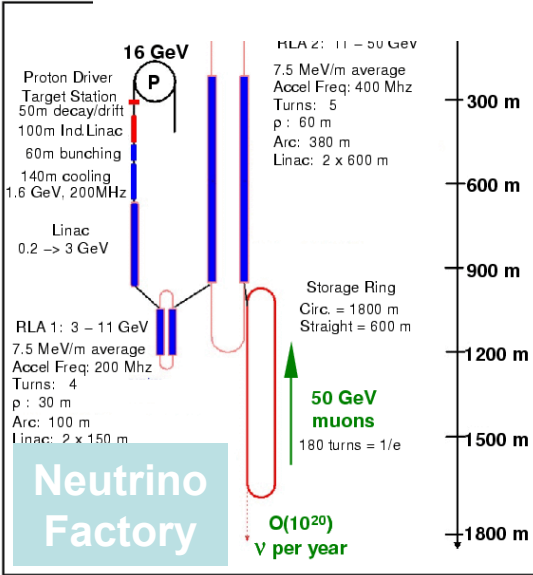
To master the global resources necessary for these discoveries, international effort must be consolidated into only a few carefully selected facilities so large that they can only be supported internationally . . .



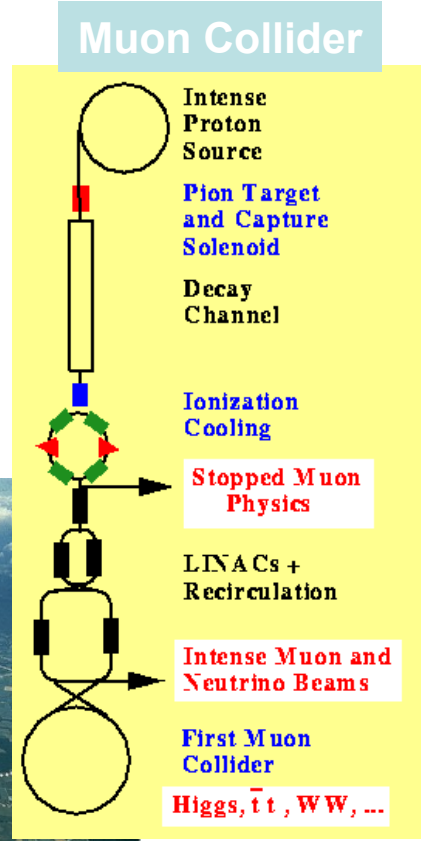
Emergence of a few grand future machines:

- Large Hadron Collider
- X-ray Free Electron Laser
- International Linear Collider
- International Neutrino Factory/Muon Collider

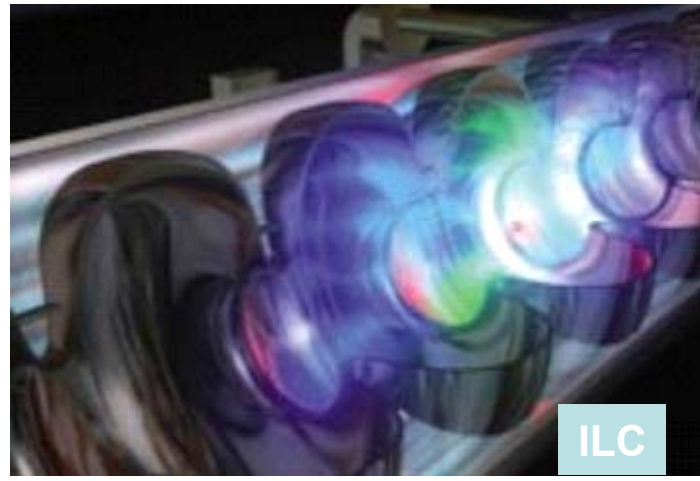
Grand Future Machines



LHC



X-FEL



ILC

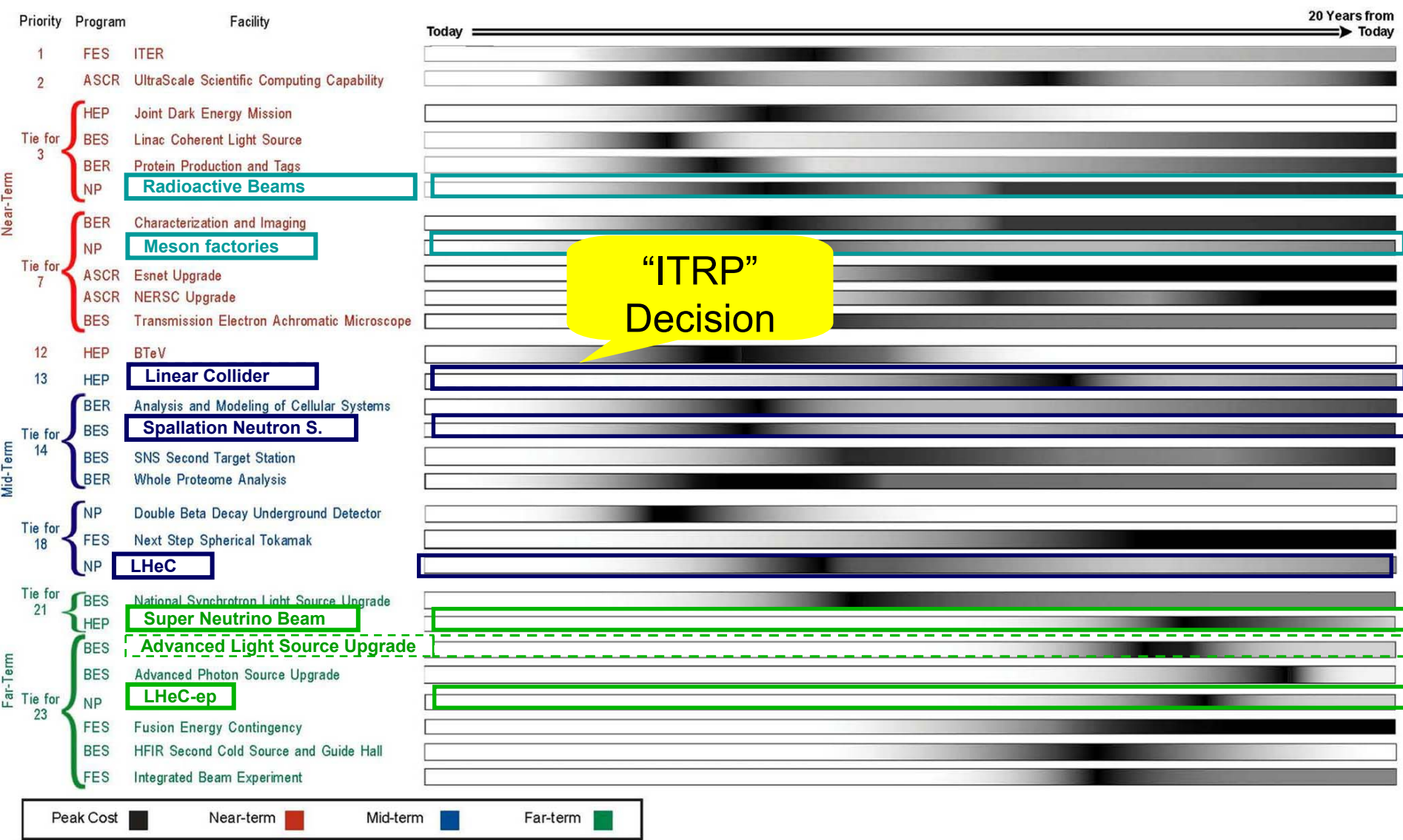
SRF will play a major role in the future SC facilities

U.S. Department of Energy

Office of Science

20-Year Facility Outlook

Peak of Cost Profile



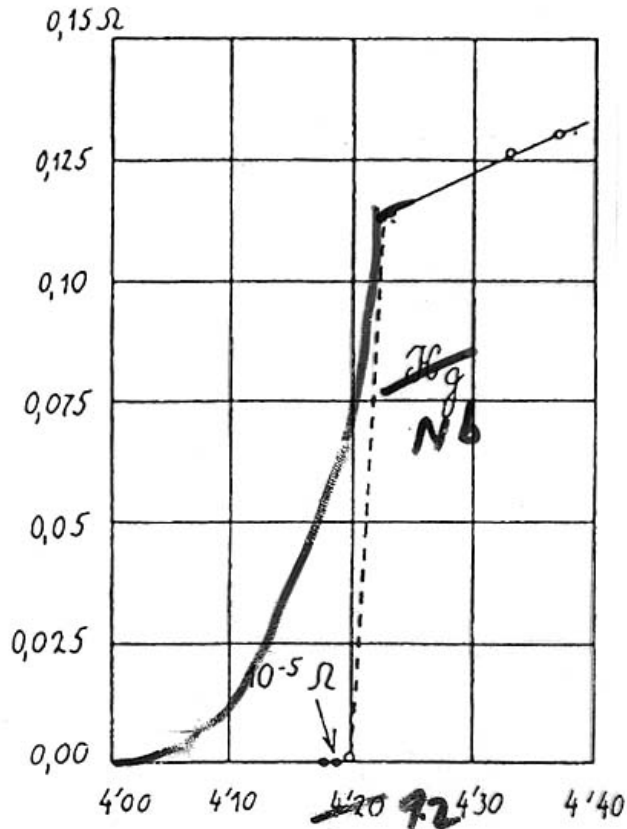
Programs:

ASCR = Advanced Scientific Computing Research
 BES = Basic Energy Sciences
 BER = Biological and Environmental Research

FES = Fusion Energy Sciences
 HEP = High Energy Physics
 NP = Nuclear Physics

Superconductivity

Heike Kammerlingh-Onnes, 1911: SC in mercury



4

The Convergence of Classical Concepts circa 1900

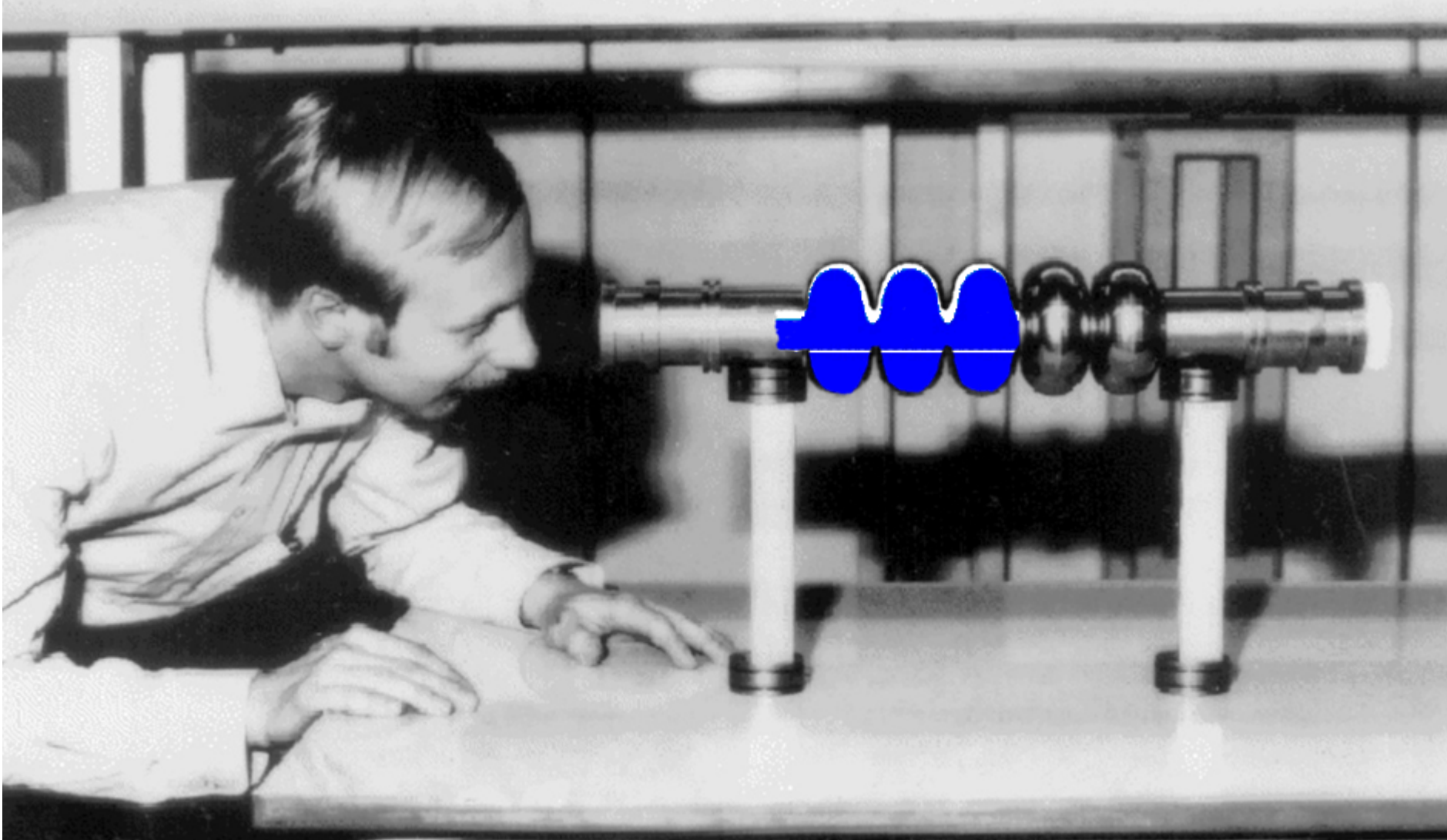


In fact, the “Onnes Road” at Jefferson Lab, home of much of Superconducting Radio Frequency Science and Technology, is named after him.

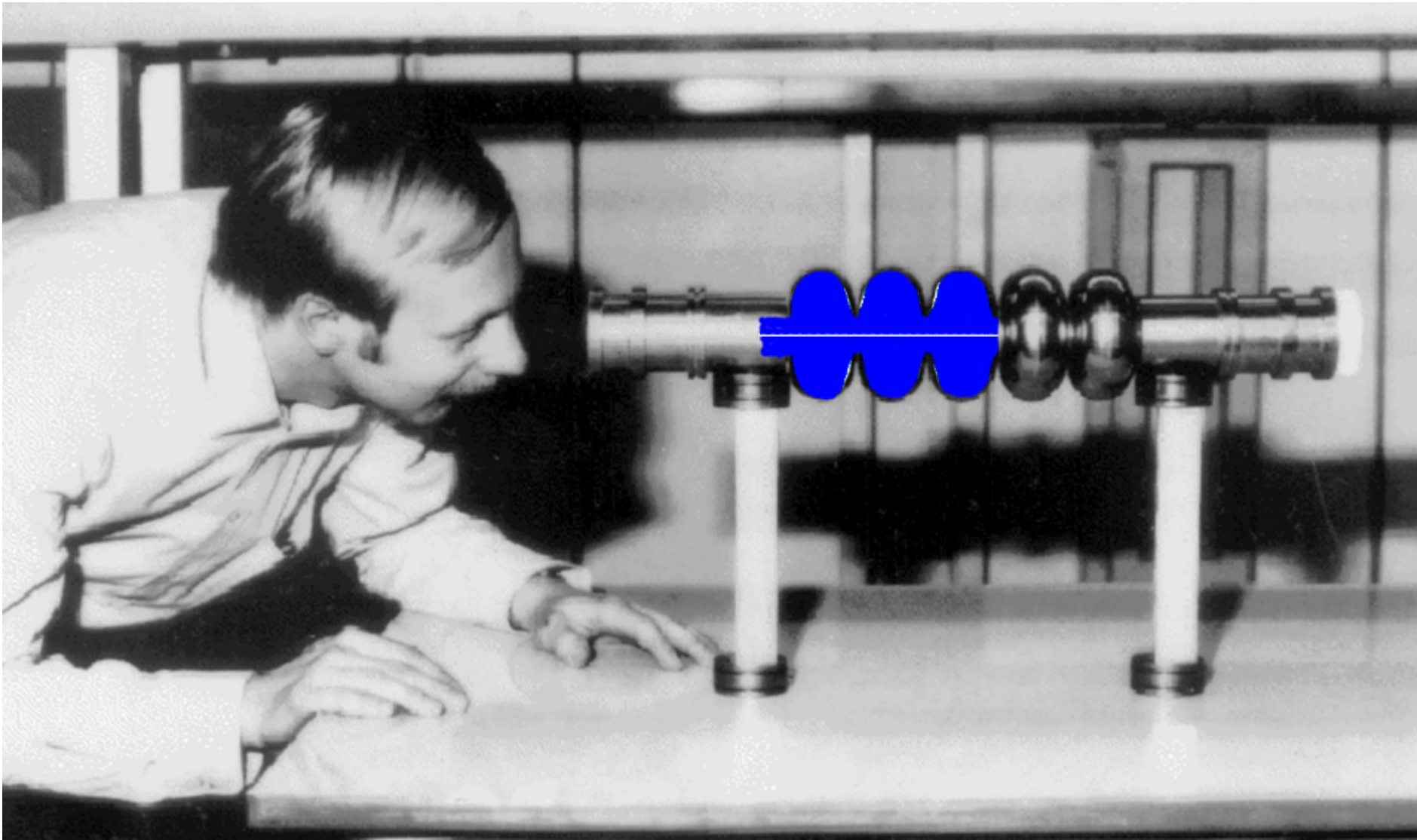
surement of superconductivity by Kamerlingh Onnes

Figure 1-2. Heike Kamerlingh Onnes. Courtesy AIP, *Exhib Library and*

Pulsed Operation of Normal Conducting Accelerating Cavities

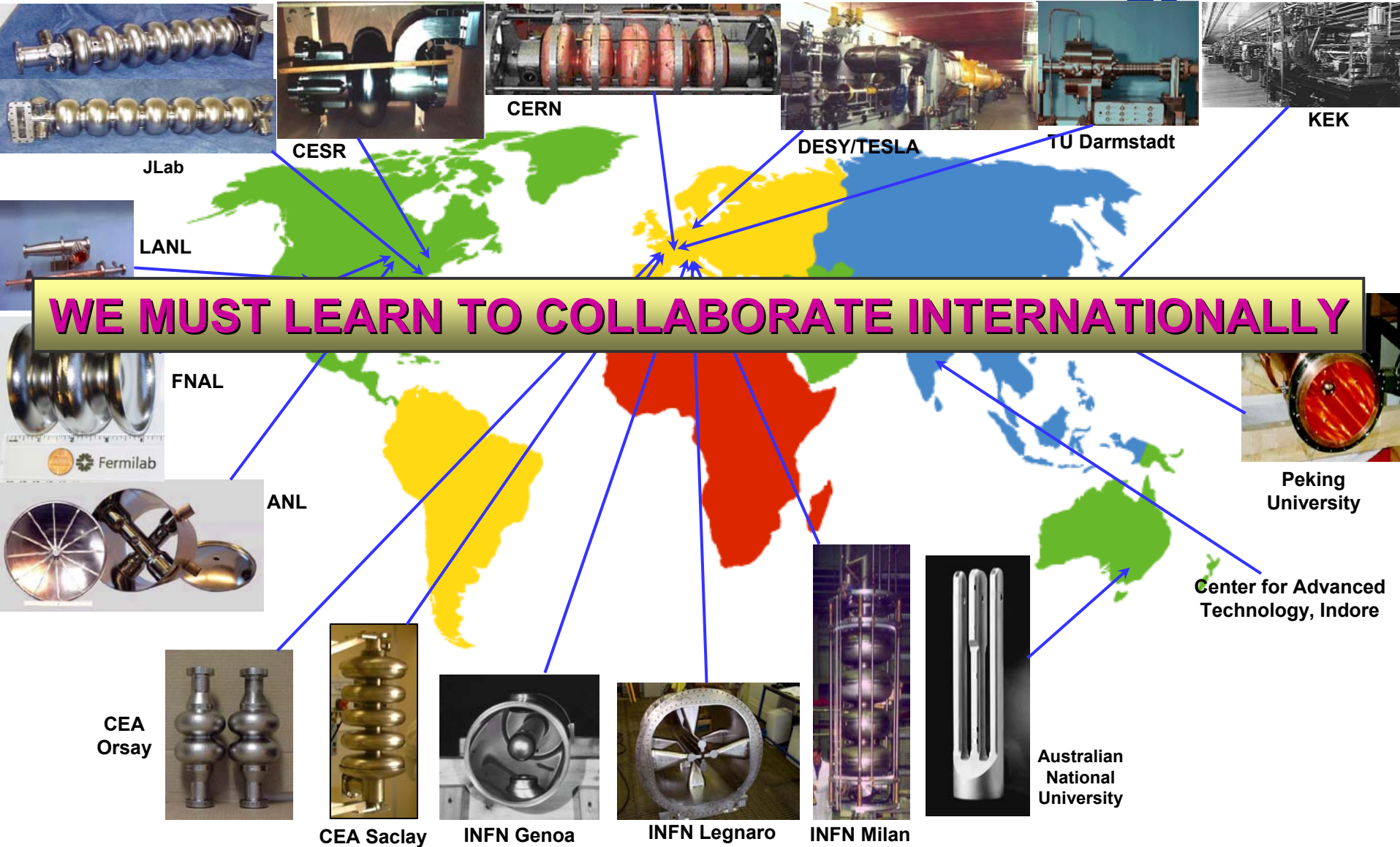


Continuous Operation of Superconducting accelerating Cavities



OUTLOOK

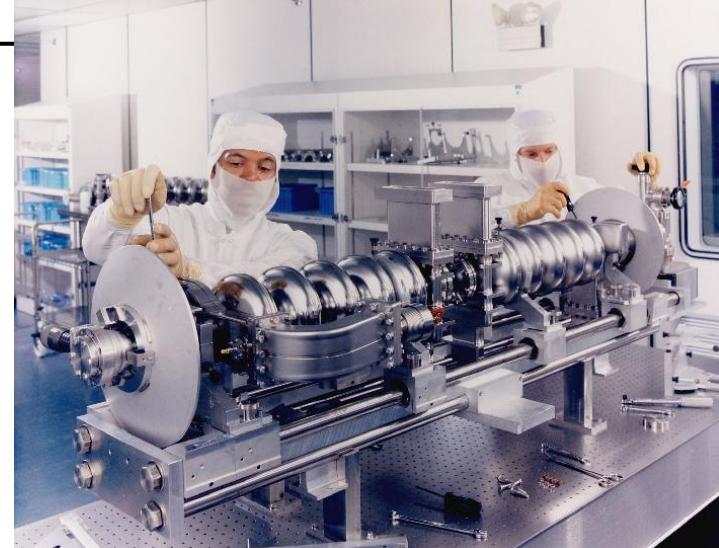
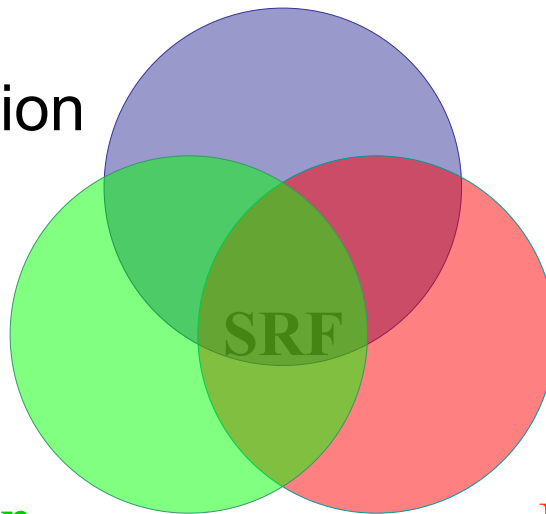
SRF – A Robust Global Technology



Overlap of SRF activities in accelerator projects

SRF technology is central to high-energy/nuclear physics, high current proton drivers, synchrotron radiation sources and free electron lasers.

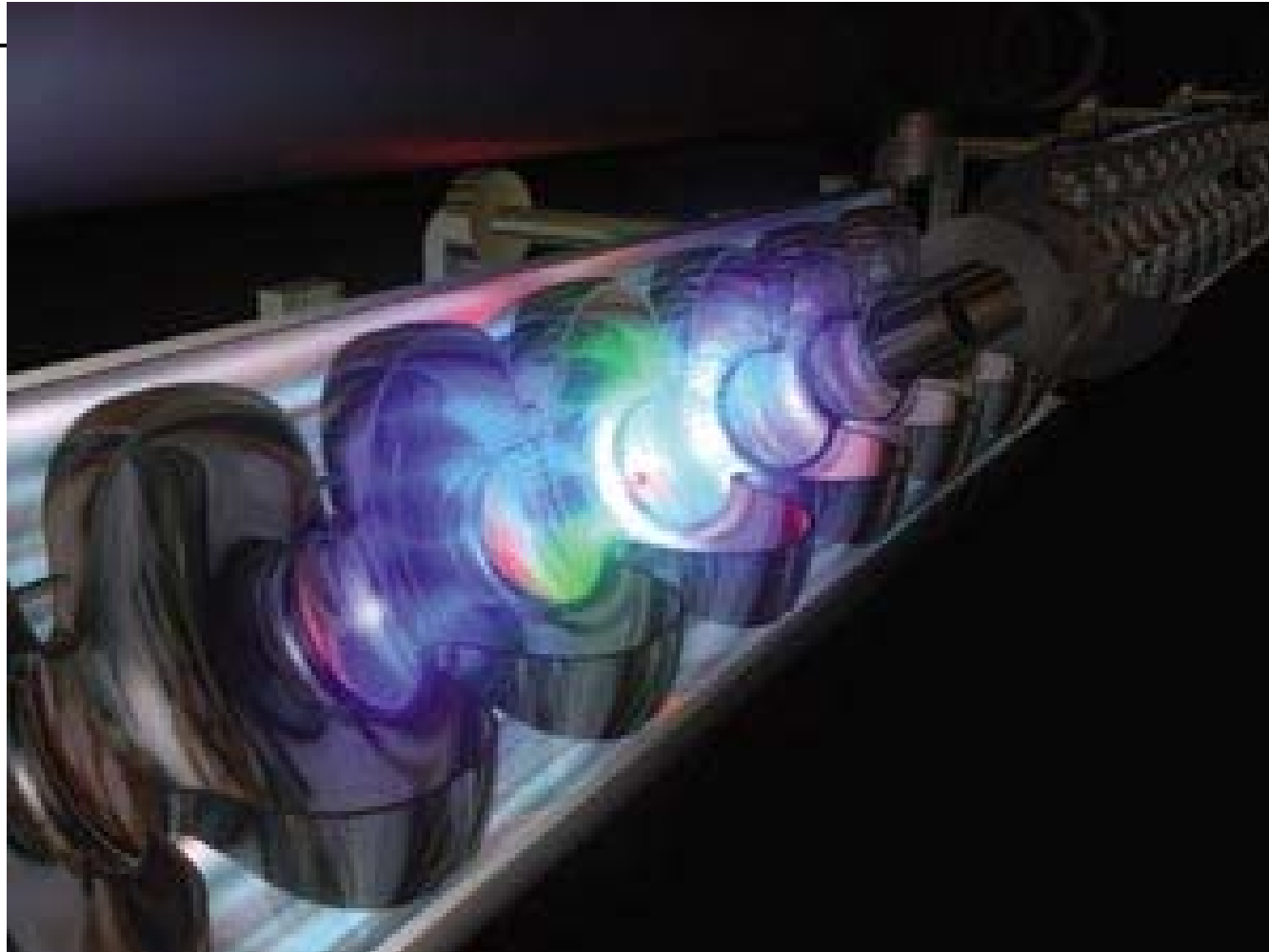
**Superconducting
linear accelerators
and colliders**



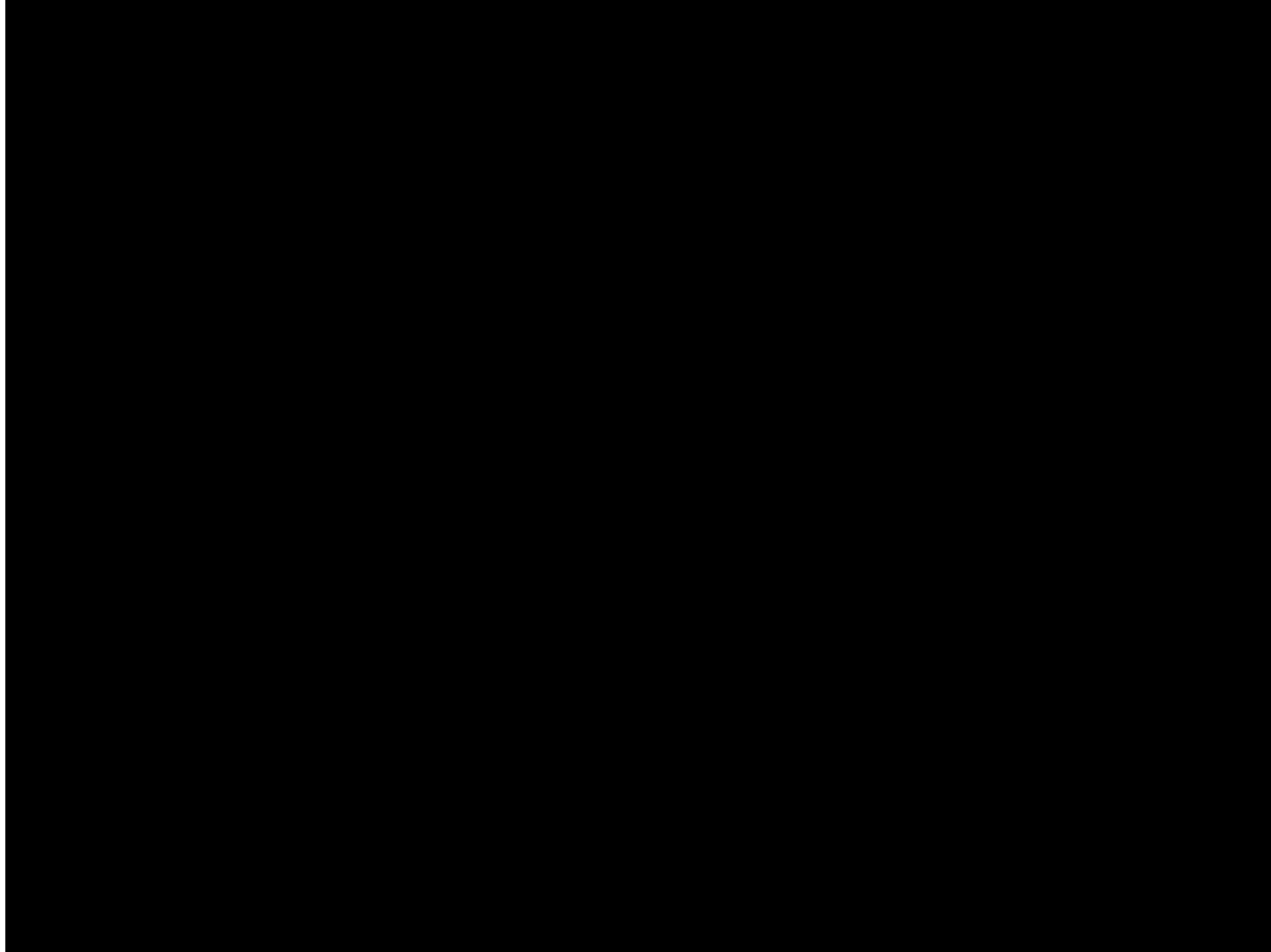
**Synchrotron Radiation
Sources and FELS (Dylla's talk)**

High Current Proton Drivers

The Superconducting Linear Accelerator







Amazing Light and Particles!

Morpho menelaus



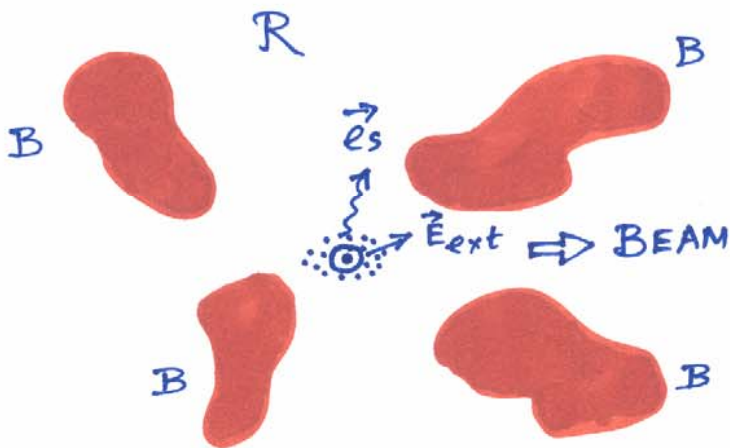
The inverse of a Radiative process is Acceleration

Courtesy: Rebecca Seviour, Cockcroft Institute/Lancaster University

Acceleration and Radiation: A Tangled Web!

$$\vec{E} = \vec{E}_{\text{ext}}(\omega, \vec{r}) + \vec{e}_s(\omega, \vec{r}) N$$

Total Field in region
'R' bounded by
boundaries 'B'



The field energy density:

$$\epsilon \sim \int |\vec{E}|^2 d^3r d\omega$$

$$= \int |\vec{E}_{\text{ext}}|^2 d^3r d\omega$$

$$+ N^2 \int |\vec{e}_s(\omega, \vec{r})|^2 d^3r d\omega$$

ENERGY LOSS TO
COHERENT SPONTANEOUS
RADIATION

EXTERNAL
STORED
ENERGY

$$+ 2 \operatorname{Re} \left[N \int \vec{E}_{\text{ext}}(\vec{r}, \omega) \cdot \vec{e}_s(\vec{r}, \omega) d^3r d\omega \right]$$

STIMULATED ABSORPTION/RADIATION: EXCHANGE OF ENERGY
BETWEEN PARTICLES and WAVES: ENERGY GAIN (DECEL.
OF PARTICLES) or LOSS (ACCEL. OF PARTICLES).

Scaling

For optimal acceleration/deceleration, linear or otherwise in \vec{E}_{ext} , there must be optimal overlap of 'acceleration' mode $\vec{E}_{\text{ext}}(\omega, \vec{k})$ with 'radiation' mode $\vec{E}_s(\omega, \vec{k})$. The particles are accelerated if the coherent radiation loss is less than the energy gain, leading to the restriction:

$$N \leq (|\vec{E}_{\text{ext}}|/e) \tilde{\lambda}^2 \equiv N_{\text{critical}}$$

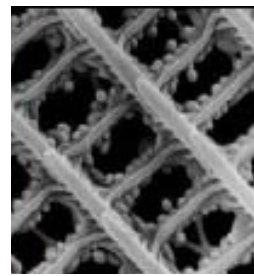
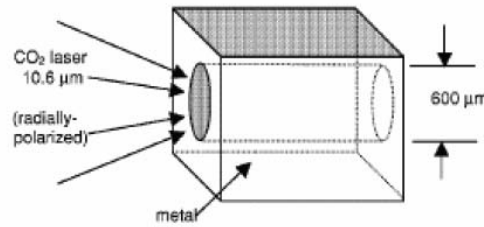
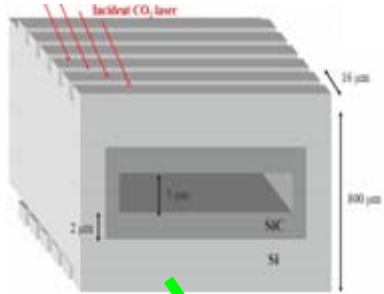
on the number of particles in a bunch that can be effectively accelerated before losses start to dominate, leading to deceleration ($\tilde{\lambda} \equiv \lambda/2\pi$ is the reduced wavelength of accelerating mode).

$$E_{\text{acc}} \sim (\tilde{\lambda})^{-1}$$

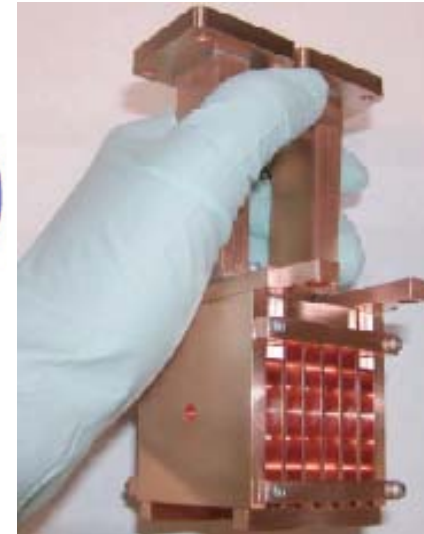
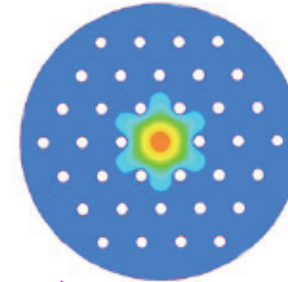


$$N_{\text{critical}} \sim \tilde{\lambda}$$

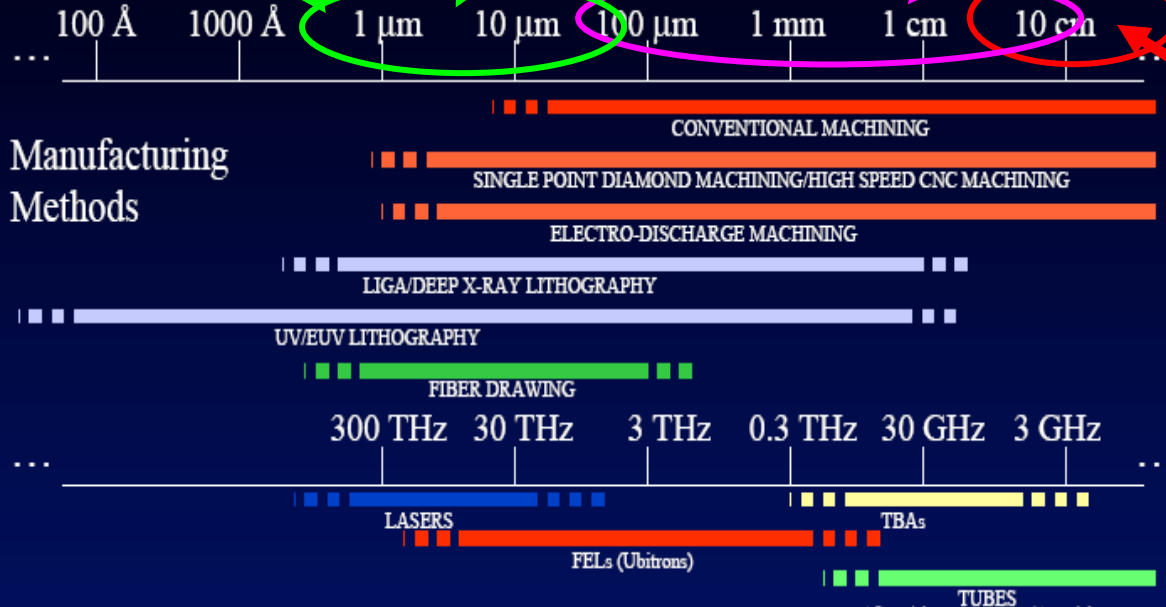
(SLAC)



E. Smirnova et. al.
(MIT), metallic photonic
fiber, 17 GHz



Manufacturability



CESR cavities

Courtesy: Rebecca Seviour, Cockcroft
Institute/Lancaster University

Technologies and Wavelengths

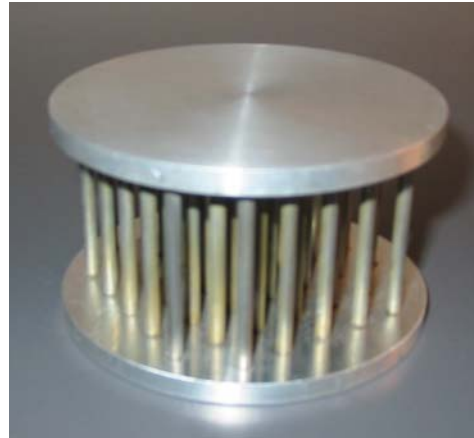
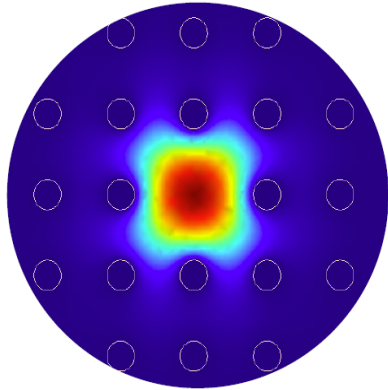
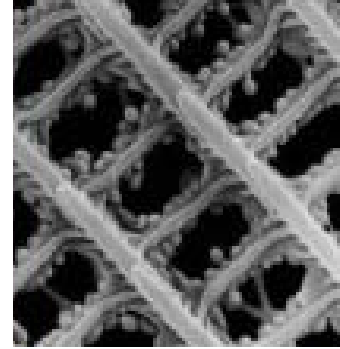
Technology	Wave-length λ	Potential Gradient	R&D	Technology Details
SCRF (Superconducting Radio-Frequency)	>20 cm	~ 100 MV/m	Superconducting materials research; new superconductor	'Bismuthate' materials and micro-layered thin-film technology
RF (Radio-Frequency)	<10 cm	~ 200 MV/m	Power sources prototype, drive beam dynamics ----- sheet beam klystron research	High frequency conventional klystrons and two-beam schemes
mm-wave, THz, Photonic Band-Gap	<2 cm	>1 GV/m	Power source invention, structure invention, fabrication tech.	Dielectric and conducting materials
Lasers & beams in plasmas & structures	<200 μm	>10 GV/m	Module prototype, rep. rate, guiding, staging, beam dynamics	Laser, structure-based Laser, plasma-based Beam, structure-based Beam, plasma-based

$$E_{\text{acc}} \sim \lambda^{-1}$$

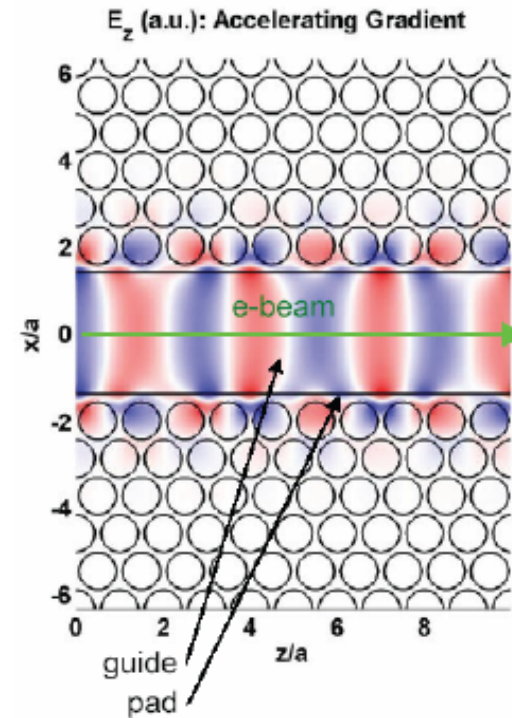
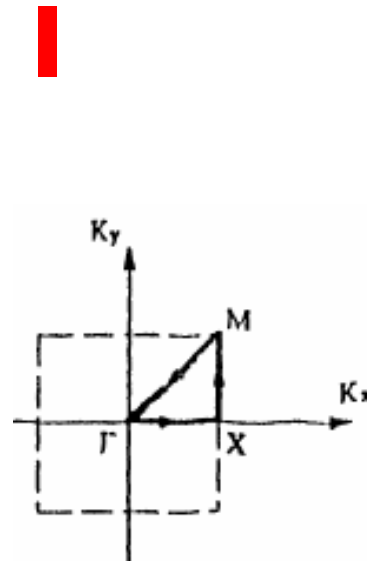
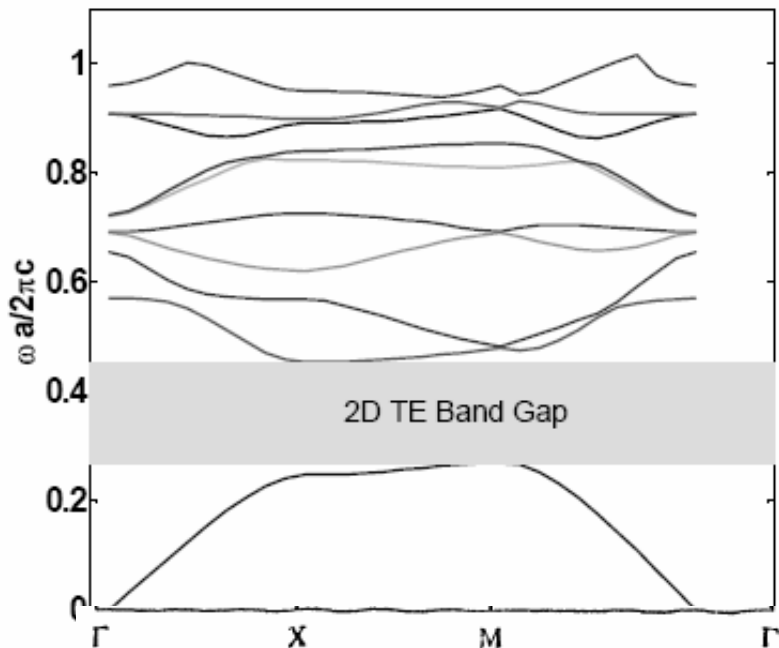
$$N_{\text{acc}} \sim ??$$

Photonic Band Gap Structure

Courtesy: Rebecca Seviour, Cockcroft Institute/Lancaster University



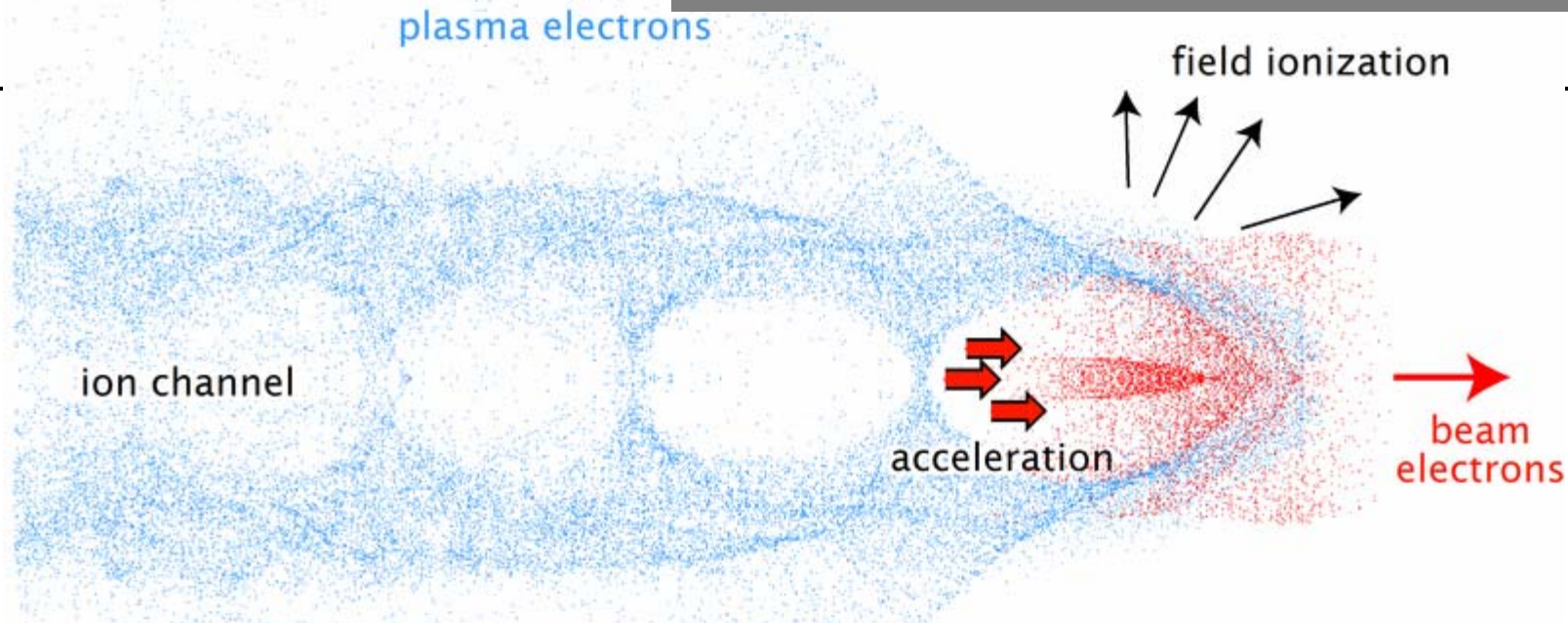
TE Band Structure of Crystal



Speed-of-light mode in PC waveguide

B. Cowan (SLAC),

Plasma Acceleration



Plasma acceleration has several types depending how the plasma wave is formed:

Plasma Wakefield acceleration: Plasma wave formed by an electron bunch

Laser Wakefield acceleration: Laser pulse is used to form a plasma wave.

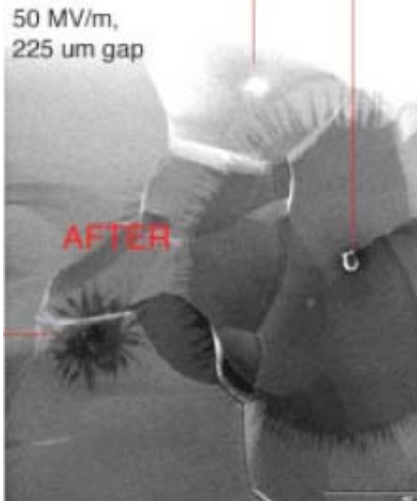
Laser Beat-wave acceleration: Plasma wave arises based on different frequency generation of two laser pulses.

Self-modulated laser Wakefield acceleration: Leave for another day

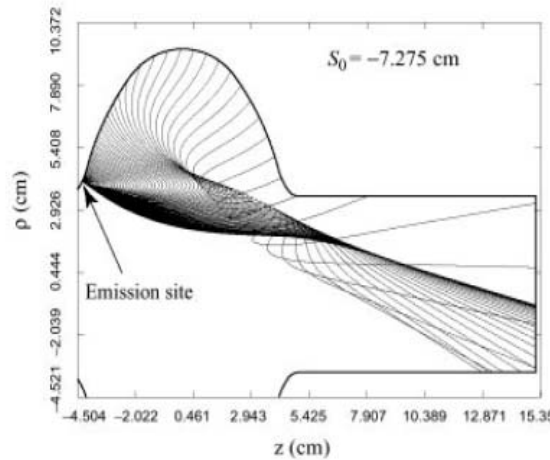
Delicate Periodicity: Issues of Surface Finish and Medium Homogeneity

Field Emission

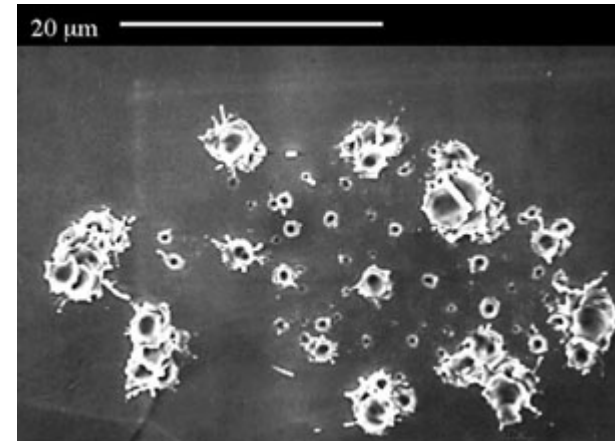
Courtesy: Rebecca Seviour, Cockcroft
Institute/Lancaster University



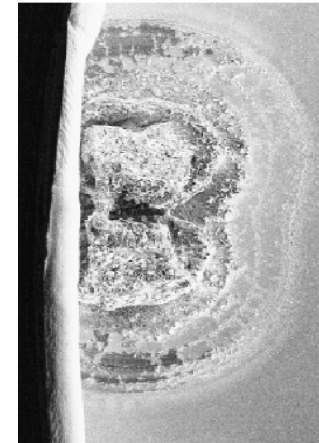
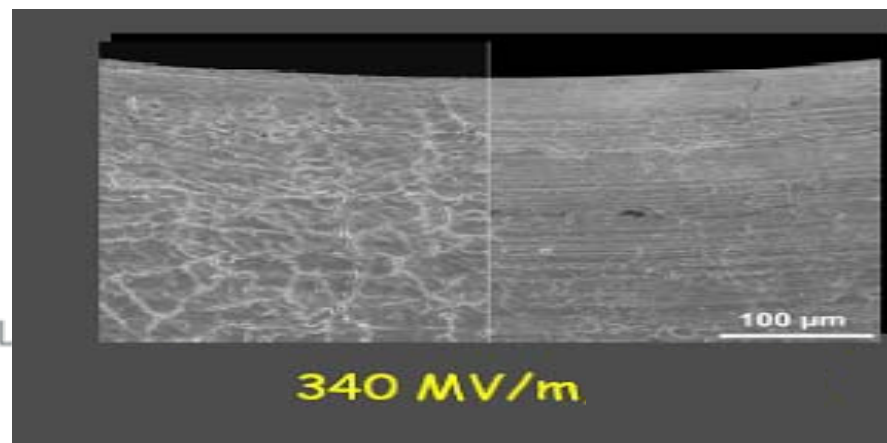
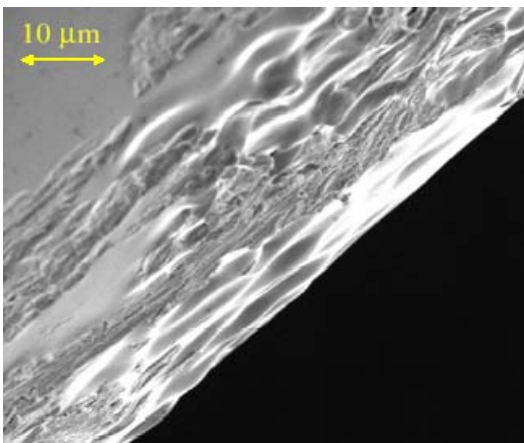
Plasma Spots



Cracking

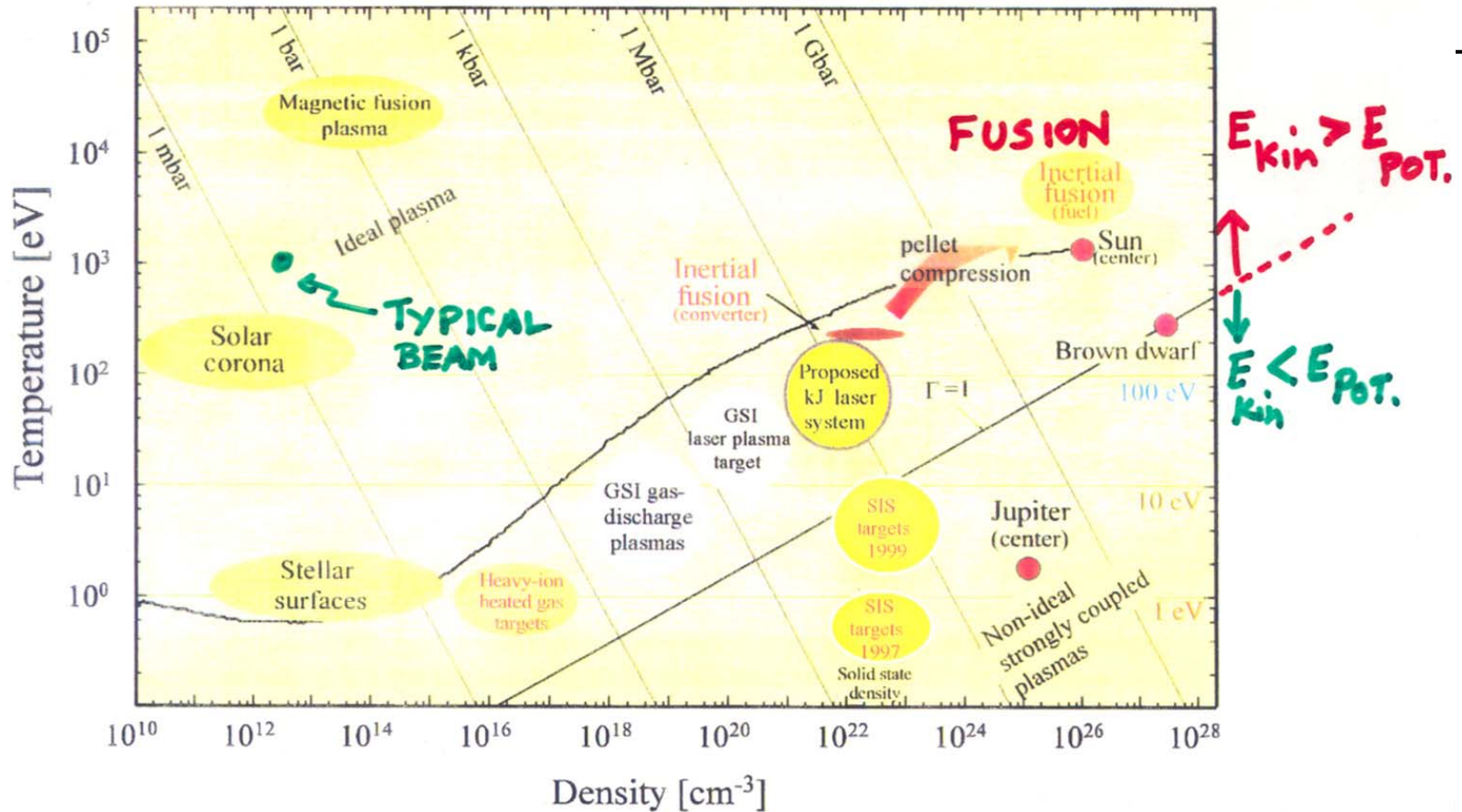


Hot Spots



States of Matter: Astrophysical & Laboratory Plasmas

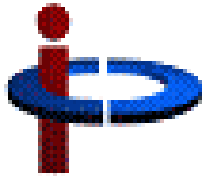
Density and Temperature



Density and temperature diagram of astrophysical and laboratory plasma phenomena. The solid black curve depicts the state diagram of the sun showing the plasma state of its center on the right end. The straight line $\Gamma = E_{pot}/E_{kin} = 1$ separates ideal and strongly coupled hydrogen plasmas.

Beams Under Extreme Conditions

E $10^2 - 10^6$ GV/m	10^{-4} eV \leftrightarrow 1mm $\tau_{cool} \sim 10^{-4}$ sec Macroscopic Coulomb Crystal	$\rho \sim 10^{18} - 10^{24}/cc$ $\lambda_p =$ interparticle distance Comparable to solids	$\tau \sim 10^{-18} - 10^{-15}$ second Ultrashort electron and x-ray bursts
Today's Technology: $E < 100$ MV/m (10^{-1} GV/m)	Today: 1 eV \leftrightarrow 1000 Å $\tau_{cool} \sim 1$ sec.	Today: $\sim 10^{13} - 10^{14}/cc$	Today: $\tau \sim 10^{-14}$ seconds (10 femtoseconds)
DISCOVERY New Phases of Matter Non-Linear QED Dark Matter Dark Energy	DISCOVERY Crystalline Beams Cold Muons Condensate Beams, Fermionic and Bosonic	DISCOVERY New Phases of Matter	DISCOVERY Ultrafast Dynamics in Condensates and Living Matter
TECHNOLOGY/INNOVATION <ul style="list-style-type: none"> • High Intensity Atomic Lasers • Free Electron Accelerators • Laser-Plasma Acceleration 	TECHNOLOGY/INNOVATION Optical Cooling	TECHNOLOGY/INNOVATION High energy-density laser plasma-beam interaction	TECHNOLOGY/INNOVATION Optical manipulation of beams



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ACCELERATOR SCIENCE AND TECHNOLOGY

ULTRABRIGHT, ULTRAFAST, ULTRACOLD, . . .

--Scientific Possibilities/Discoveries



Motivation

Scientific Possibilities with :

Femto- and Atto-second Electron Pulses, X-rays, γ -rays and FELS
at Extreme High Fields at Extreme Low Temperatures

10^{-18} seconds $\sim < \tau \sim < 10^{-15}$ seconds

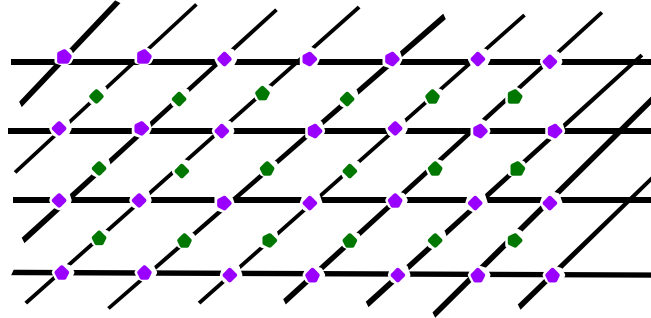
Femtosecond Laser \rightarrow Attosecond Electron Beam Pulse \rightarrow Attosecond Light and X-rays

allows pump-probe experiments @ 10^{-17} second scale

Novel interactions of bright ultrashort pulses with particles/atoms/molecules/bulk matter at the Quantum Limit of

- Condensed Matter Physics
- Biochemistry
- Life Sciences
- Statistical Physics
- Exotic Atomic Physics:
“Coherent Ionization” and
“Quantum Entangled States”
- Particle Physics
- Nuclear Physics

Phonon Dynamics on a Surface



CONDENSED
MATTER
PHYSICS

Lattice vibrations and 'Phonon' spectrum characterized by Debye time-scale :

Phonons $\rightarrow h\nu \approx kT \leftarrow$ Thermal Bath

Lattice relaxation time :

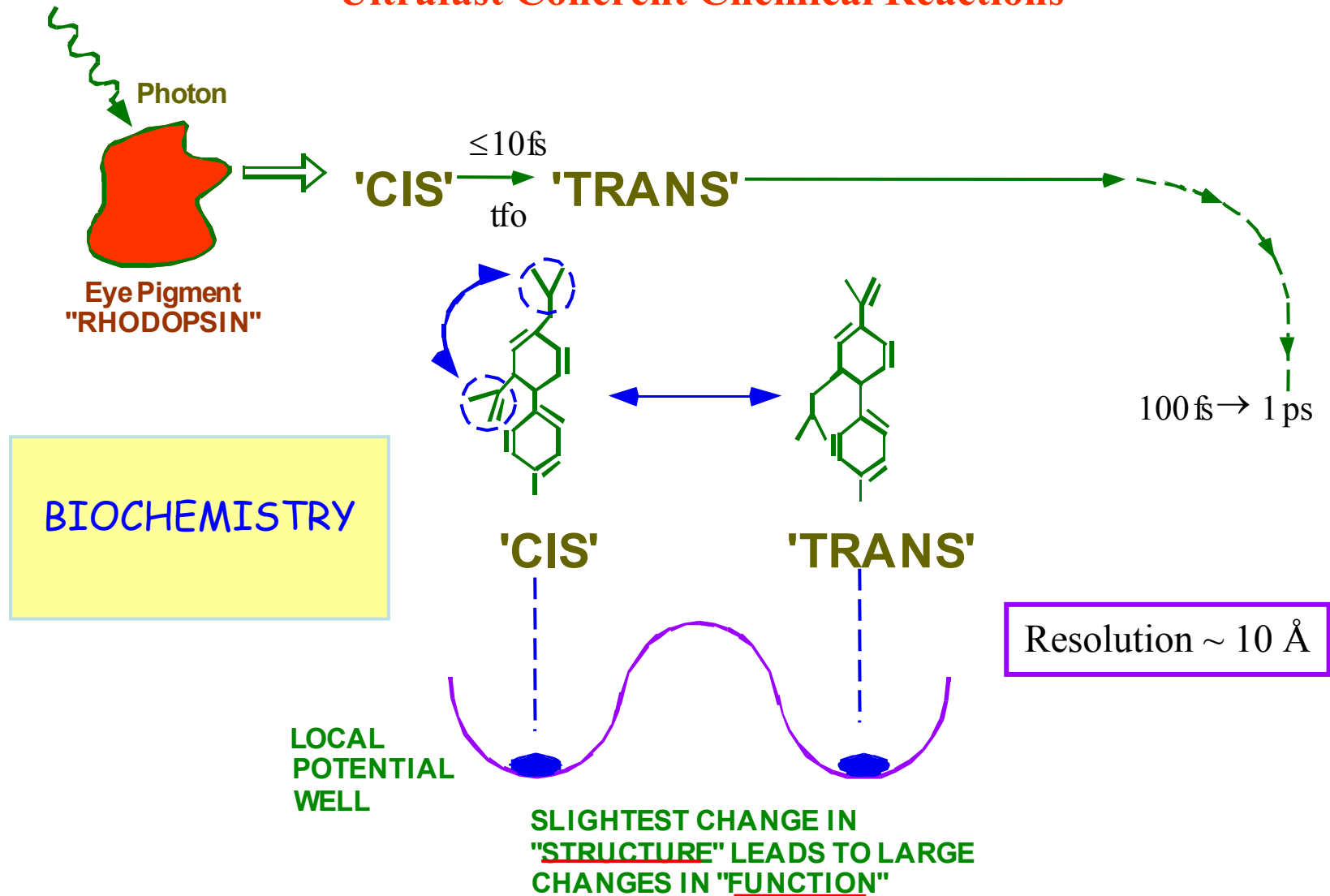
$$\tau = \nu^{-1} = h/kT \sim 100 \text{ fs @ room temp.}$$

$$\text{Resolution} \sim \text{\AA}$$

PHASE TRANSITIONS like surface melting etc. take place on this 1 - 100 fs time-scale.
EXTREMELY VALUABLE INFORMATION for SEMICONDUCTOR PHYSICS. e.g. silicon

Primary Event in "Vision"

Ultrafast Coherent Chemical Reactions



Controlled Study of “Protein Folding”

“stretched” uncoiled protein $t = 0$



“β-sheets”



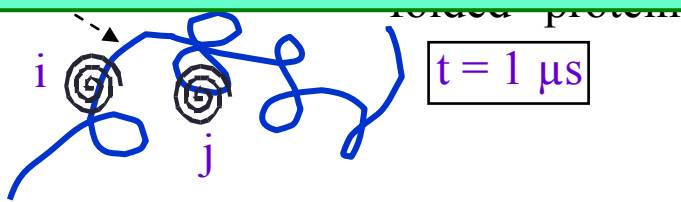
LIFE SCIENCES

via a “physical” experiment
(as opposed to chemical or biological expt.)

Resolution $\sim 1-100 \text{ \AA}$

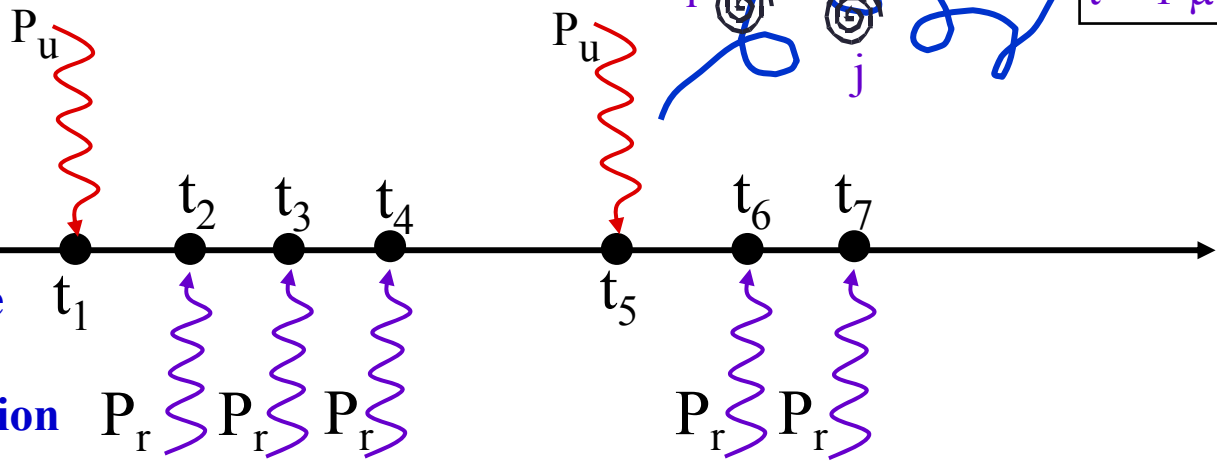
Strategic Simulation: Hybrid Langévin Code

$$R(i,j | t,t) \iff C(k,k | \omega,\omega)$$



$t = 1 \mu\text{s}$

pulse sequence schematic to study correlation



Particle Beam Condensates

Beams of BOSONS and FERMIONS at the limit of quantum degeneracy where quantum mechanical collective behavior is important. Can one ever cool particle

beams to "condensates"??

STATISTICAL
PHYSICS

BOSE - Beam

FERMI - Beam

lowest possible
temperature

N

Strategic Simulation: Molecular Dynamics Code

Quantum relaxation

Quantum diffraction-
limited volume in phase-space :

time
 $\approx 10^{-17}$ sec

Quantum diffraction-
limited volume in phase-space :

$$\epsilon_x^{(n)} \epsilon_y^{(n)} \epsilon_z^{(n)} \gg \left(\frac{\lambda_c}{2}\right)^3$$

$$\epsilon_x^{(n)} \epsilon_y^{(n)} \epsilon_z^{(n)} \gg \frac{N(\lambda_c/2)^3}{(2S+1)}$$

$$\lambda_c = \frac{\hbar}{mc} = \begin{matrix} \text{Compton} \\ \text{Wavelength} \end{matrix}$$

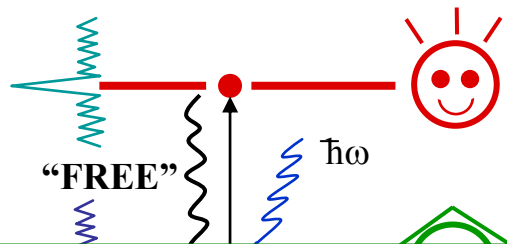
(S \equiv spin of the Fermions)

STUDY OF

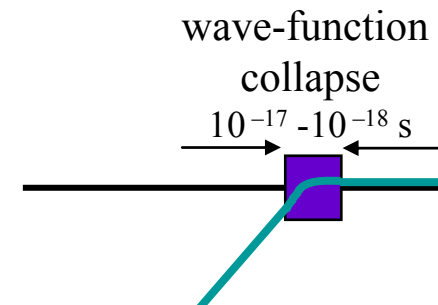
The Dynamics of Quantum Collapse & Entanglement via Attosecond Bursts

Although we are comfortable with quantum physics, we still have a hard time with “quantum control”. No understanding is complete until one can engineer simple systems.

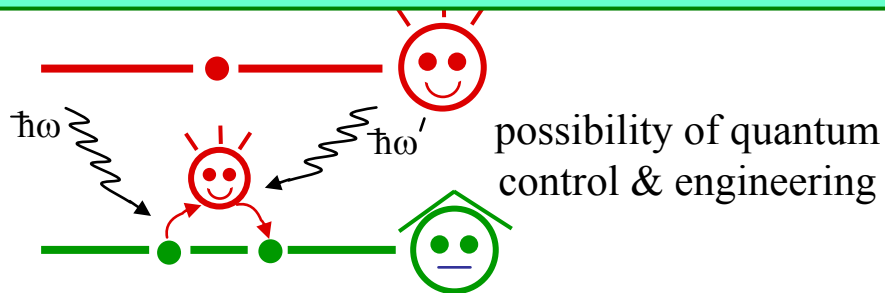
“BOUND”



ATOMIC
PHYSICS



Strategic Simulation: Many-Body Hartree-Fock Code

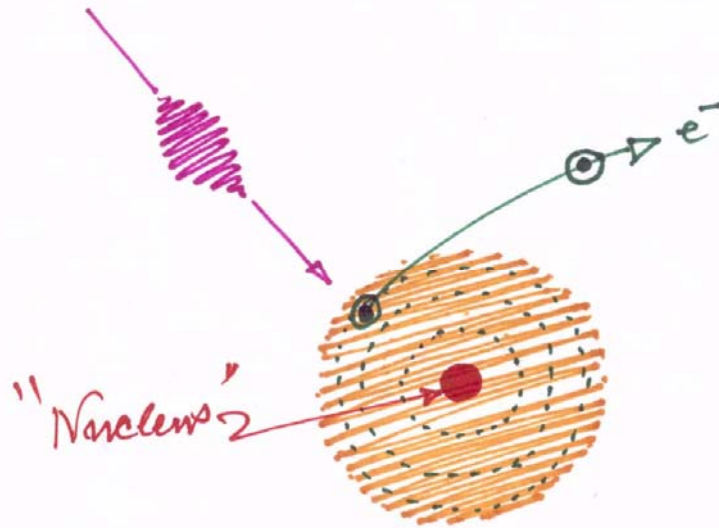


disentanglement
 $10^{-17} - 10^{-18} \text{ s}$

Resolution $\sim \text{\AA}$

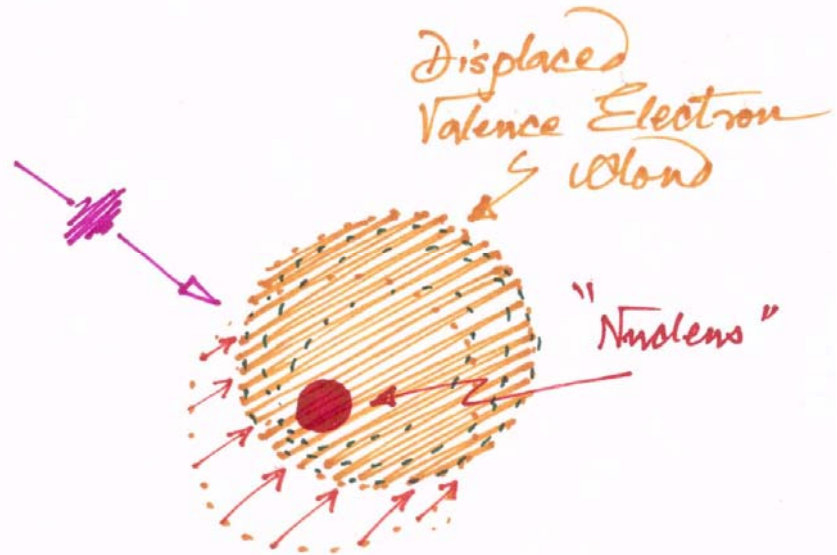
Incoherent vs. Coherent Ionization

"Incoherent" Ionization



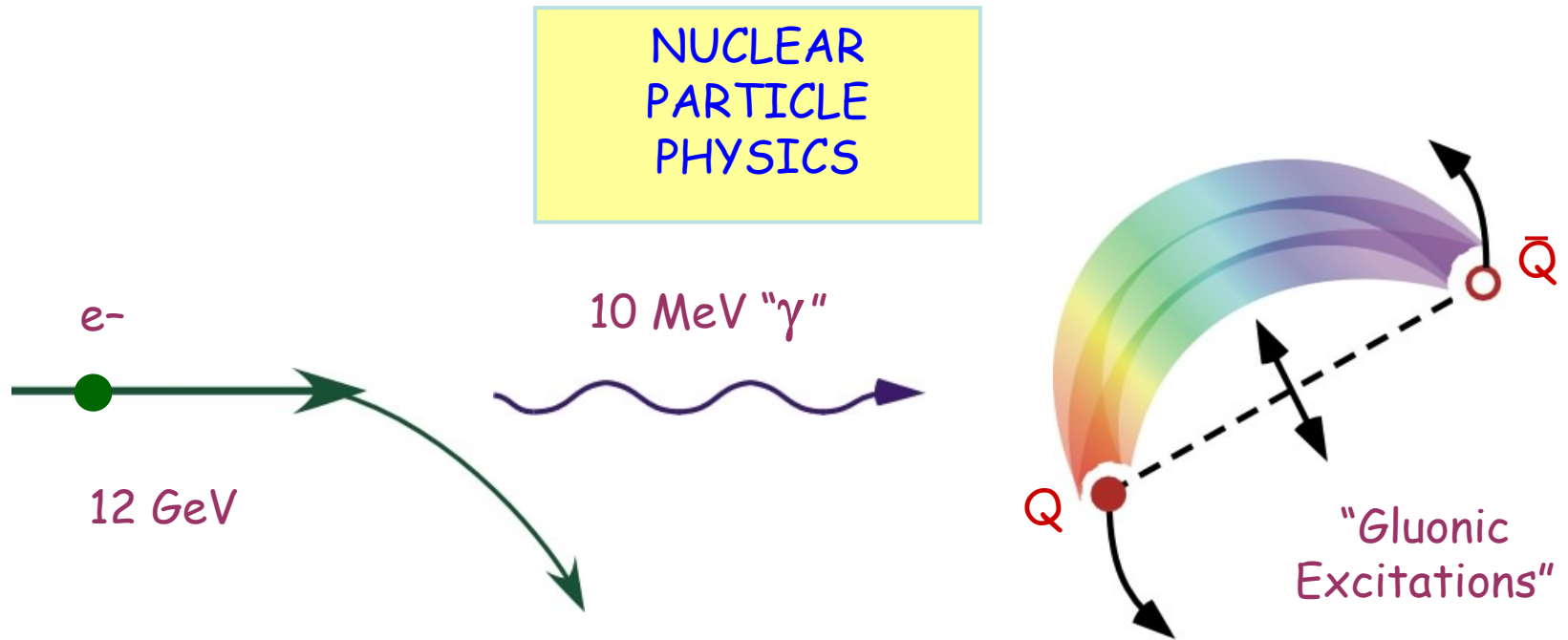
Long Pulse leading to ejection of single valence electrons

"Coherent" Ionization

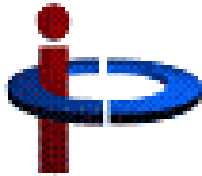


Ultrashort "attosecond" pulse leading to coherent displacement of the valence "electronic cloud" with respect to the nucleus

Color Mapping in QCD



Strategic Simulation: Lattice-gauge QCD Code



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ULTRASHORT PULSES

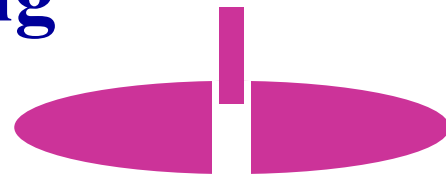
-- Innovation and Generation Mechanisms



Scattering, Slicing and Bunching

Thomson/Compton Scattering

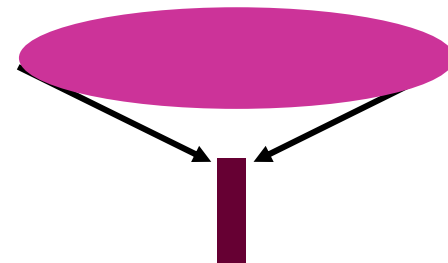
Laser-assisted atto-slicing:



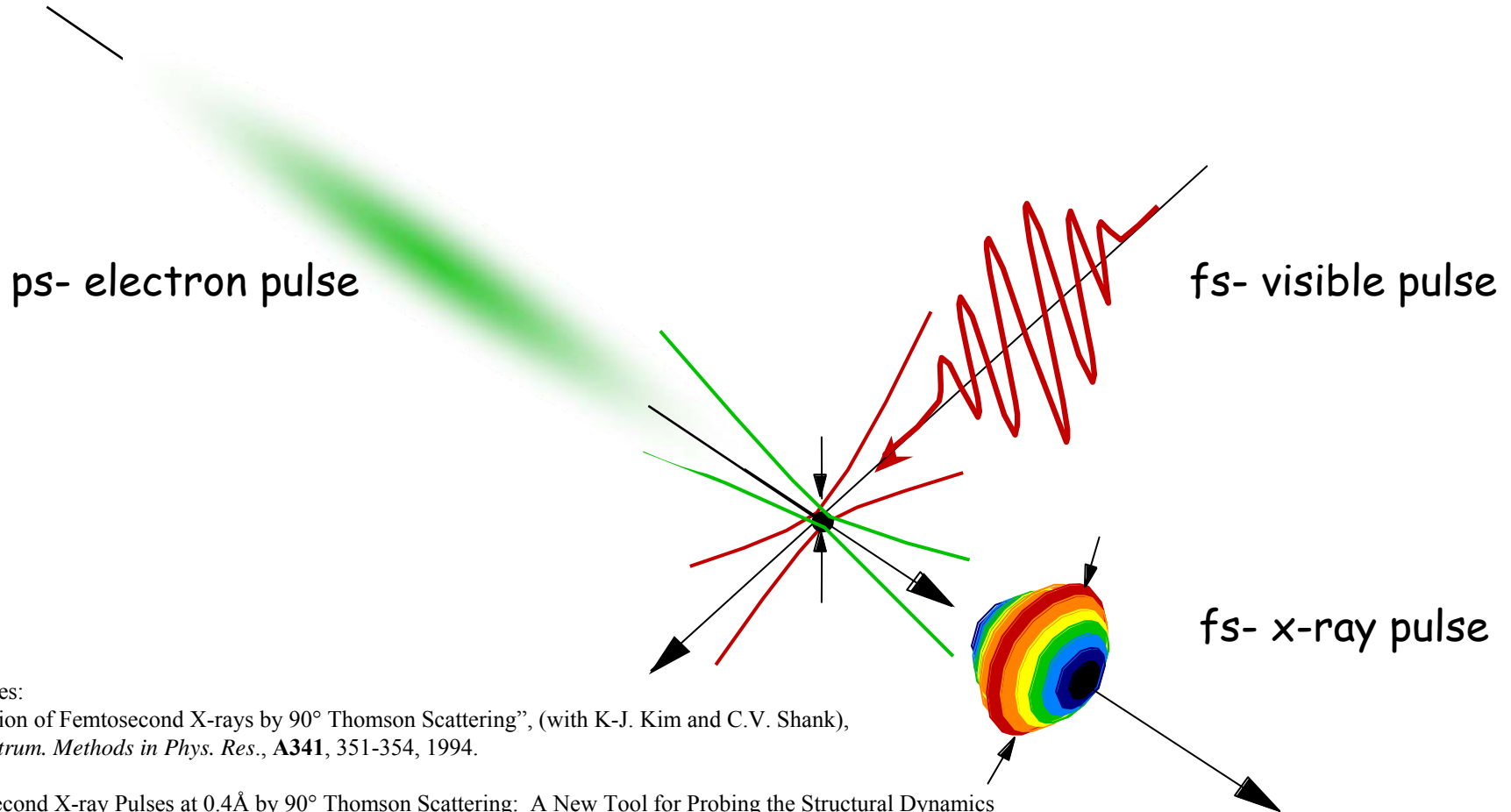
- Possibilities with a storage ring or a stand-alone linac

Laser-assisted atto-bunching:

- Laser-plasma acceleration
- Ponderomotive acceleration



Thomson Scattering for Femtosecond X-rays



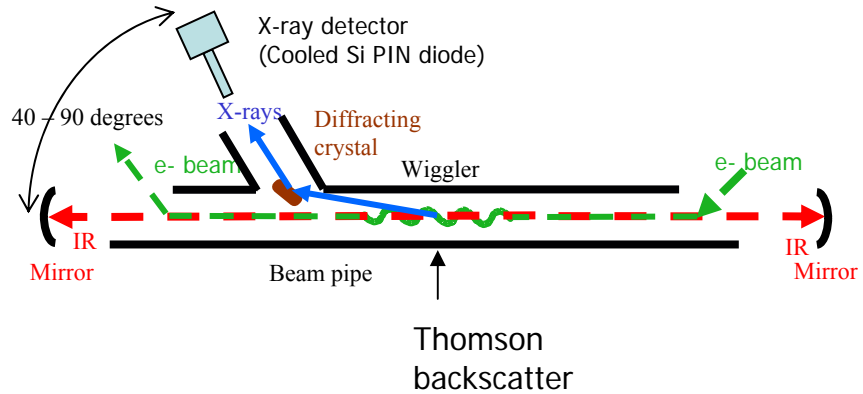
References:

"Generation of Femtosecond X-rays by 90° Thomson Scattering", (with K-J. Kim and C.V. Shank), *Nucl. Instrum. Methods in Phys. Res.*, **A341**, 351-354, 1994.

"Femtosecond X-ray Pulses at 0.4Å by 90° Thomson Scattering: A New Tool for Probing the Structural Dynamics of Materials", (with R. Schoenlein, et. al), *Science*, **274**, 11 Oct. 1996, p. 236.

"X-ray based Sub-Picosecond Electron Bunch Characterization using 90° Thomson Scattering", (with W. Leemans, et al), *PRL*, Vol. **77**, page 4182, 1996.

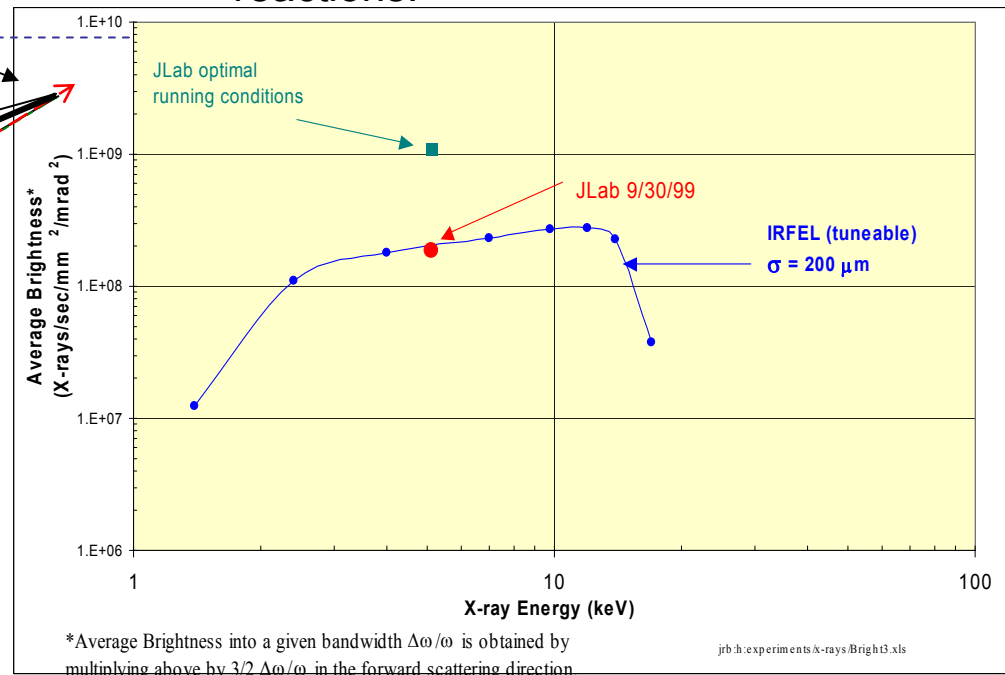
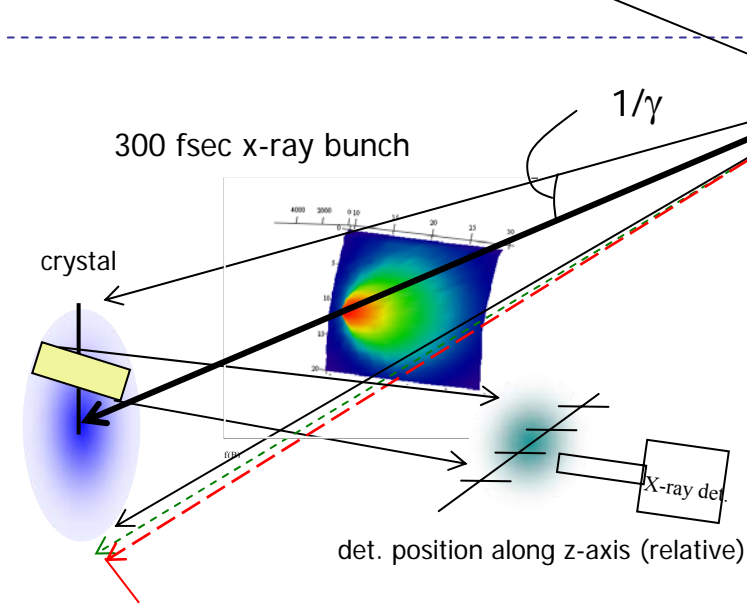
X-rays from IR DEMO at Jefferson Lab



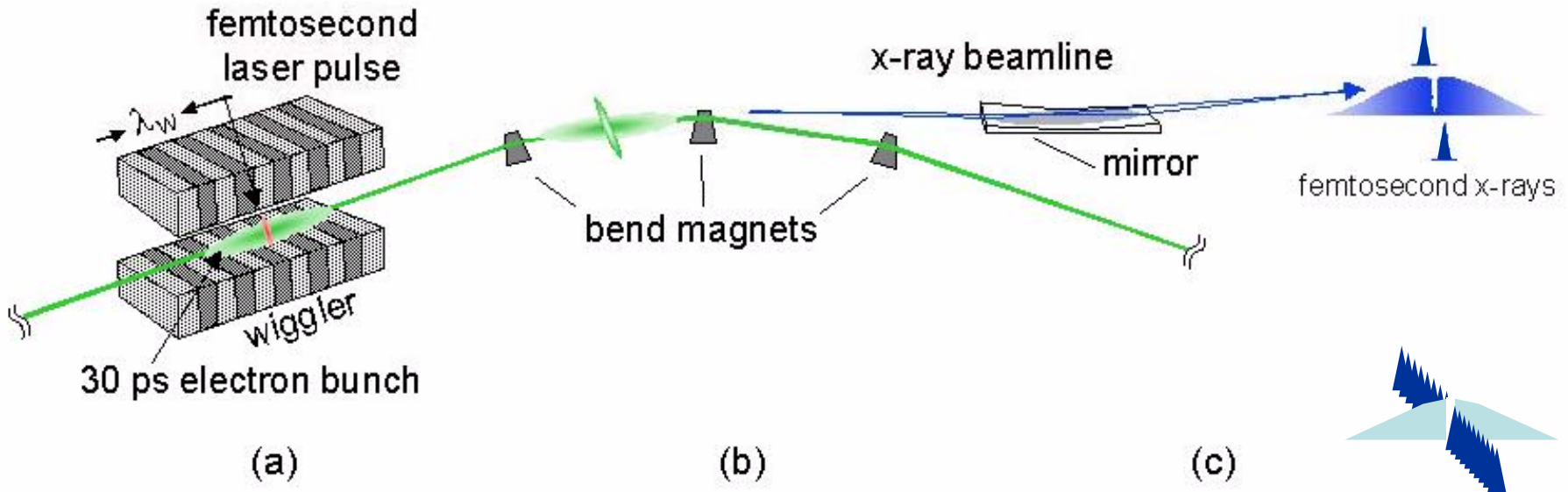
Potential Fields of Research

Femtosecond X-ray probe for:

- Solid State Physics/Material Science
 - Temporal dynamics of condensed matter phase transitions.
 - Monitoring structural changes in materials with ultra-fast time resolution.
 - Heat propagation at sub-micron dimensions.
- Biology & Chemistry
 - Short-range order changes in chemical reactions.



Laser Femto-slicing of Electron Beams



Reference:

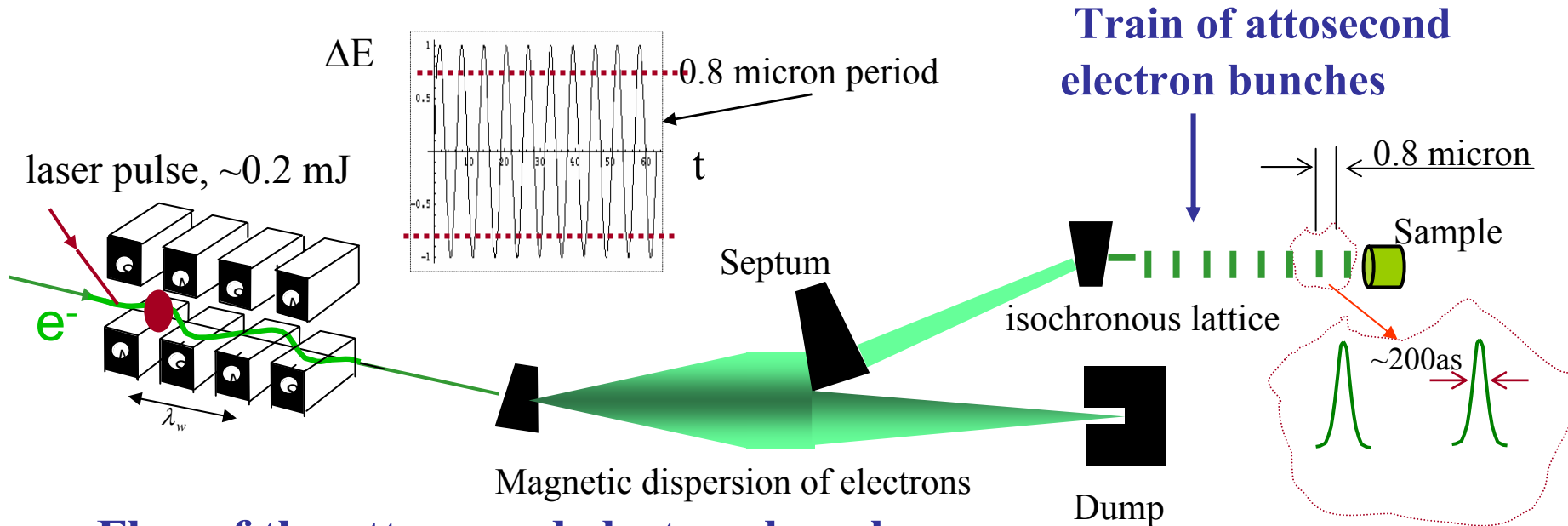
Generation of Femtosecond Pulses of Synchrotron Radiation

R. Schoenlein, S. Chattopadhyay, H.H.W. Chong, T.E. Glover, P.A. Heimann, C.V. Shank, A.A. Zholents, M.S. Zolotarev
Science, Vol. 287, No. 5461, March 24, 2000, p. 2237.

→ **Unique experiment in the world**

→ **Optical Manipulation of Beams**

Atto-Slicing: Laser Slicing Technique

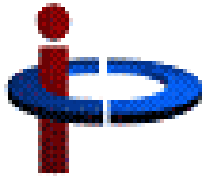


Flux of the attosecond electron bunches:

train of ~ 100 bunches, $\sim 10^6$ e/bunch, 10 kHz rep. rate

- Energy modulation was demonstrated at the ALS for femtosecond x-ray generation
- Micro-bunching at $10 \mu\text{m}$ was demonstrated at ATF/BNL
- Electron pulse separation (slicing) down to $0.1 \mu\text{m}$ must be studied

A. Zholents, et al.



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ULTRACOLD BEAMS

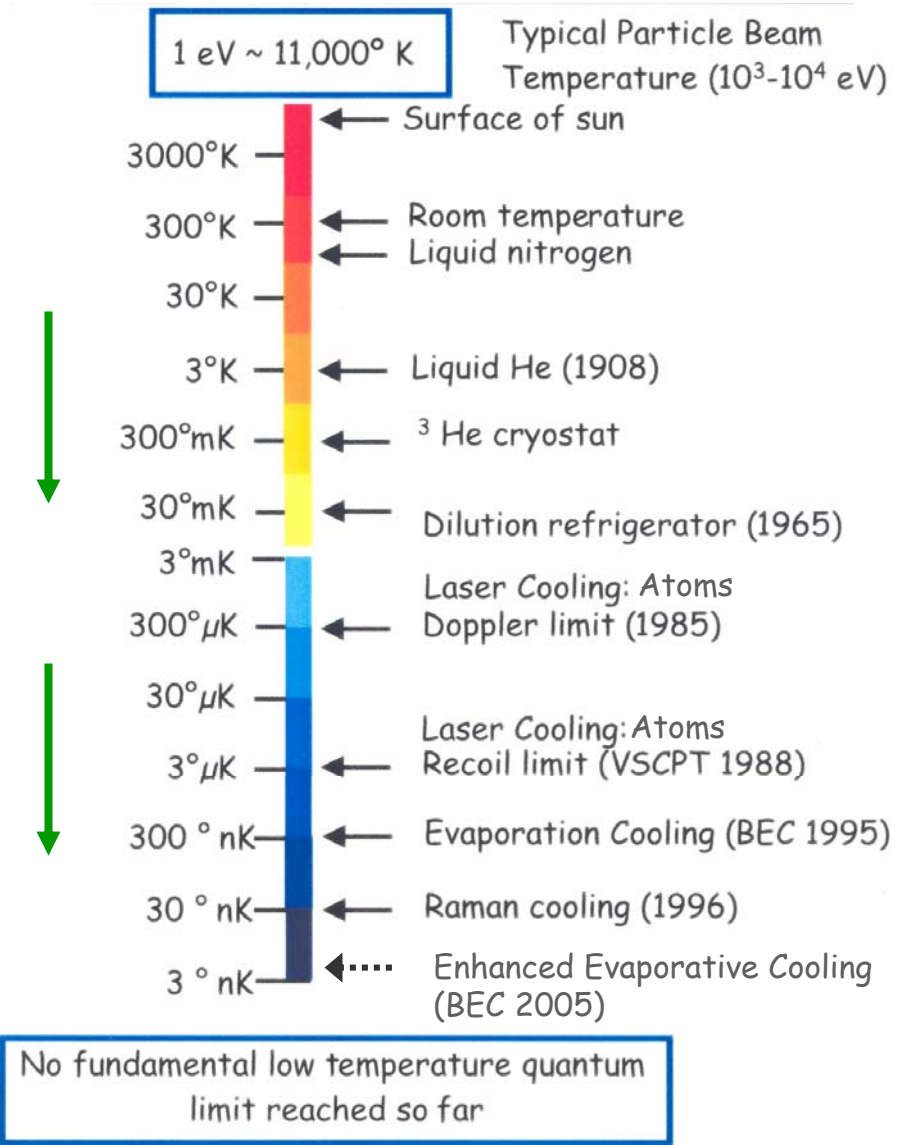
-- Innovation/Mechanisms

PHASE-SPACE COOLING: Particles and Photons

Low Temperature

Temperature Scales

Optical Cooling of
Electrons/charged
Particle Beams?



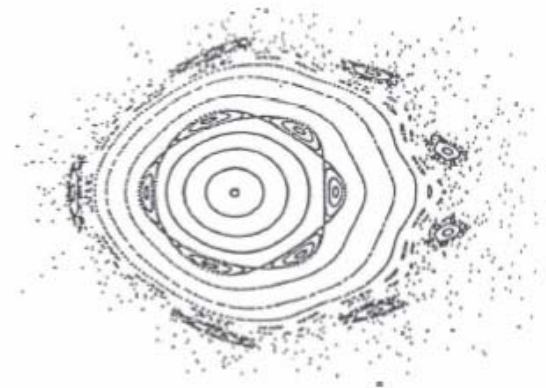
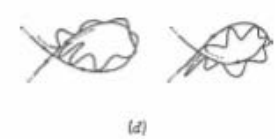
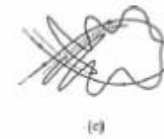
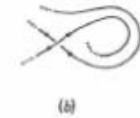
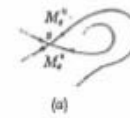
Dynamical Phase-Space of a Particle

Henri Poincaré

Geometry and Topology of Phase Space, 1880's, France



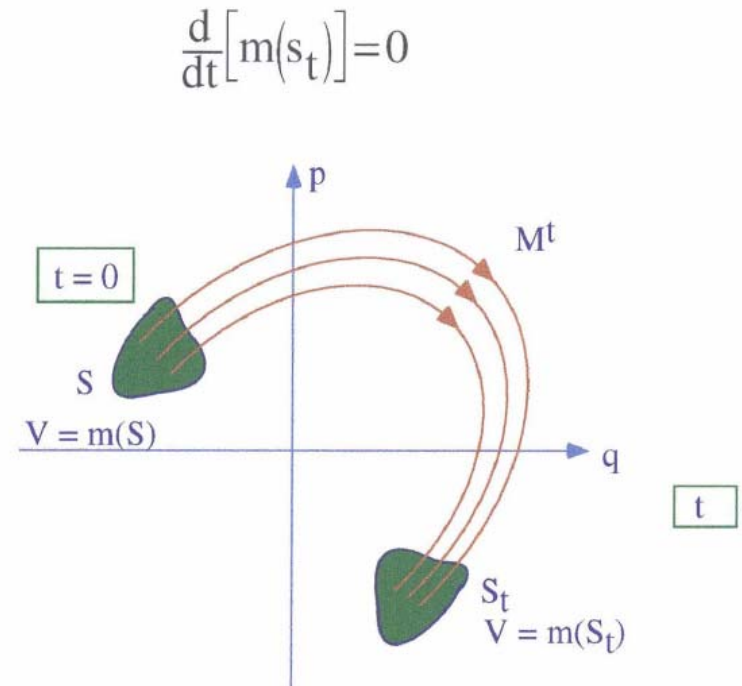
Poincaré looked at Phase-Space as full of geometrical and topological structures



Flow in Phase Space

Joseph Liouville

Phase Space Conservation, 1837 and
Non-conservation, 1838, France, with
Dissipative Forces



Hamiltonian Mapping Generating Incompressible
Liouvillian Flow in Phase-Space

To Liouville, it was all a SMOOTH FLOW, nothing violent happening anywhere except for gentle deformations: in fact, phase space volume (measure) is conserved for non-dissipative systems.

Charged Particle Beam Cooling



Simon van der Meer
**Stochastic Cooling, 1968,
CERN, Geneva, Switzerland:**

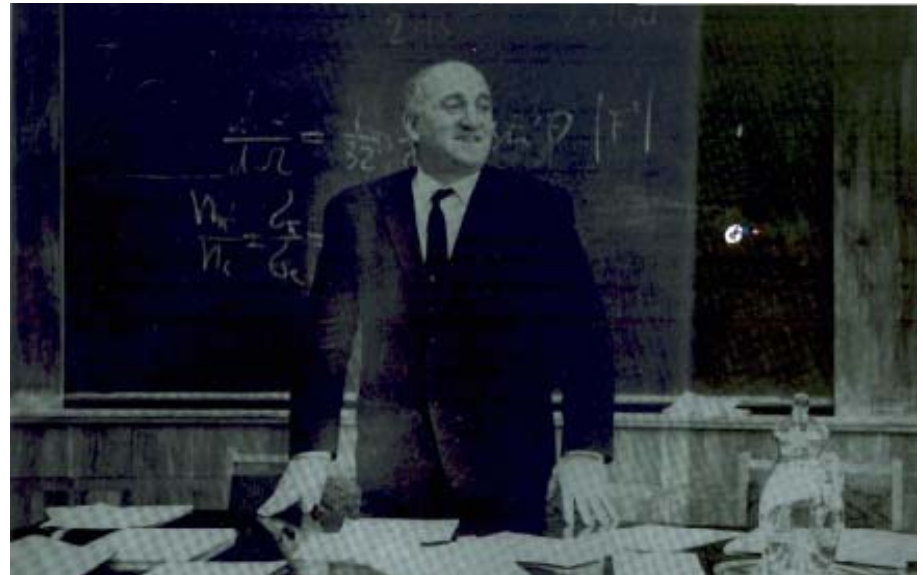
*introduced 'virtual' dissipation via a
Maxwell's Demon!*

Gersh I. Budker

Electron Cooling, 1978

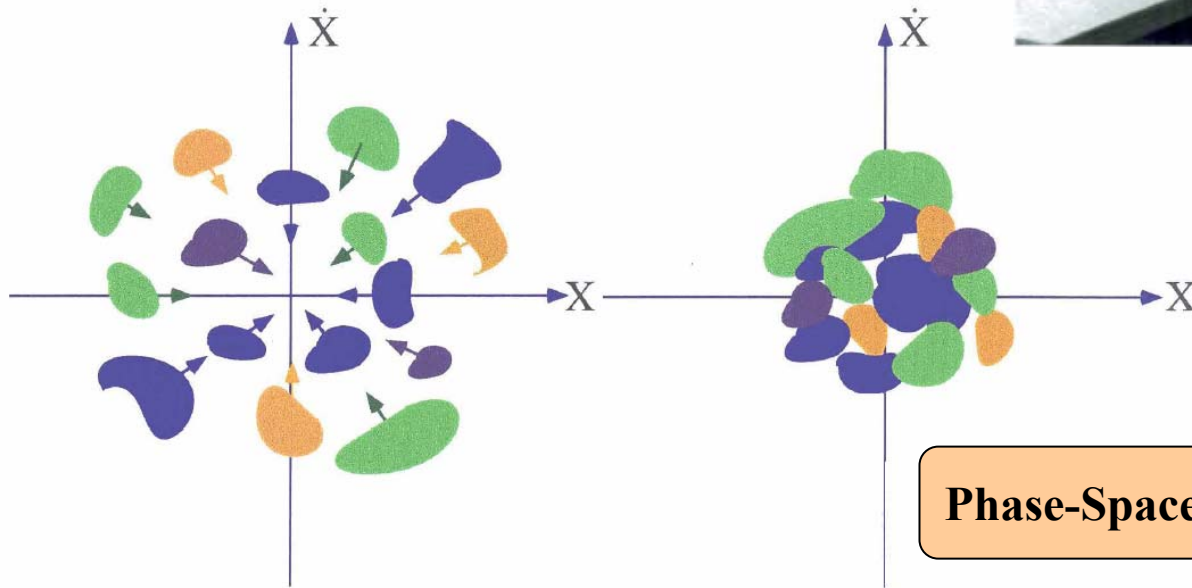
Novosibirsk, Russia:

*introduced dissipation through
Collisional Relaxation*



Stochastic Cooling

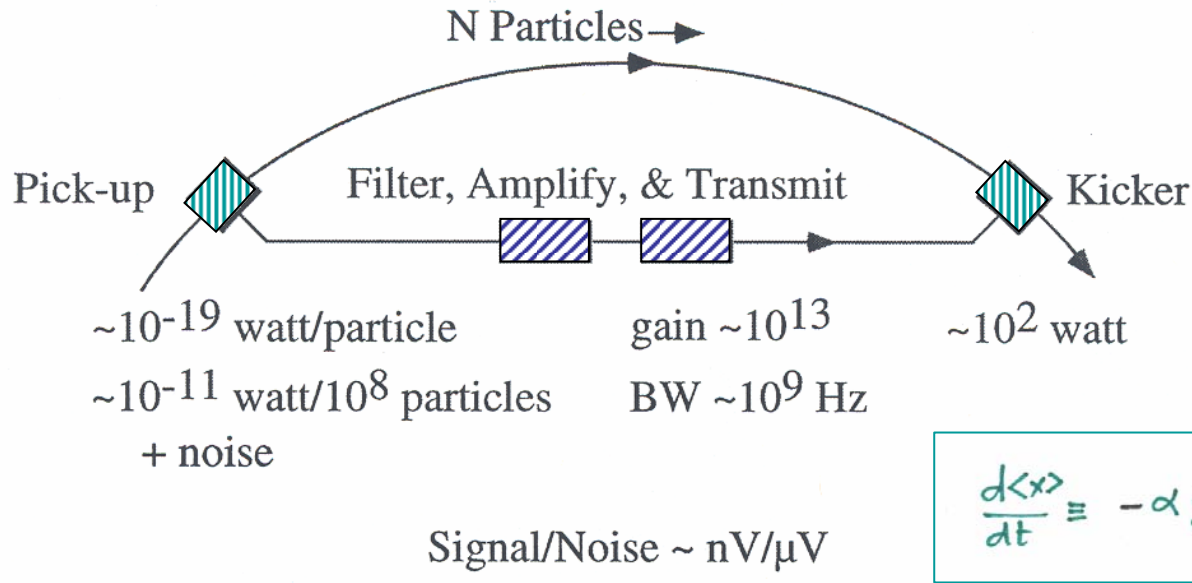
To van der Meer, phase space is mostly empty and where particles live, they cluster together leaving space in between \longrightarrow Possibility of employing a **MAXWELL'S DEMON** to herd them into a tight bunch, if only one could see the phase space clutter!



Phase-Space Cooling in Any One Dimension

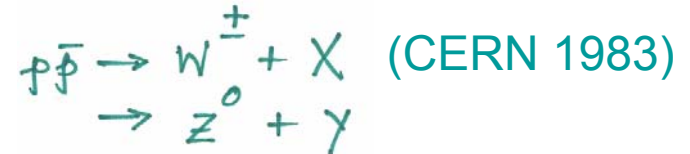
Phase Space Control and Cooling of Charged Particles in a Storage Ring

Laser cooling limited due to “fixed” narrow-band laser spectral lines. Circumvented in storage rings by microwave “Broadband” stochastic



Microwave Stochastic Beam Cooling

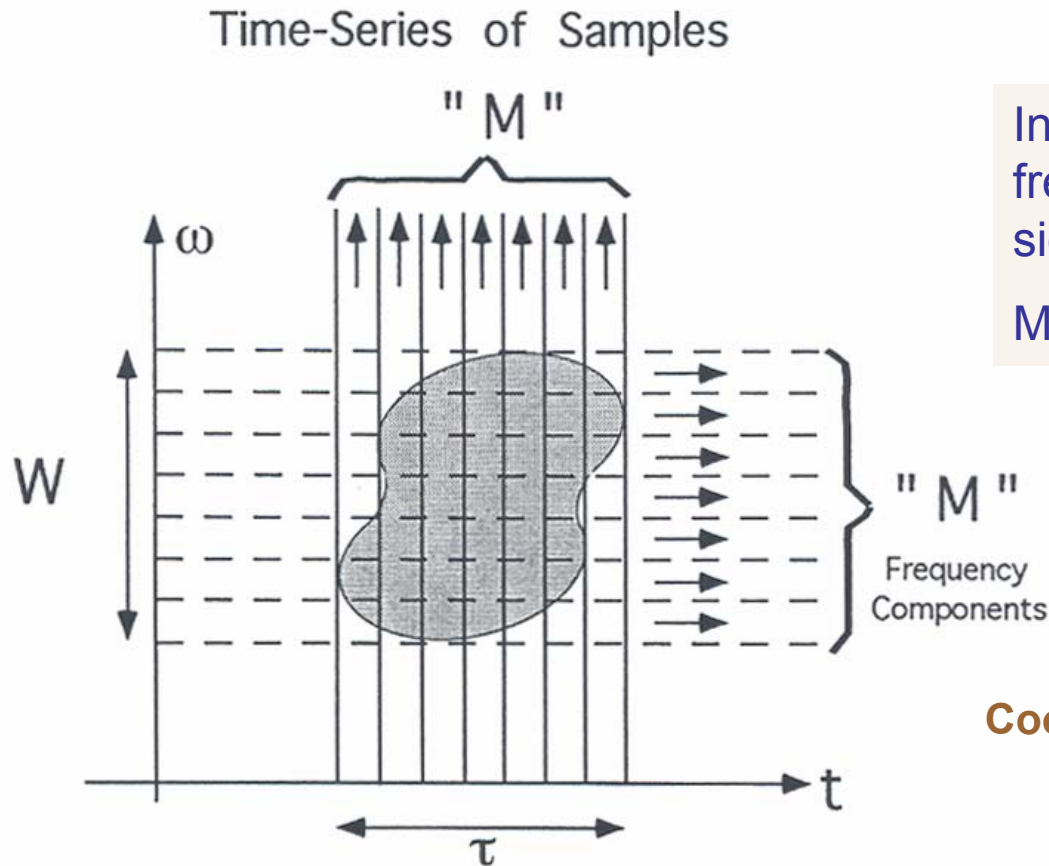
- Discovery of “W&Z Bosons”: Cold “Antiprotons”:



- Anti-Hydrogen: $\bar{p} + e^+ \rightarrow \bar{H}$ (CERN 2002)


 Cold “Antiprotons”

Information Processing in Two-Dimensional Fluctuation Signals



Independent degrees of freedom of fluctuation signal,

$$M = 2W \cdot \tau$$

(Nyquist Criterion)

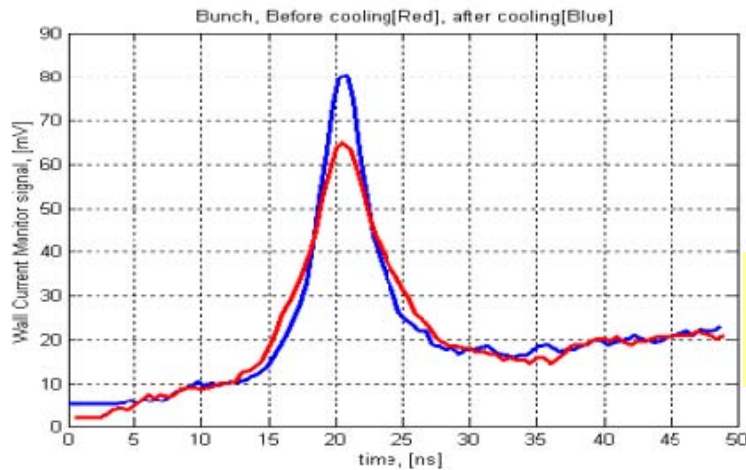
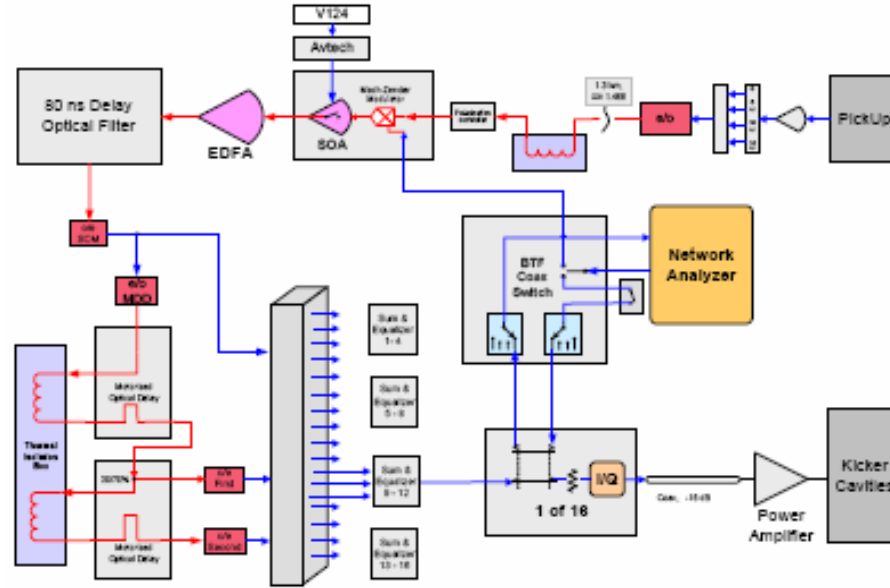
Cooling rate is proportional to "M".

Degrees of freedom of fluctuation signals in time (t)-frequency(ω) plane

These are "temporal" samples or slices in time. How about transverse "spatial" samples? Microwaves are too long in wavelength.

Wide-band Cooling Feedback Loop Electronics for Bunched Gold Beams in RHIC (Relativistic Heavy Ion Collider) at BNL

Stochastic Cooling Low Level Block Diagram



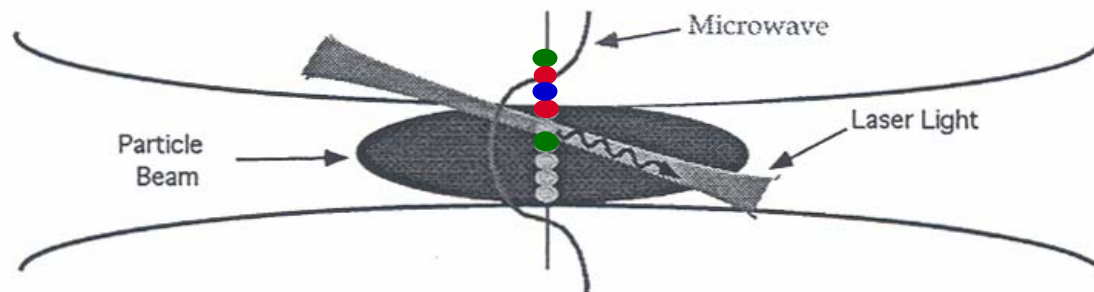
Test bunch, before (red) and after (blue) cooling.

Optical Sampling of Charged Particle Beam

Optical Coherence
Volume

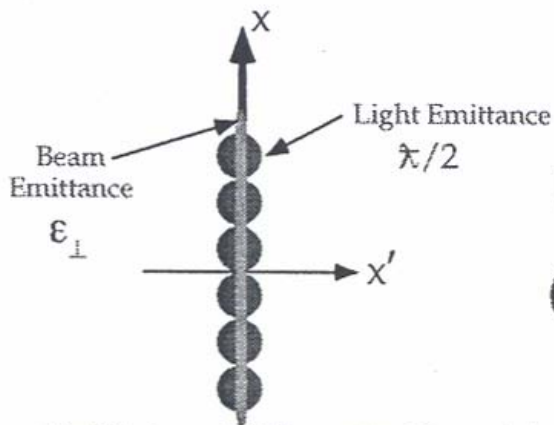
\ll

Beam Emittance



Particle
 E
 $(\Delta x_e, \Delta \phi_e)$
 β

$$\Delta x_e \cdot \Delta \phi_e = 2 \pi \epsilon_{\perp}$$



Particle beam is fully resolved in
space and time by light beam

Coherence Volume of Light < Beam Emittance

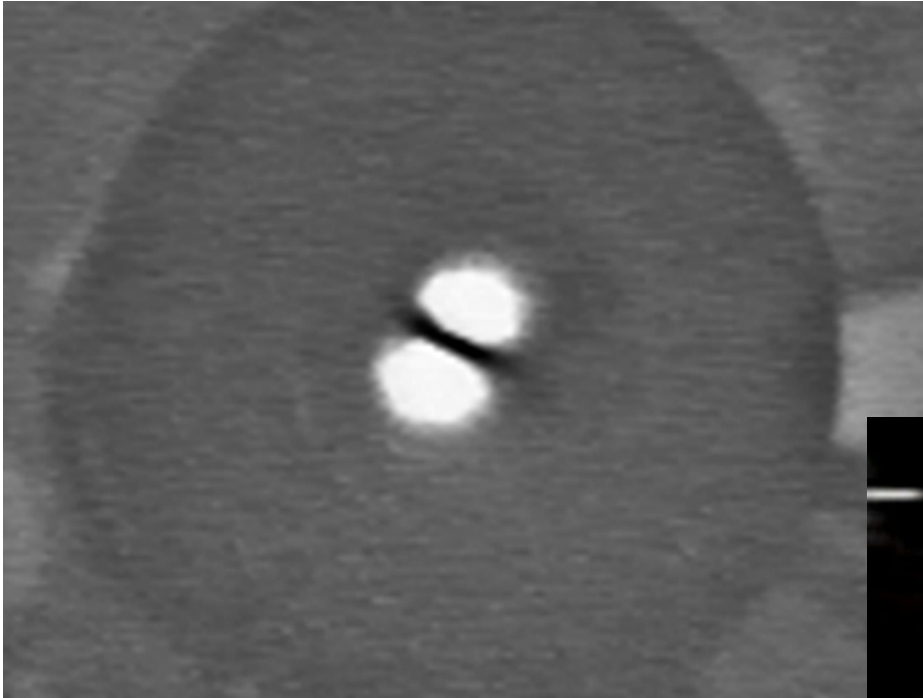
Radiation
 $\hbar \omega$
 $(\Delta x_r, \Delta \phi_r)$
 Z_r

$$\Delta \phi_r \cdot \Delta x_r = \hbar/2$$

Transverse Sampling of Particle Beams by Radiation Beam

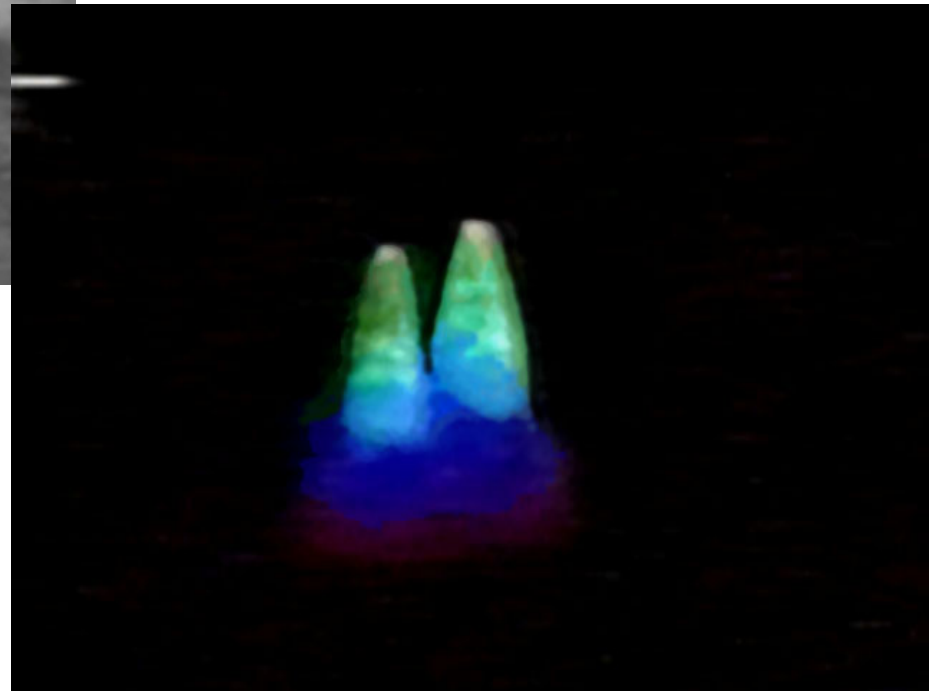
Second Harmonic Lasing at JLab FEL

resolves transverse beam at “micron” resolution



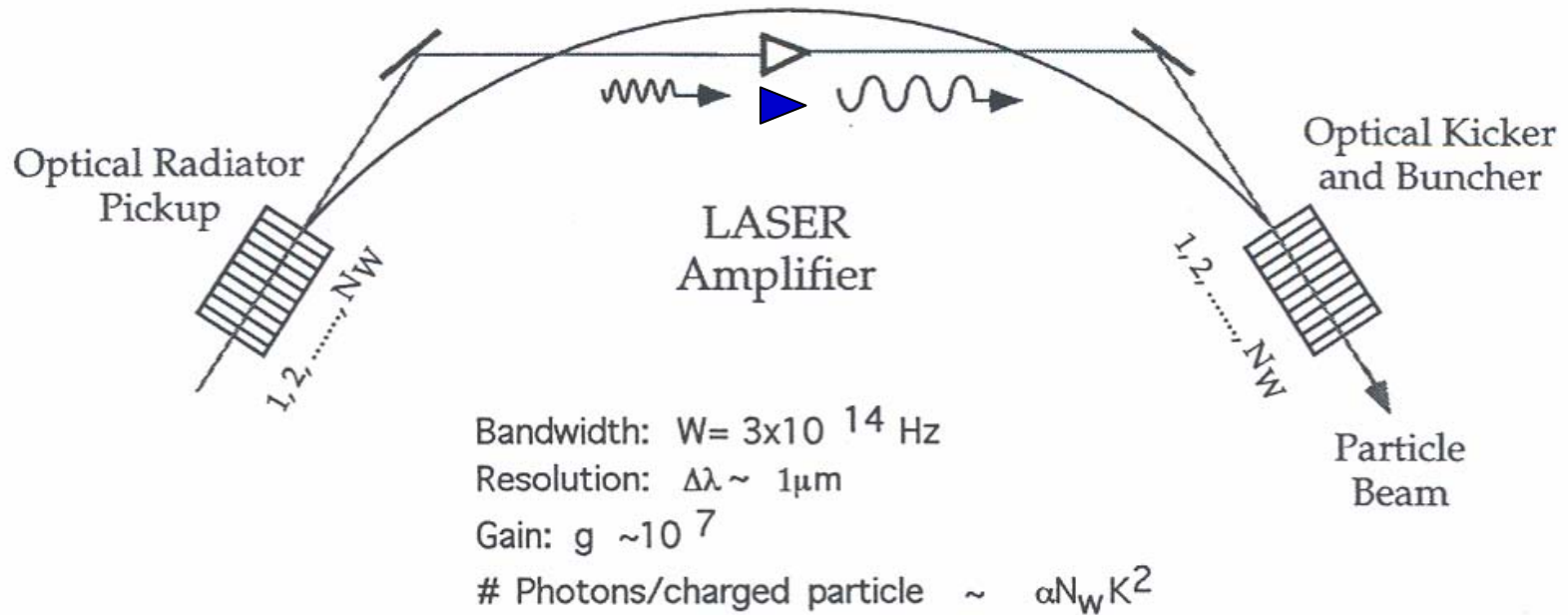
$\tau \approx 300$ fs

- **2.925 microns, 0.6 micron detuning width**
- **4.5 W average power**



Optical Cooling

(Mikhailichenko, Zholents, Zolotarev et al.)




Ultimate limitation by the “quantum” degeneracy parameter => number of photons/sample

Optical Stochastic Cooling

Can we do better?

➤ Can we tame particles as well as we tame light in lasers so we can map the phase-space of a particle beam within a light beam?

➤ What is the Reward?

- 
- **A compact Coherent X-ray Source**
 - **Compact Laser-Plasma Injectors for High Luminosity Colliders**

Compact Coherent SASE X-Ray FEL using a Laser Wiggler

FEL x-ray wavelength

$$\lambda_x = \frac{\lambda_w}{4\gamma^2} (1 + a^2)$$

Inverse gain length

$$\frac{1}{N_g} \approx \frac{2\pi}{1 + \epsilon_b / \epsilon_x} \sqrt{\frac{1}{2\gamma} \frac{I}{I_A} \frac{a^2}{1+a^2}}$$

Electron beam parameters

$$N_e = 10^6, \quad c\tau_e = 10^{-8} \text{ m}, \quad \epsilon_{nb} = 10^{-8} \text{ mrad}$$

(\equiv 30 attoseconds)

Transverse coherence requirement

$$\epsilon_b / \epsilon_x < 10$$

SASE $E_x=10$ keV

THz source ($\lambda_w=100 \mu\text{m}$)

$\gamma = 500$ (250 MeV)

$E_w=20$ J

$N_x = 6 \times 10^8$

Possible in 4GLS!!

Examples

SASE $E_x=1$ keV

Ti laser ($\lambda_w=0.8 \mu\text{m}$)

$\gamma = 13$ (6.5 MeV)

$E_w=30$ mJ

$N_x = 2 \times 10^8$

Possible on Table-top

Single Electron Quantum Diffraction Limit

- Ideal optics:

$$d_g = d_v / M^{-1}$$

where Beam Diameter is the virtual source size d_v and M^{-1} is the demagnification of the column

- Spherical aberrations:

$$d_s = 1/2 C_s a^3$$

where C_s is the spherical aberration coefficient of the final lens and a is the convergence half-angle of the beam at the target

- Chromatic aberrations:

$$d_c = C_c a DV / V_b$$

where C_c is the chromatic aberration coefficient, DV is the energy spread of the electrons, and V_b is the beam voltage

- Quantum mechanics:

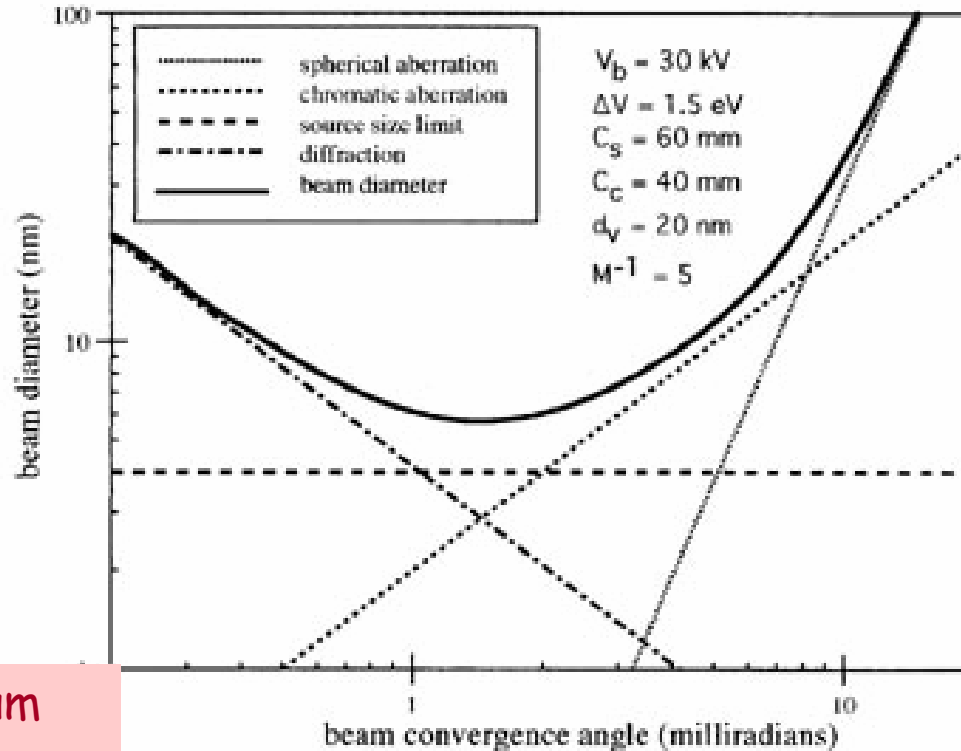
$$d_d = 0.6 L / a$$

electron wavelength $L = 1.2/(V_b)^{1/2}$ nm, although much smaller than the wavelength of light (0.008 nm at 25 kV), this wavelength can still limit the beam diameter by classical diffraction effects in very high resolution systems

To determine the theoretical beam size of a system, the contributions from various sources can be added in quadrature:

$$d = (d_g^2 + d_s^2 + d_c^2 + d_d^2)^{1/2}$$

Pure Single Particle Optics: Classical and Quantum



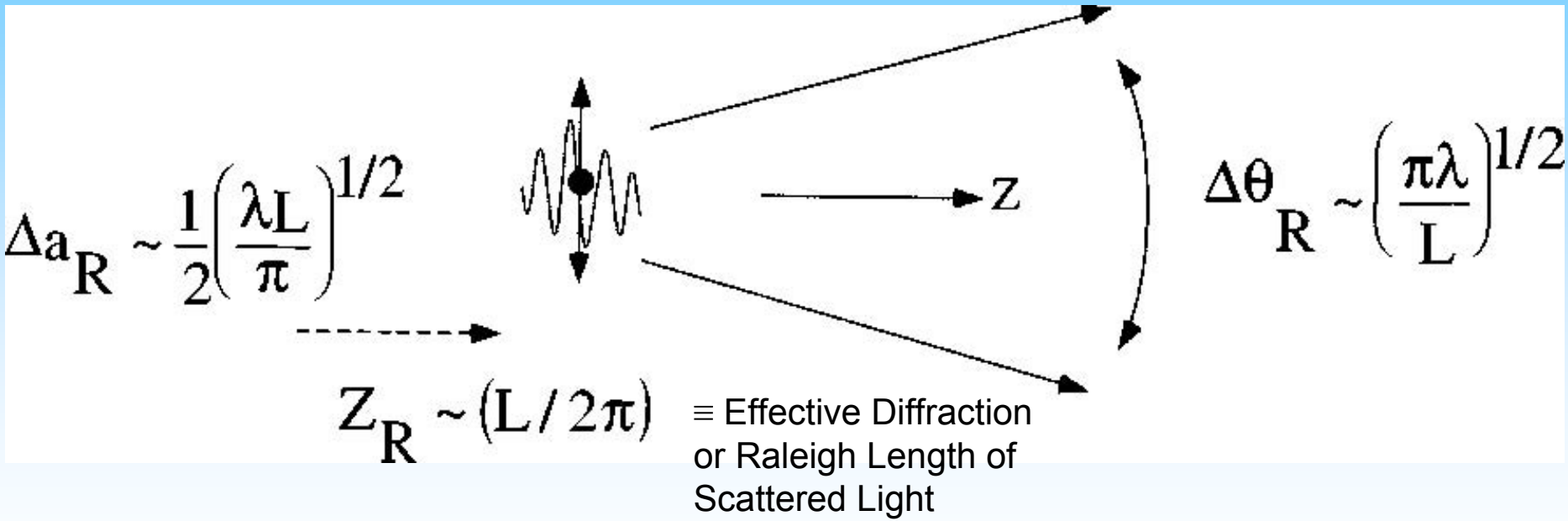
But not if the electron radiates!!!

Could reach Quantum Diffraction Limit ...

A plot showing resolution as a function of beam convergence angle for an electron beam column at 30 kV. The plot assumes an energy spread of 1.5 eV, a source diameter of 20 nm, and a fixed demagnification of 5.

Phase Space of a single oscillating electron is already comparable to the phase space of radiation

External Radiation pulse of length L , wavelength λ_0
 Radiated wavelength: $\lambda \sim \lambda_0/2\gamma^2$



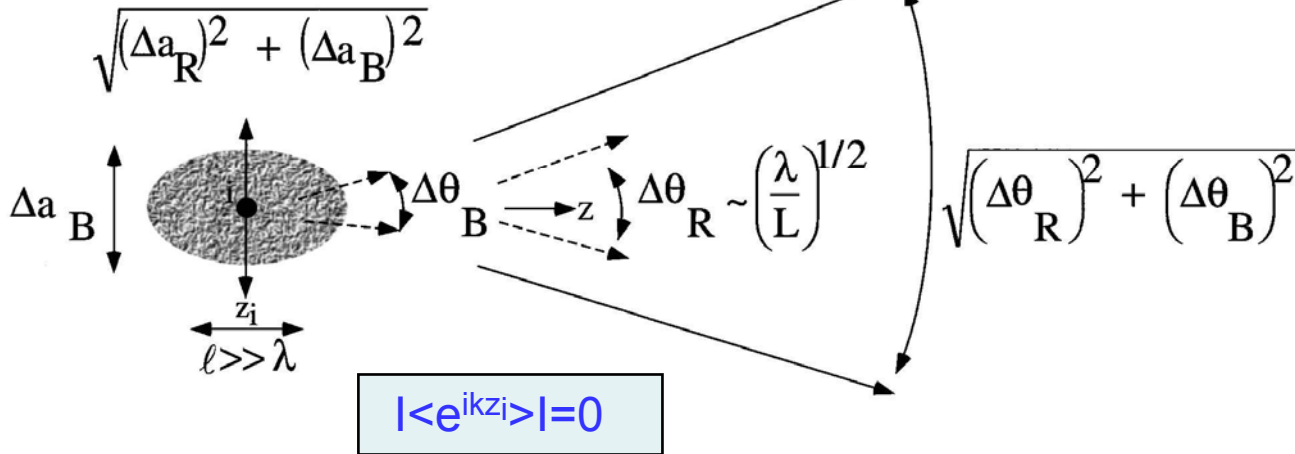
COHERENCE VOLUME:

$\Gamma = \Delta a_R \cdot \Delta \theta_R \sim \lambda/2$

Taming the Unruly ... Herding Cats

Phase Space of Radiation from a Beam

(a) Unbunched beam

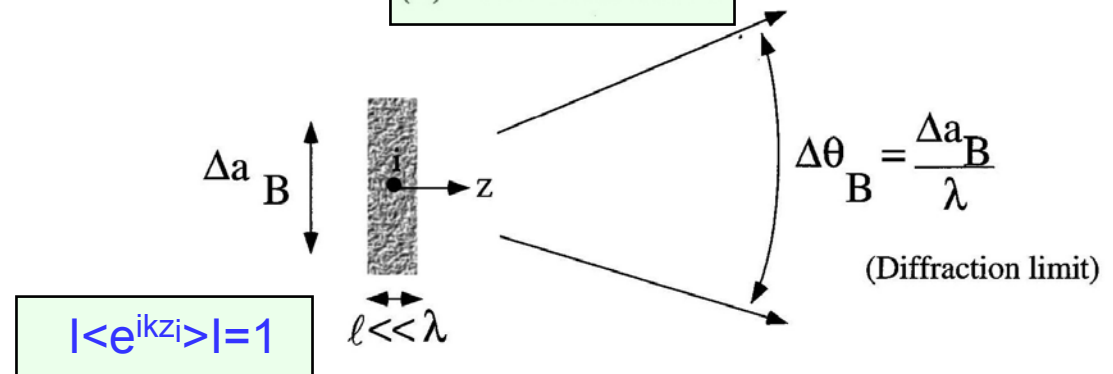


**Diffraction-limited
COHERENCE VOLUME:**

$$\Gamma = \Delta a_B \cdot A \theta_B = \frac{\Delta a_B^2}{\lambda} \sim \lambda$$

if $\Delta a_B \sim \lambda$

(b) Bunched beam



Intensity-dependent Collective Effects

- High brightness beams of today's accelerators, synchrotron radiation sources, and free electron lasers are dominated by "collective" Coulomb-space charge as well as collisional effects, in addition to single particle classical and quantum optics.
- Typical high-brightness electron beam in today's applications:

Total Charge:

$$Q \sim 1 \text{ nC} \quad (\times 10^{-5})$$

Normalized:

$$\varepsilon_{\perp} \sim 1 \text{ mm-m}_{\text{rad}} = 10^{-6} \text{ meter} \quad (\times 10^{-2})$$

Transverse Emittances:

CHALLENGE!!

Relative Energy Spread:

$$\frac{\Delta E}{E} \sim 10^{-4}$$

Pulse Length:

$$\tau \sim 200 \text{ fs to } 10 \text{ ps} \quad (\times 10^{-5})$$

Transverse Size:

$$r \sim 10\text{-}50 \text{ }\mu\text{m}$$

(can be focused to few nm at high energies such as at the ILC)

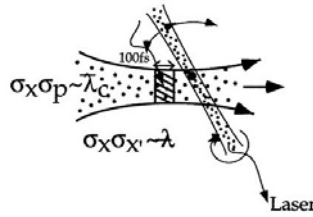
Correlated:

ACHIEVABLE

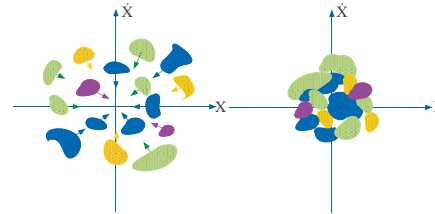
Innovations in Energy and Quality Control between Particles and Light are Key to Future Discoveries

Quality Control

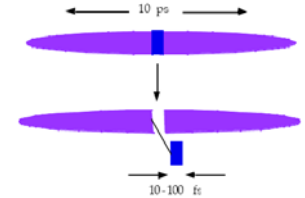
Phase-Space Mapping between Particles and Light



Phase-Space Compression

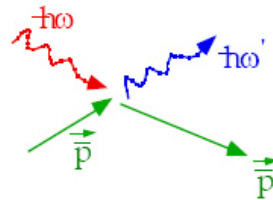


Phase-Space Slicing

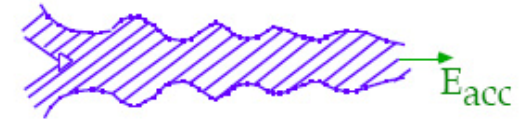


Energy Control

Energy Mapping between Particles and Light

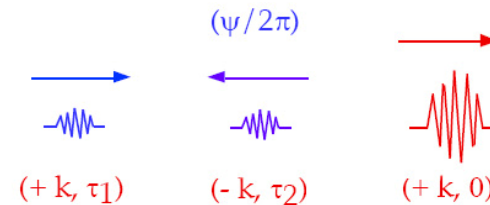


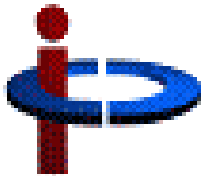
Energy Compression Focusing and Guiding



Energy and Quality Matching Between Particles and Light

Energy Mapping between Particles and Light





from Reader's Digest

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ACCELERATOR SCIENCE AND TECHNOLOGY

Don't Bet on It

AT THE END of every December, when Father Time's odometer is ready to click in another year, experts seem compelled to forecast what the coming year will bring. Economists read their econometric entrails and predict hard times or happy days accordingly; psychics announce that this is the year the San Andreas fault will pitch California into the sea. Well, before you believe any of this year's predictions, consider these vintage prognostications:

—Octave Chanute, aviation pioneer, in 1904 :
"The (flying) machine will eventually be fast ; they will be used in sport, but they are not to be thought of as commercial carriers."

—*The Literary Digest*, 1889: "The ordinary 'horseless carriage' is at present a luxury for the wealthy; and although its price will probably fall in the future, it will never come into as common use as the bicycle."

—Thomas Edison, on electricity in the home :
"Just as certain as death, [George] Westinghouse will kill a customer within six months after he puts in a system of any size."

—Lt. Joseph C. Ives, Corps of Topographical Engineers, 1861, on the Grand Canyon: "[It] is, of course, altogether valueless Ours has been the first, and will doubtless be the last, party of whites to visit this profitless locality."

—Science Digest, August 1948: "Landing and moving around on the moon offers so many serious problems for human beings that it may take science another 200 years to lick them."

—Physicist and mathematician Lord Kelvin (1824-1907), who seemed to have a corner on the wrongheaded oneliner in his day: "X-rays are a hoax." "Aircraft flight is impossible." "Radio has no future."

—Paul Dickson, *The Future File* (Rawson Associates)