

# Permanent Magnets Including Wigglers and Undulators Part III

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*June 20th-22nd, 2009*

## Part III

### ***Permanent Magnet Systems***

- Magnet design considerations
- Spectral properties of dipoles and wigglers
- Spectral properties of undulators
- Undulator shimming for field optimization
- Undulator technology
- Operation of permanent magnet undulators
- Large undulator systems for FELs

## Design phase

- function: radiation source, accelerator magnet,  
industrial application, medical application  
→ tolerance budget for the fields
- magnet stability during assembly and operation
  - baking of in-vacuum undulators (lowest gap)
  - soldering of magnets in a closed circuit (DELTA magnets)
- reproducibility (ppm vs. elect. magn., SC), reliability
- costs related to fabrication and operation (ppm vs. electromagnet)

## Construction phase

- FEM-simulations for magnetic and mechanic design
- $\mu\text{m}$ -position accuracy
- compensation of temperature effects
- magnet field measurement, shimming techniques

## Peculiarities:

- principally, infinite high fields can be realized though  $B_r < 1.6 \text{ Tesla}$   
3.9T ppm dipole: Y. Iwashita, Proc. of PAC (2003) 2198-2200.
- third quadrant operation does not mean low field contribution

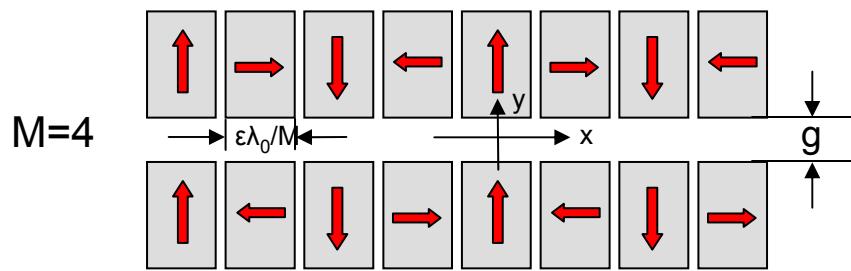
## Periodic magnet structure with field $B$ and period length $\lambda_0$

Constructive interference for the wavelength given by

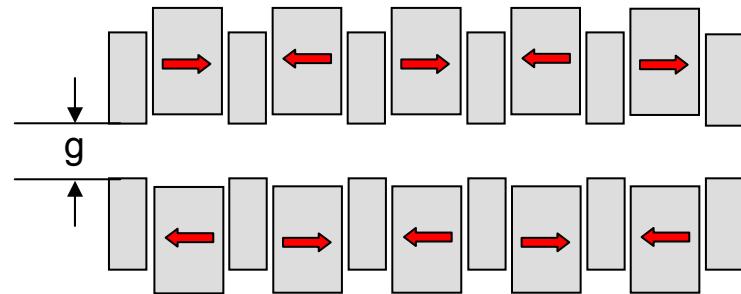
$$\lambda_n = \frac{\lambda_0}{2n\gamma^2} (1 + 0.5 \cdot K^2)$$

$$K = 93.4 \cdot B \cdot \lambda_0$$

### Halbach I: pure permanent magnet



### Halbach II: permanent magnet + Fe-pole



with  $M$ =no of magnets / period,  $\epsilon$ =filling factor

$$\vec{B}^*(\vec{z}) = i2\vec{B}_r \sum_{n=0}^{\infty} \cos(nk\vec{z}) \cdot e^{-nkg/2} \cdot (1 - e^{-nkL}) \cdot \frac{\sin(n\epsilon\pi/M)}{n\pi/M}$$

$$\vec{z} = x + i \cdot y$$

$$n = 1 + \nu \cdot M$$

$$k = 2\pi / \lambda$$

K. Halbach, Nucl. Instr. and Meth. 187 (1981) 109-117.

"One-sided fluxes -- A magnetic curiosity?"

J. Mallinson, Magnetics, IEEE Transactions on Vol. 9, No. 4 (1973) pp 678 – 682.

$$B_y \approx 3.69 \cdot \exp \left( -5.07 \cdot \frac{g}{\lambda_0} + 1.52 \cdot \left( \frac{g}{\lambda_0} \right)^2 \right)$$

Field parametrization:

P. Elleaume et al., Nucl. Instr. and Meth. in Phys. Res. A 455 (2000) 503-523

<b>1947</b>	first discussion of undulator radiation by Ginzburg
<b>1951 / 1953</b>	first production of undulator light in the mm and visible regime by Motz et al.
<b>1976</b>	FEL radiation from a superconducting helical undulator at Stanford: Madey et al.
<b>1979 / 1980</b>	first operation of insertion devices in storage rings (SSRL, LURE, VEPP3)
<b>1980...</b>	first operation of wavelength shifters in storage rings (VEPP3, SRS, VEPP2M)
<b>Today</b>	<ul style="list-style-type: none"><li>- about 20 third generation synchrotron radiation light sources</li><li>- SASE FELs operational in the infrared, visible, UV, and X-ray regime (VISA, LEUTL, FLASH, LCLS ...)</li></ul>

## first generation:

parasitic use of SR at high energy rings,  
bending magnets (DESY, DORIS...)

## second generation:

dedicated storage rings, bending magnets  
and a few insertion devices (BESSY I...)

## third generation:

dedicated storage rings optimized for the  
use of insertion devices (BESSY II, ALS, ELETTRA, MAX-II...,  
SLS, DIAMOND, SOLEIL, ALBA..., ESRF, APS, SPRING-8...)

## fourth generation:

linac based SASE-FEL (e.g.: European XFEL, LCLS, SCSS)  
seeded FEL such as: cascaded HGHG or EEHG, selfseeding  
energy recovery linacs (ERLs)  
laser plasma accelerator based table top FEL

# Synchrotron Radiation: Starting from Maxwell's Equations...

The Lienard-Wiechert potentials are the solution  
of the inhomogenous Maxwell equations

$$\Phi(\vec{x}, t) = \left[ \frac{e}{(1 - \vec{\beta} \cdot \vec{n})R} \right]_{ret}$$

The brackets are evaluated at  
the retarded time:

$$\vec{A}(\vec{x}, t) = \left[ \frac{e\vec{\beta}}{(1 - \vec{\beta} \cdot \vec{n})R} \right]_{ret}$$

$$t' = t - R(t')/c$$

The acceleration and velocity fields are derived from these potentials:

$$\vec{E}^{acc}(t) = \frac{e}{4\pi\epsilon_0 c} \cdot \left[ \left( \vec{n} \times \left[ (\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}} \right] \right) / \left( R \cdot (1 - \vec{\beta} \cdot \vec{n})^3 \right) \right]_{ret}$$

$$\vec{E}^{vel}(t) = \frac{e}{4\pi\epsilon_0} \cdot \left[ (\vec{n} - \vec{\beta}) / \left( \gamma^2 \cdot R^2 \cdot (1 - \vec{\beta} \cdot \vec{n})^3 \right) \right]_{ret}$$

$$\vec{B} = \frac{1}{c} \left[ \vec{n} \times \vec{E} \right]_{ret}$$

$$\frac{\partial^2 I}{\partial t \partial \Omega} = |\vec{S}|^2 R^2$$

$$\vec{S} = \vec{E} \times \vec{H}$$

The emitted power is given by the poynting vector  $\vec{S}$

The spectrum is evaluated via a Fourier transformation of the time dependent fields

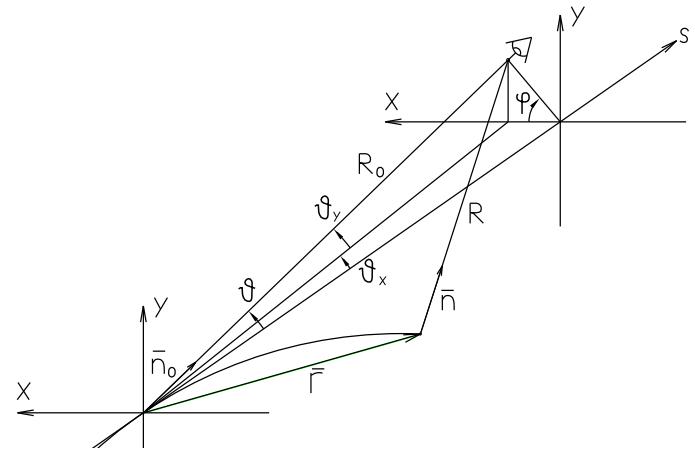
$$\frac{\partial^2 I}{\partial \omega \partial \Omega} = \frac{e^2}{16\pi^3 \epsilon_0 c} \left| \int_{-\infty}^{\infty} \left[ \left( \vec{n} \times \left( (\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}} \right) \right) \middle/ (1 - \vec{\beta} \cdot \vec{n})^3 \right]_{ret} e^{i\omega t} dt \right|^2$$

In the far field we approximate:

$$R(t') \approx R_0(t') - \vec{n}_0 \cdot \vec{r}(t')$$

$$\vec{n} = \vec{n}_0$$

$$\frac{\partial^2 I}{\partial \omega \partial \Omega} = \frac{e^2}{16\pi^3 \epsilon_0 c} \left| \int_{-\infty}^{\infty} \left[ \left( \vec{n} \times \left( (\vec{n} - \vec{\beta}) \times \dot{\vec{\beta}} \right) \right) \middle/ (1 - \vec{\beta} \cdot \vec{n})^2 \right] e^{i\omega(t - \vec{n} \cdot \vec{r})} dt \right|^2$$



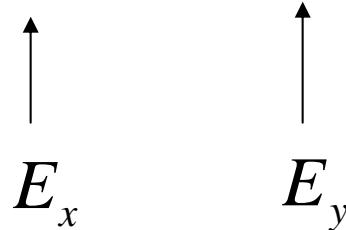
$$\frac{\partial^2 I}{\partial \omega \partial \Omega} = \frac{3e^2}{16\pi^3 \epsilon_0 c} y^2 \gamma^2 (1 + X^2)^2 \left| K_{2/3}(\xi), -i\sqrt{X^2/(1+X^2)} K_{1/3}(\xi) \right|^2$$

$$\xi = \frac{y}{2} (1 + (\gamma \theta_y)^2)^{3/2}$$

$$y = \omega / \omega_c$$

$$\omega_c = (3\gamma^3 c) / (2\rho)$$

$\rho$ =bending radius



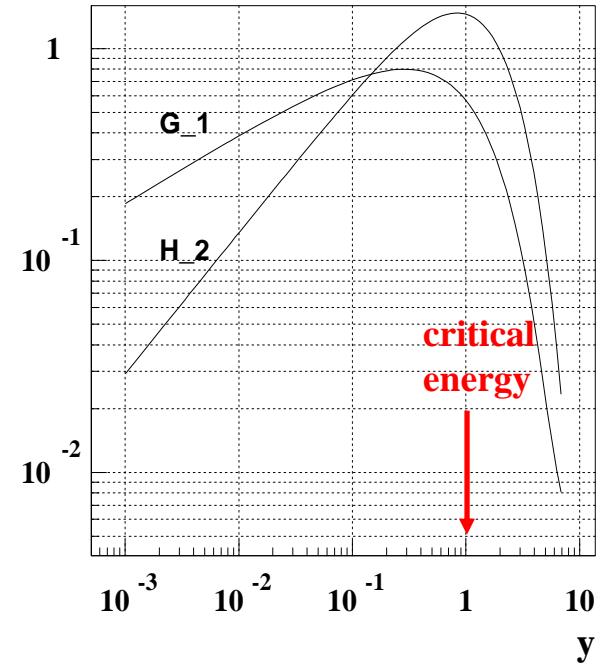
The critical energy divides the power spectrum into equal parts.

on axis flux density (ph / s / mrad\*\*2 / 0.1%BW)

$$\frac{\partial^2 \tilde{F}}{\partial (\Delta \omega / \omega) \partial \Omega} = 1.327 \cdot 10^{13} \cdot E(GeV)^2 \cdot I(A) \cdot H_2(y)$$

vertically integrated flux (ph / s / mrad / 0.1%BW)

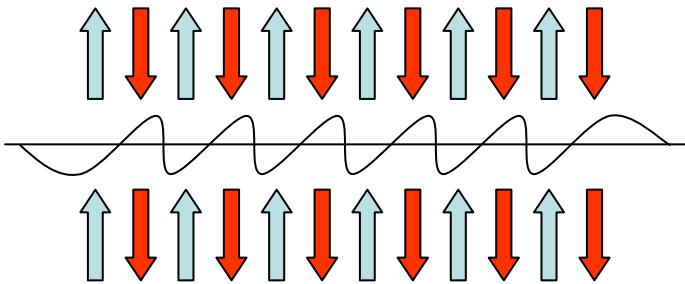
$$\frac{\partial^2 \tilde{F}}{\partial (\Delta \omega / \omega) \partial \theta_x} = 2.457 \cdot 10^{13} \cdot E(GeV) \cdot I(A) \cdot G_1(y)$$



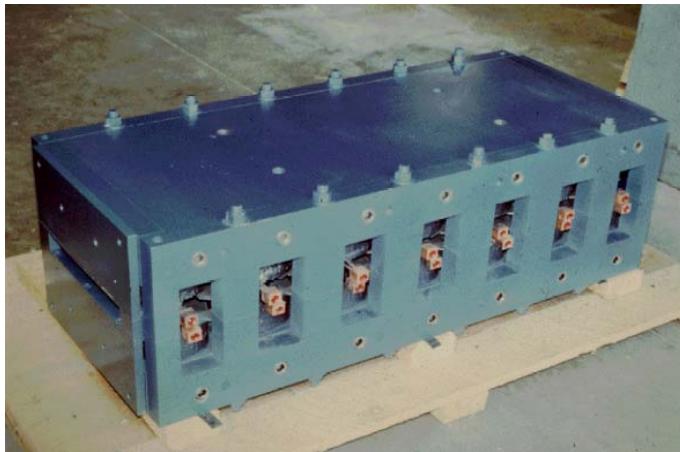
The critical energy scales with the second power of the electron energy

# Increasing the Photon Flux

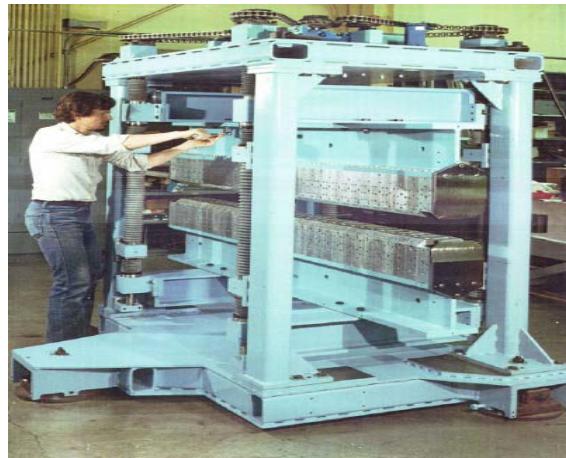
## Wiggler: A Sequence of Alternating Dipoles



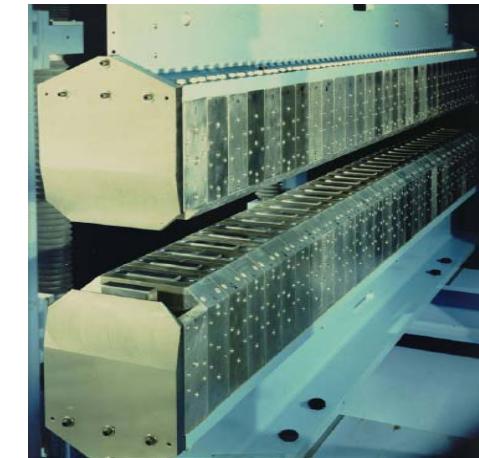
brilliance scales linearly with number of poles  
incoherent overlap of light from individual poles  
spectrum =  $n$  times dipole spectrum



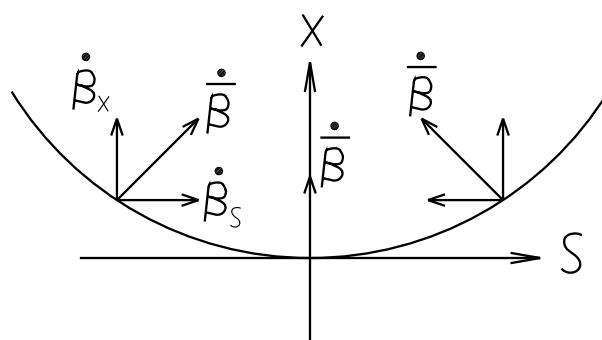
SSRL 1978  
Electromagnetic 7 poles wiggler



LBL / SSRL 1985  
54 poles hybrid wiggler



# Bending Magnets, Polarization

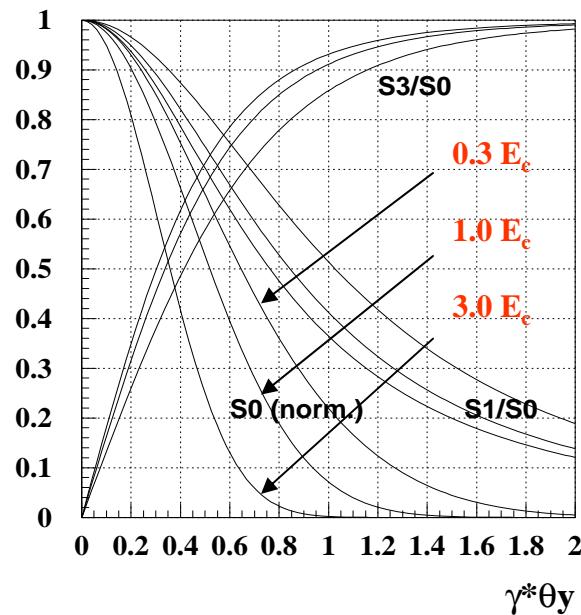


$$\beta_y = \dot{\beta}_y = 0 \quad (\text{B-field in y-direction})$$

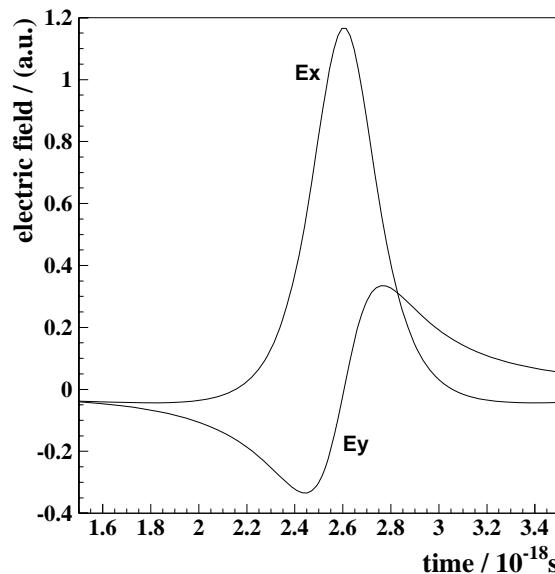
$$\Delta E_x \propto -\dot{\beta}_x \cdot (n_y^2 + n_s^2) + \dot{\beta}_s \cdot n_x n_s + (-\beta_x \dot{\beta}_s + \beta_s \dot{\beta}_x) \cdot n_s$$

$$\Delta E_y \propto \dot{\beta}_x \cdot n_x n_y + \dot{\beta}_s \cdot n_y n_s$$

small  
symmetric  
antisymmetric



S1/S0=degree of linear polarization  
S3/S0=degree of circular polarization

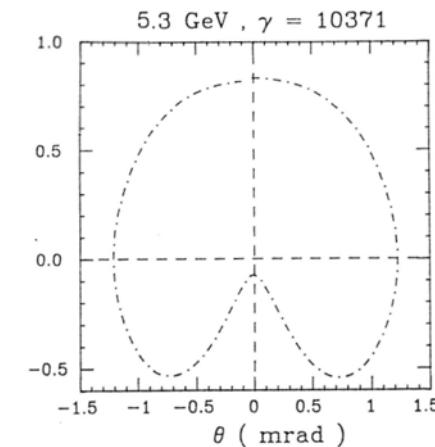
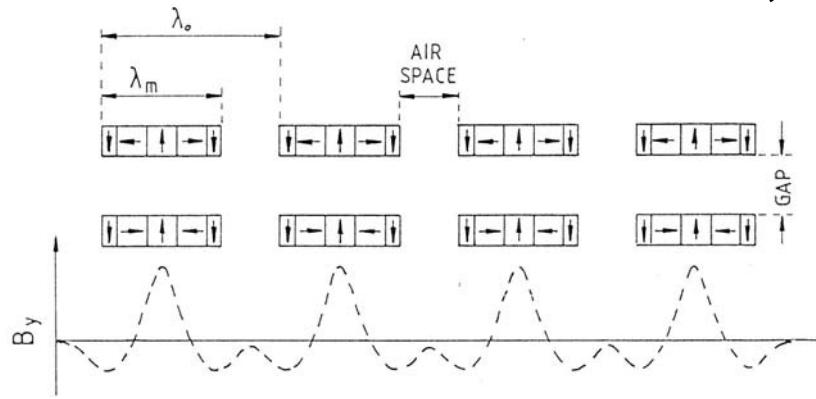


$\Delta E_x$  and  $\Delta E_y$

are out of phase  
by:  $\pi/2$

Circularly polarized off plane bending magnet radiation was widely used at BESSY I

## DESY, ESRF

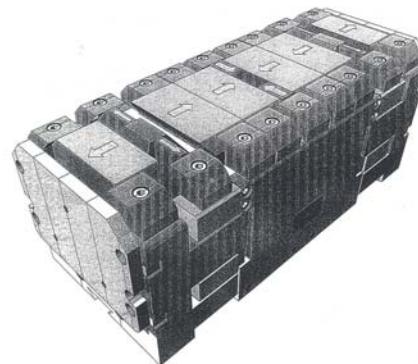


J. Pflüger, G. Heintze, Nucl. Instr. and Meth. 289 (1990) 300-306

J. Goulon et al. Nucl. Instr. and. Meth. 254 (1987) 192-201

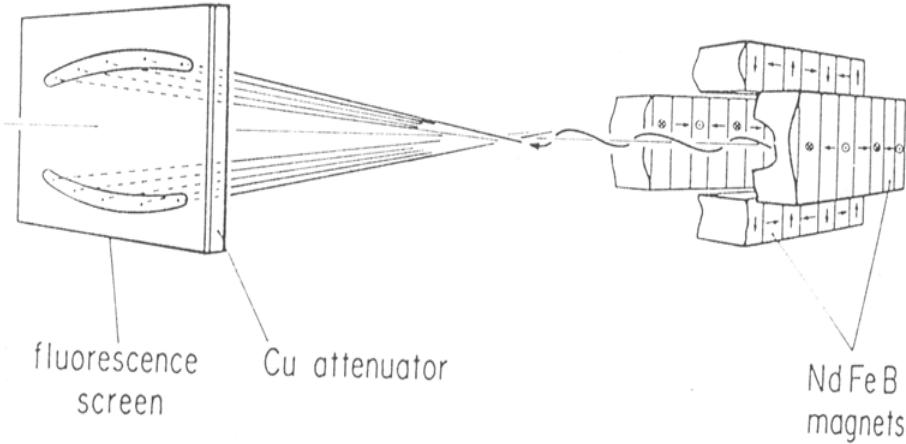
## Asymmetric wiggler, ESRF

Hybrid type,  $B = 3.1$  Tesla  
 $\text{gap} = 11\text{mm}$ ,  $\lambda = 378\text{mm}$

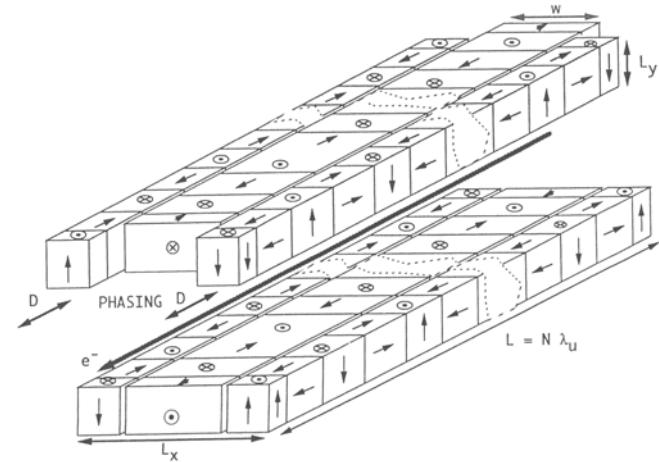


Helicity switching  
via changing the  
observation angle

J. Chavanne, P. Van Vaerenbergh and P. Elleaume,  
*Nucl. Instr. And Meth. in Phys. Res. A*, 421 (1999) 352-360



S. Yamamoto *et al.*, Phys. Rev. Lett.,  
62 (1989) 2672-2675



X. M. Marechal *et al.*, Rev. Sci. Instr.  
66 (1995) 1937-1939

Helicity Switching via mechanical movement of magnet rows

resonance condition

$$\lambda = \frac{\lambda_0}{2\gamma^2} \left( 1 + K^2 / 2 + \gamma^2 \theta^2 \right)$$

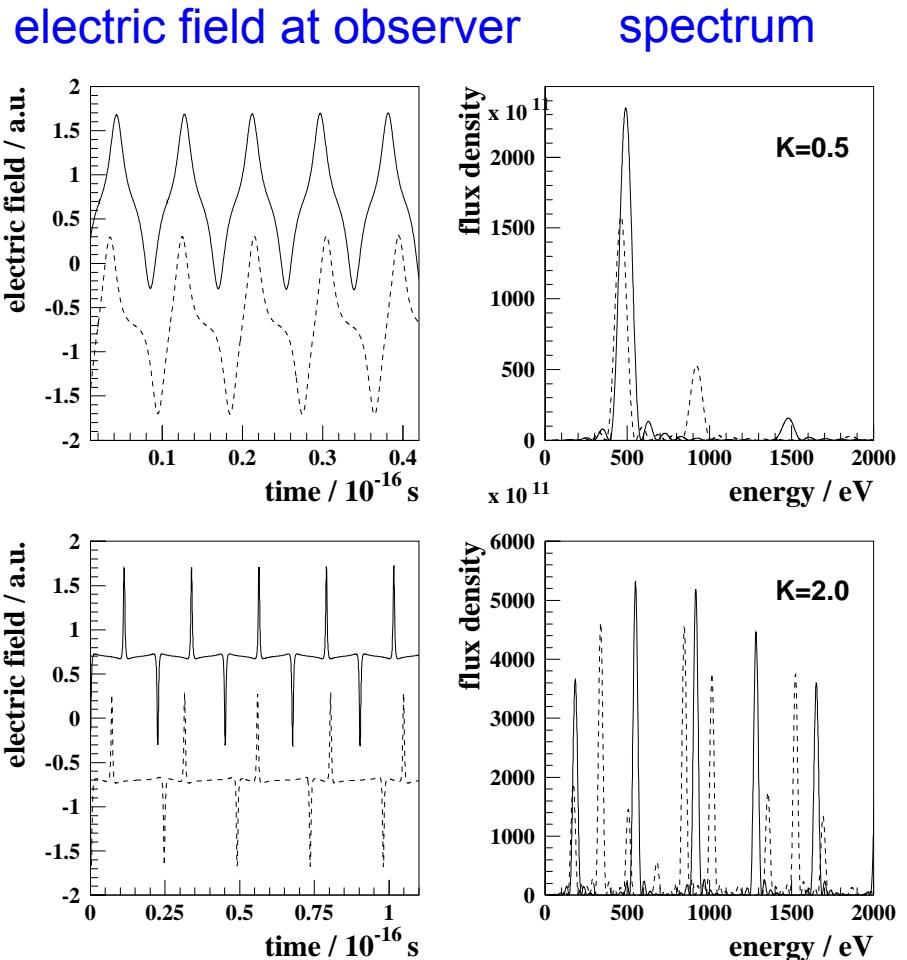
$$K = 93.4 \cdot \lambda_0 \cdot B_0$$

figure 8 motion in moving frame produces higher harmonics  
on axis: only odd harmonics

$$x(t) = \frac{Kc}{\gamma\omega_u} \sin(\omega_u t)$$

$$s(t) = \bar{\beta}ct - \frac{K^2 c}{8\gamma^2 \omega_u} \sin(2\omega_u t)$$

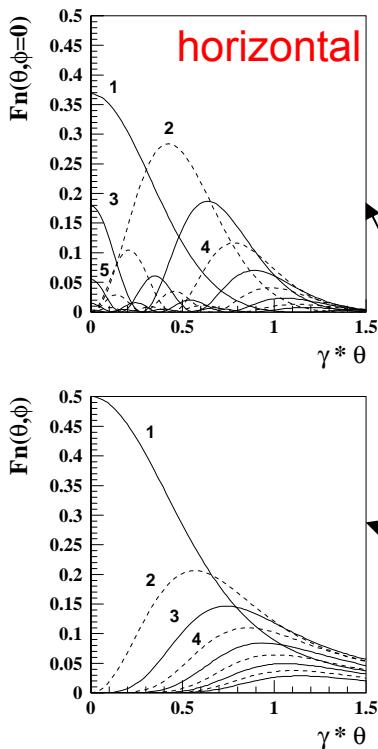
off axis: also even harmonics



$$\frac{\partial^2 I}{\partial \omega \partial \Omega} = \frac{e^2 \gamma^2 N^2}{4\pi \epsilon_0 c} \cdot F_n(K_x, K_y, \gamma\theta, \gamma\Phi) \cdot \frac{\sin^2(N\pi \cdot \Delta\omega / \omega_1(\theta))}{N^2 \sin^2(\pi \cdot \Delta\omega / \omega_1(\theta))}$$

Fn represents an infinite sum over BESSEL functions.  
 The line shape function (last term) describes the interference effects.

Fn



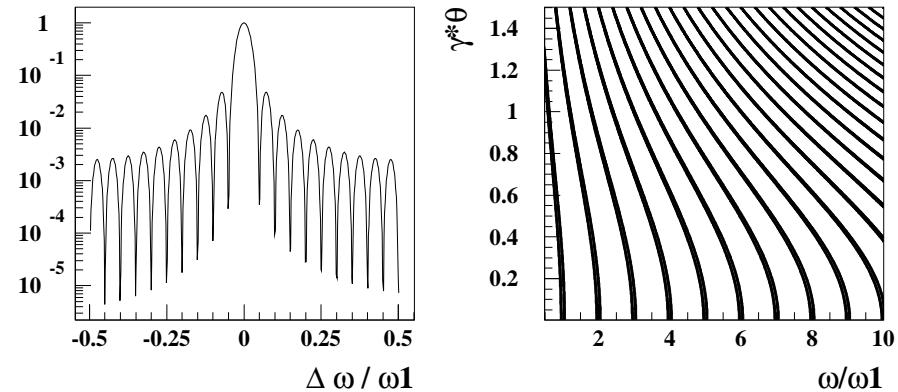
planar device

Ky=1

helical device

Kx=Ky=1

line shape function



The angular divergence and the spectral width can be derived from the line shape function

divergence:  $\sigma_{r'} = \sqrt{\lambda / 2L}$

spectral width:  $\frac{\Delta\omega}{\omega_n} = \frac{1}{nN}$

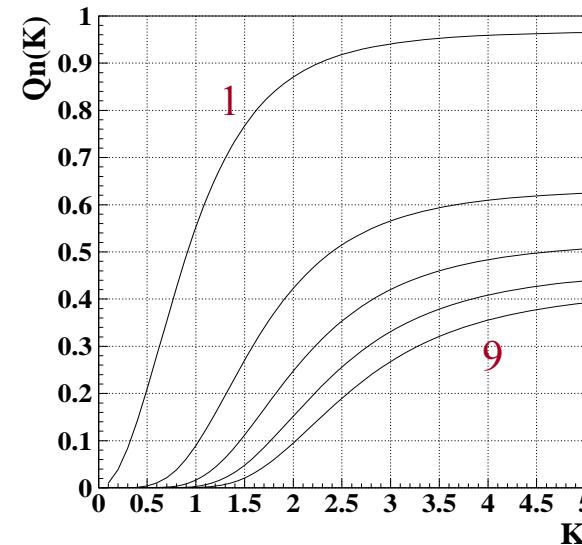
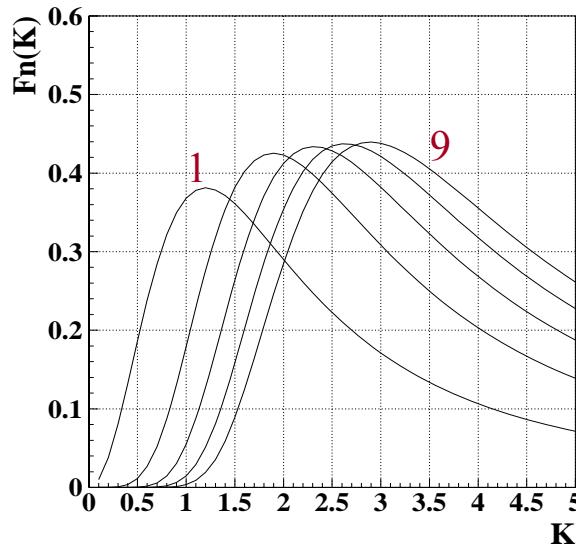
on axis flux density of the nth harmonic (ph / s / mrad\*\*2/ 0.1%BW)

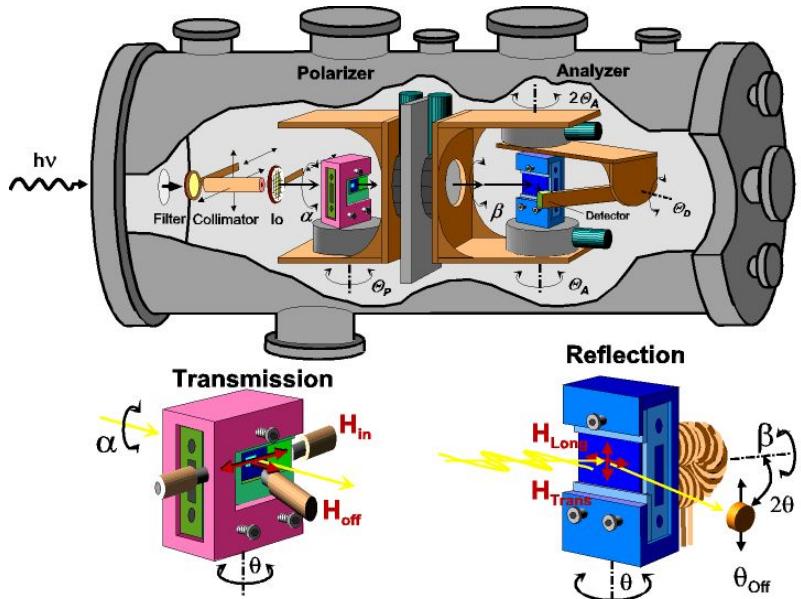
$$\frac{\partial^2 \tilde{F}}{\partial(\Delta\omega/\omega)\partial\Omega} = 1.744 \cdot 10^{14} \cdot N^2 \cdot E^2 (GeV) \cdot I(A) \cdot F_n(K)$$

flux inside the central cone (ph / s / mrad\*\*2/ 0.1%BW)

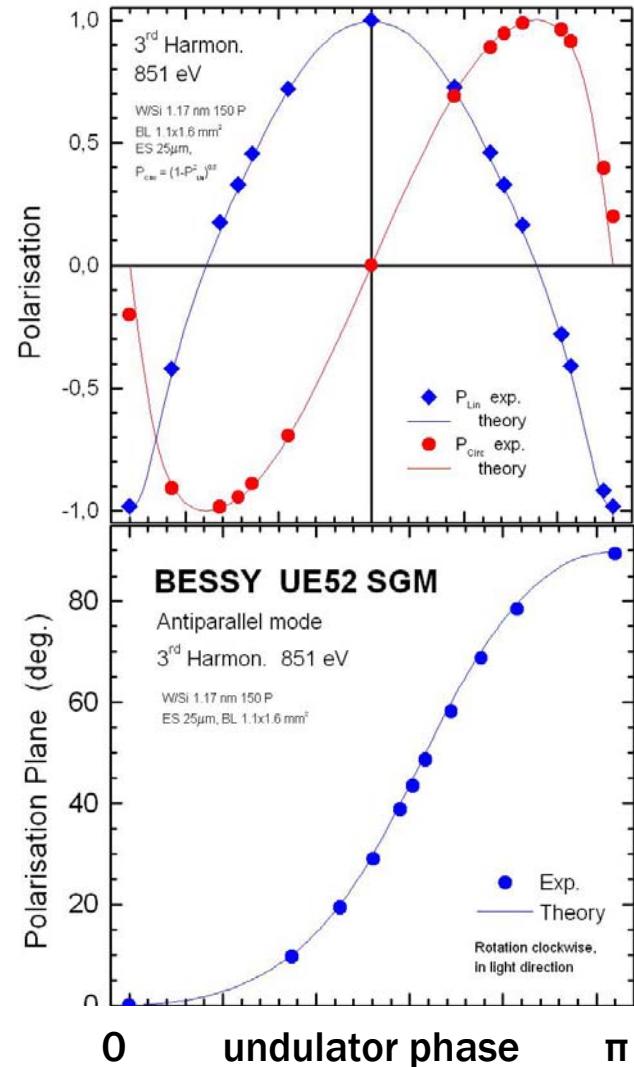
$$\frac{\partial \tilde{F}}{\partial(\Delta\omega/\omega)} = 1.431 \cdot 10^{14} \cdot N \cdot I(A) \cdot Q_n(K)$$

$$Q_n(K) = (1 + K^2 / 2) \cdot F_n / n$$





elliptical mode



The BESSY II Soft X-ray polarimeter

We observe excellent agreement between simulations and measurement

# Difference between Wigglers and Undulators

Undulator parameter  $K = 93.4 \cdot \lambda_0(m) \cdot B_0(T)$

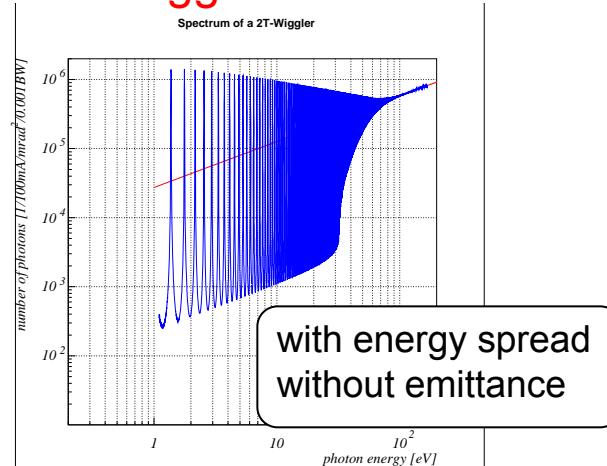
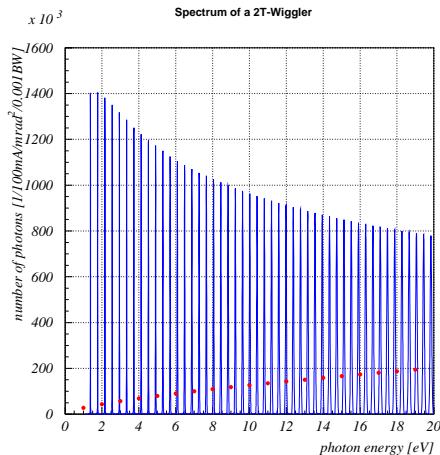
horizontal divergence:  $K / \gamma$

vertical divergence:  $1 / \gamma$

ratio:

wiggler:  $K \gg 1$

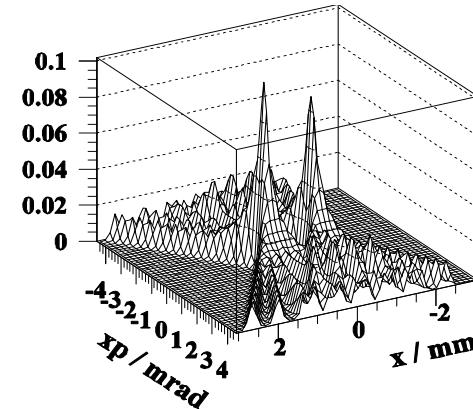
there is, however, no principle difference  
between undulators and wigglers



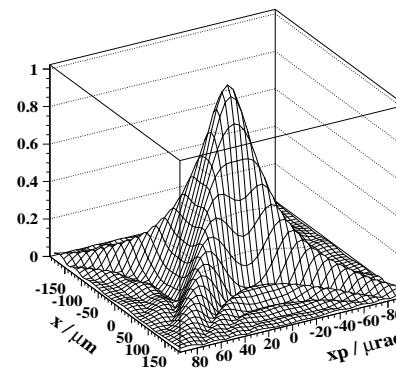
wiggler spectrum  
corresponding dipole spectrum

radiation phase space  
is more compact  
for small K-values

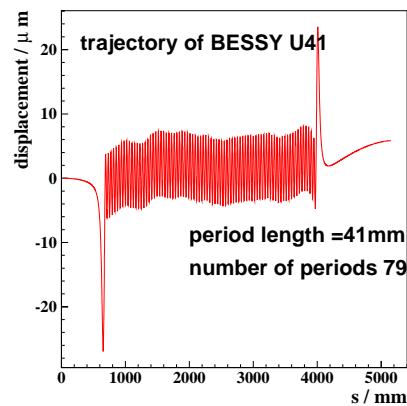
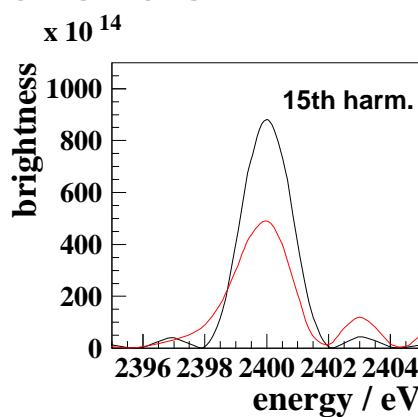
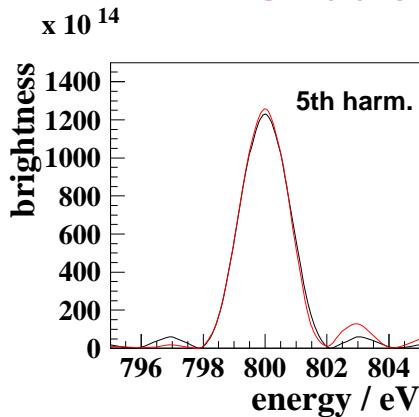
7 Tesla Wiggler



Undulator



## Undulator errors



Phase error U41:  
 $\Delta\Phi$  (rms) = 2.6°

reduction of on axis  
 flux density (Walker):

$$R = \exp(-\sigma_\Phi^2 n^2)$$

$$\Delta\Phi = \frac{2\pi}{\beta\lambda(B\rho)^2} \cdot \int_0^z \left[ \int_0^{z'} B_y^{fit} dz'' \cdot \int_0^{z'} B_y^{res} dz'' \right] \cdot dz' +$$

phase error from  
 measured fields:

$$0.5 \cdot \frac{2\pi}{\beta\lambda(B\rho)^2} \cdot \int_0^z \left[ \int_0^{z'} B_y^{res} dz'' \cdot \int_0^{z'} B_y^{res} dz'' \right] \cdot dz'$$

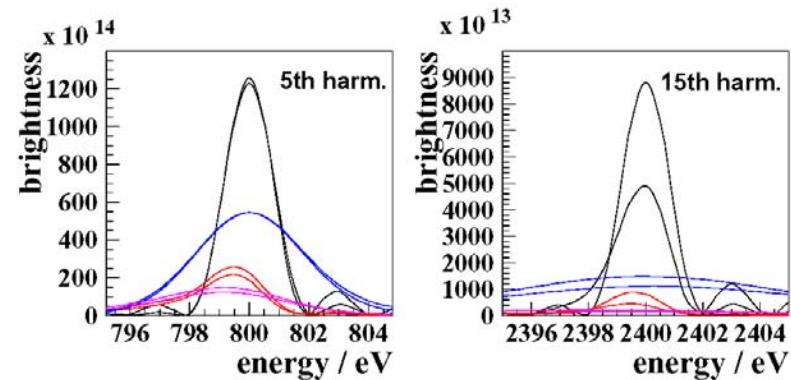
## Beam parameters of a typical 3rd generation light source

beam emittance:  $6 \times 10^{-9}\pi$  m rad

$$\beta_x = 0.94 \text{ m}$$

$$\beta_y = 2.1 \text{ m}$$

energy spread:  $8 \times 10^{-4}$



black: without emittance, energy spread

red: emittance included

blue: energy spread included

magenta: emittance and energy spread incl.

## Field optimization of undulators has two aspects:

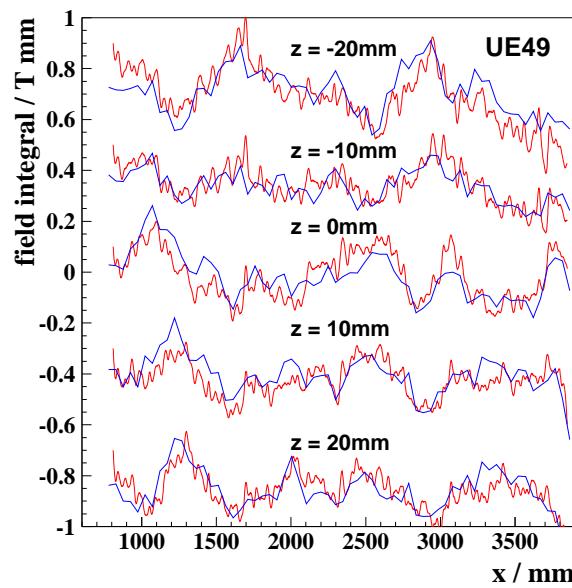
- 1) *optimization of spectral performance*  
today, spectral performance of undulators is limited  
by beam emittance and energy spread
- 2) *minimization of the interaction with the storage ring*  
minimize static and dynamic multipoles

## Methods:

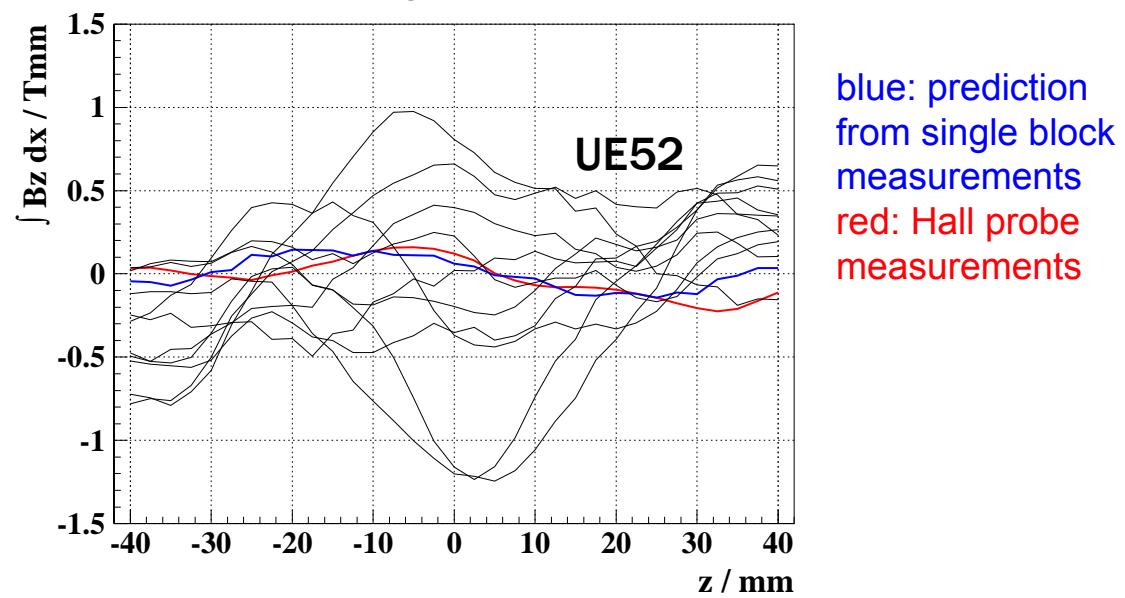
- 1) *Magnet characterization and sorting before assembly*
- 2) *Minimization of optical phase error of magnet assembly*
- 3) *Compensation of static multipoles of magnet assembly*
  - Fe- shims
  - permanent magnet shims (increases minimum gap)
  - air coils at either end of the device (final compensation in SR)
- 4) *Compensation of dynamic multipoles of magnet assembly*
  - Fe-L-shims (suitable for APPLE in linear / elliptical mode)
  - flat wires glued onto the chamber (full flexibility for APPLE operation)

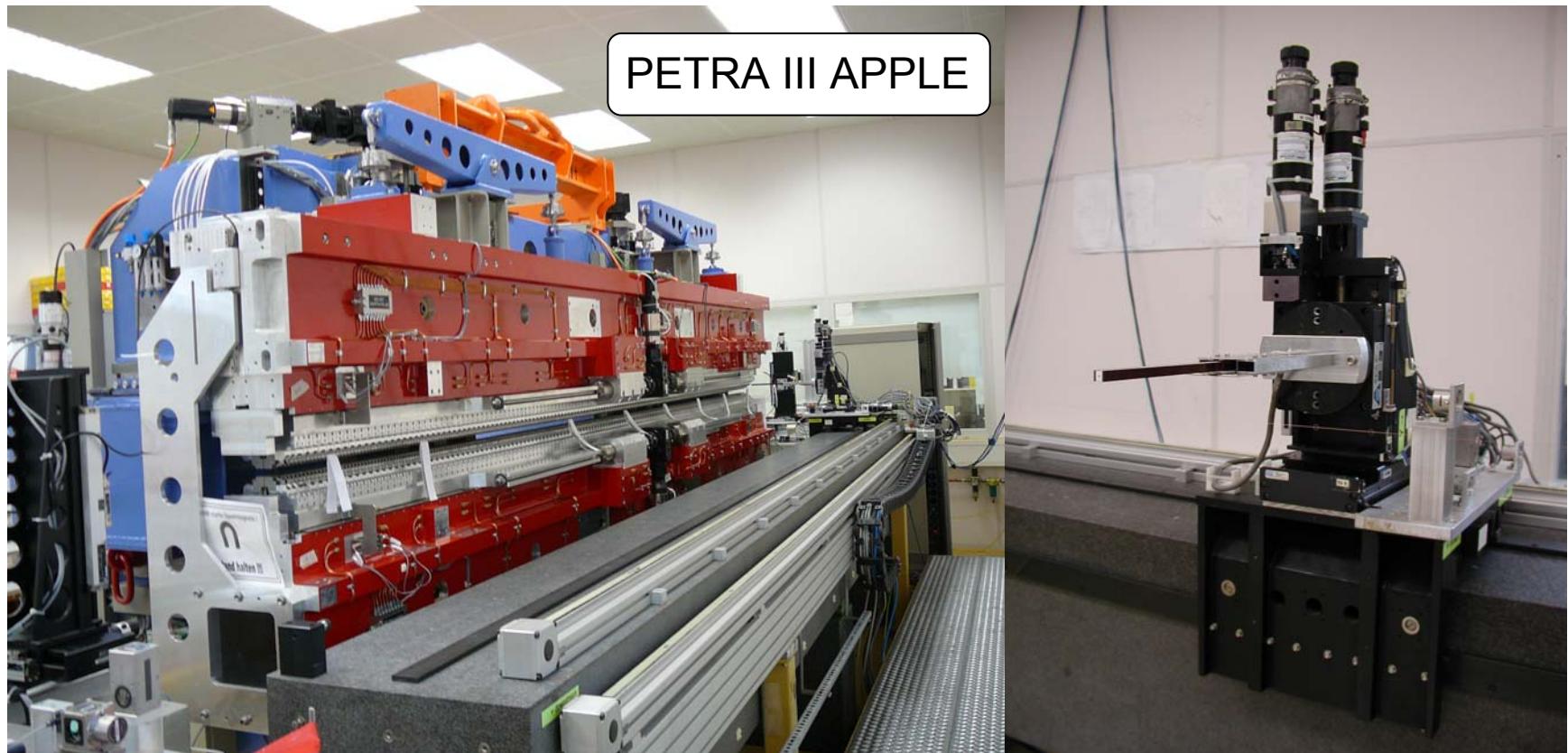
Magnet characterization and sorting minimizes shimming work after assembly  
 excellent agreement between predicted and measured fields integrals  
 for BESSY undulators UE52, UE49, UE112

longitudinal distribution  
 of field integrals



transverse distribution  
 of field integrals



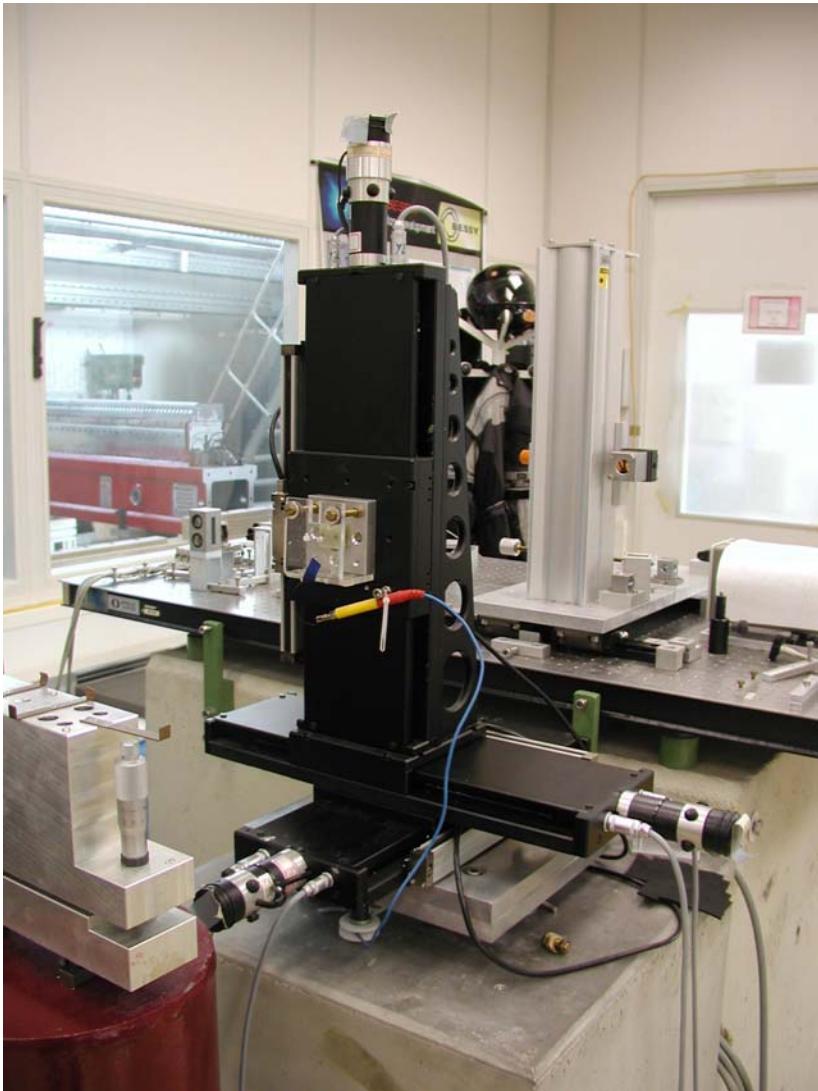


**Granite bench:** travel: 5.5 m x 100mm x 100mm

rms repeatability of SENTRON Hall probes: 0.025 Tmm / 75 Tmm<sup>2</sup>

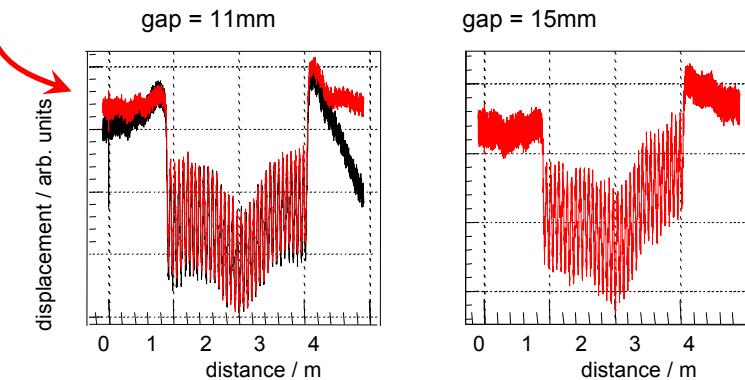
(single measurement, 4min per scan)

alternative sensors: search coil, lambda coil, fluxgate sensor (small fields)



**Moving wire system:**  
single wire, CuB  $\varnothing$  125  $\mu\text{m}$   
length: 6.5m  
travel: 200mm x 200mm  
rms repeatability: 0.003 Tmm  
(single scan)

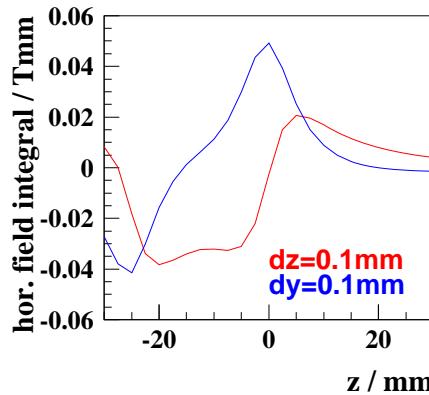
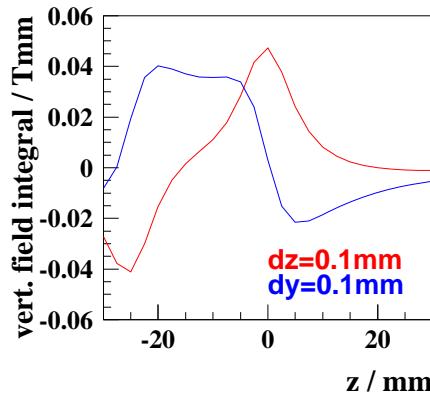
The system can be used also in  
a **pulsed wire** mode to detect  
the local distribution of  
first and second field integrals



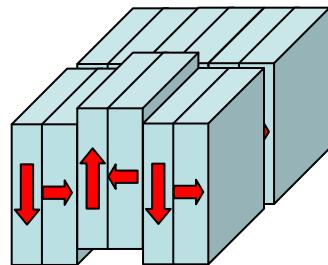
Correction coils not powered  
**Correction coils powered**

## trajectory straightening and phase shimming

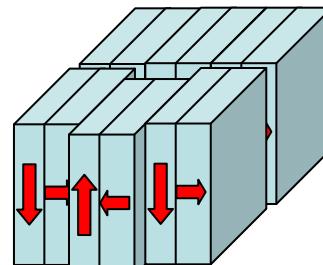
method: virtual shimming (VS): horizontal and vertical block movement  
 VS introduces additional phase dependent field integrals



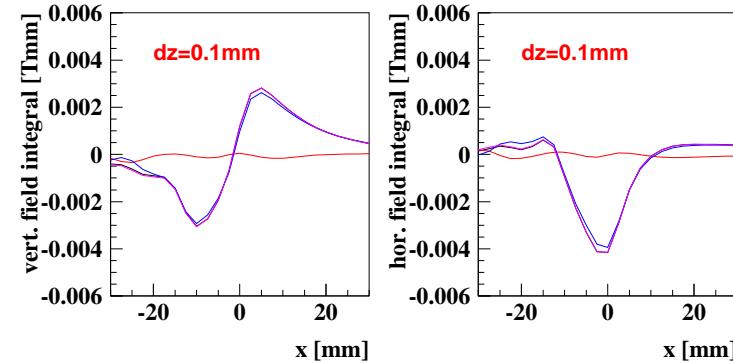
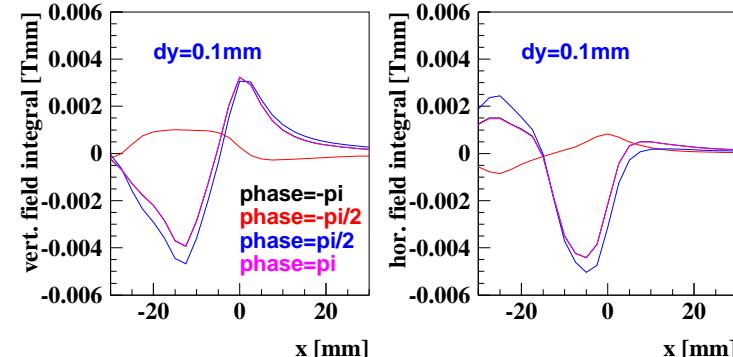
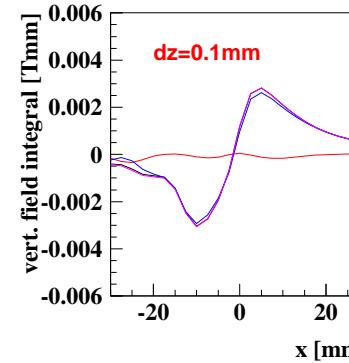
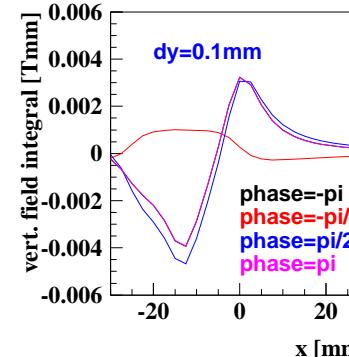
Field integrals as produced by virtual shimming



vertical movement ( $dy$ )



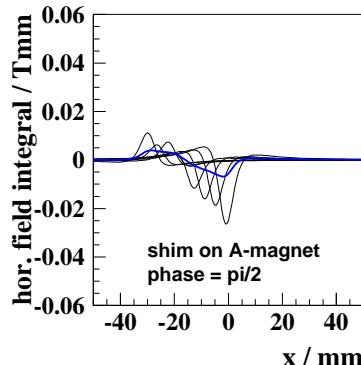
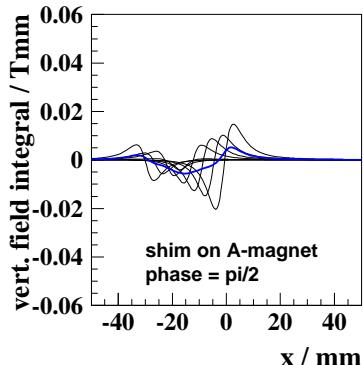
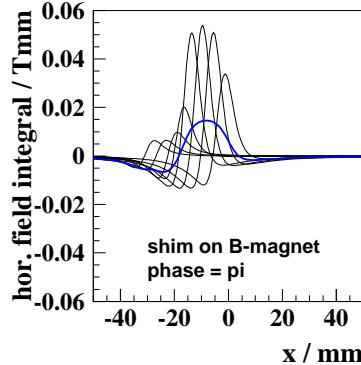
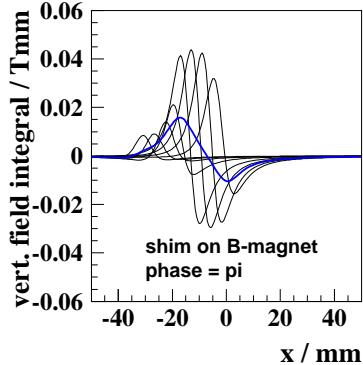
horizontal movement ( $dz$ )



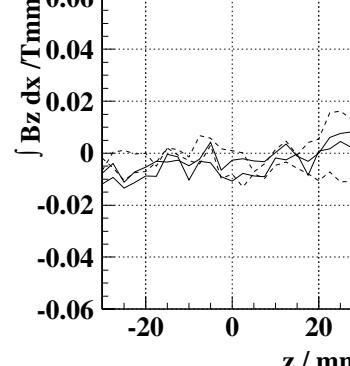
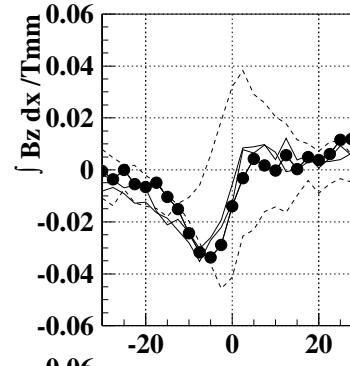
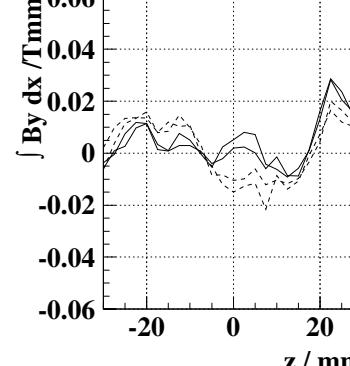
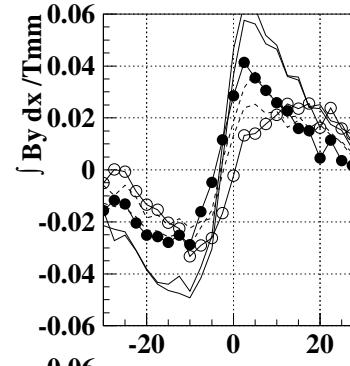
Phase dependent field integrals  
 as produced by virtual shimming

## shimming of phase dependent field integrals

method: Fe-shims with phase dependent response



shim response of Fe-shims  
on APPLE undulator magnets



field integrals before (top)  
and after (bottom) shimming

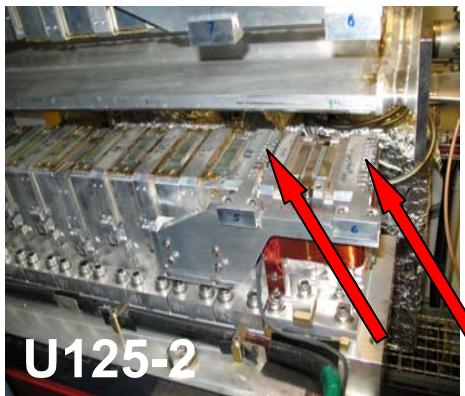
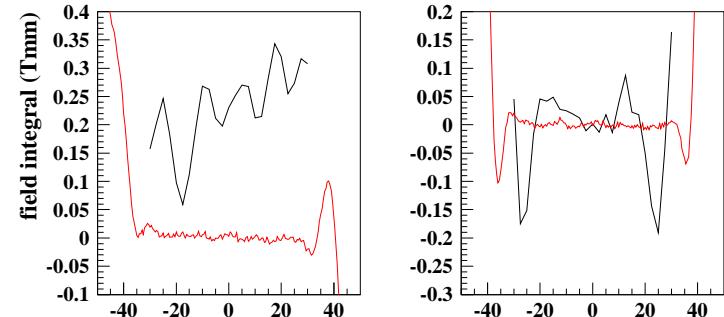
*J. Bahrdt et al, Nucl. Instr. and Meth,  
in Phys. Res. A 516 (2004) 575-585*

phases:  
dashed:  
 $\pm\lambda/4$   
solid:  
 $\pm\lambda/2$

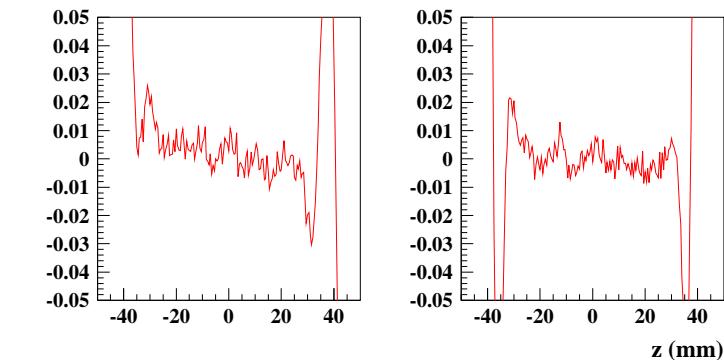
## shimming of shift independent field integrals with permanent magnets



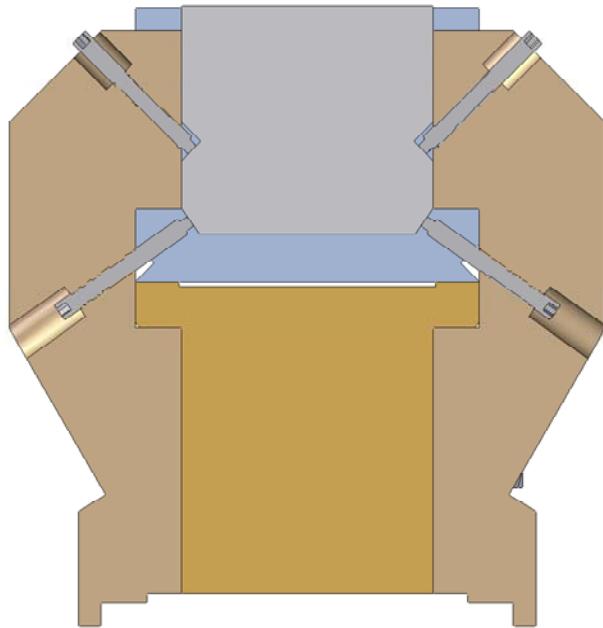
BESSY  
standard  
magic finger



arrays of permanent magnets  
at either end of the device  
magnet dimensions:  
 $4 \times 4 \text{ mm}^2$ , variable thickness,  
grid size 4mm



BESSY II U125-2  
black: without MF  
red: with MF



Shimming of vertical field errors:

→ vertical pole movement

Shimming of horizontal field errors:

→ pole tilt

Adjustment Range:

Pole Height :  $\pm 0.3\text{mm}$

Pole Tilt :  $\pm 1\text{mrad}$

*J. Pflüger, H. Lu, T. Teichmann NIM A429 (1999), 368*

*Courtesy of J. Pflüger, XFEL*

Successfully applied to FLASH and PETRA III undulators

## Classification of permanent magnet undulators

### *Spacing of undulator spectral harmonics*

- equally spaced: periodic undulator
- non equally spaced: quasiperiodic undulator

### *On axis radiation power*

- high power on axis: planar undulator  
reduced power on axis: helical, figure 8 undulator

### *Polarization*

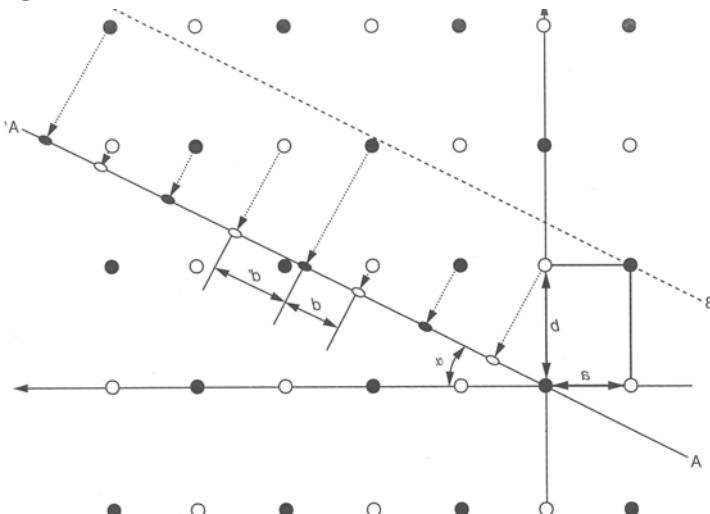
#### fixed polarization

- planar device for linear polarization
- helical device for circular polarization

#### variable polarization

- hor. and vert. lin. and elliptical
- additionally variable angle of linear polarization
- arbitrary polarization

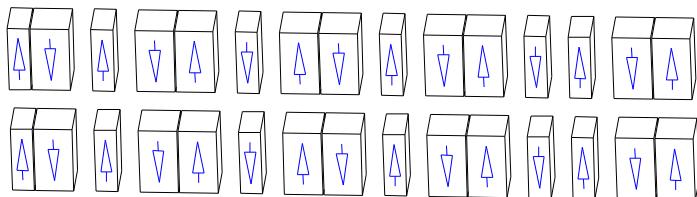
generate 1D-quasiperiodic lattice



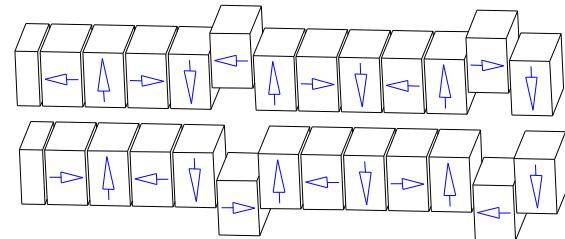
$$z_m = \frac{d}{r \cdot \tan(\alpha)} \cdot (m + (r \cdot \tan(\alpha) - 1) \left\lfloor \frac{\tan(\alpha)}{r + \tan(\alpha)} m + 1 \right\rfloor)$$

$$r = b/a$$

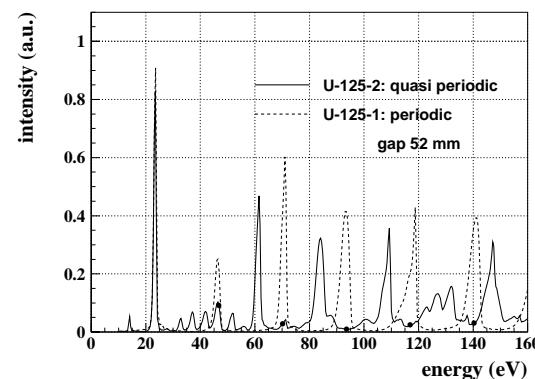
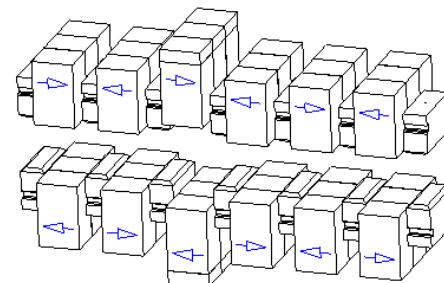
original design



ESRF / ELETTRA design



BESSY II design



spectra derived  
from measured  
magn. fields

# Reduced On-axis Flux Density Designs

$$\frac{\partial P}{\partial \Omega} (W / mrad^2) = 0.01344 \cdot E(GeV)^2 \cdot I(A) \cdot N \cdot$$

$$\int_{-\lambda_0/2}^{\lambda_0/2} \left[ \frac{v_x'^2 + v_y'^2}{D^3} - \frac{((v_x^2)' + (v_y^2)')^2}{D^5} \right] \cdot ds$$

$$D = 1 + v_x^2 + v_y^2$$

$$v_{x/y} = \gamma(\beta_{x/y} - \theta_{x/y})$$

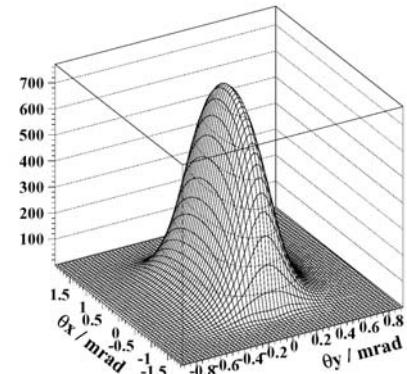
example: angular flux density for:

energy=1.7GeV, current=0.1A,

N=100,  $\lambda = 50\text{mm}$

Kx/Ky=0, 0.25, 0.5, 0.75, 1.0

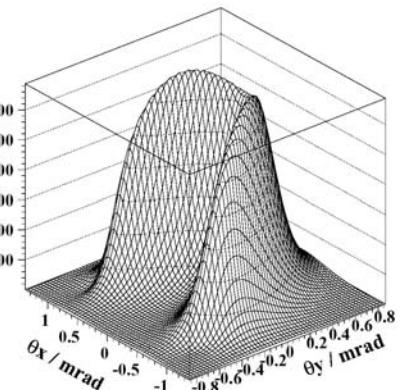
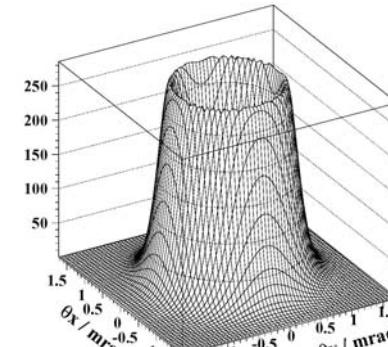
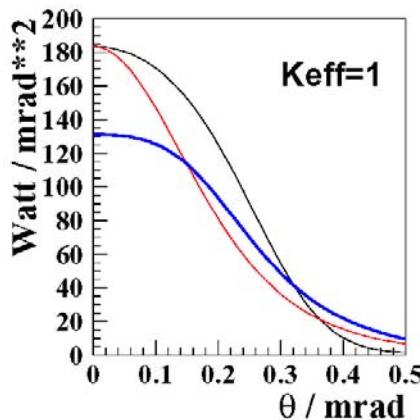
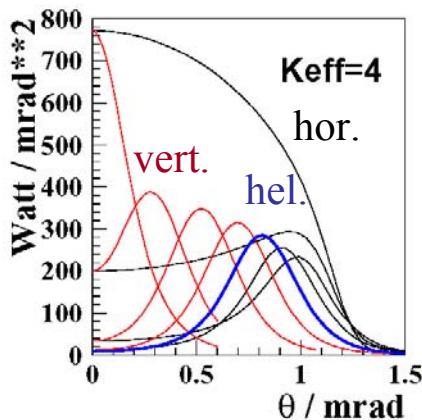
High on axis power density  
planar device, K=4

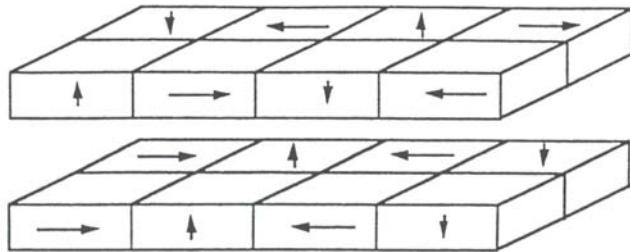


low on axis power density

helical device, Keff=4

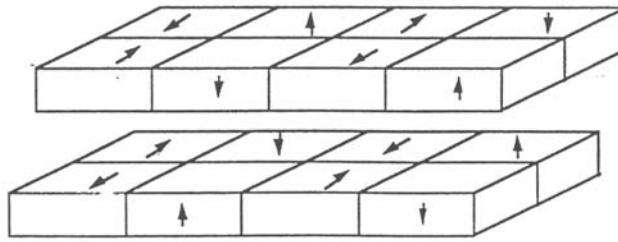
figure-8 undulator





## ESRF

- (+) variable polarization
  - upper beam: vert. field
  - lower beam: hor. Field
- (-) vertical steering
- (-) medium fields

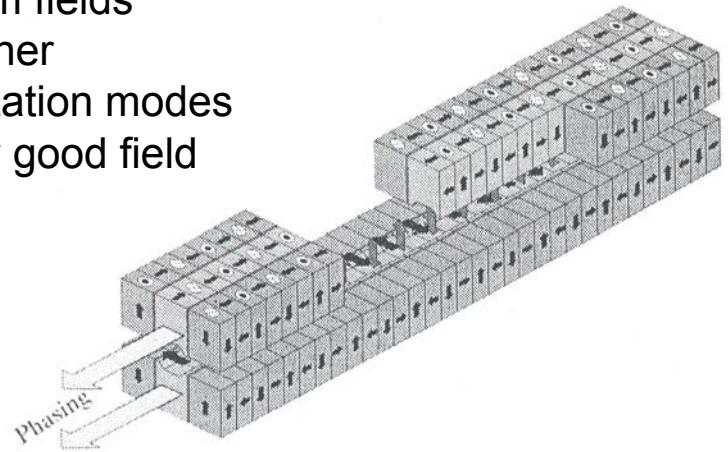


## ELETTRA

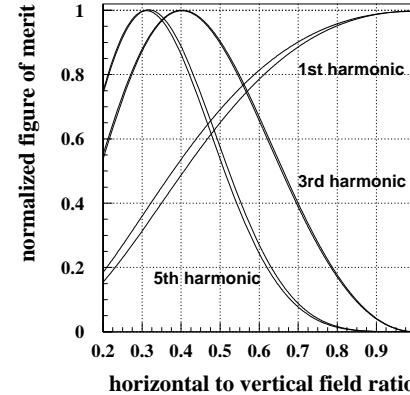
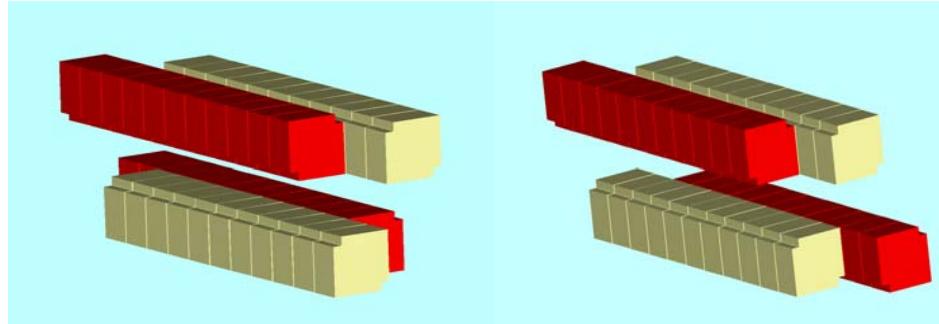
- (+) helical, independent on gap setting
- (-) medium fields
- (-) no further polarization modes
- (-) narrow good field region

## SPRING-8

- (+) variable polarization
- (+) larger good field region
- (-) week fields
- (-) mechanically complicated

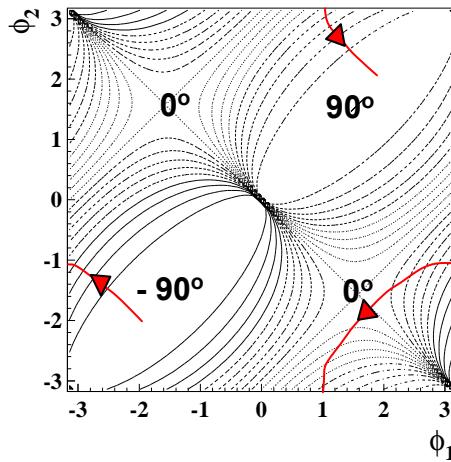


## APPLE II, Advanced Polarizing Photon Light Emitter

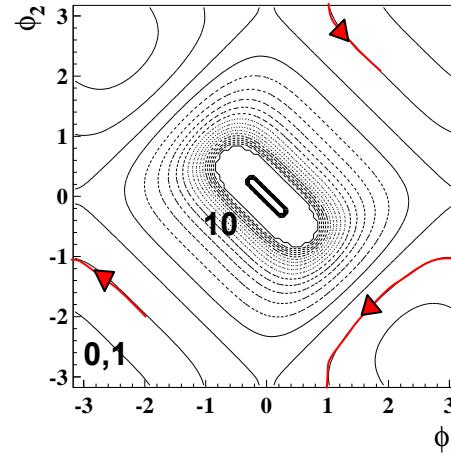


- (+) highest fields
- (+) full flexibility  
e.g. APU
- (-) mechanically complicated
- (-) narrow good field region

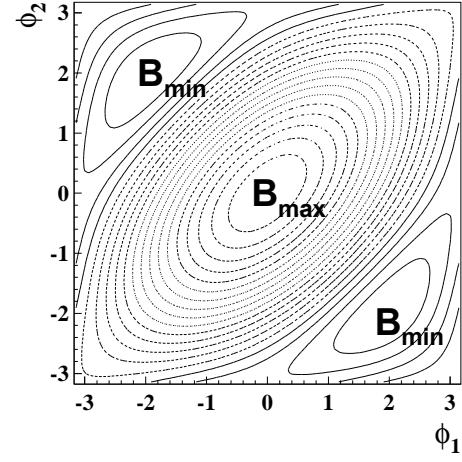
relative phase of  $B_y, B_z$   
defines ellipticity



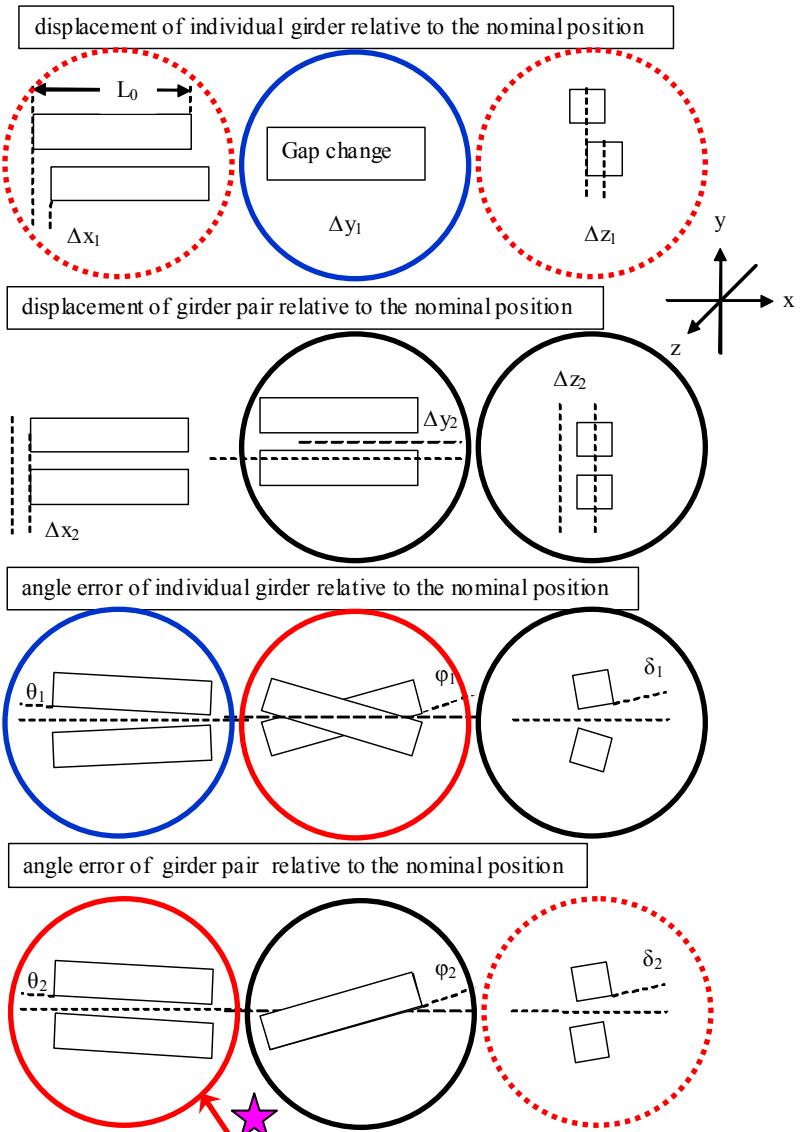
ratio  $B_y / B_z$   
defines inclination



effective field



# Geometric Tolerances



black:

independent on forces  
**accuracy and stiffness of  
of support structure**

blue:

**closed loop servo systems**

red, dotted:

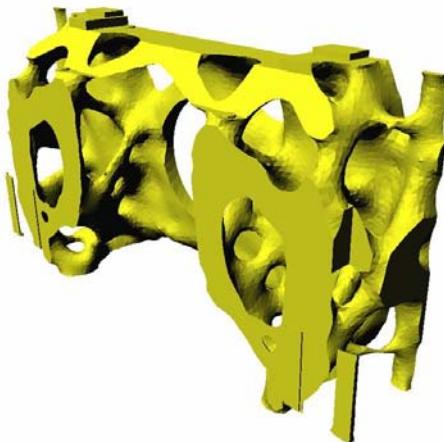
dependent on forces  
appears in inclined mode  
produces K-shift  
**stiff support structure**

red, solid:

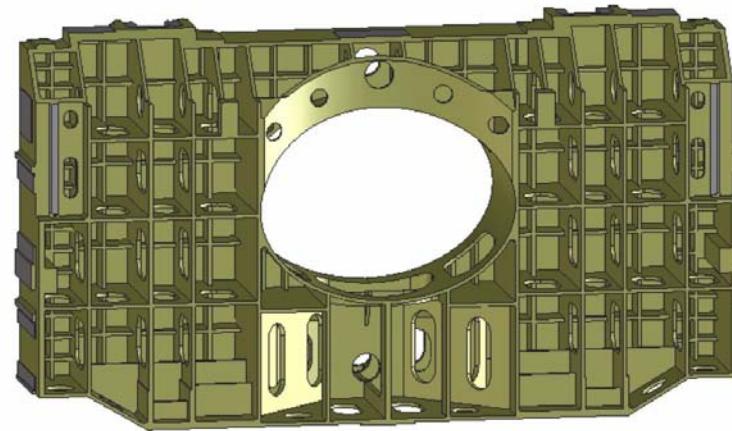
dependent on forces  
appears in inclined mode  
produces  $\nabla$ K/K-shift  
**feed back compensation  
using 4 motors**



# Stiff Design: Cast Iron Support Structure



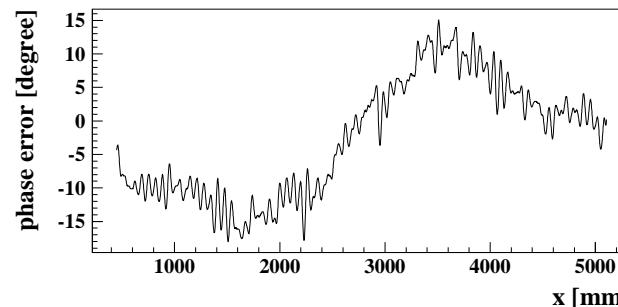
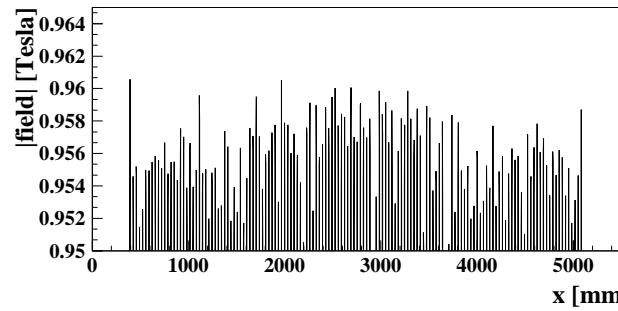
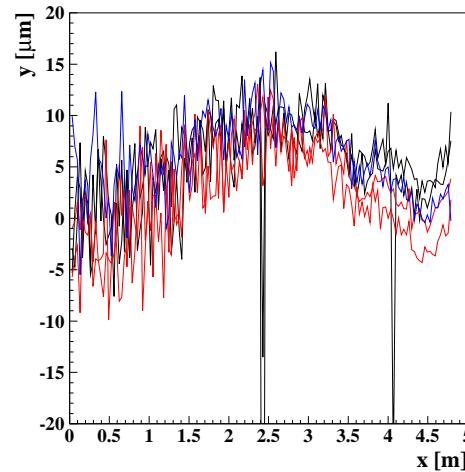
bionic  
optimization



## Magnet girder



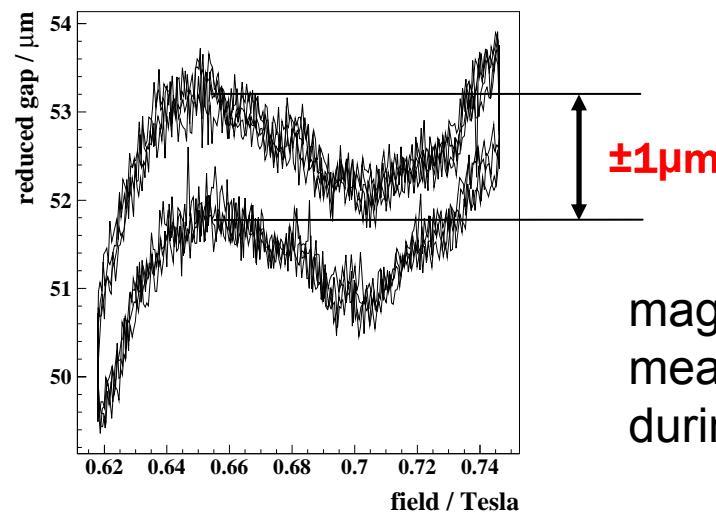
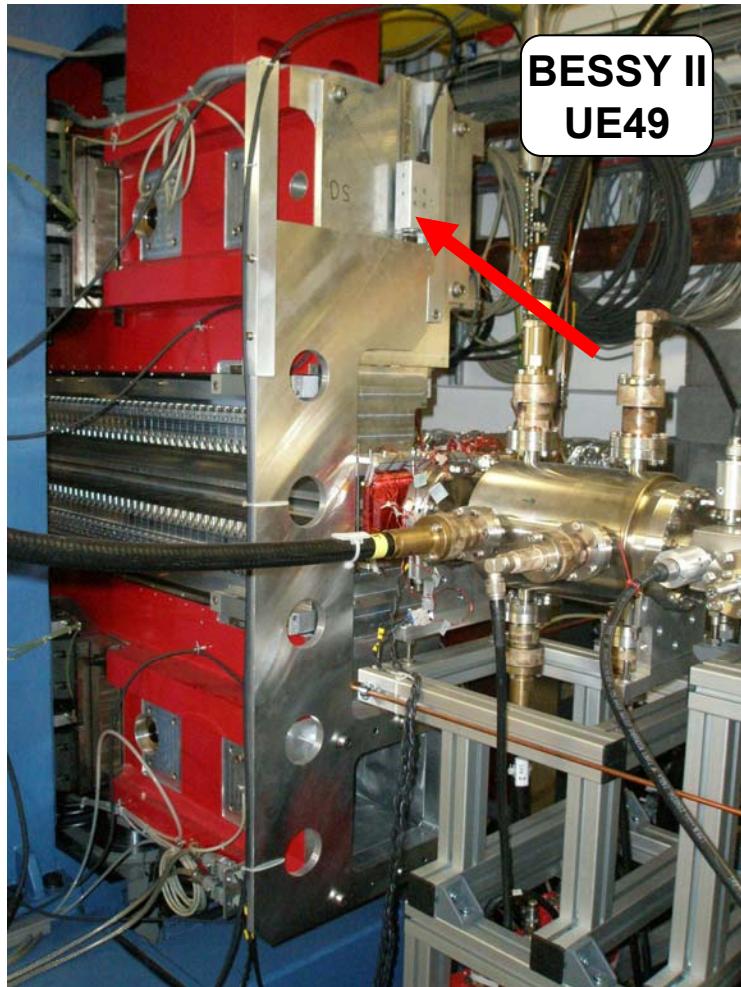
material: cast Aluminum  
length: 5m  
single piece of Al



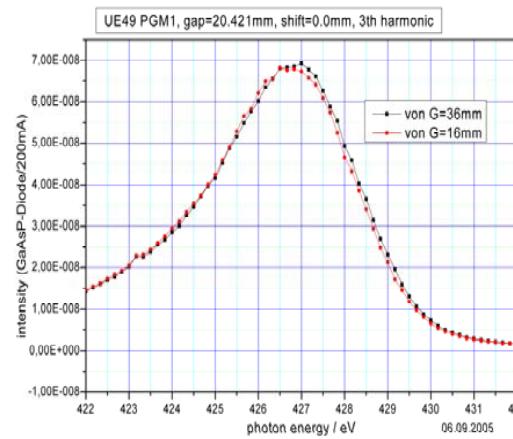
Laser interferometer  
measurements at HZB:  
**Straightness:**  
**10 μm over 5m**

phase error  
for phase =  $\pi$   
is dominated by  
geometric error  
of girder  
→  
simple  
compensation  
with spacers

# Gap Positioning Accuracy

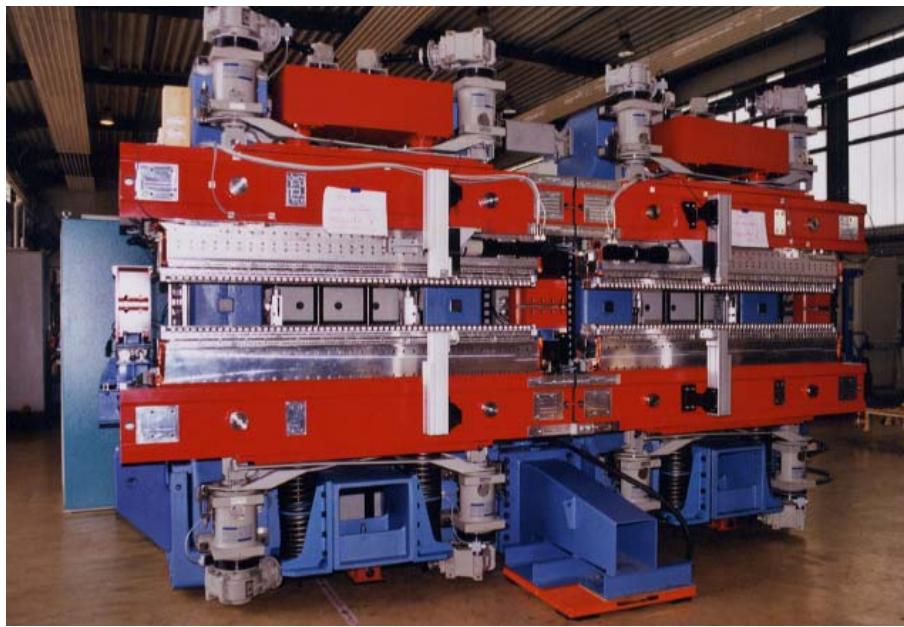


magnetic field  
measurement  
during gap drive



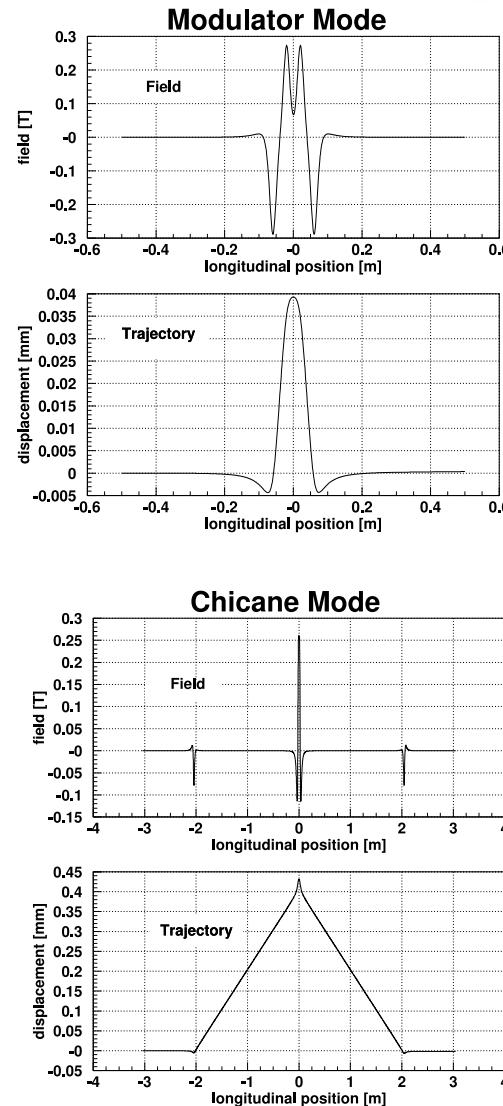
measured spectra  
for different  
directions of  
gap drive

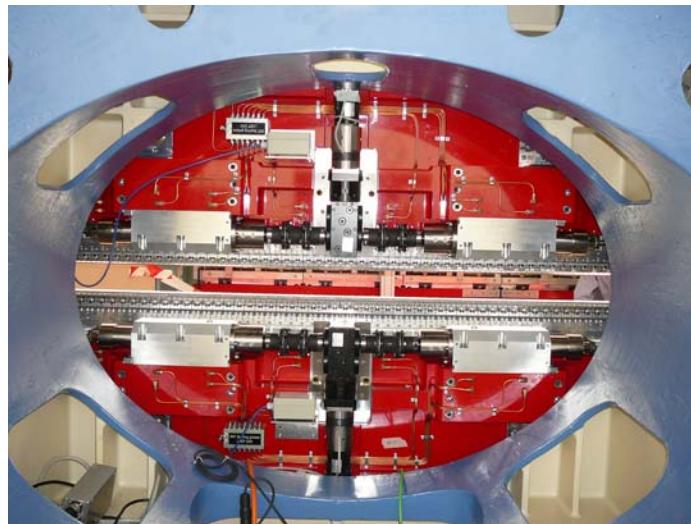
# BESSY II Double Undulator for Fast Helicity Switching



BESSY II UE56  
double undulator (top)  
and permanent  
magnet modulator /  
chicane (left)

*J. Bahrdt et al., SRI2000*

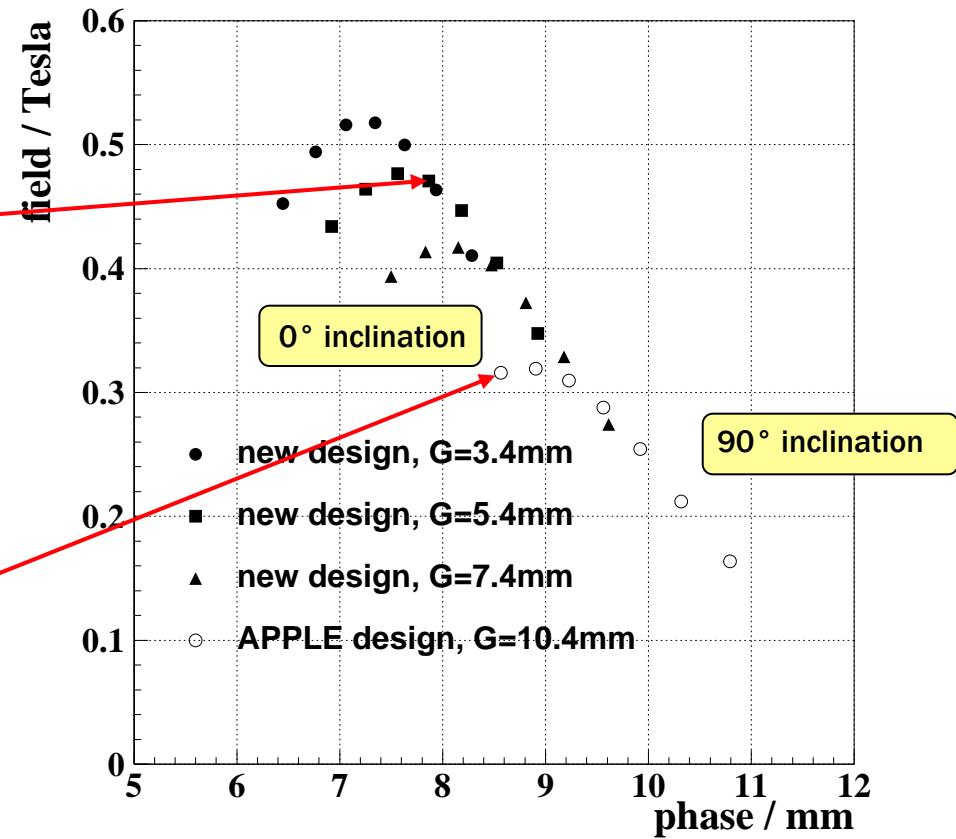
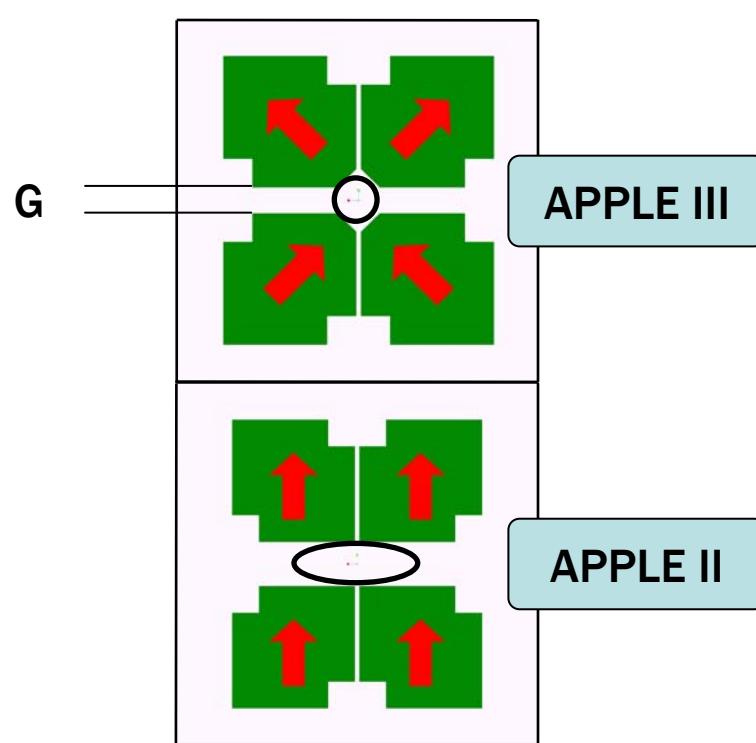




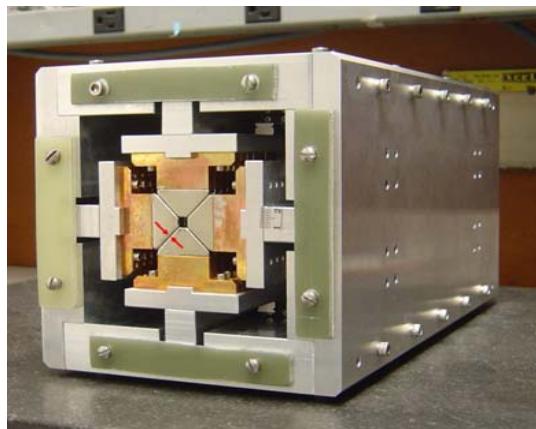
total length: 5m  
weight: 18t  
# of magnets: 1200  
maximum force: 70 kN

- full polarization control via four phase motors
- independent drive systems for lower girder and gap motion

## APPLE III design: factor 1.4 higher field as compared to APPLE II

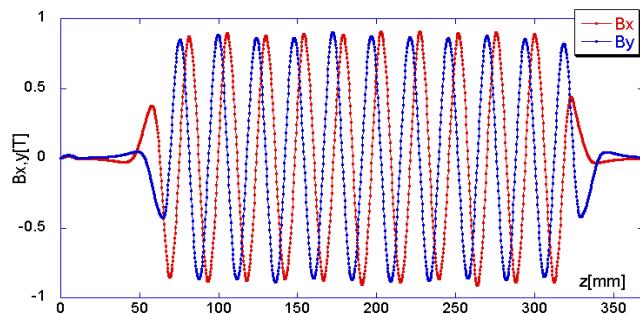


J. Bahrdt et al., Proceedings of the 26th International FEL Conference, Trieste, Italy, 2004, pp610-613

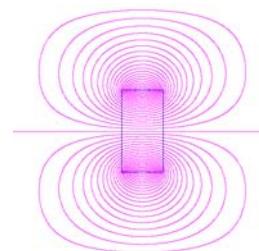


length: 300mm  
inner diameter: 5mm  
slit between arrays: 0.5mm

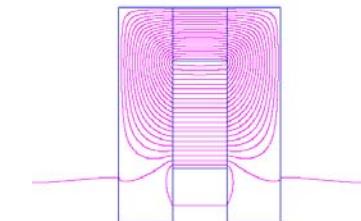
A. Temnykh, PRST-AB,  
11, 120702 (2008)



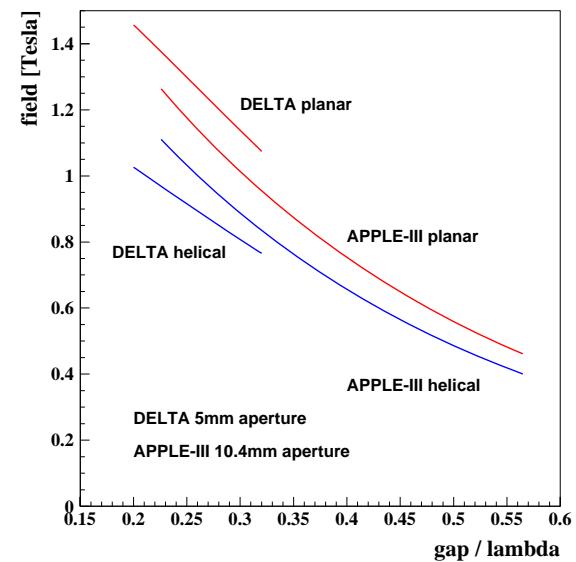
Measured fields of Delta undulator



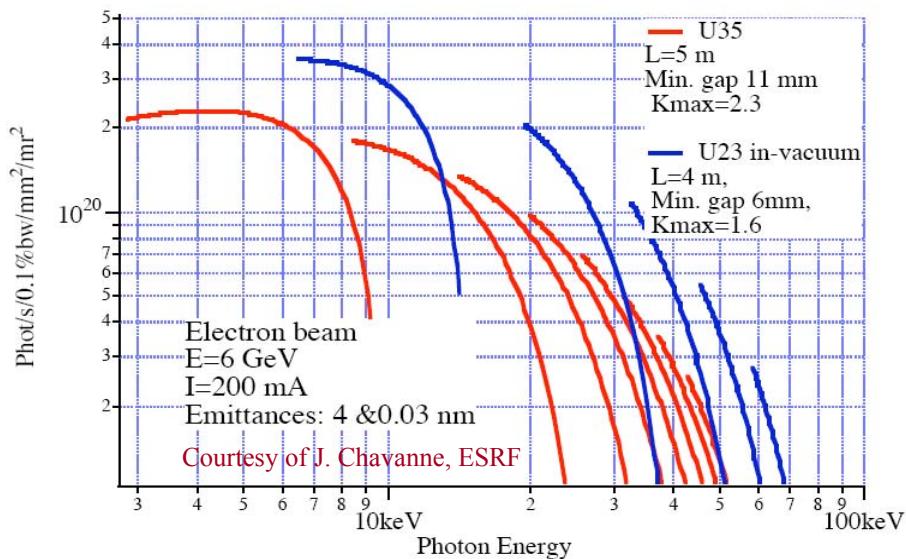
Single NdFeB (40SH) PM block,  
 $T_{demag} \sim 132\text{degC}$



PM block in steel jacket  
 $T_{demag} \sim 228\text{degC} !$

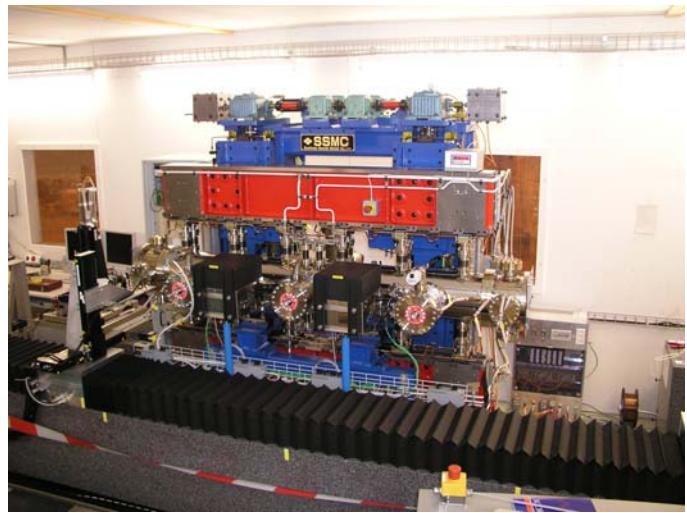
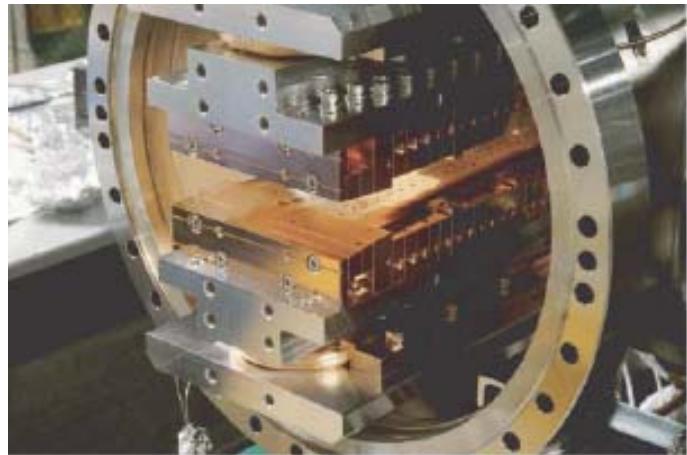


Comparison of  
DELTA and APPLE III ID



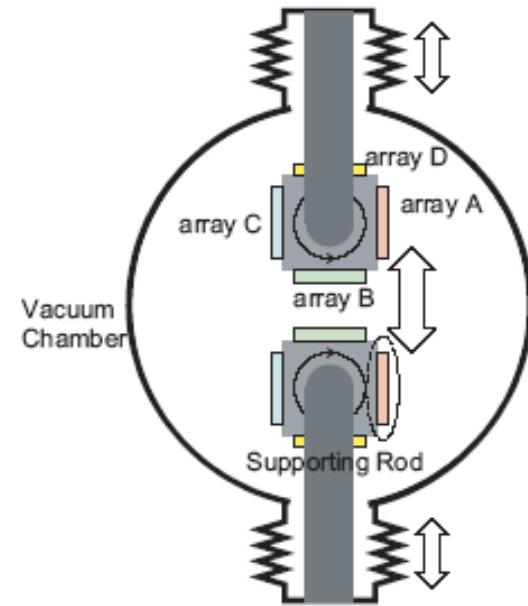
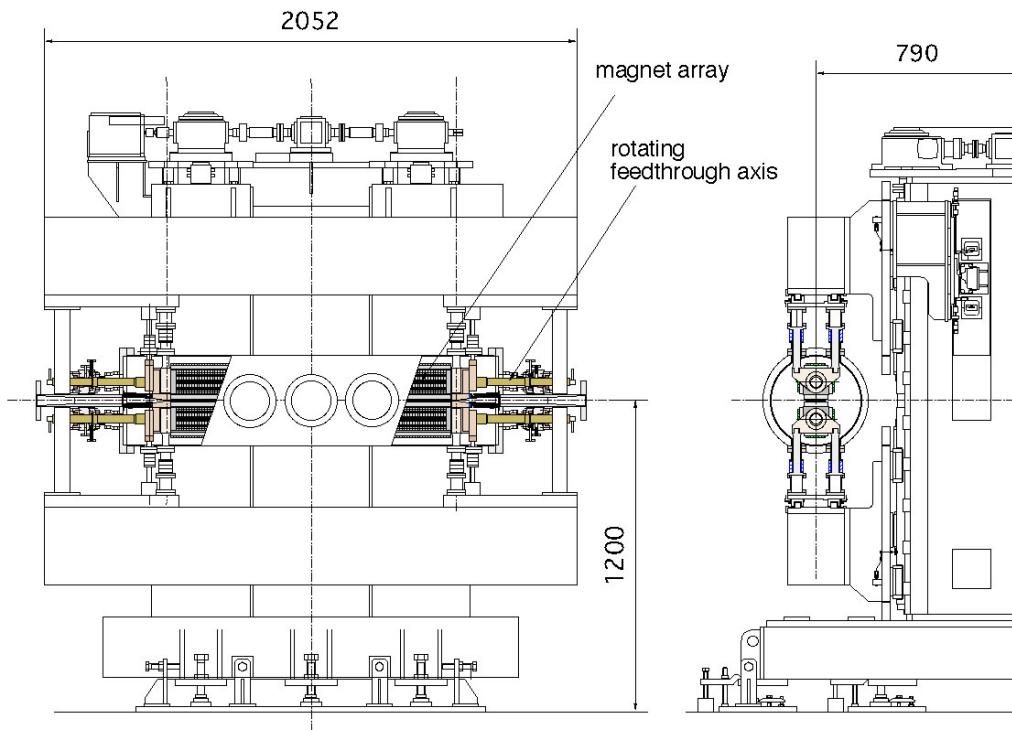
Mechanically complicated  
but mature technique

- coating of magnets to reduce outgassing  
Ti+TiN ion plating of NdFeB magnets (SPRING8)
- high coercive magnetic material (bakeout at 125°)
- thin metal sheet to reduce image current heating  
(50  $\mu$ m Ni + 10  $\mu$ m Cu)
- water cooled RF-fingers
- special shimming techniques



SLS U19 In-Vacuum Undulator  
Courtesy of Th. Schmidt, SLS

## SPRING 8



Covering a wide photon energy range with several devices  
which have slightly different period lengths: overlap of 1st & 3rd harm.

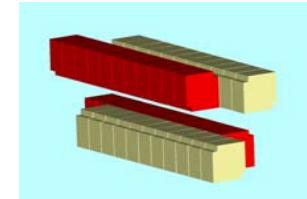
*T. Bizen et al., AIP Conf. Proc. of SRI conference, Vol. 705 (2004) pp175-178.*

# Undulator Operation: Dynamic Multipoles (DM)

second order kicks (*Elleaume, EPAC 1992*):

$$\theta_{x/y} = -\frac{1}{(B\rho)^2} \int \left\{ \int B_x dz' \cdot \int \frac{\partial B_x}{\partial x/y} dz' + \int B_y dz' \cdot \int \frac{\partial B_y}{\partial x/y} dz' \right\} dz$$

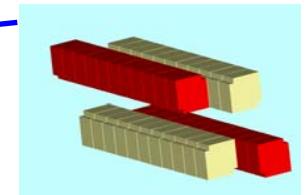
$$\theta_{x/y} = -\frac{L}{2(B\rho)^2} \frac{\lambda_u^2}{(2\pi)^2} \left\{ B_x^0 \cdot \frac{\partial B_x^0}{\partial x/y} + B_y^0 \cdot \frac{\partial B_y^0}{\partial x/y} \right\}$$

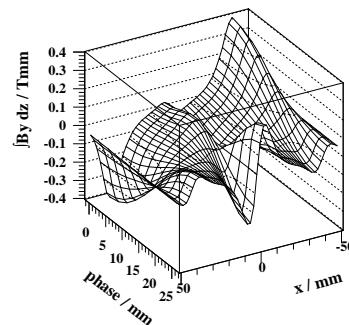
APPLE,  
elliptical mode

generic representation of second order kicks:

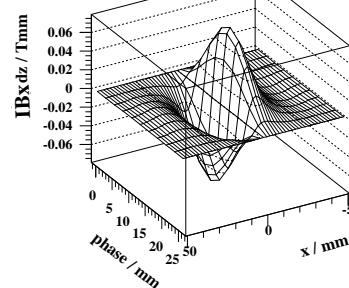
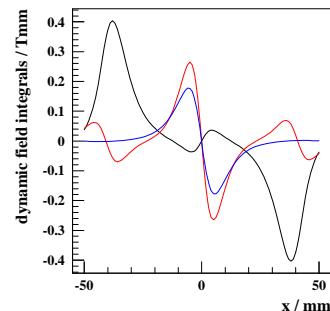
$$\theta_x(x) = f_0(x) \cos^2(\varphi/2) + f_\pi(x) \sin^2(\varphi/2) + f_{\pi/2}(x) \sin^2(\varphi)$$



APPLE  
inclined mode

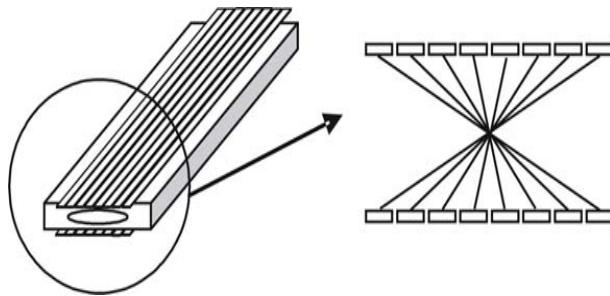
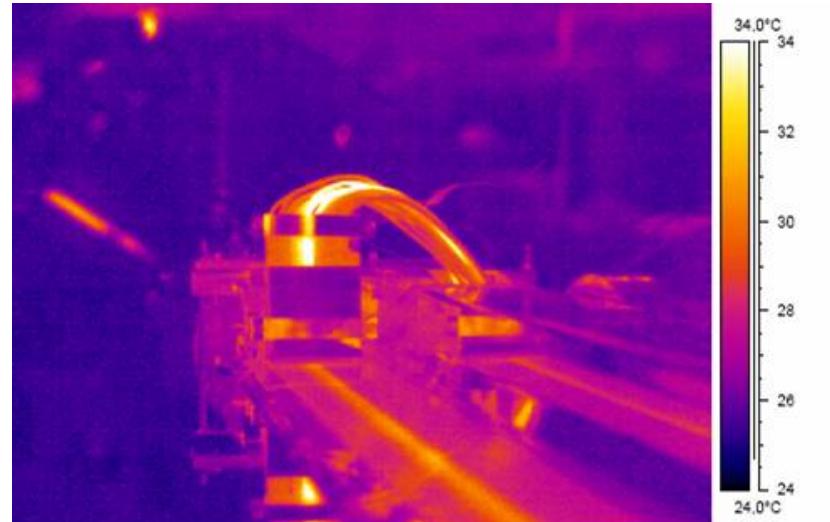
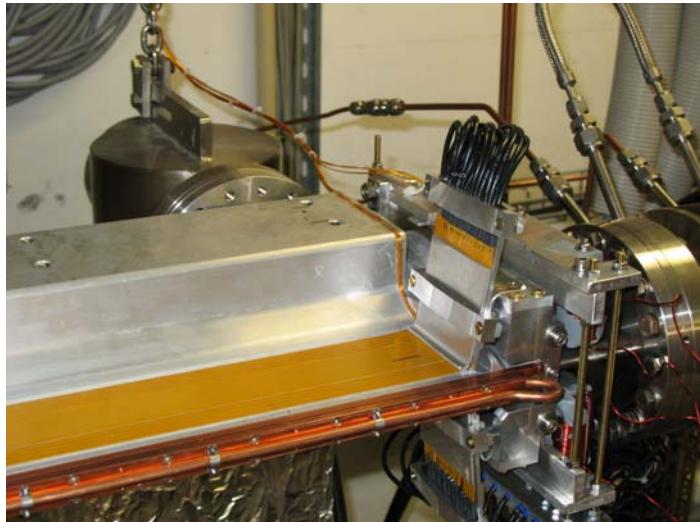


inclined mode

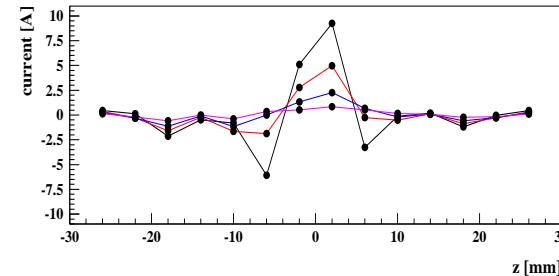


inclined mode

*J. Bahrdt et al., SRI 2007*

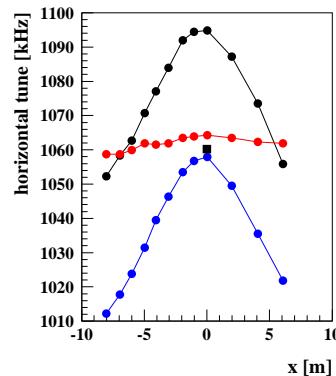


2 x 14 wires, 14 power supplies  
 maximum currents: 16A  
 wire diameter: 3 x 0.3mm<sup>\*\*2</sup>  
 wire separation: 4mm

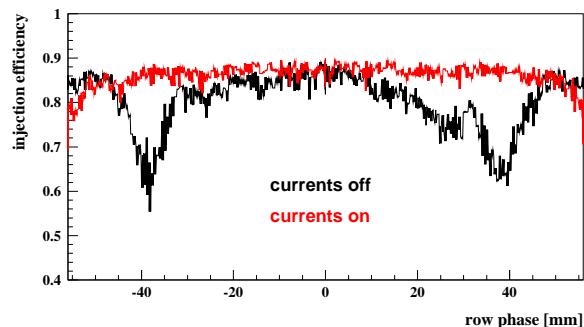


Current settings for gaps of 20mm  
 24mm, 30mm and 40mm

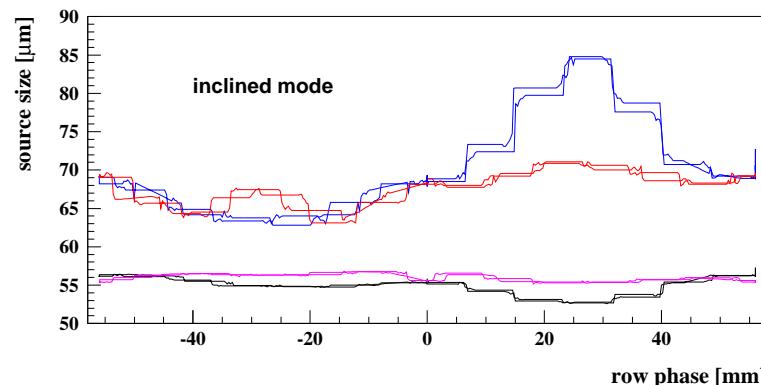
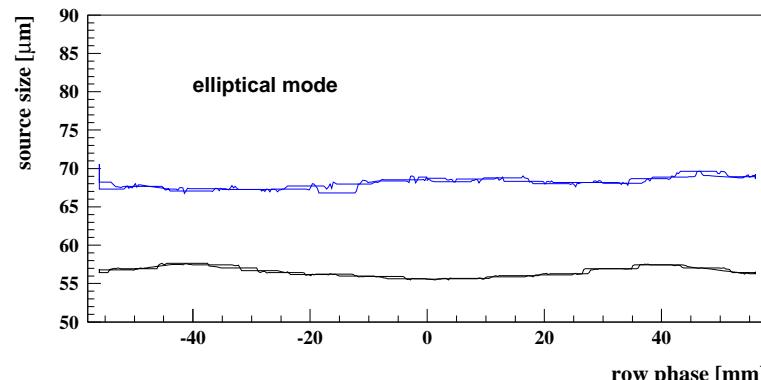
*J. Bahrdt et al., EPAC 2008*



Horizontal and vertical tunes  
 vs horizontal displacement  
 black: without compensation  
 blue: quadrupole compensation  
 red: compensation with flat wires



Injection efficiency with UE112  
 black: without compensation  
 red: with compensation



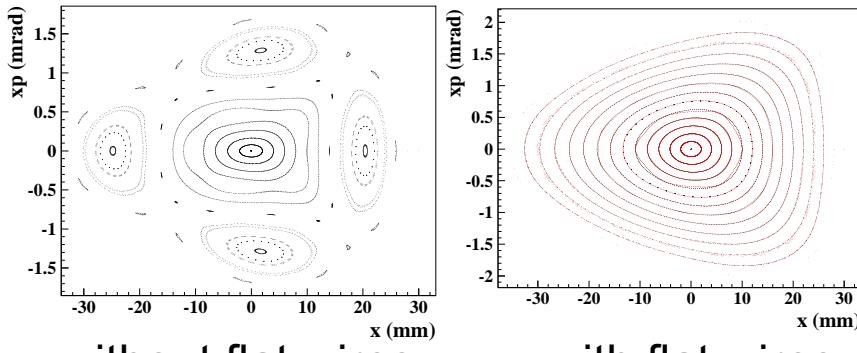
Source size variation with row phase of the UE112  
 at gap = 24mm in the elliptical mode (top) and the  
 inclined mode (bottom). Black, blue: currents  
 switched off; red, magenta: currents switched on.

Undulator fields can not be represented with 2D-multipoles due to limited radius of convergence

## Procedure

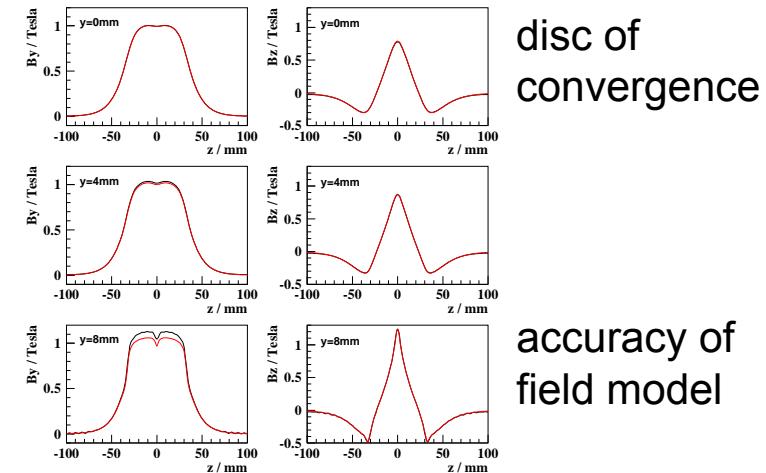
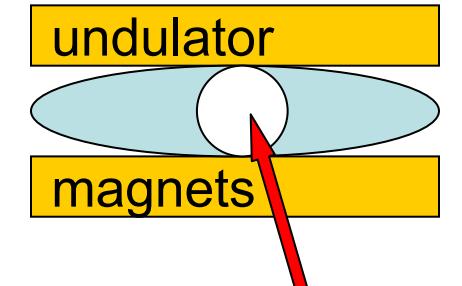
- evaluation of transverse field distribution of one magnet row
- Fourier decomposition of these distributions
- analytical Ansatz for complete undulator structure
- similar procedure for field integrals of Fe-shims
- generate analytic expresison for scalar potentials of main field and shim field integrals
- use this scalar potential in generating function algorithm

## Horizontal phase space



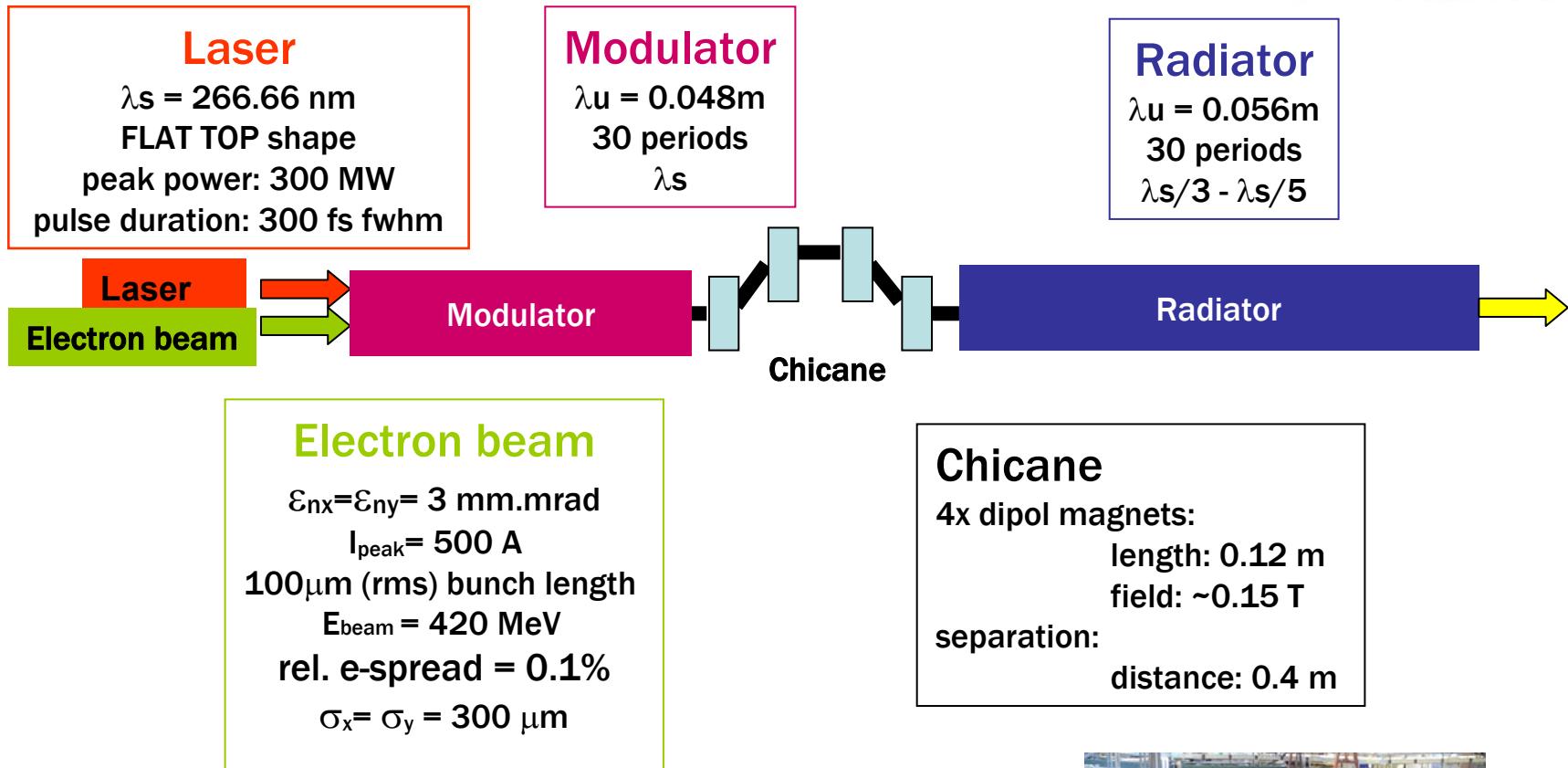
without flat wires

with flat wires



accuracy of field model

*J. Bahrdt, M. Scheer, G. Wuestefeld,  
 Mini-Workshop, Frascati, 2005*  
*J. Bahrdt et al. SRI, Daegu, Korea, 2006*  
*G. Wuestefeld, J. Bahrdt, EPAC 2006*  
*J. Bahrdt et al., PAC 2007, EPAC 2008*

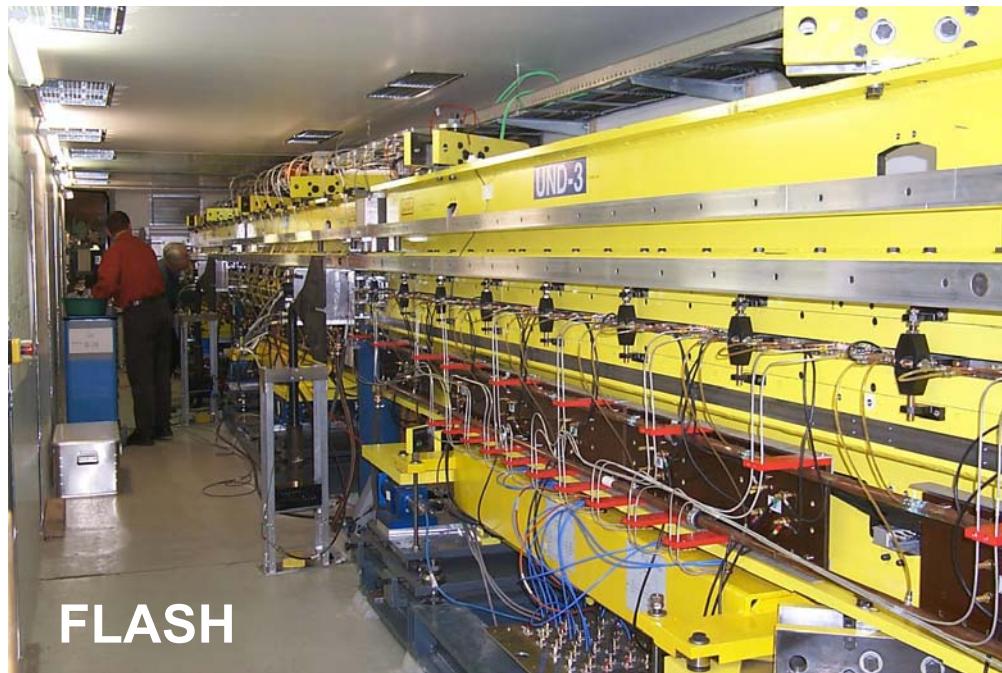
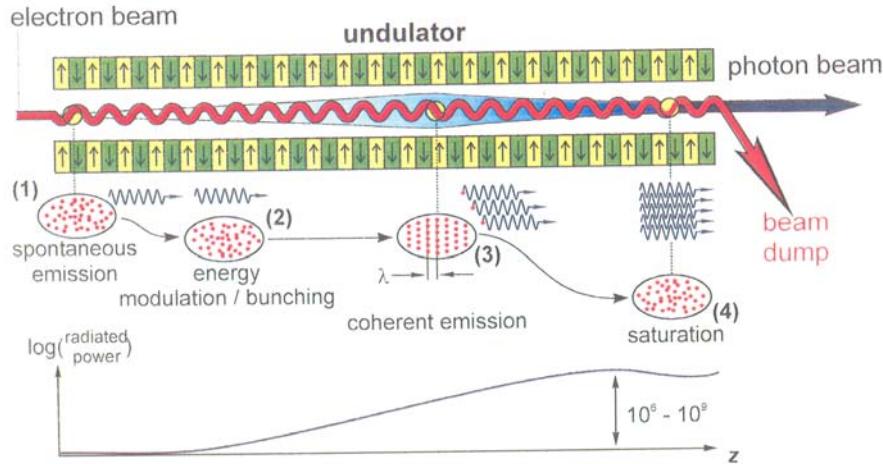


## Collaboration between MAX-lab and HZB

- test bed for studies of seeded FEL scheme
- test of specific diagnostic hardware for future light source  
e.g. Cherenkov, Powermeter glass fibers, THz detectors



# Long Undulators for SASE-FEL Application



saturation demonstrated:

VISA	800 nm
LEUTL	300 nm
FLASH	6.4 nm
SPRING8 VUV	60 nm
LCLS	0.15nm

projects:

XFEL	0.1 nm
SPRING8 X-ray	0.15 nm
(SLS X-Ray FEL)	0.1 nm)

Undulator:

$$\lambda_u = 27.3 \text{ mm}$$

$$\text{Gap} = 12 \text{ mm}$$

$$B_{\text{peak}} = 0.46 \text{ T}$$

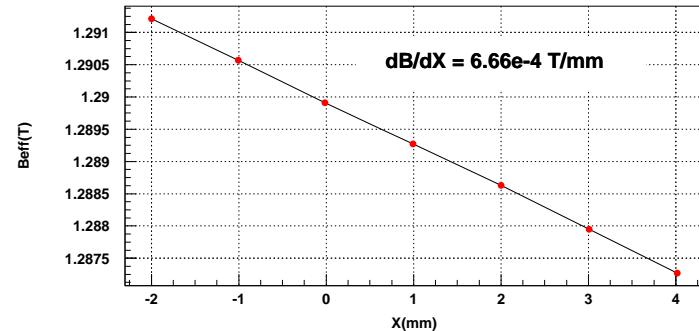
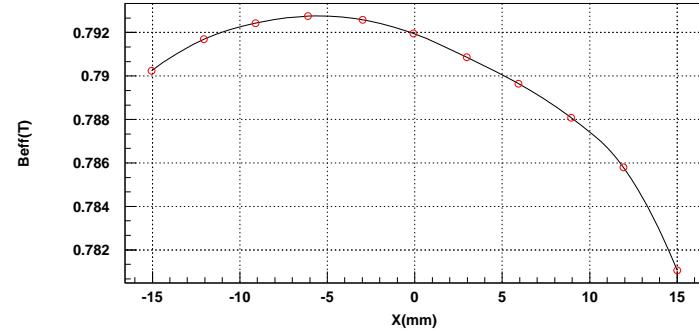
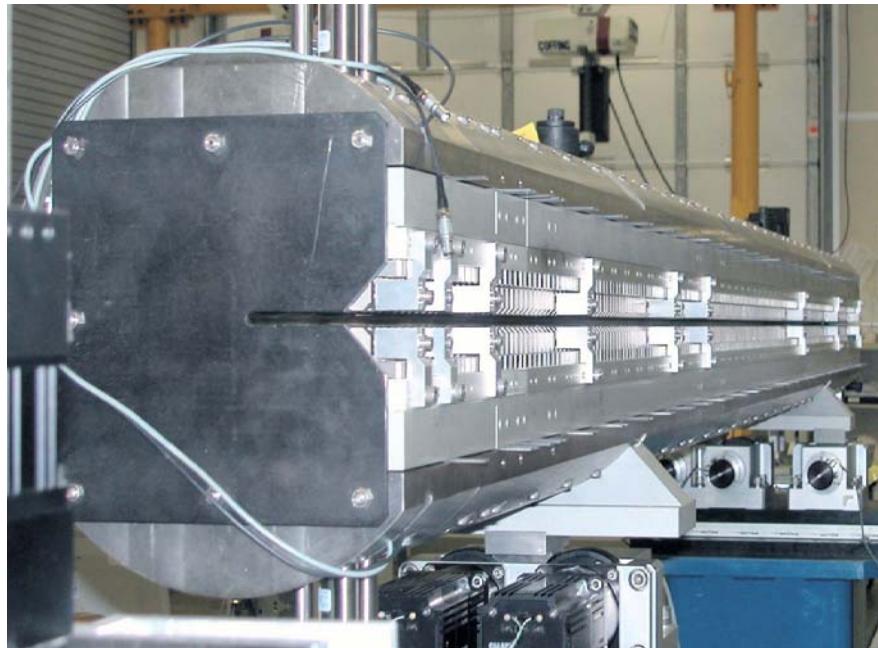
$$K = 1.17$$

$$L \approx 15 \text{ m}$$

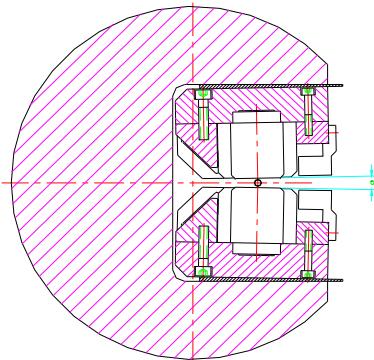
fixed gap  
undulators

Courtesy of  
J. Pflüger, XFEL

# Prototype Undulator for LCLS



S. Milton, WUS workshop,  
DESY, Hamburg, Germany, 2005



canting of poles  
for fine tuning  
of K-parameter

fine tuning via transverse  
displacement of undulator  
using cam shaft movers

fixed gap undulators

