

CERN ACCELERATOR SCHOOL / ACCELERATOR PHYSICS COURSE Baden, Austria, 12-24 September 2004

SYNCHROTRON LIGHT SOURCES

Albin F. Wrulich

- SYNCHROTRON LIGHT-SOURCES
- SYNCHROTRON-LIGHT SOURCES



SYNCHROTRON RADIATION FROM CRAB NEBULA



FED

PRINCIPLE OF ACCELERATOR BASED LIGHT PRODUCTION

Accelerated charged particles are emitting electromagnetic radiation. The dominant effect comes from transverse acceleration, as the deflection of a charged particle in a bending magnet of a circular accelerator:





Due to the emission the energy of the particle is changed !



Liénard: 1898

$$P = \frac{2}{3} \frac{e^2 \gamma^6}{4\pi\varepsilon_o c} \left[\dot{\vec{\beta}}^2 - \left(\vec{\beta} \times \dot{\vec{\beta}} \right) \right]$$

LONGITUDINAL:

Radiation field cannot separate itself from the Coulomb field





POWER emitted:

TRANSVERSE:

Radiation field quickly separates itself from the Coulomb field



ENERGY lost per turn: The POWER of the emitted radiation is increasing with the 4th power of the Lorentz factor!

$$P \sim \frac{\gamma^4}{\rho^2}$$

1

U

Since:
$$\gamma = 1 + \frac{E_k}{E_o} \approx \frac{E_k}{E_o} = \frac{eU}{E_o}$$



ELECTRONS, POSITRONS

$$\beta = \frac{v}{c} = \sqrt{1 - \frac{1}{\gamma^2}} \quad \Rightarrow$$



 E_{a} Rest energy

 E_{k} Kinetic energy

Accelerating voltage

eU MeV

SYNCHROTRON RADIATION FROM A BENDING MAGNET



1949 - On the classical radiation of accelerated electrons / J.S. Schwinger



WHAT LIGHT CHRACTERISTIC IS REQUESTED FOR EXPERIMENTS



LOTS OF OTHER REQUIREMENTS as stability, tunability, wide spectral range, higher photon energies (shorter wavelengths)

FED

HIGH BRILLIANCE

Users want a MANY PHOTONS on the sample!





For smaller sample size most of the photons are wasted. They generate an unwanted heating of the optical elements !





To overcome this problem: decrease source size and divergence, i.e. increase the brilliance









$$\sigma_{e} \gg \sigma_{\gamma} \rightarrow \Sigma_{x} \Sigma_{x} \approx \sigma_{x} \sigma_{x} = \varepsilon_{x}$$

$$\Rightarrow \text{ TRUE FOR MOST PRACTICAL CASES} \qquad x'$$

we assumed: $\sigma_{x} = \sqrt{\varepsilon_{x} \beta_{x}} \sigma_{x}' = \sqrt{\frac{\varepsilon_{x}}{\beta_{x}}} \sqrt{\frac{\varepsilon_{x}}{\sigma_{x}}} \sqrt{\frac{\varepsilon_{x}}{\sigma_{x}}}} \sqrt{\frac{\varepsilon_{x}}{\sigma_{x}}} \sqrt{\frac{\varepsilon_{x}}{\sigma_{x}}}} \sqrt{\frac{\varepsilon_{x}}{\sigma_{x}}} \sqrt{\frac{\varepsilon_{x}}{\sigma_{x}}}} \sqrt{\frac{\varepsilon_{x}}{$

$$\sigma_{\gamma} = \frac{\sqrt{\lambda L}}{4\pi} \quad \sigma_{\gamma}' = \sqrt{\frac{\lambda}{L}} \quad IF: \quad \sigma_{\gamma}\sigma_{\gamma}' = \frac{\lambda}{4\pi} = \sigma_{x}\sigma_{x}' = \varepsilon_{x}$$

Here

DIFFRACTION LIMIT



HIGH BRILLIANCE is needed for:

CRYSTALLOGRAPHY



N. Ban, S. Iwata, U. Baumnan et al.

Siccinat-Dehydrogenase

... to get the maximum flux into the sample acceptance phase space !

FEI

COHERENCE

is the property that enables a wave to produce visible diffraction and interference effects



A point-like monochromatic source always creates diffraction patterns



LATERAL COHERENCE - is increasing with brilliance



Extended monochromatic source

$$F_{c} = \left(\frac{\lambda}{2}\right)^{2} \frac{1}{\left(4\pi\right)^{2}} \frac{F}{S\Omega} \sim \left(\frac{\lambda}{2}\right)^{2} B$$

Full lateral coherence exists if
$$\rightarrow d \theta = 2\lambda$$

$$S = \left(\frac{d}{2}\right)\pi$$
$$\Omega = 4\pi \sin^2 \frac{\theta}{4} \approx \frac{\theta^2 \pi}{4}$$



LONGITUDINAL COHERENCE

- needs light emitted in a small bandwidth

UNDULATOR:
$$\frac{\Delta \lambda}{\lambda} = \frac{1}{2N}$$
 N ... number of magnet poles

→ long undulators can be used to increase the longitudinal coherence (suggested for some RECIRCULATOR projects)

Coherent length of a point-like source with $\Delta \lambda$ bandwidth

$$L_{c}=rac{\lambda}{arDelta\lambda/\lambda}$$

→ is the length over which 2 waves with $\Delta \lambda$ wavelength difference run 180 deg out of phase !

COHERENCE is needed for

PHASE COMTRAST IMAGING HOLOGRAPHY SPECKLE INTERFEROMETRY

EYE OF A FLY



MATERIAL SCIENCE BEAMLINE: Marco Stampanoni, Rafael Abela



M. Stampanoni et al



Contact: only absorption contrast

$\lambda = 0.08$ nm



R=100 mm: features of size $\zeta \sim 3 \mu m$ appear in enhanced *phase* contrast

"edge-enhanced contrast"



RELEVANCE OF COHERENCE for *CRYSTALLOGRAPHY*

→ Structure of a molecule (Ribosome)



Pictures: Jörg Harms, Arbeitsgruppe für Ribosomenstruktur, Max-Planck-Gesellschaft

Diffraction pattern

<u>Problem</u>: phase of the diffraction pattern is unknown !



RELEVANCE OF COHERENCE - DIFFRACTION PATTERN OF A DUCK

A (2-dimensional) DUCK

Creates this diffraction pattern (the colors encode the phase)







RELEVANCE OF COHERENCE - DIFFRACTION PATTERN OF A CAT

A CAT

... and its diffraction pattern







RELEVANCE OF COHERENCE - *RECONSTRUCTION*

Combine the AMPLITUDE of the diffraction pattern OF THE CAT with the PHASE of the diffraction pattern OF THE DUCK \rightarrow





The result: A DUCK !!

FED

POLARISATION

 Electric vector oscillates in one plane only or rotates as the wave propagates





POLARISATION is needed for:

MAGNETIC CIRCULAR DICHROISM TO FIND OUT THE ORIENTATION OF MOLECULES

FED

PEEM INVESTIGATION OF NANOPATTERNED MAGNETOSTRICTIVE SYSTEMS

IMAGING OF MAGNETIC DOMAINS



Magnetic ripple in as-grown cobalt-Terfenol sandwich film on prepatterned Si substrate.



G.Schütz,G.Schmahl, P. Fischer



POLARIZED LIGHT is generated by special undulators:



FED

SHORT PULSES

WHY SHORT PULSES ?

On the long time scale the fast motion is averaged out. On the short time scale the world stands still.

SHORT PULSES in the range of fs are needed in order to study the dynamics on the atomic and molecular level
 SHORT PULSES are mandatory to take snap shot before molecule flies apart (takes only 4-20 fs!)





STORAGE RING BASED LIGHT SOURCES:

ARE GOOD FOR \rightarrow

- diffraction limited light in the VUV range (~ 100 eV)
- high brilliance in the soft- and hard X-ray regime and related Lateral coherence
- any type of polarized light (generated by special insertion devices

HAVE MADE ENORMEOUS PROGRESS \rightarrow

- energy, position and intensity stability
- Achievement of higher photon energies (also from medium energy electrons)

DO NOT COVER THE NEEDS FOR \rightarrow

- high temporal coherence
 - short pulses



HOW ARE THESE LIGHT FEATURES ACCOMPLISHED BY ACCELERATOR CHARACTERISTICS



LIGHT

MAGNET STRUCTURE



PARTICULARITIES OF A LIGHT SOURCE LATTICE

How to get the best performance of the light, i.e. maximum Brilliance

$$B = \frac{F}{(4\pi)^2 \Sigma_x \Sigma_x' \Sigma_y \Sigma_y'} = \frac{F}{(4\pi)^2 \varepsilon_x \varepsilon_y} = \frac{F}{(4\pi)^2 \varepsilon_x \varepsilon_y}$$

The Flux F is proportional to the stored beam current κ is the emittance coupling.

In order to get the maximum Brilliance, the emittance must be minimized!

The emittance of an electron storage ring is defined as the phase space area that contains one standard deviation of the gaussian particle distribution



The emittance of an electron storage ring is given by the equilibrium between quantum fluctuation and radiation damping



IN AN ELECTRON STORAGE RING THE EMITTANCE IS A CHARACTERISTIC QUANTITY OF THE MAGNET LATTICE

In order to minimize it we have to understand how it is generated!

BASICS 1:

BENDING MAGNET



Particles with different energies are moving on different orbits in a bending magnet → DISPERSION orbit! Basic equation:





BASICS 2:

If a particle is not on its closed orbit, it performs betatron oscillations around this closed orbit:

$$x(s) = A\cos[\phi(s) - \phi_o]$$

$$x'(s) = -A\frac{\alpha}{\beta}\cos[\phi - \phi_o] - A\frac{1}{\beta}\sin[\phi - \phi_o]$$
CONSTANT OF
THE MOTION
$$A^2 = \varepsilon\beta = x^2 + (x\alpha + x'\beta)^2 \quad \text{at position 's'}$$
OR
$$\varepsilon = x^2\gamma + 2xx'\alpha + x'^2\beta \quad \text{everywhere in the ring}$$

$$\gamma = \frac{1 + \alpha^2}{\beta}$$

An electron emitting a radiation quantum in the bending magnet loses energy and finds itself afterwards not on its closed orbit anymore



The particle starts to oscillate around the new closed orbit with a betatron amplitude corresponding to the difference in closed orbit before and after the energy jump.

Substitution of these changes into the expression for the constant of motion leads to: $\sqrt{2}$

$$A^{2} = \left(x - D\frac{u}{E_{o}}\right)^{2} + \left[\left(x' - D'\frac{u}{E_{o}}\right)\alpha + \left(x' - D'\frac{u}{E_{o}}\right)\beta\right]^{2}$$

$$A^{2} = A_{o}^{2} - 2\frac{u}{E_{o}}\left[xD + (x\alpha + x'\beta)(D\alpha + D'\beta)\right] + \left(\frac{\Delta u}{E_{o}}\right)^{2}\left[D^{2} + (D\alpha + D'\beta)^{2}\right]$$



Averaging over many turns makes the mid term vanishing and we get:

$$\Delta(A^{2}) = A^{2} - A_{o}^{2} = \frac{u^{2}}{E_{o}^{2}} \left[D_{x}^{2} + (D_{x}\alpha_{x} + D_{x}^{\prime}\beta_{x})^{2} \right]$$

$$H(s)$$

COURANT SNYDER INVARIANT

In order to get the beam size, respectively the emittance one has to perform:

- → Statistical averaging over all emissions in one turn
- \rightarrow Averaging over all betatron phases of the particle motion
- \rightarrow Equilibration to the radiation damping

$$\Rightarrow \quad \varepsilon_x = C_q \frac{\gamma^2}{J_x} \frac{\left\langle H / \rho^3 \right\rangle}{\left\langle 1 / \rho^2 \right\rangle}$$

For constant radius ρ we get:





INSERT: RADIATION DAMPING



Substituting in the expression for the constant of motion and averaging over all betatron phases leads to (neglecting quadratic terms) \rightarrow

$$\Delta A^2 = A^2 - A_o^2 = -A^2 \frac{u}{E_o} \rightarrow \frac{\Delta A}{A} = -\frac{1}{2} \frac{u}{E_o}$$

Summation over all energy emissions in one turn:

$$\sum u_i = U_T \quad \rightarrow \quad \left\langle \frac{\Delta A}{A} \right\rangle = -\frac{1}{2} \frac{U_T}{E_o} \quad \rightarrow \quad \frac{1}{A} \frac{dA}{dt} = \frac{1}{T_o} \left\langle \frac{\Delta A}{A} \right\rangle = \frac{1}{\tau_x} = -\frac{1}{2} \frac{U_T}{E_o T_o}$$



INSERT: EQUILIBRIUM

Averaging over all emission processes of one turn leads to \rightarrow

$$\left\langle \frac{dA^2}{dt} \right\rangle = \frac{\left\langle \dot{N}_{ph} \left\langle u^2 \right\rangle H \right\rangle}{E_o^2}$$

Averaging over all betatron phases for the radiation damping \rightarrow

$$\frac{1}{A}\frac{dA}{dt} = \frac{1}{T_o}\left\langle\frac{\Delta A}{A}\right\rangle = \frac{1}{\tau_x}$$

Equilibrium between quantum fluctuation and radiation damping:

$$\left\langle \frac{dA^2}{dt} \right\rangle = 2 \left\langle A \frac{dA}{dt} \right\rangle = 2 \left\langle A^2 \frac{1}{A} \frac{dA}{dt} \right\rangle = \frac{2}{\tau_x} \left\langle A^2 \right\rangle$$

$$\sigma_x^2 = \frac{\langle A^2 \rangle}{2} = \frac{1}{4} \tau_x \frac{\langle \dot{N}_{ph} \langle u^2 \rangle H \rangle}{E_o^2} \implies \varepsilon_x = C_q \frac{\gamma^2}{J_x} \frac{\langle H / \rho^3 \rangle}{\langle I / \rho^2 \rangle}$$

To get the minimum emittance the integral over the Courant Snyder invariant H over the length of the bending magnets has to be minimized:

$$\langle H(s) \rangle_{BEND} = \frac{1}{L} \int_{0}^{L} H(s) ds \rightarrow min.$$

SINGLE MAGNET OPTIMIZATION:



A rectangular magnet corresponds to a drift in the horizontal plane and the optical functions α , β , γ inside have a simple relations to the initial values at the entrance of the magnet:

In a bending magnet the dispersion is developing as:

$$D(s) = \rho(1 - \cos\frac{s}{\rho})$$
$$D'(s) = \sin\frac{s}{\rho}$$

$$\beta(s) = \beta_o - 2\alpha_o s + \gamma_o s^2$$

$$\alpha(s) = \alpha_o - \gamma_o s$$

$$\gamma(s) = \gamma_o$$

FED

Substitution of these relations into the expression for the Courant Snyder Invariant (for $D_o=0$ and $D_o'=0$) \rightarrow

$$D_x^2(s) + \left[D_x(s)\alpha_x(s) + D_x'(s)\beta_x(s)\right]^2$$

We get a functional dependence on s and coefficients that include the initial parameters β_o , α_o and the bending radius ρ .

After performing the integration we get:

$$\langle H(s) \rangle = \frac{L^2}{\rho^2} \left[\frac{1}{3} \beta_o - \frac{1}{4} \alpha_o L + \frac{1}{20} \gamma_o L^2 \right]$$

To find the minimum we have to solve:

$$\frac{\partial H}{\partial \beta_o} = 0 \qquad \Rightarrow \text{ leads to:} \qquad \begin{array}{l} \beta_o = 2L\sqrt{\frac{3}{5}} \\ \alpha_o = \sqrt{15} \end{array}$$

Substituting this values in the expression for the emittance we find for the minimum \rightarrow







We can now construct a simple achromat structure \rightarrow





➔ Light Sources are built up by a large number of identical achromat structures connected by long (empty) dispersion free sections !

The dispersion has to be matched to zero in the straight section in order to get a small beam size and correspondingly high brilliance !

USE of the long straight sections (~ 2 - 12 m):

For the implementation of insertion devices – **WIGGLERS** and **UNDULATORS** for enhanced flux and brilliance of the light \rightarrow



EXAMPLE 1 SB / IPEP / LPAP - Laboratory for Particle Accelerator Physics

FED

PROBLEM with the DBA

In the center of the achromat we have a symmetry point, i.e. \rightarrow

$$\begin{aligned} u &= 0 \\ D'_o &= 0 \end{aligned}$$

. **^**

Beta function and dispersion must be matched to zero slope in the center by the quadrupole:





To reach the theoretical minimum for a DBA lattice at least 2 quadrupoles are needed which are seperated by a certain distance:





EXAMPLE: **DBA**

OPTICAL FUNCTIONS

With ONE quadrupole in the achromat



MAGNET STRUCTURE

With >TWO quadrupoles to approach the theoretical minimum







Horizontal damping partition number !

$$\frac{1}{\tau_x} = -\frac{1}{2J_x} \frac{U_T}{E_o T_o}$$

The sum of all 3 damping partition numbers is constant, i.e. damping can be transferred from the longitudinal direction to the horizontal direction for a proper chosen magnet structure.

•/

$$J_x + J_y + J_s = 4$$

If focusing and bending are seperated in amgnet structure – **separate function magnet structure** – we have:

With a combined function magnet structure we can have $J_x > 1$ and therefore further reduce the emittance.

$$J_x = 1, J_y = 1, J_s = 2$$





EXAMPLE: **ELETTRA**





 \rightarrow adds also vertical focusing and keeps β_v low !





CENTER MAGNET OPTIMIZATION (starting from the center):



FED

PROBLEM (1) with the TBA

We have to match now dispersion and beta function from the exit of the optimized outer bending magnet to the center of the optimized inner bending magnet

THIS IS NOT POSSIBLE !! (under no circumstances)

The theoretical minimum of the TBA structure can't be reached but just approached !

But there is nevertheless a big gain due to the reduction of the bending angle \rightarrow

$$\varepsilon_{min} = \frac{C_q \gamma^2}{J_x} K \phi_{BEND}^3$$
$$\phi_{TBA} = \frac{2}{3} \phi_{DBA}$$

NOTE: if a dispersion in the straight section is permitted the emittance can be further reduced!



PROBLEM (2) with the TBA

- $\frac{\Delta Q}{\Delta p/p_o} = \xi = \frac{1}{4\pi} \oint_C \beta(s) K(s) ds$
- Has to do with the <u>chromaticity correction</u>:

Which is done by introducing sextupoles in the magnet structure.

$$\Delta x' = m(x^2 - y^2)$$

$$\Delta y' = -2mxy$$

$$m = \frac{1}{2} \frac{B'' L}{B_o \rho}$$

$$x = x_\beta + \delta D_x$$

$$\delta = \frac{\Delta p}{p_o}$$

$$y = y_\beta$$

$$x_\beta \dots \text{ betatron oscillations}$$

$$\Delta x' = m \left[(x_\beta + \delta D_x)^2 - y_\beta^2 \right] = m(x_\beta^2 - y_\beta^2) + \frac{(\delta 2mD_x)x_\beta}{(\delta 2mD_x)x_\beta} + m(\delta D_x)^2$$

$$\Delta y' = -2m(x_{\beta} + \delta D_x)y_{\beta} = -2mx_{\beta} - \frac{(\delta 2mD_x)y_{\beta}}{(\delta 2mD_x)y_{\beta}}$$

$$\xi_x = \frac{1}{4\pi} \left[\sum_{i,j} \beta_{xi} (kl)_i + 2(ml)_j D_{xj} \beta_{xj} \right] \rightarrow 0$$

Sextupoles are nonlinear elements and reduce the dynamic aperture. In order to keep their strengths low they have to be placed at positions with large dispersion (and large decoupling of the beta function).

Chromatic corrections are more difficult in TBA lattices !

COMPARISON OF LATTICES FOR LIGHT SOURCES AND HEP COLLIDERS

HEP COLLIDER



 \rightarrow large circumferences



HEP colliders are composed by long regular FODO cells in the arcs and a few low beta insertions:

Large circumferences are necessary to reach the highest possible energies

$$\frac{1}{\rho} = \frac{e}{p}B$$

 \boldsymbol{B}_{max}

nc: 1.6 T

sc: ~ 9 T

COMPARISON OF LATTICES FOR LIGHT SOURCES AND HEP COLLIDERS

LIGHT SOURCE

Light Sources are built up by a large number of identical achromat structures.

Large circumferences are wanted to increase the BRILLIANCE and to provide many straights for IDs !





 $B = \frac{F}{(4\pi)^2 \kappa \varepsilon_x^2}$ $\varepsilon_{min} = \frac{C_q \gamma^2}{J_x} K \phi_{BEND}^3$



WHAT ELSE IS IMPORTANT FOR A LIGHT SOURCE

SUPPRESSION OF ENERGY WIDENING EFFECTS

Shift of the radiation harmonics from an undulator \rightarrow intensity fluctuations, broadning of the lines

INTENSITY STABILITY

Change in background conditions and thermal load on beamline optics and machine components (\rightarrow position stability!)

POSITION STABILITY

Dilution of the emittance \rightarrow reduced brilliance, intensity fluctuation

ENERGY STABILITY

Shift of the radiation harmonics from an undulator \rightarrow intensity fluctuation

TUNABILITY

HIGH PHOTON ENERGIES

SUPPRESSION OF ENERGY WIDENING EFFECTS

- MULTIBUNCH FEEDBACK SYSTEMS
- PASSIVE SUPERCONDUCTING HIGHER HARMONIC CAVITY

3HC COLLABORATION CEA (Saclay), CERN, Sincrotrone Trieste, PSI





Phase variation along the bunch train (for a partially filled ring) causes a split in frequency for the individual bunches and therefore a suppression of longitudinal mulit-bunch instabilities





INTENSITY STABILITY





ENERGY STABILITY

CORRECTING THE AVERAGE HORIZONTAL ORBIT BY ADJUSTING THE RF FREQUENCY AND THUS ADJUSTING THE ELECTRON ENERGY

HIGH INTENSITY STABILITY OF MONOCHROMATOR OUTPUT

$$\lambda = \frac{\lambda_o}{2\gamma^2} \left(1 + \frac{K^2}{2} \right)$$





FED

DAY / NIGHT TEMPERATURE VARIATIONS

CIRCUMFERENCE OF THE SLS RING CHANGES WITH OUTSIDE TEMPERATURE

RF FREQUENCY IS ADJUSTED TO COMPENSATE FOR THESE CHANGES



FED

TUNABILITY

 \rightarrow To adjust the photon energy to the needs of the experiment !

EXAMPLES:

ABSORPTION TOMOGRAPHY SLS-MATERIAL SCIENCE BEAMLINE Bone sample damage



uni | **eth** | zürich Institute for Biomedical Engineering



Philipp Thurner, EMPA and IBT, Marco Stampanoni, SLS

PHASE CONTRAST TOMOGRAPHY SLS-MATERIAL SCIENCE BEAMLINE 3-dimensional reconstruction of the vesicular distribution in mouse brains"

1 mm³ Resolution ~ 1 μm







■ ALSO IMPORTANT \rightarrow

TO REACH HIGH PHOTON ENERGIES WITH A MEDIUM ENERGY MACHINE



SYNCHROTRON RADIATION CENTRES AROUND THE WORLD





EUROPE → LORD OF THE RINGS





OUTLOOK NEW GENERATION OF LIGHT SOURCES

Performance of 3rd Generation Light Sources:



Storage ring based light sources are for short wavelengths (high photon energies) far away from the theoretical limits →

NEW GENERATION LIGHT SOURCE:

SASE FREE ELECTRON LASERS

- Unbeatable peak and average BRILLIANCE (10³⁰ - 10³³)
- Short PULSES (1 ps 50 fs)
- Small BANDWIDTH













REQUIRES A SMALL ELECTRON BEAM !





PHOTON BEAM SIZE







TESLA X - FEL at DESY





USERS DREAMS WILL THEN BECOME REALITY \rightarrow

 SINGLE SHOT imaging of single biomolecular complexes

NEEDS MANY PHOTONS ON THE SAMPLE !

LYSOZYME MOLEKUEL



Light induced structural changes during photocycle



TIME RESOLVED studies of structural processes during chemical and biological reactions

NEEDS VERY SHORT PULSES !





CONCLUSION

- Storage ring based Light Sources need a highly optimized lattice to reach the maximum brilliance (coherence)
- Nonlinear compensation must already be optimized with the linear lattice design
- Large circumferences are wanted to reduce the emittance, i.e. to increase the brilliance and to provide space for many insertion devices
- Not all user requirements can be met with storage ring based light sources (longitudinal coherence, short pulses)
- A new generation of light sources Free Electron Laser is needed to meet these requirements
- Stability of intensity, energy and position are crucial issues





THE END